

1.6

Exercise 4

(a)

p: Kangaroos live in Australia

q: Kangaroos are marsupials

$$\frac{q \wedge p}{\therefore q}$$

(b)

p: it is hotter than 100 today.

q: the pollution is dangerous.

$$\frac{p \vee q \quad \neg q}{\therefore p}$$

(c)

p: Linda is an excellent swimmer.

q: Linda can work as a lifeguard.

$$\frac{p \quad p \rightarrow q}{\therefore q}$$

(d)

p: Steve will work at a computer company this summer.

q: He will be a beach bum.

$$\frac{p}{\therefore p \vee q}$$

(e)

p: I work all night on this homework.

q: I can answer all the exercise.

r: I will understand the material.

$$\frac{p \rightarrow q \quad q \rightarrow r}{\therefore p \rightarrow r}$$

Exercise 24

$\forall x(P(x) \vee Q(x))$ is true so $\forall xP(x) \vee Q(x)$ is true

following the step 1, I can get premise is $\forall x(P(x) \vee Q(x))$

use universal instantiation get $P(c) \vee Q(c)$

and then we can get the step 3 is error, if the step 3 is error the step 5 also is error too.

and the step 7 conjunction should be \wedge

answer: the step 3,5 and 7 are error.

1.7

Exercise 6

let use x and y to be two odd integers.

$$x=2m+1$$

$$y=2n+1$$

$$x*y=(2m+1)*(2n+1)$$

$$=4mn+2m+2n+1$$

$$=2(2mn+m+n)+1$$

$$x*y=2z+1 (z \text{ is a even integers})$$

so product two odd number is odd.

Exercise 20

(1)

if $3n+2$ is even integer then n is even.

so we can get $p \rightarrow q$ and $\neg q \rightarrow \neg p$

p : n and $3n+2$ is even

$\neg p$: $3n+2$ are not even

q : n is even

$\neg q$: n is odd

(2)

if n is odd that meaning $n=2x+1$

$$3n+2=3(2x+1)+2$$

$$=6x+3+2$$

$$=6x+5$$

$$=6x+4+1$$

$$=2(3x+2)+1 \text{ is odd}$$

so $(3n+2)$ is odd, so if $(3n+2)$ is even the n must be even.

1.8

Exercise 6

$$\min(a, \min(b, c)) = \min(\min(a, b), c)$$

(1)

$a \leq \min(b, c)$ if a is the smallest $a \leq b$ or $a \leq c$

$$\min(a, b) = a$$

$$\min(\min(a, b), c) = \min(a, c) = a$$

(2)

if $b \leq a$ and $b \leq \min(b, c)$

$a \leq b$ or $a \leq c$

$$\min(a, b) = b$$

$$\min(\min(a, b), c) = \min(b, c) = b$$

(c)

c is same with a and b the $\min(a, \min(b, c)) = \min(\min(a, b), c)$

just depend on the which one number is smallest.

Exercise 20

$$x < r < x + 1$$

$$|x - r| < 1/2 \text{ or } |(x + 1) - r| < 1/2$$

if $|x - r| < 1/2$, we can choose $n = x$

if $|(x + 1) - r| < 1/2$ we can choose $n = x + 1$

$$|r - y| < 1/2$$

$$|n - y| \leq |n - r| + |r - y| = |n - r| + |y - r| = 1/2 + 1/2 = 1$$

$$n = y$$

so r is an irrational number and less than $1/2$ with n