

5)

	$Y=0$	$Y=1$	
$X=0$	8/24	4/24	12/24
$X=1$	6/24	6/24	12/24
	14/24	10/24	

$$13. P(X=1 | Y=1) = 6/24$$

$$14. P(Y=0) = 58\%$$

$$P(Y=1) = 42\%$$

$$15. E(Y) = 0 \cdot .58 + 1 \cdot .42 = .42$$

$$16. \text{Var}(Y) = E(Y^2) - E(Y)^2$$

$$= (0^2 \cdot .58 + 1^2 \cdot .42) - (.42^2)$$

$$= .42 - .1764$$

$$\text{var}(Y) = .2436$$

$$17. \text{sd}(Y) = \sqrt{\text{var}(Y)}$$

$$\text{sd}(X) = \sqrt{.2436}$$

$$18. \text{corr}(Y, X) = \frac{\text{cov}(Y, X)}{\text{sd}(Y) \cdot \text{sd}(X)}$$

$$E(X) = 0 \cdot .5 + 1 \cdot .5 = .5$$

$$E(YX) = 0 \cdot 18/24 + 1 \cdot 6/24 = 6/24 = .25$$

$$\text{cov}(YX) = .25 - (.42 \cdot .5)$$

$$= .25 - .21 = .04$$

$$\text{sd}(X) = \sqrt{\text{var}(X)}$$

$$\text{var}(X) = E(X^2) - E(X)^2$$

$$E(X^2) = 0^2 \cdot .5 + 1^2 \cdot .5 = .5$$

$$E(X)^2 = (0 \cdot .5 + 1 \cdot .5)^2 = .25$$

$$\text{Var}(x) = .5 \cdot .25 = .25$$

$$\text{sd}(x) = \sqrt{.25}$$

$$\text{Corr}(Y, X) = \frac{.04}{\sqrt{2436} \cdot \sqrt{.25}}$$

19 No, since  $\text{Corr}(Y, X) \neq 0$   $X$  and  $Y$  are on some level dependent.

$$20. E(Y|X=1) = 0 \cdot \frac{1}{24} + 1 \cdot \frac{1}{24} = .29$$