

yz709-compiler-sup3

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Question 2 (CPS and defunctionalisation exercise sheet)

Problem 1

Again by hand, eliminate tail recursion from `fold_left`. Does your source-to-source transformation change the type of the function? If so, can you rewrite your code so that the type does not change?

```
(* tail-recursive version: no deferred operation *)
(* fold_left : ('a -> 'b -> 'a) -> 'a -> 'b list -> 'a *)
let rec fold_left f accu l =
  match l with
  | [] -> accu
  | a::l -> fold_left f (f accu a) l

(* sum up a list *)
let sum1 = fold_left (+) 0 [1;2;3;4;5;6;7;8;9;10] (* 55 *)
let product1 = fold_left (fun x y -> x * y) 1 [1;2;3;4] (* 24 *)
let concat1 = fold_left (fun x y -> y :: x) [9;8;7;6] [1;2;3;4]
(* [4; 3; 2; 1; 9; 8; 7; 6] *)
```

- No it has the same type `val fold_left_iterative : ('a -> 'b -> 'a) -> 'a -> 'b list -> 'a = <fun>`

```
(* eliminate tail recursion *)
let fold_left_iterative f accu l =
```

```

let accu_ref = ref accu in
let r = ref l in
let _ = while (!r) != [] do
  match !r with
  | [] -> r := [] (* this case will never been seen *)
  | x::xs -> r := xs; accu_ref := (f (!accu_ref) x);
done
in !accu_ref

let sum2 = fold_left_iterative (+) 0 [1;2;3;4;5;6;7;8;9;10] (* 55 *)
let product2 = fold_left_iterative (fun x y -> x * y) 1 [1;2;3;4] (* 24 *)
let concat2 = fold_left_iterative (fun x y -> y :: x) [9;8;7;6] [1;2;3;4]
(* [4; 3; 2; 1; 9; 8; 7; 6] *)

```



Comments:

Problem 2

Apply by hand the CPS transformation to the gcd code. Explain your results.

```

let rec gcd(m, n) =
  if m = n
  then m
  else if m < n
    then gcd(m, n - m)
    else gcd(m - n, n)

let gcd_test_1 = List.map gcd [(24, 638); (17, 289); (31, 1889)]
(* int list = [2; 17; 1] *)

```

- We can eliminate tail recursion in the `gcd` function easily, because at each stage, we only recursively call the function `gcd` once

```

(* eliminate tail recursion *)
let gcd_iter(m, n) =
  let m_ref = ref m in
  let n_ref = ref n in
  let _ = while (!m_ref) != (!n_ref) do
    if (!m_ref) < (!n_ref) then n_ref := (!n_ref) - (!m_ref)
    else m_ref := (!m_ref) - (!n_ref)
  done
  in !m_ref

let gcd_test_3 = List.map gcd_iter [(24, 638); (17, 289); (31, 1889)]
(* val gcd_test_3 : int list = [2; 17; 1] *)

```

- For a cps transformation, `cnt` is the continuation/function, in `gcd_cps_util(m, n, cnt)`, it expects the result of `gcd(m, n)` as its argument, similarly, `fun a -> cnt a` is the continuation waiting for `gcd(m, n - m)`, and `fun b -> cnt b` is the continuation waiting for `gcd(m - n, n)`.
- Since we output `m` when arrived at the base case `m = n`, so the continuation `cnt` is the identity function `fun x -> x`.

```
let rec gcd_cps_util(m, n, cnt) =
  if m = n then cnt m
  else if m < n
    then gcd_cps_util(m, n - m, fun a -> cnt a)
    else gcd_cps_util(m - n, n, fun b -> cnt b)
let rec gcd_cps(m, n) = gcd_cps_util(m, n, fun x -> x)

let gcd_test_2 = List.map gcd_cps [(24, 638); (17, 289); (31, 1889)]
(* int list = [2; 17; 1] *)
```



Comments:

Problem 3

Environments are treated as functions in `interp_0.ml`. Can you transform these definitions, starting with defunctionalisation, and arrive at a list-based implementation of environments?

```
(* update : ('a -> 'b) * ('a * 'b) -> 'a -> 'b *)
let update(env, (x, v)) = fun y -> if x = y then v else env y

(* mupdate : ('a -> 'b) * ('a * 'b) list -> 'a -> 'b *)
let rec mupdate(env, bl) =
  match bl with
  | [] -> env
  | (x, v) :: rest -> mupdate(update(env, (x, v)), rest)

(* env_empty : string -> 'a *)
let env_empty = fun y -> failwith (y ^ " is not defined!\n")

(* env_init : (string * 'a) list -> string -> 'a *)
let env_init bl = mupdate(env_empty, bl)
```

- The function `mupdate` is a recursive function, so we have to use CPS and DFC to turn it into a function carrying an explicit stack.

```

(* CPS of recursive function `mupdate` *)
(* val mupdate_cps_util :
  ('a -> 'b) * ('a * 'b) list * (('a -> 'b) -> 'c) -> 'c = <fun>
val mupdate_cps : ('a -> 'b) * ('a * 'b) list -> 'a -> 'b = <fun> *)
let rec mupdate_cps_util(env, bl, cnt) =
  match bl with
  | [] -> cnt env
  | (x, v) :: rest -> mupdate_cps_util(update(env, (x, v)), [],
    fun a -> mupdate_cps_util(a, rest, fun b -> cnt b))
let rec mupdate_cps(env, bl) = mupdate_cps_util(env, bl, fun x -> x)

(* Defunctionalisation:
  1. a list of continuations fun x -> e
  fun a -> mupdate_cps_util(a, rest, fun b -> cnt b)
  fun b -> cnt b
  fun x -> x
  2. get a set of free variables fv(e) - {x}
  3. define a new data structure for the continuations
  with types composed of free variables
  4. an apply function, each fun type maps to a dfc(e)
*)

type ('a, 'b) funs =
|CNT_MUPDATEA of ('a * 'b) list * ('a, 'b) funs
|CNT_MUPDATEB of ('a, 'b) funs
|CNT_ID

(* val apply_funs : (string, 'a) funs * string -> 'a = <fun> *)
let rec apply_funs = function
|(CNT_MUPDATEA(rest, cnt), a) -> mupdate_cps_dfc(a, rest, CNT_MUPDATEB(cnt))
|(CNT_MUPDATEB(cnt), b) -> apply_funs(cnt, b)
|(CNT_ID, x) -> x

and mupdate_cps_dfc(env, bl, cnt) =
  match bl with
  | [] -> apply_funs(cnt, env)
  | (x, v) :: rest -> mupdate_cps_dfc(
    update(env, (x, v)), [], CNT_MUPDATEA(rest, cnt))

(* Turn to a list of continuations *)
type ('a, 'b) tag =
|MUPDATEA of ('a * 'b) list
|MUPDATEB
type ('a, 'b) tag_list = ('a, 'b) tag list

(* val apply_tag_list_cnt :
  ('a, 'b) tag list * ('a -> 'b) -> 'a -> 'b = <fun>
val mupdate_cps_dfc_tags :
  ('a -> 'b) * ('a * 'b) list * ('a, 'b) tag list -> 'a -> 'b = <fun> *)
let rec apply_tag_list_cnt = function
|([], x) -> x
|(MUPDATEA(rest)::cnt, a) -> mupdate_cps_dfc_tags(a, rest, MUPDATEB::cnt)
|(MUPDATEB::cnt, b) -> apply_tag_list_cnt(cnt, b)

and mupdate_cps_dfc_tags(env, bl, cnt) =
  match bl with
  | [] -> apply_tag_list_cnt(cnt, env)

```

```
| (x, v) :: rest -> mupdate_cps_dfc_tags(
  update(env, (x, v)), [], MUPDATEEA(rest)::cnt)
```



Comments:

Problem 4

Below is the code for (uncurried) map, with a test using `fib`, can you apply the CPS transformation to map to produce `map_cps`? Will this `map_cps` work with `fib`? If not, what to do?

```
(* map : ('a -> 'b) * 'a list -> 'b list *)
let rec map(f, l) =
  match l with
  | [] -> []
  | a :: rest -> (f a) :: (map(f, rest))

(* fib : int -> int *)
let rec fib m =
  if m = 0
  then 1
  else if m = 1
  then 1
  else fib(m - 1) + fib (m - 2)

let map_test_1 = map(fib, [0; 1; 2; 3; 4; 5; 6; 7; 8; 9; 10])
(* val map_test_1 : int list = [1; 1; 2; 3; 5; 8; 13; 21; 34; 55; 89] *)
```

- The function `map_cps` does not work with `fib` because the required function type is `'a -> 'a list` rather than `'a -> 'a`, but we can transform the function argument `f` to make it work.

```
(* val map_cps : ('a -> 'a list) * 'a list * ('a list -> 'b) -> 'b = <fun> *)
let rec map_cps(f, l, cnt) =
  match l with
  | [] -> cnt l
  | [a] -> cnt (f a)
  | a :: rest -> map_cps(f, [a], fun x ->
    map_cps(f, rest, fun y -> cnt (x @ y)))

(* val cnt : 'a -> 'a = <fun> *)
let cnt(x) = x

(* val map_cps_2 : ('a -> 'a) * 'a list * ('a list -> 'b) -> 'b = <fun> *)
let map_cps_2(f, l, cnt) = map_cps((fun x -> [f x]), l, cnt)
```

```
let map_test_2 = map_cps_2(fib, [0; 1; 2; 3; 4; 5; 6; 7; 8; 9; 10], cnt)
(* val map_test_2 : int list = [1; 1; 2; 3; 5; 8; 13; 21; 34; 55; 89] *)
```



Comments:

Question 3

How is the state data type in interpreter 1 used? What is the difference between EXAMINE and COMPUTE constructors? Discuss in detail.

- In interpreter 1, a state instance is either an `EXAMINE` instance or a `COMPUTE` instance. `EXAMINE` instance is a syntactic analysis stage instance, `COMPUTE` instance is a computation stage instance.
- We will evaluate a list of expression tokens into a list of continuations, and do computation on continuations whenever we are allowed to. Eventually, evaluate the list of expression tokens into a value.
- We can transfer from `EXAMINE` to a different `EXAMINE` state, or from `COMPUTE` to a different `COMPUTE` state, or transit between `EXAMINE` and `COMPUTE` states. So the `state` data type indicates which stage we are in and what is the next stage we can transfer to via a deterministic `step` function.
- An `EXAMINE` instance encapsulates the current expression token that needs to be evaluated in the current environment, the current environment and a list of continuations that have already been converted from the expression tokens.
- A `COMPUTE` instance encapsulates a list of continuations converted from expression tokens, and a previous value computed. Then do corresponding operations on those expression tokens and the previous value to convert them into a new value.

```
type state =
  | EXAMINE of expr * env * continuation
  | COMPUTE of continuation * value
```



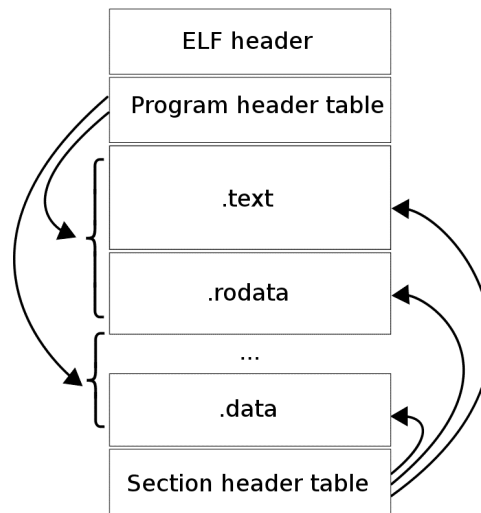
Comments:

Question 4

How can multiple source files be compiled separately and linked together? How and which parts of ELF help you do that?

- Source files will be compiled into separate object files. Name resolution is then done to note all undefined symbols in the object files. A recursive library search is used to find the definitions of those symbols, and add those definitions into the ELF file, specifically, into one of the sections.
 - The section header of an ELF file is used at link-time. For an executable file, there are four main sections: text (executable code), data (initialised data with read/write access rights), rodata (read-only data), bss (uninitialised data with read/write access rights), so those definitions of those symbols will be added into one of the sections.
- If no link errors are generated, then we can concatenate the code segments to form output code segment, concatenate data segments to form output data segment, then perform address relocations to update code or data segments at the specified offset, create a single address space.
 - A segment is a group of sections, defined by the program header table of the ELF file. It is used at run-time. It tells the system how to create a process image, the kernel will map those segments into the virtual address space.
- ELF (executable-and-linkable format) is the common standard file format for executable files and object code. It supports different CPU or instruction set architecture, allowing it to be adopted by different operating systems and hardware platforms. Each ELF file is made up of:
 - One ELF header: (1) identify the file format (ELF), 32-bit or 64-bit, uses little or big endianness and machine instruction set architecture; (2) metadata about program header table and section header table
 - Followed by file data: (1) consists of a program header table describing zero or more sections, data referred to by entries from the program header table, then the section header table; (2) program header shows the segments used

at run-time, (3) section header defines sections, used for linking and relocation.



source: https://linuxhint.com/understanding_elf_file_format/



Comments:

Question 5(y2017p3q4)

Consider the following simple evaluator for a language of expressions written in OCaml.

```

type expr =
  | Integer of int           (* integer *)
  | Pair of expr * expr      (* pair *)
  | Apply of string * expr   (* apply a named function *)

type value =
  | INT of int
  | PAIR of value * value

(* eval : expr -> value *)
let rec eval = function
  | Integer n       -> INT n
  | Pair (e1, e2)   -> PAIR (eval e1, eval e2)
  | Apply (f, e)    -> eval_function(f, eval e)

```

In this code the function `eval_function` has type `string * value -> value` and is used to evaluate some “built in” functions. For example,

```
eval_function("add", PAIR(INT 10, INT 7))
```

could return the value `INT 17`.

- (a) Rewrite the `eval` function in continuation passing style (CPS) to produce a function `eval_cps` so that the function

```
let eval_2 e = eval_cps (fun x -> x) e
```

will produce the same results as the function `eval`. [10 marks]

- The function `eval` is a recursive function using OCaml’s runtime stack, so we try to indicate the explicit evaluation order for `e1` and `e2` in `Pair (e1, e2)`, where continuation `fun a -> ...` expects the computation of `eval(e1)`, the continuation `fun b -> ...` expects the computation of `eval(e2)`, then construct a pair `PAIR(a,b)`.
- In `Apply (f, e)`, the continuation `fun c -> ...` expects the computation of `eval(e)`.

```

let rec eval_cps_util (exp, cnt) =
  match exp with
  | Integer n -> cnt (INT n)
  | Pair (e1, e2) -> eval_cps_util(e1,
    fun a -> eval_cps_util(e2, fun b -> cnt (PAIR(a, b))))
  | Apply (f, e) -> eval_cps_util(e, fun c -> eval_function(f, CNT(c)))

```

```
let eval_cps cnt exp = eval_cps_util (exp, cnt)
```

- (b) Eliminate higher-order continuations from your `eval_cps` function. That is, introduce a data type `cnt` to represent continuations and write functions of type

```
eval_cps_dfn : cnt -> expr -> value  
apply_cnt    : cnt * value -> value  
eval_3       : expr -> value
```

using the technique of defunctionalisation. Note that functions `eval_cps_dfn` and `apply_cnt` will be mutually recursive. [10 marks]

```
type cnt =  
  |CNTA of expr * cnt  
  |CNTB of value * cnt  
  |CNTC of string * cnt  
  |ID  
  
let rec apply_cnt = function  
  |(CNTA(e2, cnt), a) -> eval_cps_dfn (CNTB(a, cnt)) e2  
  |(CNTB(a, cnt), b) -> apply_cnt(cnt, PAIR(a, b))  
  |(CNTC(f, cnt), c) -> eval_function(f, apply_cnt(cnt, c))  
  |(ID, x) -> x  
  
and eval_cps_dfn cnt exp =  
  match exp with  
  |Integer n -> apply_cnt(cnt, INT n)  
  |Pair (e1, e2) -> eval_cps_dfn (CNTA(e2, cnt)) e1  
  |Apply (f, e) -> eval_cps_dfn (CNTC(f, cnt)) e  
  
let eval_3 e = eval_cps_dfn (ID) e
```




Comments:

Question 6

Write a program with the following specification on Linux outputting an ELF binary using x86_64 instruction set:

Input: An integer N (supplied as command line argument or standard input)

Output: N lines. In the first of which there is a  and in each subsequent lines there is an extra star.

Example:

```
Input: 5
Output:
*
**
***
****
*****
```

```
/*
example file: stars.c
*/
#include <stdio.h>
#include <stdlib.h>
int main(int argc, char *argv[])
{
    int n = argc == 2 ? atoi(argv[1]) : 0;
    for (int i = 1; i <= n; i++)
    {
        for (int j = 0; j < i; j++)
        {
            printf("*");
        }
        printf("\n");
    }
    return 0;
}

/* after compiling with gcc stars.c to produce the binary file a.out
a.out:
ELF 64-bit LSB executable, x86-64, version 1 (SYSV),
dynamically linked (uses shared libs), for GNU/Linux 2.6.32, not stripped
*/

/* inspect the ELF header */
ELF Header:
  Magic:   7f 45 4c 46 02 01 01 00 00 00 00 00 00 00 00 00
  Class:                           ELF64
  Data:                               2's complement, little endian
  Version:                           1 (current)
  OS/ABI:                            UNIX - System V
  ABI Version:                       0
  Type:                               EXEC (Executable file)
  Machine:                           Advanced Micro Devices X86-64
  Version:                           0x1
  Entry point address:                0x400570
  Start of program headers:           64 (bytes into file)
  Start of section headers:          6488 (bytes into file)
  Flags:                              0x0
```

```

Size of this header:          64 (bytes)
Size of program headers:      56 (bytes)
Number of program headers:    9
Size of section headers:      64 (bytes)
Number of section headers:    30
Section header string table index: 29

```

```
/* inspect the ELF sections */
```

```
There are 30 section headers, starting at offset 0x1958:
```

```
Section Headers:
```

[Nr]	Name	Type	Address	Offset
	Size	EntSize	Flags Link Info Align	
[0]		NULL	0000000000000000	00000000
	0000000000000000	0000000000000000	0 0 0	
[1]	.interp	PROGBITS	0000000000400238	00000238
	000000000000001c	0000000000000000	A 0 0 1	
[2]	.note.ABI-tag	NOTE	0000000000400254	00000254
	0000000000000020	0000000000000000	A 0 0 4	
[3]	.hash	HASH	0000000000400278	00000278
	0000000000000028	0000000000000004	A 4 0 8	
[4]	.dynsym	DYNSYM	00000000004002a0	000002a0
	0000000000000078	0000000000000018	A 5 1 8	
[5]	.dynstr	STRTAB	0000000000400318	00000318
	0000000000000151	0000000000000000	A 0 0 1	
[6]	.gnu.version	VERSYM	000000000040046a	0000046a
	000000000000000a	0000000000000002	A 4 0 2	
[7]	.gnu.version_r	VERNEED	0000000000400478	00000478
	0000000000000020	0000000000000000	A 5 1 8	
[8]	.rela.dyn	RELA	0000000000400498	00000498
	0000000000000018	0000000000000018	A 4 0 8	
[9]	.rela.plt	RELA	00000000004004b0	000004b0
	0000000000000048	0000000000000018	AI 4 23 8	
[10]	.init	PROGBITS	00000000004004f8	000004f8
	000000000000001a	0000000000000000	AX 0 0 4	
[11]	.plt	PROGBITS	0000000000400520	00000520
	0000000000000040	0000000000000010	AX 0 0 16	
[12]	.plt.got	PROGBITS	0000000000400560	00000560
	0000000000000008	0000000000000000	AX 0 0 8	
[13]	.text	PROGBITS	0000000000400570	00000570
	00000000000001e2	0000000000000000	AX 0 0 16	
[14]	.fini	PROGBITS	0000000000400754	00000754
	0000000000000009	0000000000000000	AX 0 0 4	
[15]	.rodata	PROGBITS	0000000000400760	00000760
	0000000000000004	0000000000000004	AM 0 0 4	
[16]	.eh_frame_hdr	PROGBITS	0000000000400764	00000764
	000000000000003c	0000000000000000	A 0 0 4	
[17]	.eh_frame	PROGBITS	00000000004007a0	000007a0
	000000000000010c	0000000000000000	A 0 0 8	
[18]	.init_array	INIT_ARRAY	0000000000600e00	00000e00
	0000000000000008	0000000000000008	WA 0 0 8	
[19]	.fini_array	FINI_ARRAY	0000000000600e08	00000e08
	0000000000000008	0000000000000008	WA 0 0 8	
[20]	.jcr	PROGBITS	0000000000600e10	00000e10
	0000000000000008	0000000000000000	WA 0 0 8	
[21]	.dynamic	DYNAMIC	0000000000600e18	00000e18
	00000000000001e0	0000000000000010	WA 5 0 8	
[22]	.got	PROGBITS	0000000000600ff8	00000ff8

	0000000000000008	0000000000000008	WA	0	0	8
[23]	.got.plt	PROGBITS	00000000000601000	00001000		
	0000000000000030	0000000000000008	WA	0	0	8
[24]	.data	PROGBITS	00000000000601030	00001030		
	0000000000000010	0000000000000000	WA	0	0	8
[25]	.bss	NOBITS	00000000000601040	00001040		
	0000000000000008	0000000000000000	WA	0	0	1
[26]	.comment	PROGBITS	00000000000000000	00001040		
	000000000000003e	0000000000000001	MS	0	0	1
[27]	.symtab	SYMTAB	00000000000000000	00001080		
	00000000000000600	0000000000000018		28	46	8
[28]	.strtab	STRTAB	00000000000000000	00001680		
	000000000000001df	0000000000000000		0	0	1
[29]	.shstrtab	STRTAB	00000000000000000	0000185f		
	00000000000000f5	0000000000000000		0	0	1

Key to Flags:

W (write), A (alloc), X (execute), M (merge), S (strings), I (info),
 L (link order), O (extra OS processing required), G (group), T (TLS),
 C (compressed), x (unknown), o (OS specific), E (exclude),
 l (large), p (processor specific)



Comments:

Question 1

Read the [paper by Reynolds \(1972\)](#) up to and including section seven. Later sections are delightful as well, but less relevant to the course. Section one can be skimmed, but it nicely sets up the scene. He talks about Algol a lot. For the unfamiliar it is the archetype of block structured programming languages e.g. C, but unlike C it has *some* high-order function support.

This is a great paper in computer science. Apart from historical value, it is also what the lecturer basis his interpreter upon. It will allow you to deeply understand how and why we bother with defunctionalisation & continuation-passing style.

I strongly suggest you read it before you attempt the rest of the workset.

Notes for the paper

- A defined language is defined by an interpreter that is written in a defining language.
 - The variety of values provided in the defining language is richer than in the defined language, we can represent each defined-language value by the same defining-language value
- Applicative features of a language include evaluation and the definition and application of functions.
 - Purely applicable languages are based on lambda calculus, but the semantics of the “real” lambda calculus implies a different order of application than most applicative programming languages
- Imperative features of a language include statement sequencing, labels, jumps, assignment, and procedural side-effects. e.g., purely imperative language such as machine languages
- Higher-order programming language: procedures or labels can be treated as data (e.g., used as arguments to procedures, as results of functions, or as values of assignable variables)
 - In contrast, we have first-order language.
- Function order of application:
 - (1) Call by value: the application process does not begin until after the operator and all of its operands have been evaluated.
 - (2) Call by name: the application process would begin as soon as the operator had been evaluated, and each operand would only be evaluated when and if the function being applied actually depended upon its value.
 - If any arguments cause an infinite loop and are not used in the function body, then call-by-name can terminate while call-by-value cannot.
- Expressions: the meaningful phrases of a program (e.g., constants and variables)
- Evaluation: the process of evaluating an expression
- Value: the result of evaluating an expression
- Environment: binds variables to values, aid in the evaluation of expressions
- For lambda function application $\lambda(x_1, \dots, x_n).r$, the environment in which the body is evaluated during application is an extension of the earlier environment in

which the lambda expression was evaluated (i.e., we have binds the value to the variables x_1, \dots, x_n in the body r).

- However when evaluating x_1, \dots, x_n , we used the same environment, this means we cannot use `let` to define recursive functions, but introduce `letrec`

```
let x = x + 1 and y = x - 1 in x * y
(* with input x = 4, output 15, y = 4 - 1 = 3,
   not using the updated environment *)

(* use let to define recursive functions is invalid *)
let f = λx. if x = 0 then 1 else x × f(x-1) in ...
(* the occurrence of f inside the declaration
   cannot feel the binding of f *)

LAMBDA = [fp: VAR, body: EXP]
evlambda = λ(l,e).λa.eval(body(l), ext(fp(l),a,e))
where ext = λ(z,a,e).λx.if x = z then a else e(x)
(* ext produces an extended environment
   we evaluate l in env e, evaluate body(l) in env ext(fp(l),a,e) *)

LETREC = [dvar: VAR, dexp: LAMBDA, body: EXP]
letrec?(r) -> (* if r is a recursive function *)
letrec e' = λx. if x = dvar(r)
  then evalambda(dexp(r), e') else e(x) in eval(body(r), e'))
```

- Continuation: provides an additional degree of freedom that can be used to meet the condition of order-of-application independence.
 - Instead of performing actions after the function has returned, we embed the further actions in the continuation as an argument to the function.