Scheme Notes 03

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Recursion vs. Tail-recursion

```
a^b = \left\{ \begin{array}{ll} 1 & \text{if } b = 0 \\ a(a^{b-1}) & \text{otherwise} \end{array} \right. (define pow-rec (lambda (a b) (if (zero? b) 1 & (* \text{ a (pow-rec a (- b 1)) ))))
```

Recursion vs. Tail-recursion

```
a^b = \begin{cases} 1 & \text{if } b = 0 \\ a(a^{b-1}) & \text{otherwise} \end{cases}
(define pow-rec
  (lambda (a b)
     (if (zero? b)
          (* a (pow-rec a (- b 1)) ))))
(define pow-iter
  (lambda (a b)
     (define loop
        (lambda (b product)
          (if (zero? b)
               product
                (loop (- b 1) (* a product)) )))
     (loop b 1)))
```

Named let

```
(define pow-iter
  (lambda (a b)
    (define loop
      (lambda (b product)
        (if (zero? b)
            product
            (loop (- b 1) (* a product)))))
    (loop b 1)))
(define pow-iter-2
  (lambda (a b)
    (let loop ((b b) (product 1))
      (if (zero? b)
          product
          (loop (- b 1) (* a product))))))
```

Fast recursion

$$a^b = \left\{ egin{array}{ll} 1 & ext{if } b=0 \ (a^{b/2})^2 & ext{if } b ext{ is even} \ a(a^{b-1}) & ext{otherwise} \end{array}
ight.$$

Lists

A **list** is either:

- 1. the empty list, or
- 2. an item and a list

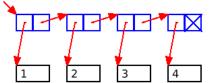
Lists

A list is either:

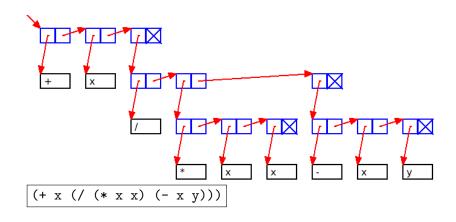
- 1. the **empty list**, or
- 2. an item and a list

Scheme uses:

- 1. the null pointer for the empty list, and
- 2. a cons cell of two pointers for a non-empty list.
- 3. The first pointer in a cons cell is called car.
- 4. The second pointer in a cons cell is called **cdr**.
- 5. The empty list has predicate empty?.



Scheme Programs are Lists



Building Lists in Scheme:

- 1. The empty list in Scheme: ()
- 2. Create a list from 3 and the empty list:

```
(cons 3 '()) \Rightarrow (3)
```

3. Create the list (4 7 2):

(cons 4 (cons 7 (cons 2 '())))
$$\Rightarrow$$
 (4 7 2)

4. Shorthand for long lists: (list 4 7 2) \Rightarrow (4 7 2)

Building Lists in Scheme:

- 1. The empty list in Scheme: ()
- 2. Create a list from 3 and the empty list:

```
(\cos 3 '()) \Rightarrow (3)
```

3. Create the list (4 7 2):

$$(\cos 4 (\cos 7 (\cos 2 ()))) \Rightarrow (4 7 2)$$

- 4. Shorthand for long lists: (list 4 7 2) \Rightarrow (4 7 2)
- 5. Using quote: $(4 7 2) \Rightarrow (4 7 2)$

$$(+ 4 7 2) \Rightarrow (+ 4 7 2)$$

$$(a b c) \Rightarrow (a b c)$$

(a b c)
$$\Rightarrow$$
 error

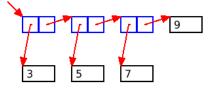
$$(+ 4 7 2) \Rightarrow 13$$

'(list (+ 2 2) 7 2)
$$\Rightarrow$$
 (list (+ 2 2) 7 2)

(list (+ 2 2) 7 2)
$$\Rightarrow$$
 (4 7 2)

An improper list results in a dot:

- $(cons 4 8) \Rightarrow (4 . 8)$
- (cons 3 (cons 5 (cons 7 9))) \Rightarrow (3 5 7 . 9)
- Run boxarrow.rkt for pictures.



length

```
(length '(1 2 3)) => 3
(length '()) => 0
(length '(a (b c d) e (f g))) => 4
```

length

(length '(1 2 3))

nth

nth

```
(nth '(a b c d) 0)
(nth '(a b c d) 3)
                          => d
(nth '(a b c d) 8)
                          => (error 'nth "Not defined")
(define (nth 1st n)
  (cond ((empty? lst) (error 'nth "Not defined"))
        ((= n 0) (car lst))
        (else (nth (cdr lst) (- n 1)))))
```

last

last

scale-list

```
(scale-list '(1 2 3) 2) \Rightarrow (2 4 6)
(scale-list '(1 2 3) 3) \Rightarrow (3 6 9)
```

scale-list

```
(scale-list '(1 2 3) 2) \Rightarrow (2 4 6)
(scale-list '(1 2 3) 3) => (3 6 9)
(define (scale-list 1st n)
  (cond ((empty? lst) '())
        (else
             (cons (* n (car lst))
                    (scale-list (cdr lst) n))))
```

increment-list

```
(increment-list '(1 3 99)) => (2 4 100)
(increment-list '(8 3 0 1)) => (9 4 1 2)
```

increment-list

```
(increment-list '(1 3 99)) => (2 4 100)
(increment-list '(8 3 0 1)) => (9 4 1 2)
(define (increment-list lst)
 (cond ((empty? lst) '())
        (else
            (cons (+ 1 (car lst))
                  (increment-list (cdr lst))))))
```

map

map

```
(map (lambda (x) (* 2 x))
     '(1 2 3))
                             => (2 4 6)
(map (lambda (x) (list x x))
     (123)
                             => ((1 1) (2 2) (3 3))
(define (map op lst)
  (cond ((empty? lst) '())
        (else
            (cons (op (car lst))
                  (map (cdr lst) op))))
```

scale-list using map

scale-list using map

```
(define (scale-list lst n)
  (map (lambda (x) (* n x)) lst))
```

increment-list using map

increment-list using map

```
(define (increment-list lst)
  (map (lambda (x) (+ x 1)) lst))
```

append

```
(append '(1 2 3) '(a b c)) => (1 2 3 a b c))
```

append

remove

(remove 3 '(1 2 3 4 5 4 3 2 1)) => (1 2 4 5 4 2 1)

remove