initial system:

$$\frac{ \sqcap \Gamma}{\Gamma \vdash Q} \text{ (empty)} \quad \frac{ \sqcap \Gamma}{\Gamma \vdash \Pi_i : \Pi_{i+1}} \text{ (univ)} \quad \frac{\Gamma \vdash A : \Pi_i}{\Gamma \vdash A : \Pi_{i+1}} \text{ (hier)}$$
 
$$\frac{ \Gamma \vdash A : \Pi_i}{\sqcap \Gamma_i \Gamma_i X : A} \text{ (ext)} \quad \frac{ \sqcap \Gamma_i \Gamma_i X : A}{\Gamma_i \Gamma_i X : A \vdash X : A} \text{ (var)}$$
 
$$\frac{ \Gamma \vdash A : \Pi_i}{\Gamma \vdash \Pi(x : A) \cdot B : \Pi_i} \text{ ($\Pi$)}$$
 
$$\frac{ \Gamma \vdash A : \Pi_i}{\Gamma \vdash \Pi(x : A) \cdot B} \text{ ($\Pi$)} \quad \frac{ \Gamma \vdash e_1 : \Pi(x : A) \cdot B}{\Gamma \vdash e_1 \otimes e_2 : B[e_1/x]} \text{ ($\Pi$)}$$
 
$$\frac{ \Gamma \vdash A : \Pi_i}{\Gamma \vdash A : \Pi_i} \text{ ($\Gamma$)} \quad \frac{ \Gamma \vdash e_1 : \Pi(x : A) \cdot B}{\Gamma \vdash e_1 \otimes e_2 : B[e_1/x]} \text{ ($\Pi$)}$$
 
$$\frac{ \Gamma \vdash A : \Pi_i}{\Gamma \vdash A : \Pi_i} \text{ ($\Gamma$)} \quad \frac{ \Gamma \vdash e_1 : A \vdash B : \Pi_i}{\Gamma \vdash (e_1, \dots, e_n) : \Sigma(x_1 : A_1, \dots, x_{n-1} : A_{n-1}) \cdot A_n} \text{ ($\Sigma$)}$$
 
$$\frac{ \Gamma \vdash e_1 : \Delta(x_1 : A_1, \dots, x_{n-1} : A_{n-1}) \cdot A_n}{\Gamma \vdash (e_1, \dots, e_n) : \Sigma(x_1 : A_1, \dots, x_{n-1} : A_{n-1}) \cdot A_n} \text{ ($\Sigma$)}$$
 
$$\frac{ \Gamma \vdash e_1 : \Sigma(x_1 : A_1, \dots, x_{n-1} : A_{n-1}) \cdot A_n}{\Gamma \vdash \text{let } (x_1, \dots, x_n)} = e_1 \text{ in } e_2 : B[e_1/z]} \text{ ($\Sigma$e)}$$
 
$$\frac{ \Gamma \vdash e_1 : \Delta(x_1 : A_1, \dots, x_{n-1} : A_{n-1}) \cdot A_n}{\Gamma \vdash \text{rec } x \cdot e : A} \text{ (rec)} \qquad \frac{ \Gamma \vdash e_1 : A_c}{\Gamma \vdash e_1 : A_c} \text{ (constant)}$$

modal:

$$P ::= x \mid \Sigma(x_1 : N_1, \dots, x_n : N_n). M \mid \downarrow N$$
  
$$N ::= \Pi(x : N). M \mid \uparrow P$$