

# BANGLADESH UNIVERSITY OF ENGINEERING AND TECHNOLOGY



## DEPARTMENT OF ELECTRICAL AND ELECTRONIC ENGINEERING

### Project Report

**Course No :** EEE 318

**Section :** A

**Course Title :** Control System I Laboratory

**Project Title:** Analysis of the control system described in the publication titled “Variable-gain control for respiratory systems”

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Using these values:

$$A_h = -5.4430, B_h = 5.0633$$

$$C_h = \begin{bmatrix} 0.4557 \\ -108.8608 \end{bmatrix}, D_h = \begin{bmatrix} 0.5063 \\ 101.2658 \end{bmatrix}$$

Hence, from (1), transfer function of respiratory system:

$$H(s) = \begin{bmatrix} \frac{0.5063s + 5.063}{s + 5.443} \\ \frac{101.3s}{s + 5.443} \end{bmatrix}$$

$$\text{Where, } H_1(s) = \frac{0.5063s + 5.063}{s + 5.443}, \text{ and } H_2(s) = \frac{101.3s}{s + 5.443}$$

We can also calculate the transfer function of blower:

$$B(s) = \frac{3.553 \times 10^4}{s^2 + 377s + 3.553 \times 10^4}$$

## Task 2: Determination the overall transfer function of the system shown in Fig. 4

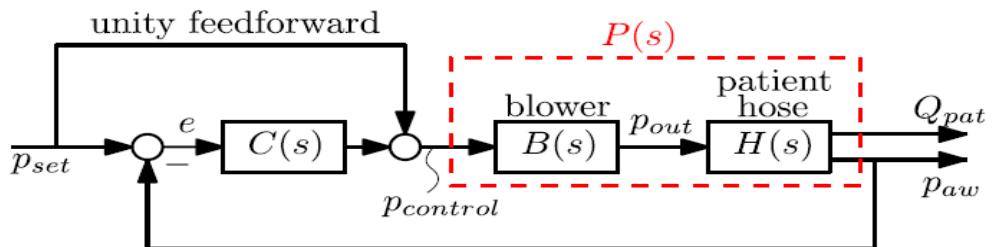
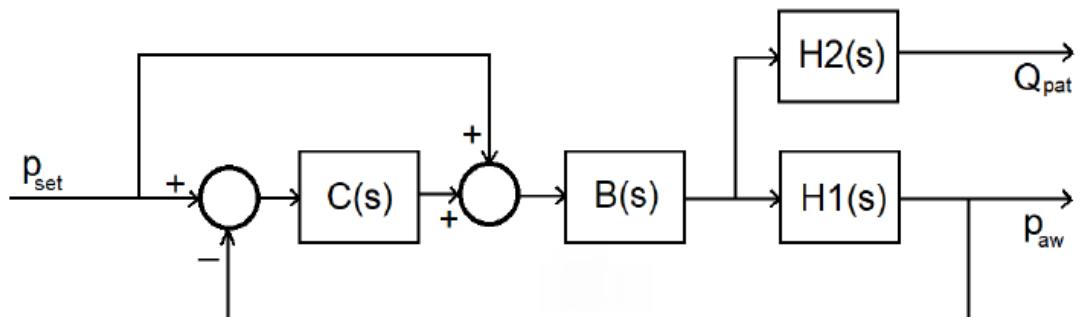


Fig. 4. Closed-loop control scheme with a linear controller  $C(s)$ .

Redrawing the flow diagram, we get:



We use Mason's rule to determine the transfer functions. Again, there is a integral controller, hence,  $C(s) = \frac{1}{s}$

Again, let,  $P1(s) = B(s)H1(s)$  and  $P2(s) = B(s)H2(s)$

$$\text{After calculation, } P1(s) = \frac{1.799 \times 10^4 s + 1.799 \times 10^5}{s^3 + 382.4s^2 + 3.758 \times 10^4 s + 1.934 \times 10^5}$$

$$\text{And, } P2(s) = \frac{3.598 \times 10^6 s}{s^3 + 382.4s^2 + 3.758 \times 10^4 s + 1.934 \times 10^5}$$

$$1. \text{ Here, } T_{aw}(s) = \frac{P_{aw}(s)}{P_{set}(s)}$$

$$\text{Finally we find, } T_{aw}(s) = \frac{[1+C(s)]P1(s)}{1+C(s)P1(s)}$$

$$\text{So, } T_{aw}(s) = \frac{1.799 \times 10^4 s^2 + 1.979 \times 10^5 s + 1.799 \times 10^5}{s^4 + 382.4s^3 + 3.758 \times 10^4 s^2 + 2.114 \times 10^5 s + 1.799 \times 10^5}$$

$$2. 1. \text{ Here, } T_{pat}(s) = \frac{Q_{pat}(s)}{P_{set}(s)}$$

$$\text{Finally we find, } T_{aw}(s) = \frac{[1+C(s)]P2(s)}{1+C(s)P1(s)}$$

$$\text{So, } T_{pat}(s) = \frac{3.598 \times 10^6 s^2 + 3.598 \times 10^6 s}{s^4 + 382.4s^3 + 3.758 \times 10^4 s^2 + 2.114 \times 10^5 s + 1.799 \times 10^5}$$

### Task 3: Sketch the root locus of in Figure 4 for $0 < \omega < \infty$ of the integral controller $C(s)$

We found the transfer functions for  $T_{aw}(s)$  and  $T_{pat}(s)$  in the previous task. Since the denominator for the two transfer functions are the same, the root locus will be same.  $T_{aw}(s)$  and  $T_{pat}(s)$  are represented by  $T1(s)$  and  $T2(s)$  respectively. The root locus is shown below using **rlocus()** function in MATLAB:

```
clc;
clear all;
close all;
% arbitrary variables taken from table 1
R_lung = 5/1000;
C_lung = 20;
R_leak = 60/1000;
R_hose = 4.5/1000;
W = 2*pi*30;
zeta = 1;
```

```

% variables from equations 9
A_h = (-1)*((1/R_hose)+(1/R_leak))/(R_lung*C_lung*(1/R_lung + 1/R_hose +
1/R_leak));
B_h = (1/R_hose)/(R_lung*C_lung*(1/R_lung + 1/R_hose + 1/R_leak));
C_h = transpose([(1/R_lung)/(1/R_lung + 1/R_hose + 1/R_leak) , (-1/R_hose -
1/R_leak)/(R_lung*(1/R_lung + 1/R_hose + 1/R_leak))]);
D_h = transpose([(1/R_hose)/(1/R_lung + 1/R_hose +
1/R_leak), (1/R_hose)/(R_lung*(1/R_lung + 1/R_hose + 1/R_leak))]);

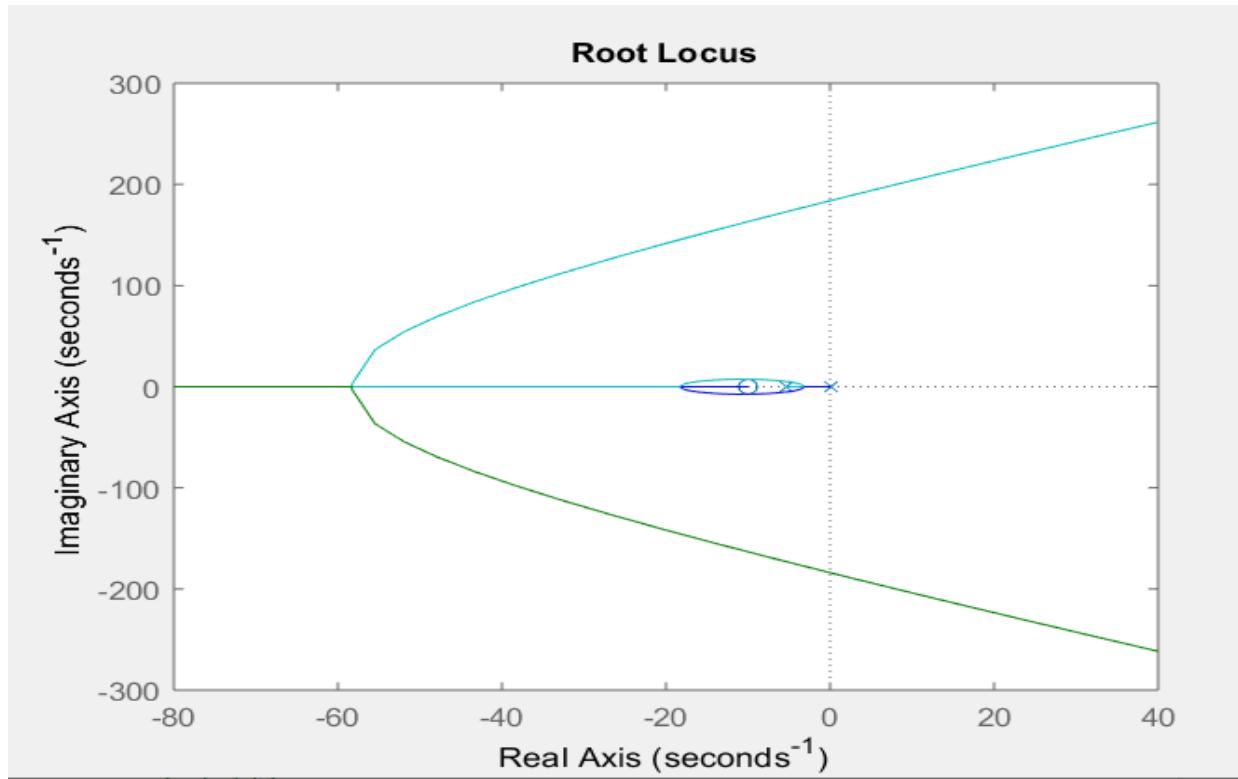
%Patient hose transfer function
s=tf('s');
H = C_h*((s*eye(1)-A_h)^-1)*B_h + D_h

B= (W^2) / (s^2+2*zeta*W*s+W^2)
P = B*H
C = 1/s;

T1 = minreal((P(1)+P(1)*C)/(1+P(1)*C))
T2 = minreal((P(2)+P(2)*C)/(1+P(1)*C))

rlocus(P(1)/s,0:0.01:1000)
sgrid(1,0)
axis([-80 40 -300 300])

```



## Task 4: Reproducing Fig.7 results and discussion on the necessity of both feedback and feed-forward control

The expected results are (according to the paper),

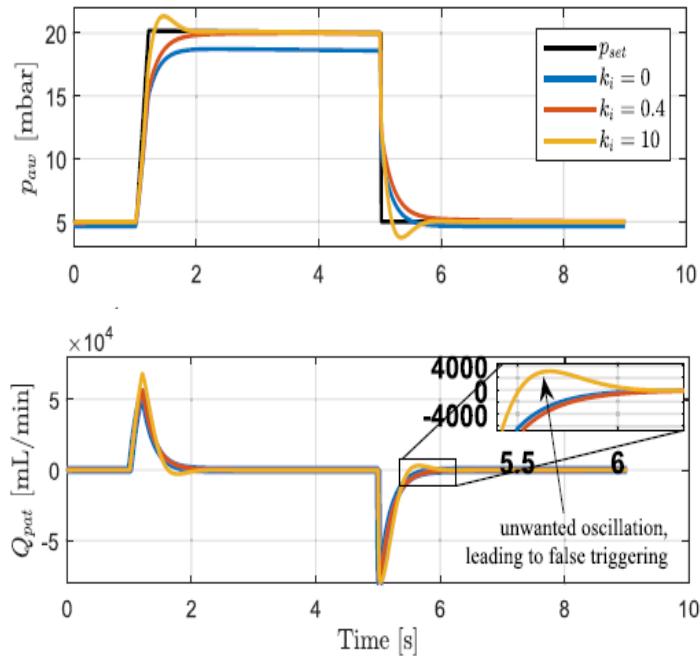


Figure: Simulation result of the closed-loop system using no controller, a low-gain controller ( $k_i = 0.4$ ), and a high-gain controller ( $k_i = 10$ ).

We have used SIMULINK to design the system.

The observations from the above two figures are:

1. The input  $P_{set}(s)$  starts from 5 mbar and is limited to 20 mbar.
2. The input  $P_{set}(s)$  is not exactly a pulse with infinite slopes.
3. The upward slope has finite (very high) magnitude but the downward slope is of infinite value.

We used ramp and step functions to generate our required  $P_{set}(s)$ . To simplify the problem and mitigate some transient errors, we kept  $P_{set}(s)$  between 0-15 instead of 5-20 mbar. The finally chosen  $P_{set}(s)$  is:

$$64.865[r(t-1)-r(t-1.23125)] - 15u(t-5) \leftrightarrow \frac{64.865}{s^2} [e^{-s} - e^{-1.23125s}] - \frac{15e^{-5s}}{s}$$

For each value of (0,0.4,10), a separate block diagram is made. As zero gain is not feasible in real application, we used very small value 0.0001 instead of 0.

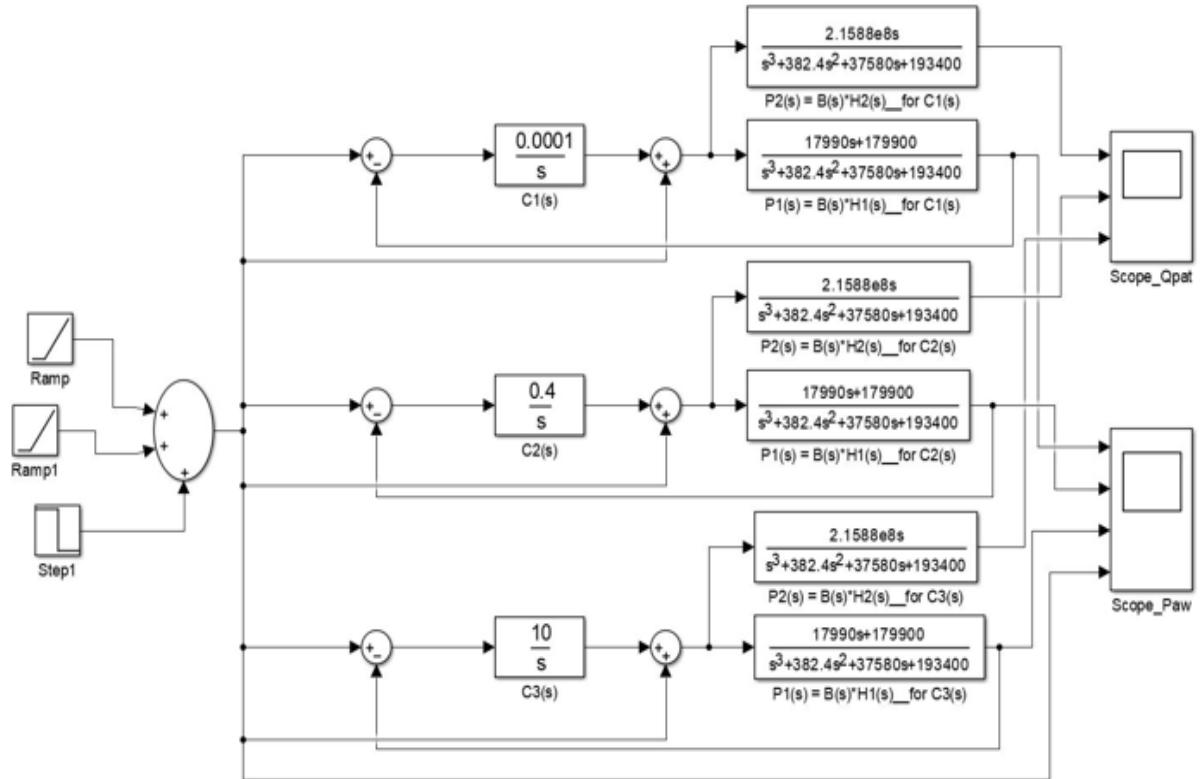
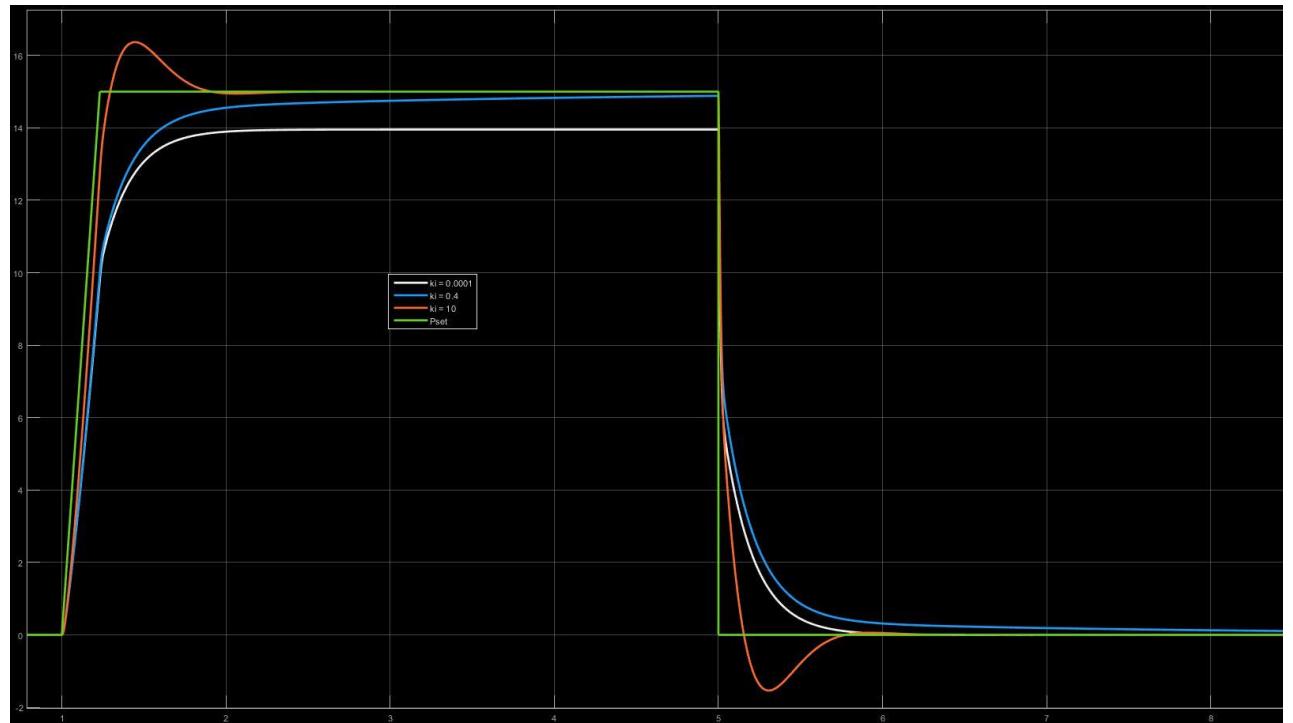
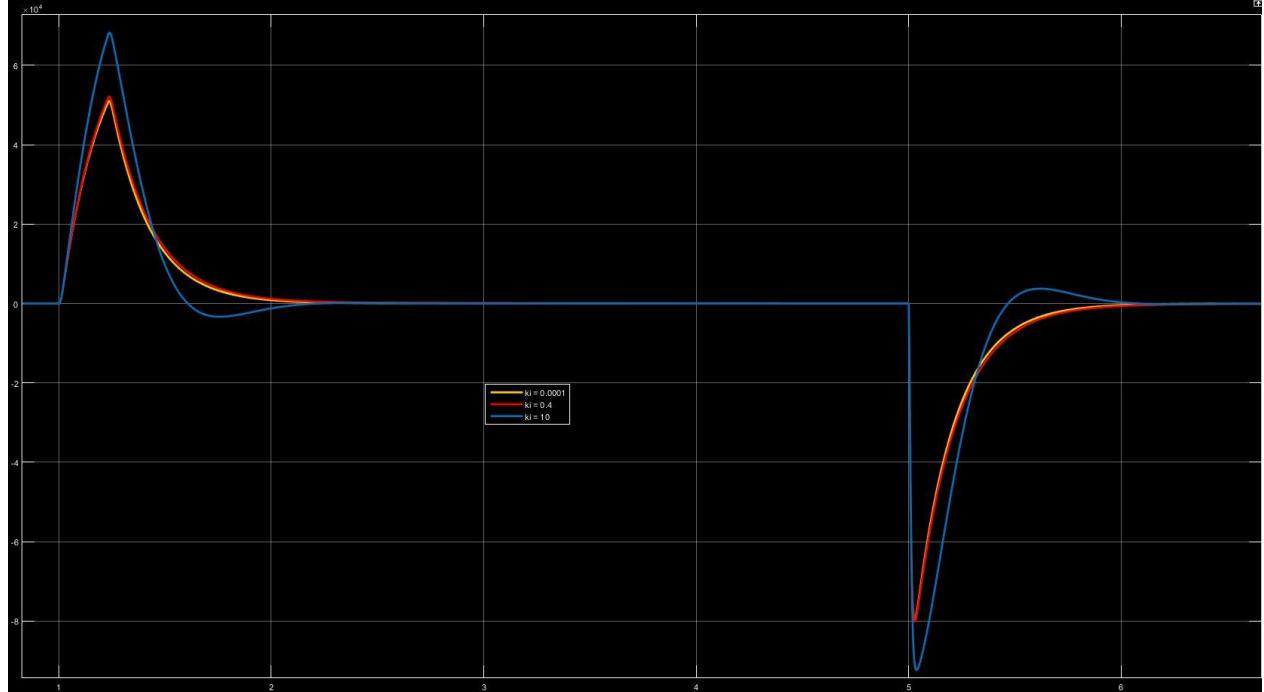


Figure: SIMULINK diagram for the given systems

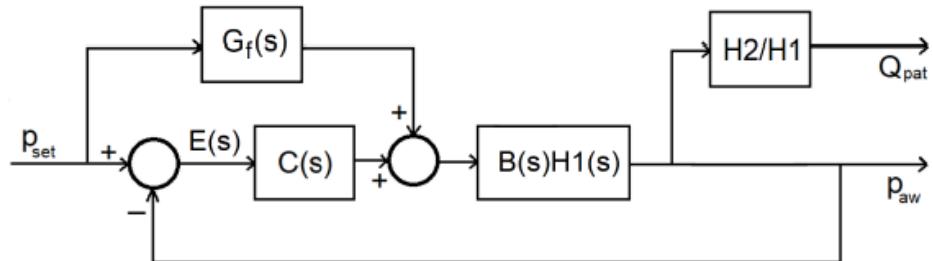
### Output for Scope\_Paw:



## Output for Scope\_Qpat:



## Necessity of both feed-forward and feedback systems:



From Task 2, we found:

$$T_{aw}(s) = \frac{P_{aw}(s)}{P_{set}(s)} = \frac{[1+C(s)]P_1(s)}{1+C(s)P_1(s)}$$

Here, we used a feed-forward system with gain  $G_f$ . Hence, the modified system:

$$T_{aw}(s) = \frac{P_{aw}(s)}{P_{set}(s)} = \frac{[G_f(s)+C(s)]P_1(s)}{1+C(s)P_1(s)}$$

Hence,  $e(s) = P_{set}(s) - P_{aw}(s) = P_{set}(s) \left[ 1 - \frac{(G_f(s)+C(s))P_1(s)}{1+C(s)P_1(s)} \right]$

So,  $e(s) = P_{set}(s) \left[ \frac{1-G_f(s)P_1(s)}{1+C(s)P_1(s)} \right] \dots \dots \dots \quad (2)$

For a steady state errorless system,

$$e(\infty) = \lim_{s \rightarrow \infty} sE(s) = 0$$

$$e(\infty) = \lim_{s \rightarrow \infty} sP_{set}(s) \frac{1 - Gf(s)P_1(s)}{1 + C(s)P_1(s)} = 0 \quad \text{so, } [1 - Gf(s)P_1(s)] \lim_{s \rightarrow \infty} \frac{sP_{set}(s)}{1 + C(s)P_1(s)} = 0$$

The plant provides a non-zero error. Hence, the required condition:

$$[1 - Gf(0)P_1(0)] = 0 \quad \text{so, } Gf(0) = \frac{1}{P_1(0)}$$

$$\text{Now, } P_1(0) = B(0)H_1(0)$$

$$B(0) = \left. \frac{\omega_n^2}{s^2 + 2\xi\omega_n s + \omega_n^2} \right|_{s=0} = 1$$

$$\text{And, } H_1(0) = \frac{179900}{193400} = 0.9302$$

$$\text{Therefore, } Gf(0) = \frac{1}{0.9302} = 1.075$$

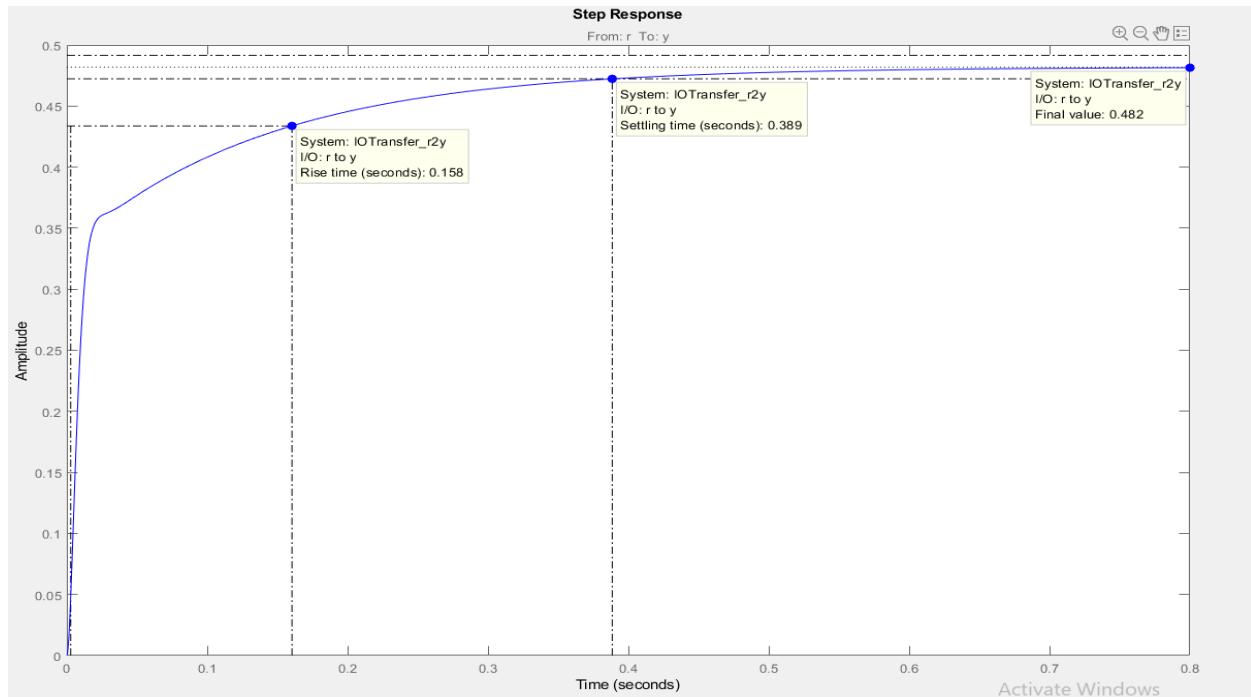
In this paper,  $Gf(0) = 1$ , which is very near to our new calculated gain. So the feed forward system is very much acceptable.

Therefore, a feed-forward system reduces steady state error if set properly.

The feedback introduces an error value between the input and output to the system which can control the response of the system. The system's response moves faster or slower based on the plant and controller, but the error makes the output follow the input set value. Without the feedback, the output may go out of bounds or become unstable as it cannot get any information or correction based on how it is performing.

## Task 5: Preference amongst pure integral, PI and lag controller

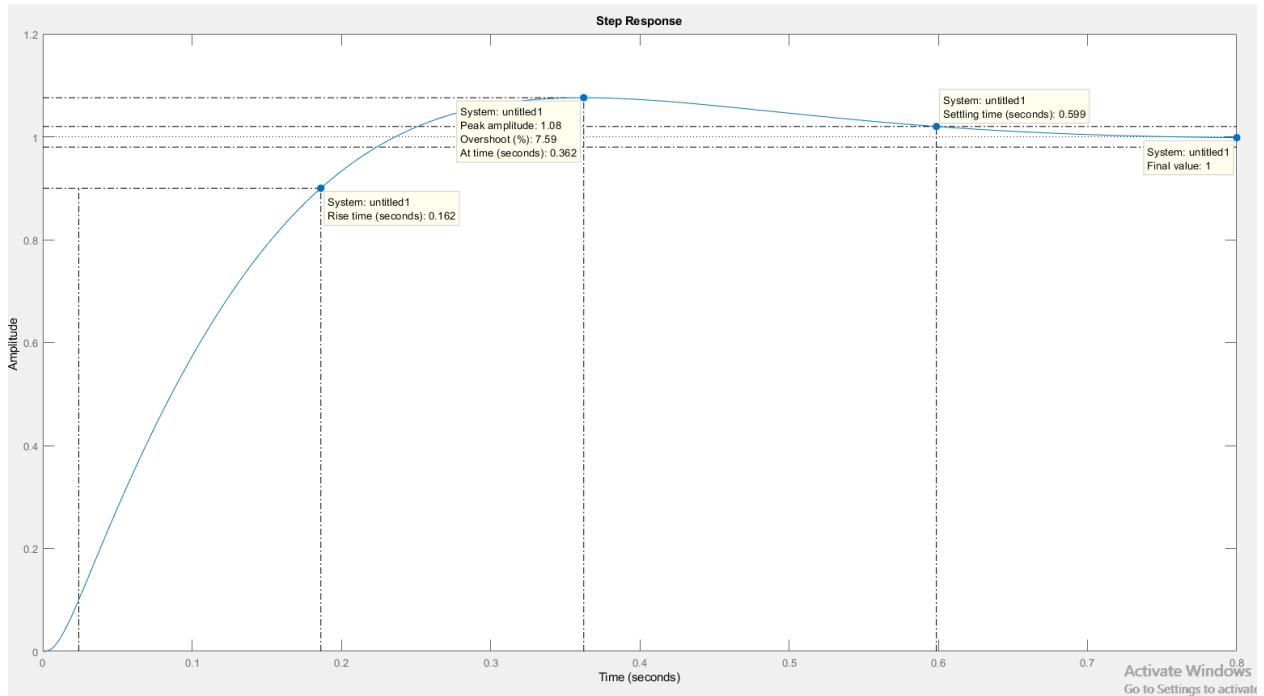
Step response characteristics for no controller



High steady state error can be observed.

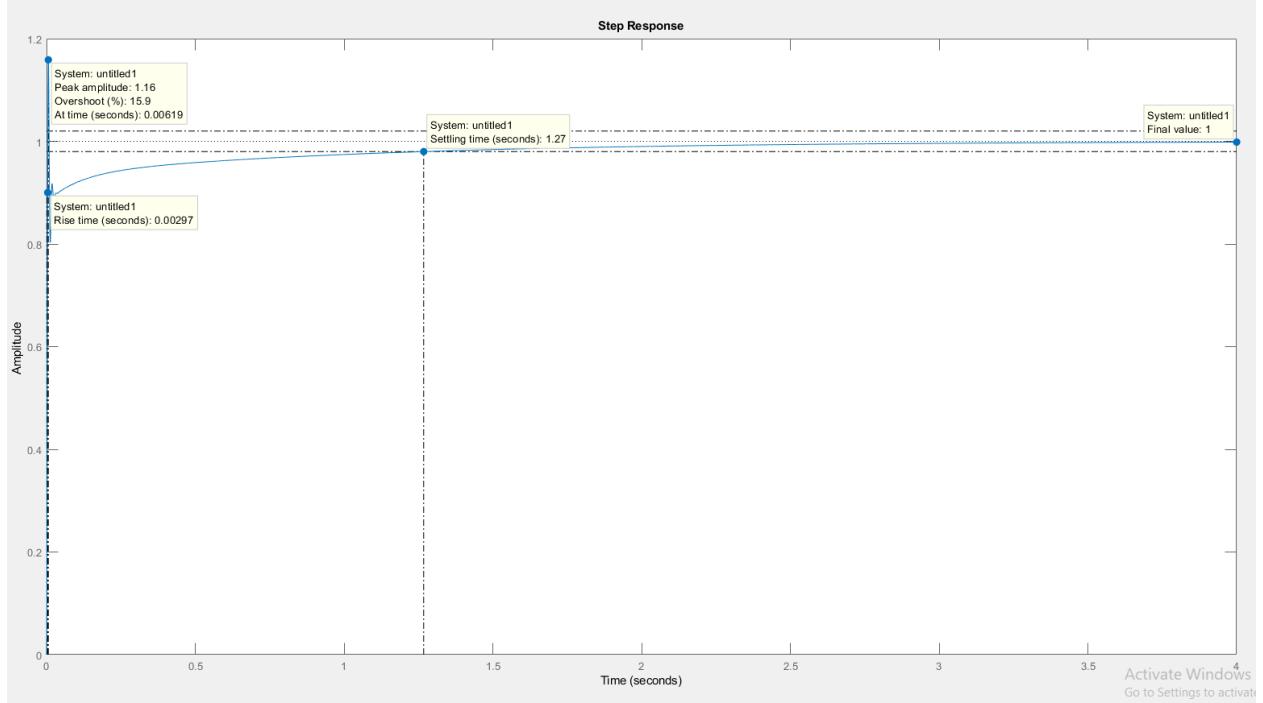
Now, the performance of a Pure integral controller was evaluated. Taking controller 14/s

the following step response was determined



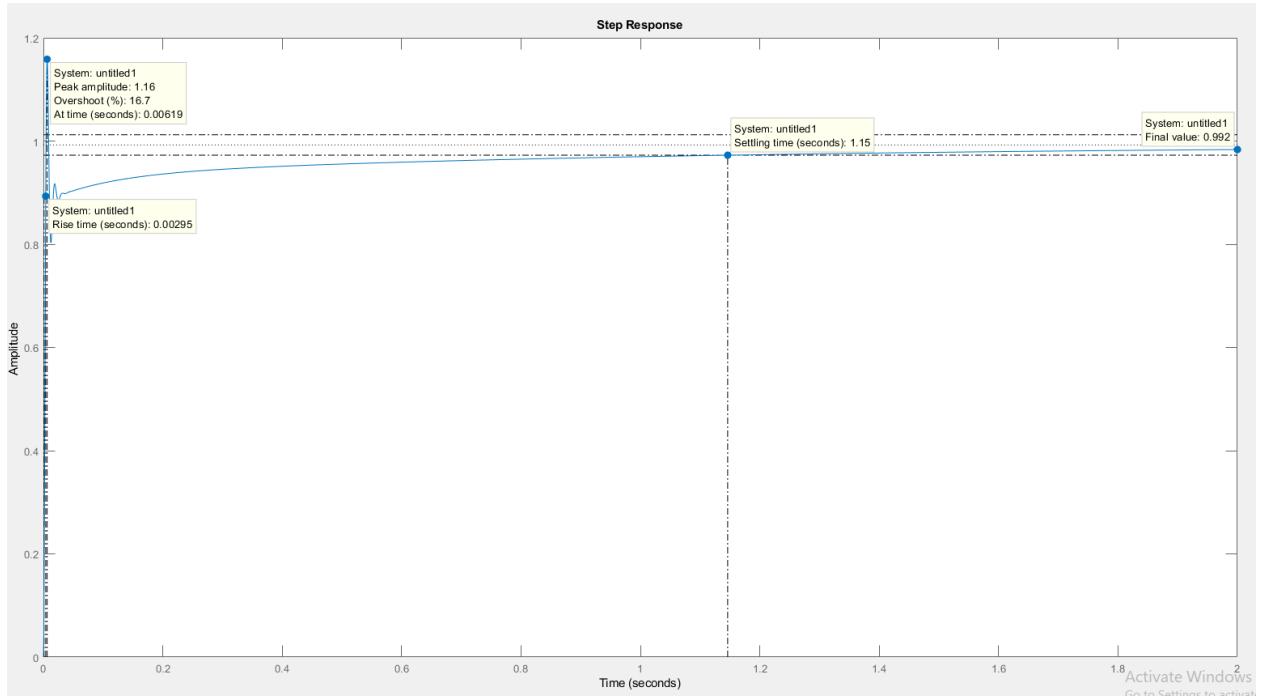
Here, it can be observed that the percentage overshoot has decreased a lot and the rise time and steady state error is optimum.

For further comparison, a PI controller  $14(s+1)/s$  was implemented and the following step response was obtained



Here, it can be seen that, although the rise time has reduced a lot, the overshoot has increased and the settling time has increased.

Finally, for comparison. a lag controller  $14(s+1)/(s+0.1)$  was implemented and the step response was visualized



Here, it can be seen that the overshoot percentage and rise time both exceed the optimum range.

Among all the controllers, the Pure Integral controller performs better for the given conditions.

### **Task 6: Designing a linear controller to meet the requirements in page-166 (column 1 & 2)**

We need to find the boundary of the linear controller gain in order to meet the specifications.

For type-0 system:

$$\text{The steady state error} = \frac{1}{1 + \lim_{s \rightarrow 0} G(s)} = \frac{1}{1 + K P_1(0)} = \frac{1}{1 + 0.9302K}$$

From the paper:

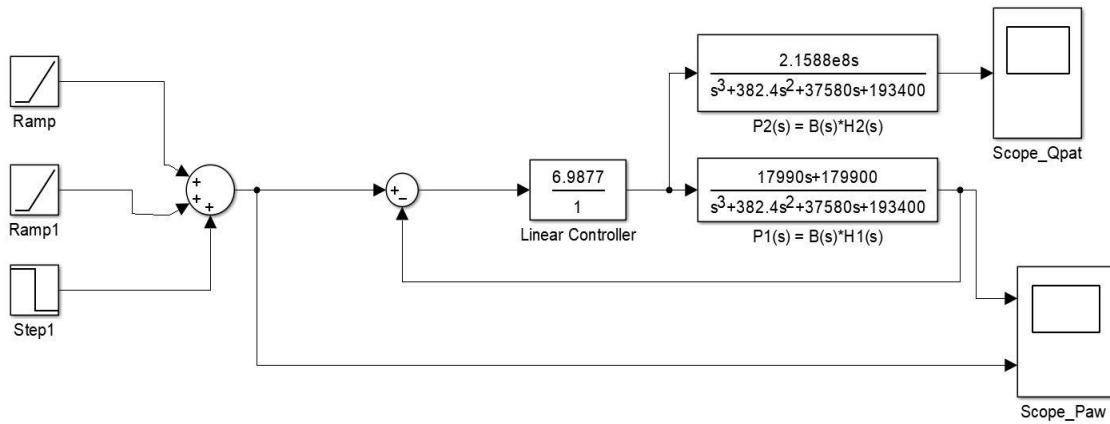
The goal of the pressure controller is to achieve sufficiently fast pressure buildup and accurate tracking of the desired pressure profile  $P_{set}$  while simultaneously not introducing the oscillations in the flow signal, which may result in false triggers of the inhalation cycle. Quantitatively, these specifications can be formulated as follows,

- 1) The rise time from 10% to 90% of a pressure set point should be approximately 200 ms.
- 2) The pressure at the end of an inspiration, the so-called plateau pressure, should be within a pressure band of  $\pm 2$  mbar of the pressure set point.
- 3) The overshoot in the flow during an expiration should be below the triggering value set by the clinician, and a typical value is 2 L/min.

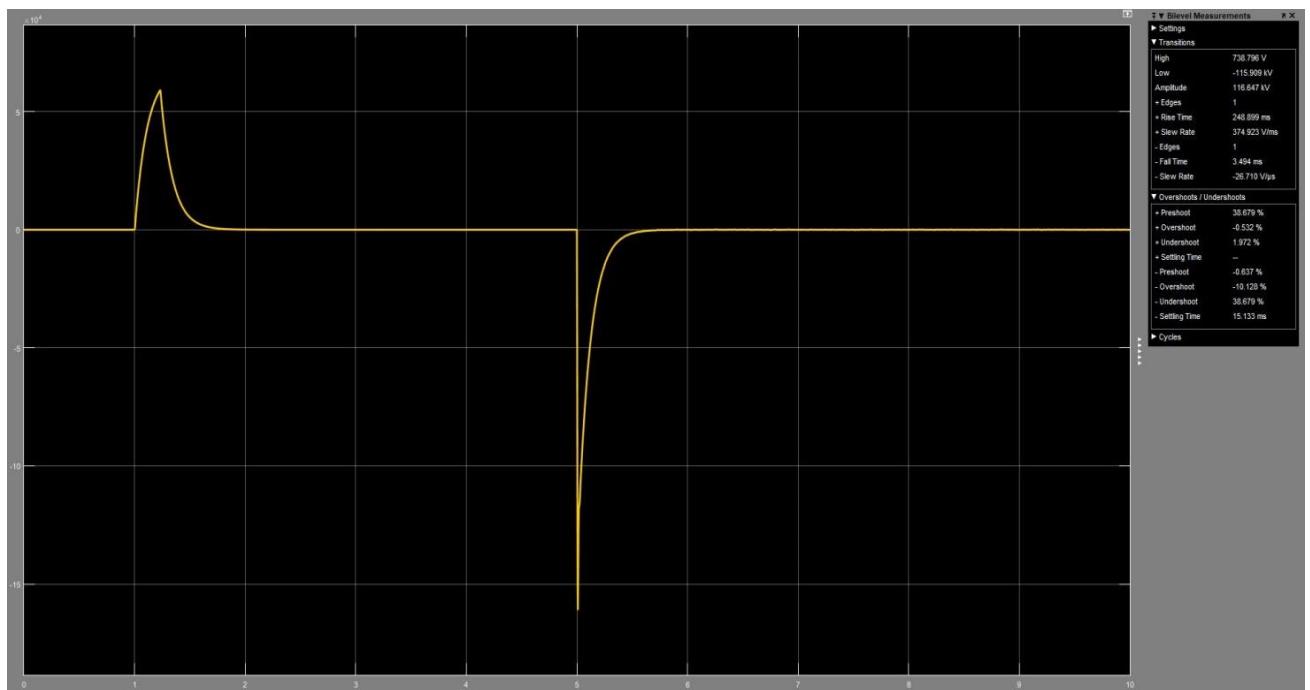
Hence, the pressure has to be  $15 \pm 2$  mbar. We used the settling value =  $15 - 2 = 13$  mbar.

$$\text{Hence, the steady state error} = \frac{1}{1 + 0.9302K} = \frac{2}{15}$$

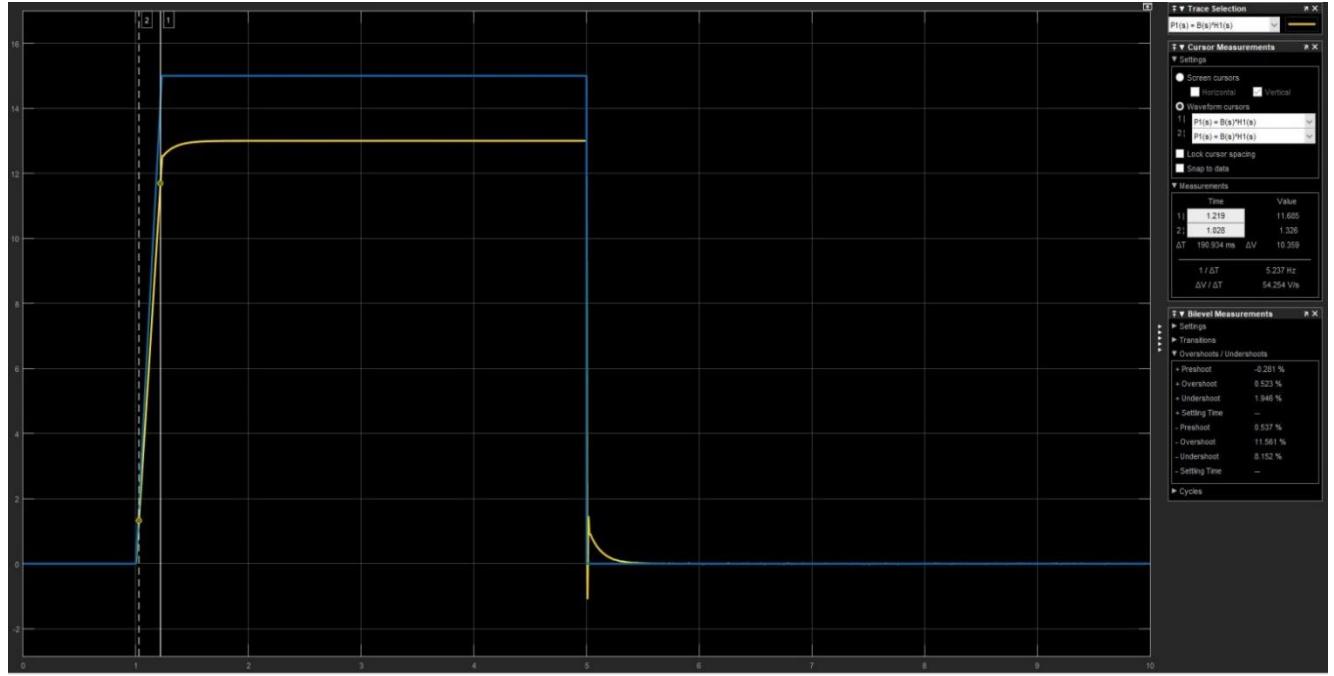
Solving,  $K = 6.9877$



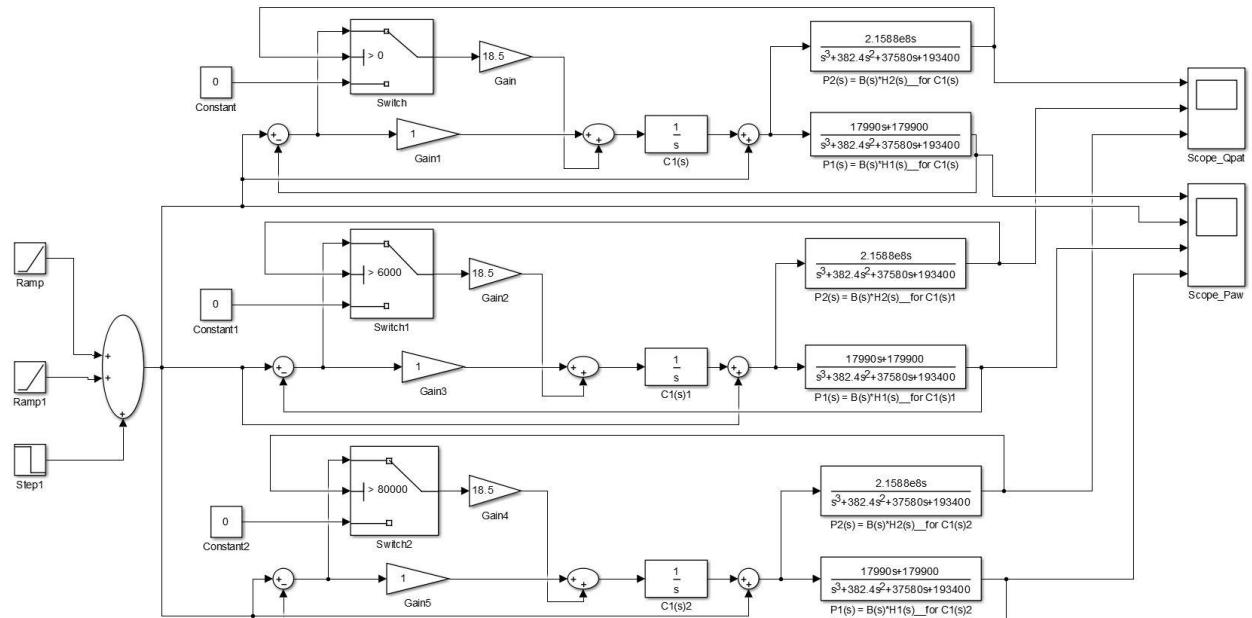
## Output at Scope\_Qpat:



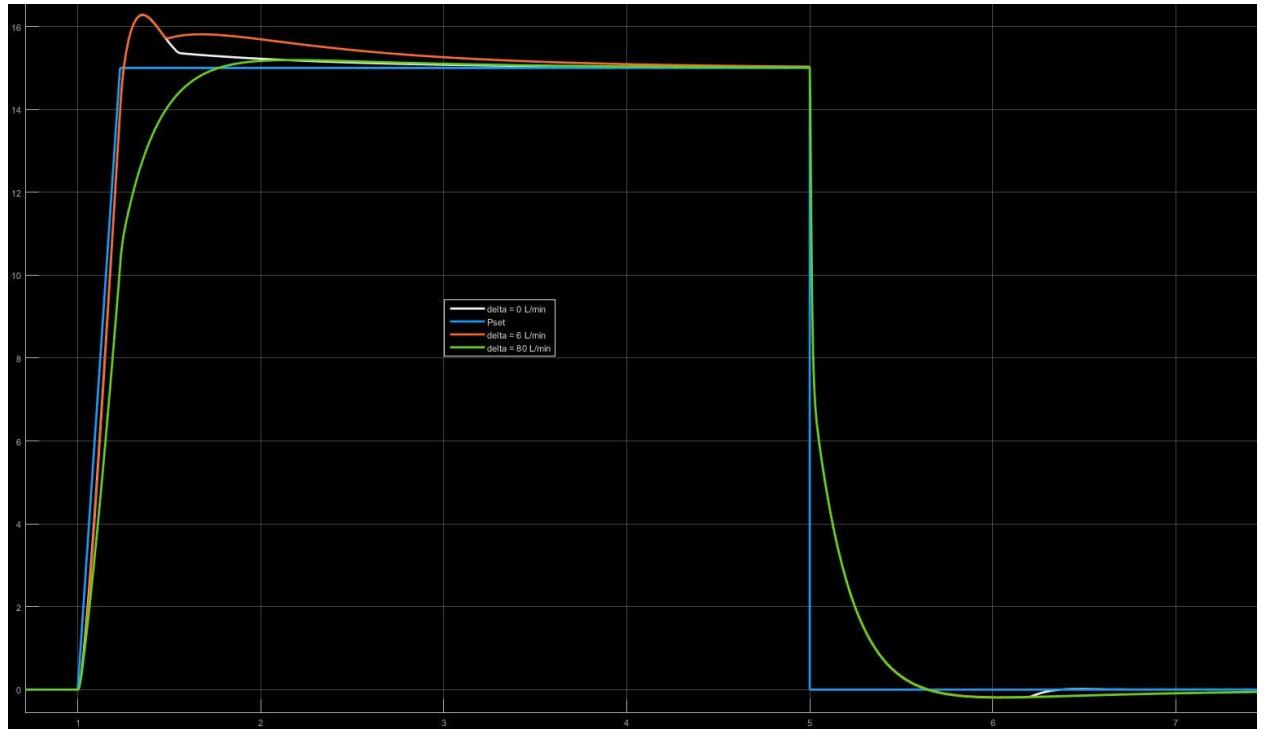
## Output at Scope\_Paw:



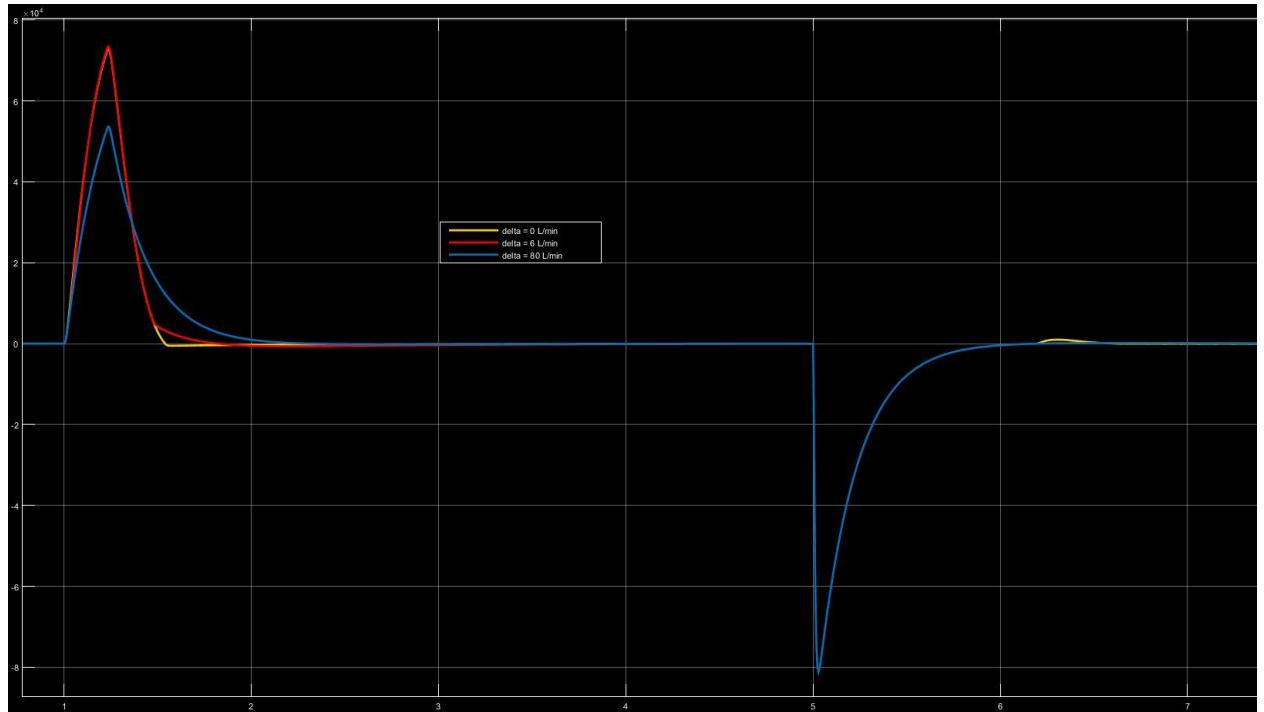
**Task 7: Reproduce the results shown in Fig. 14 for linear and variable gain controllers. What are the pros & cons of non linear control over linear control?**



## Output at Scope\_Paw:



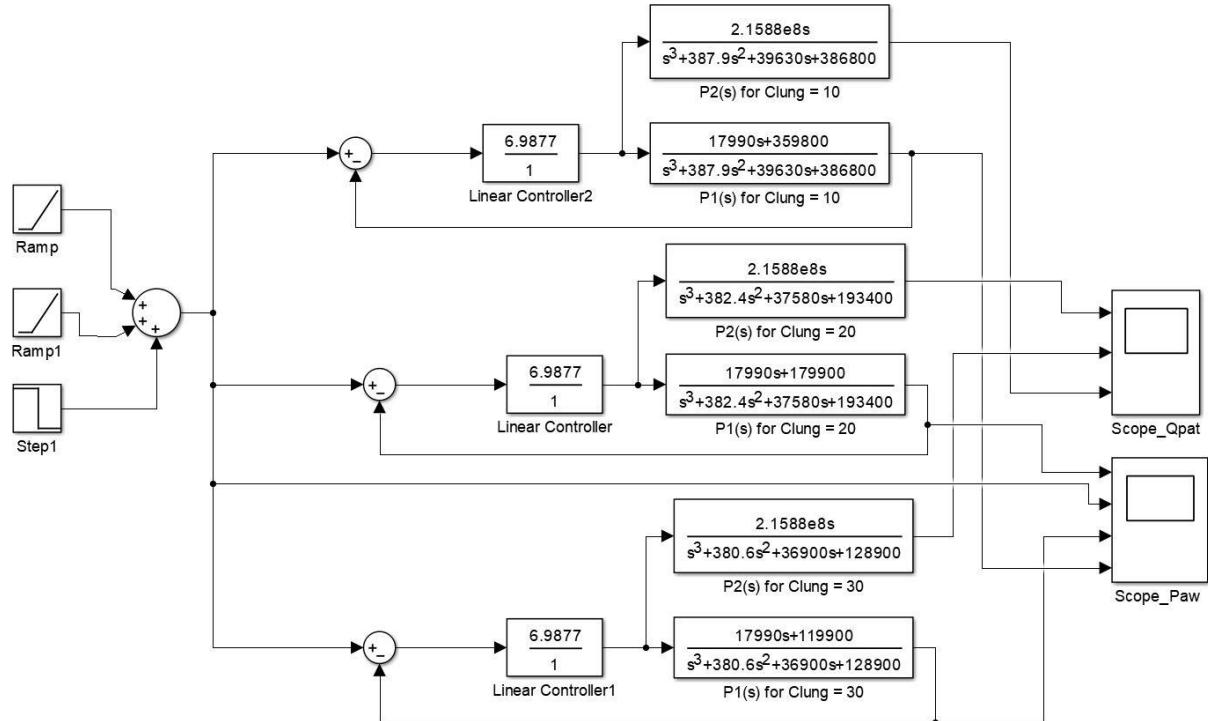
## Output at Scope\_Qpat:



Even if the plant is linear, a nonlinear controller can often have attractive features such as simpler implementation, faster speed, more accuracy, or reduced control energy, which justify the more difficult design procedure.

**Task 8: Discuss the performance of both linear and non linear control systems in presence of uncertainties such as different lung parameters, pressure drop etc.**

**(i) Variation of  $C_{lung}$  in Linear Control System :**



**Output at Scope\_Paw:**



Trace Selection	
Clung = 10	—
<b>Bilevel Measurements</b>	
▶ Settings	
▼ Transitions	
High	12.931 V
Low	45.516 mV
Amplitude	12.885 V
+ Edges	1
+ Rise Time	190.012 ms
+ Slew Rate	54.251 V/s
- Edges	1
- Fall Time	4.746 ms
- Slew Rate	-2.172 V/ms
▼ Overshoots / Undershoots	
+ Preshoot	0.353 %
+ Overshoot	0.522 %
+ Undershoot	1.985 %
+ Settling Time	—
- Preshoot	0.537 %
- Overshoot	10.924 %
- Undershoot	6.989 %
- Settling Time	—
▶ Cycles	

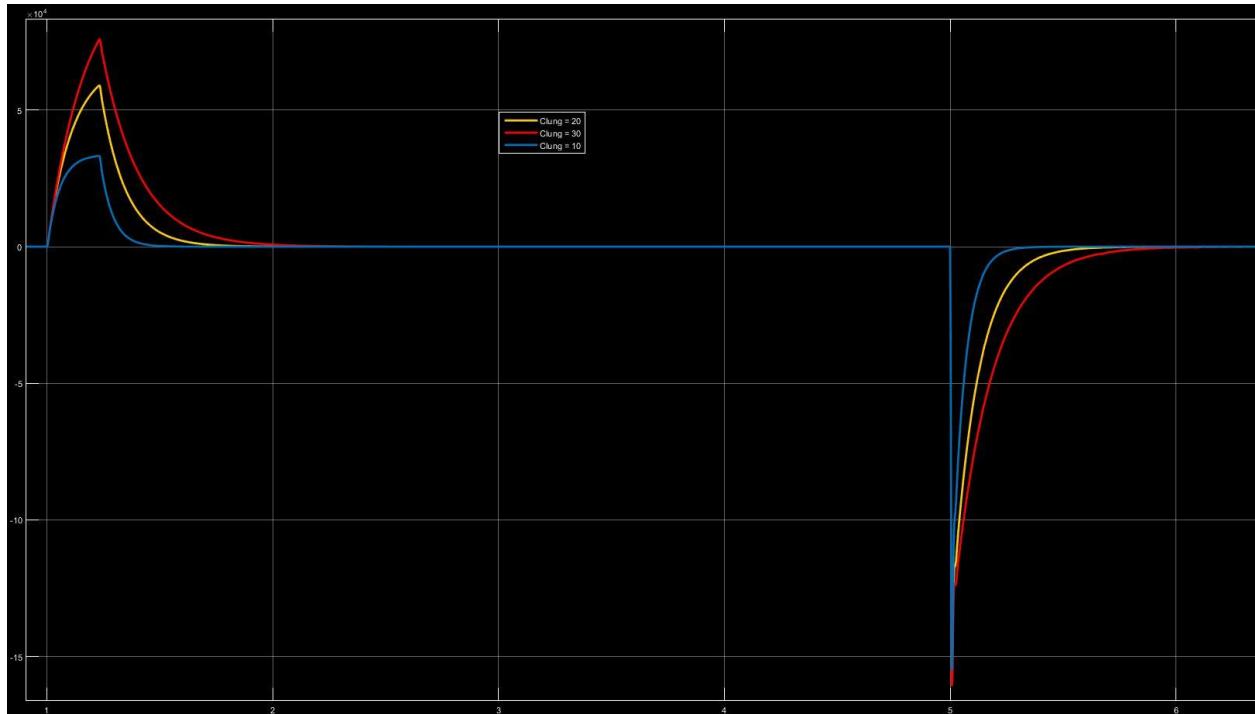
  

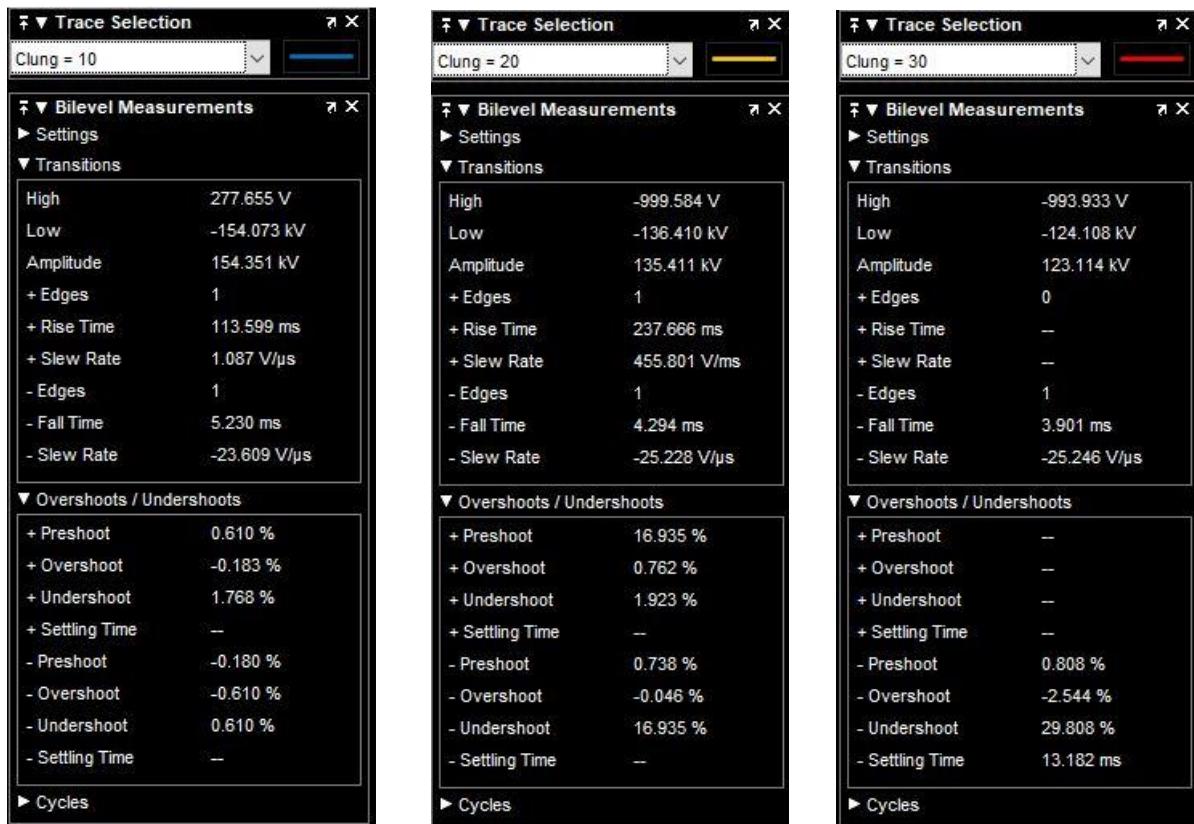
Trace Selection	
Clung = 20	—
<b>Bilevel Measurements</b>	
▶ Settings	
▼ Transitions	
High	12.931 V
Low	-22.064 mV
Amplitude	12.953 V
+ Edges	1
+ Rise Time	193.714 ms
+ Slew Rate	53.495 V/s
- Edges	1
- Fall Time	4.832 ms
- Slew Rate	-2.144 V/ms
▼ Overshoots / Undershoots	
+ Preshoot	-0.170 %
+ Overshoot	0.451 %
+ Undershoot	1.932 %
+ Settling Time	—
- Preshoot	0.530 %
- Overshoot	11.988 %
- Undershoot	5.851 %
- Settling Time	—
▶ Cycles	

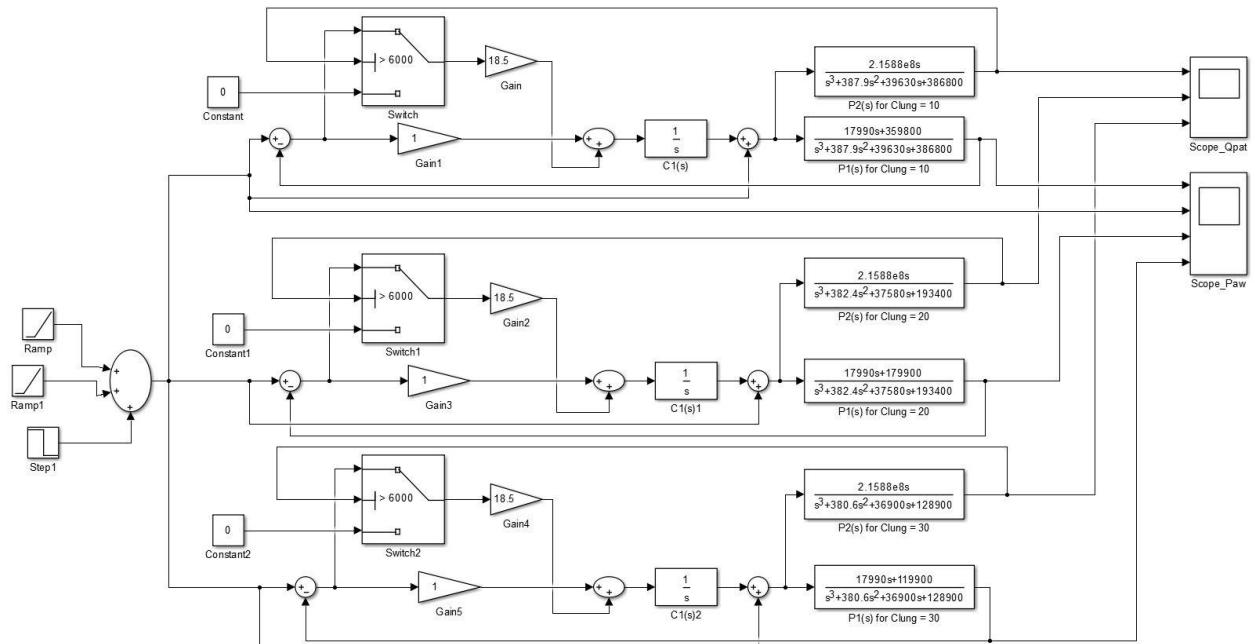
Trace Selection	
Clung = 30	—
<b>Bilevel Measurements</b>	
▶ Settings	
▼ Transitions	
High	12.930 V
Low	-14.409 mV
Amplitude	12.944 V
+ Edges	1
+ Rise Time	187.073 ms
+ Slew Rate	55.354 V/s
- Edges	1
- Fall Time	4.719 ms
- Slew Rate	-2.195 V/ms
▼ Overshoots / Undershoots	
+ Preshoot	-0.111 %
+ Overshoot	0.543 %
+ Undershoot	1.736 %
+ Settling Time	—
- Preshoot	0.543 %
- Overshoot	9.767 %
- Undershoot	8.152 %
- Settling Time	—
▶ Cycles	

## Output at Scope\_Qpat:

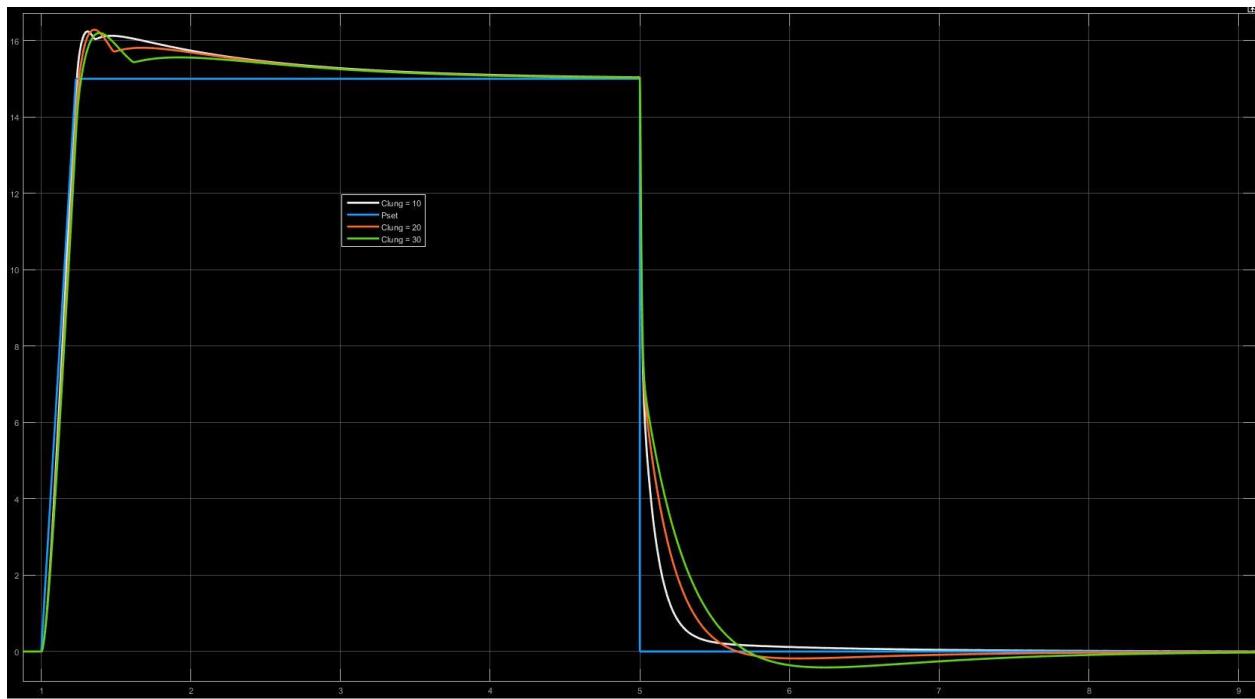




## (ii) Variation of Clung in Non-Linear Control System :



## Output at Scope\_Paw:



<b>Bilevel Measurements</b>	
► Settings	
<b>Transitions</b>	
High	15.025 V
Low	81.216 mV
Amplitude	14.944 V
+ Edges	1
+ Rise Time	168.948 ms
+ Slew Rate	70.761 V/s
- Edges	1
- Fall Time	170.212 ms
- Slew Rate	-70.236 V/s

**Overshoots / Undershoots**

+ Preshoot	—
+ Overshoot	8.152 %
+ Undershoot	1.646 %
+ Settling Time	—
- Preshoot	0.256 %
- Overshoot	1.861 %
- Undershoot	-0.367 %
- Settling Time	—

**Cycles**



<b>Bilevel Measurements</b>	
► Settings	
<b>Transitions</b>	
High	15.051 V
Low	-100.298 mV
Amplitude	15.152 V
+ Edges	1
+ Rise Time	179.553 ms
+ Slew Rate	67.508 V/s
- Edges	1
- Fall Time	300.584 ms
- Slew Rate	-40.326 V/s

**Overshoots / Undershoots**

+ Preshoot	—
+ Overshoot	8.152 %
+ Undershoot	1.859 %
+ Settling Time	—
- Preshoot	0.206 %
- Overshoot	1.844 %
- Undershoot	0.543 %
- Settling Time	—

**Cycles**



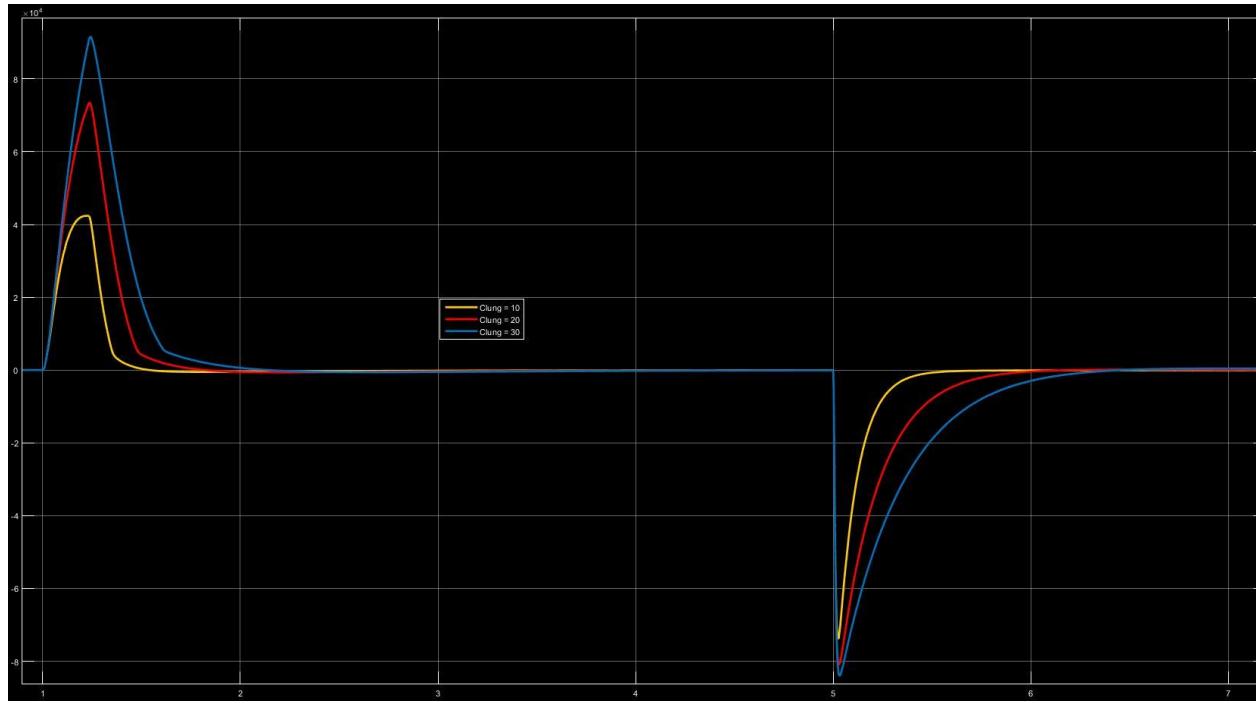
<b>Bilevel Measurements</b>	
► Settings	
<b>Transitions</b>	
High	15.118 V
Low	-2.315 mV
Amplitude	15.120 V
+ Edges	1
+ Rise Time	184.141 ms
+ Slew Rate	65.689 V/s
- Edges	1
- Fall Time	383.219 ms
- Slew Rate	-31.564 V/s

**Overshoots / Undershoots**

+ Preshoot	—
+ Overshoot	7.143 %
+ Undershoot	0.767 %
+ Settling Time	—
- Preshoot	-0.130 %
- Overshoot	1.781 %
- Undershoot	2.747 %
- Settling Time	—

**Cycles**

## Output at Scope\_Qpat:



**Trace Selection**

Clung = 10

**Bilevel Measurements**

- Settings
- ▼ Transitions

High	-31.048 V
Low	-73.254 kV
Amplitude	73.223 kV
+ Edges	1
+ Rise Time	214.426 ms
+ Slew Rate	273.187 V/ms
- Edges	1
- Fall Time	13.115 ms
- Slew Rate	-4.467 V/μs

▼ Overshoots / Undershoots

+ Preshoot	0.794 %
+ Overshoot	-0.066 %
+ Undershoot	1.701 %
+ Settling Time	--
- Preshoot	0.010 %
- Overshoot	-0.351 %
- Undershoot	0.351 %
- Settling Time	--

► Cycles

**Trace Selection**

Clung = 20

**Bilevel Measurements**

- Settings
- ▼ Transitions

High	64.790 V
Low	-6.115 kV
Amplitude	6.179 kV
+ Edges	1
+ Rise Time	389.241 ms
+ Slew Rate	12.701 V/ms
- Edges	1
- Fall Time	1.893 ms
- Slew Rate	-2.611 V/μs

▼ Overshoots / Undershoots

+ Preshoot	1212.500 %
+ Overshoot	1.258 %
+ Undershoot	1.996 %
+ Settling Time	--
- Preshoot	-1.778 %
- Overshoot	-176.720 %
- Undershoot	447.961 %
- Settling Time	--

► Cycles

**Trace Selection**

Clung = 30

**Bilevel Measurements**

- Settings
- ▼ Transitions

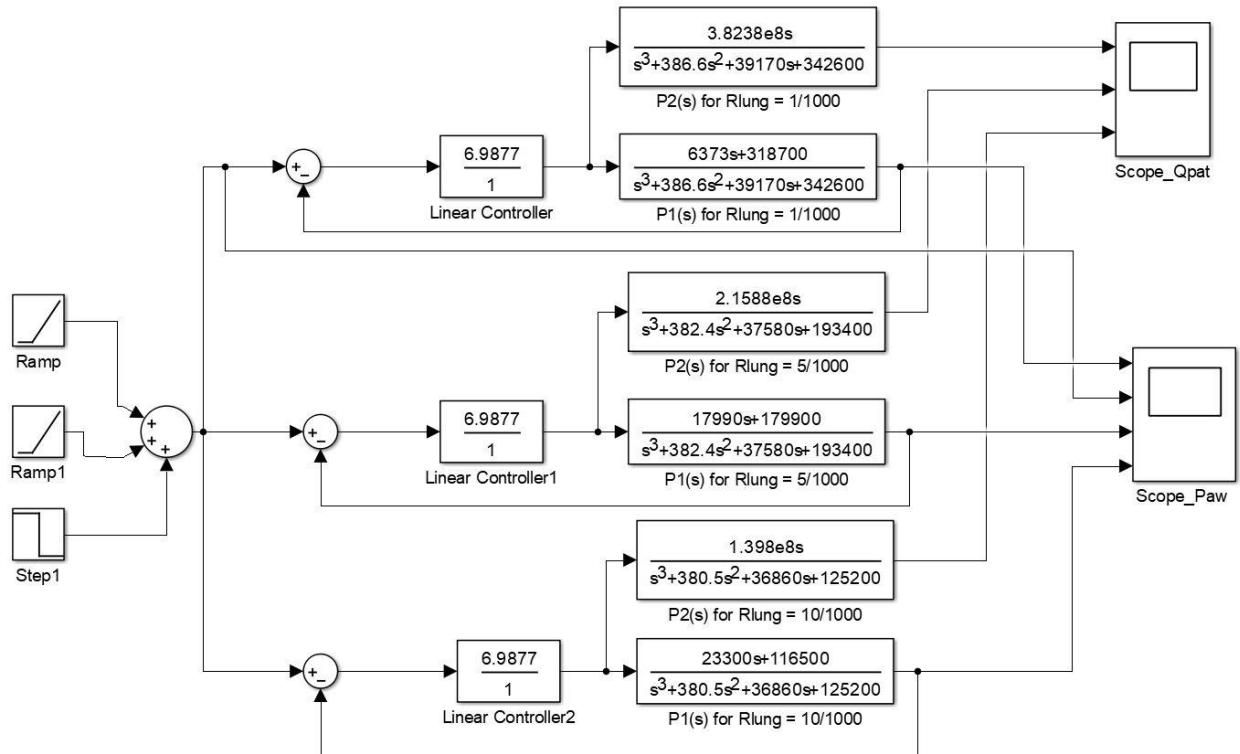
High	6.377 kV
Low	-647.080 V
Amplitude	7.024 kV
+ Edges	0
+ Rise Time	--
+ Slew Rate	--
- Edges	1
- Fall Time	513.707 ms
- Slew Rate	-10.939 V/ms

▼ Overshoots / Undershoots

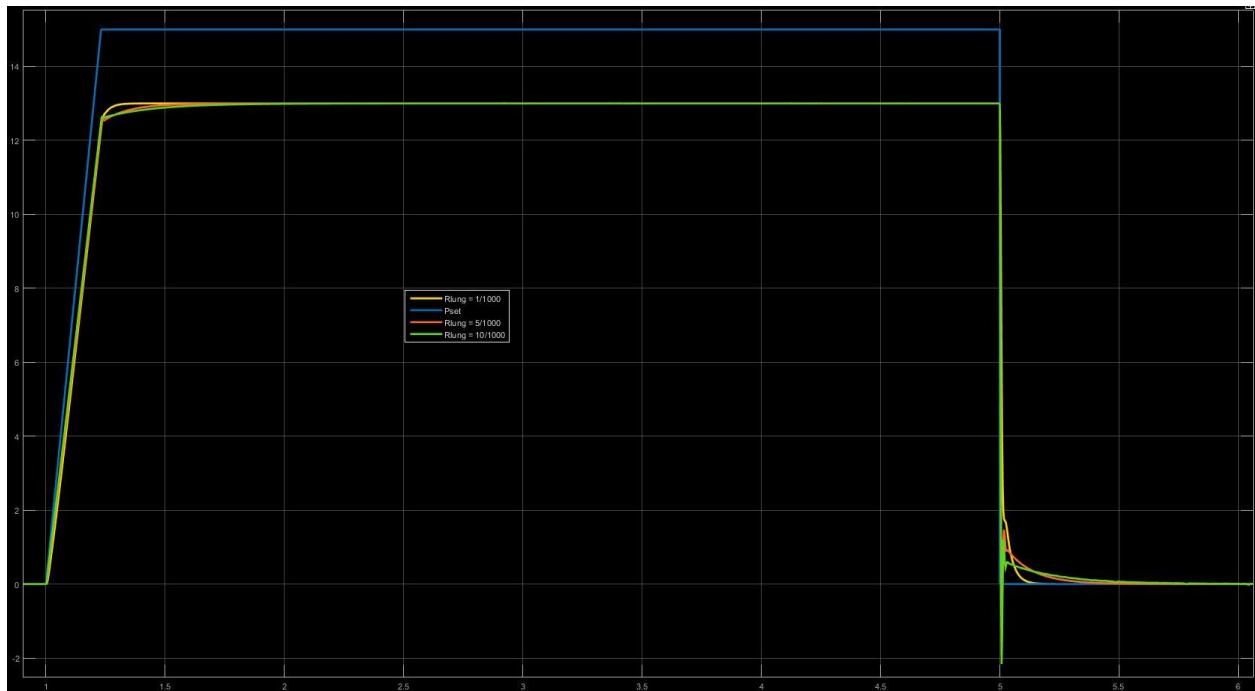
+ Preshoot	--
+ Overshoot	--
+ Undershoot	--
+ Settling Time	--
- Preshoot	1212.500 %
- Overshoot	6.132 %
- Undershoot	-0.704 %
- Settling Time	--

► Cycles

### (iii) Variation of $R_{lung}$ in Linear Control System:

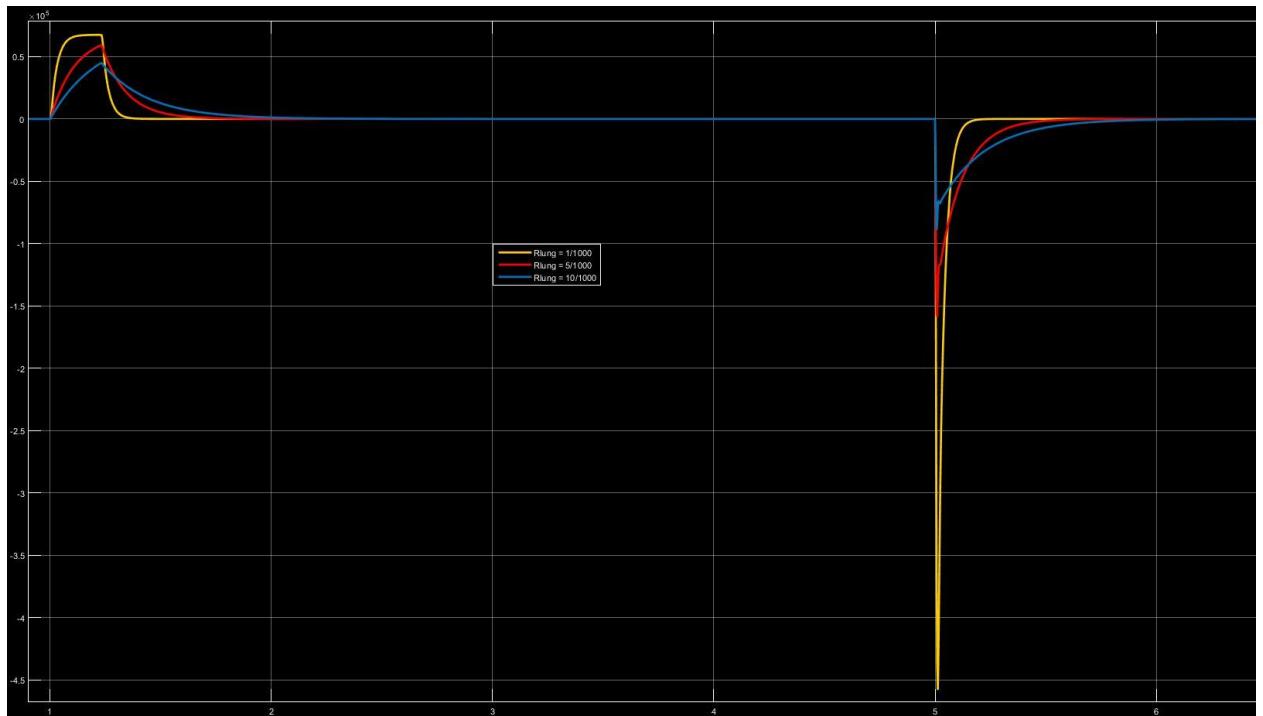


**Output at Scope\_Paw:**



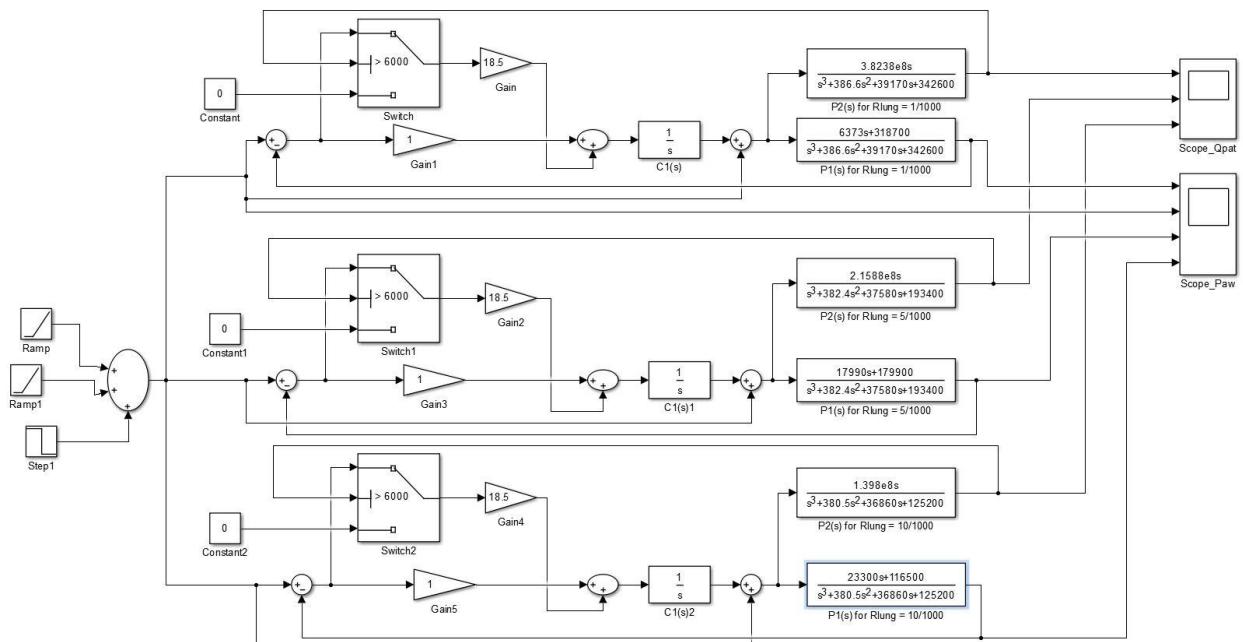
Trace Selection	
Rlung = 1/1000	Yellow
<b>Bilevel Measurements</b>	
► Settings	
▼ Transitions	
High	12.935 V
Low	65.000 mV
Amplitude	12.870 V
+ Edges	1
+ Rise Time	185.826 ms
+ Slew Rate	55.407 V/s
- Edges	1
- Fall Time	30.344 ms
- Slew Rate	-339.312 V/s
▼ Overshoots / Undershoots	
+ Preshoot	—
+ Overshoot	0.505 %
+ Undershoot	1.806 %
+ Settling Time	—
- Preshoot	0.505 %
- Overshoot	1.938 %
- Undershoot	0.398 %
- Settling Time	—
► Cycles	
Trace Selection	
Rlung = 5/1000	Red
<b>Bilevel Measurements</b>	
► Settings	
▼ Transitions	
High	12.930 V
Low	22.625 mV
Amplitude	12.907 V
+ Edges	1
+ Rise Time	190.350 ms
+ Slew Rate	54.246 V/s
- Edges	1
- Fall Time	4.819 ms
- Slew Rate	-2.143 V/ms
▼ Overshoots / Undershoots	
+ Preshoot	0.175 %
+ Overshoot	0.529 %
+ Undershoot	1.943 %
+ Settling Time	—
- Preshoot	0.543 %
- Overshoot	11.189 %
- Undershoot	8.152 %
- Settling Time	—
► Cycles	
Trace Selection	
Rlung = 10/1000	Green
<b>Bilevel Measurements</b>	
► Settings	
▼ Transitions	
High	12.926 V
Low	34.968 mV
Amplitude	12.891 V
+ Edges	1
+ Rise Time	189.071 ms
+ Slew Rate	54.545 V/s
- Edges	1
- Fall Time	4.029 ms
- Slew Rate	-2.559 V/ms
▼ Overshoots / Undershoots	
+ Preshoot	0.271 %
+ Overshoot	0.401 %
+ Undershoot	1.964 %
+ Settling Time	—
- Preshoot	0.578 %
- Overshoot	9.091 %
- Undershoot	17.059 %
- Settling Time	—
► Cycles	

## Output at Scope\_Qpat:

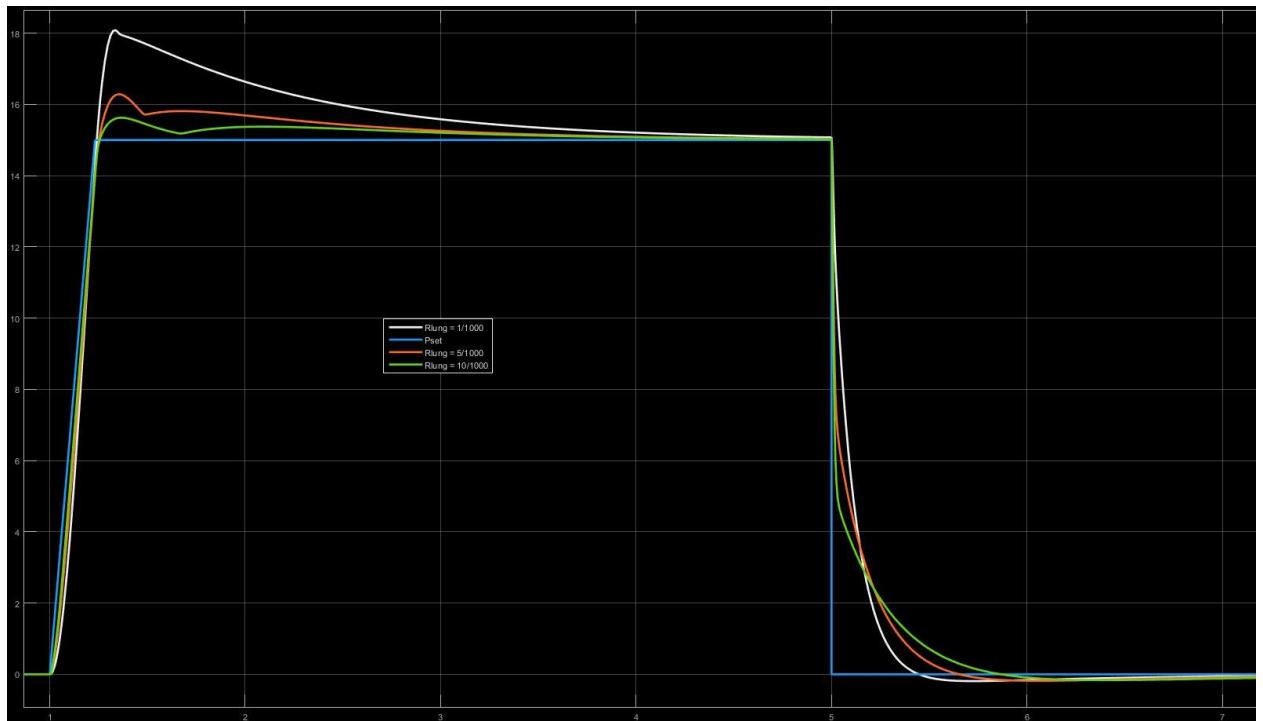




#### (iv) Variation of R<sub>lung</sub> in Non-Linear Control System :



## Output at Scope\_Paw:



**Trace Selection**

Rlung = 1/1000

**Bilevel Measurements**

- Settings
- Transitions**

High	15.070 V
Low	-98.719 mV
Amplitude	15.168 V
+ Edges	1
+ Rise Time	161.782 ms
+ Slew Rate	75.007 V/s
- Edges	1
- Fall Time	229.523 ms
- Slew Rate	-52.870 V/s

- Overshoots / Undershoots**

+ Preshoot	--
+ Overshoot	19.880 %
+ Undershoot	1.963 %
+ Settling Time	--
- Preshoot	0.527 %
- Overshoot	1.518 %
- Undershoot	0.602 %
- Settling Time	--

- Cycles

**Trace Selection**

Rlung = 5/1000

**Bilevel Measurements**

- Settings
- Transitions**

High	15.051 V
Low	-99.570 mV
Amplitude	15.151 V
+ Edges	1
+ Rise Time	179.544 ms
+ Slew Rate	67.507 V/s
- Edges	1
- Fall Time	300.893 ms
- Slew Rate	-40.282 V/s

- Overshoots / Undershoots**

+ Preshoot	--
+ Overshoot	8.152 %
+ Undershoot	1.830 %
+ Settling Time	--
- Preshoot	0.199 %
- Overshoot	1.934 %
- Undershoot	0.543 %
- Settling Time	--

- Cycles

**Trace Selection**

Rlung = 10/1000

**Bilevel Measurements**

- Settings
- Transitions**

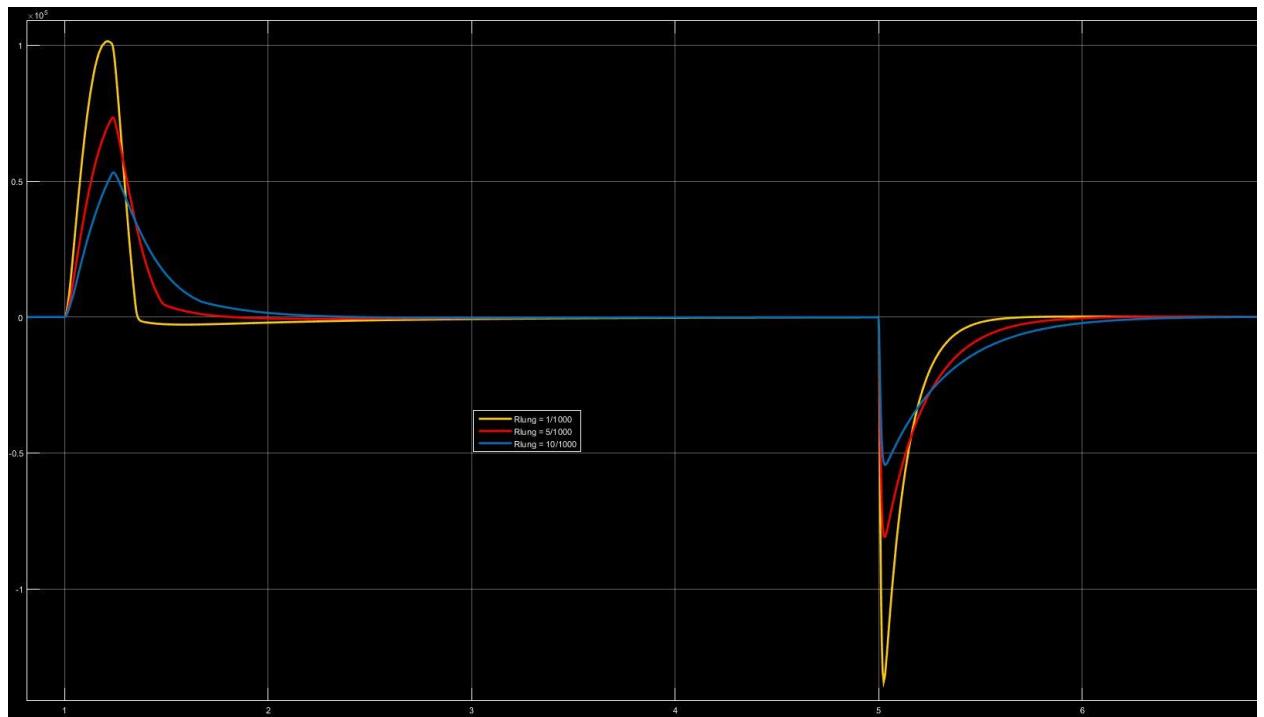
High	15.074 V
Low	-84.820 mV
Amplitude	15.159 V
+ Edges	1
+ Rise Time	181.737 ms
+ Slew Rate	66.730 V/s
- Edges	1
- Fall Time	342.628 ms
- Slew Rate	-35.395 V/s

- Overshoots / Undershoots**

+ Preshoot	--
+ Overshoot	3.646 %
+ Undershoot	1.995 %
+ Settling Time	--
- Preshoot	0.010 %
- Overshoot	1.991 %
- Undershoot	0.521 %
- Settling Time	--

- Cycles

## Output at Scope\_Qpat:



**Trace Selection**  
Rlung = 1/1000

**Bilevel Measurements**

- Settings
- Transitions

High	-1.033 kV
Low	-132.957 kV
Amplitude	131.925 kV
+ Edges	1
+ Rise Time	242.589 ms
+ Slew Rate	435.055 V/ms
- Edges	1
- Fall Time	13.178 ms
- Slew Rate	-8.009 V/ $\mu$ s

- Overshoots / Undershoots

+ Preshoot	0.893 %
+ Overshoot	0.917 %
+ Undershoot	1.713 %
+ Settling Time	--
- Preshoot	0.712 %
- Overshoot	-0.893 %
- Undershoot	0.893 %
- Settling Time	12.155 ms

Cycles

**Trace Selection**  
Rlung = 5/1000

**Bilevel Measurements**

- Settings
- Transitions

High	82.682 V
Low	-4.551 kV
Amplitude	4.634 kV
+ Edges	1
+ Rise Time	379.544 ms
+ Slew Rate	9.767 V/ms
- Edges	1
- Fall Time	1.580 ms
- Slew Rate	-2.347 V/ $\mu$ s

- Overshoots / Undershoots

+ Preshoot	1650.000 %
+ Overshoot	1.306 %
+ Undershoot	1.883 %
+ Settling Time	--
- Preshoot	-1.524 %
- Overshoot	-146.656 %
- Undershoot	495.769 %
- Settling Time	--

Cycles

**Trace Selection**  
Rlung = 10/1000

**Bilevel Measurements**

- Settings
- Transitions

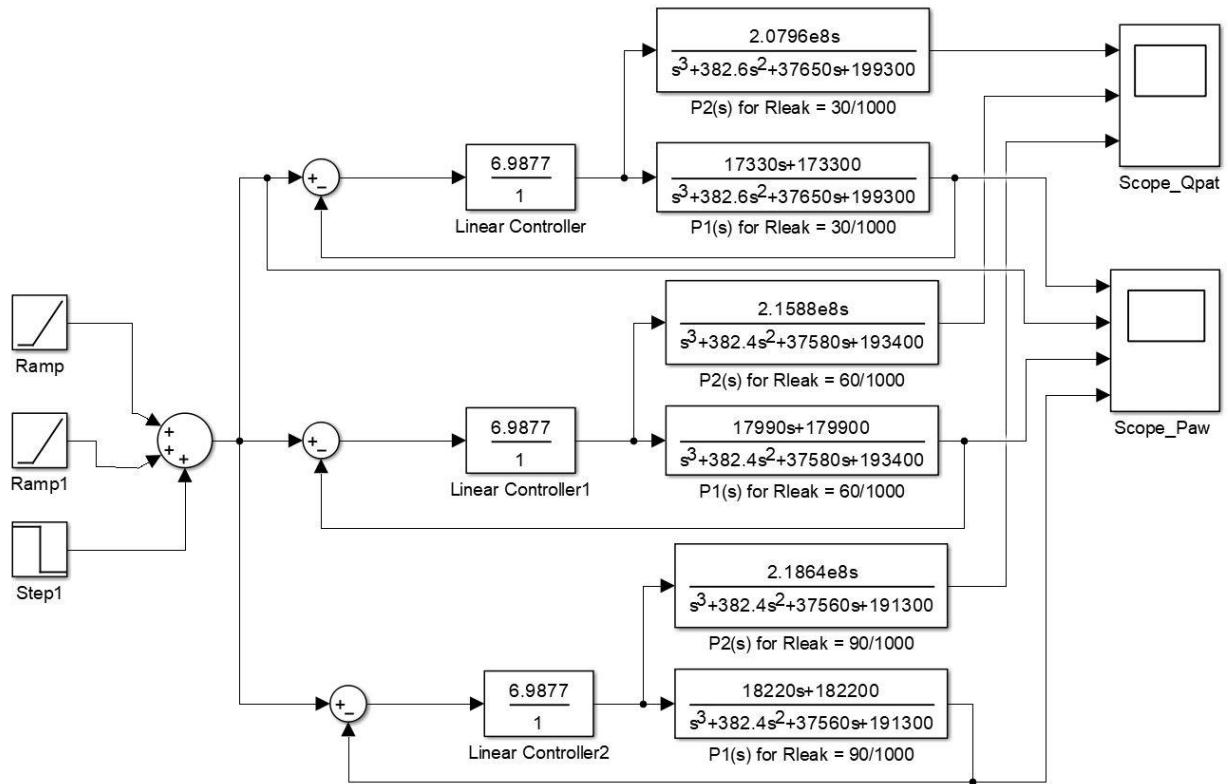
High	-133.983 V
Low	-1.211 kV
Amplitude	1.077 kV
+ Edges	1
+ Rise Time	321.963 ms
+ Slew Rate	2.677 V/ms
- Edges	1
- Fall Time	623.121 $\mu$ s
- Slew Rate	-1.383 V/ $\mu$ s

- Overshoots / Undershoots

+ Preshoot	2754.187 %
+ Overshoot	21.688 %
+ Undershoot	1.496 %
+ Settling Time	--
- Preshoot	8.543 %
- Overshoot	-98.627 %
- Undershoot	98.627 %
- Settling Time	--

Cycles

### (v) Variation of R<sub>leak</sub> in Linear Control System :

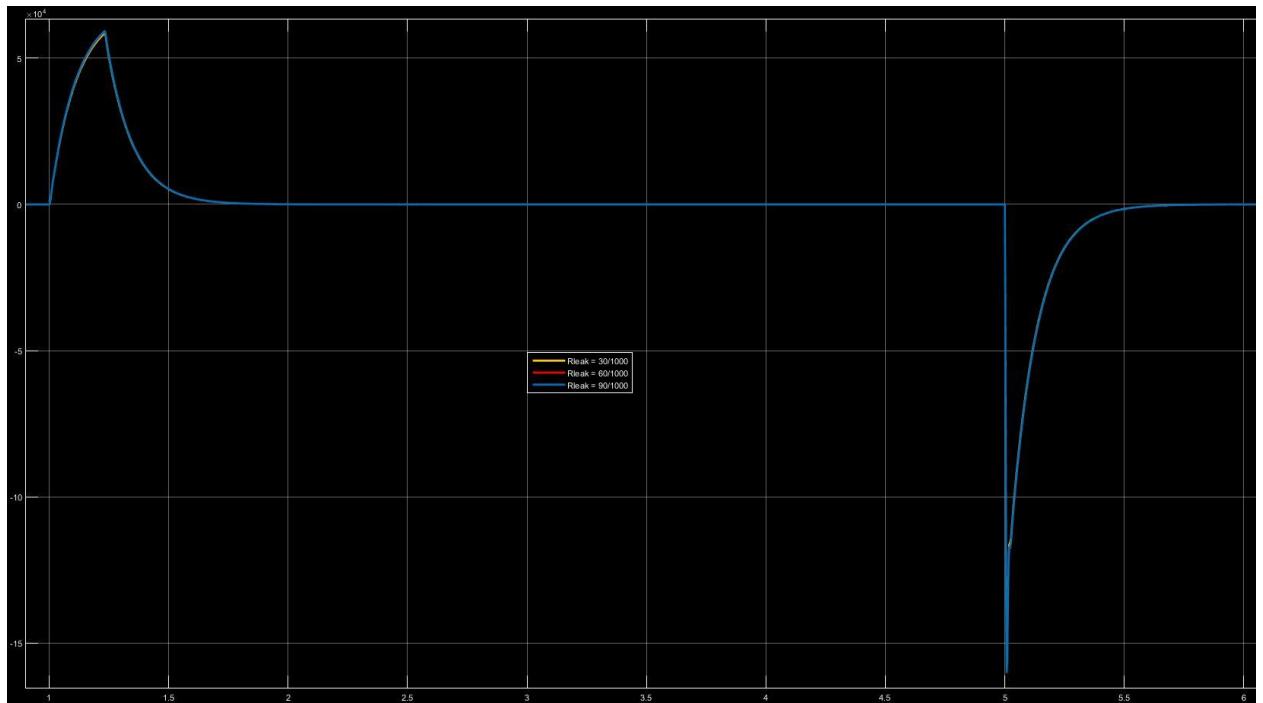


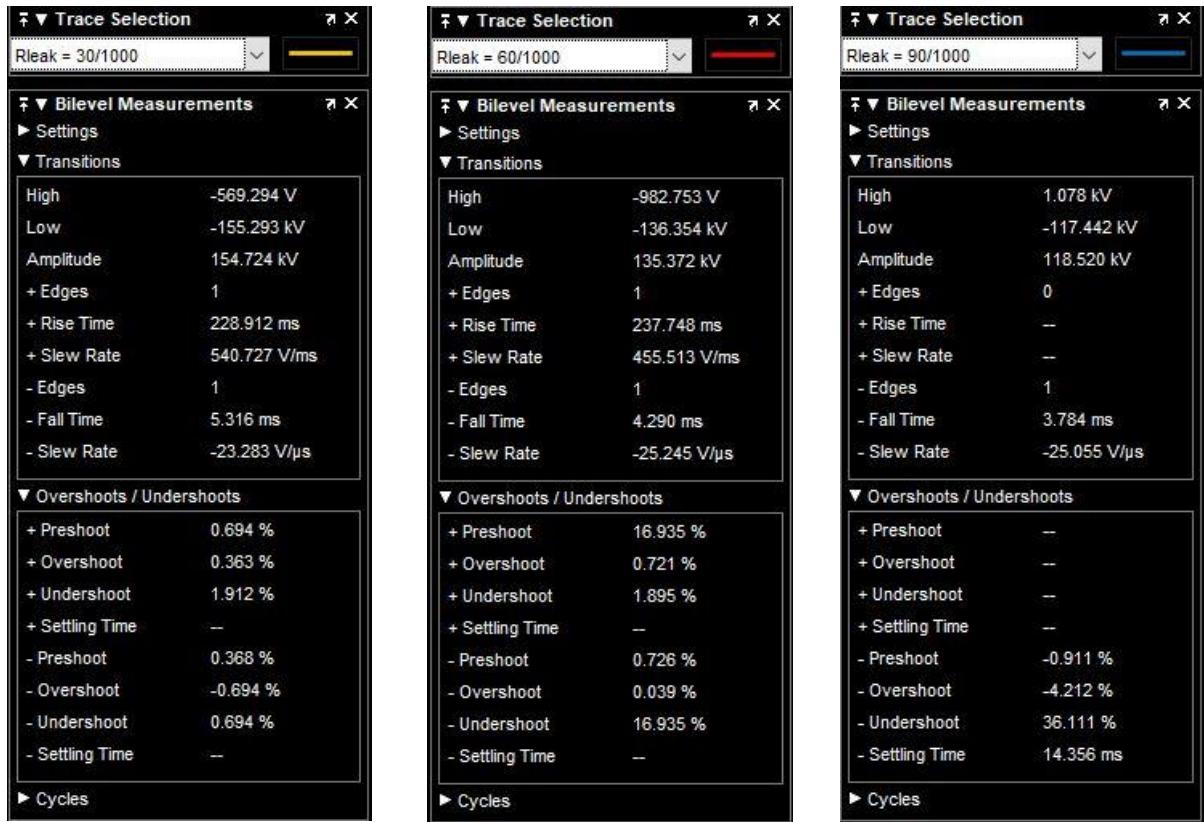
**Output at Scope\_Paw:**



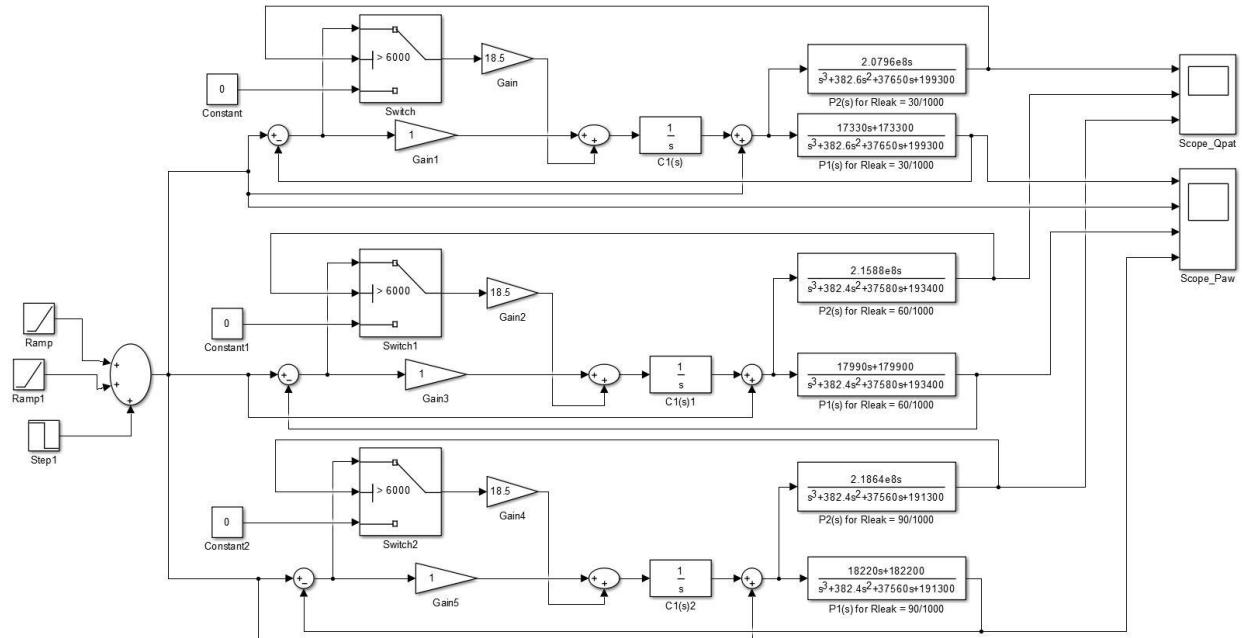
Trace Selection	
Rleak = 30/1000	Yellow
<b>Bilevel Measurements</b>	
▶ Settings	
▼ Transitions	
High	12.812 V
Low	32.866 mV
Amplitude	12.779 V
+ Edges	1
+ Rise Time	190.146 ms
+ Slew Rate	53.764 V/s
- Edges	1
- Fall Time	4.912 ms
- Slew Rate	-2.081 V/ms
▼ Overshoots / Undershoots	
+ Preshoot	0.257 %
+ Overshoot	0.523 %
+ Undershoot	1.956 %
+ Settling Time	--
- Preshoot	0.538 %
- Overshoot	10.847 %
- Undershoot	6.989 %
- Settling Time	--
▶ Cycles	
Trace Selection	
Rleak = 60/1000	Orange
<b>Bilevel Measurements</b>	
▶ Settings	
▼ Transitions	
High	12.931 V
Low	38.713 mV
Amplitude	12.892 V
+ Edges	1
+ Rise Time	190.114 ms
+ Slew Rate	54.249 V/s
- Edges	1
- Fall Time	4.753 ms
- Slew Rate	-2.170 V/ms
▼ Overshoots / Undershoots	
+ Preshoot	0.300 %
+ Overshoot	0.523 %
+ Undershoot	1.975 %
+ Settling Time	--
- Preshoot	0.538 %
- Overshoot	10.978 %
- Undershoot	6.989 %
- Settling Time	--
▶ Cycles	
Trace Selection	
Rleak = 90/1000	Green
<b>Bilevel Measurements</b>	
▶ Settings	
▼ Transitions	
High	12.971 V
Low	37.934 mV
Amplitude	12.933 V
+ Edges	1
+ Rise Time	190.150 ms
+ Slew Rate	54.412 V/s
- Edges	1
- Fall Time	4.722 ms
- Slew Rate	-2.191 V/ms
▼ Overshoots / Undershoots	
+ Preshoot	0.293 %
+ Overshoot	0.524 %
+ Undershoot	1.983 %
+ Settling Time	--
- Preshoot	0.537 %
- Overshoot	11.033 %
- Undershoot	6.989 %
- Settling Time	--
▶ Cycles	

## Output at Scope\_Qpat:

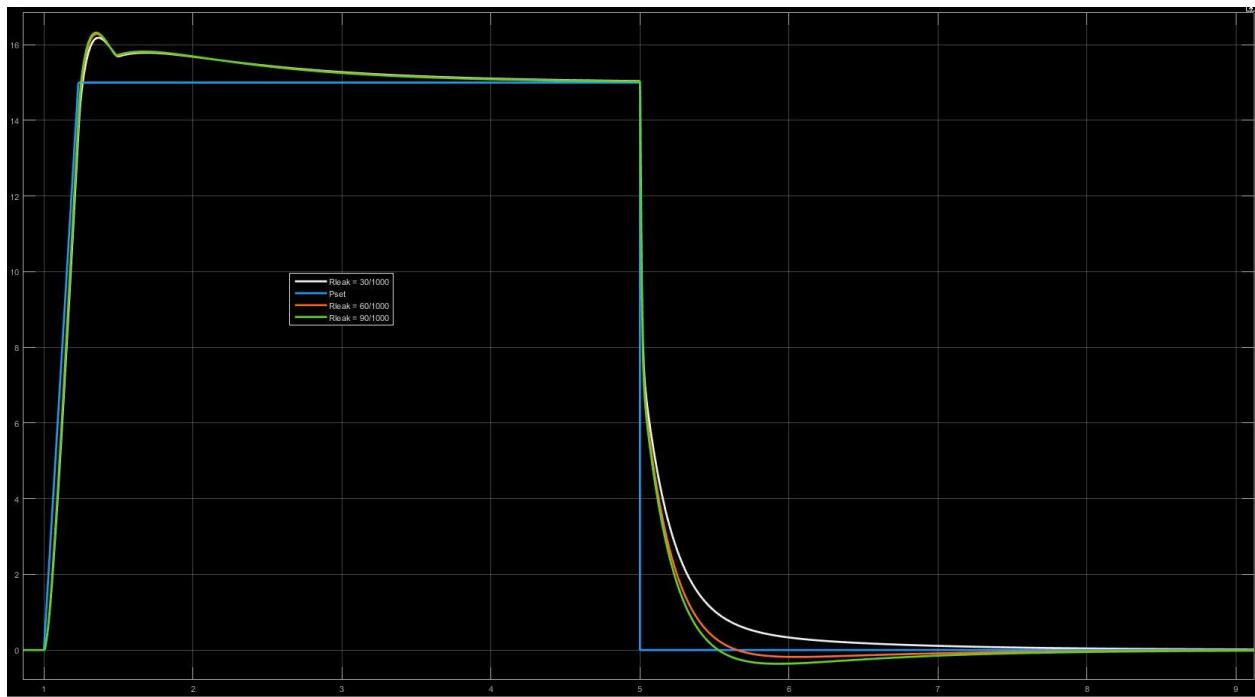




## (vi) Variation of Rleak in Non-Linear Control System :



## Output at Scope\_Paw:



Bilevel Measurements	
► Settings	
<b>Transitions</b>	
High	15.134 V
Low	80.929 mV
Amplitude	15.053 V
+ Edges	1
+ Rise Time	180.164 ms
+ Slew Rate	66.840 V/s
- Edges	1
- Fall Time	373.346 ms
- Slew Rate	-32.255 V/s
<b>Overshoots / Undershoots</b>	
+ Preshoot	—
+ Overshoot	6.989 %
+ Undershoot	1.185 %
+ Settling Time	—
- Preshoot	-0.106 %
- Overshoot	1.963 %
- Undershoot	-0.182 %
- Settling Time	—
► Cycles	

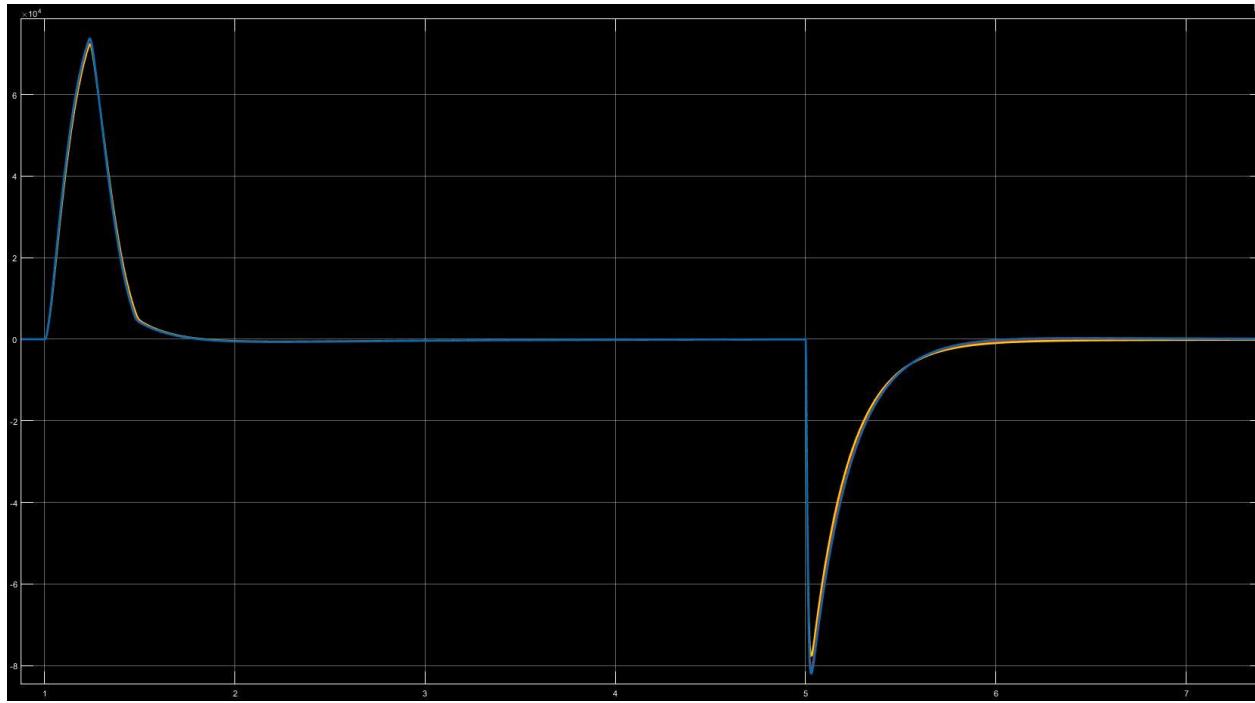


Bilevel Measurements	
► Settings	
<b>Transitions</b>	
High	15.051 V
Low	-99.577 mV
Amplitude	15.151 V
+ Edges	1
+ Rise Time	179.579 ms
+ Slew Rate	67.495 V/s
- Edges	1
- Fall Time	300.778 ms
- Slew Rate	-40.298 V/s
<b>Overshoots / Undershoots</b>	
+ Preshoot	—
+ Overshoot	8.152 %
+ Undershoot	1.715 %
+ Settling Time	—
- Preshoot	0.202 %
- Overshoot	1.862 %
- Undershoot	0.543 %
- Settling Time	—
► Cycles	



Bilevel Measurements	
► Settings	
<b>Transitions</b>	
High	15.070 V
Low	-113.368 mV
Amplitude	15.183 V
+ Edges	1
+ Rise Time	179.066 ms
+ Slew Rate	67.832 V/s
- Edges	1
- Fall Time	276.490 ms
- Slew Rate	-43.931 V/s
<b>Overshoots / Undershoots</b>	
+ Preshoot	—
+ Overshoot	8.242 %
+ Undershoot	1.212 %
+ Settling Time	—
- Preshoot	0.008 %
- Overshoot	1.946 %
- Undershoot	1.648 %
- Settling Time	—
► Cycles	

## Output at Scope\_Qpat:



**Trace Selection**  
P2(s) for Rleak = 30/1000

**Bilevel Measurements**

- Settings
- Transitions**

High	-377.439 V
Low	-3.379 kV
Amplitude	3.002 kV
+ Edges	1
+ Rise Time	397.142 ms
+ Slew Rate	6.047 V/ms
- Edges	1
- Fall Time	1.062 ms
- Slew Rate	-2.261 V/μs

- Overshoots / Undershoots**

+ Preshoot	2475.000 %
+ Overshoot	9.468 %
+ Undershoot	1.550 %
+ Settling Time	--
- Preshoot	10.852 %
- Overshoot	-26.350 %
- Undershoot	328.651 %
- Settling Time	--

- Cycles

**Trace Selection**  
P2(s) for Rleak = 60/1000

**Bilevel Measurements**

- Settings
- Transitions**

High	155.301 V
Low	-4.473 kV
Amplitude	4.629 kV
+ Edges	1
+ Rise Time	401.852 ms
+ Slew Rate	9.215 V/ms
- Edges	1
- Fall Time	1.578 ms
- Slew Rate	-2.347 V/μs

- Overshoots / Undershoots**

+ Preshoot	1650.000 %
+ Overshoot	-0.279 %
+ Undershoot	1.953 %
+ Settling Time	--
- Preshoot	-0.238 %
- Overshoot	-200.306 %
- Undershoot	559.735 %
- Settling Time	--

- Cycles

**Trace Selection**  
P2(s) for Rleak = 90/1000

**Bilevel Measurements**

- Settings
- Transitions**

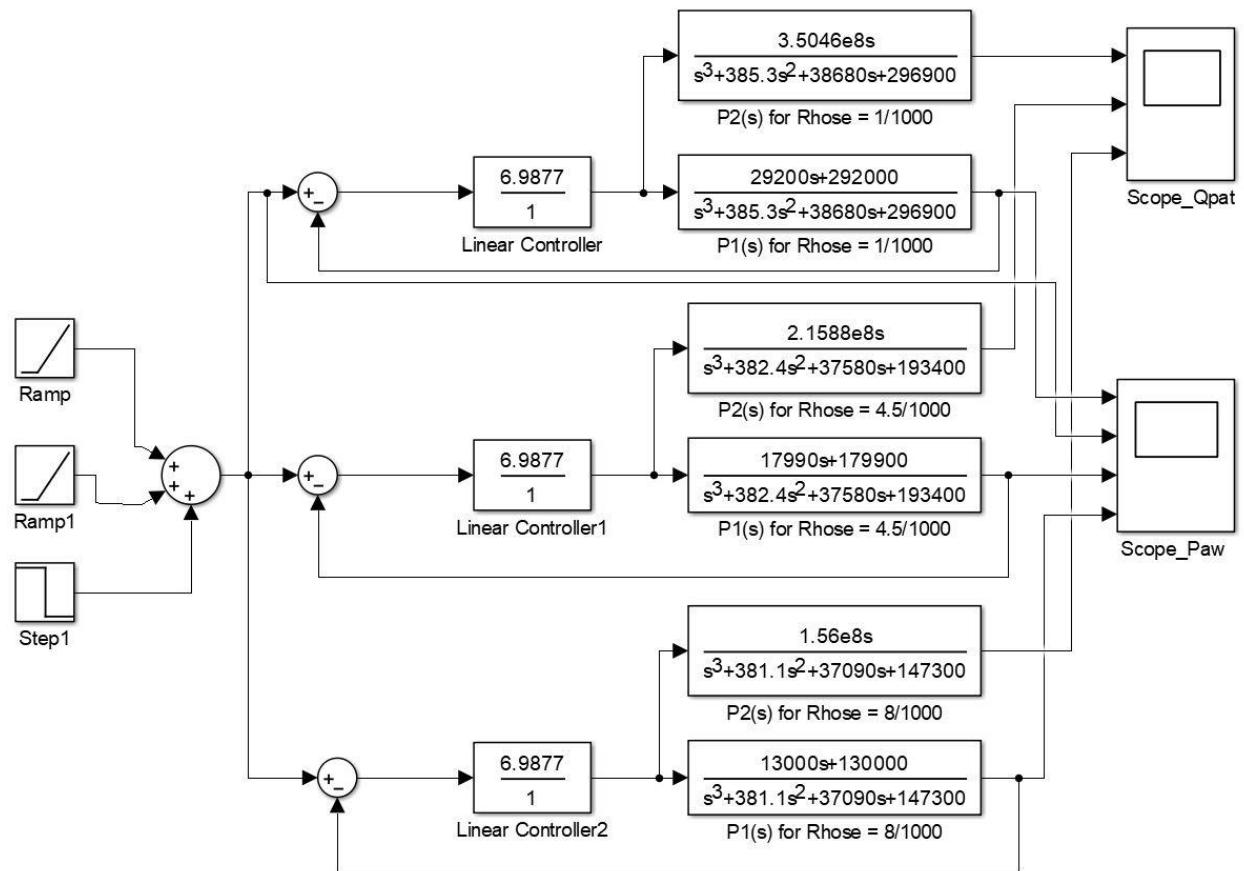
High	-186.855 V
Low	-4.859 kV
Amplitude	4.672 kV
+ Edges	1
+ Rise Time	287.839 ms
+ Slew Rate	12.984 V/ms
- Edges	1
- Fall Time	1.568 ms
- Slew Rate	-2.384 V/μs

- Overshoots / Undershoots**

+ Preshoot	1650.000 %
+ Overshoot	10.100 %
+ Undershoot	1.501 %
+ Settling Time	--
- Preshoot	3.094 %
- Overshoot	-193.908 %
- Undershoot	554.606 %
- Settling Time	--

- Cycles

### (vii) Variation of Rho<sub>e</sub> in Linear Control System :

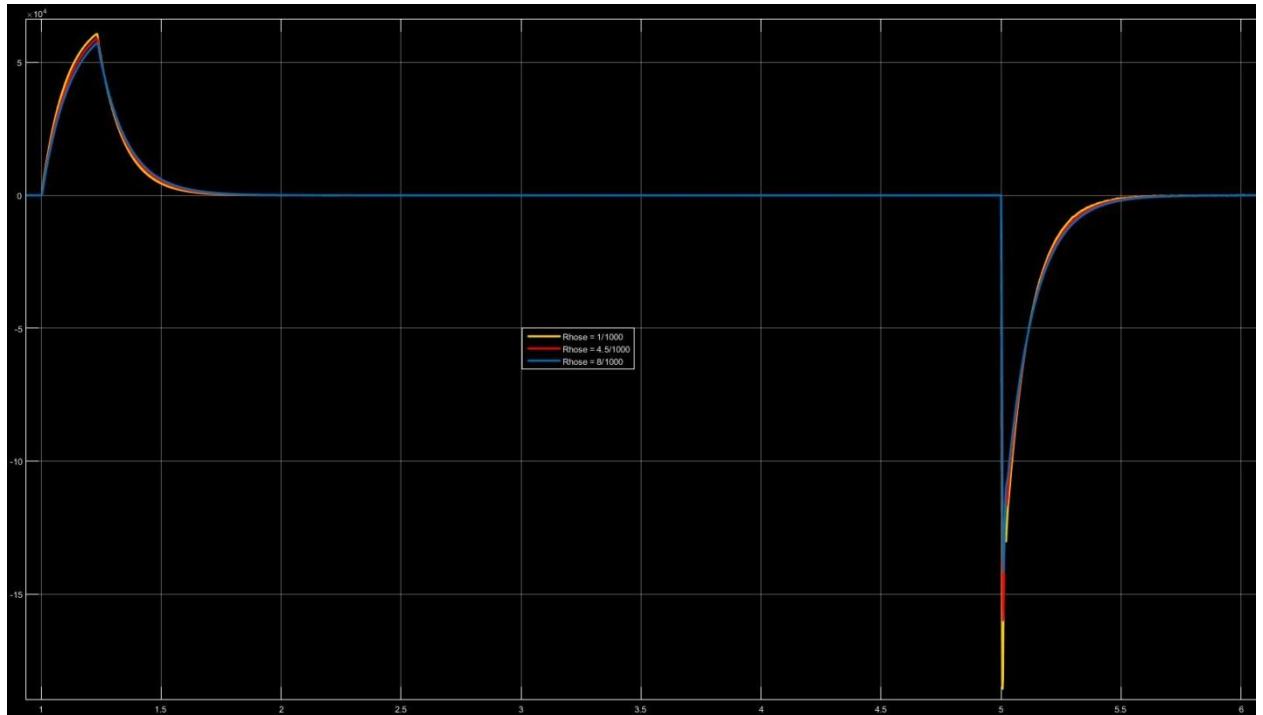


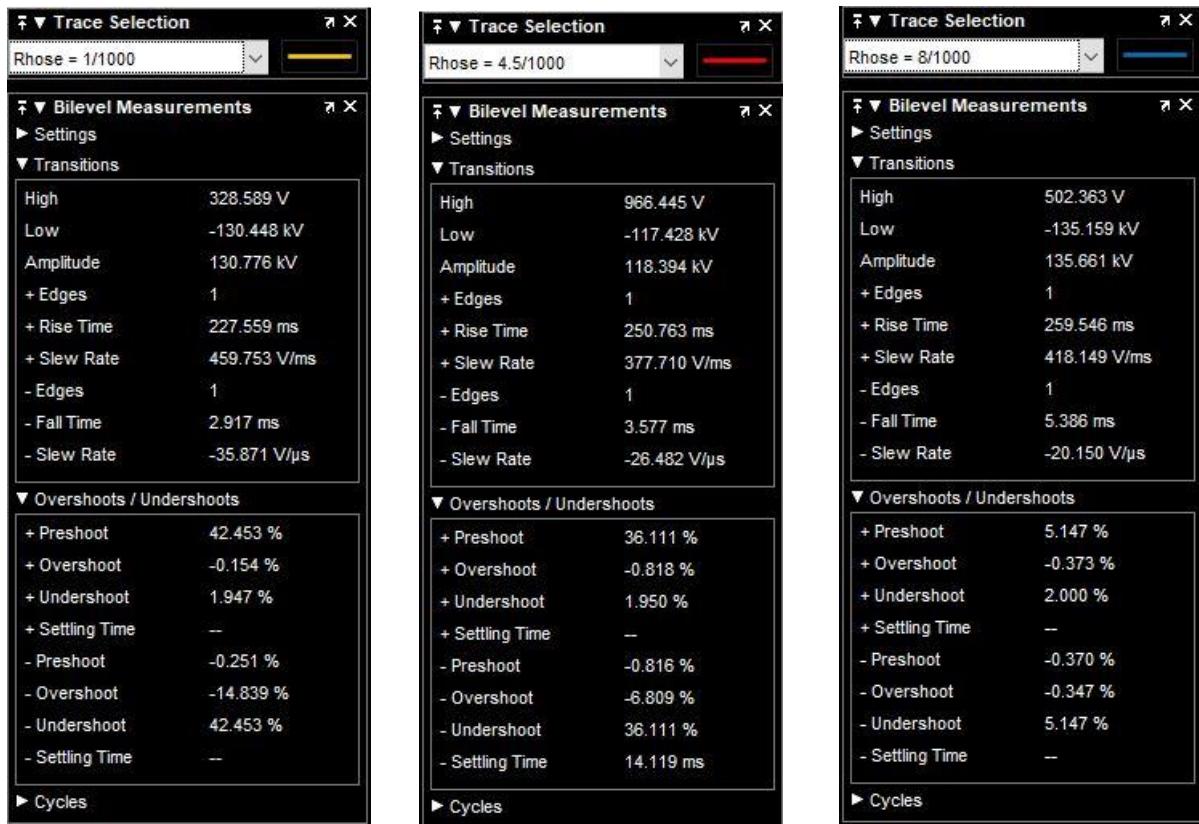
### Output at Scope\_Paw:



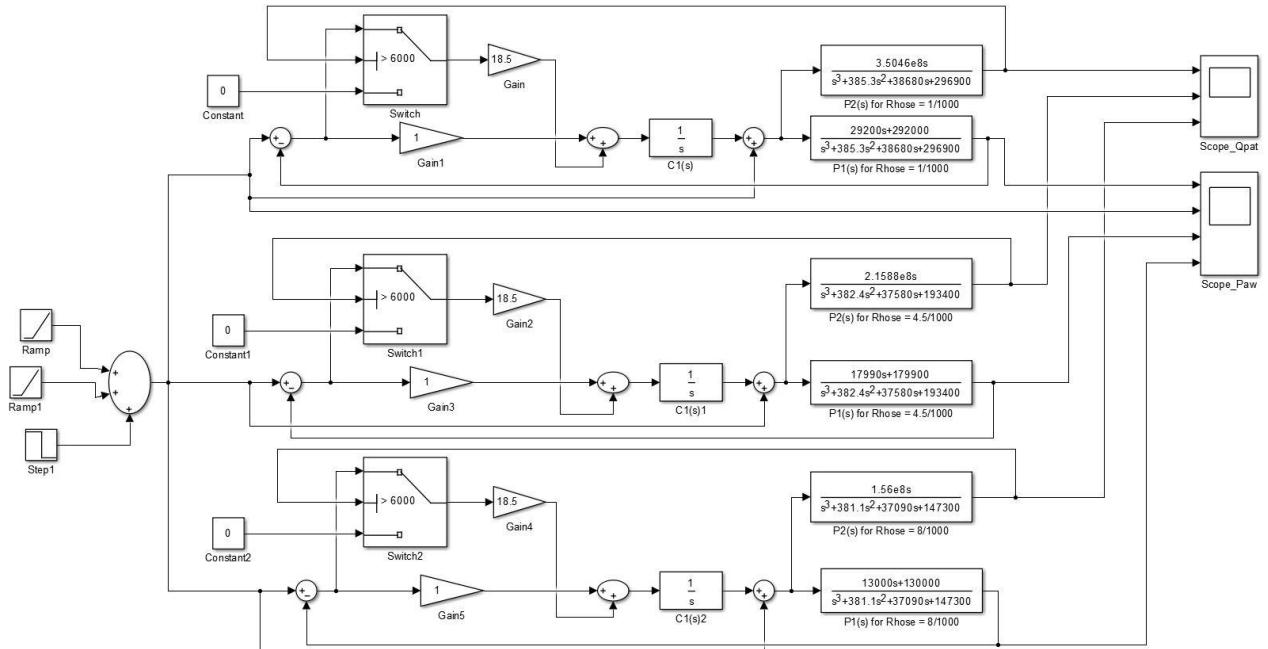
Trace Selection	
Rhose = 1/1000	Yellow
Bilevel Measurements	
► Settings	
▼ Transitions	
High	13.015 V
Low	61.422 mV
Amplitude	12.954 V
+ Edges	1
+ Rise Time	184.517 ms
+ Slew Rate	56.163 V/s
- Edges	1
- Fall Time	3.287 ms
- Slew Rate	-3.153 V/ms
▼ Overshoots / Undershoots	
+ Preshoot	0.474 %
+ Overshoot	0.610 %
+ Undershoot	0.963 %
+ Settling Time	—
- Preshoot	0.613 %
- Overshoot	7.315 %
- Undershoot	22.840 %
- Settling Time	15.690 ms
► Cycles	
Trace Selection	
Rhose = 4.5/1000	Red
Bilevel Measurements	
► Settings	
▼ Transitions	
High	12.930 V
Low	-22.750 mV
Amplitude	12.953 V
+ Edges	1
+ Rise Time	191.055 ms
+ Slew Rate	54.238 V/s
- Edges	1
- Fall Time	4.602 ms
- Slew Rate	-2.252 V/ms
▼ Overshoots / Undershoots	
+ Preshoot	-0.176 %
+ Overshoot	0.523 %
+ Undershoot	1.896 %
+ Settling Time	—
- Preshoot	0.538 %
- Overshoot	11.574 %
- Undershoot	6.989 %
- Settling Time	--
► Cycles	
Trace Selection	
Rhose = 8/1000	Green
Bilevel Measurements	
► Settings	
▼ Transitions	
High	12.843 V
Low	64.536 mV
Amplitude	12.778 V
+ Edges	1
+ Rise Time	194.742 ms
+ Slew Rate	52.492 V/s
- Edges	1
- Fall Time	6.257 ms
- Slew Rate	-1.634 V/ms
▼ Overshoots / Undershoots	
+ Preshoot	0.505 %
+ Overshoot	0.486 %
+ Undershoot	1.908 %
+ Settling Time	—
- Preshoot	0.505 %
- Overshoot	14.591 %
- Undershoot	-1.998 %
- Settling Time	—
► Cycles	

## Output at Scope\_Qpat:

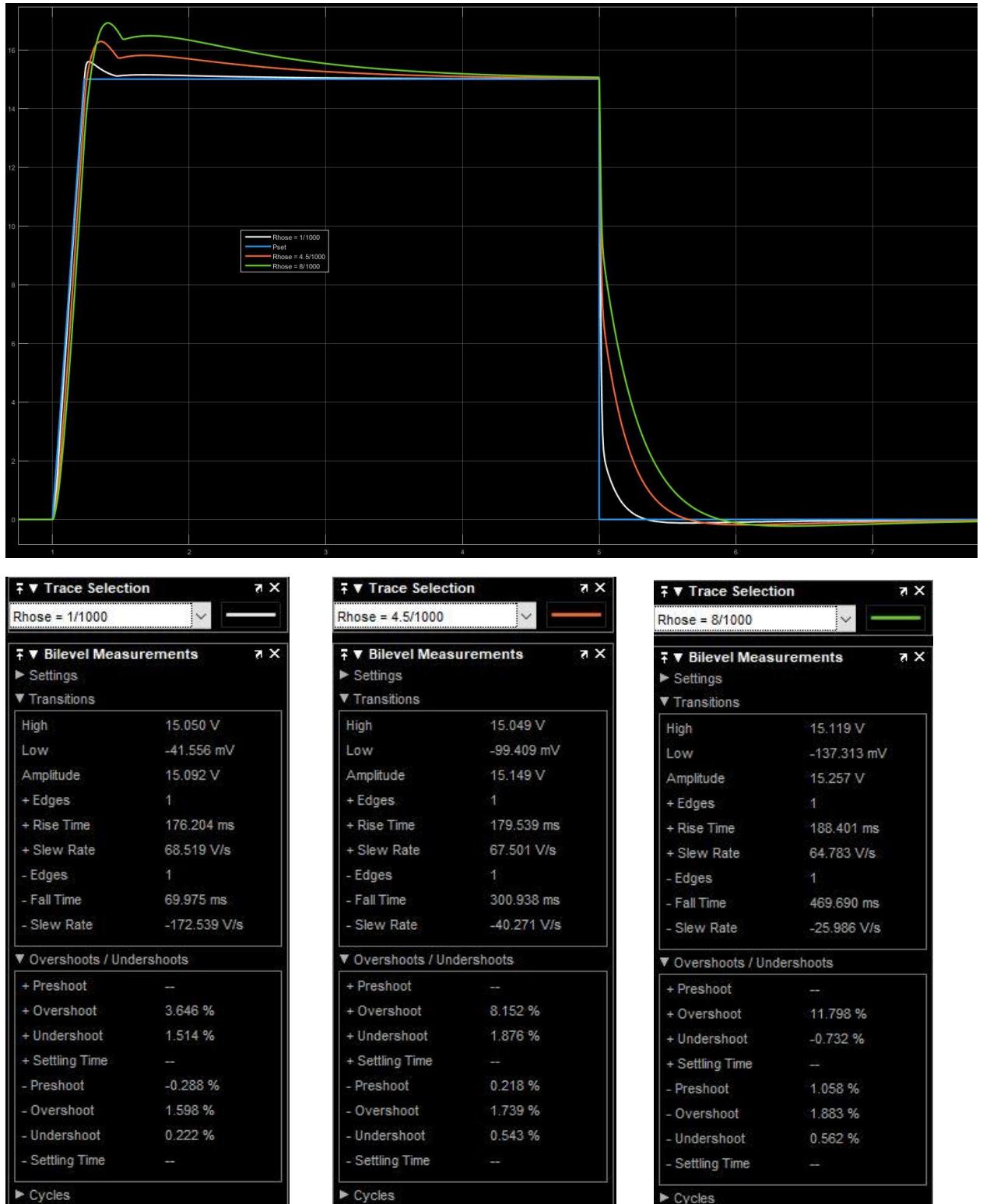




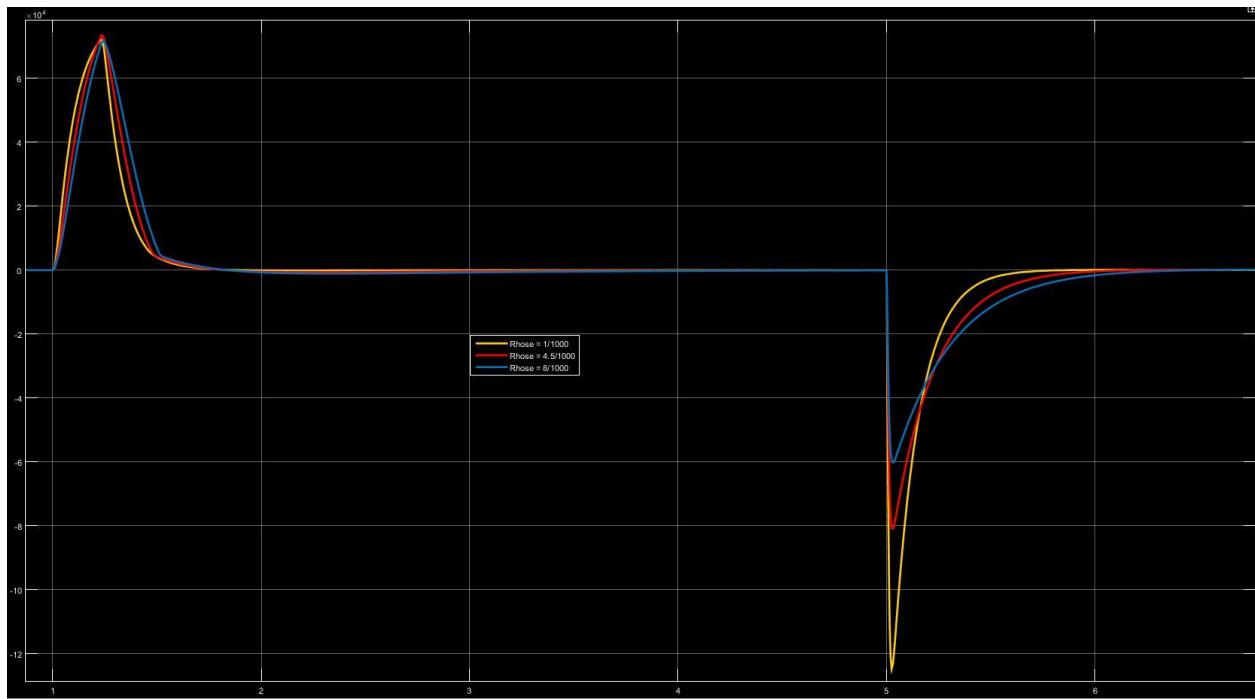
### (viii) Variation of Rhoose in Non-Linear Control System :



## Output at Scope\_Paw:



## Output at Scope\_Qpat:



**Trace Selection**

Rhose = 1/1000

Bilevel Measurements	
► Settings	
▼ Transitions	
High	248.297 V
Low	-123.748 kV
Amplitude	123.996 kV
+ Edges	1
+ Rise Time	270.291 ms
+ Slew Rate	366.999 V/ms
- Edges	1
- Fall Time	13.560 ms
- Slew Rate	-7.315 V/μs

Overshoots / Undershoots	
+ Preshoot	0.794 %
+ Overshoot	-0.130 %
+ Undershoot	1.821 %
+ Settling Time	--
- Preshoot	-0.207 %
- Overshoot	-0.794 %
- Undershoot	0.794 %
- Settling Time	12.774 ms

► Cycles

**Trace Selection**

Rhose = 4.5/1000

Bilevel Measurements	
► Settings	
▼ Transitions	
High	83.451 V
Low	-4.550 kV
Amplitude	4.633 kV
+ Edges	1
+ Rise Time	379.694 ms
+ Slew Rate	9.763 V/ms
- Edges	1
- Fall Time	1.577 ms
- Slew Rate	-2.350 V/μs

Overshoots / Undershoots	
+ Preshoot	1650.000 %
+ Overshoot	1.292 %
+ Undershoot	1.940 %
+ Settling Time	--
- Preshoot	-1.737 %
- Overshoot	-144.163 %
- Undershoot	493.205 %
- Settling Time	--

► Cycles

**Trace Selection**

Rhose = 8/1000

Bilevel Measurements	
► Settings	
▼ Transitions	
High	4.976 kV
Low	-300.474 V
Amplitude	5.276 kV
+ Edges	0
+ Rise Time	--
+ Slew Rate	--
- Edges	1
- Fall Time	287.290 ms
- Slew Rate	-14.692 V/ms

Overshoots / Undershoots	
+ Preshoot	--
+ Overshoot	--
+ Undershoot	--
+ Settling Time	--
- Preshoot	1262.500 %
- Overshoot	1.196 %
- Undershoot	15.075 %
- Settling Time	--

► Cycles