Objective Wine Evaluation

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```
if(!require(tibble))
        install.packages('tibble', repos = "http://cran.us.r-project.org")
if(!require(dplyr))
        install.packages('dplyr', repos = "http://cran.us.r-project.org")
if(!require(tidyr))
        install.packages('tidyr', repos = "http://cran.us.r-project.org")
if(!require(ggplot2))
        install.packages('ggplot2', repos = "http://cran.us.r-project.org")
if(!require(leaps))
        install.packages('leaps', repos = "http://cran.us.r-project.org")
if(!require(pls))
        install.packages('pls', repos = "http://cran.us.r-project.org")
if(!require(glmnet))
        install.packages('glmnet', repos = "http://cran.us.r-project.org")
library(tibble)
library(dplyr)
library(tidyr)
library(ggplot2)
library(leaps)
library(pls)
library(glmnet)
```

1. Overview of Data

```
red = read.csv("../data/winequality-red.csv", header = TRUE, sep = ";")
# white = read.csv("../data/winequality-white.csv", header = TRUE, sep = ";")
# 1) summary of the data
summary(red)
```

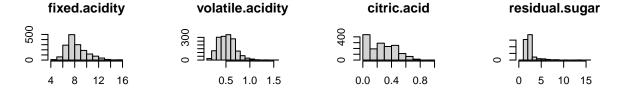
```
fixed.acidity
                 volatile.acidity citric.acid
                                               residual.sugar
## Min. : 4.60 Min. :0.1200 Min.
                                     :0.000
                                              Min.
                                                    : 0.900
## 1st Qu.: 7.10
                1st Qu.:0.3900
                                1st Qu.:0.090
                                              1st Qu.: 1.900
## Median : 7.90
                Median :0.5200
                               Median :0.260
                                              Median : 2.200
## Mean : 8.32
                Mean :0.5278
                                Mean :0.271
                                              Mean : 2.539
## 3rd Qu.: 9.20
                 3rd Qu.:0.6400
                                3rd Qu.:0.420
                                               3rd Qu.: 2.600
## Max. :15.90
                 Max. :1.5800
                                Max.
                                       :1.000
                                              Max. :15.500
##
                   free.sulfur.dioxide total.sulfur.dioxide
     chlorides
                                                          density
## Min. :0.01200 Min. : 1.00
                                   Min. : 6.00
                                                   Min.
                                                              :0.9901
```

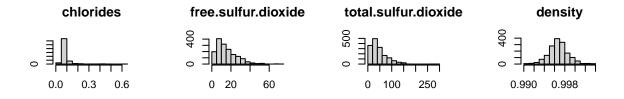
```
1st Qu.:0.07000
                      1st Qu.: 7.00
                                           1st Qu.: 22.00
                                                                 1st Qu.:0.9956
##
    Median :0.07900
                      Median :14.00
                                           Median : 38.00
                                                                 Median :0.9968
                      Mean :15.87
                                           Mean
                                                  : 46.47
           :0.08747
                                                                 Mean
                                                                        :0.9967
    3rd Qu.:0.09000
                      3rd Qu.:21.00
                                           3rd Qu.: 62.00
                                                                 3rd Qu.:0.9978
##
##
           :0.61100
                      Max.
                            :72.00
                                           Max.
                                                   :289.00
                                                                         :1.0037
##
          рΗ
                       sulphates
                                         alcohol
                                                          quality
           :2.740
                            :0.3300
                                             : 8.40
                                                              :3.000
    Min.
                    Min.
                                      Min.
                                                       Min.
                                      1st Qu.: 9.50
                                                       1st Qu.:5.000
##
    1st Qu.:3.210
                    1st Qu.:0.5500
##
    Median :3.310
                    Median :0.6200
                                      Median :10.20
                                                       Median :6.000
##
    Mean
           :3.311
                    Mean
                            :0.6581
                                      Mean
                                             :10.42
                                                       Mean
                                                              :5.636
    3rd Qu.:3.400
                    3rd Qu.:0.7300
                                      3rd Qu.:11.10
                                                       3rd Qu.:6.000
    Max.
           :4.010
                    Max.
                            :2.0000
                                             :14.90
                                                       Max.
                                                              :8.000
                                      Max.
```

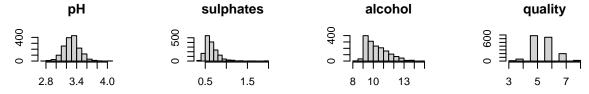
```
# 2) histogram: distribution of each variable
varnames = colnames(red)

par(mfrow = c(3, 4))

for(name in varnames){
    hist(red[[name]], main = name, xlab = NULL, ylab = NULL)}
}
```

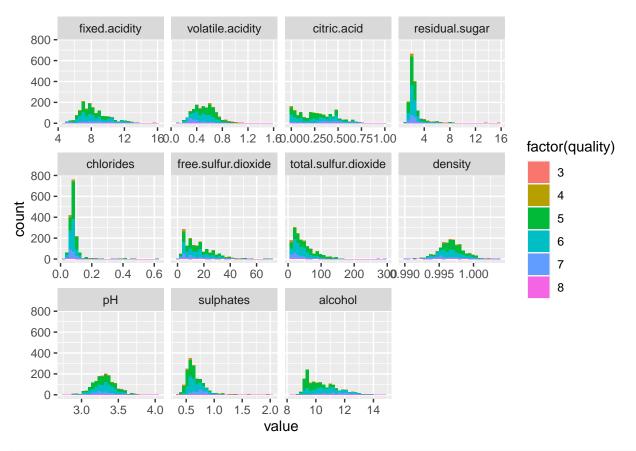






```
# 3) scatter plot:
# average distribution of each variable based on the quality
mean_summary = red %>% group_by(quality) %>% summarise_all(mean)
par(mfrow = c(3, 4))
for(name in varnames){
```

```
plot(mean_summary$quality,
                  mean_summary[[name]],
                  xlab = "quality",
                  ylab = name
           )
}
                                                                                                 residual.sugar
                                volatile.acidity
fixed.acidity
                                     0.9
                                                                 citric.acid
                                     0.4
                                                                      0.20
                                                                                                      2.50
          3
                5
                      7
                                          3
                                                5
                                                       7
                                                                           3
                                                                                 5
                                                                                                            3
                                                                                                                 5
                                                                                                                        7
                                               quality
                                                                                quality
               quality
                                                                                                                 quality
                                free.sulfur.dioxide
                                                                 total.sulfur.dioxide
chlorides
                                                                      22
                                     11 16
                                                                                                 density
                                                                                                      0.9955
     0.07
                                                                      25
          3
                5
                      7
                                          3
                                                5
                                                                           3
                                                                                                            3
                                                                                                                  5
               quality
                                               quality
                                                                                quality
                                                                                                                 quality
                                sulphates
                                                                 alcohol
                                                                                                 quality
펀
                                                                                                       9
     3.28
                                     0.60
                                                                      10.0
          3
                      7
                                          3
                                                       7
                                                                           3
                                                                                                            3
                5
                                                                                                                  5
               quality
                                               quality
                                                                                quality
                                                                                                                 quality
# 4) histogram: distribution of each variable grouped by quality
ggplot(gather(red, key, value, -c(quality), factor_key = TRUE),
          aes(value, fill = factor(quality))) +
           geom_histogram(bins = 30) +
           facet_wrap(~ key, scales = 'free_x')
```



5) linear regression analysis of original data
lm_ori = lm(quality ~ ., red)
summary(lm_ori)

```
## lm(formula = quality ~ ., data = red)
##
## Residuals:
##
        Min
                  1Q
                       Median
                                     3Q
                                             Max
## -2.68911 -0.36652 -0.04699 0.45202
                                        2.02498
##
## Coefficients:
                          Estimate Std. Error t value Pr(>|t|)
##
                                    2.119e+01
                                                         0.3002
## (Intercept)
                         2.197e+01
                                                 1.036
## fixed.acidity
                                     2.595e-02
                                                 0.963
                                                         0.3357
                         2.499e-02
## volatile.acidity
                        -1.084e+00
                                     1.211e-01
                                                -8.948
                                                        < 2e-16 ***
## citric.acid
                                                -1.240
                                                         0.2150
                         -1.826e-01
                                     1.472e-01
## residual.sugar
                         1.633e-02
                                     1.500e-02
                                                 1.089
                                                         0.2765
## chlorides
                        -1.874e+00
                                     4.193e-01
                                                -4.470 8.37e-06 ***
## free.sulfur.dioxide
                         4.361e-03
                                     2.171e-03
                                                 2.009
                                                         0.0447 *
## total.sulfur.dioxide -3.265e-03
                                     7.287e-04
                                                -4.480 8.00e-06 ***
## density
                                                -0.827
                                                         0.4086
                        -1.788e+01
                                     2.163e+01
## pH
                        -4.137e-01
                                     1.916e-01
                                                -2.159
                                                         0.0310 *
## sulphates
                         9.163e-01
                                     1.143e-01
                                                 8.014 2.13e-15 ***
## alcohol
                         2.762e-01 2.648e-02 10.429 < 2e-16 ***
```

Call:

```
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.648 on 1587 degrees of freedom
## Multiple R-squared: 0.3606, Adjusted R-squared: 0.3561
## F-statistic: 81.35 on 11 and 1587 DF, p-value: < 2.2e-16
par(mfrow = c(2, 2))
plot(lm_ori)
                                                     Standardized residuals
                 Residuals vs Fitted
                                                                          Normal Q-Q
                             ത്തുത്ത
Residuals
      0
                                                           0
                                          6530
      က
                          0833
                                                           4
                      5.5 6.0
                                  6.5
                                      7.0
                                           7.5
                                                                  -3
                                                                       -2
                                                                                 0
                                                                                           2
                                                                                                3
                 5.0
                      Fitted values
                                                                       Theoretical Quantiles
|Standardized residuals
                                                     Standardized residuals
                    Scale-Location
                                                                    Residuals vs Leverage
     2.0
                             \mathbf{0000}
      1.0
                                                                                                1520
     0.0
                                  6.5
                                            7.5
                                                                     0.02
             4.5
                  5.0
                       5.5
                            6.0
                                       7.0
                                                               0.00
                                                                            0.04
                                                                                   0.06
                                                                                          80.0
                                                                                                 0.10
```

Leverage

6) Check multicolinearity cor(red)

Fitted values

```
##
                         fixed.acidity volatile.acidity citric.acid residual.sugar
## fixed.acidity
                           1.00000000
                                           -0.256130895 0.67170343
                                                                        0.114776724
## volatile.acidity
                           -0.25613089
                                            1.00000000 -0.55249568
                                                                        0.001917882
## citric.acid
                           0.67170343
                                           -0.552495685
                                                          1.00000000
                                                                        0.143577162
## residual.sugar
                           0.11477672
                                            0.001917882
                                                         0.14357716
                                                                        1.00000000
## chlorides
                           0.09370519
                                            0.061297772
                                                         0.20382291
                                                                        0.055609535
## free.sulfur.dioxide
                                           -0.010503827 -0.06097813
                           -0.15379419
                                                                        0.187048995
## total.sulfur.dioxide
                           -0.11318144
                                            0.076470005
                                                         0.03553302
                                                                        0.203027882
## density
                                            0.022026232
                                                         0.36494718
                           0.66804729
                                                                        0.355283371
## pH
                           -0.68297819
                                            0.234937294 -0.54190414
                                                                       -0.085652422
## sulphates
                           0.18300566
                                           -0.260986685
                                                         0.31277004
                                                                        0.005527121
## alcohol
                           -0.06166827
                                           -0.202288027
                                                         0.10990325
                                                                        0.042075437
## quality
                           0.12405165
                                           -0.390557780 0.22637251
                                                                        0.013731637
                           chlorides free.sulfur.dioxide total.sulfur.dioxide
## fixed.acidity
                         0.093705186
                                             -0.153794193
                                                                    -0.11318144
```

```
## volatile.acidity
                      0.061297772
                                        -0.010503827
                                                             0.07647000
## citric.acid
                      0.203822914
                                        -0.060978129
                                                             0.03553302
## residual.sugar
                                                             0.20302788
                      0.055609535
                                         0.187048995
## chlorides
                      1.000000000
                                         0.005562147
                                                             0.04740047
## free.sulfur.dioxide
                      0.005562147
                                         1.000000000
                                                             0.66766645
## total.sulfur.dioxide 0.047400468
                                         0.667666450
                                                             1.00000000
## density
                      0.200632327
                                        -0.021945831
                                                             0.07126948
                     -0.265026131
## pH
                                         0.070377499
                                                            -0.06649456
## sulphates
                      0.371260481
                                         0.051657572
                                                             0.04294684
## alcohol
                     -0.221140545
                                        -0.069408354
                                                            -0.20565394
## quality
                     -0.128906560
                                        -0.050656057
                                                            -0.18510029
                         density
                                         рН
                                              sulphates
                                                           alcohol
                                            0.183005664 -0.06166827
## fixed.acidity
                      0.66804729 -0.68297819
## volatile.acidity
                      ## citric.acid
                      0.36494718 -0.54190414 0.312770044 0.10990325
## residual.sugar
                      0.35528337 -0.08565242 0.005527121 0.04207544
## chlorides
                      ## free.sulfur.dioxide -0.02194583 0.07037750 0.051657572 -0.06940835
## total.sulfur.dioxide 0.07126948 -0.06649456 0.042946836 -0.20565394
## density
                      ## pH
                     -0.34169933 1.00000000 -0.196647602 0.20563251
## sulphates
                      0.14850641 -0.19664760 1.000000000 0.09359475
## alcohol
                     -0.49617977 0.20563251 0.093594750 1.00000000
## quality
                     -0.17491923 -0.05773139 0.251397079 0.47616632
##
                         quality
## fixed.acidity
                      0.12405165
## volatile.acidity
                     -0.39055778
## citric.acid
                      0.22637251
## residual.sugar
                      0.01373164
## chlorides
                      -0.12890656
## free.sulfur.dioxide -0.05065606
## total.sulfur.dioxide -0.18510029
## density
                     -0.17491923
## pH
                     -0.05773139
## sulphates
                      0.25139708
## alcohol
                      0.47616632
## quality
                      1.00000000
```

2. Transformations

logred\$logVA = log(red\$volatile.acidity)

colnames(red)

```
logred$logCA = red$citric.acid
logred$logRS = log(red$residual.sugar)
logred$logCL = log(red$chlorides)
logred$logFS = log(red$free.sulfur.dioxide)
logred$logTS = log(red$total.sulfur.dioxide)
logred$logDE = log(red$density)
logred$logPH = red$pH
logred$logSP = log(red$sulphates)
logred$logAL = log(red$alcohol)
# 2) compare the AIC (lm_ori vs lm using the log(data) as a predictor)
lm_log = lm(quality ~ ., logred[,12:23])
comp_AIC = data.frame(lm = c("Ori.", "Log."),
                      AIC = c(AIC(lm_ori), AIC(lm_log)))
comp_AIC$AIC = round(comp_AIC$AIC, 3)
comp_AIC
##
       lm
               AIC
## 1 Ori. 3164.277
## 2 Log. 3154.790
# 3) select the predictor to use with the log transformation.
boolExpand = expand.grid(c(0,1), c(0,1), c(0,1), c(0,1), c(0,1),
                          c(0,1), c(0,1), c(0,1), c(0,1)
boolExpand = cbind(boolExpand[,1:2], 0, boolExpand[,3:7], 0, boolExpand[,8:9])
df1 = logred[,1:12] # ori. data
lm1 = lm(quality ~ ., df1) # lm model
aic1 = AIC(lm1) # ori. AIC
for (i in 1:nrow(boolExpand)) {
       bool = as.numeric(boolExpand[i,])
        df_trans = logred[, c(bool*12 + 1:11, 12)]
       lm2 = lm(quality ~ ., df_trans)
        aic2 = AIC(1m2)
        if(aic2 < aic1){</pre>
                df1 = df_trans
                lm1 = lm2
                aic1 = aic2
                print(paste0('switching ', i))
        }
}
## [1] "switching 2"
## [1] "switching 6"
## [1] "switching 17"
## [1] "switching 18"
## [1] "switching 129"
## [1] "switching 130"
## [1] "switching 134"
## [1] "switching 145"
```

```
## [1] "switching 146"
## [1] "switching 150"
## [1] "switching 214"
head(df1)
        logFA volatile.acidity citric.acid
                                               logRS chlorides
                                                                   logFS
## 1 2.001480
                          0.70
                                     0.00 0.6418539
                                                          0.076 2.397895
## 2 2.054124
                          0.88
                                      0.00 0.9555114
                                                          0.098 3.218876
## 3 2.054124
                          0.76
                                      0.04 0.8329091
                                                          0.092 2.708050
## 4 2.415914
                          0.28
                                      0.56 0.6418539
                                                          0.075 2.833213
## 5 2.001480
                          0.70
                                      0.00 0.6418539
                                                          0.076 2.397895
## 6 2.001480
                                                          0.075 2.564949
                          0.66
                                      0.00 0.5877867
                                         рΗ
   total.sulfur.dioxide
                                 logDE
                                                 logSP alcohol quality
## 1
                       34 -0.002202424 3.51 -0.5798185
                                                            9.4
                                                                      5
## 2
                       67 -0.003205131 3.20 -0.3856625
                                                            9.8
                                                                      5
## 3
                       54 -0.003004509 3.26 -0.4307829
                                                            9.8
                                                                      5
## 4
                       60 -0.002002003 3.16 -0.5447272
                                                            9.8
                                                                      6
## 5
                       34 -0.002202424 3.51 -0.5798185
                                                            9.4
                                                                      5
## 6
                       40 -0.002202424 3.51 -0.5798185
                                                            9.4
names(df1) # final columns selected
  [1] "logFA"
                                "volatile.acidity"
                                                       "citric.acid"
   [4] "logRS"
                                "chlorides"
                                                       "logFS"
## [7] "total.sulfur.dioxide" "logDE"
                                                       "pH"
## [10] "logSP"
                                "alcohol"
                                                       "quality"
# 4) compare the AIC (lm_ori vs lm_log vs final model after transformation)
comp_AIC = rbind(comp_AIC, c("Trans.", round(AIC(lm1), 3)))
comp_AIC
                 AIC
##
         lm
## 1
       Ori. 3164.277
## 2
      Log. 3154.79
## 3 Trans.
              3127.7
# 5) Map dependent variable to the real line.
logitlm = lm(log(quality/(11-quality)) ~., data = df1)
summary(logitlm)
##
## lm(formula = log(quality/(11 - quality)) ~ ., data = df1)
## Residuals:
        Min
                  1Q
                       Median
                                    3Q
## -1.06846 -0.13385 -0.01661 0.15906 0.79613
## Coefficients:
```

```
##
                        Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                      -5.045e-01 3.712e-01 -1.359 0.17434
## logFA
                       1.664e-01 8.524e-02
                                             1.952 0.05106 .
## volatile.acidity
                      -3.760e-01 4.487e-02 -8.380 < 2e-16 ***
## citric.acid
                      -7.908e-02 5.418e-02 -1.460 0.14455
## logRS
                       4.823e-02 2.365e-02
                                             2.039 0.04161 *
## chlorides
                      -7.059e-01 1.523e-01 -4.635 3.86e-06 ***
## logFS
                        3.255e-02 1.231e-02
                                             2.643 0.00829 **
## total.sulfur.dioxide -1.297e-03 2.735e-04 -4.740 2.33e-06 ***
## logDE
                      -1.890e+01 8.461e+00 -2.234 0.02563 *
## pH
                      -1.310e-01 7.319e-02 -1.790 0.07363 .
## logSP
                                             9.713 < 2e-16 ***
                        3.151e-01 3.244e-02
## alcohol
                        8.989e-02 1.021e-02
                                             8.801 < 2e-16 ***
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 0.2398 on 1587 degrees of freedom
## Multiple R-squared: 0.373, Adjusted R-squared: 0.3686
## F-statistic: 85.81 on 11 and 1587 DF, p-value: < 2.2e-16
summary(lm1)
##
## Call:
## lm(formula = quality ~ ., data = df_trans)
## Residuals:
##
      Min
               1Q Median
                              3Q
                                     Max
## -2.7410 -0.3635 -0.0474 0.4389 2.0094
##
## Coefficients:
##
                         Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                        4.050e+00 9.918e-01 4.083 4.66e-05 ***
                        4.622e-01 2.277e-01
                                              2.030 0.04255 *
## logFA
## volatile.acidity
                      -1.007e+00 1.199e-01 -8.399 < 2e-16 ***
## citric.acid
                      -2.166e-01 1.447e-01 -1.496 0.13476
## logRS
                       1.301e-01 6.319e-02
                                            2.059 0.03963 *
## chlorides
                       -1.868e+00 4.069e-01 -4.590 4.79e-06 ***
## logFS
                        8.940e-02 3.290e-02
                                             2.717 0.00666 **
## total.sulfur.dioxide -3.559e-03 7.308e-04 -4.869 1.23e-06 ***
## logDE
                      -5.111e+01 2.260e+01 -2.261 0.02388 *
## pH
                       -3.331e-01 1.955e-01 -1.703 0.08870 .
## logSP
                        8.455e-01 8.668e-02
                                             9.755 < 2e-16 ***
## alcohol
                        2.408e-01 2.729e-02
                                             8.824 < 2e-16 ***
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 0.6406 on 1587 degrees of freedom
## Multiple R-squared: 0.375, Adjusted R-squared: 0.3707
## F-statistic: 86.57 on 11 and 1587 DF, p-value: < 2.2e-16
AIC_correction = sum(log(11/df1$quality/(11-df1$quality))) *2
```

```
comp_AIC = rbind(comp_AIC, c("Logit.", round(AIC(logitlm) - AIC_correction, 3)))
comp_AIC
##
        lm
                AIC
## 1
      Ori. 3164.277
## 2 Log. 3154.79
## 3 Trans.
            3127.7
## 4 Logit. 3146.288
3. Variable Selection
colnames(df1)
## [1] "logFA"
                               "volatile.acidity"
                                                     "citric.acid"
## [4] "logRS"
                               "chlorides"
                                                     "logFS"
## [7] "total.sulfur.dioxide" "logDE"
                                                     "Hq"
## [10] "logSP"
                              "alcohol"
                                                     "quality"
quadred = df1
# 1) add 11 new columns that transform each column data into (data)^2
quadred$quadFA = (quadred$logFA)^2
quadred$quadVA = (quadred$volatile.acidity)^2
quadred$quadCA = (quadred$citric.acid)^2
quadred$quadRS = (quadred$logRS)^2
quadred$quadCL = (quadred$chlorides)^2
quadred$quadFS = (quadred$logFS)^2
quadred$quadTS = (quadred$total.sulfur.dioxide)^2
quadred$quadDE = (quadred$logDE)^2
quadred$quadPH = (quadred$pH)^2
quadred$quadSP = (quadred$logSP)^2
quadred$quadAL = (quadred$alcohol)^2
lm_trans = lm(quality ~ ., quadred)
summary(lm_trans)
##
## Call:
## lm(formula = quality ~ ., data = quadred)
##
## Residuals:
##
                 1Q Median
       Min
                                   3Q
                                           Max
## -2.70481 -0.38031 -0.01694 0.42765 1.99261
##
## Coefficients:
                        Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                       -2.209e+00 5.280e+00 -0.418 0.67568
## logFA
                       5.032e+00 1.777e+00 2.832 0.00469 **
## volatile.acidity -6.082e-01 4.271e-01 -1.424 0.15460
```

-5.141e-01 3.197e-01 -1.608 0.10808

citric.acid

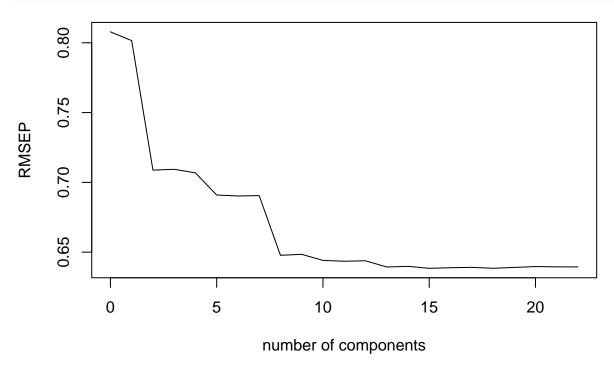
```
## logRS
                        1.685e-01 1.864e-01
                                               0.904 0.36612
                       -1.460e+00
## chlorides
                                   1.103e+00 -1.323 0.18594
## logFS
                        2.745e-01
                                   1.460e-01
                                               1.880
                                                      0.06028 .
                                   1.768e-03 -3.149
## total.sulfur.dioxide -5.568e-03
                                                      0.00167 **
## logDE
                       -7.760e+00
                                   3.047e+01 -0.255
                                                      0.79897
                                   3.404e+00
                                               0.138
                                                      0.89040
## pH
                        4.691e-01
                                   1.690e-01
                                               0.597
                                                      0.55062
## logSP
                        1.009e-01
## alcohol
                        2.772e-01
                                   2.749e-01
                                               1.009
                                                      0.31330
                                   4.173e-01 -2.631
## quadFA
                       -1.098e+00
                                                      0.00860 **
## quadVA
                       -2.763e-01
                                   3.273e-01 -0.844
                                                      0.39863
## quadCA
                        5.996e-01
                                   4.741e-01
                                               1.265
                                                      0.20612
## quadRS
                       -2.873e-02
                                   7.263e-02 -0.396
                                                      0.69246
## quadCL
                       -2.501e-01
                                   2.407e+00 -0.104
                                                      0.91727
                                   2.943e-02 -1.262
## quadFS
                       -3.715e-02
                                                     0.20711
## quadTS
                        1.496e-05
                                   9.375e-06
                                               1.596 0.11080
## quadDE
                        7.943e+03
                                   3.560e+03
                                               2.231
                                                      0.02583 *
                                   5.105e-01
## quadPH
                       -1.415e-01
                                              -0.277
                                                     0.78171
## quadSP
                       -1.135e+00
                                   2.071e-01 -5.480 4.95e-08 ***
                       -2.508e-03 1.272e-02 -0.197 0.84372
## quadAL
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.6331 on 1576 degrees of freedom
## Multiple R-squared: 0.3938, Adjusted R-squared: 0.3853
## F-statistic: 46.54 on 22 and 1576 DF, p-value: < 2.2e-16
# 1) AIC
require(leaps)
b = regsubsets(quality ~ ., quadred, nvmax = 22)
rs = summary(b)
rs$which
```

```
(Intercept) logFA volatile.acidity citric.acid logRS chlorides logFS
## 1
             TRUE FALSE
                                   FALSE
                                                FALSE FALSE
                                                                FALSE FALSE
## 2
             TRUE FALSE
                                     TRUE
                                                FALSE FALSE
                                                                 FALSE FALSE
## 3
                                                                FALSE FALSE
             TRUE FALSE
                                     TRUE
                                                FALSE FALSE
             TRUE FALSE
                                     TRUE
                                                FALSE FALSE
                                                                FALSE FALSE
## 5
             TRUE FALSE
                                     TRUE
                                                FALSE FALSE
                                                                 TRUE FALSE
## 6
             TRUE FALSE
                                     TRUE
                                                FALSE FALSE
                                                                 TRUE FALSE
## 7
             TRUE FALSE
                                     TRUE
                                                FALSE FALSE
                                                                 TRUE TRUE
## 8
             TRUE FALSE
                                     TRUE
                                                FALSE FALSE
                                                                 TRUE
                                                                       TRUE
## 9
             TRUE FALSE
                                                FALSE FALSE
                                                                  TRUE
                                     TRUE
                                                                        TRUE
## 10
             TRUE TRUE
                                     TRUE
                                                FALSE FALSE
                                                                 TRUE
                                                                        TRUE
## 11
             TRUE TRUE
                                    FALSE
                                                FALSE FALSE
                                                                  TRUE
                                                                        TRUE
## 12
             TRUE TRUE
                                    FALSE
                                                FALSE TRUE
                                                                  TRUE
                                                                       TRUE
## 13
             TRUE
                   TRUE
                                     TRUE
                                                FALSE
                                                       TRUE
                                                                  TRUE
                                                                        TRUE
## 14
             TRUE TRUE
                                     TRUE
                                                 TRUE TRUE
                                                                  TRUE
                                                                       TRUE
## 15
             TRUE
                  TRUE
                                     TRUE
                                                 TRUE TRUE
                                                                  TRUE
                                                                        TRUE
## 16
             TRUE
                   TRUE
                                                 TRUE TRUE
                                     TRUE
                                                                 TRUE
                                                                       TRUE
## 17
             TRUE
                   TRUE
                                     TRUE
                                                 TRUE
                                                       TRUE
                                                                  TRUE
                                                                        TRUE
## 18
             TRUE TRUE
                                     TRUE
                                                 TRUE TRUE
                                                                 TRUE
                                                                       TRUE
## 19
             TRUE TRUE
                                     TRUE
                                                 TRUE TRUE
                                                                  TRUE
                                                                       TRUE
             TRUE TRUE
                                     TRUE
                                                 TRUE TRUE
                                                                  TRUE TRUE
## 20
```

```
## 21
             TRUE TRUE
                                    TRUE
                                                TRUE TRUE
                                                                 TRUE TRUE
## 22
             TRUE TRUE
                                                TRUE TRUE
                                                                TRUE TRUE
                                    TRUE
      total.sulfur.dioxide logDE
                                    pH logSP alcohol quadFA quadVA quadCA quadRS
                                                TRUE FALSE FALSE FALSE
## 1
                     FALSE FALSE FALSE
## 2
                     FALSE FALSE FALSE
                                                TRUE
                                                      FALSE
                                                             FALSE
                                                                     FALSE FALSE
## 3
                     FALSE FALSE FALSE
                                                TRUE FALSE
                                                             FALSE FALSE FALSE
## 4
                     FALSE FALSE FALSE
                                                      FALSE
                                                             FALSE
                                                                    FALSE FALSE
                                                TRUE
                     FALSE FALSE FALSE
                                                      FALSE
                                                             FALSE
                                                                    FALSE FALSE
## 5
                                                TRUE
## 6
                     TRUE FALSE FALSE FALSE
                                                TRUE
                                                      FALSE
                                                             FALSE
                                                                     FALSE
                                                                            FALSE
## 7
                     TRUE FALSE FALSE FALSE
                                                TRUE
                                                      FALSE
                                                             FALSE
                                                                     FALSE
                                                                            FALSE
## 8
                    TRUE FALSE FALSE FALSE
                                                TRUE
                                                      FALSE
                                                             FALSE
                                                                     FALSE
                                                                            FALSE
## 9
                   TRUE FALSE FALSE FALSE
                                                TRUE
                                                      FALSE
                                                             FALSE
                                                                    FALSE FALSE
                  TRUE FALSE FALSE FALSE
TRUE FALSE FALSE FALSE
TRUE FALSE FALSE FALSE
## 10
                                                TRUE
                                                       TRUE
                                                             FALSE
                                                                    FALSE FALSE
## 11
                                                TRUE
                                                        TRUE
                                                               TRUE
                                                                    FALSE FALSE
## 12
                                                TRUE
                                                        TRUE
                                                               TRUE
                                                                    FALSE FALSE
## 13
                                                TRUE
                                                        TRUE
                                                             FALSE
                                                                     FALSE
                                                                            FALSE
## 14
                     TRUE FALSE FALSE FALSE
                                                TRUE
                                                             FALSE
                                                                     FALSE FALSE
                                                        TRUE
## 15
                    TRUE FALSE FALSE FALSE
                                                TRUE
                                                        TRUE
                                                             FALSE
                                                                      TRUE FALSE
## 16
                   TRUE FALSE FALSE FALSE
                                                TRUE
                                                        TRUE
                                                               TRUE
                                                                      TRUE FALSE
## 17
                      TRUE FALSE FALSE
                                        TRUE
                                                TRUE
                                                        TRUE
                                                               TRUE
                                                                      TRUE
                                                                            FALSE
## 18
                     TRUE FALSE FALSE
                                        TRUE
                                                TRUE
                                                        TRUE
                                                               TRUE
                                                                      TRUE
                                                                             TRUE
## 19
                     TRUE
                           TRUE FALSE
                                        TRUE
                                                TRUE
                                                        TRUE
                                                               TRUE
                                                                      TRUE
                                                                             TRUE
## 20
                      TRUE
                            TRUE FALSE
                                        TRUE
                                                TRUE
                                                               TRUE
                                                                      TRUE
                                                        TRUE
                                                                             TRUE
## 21
                      TRUE
                            TRUE
                                  TRUE
                                        TRUE
                                                TRUE
                                                        TRUE
                                                               TRUE
                                                                      TRUE
                                                                             TRUE
## 22
                      TRUE
                           TRUE TRUE TRUE
                                                TRUE
                                                        TRUE
                                                               TRUE
                                                                      TRUE
                                                                             TRUE
      quadCL quadFS quadTS quadDE quadPH quadSP quadAL
## 1
       FALSE FALSE FALSE
                                  FALSE
                                          FALSE FALSE
       FALSE FALSE FALSE
                                   FALSE
                                          FALSE
                                                 FALSE
## 2
## 3
       FALSE FALSE
                    FALSE FALSE
                                   FALSE
                                           TRUE FALSE
       FALSE FALSE
                    FALSE FALSE
## 4
                                    TRUE
                                           TRUE
                                                 FALSE
## 5
       FALSE
              FALSE
                     FALSE
                           FALSE
                                    TRUE
                                           TRUE
                                                 FALSE
## 6
       FALSE
             FALSE
                     FALSE
                            FALSE
                                    TRUE
                                           TRUE
                                                 FALSE
## 7
       FALSE
              FALSE
                     FALSE
                            FALSE
                                    TRUE
                                           TRUE
                                                 FALSE
## 8
       FALSE
             FALSE
                     FALSE
                                    TRUE
                                           TRUE
                                                 FALSE
                             TRUE
## 9
       FALSE
             FALSE
                      TRUE
                             TRUE
                                    TRUE
                                           TRUE
                                                 FALSE
## 10
      FALSE FALSE
                     FALSE
                             TRUE
                                    TRUE
                                           TRUE FALSE
## 11
      FALSE FALSE
                      TRUE
                             TRUE
                                    TRUE
                                           TRUE
                                                FALSE
## 12
      FALSE
             FALSE
                      TRUE
                             TRUE
                                    TRUE
                                           TRUE
                                                FALSE
## 13
       FALSE
               TRUE
                      TRUE
                             TRUE
                                    TRUE
                                           TRUE
                                                 FALSE
## 14
      FALSE
               TRUE
                      TRUE
                             TRUE
                                           TRUE
                                                FALSE
                                    TRUE
      FALSE
               TRUE
                      TRUE
                             TRUE
                                    TRUE
                                           TRUE
                                                 FALSE
## 15
## 16
      FALSE
               TRUE
                      TRUE
                             TRUE
                                    TRUE
                                           TRUE
                                                FALSE
       FALSE
##
  17
               TRUE
                      TRUE
                             TRUE
                                    TRUE
                                           TRUE
                                                 FALSE
## 18
      FALSE
               TRUE
                      TRUE
                             TRUE
                                    TRUE
                                           TRUE
                                                 FALSE
       FALSE
                      TRUE
                                           TRUE
## 19
               TRUE
                             TRUE
                                    TRUE
                                                 FALSE
## 20
       FALSE
               TRUE
                      TRUE
                             TRUE
                                    TRUE
                                           TRUE
                                                  TRUE
## 21
       FALSE
               TRUE
                      TRUE
                             TRUE
                                    TRUE
                                           TRUE
                                                  TRUE
## 22
        TRUE
               TRUE
                      TRUE
                                           TRUE
                             TRUE
                                    TRUE
                                                  TRUE
par(mfrow = c(1, 3))
p = 22
eval_aic = nrow(red)*log(rs$rss/nrow(red)) + (2:(p+1))*2
plot(eval_aic ~ I(1:p),
```

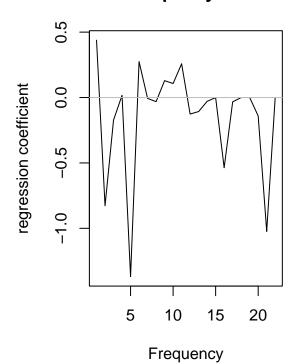
```
ylab = 'AIC',
     xlab = 'Number of Predictors', pch = 20)
text(I(1:p), eval_aic, round(eval_aic, 2), cex = 0.5, pos = 4)
paste("min AIC: ", which.min(eval_aic))
## [1] "min AIC: 12"
min_aic = which.min(eval_aic)
boolCol_step = as.vector(rs$which[min_aic, -1]) # columns selected by min AIC
# 2) Adjusted R-Squre
plot(1:p, rs$adjr2,
     xlab = 'Number of Predictors',
     ylab='Adjusted R-Square', pch = 20)
paste("max Adjusted R-Squre: ", which.max(rs$adjr2))
## [1] "max Adjusted R-Squre: 15"
# 3) Mellow's Cp
plot(2:(p+1), rs$cp,
     xlab = 'Number of Parameters',
     ylab = 'Cp Statistic', pch = 20)
abline(0,1)
                                                                       400
                                     0.35
    -1200
                                                                      300
                                 Adjusted R-Square
                                                                  Cp Statistic
                                                                      200
                                     0.30
    -1300
          -1288.14
                                                                       100
                                     0.25
                10
                    15
                         20
                                             5
                                                 10
                                                     15
                                                          20
                                                                                  10
                                                                                      15
                                                                                           20
          Number of Predictors
                                           Number of Predictors
                                                                            Number of Parameters
par(mfrow = c(1, 1))
# 4) Principal component regression
require(pls)
```

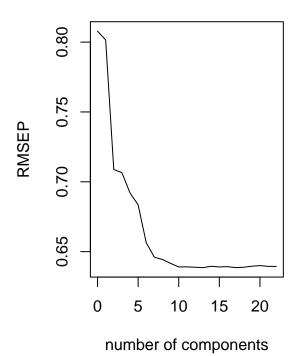
```
set.seed(664)
lm_pcr = pcr(quality ~ ., data = quadred, validation = "CV", ncomp = 22)
cv_pcr = RMSEP(lm_pcr, estimate = "CV")
min_pcr = which.min(cv_pcr$val) - 1
plot(cv_pcr, main = "")
```

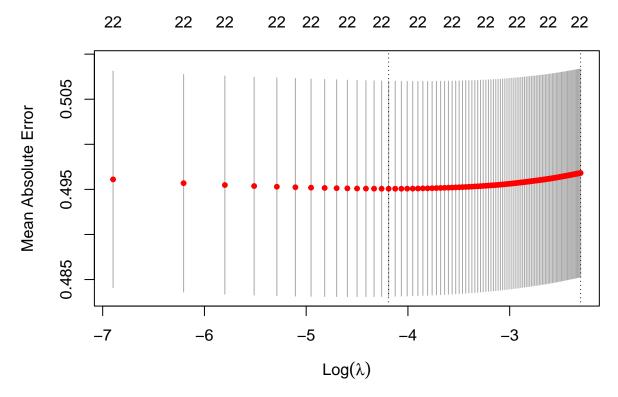


```
# 5) Partial least squares regression
set.seed(664)
lm_pls = plsr(quality ~ ., data = quadred, validation = "CV", ncomp = 22)
cv_pls = RMSEP(lm_pls, estimate = "CV")
min_pls = which.min(cv_pls$val) -1
par(mfrow = c(1,2))
coefplot(lm_pls, ncomp = min_pls, xlab = "Frequency")
plot(cv_pls, main = "")
```

quality



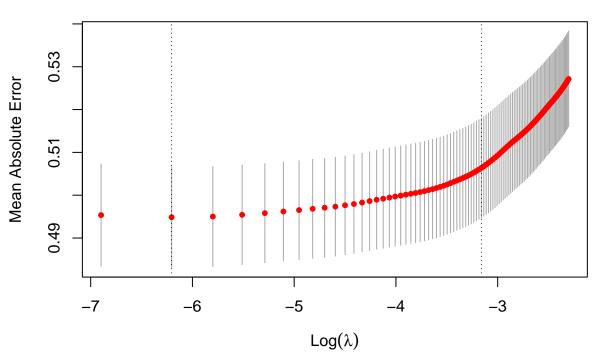




```
opt_lambda_ridge = cv_ridge$lambda.min
lm_ridge = cv_ridge$glmnet.fit

opt_lambda_ridge # optimum lambda by ridge regression
```

[1] 0.01515152



```
opt_lambda_lasso = cv_lasso$lambda.min
lm_lasso = cv_lasso$glmnet.fit
opt_lambda_lasso # optimum lambda by LASSO
```

[1] 0.002020202

```
lasso_beta = lm_lasso$beta[,which(lm_lasso$lambda == opt_lambda_lasso)]
boolCol_lasso = as.vector(lasso_beta != 0) # column selected by LASSO

# 8) comparing final model selected using AIC vs LASSO
find_hierarchical <- function(boolCol, p){
        return(c(boolCol[1:p]|boolCol[(p+1):(2*p)], T, boolCol[(p+1):(2*p)]))
}
boolCol_step = find_hierarchical(boolCol_step, 11)
boolCol_lasso = find_hierarchical(boolCol_lasso, 11)

df_step_hier = quadred[,boolCol_step]
df_lasso_hier = quadred[,boolCol_lasso]

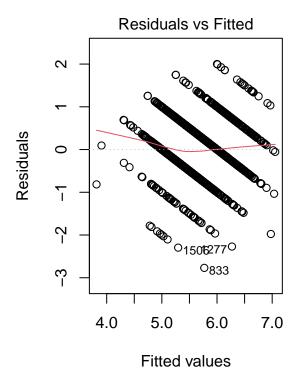
lm_step_hier = lm(quality ~., data = df_step_hier)
lm_lasso_hier = lm(quality ~., data = df_lasso_hier)

summary(lm_step_hier)</pre>
```

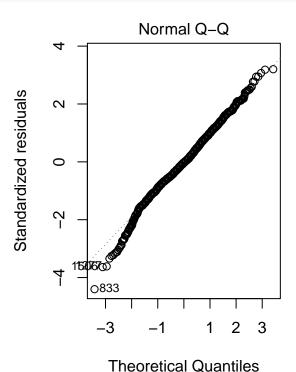
```
##
## Call:
## lm(formula = quality ~ ., data = df_step_hier)
```

```
##
## Residuals:
       Min
                 1Q Median
## -2.76915 -0.38617 -0.01881 0.42996
                                      2.00074
## Coefficients:
                        Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                       -1.103e+00 5.064e+00 -0.218 0.827688
## logFA
                       4.533e+00 1.707e+00
                                             2.656 0.007984 **
## volatile.acidity
                       -3.375e-01 3.913e-01 -0.863 0.388526
## logRS
                        9.094e-02 6.413e-02
                                             1.418 0.156382
## chlorides
                       -1.587e+00 4.019e-01 -3.948 8.23e-05 ***
                                             2.989 0.002845 **
## logFS
                        1.068e-01 3.574e-02
## total.sulfur.dioxide -6.278e-03 1.664e-03 -3.774 0.000166 ***
                       -1.022e+01 2.998e+01 -0.341 0.733337
## logDE
## pH
                        3.490e-01 3.357e+00
                                              0.104 0.917228
## logSP
                       1.077e-01 1.647e-01
                                             0.654 0.513094
## alcohol
                        2.246e-01 2.881e-02 7.798 1.13e-14 ***
## quadFA
                       -9.943e-01 3.989e-01 -2.493 0.012769 *
## quadVA
                       -4.104e-01 3.149e-01 -1.303 0.192642
## quadTS
                       1.611e-05 9.035e-06
                                             1.783 0.074830 .
## quadDE
                       7.177e+03 3.261e+03
                                             2.201 0.027864 *
                       -1.209e-01 5.035e-01 -0.240 0.810333
## quadPH
                       -1.115e+00 2.019e-01 -5.523 3.89e-08 ***
## quadSP
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.6328 on 1582 degrees of freedom
## Multiple R-squared: 0.3921, Adjusted R-squared: 0.386
## F-statistic: 63.78 on 16 and 1582 DF, p-value: < 2.2e-16
summary(lm_lasso_hier)
##
## Call:
## lm(formula = quality ~ ., data = df_lasso_hier)
##
## Residuals:
##
       Min
                 1Q
                    Median
                                   3Q
## -2.78658 -0.37651 -0.02757 0.43257 2.00030
## Coefficients:
##
                         Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                       -2.917e+00 5.002e+00 -0.583 0.559866
## logFA
                        3.900e-01 2.315e-01
                                              1.685 0.092263
## volatile.acidity
                       -5.387e-01 4.194e-01 -1.285 0.199112
## citric.acid
                       -1.861e-01 1.472e-01
                                             -1.264 0.206362
## logRS
                       1.010e-01 6.416e-02
                                             1.575 0.115567
## chlorides
                       -1.331e+00 4.132e-01 -3.222 0.001300 **
                        1.016e-01 3.612e-02
## logFS
                                             2.814 0.004955 **
## total.sulfur.dioxide -6.087e-03 1.678e-03 -3.627 0.000296 ***
## logDE
                       -3.633e+01 2.802e+01 -1.297 0.194940
## pH
                        4.095e+00 2.951e+00 1.388 0.165420
                        1.411e-01 1.642e-01 0.859 0.390476
## logSP
```

```
## alcohol
                         2.240e-01
                                    2.916e-02
                                                7.682 2.72e-14 ***
## quadVA
                        -2.985e-01
                                    3.231e-01 -0.924 0.355720
## quadTS
                         1.722e-05
                                    9.035e-06
                                                1.906 0.056895 .
## quadDE
                                    2.984e+03
                                                1.231 0.218321
                         3.675e+03
                                               -1.561 0.118719
## quadPH
                        -6.893e-01
                                    4.415e-01
## quadSP
                        -1.075e+00
                                    2.013e-01
                                               -5.341 1.06e-07 ***
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.6337 on 1582 degrees of freedom
## Multiple R-squared: 0.3903, Adjusted R-squared: 0.3842
## F-statistic: 63.31 on 16 and 1582 DF, p-value: < 2.2e-16
comp_AIC = rbind(comp_AIC, c("quad_step", round(AIC(lm_step_hier), 3)))
comp_AIC = rbind(comp_AIC, c("quad_lasso", round(AIC(lm_lasso_hier), 3)))
comp_AIC
##
                     AIC
             lm
## 1
           Ori. 3164.277
           Log. 3154.79
## 2
## 3
         Trans.
                  3127.7
## 4
         Logit. 3146.288
## 5
     quad step 3093.325
## 6 quad_lasso 3097.98
par(mfrow = c(1, 2))
plot(lm_step_hier, which = 1)
```



plot(lm_step_hier, which = 2)

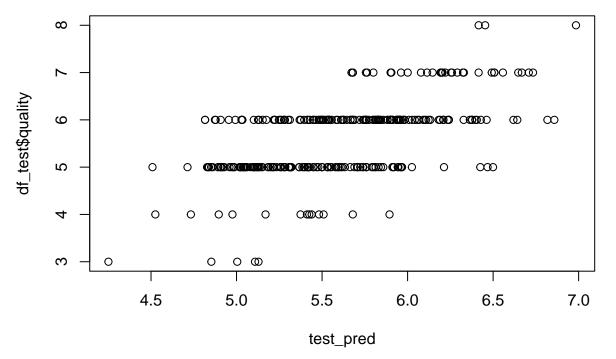


```
par(mfrow = c(1, 1))
```

4. Estimation of Error

```
df_final = df_step_hier
n = nrow(df_final)
df_train = df_final[(1:n)%%5 != 0,]
df_test = df_final[(1:n)%%5 == 0,]

lm_train = lm(quality ~ ., data = df_train)
test_pred = predict(lm_train, df_test)
plot(test_pred, df_test$quality)
```



mean((test_pred-df_test\$quality)^2)

```
## [1] 0.4533842
```

```
mean((test_pred-df_test$quality)^2) - 1/12
```

[1] 0.3700508

table(round(test_pred), df_test\$quality)

```
##
##
        3
           4
              5
                 6
##
           0
              0
     5
        4 10 79 41
                       0
##
                    0
##
        0
           3 45 94 28
        0 0
             0
                4
                   7
##
```

```
lm_final = lm(quality ~ ., data = df_final)
table(round(predict(lm_final, data = df_final)), df_final$quality)
##
##
        3
          4
               5 6
##
    4
        1
           3
               5 0
                          0
    5
       8 34 468 170
                          0
##
##
    6
       1 16 207 441 140
                          9
##
          0
               1 27 53
5. Weighted Least Squares for imbalanced data
wt1 = 1/sqrt(table(df_train$quality))
wts1 = wt1[df_train$quality-2]
wt2 = 1/table(df_train$quality)
wts2 = wt2[df_train$quality-2]
lm_train = lm(quality~., data = df_train)
table(round(predict(lm_train, newdata = df_test)), df_test$quality)
##
##
       3 4 5 6 7
##
    4 1 0 0 0 0 0
##
    5 4 10 79 41 0 0
    6 0 3 45 94 28 2
##
    7 0 0 0 4 7 1
lm_wt1 = lm(quality~., data = df_train, weights = wts1)
table(round(predict(lm_wt1, newdata = df_test)), df_test$quality)
##
##
       3 4 5 6 7
    3 1 0 0 0 0
##
##
    4 1 3 3 2 0
    5 3 7 79 46 0 0
##
    6 0 3 39 77 19 0
    7 0 0 3 14 16 2
##
    8 0 0 0 0 0 1
lm_wt2 = lm(quality~., data = df_train, weights = wts2)
table(round(predict(lm_wt2, newdata = df_test)), df_test$quality)
##
##
       3 4 5 6 7 8
    3 2 1 1 0 0
##
##
    4 2 3 34 13 0 0
    5 1 7 54 45 5 0
##
    6 0 2 29 58 12 0
##
```

7 0 0 6 18 16 2

8 0 0 0 5 2 1

##

##