

## Lesson 17 - Two Groups - Two Means - Theoretical

Two Means (One categorical var and one Quantitative variable)

Parameter  $\mu_1 - \mu_2$

Statistic  $\bar{x}_1 - \bar{x}_2$

Validity Conditions Both Groups Symmetrical  
OR

$\geq 20$  observations per group  
and not strongly skewed

Hypotheses

$$H_0: \mu_1 - \mu_2 =$$

$$H_a: \mu_1 - \mu_2 > \\ \neq \\ <$$

Standardized  
Statistic

$$t = \frac{\bar{x}_1 - \bar{x}_2 - (\text{null})}{\sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}}$$

Null = 0

P-value

$$H_a: < \quad pt(t, n-2)$$

$$> \quad 1 - pt(t, n-2)$$

$$\neq \quad 2 * (1 - pt(\text{abs}(t), n-2))$$

CI = Statistic  $\pm$  Multiplier \* SE

$$(\bar{x}_1 - \bar{x}_2) \pm \left[ qt\left(1 - \frac{\alpha}{2}, n-2\right) \right] * \sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}$$

Impacts SOE (p-value)

$\uparrow$  Sample size  $\downarrow$

$\uparrow$  Variability of sample (s)  $\uparrow$

$\uparrow$  Difference btwn Stat and null  $\downarrow$

Impacts Confidence Interval

$\uparrow$  Sample size  $\downarrow$

$\uparrow$  Significance level ( $\alpha$ )  $\downarrow$

$\uparrow$  Variability (s) of sample  $\uparrow$