Question 1

1. $1 + 2 + 3 + \dots + n = \frac{n(n+1)}{2} = O(n^2)$

The while loop will run n times. Inserting would first cost 1, the second time 2 since it has to shift 1 element and insert. The third time would cost 3 since it has to shift 2 elements and insert. This would go on until the while loop ends. Therefore the total cost would be $1 + 2 + 3 \dots + n = \frac{n(n+1)}{2} = O(n^2)$

2. The while loop would run n times. Appending would add an element to the list until it has to resize the list. There fore the total cost would be $1 + 2 + 4 + 8 \dots n = 2n - 1 = O(n)$.

Question 3

worst-case

The runtime would be $O(n)$ since we would have to account for resizing due to the append method. The total cost would be $1 + 2 + 4 + 8 \dots n = (2n - 1) = O(n$

Question 4

a) The worst case runtime would be $O(n^2)$ since the worst case is if the input is a list containing all of the same elements, the while loop would run the length of the list and will have to resize each time an occurance of the value is removed.

The total cost would be $n+(n-1)+(n-2)+\ldots+1 = \frac{n(n+1)}{2}$

$= O(n^2)$