

## CS1555/CS2055 Recitation 14

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Objective: Practice B+ Tree, Concurrency Control, Linear Hashing

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### Part 1: B+ Tree

1. Build the B+ Tree maintaining the index on the name of students ( $n=3$ ), with the following items: Alex, Christine, Bella, Mary, Peter, Dave.
2. Then do the followings:
  - a) Add "Nancy" to the tree
  - b) Delete "Mary" from the tree.
  - c) Delete "Peter" from the tree.
3. Build a B+ tree for  $n=4$  for the following keys (2, 3, 4, 5, 14, 10, 6, 25, 13, 30, 1)

### Part 2: Concurrency Control

1. Consider the following two transactions:

T1:     $r_1(A)$  ;  
       $r_1(B)$ ;  
      If  $A=0$  then  $B:= B+1$ ;  
       $w_1(B)$ ;

T2:     $r_2(C)$ ;  
       $r_2(B)$ ;  
       $r_2(A)$ ;  
      if  $B>C$  then  $\{A:= A+1; C:=C+1;\}$   
       $w_2(C)$   
       $w_2(A)$

- For each of the following histories/schedules:
  - a) Is it a valid history?
  - b) Use *serializability graphs* to check whether it is serializable or not, and if it is, what is the equivalent serial history/schedule

H1:  $r_1(A) r_1(B) r_2(C) w_1(B) r_2(B) r_2(A) w_2(C) w_2(A)$

H2:  $r_1(A) r_1(B) r_2(C) r_2(B) w_1(B) r_2(A) w_2(C) w_2(A)$

2. Consider the following two transactions:

T1:    r1(A) ;  
          A:=A+100;  
          w1(A);  
          r1(B);  
          B:=B+100;  
          w1(B)

T2:    r2(A);  
          A:=A\*2;  
          w2(A);  
          r2(B);  
          B:=B\*2;  
          w2(B)

- For each of the following histories/schedules check:  
 a) Is it a serializable history?  
 b) What histories are conflict equivalent?

H1: r1(A), w1(A), r1(B), w1(B), r2(A), w2(A), r2(B), w2(B)  
 H2: r1(A), w1(A), r2(A), w2(A), r1(B), w1(B), r2(B), w2(B)  
 H3: r1(A), w1(A), r2(A), w2(A), r2(B), w2(B), r1(B), w1(B)  
 H4: r2(A), w2(A), r1(A), r2(B), w1(A), w2(B), r1(B), w1(B)  
 H5: r1(A), w1(A), r1(B), w1(B), r2(A), w2(A), w2(B), r2(B)

3. Consider the following history, with lock and unlock statements added for each transaction:

| T1  | T2   |
|---|--|
| r1l(A)<br>r1(A)<br>r1l(B)<br>r1(B)<br><br>w1l(B)<br>w1(B)<br><br><br><br>unlock1(A), unlock1(B)<br>commit | <br><br><br><br><br>r12(C)<br>r2(C)<br>r12(B)<br>r2(B)<br><br><br><br><br><br>r12(A)<br>r2(A)<br>w12(C)<br>w2(C)<br>w12(A)<br>w2(A)<br><br><br><br>unlock2(C), unlock2(A) unlock2(B)<br>commit |

- a) Does the history follow 2PL protocol?
- b) Did deadlock happen?

### Part 3: Linear Hashing

#### 1) Dynamic hashing:

##### a) Linear hashing:

- Allows a hash file to expand and shrink the number of buckets dynamically *without* the use of a directory
- **Initial hash function:**  $h_0(K) = K \bmod M$ , where K is the key and M is the number of buckets available
- **s** is the number of buckets (initially  $s = M$ )
- **BLast** and **BSplit** pointers are recorded. BLast is a pointer to the current last bucket (initially  $BLast = M-1$ ). BSplit is a pointer to the bucket that should be split next (initially  $BSplit = 0$ ).
- **bfr** is the blocking factor (number of records per block).
- When inserting a new tuple, if there is a collision, push tuple to an overflow bucket.
- If there are no overflow buckets available, proceed as follows until one becomes available:
  - A new bucket is appended at the end of the hash table and  $BLast'' = BLast + 1$
  - Records in BSplit bucket are hashed again using  $h_1(key) = key \bmod (2 * M)$ 
    - these will either remain in BSplit or stored in BLast''
    - this action may free an overflow bucket.!
  - BSplit becomes  $BSplit + 1$ .
- if  $(BLast = 2s-1)$  then
  - set  $s = 2s$
  - $BLast = s-1$
  - $BSplit = 0$ ,
  - $h_0(key) = h_1(key)$

1. Consider the following record keys: (3, 2, 1, 8, 6, 4, 14, 5, 9). Create the linear hashing structure for the above records after each split assuming  $h_0(k) = k \bmod 4$ ,  $bfr=2$  and:

- a) no overflow buckets.
- b) 1 overflow bucket (add two additional values: 10, 17).