house price prediction

September 26, 2023

1 House Price Prediction

1.0.1 Motivation

- I am always facinated by pricing prediction. Real estate market has interesting stories and events. I believe this is going to be an interesting and challenging project to be able to predict the prices correctly.
- I want to find out how accurately we can model the problem and see how we can predict.

1.0.2 Objective

- The objective of the project is to utilize advanced predictive modeling techniques to analyze historical and current data on property prices.
- The aim is to forecast future trends in the housing market, thereby providing invaluable insights to stakeholders.

1.0.3 Data

- We will be using Kaggle House Prices dataset, https://www.kaggle.com/competitions/house-prices-advanced-regression-techniques/overview.
- The dataset has 81 features that cover a wide range of attributes like square footage, neighborhood, quality of materials, and many more
- The objective is to build a robust predictive model that leverages the 81 features to accurately predict house prices. Special attention will be given to feature selection and engineering, as well as evaluating various machine learning algorithms to arrive at a model that minimizes error rates.

```
import pandas as pd
import numpy as np
import matplotlib.pyplot as plt
import seaborn as sns

from sklearn.model_selection import train_test_split, KFold, cross_val_score,
GridSearchCV
from sklearn.metrics import mean_squared_error
from scipy.stats import kurtosis, skew

from sklearn.preprocessing import LabelEncoder
```

```
import xgboost as xgb
       from catboost import CatBoost, CatBoostRegressor, Pool
       from statsmodels.stats.outliers_influence import variance_inflation_factor
[493]: import warnings
       warnings.filterwarnings('ignore')
[494]: def correlation_matrix_plot(correlation_matrix):
           sns.set_theme(style="white")
           mask = np.triu(np.ones_like(correlation_matrix, dtype=bool))
           f, ax = plt.subplots(figsize=(15, 12))
           cmap = sns.diverging_palette(230, 20, as_cmap=True)
           sns.heatmap(correlation matrix, mask=mask, cmap=cmap, vmax=.3, center=0,
                        square=True, linewidths=.5, cbar_kws={"shrink": .5})
          Data Cleaning
[495]: train_df = pd.read_csv('data/train.csv')
       train_df.head(10)
[495]:
          Ιd
              MSSubClass MSZoning LotFrontage LotArea Street Alley LotShape \
                                RL
                                            65.0
                                                             Pave
           1
                       60
                                                      8450
                                                                    NaN
                                                                              Reg
                                                             Pave
       1
                       20
                                RL
                                            80.0
                                                      9600
                                                                    NaN
                                                                              Reg
       2
           3
                       60
                                R.L.
                                            68.0
                                                    11250
                                                             Pave
                                                                    NaN
                                                                              IR1
       3
           4
                       70
                                RL
                                            60.0
                                                     9550
                                                             Pave
                                                                    NaN
                                                                              IR1
       4
           5
                       60
                                RL
                                            84.0
                                                    14260
                                                             Pave
                                                                    NaN
                                                                              IR1
       5
                                R.L.
           6
                       50
                                            85.0
                                                             Pave
                                                                    NaN
                                                                              IR1
                                                    14115
       6
           7
                       20
                                            75.0
                                RL
                                                     10084
                                                             Pave
                                                                    NaN
                                                                              Reg
       7
           8
                       60
                                RL
                                             {\tt NaN}
                                                     10382
                                                             Pave
                                                                    NaN
                                                                              IR1
       8
           9
                       50
                                RM
                                            51.0
                                                     6120
                                                             Pave
                                                                    NaN
                                                                              Reg
          10
                      190
                                RL
                                            50.0
                                                      7420
                                                             Pave
                                                                    NaN
                                                                              Reg
         LandContour Utilities ... PoolArea PoolQC Fence MiscFeature MiscVal \
                 Lvl
                         AllPub
                                           0
                                                                    NaN
       0
                                                NaN
                                                        NaN
                                                                               0
       1
                 Lvl
                         AllPub ...
                                           0
                                                NaN
                                                        NaN
                                                                    NaN
                                                                               0
       2
                 Lvl
                                                        NaN
                         AllPub ...
                                           0
                                                NaN
                                                                    NaN
                                                                               0
       3
                 Lvl
                         AllPub ...
                                           0
                                                NaN
                                                        NaN
                                                                    NaN
                                                                               0
       4
                 Lvl
                         AllPub ...
                                                NaN
                                                        NaN
                                                                    NaN
                                                                               0
```

NaN

NaN

NaN

NaN

0

0

0

MnPrv

NaN

NaN

NaN

Shed

NaN

Shed

NaN

700

350

0

0

Lvl

Lvl

Lvl

Lvl

5

6

7

AllPub ...

AllPub ...

AllPub ...

AllPub ...

9		Lvl	AllPub	O N	aN NaN	NaN	0
	MoSold	YrSold	SaleType	SaleCondition	SalePrice		
0	2	2008	WD	Normal	208500		
1	5	2007	WD	Normal	181500		
2	9	2008	WD	Normal	223500		
3	2	2006	WD	Abnorml	140000		
4	12	2008	WD	Normal	250000		
5	10	2009	WD	Normal	143000		
6	8	2007	WD	Normal	307000		
7	11	2009	WD	Normal	200000		
8	4	2008	WD	Abnorml	129900		
9	1	2008	WD	Normal	118000		

[10 rows x 81 columns]

```
[496]: train_df_shape = train_df.shape print(f'Total number of samples {train_df_shape[0]} and total number of of samples {train_df_shape[1]}')
```

Total number of samples 1460 and total number of features 81

```
[497]: train_df.info()
```

<class 'pandas.core.frame.DataFrame'>
RangeIndex: 1460 entries, 0 to 1459
Data columns (total 81 columns):

Dava	COTAMINE (COCCE	or coramito,.	
#	Column	Non-Null Count	Dtype
0	Id	1460 non-null	int64
1	MSSubClass	1460 non-null	int64
2	MSZoning	1460 non-null	object
3	LotFrontage	1201 non-null	float64
4	LotArea	1460 non-null	int64
5	Street	1460 non-null	object
6	Alley	91 non-null	object
7	LotShape	1460 non-null	object
8	LandContour	1460 non-null	object
9	Utilities	1460 non-null	object
10	LotConfig	1460 non-null	object
11	LandSlope	1460 non-null	object
12	Neighborhood	1460 non-null	object
13	Condition1	1460 non-null	object
14	Condition2	1460 non-null	object
15	BldgType	1460 non-null	object
16	HouseStyle	1460 non-null	object
17	OverallQual	1460 non-null	int64
18	OverallCond	1460 non-null	int64

4.0		4400	
	YearBuilt	1460 non-nul	
		1460 non-nul	
21	RoofStyle	1460 non-nuli	•
22	RoofMatl	1460 non-nul	3
23	Exterior1st	1460 non-nul	3
	Exterior2nd	1460 non-nul	3
25	MasVnrType	588 non-null	3
26	MasVnrArea	1452 non-nul	
27	ExterQual	1460 non-nul	l object
28	ExterCond	1460 non-nul	l object
29	Foundation	1460 non-nul	l object
30	BsmtQual	1423 non-nul	l object
31	BsmtCond	1423 non-nul	l object
32	${\tt BsmtExposure}$	1422 non-nul	l object
33	BsmtFinType1	1423 non-nul	l object
34	BsmtFinSF1	1460 non-nul	l int64
35	BsmtFinType2	1422 non-nul	l object
36	BsmtFinSF2	1460 non-nul	l int64
37	BsmtUnfSF	1460 non-nul	l int64
38	TotalBsmtSF	1460 non-nul	l int64
39	Heating	1460 non-nul	l object
40	HeatingQC	1460 non-nul	l object
41	CentralAir	1460 non-nul	l object
42	Electrical	1459 non-nul	l object
43	1stFlrSF	1460 non-nul	l int64
44	2ndFlrSF	1460 non-nul	l int64
45	LowQualFinSF	1460 non-nul	l int64
46	GrLivArea	1460 non-nul	
47	BsmtFullBath	1460 non-nul	l int64
48	BsmtHalfBath	1460 non-nul	
49		1460 non-null	
50	HalfBath	1460 non-nuli	l int64
51	BedroomAbvGr	1460 non-null	
52	KitchenAbvGr	1460 non-null	
53	KitchenQual	1460 non-null	
54	TotRmsAbvGrd	1460 non-null	•
55	Functional	1460 non-null	
56	Fireplaces	1460 non-null	
57	FireplaceQu	770 non-null	
58	GarageType	1379 non-null	
59	GarageYrBlt	1379 non-nul:	-
60	GarageFinish	1379 non-nul:	
61	GarageCars		-
62	•	1460 non-nul	
	GarageArea	1460 non-nul	
63	GarageQual	1379 non-null	· ·
64 65	GarageCond	1379 non-null	· ·
65 66	PavedDrive	1460 non-null	•
66	WoodDeckSF	1460 non-null	l int64

```
67
           OpenPorchSF
                          1460 non-null
                                          int64
       68 EnclosedPorch 1460 non-null
                                          int64
          3SsnPorch
                          1460 non-null
                                          int64
       69
       70 ScreenPorch
                          1460 non-null
                                          int64
       71 PoolArea
                          1460 non-null
                                          int64
       72 PoolQC
                          7 non-null
                                          object
       73 Fence
                          281 non-null
                                          object
       74 MiscFeature
                          54 non-null
                                          object
       75 MiscVal
                          1460 non-null
                                          int64
       76 MoSold
                          1460 non-null
                                          int64
       77 YrSold
                         1460 non-null
                                          int64
       78 SaleType
                         1460 non-null
                                          object
       79 SaleCondition 1460 non-null
                                          object
       80 SalePrice
                          1460 non-null
                                          int64
      dtypes: float64(3), int64(35), object(43)
      memory usage: 924.0+ KB
[498]: numerical_cols = train_df.select_dtypes(include = ['float', 'int64']).columns
      nominal_cols = train_df.select_dtypes(include = ['object']).columns
      print(f'Number of Numerical data features {len(numerical_cols)}')
      print(f'Number of Nominal data features {len(nominal_cols)}')
      Number of Numerical data features 38
      Number of Nominal data features 43
      2.1 Handling Missing Value
[499]: def find_null_value(df):
          total = df.isnull().sum().sort_values(ascending=False)
          percent = (df.isnull().sum() / df.isnull().count()).
        ⇔sort_values(ascending=False)
          missing_data = pd.concat([total, percent], axis=1, keys=['Total',_

¬'Percent'])
          return missing_data
[500]: missing_data = find_null_value(train_df)
      missing_data.head(20)
```

```
[500]:
                     Total
                            Percent
                      1453 0.995205
      PoolQC
      MiscFeature
                     1406 0.963014
      Alley
                     1369
                           0.937671
      Fence
                      1179
                           0.807534
      MasVnrType
                      872 0.597260
      FireplaceQu
                       690
                           0.472603
      LotFrontage
                       259
                           0.177397
```

```
GarageYrBlt
                 81 0.055479
GarageCond
                 81 0.055479
GarageType
                 81
                    0.055479
GarageFinish
                 81
                    0.055479
GarageQual
                 81
                    0.055479
BsmtFinType2
                    0.026027
                 38
BsmtExposure
                 38
                    0.026027
BsmtQual
                 37
                    0.025342
BsmtCond
                 37 0.025342
BsmtFinType1
                 37 0.025342
MasVnrArea
                  8 0.005479
Electrical
                  1
                    0.000685
Ιd
                    0.000000
```

2.1.1 Remove features which null value percent > 80%

```
[501]: remove_cols = missing_data[missing_data['Percent'] > 0.8].index
    print(f'{remove_cols}')

Index(['PoolQC', 'MiscFeature', 'Alley', 'Fence'], dtype='object')

[502]: train_df = train_df.drop(columns = remove_cols, axis = 1)

[503]: missing_data = find_null_value(train_df)
    missing_data.head(20)
```

```
[503]:
                    Total
                            Percent
      MasVnrType
                      872 0.597260
      FireplaceQu
                      690
                           0.472603
      LotFrontage
                      259
                           0.177397
      GarageCond
                       81
                           0.055479
      GarageYrBlt
                       81
                           0.055479
      GarageFinish
                       81
                           0.055479
      GarageQual
                       81 0.055479
      GarageType
                       81
                           0.055479
      BsmtFinType2
                       38 0.026027
      BsmtExposure
                       38
                           0.026027
      BsmtFinType1
                       37
                           0.025342
      BsmtCond
                       37
                           0.025342
      BsmtQual
                       37
                           0.025342
      MasVnrArea
                        8 0.005479
                           0.000685
      Electrical
      BsmtFullBath
                        0.000000
      Functional
                          0.000000
      TotRmsAbvGrd
                        0.000000
      GrLivArea
                           0.000000
      HalfBath
                        0.000000
```

We have remove the null values. We will impute top 2 nominal features which null values percent > 40 %.

2.1.2 Imputation

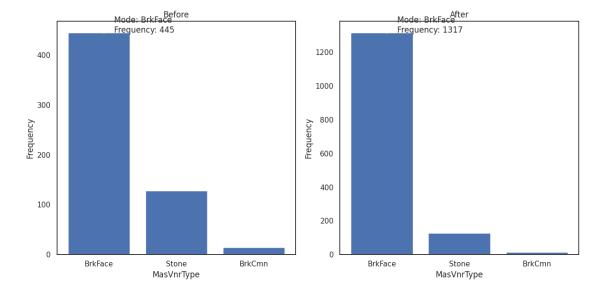
I will test different approaches to replace null values and discuss its pros and cons.

Mode Imputation

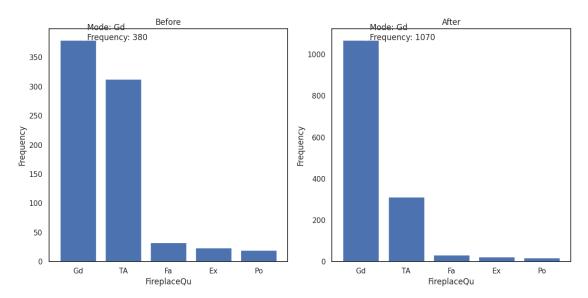
```
[504]: def plot_mode_imputation(before_df, after_df, column):
           fig, axs = plt.subplots(1, 2, figsize=(12, 6))
           axs[0].bar(before_df[column].value_counts().index,
                      before_df[column].value_counts().values)
           axs[0].set title('Before')
           axs[0].set_xlabel(column)
           axs[0].set_ylabel('Frequency')
           before_mode = before_df[column].mode()[0]
           most_frequent = before_df[column].value_counts().iloc[0]
           axs[0].annotate(f'Mode: {before mode}\nFrequency: {most_frequent}',
                           xy=(0, most_frequent), xytext=(0.2, most_frequent + 0.1),
                           arrowprops=dict(arrowstyle='->'))
           after_df[column].fillna(before_mode, inplace=True)
           axs[1].bar(after df[column].value counts().index,
                      after_df[column].value_counts().values)
           axs[1].set_title('After')
           axs[1].set_xlabel(column)
           axs[1].set_ylabel('Frequency')
           after_mode = after_df[column].mode()[0]
           most_frequent = after_df[column].value_counts().iloc[0]
           print(most_frequent)
           axs[1].annotate(f'Mode: {after_mode}\nFrequency: {most_frequent}',
                           xy=(after_mode, most_frequent), xytext=(0.2, most_frequent_
        \hookrightarrow+ 0.1),
                           arrowprops=dict(arrowstyle='->'))
           plt.tight_layout()
           plt.show()
```

```
[505]: train_df_clone = train_df.copy()

[506]: plot_mode_imputation(train_df, train_df_clone, 'MasVnrType')
    plot_mode_imputation(train_df, train_df_clone, 'FireplaceQu')
```



1070



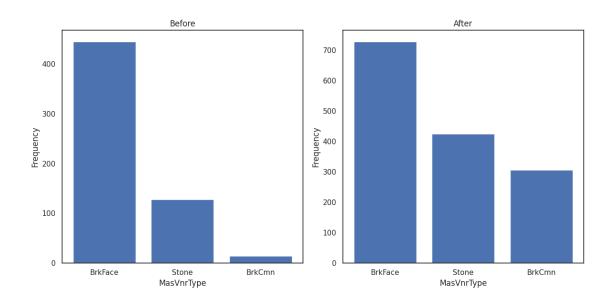
Pros - For categorical data where mean or median cannot be calculated, mode is a good statistical measure for central tendency. - BrkFace and Gd are the most frequent feature sample in the data. - It is straightforward, it's also computationally inexpensive, making it feasible for large datasets.

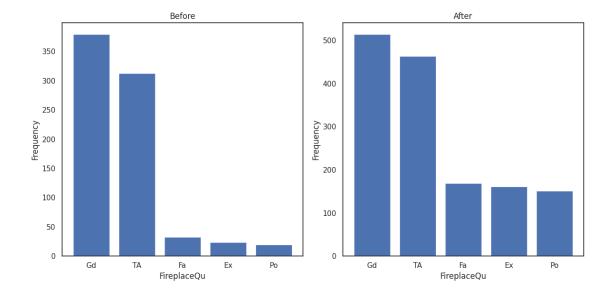
Cons - Mode imputation might lead the data to have bias to most frequent feature value, which might lead data imbalance when we train the model. - It can hurt the variability of the data. - If the number of missing values is high, filling them all with the mode can disproportionately inflate the frequency of that category, leading to incorrect analysis or predictions.

Conclusion, I will choose to go with Random Imputation because the above reasons.

```
[511]: train_df_clone = train_df.copy()

[512]: plot_random_imputation(train_df, train_df_clone, 'MasVnrType')
    plot_random_imputation(train_df, train_df_clone, 'FireplaceQu')
```





• Pros

- All unique samples will be randomly selected as a fair choice.
- It can maintain the original distribution and variance of the dataset because it uses actual observed values for imputation.

• Cons

- Because the imputation is random, this may add noise into the dataset, especially if the missing values are not completely at random.
- The imputation is stochastic, leading to different results every time the imputation is carried out, which might not be desirable in all scenarios.

```
[513]: | train_df = random_imputation(train_df, 'MasVnrType')
       train_df = random_imputation(train_df, 'FireplaceQu')
[514]: missing_data = find_null_value(train_df)
       missing_data.head(20)
[514]:
                     Total
                             Percent
      LotFrontage
                       259 0.177397
       GarageType
                        81 0.055479
       GarageCond
                        81 0.055479
       GarageYrBlt
                        81
                            0.055479
       GarageFinish
                        81
                            0.055479
       GarageQual
                            0.055479
       BsmtFinType2
                        38
                            0.026027
       BsmtExposure
                        38
                            0.026027
       BsmtFinType1
                        37 0.025342
       BsmtCond
                        37 0.025342
       BsmtQual
                        37 0.025342
      MasVnrArea
                         8 0.005479
       Electrical
                         1 0.000685
       WoodDeckSF
                         0.000000
      KitchenAbvGr
                         0.000000
      LowQualFinSF
                         0 0.000000
       GrLivArea
                         0 0.000000
      BsmtFullBath
                         0 0.000000
      BsmtHalfBath
                         0 0.000000
      FullBath
                         0 0.000000
      Median Imputation I will use Median Imputation which is more robust to outliers.
[515]: train df['LotFrontage'].fillna(train_df['LotFrontage'].median(), inplace=True)
      Drop NA
[516]: train_df = train_df.dropna()
[517]: missing_data = find_null_value(train_df)
       missing_data.head(20)
[517]:
                     Total
                            Percent
       Ιd
                         0
                                0.0
      HalfBath
                         0
                                0.0
                         0
       FireplaceQu
                                0.0
      Fireplaces
                         0
                                0.0
      Functional
                         0
                                0.0
       TotRmsAbvGrd
                         0
                                0.0
       KitchenQual
                         0
                                0.0
```

```
KitchenAbvGr
                   0
                           0.0
                           0.0
BedroomAbvGr
                   0
FullBath
                   0
                           0.0
HeatingQC
                   0
                           0.0
BsmtHalfBath
                   0
                           0.0
BsmtFullBath
                   0
                           0.0
GrLivArea
                   0
                           0.0
LowQualFinSF
                   0
                           0.0
2ndFlrSF
                   0
                           0.0
1stFlrSF
                   0
                           0.0
Electrical
                   0
                           0.0
GarageType
                   0
                           0.0
GarageYrBlt
                   0
                           0.0
```

Drop Id

Total number of missing data in the dataset 0

3 Exploratory Data Analysis (EDA)

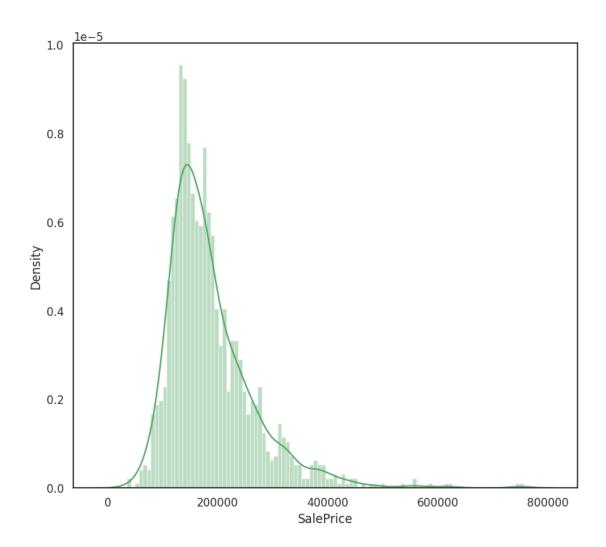
3.0.1 Target Data Distribution (Sale Price Data Distribution)

We will see its distribution and the outliers through the graph as well as from Skewiness and Kurtosis

```
[521]: print(train_df.SalePrice.describe())
plt.figure(figsize=(9, 8))
sns.distplot(train_df.SalePrice, color='g', bins=100, hist_kws={'alpha': 0.4});

print(f' median sale price according to the dataset {np.median(train_df.
SalePrice.values)}')
```

```
1338.000000
count
         186761.782511
mean
std
          78913.847668
min
          35311.000000
25%
         135000.000000
50%
         168500.000000
75%
         220000.000000
         755000.000000
max
Name: SalePrice, dtype: float64
median sale price according to the dataset 168500.0
```



Skewiness and Kurtosis

```
[522]: print(f' Skewiness {np.round(skew(train_df.SalePrice), 2)}')
print(f' Kurtosis {np.round(kurtosis(train_df.SalePrice), 2)}')
```

Skewiness 1.94 Kurtosis 6.79

- Skewness of 1.94: The data distribution is significantly skewed to the right. It indicates that the tail on the right side of the distribution is long towards the lower end of the distribution.
- Kurtosis of 6.79: It indicates that the data distribution has heavier tails and a sharper peak than a normal distribution. There might be more extreme values in the dataset than a normally distributed dataset.

3.1 Find Correlation

It is important to understand the correlation between features and target. It is unlikely to need all the features we have for the prediction the target value.

```
[523]: numerical_cols = train_df.select_dtypes(include = ['float', 'int64']).columns
```

3.1.1 Variant Inflation Factor (VIF)

```
feature
                            VIF
33
          MiscVal 1.034466e+00
30
        3SsnPorch 1.041128e+00
32
         PoolArea 1.121488e+00
31
      ScreenPorch 1.210673e+00
17
     BsmtHalfBath 1.235575e+00
29
    EnclosedPorch
                  1.446397e+00
28
      OpenPorchSF 1.901133e+00
7
       MasVnrArea
                  1.930214e+00
27
       WoodDeckSF
                  1.958869e+00
2
          LotArea 2.626542e+00
23
      Fireplaces 3.148739e+00
19
         HalfBath 3.689704e+00
16
    BsmtFullBath 3.855628e+00
0
      MSSubClass 4.861169e+00
34
           MoSold 6.704515e+00
1
     LotFrontage 1.763438e+01
18
         FullBath 2.871363e+01
26
      GarageArea 3.421433e+01
36
        SalePrice
                  3.452003e+01
20
    BedroomAbvGr
                   3.471463e+01
25
       GarageCars
                  4.113357e+01
4
      OverallCond 4.726799e+01
21
    KitchenAbvGr 5.313573e+01
3
     OverallQual 8.347544e+01
22
    TotRmsAbvGrd 8.528044e+01
6
    YearRemodAdd 2.474417e+04
5
        YearBuilt 2.700007e+04
35
           YrSold 2.734012e+04
24
      GarageYrBlt
                   2.870470e+04
         2ndFlrSF
13
                            inf
11
      TotalBsmtSF
                            inf
9
       BsmtFinSF2
                            inf
10
        BsmtUnfSF
                            inf
15
        GrLivArea
                            inf
12
         1stFlrSF
                            inf
```

```
8 BsmtFinSF1 inf
14 LowQualFinSF inf
```

The last 8 features with "inf" VIF are near perfectly collinear with each other. For example, TotalBsmtSF might be the sum of BsmtFinSF1, BsmtFinSF2, and BsmtUnfSF, leading to perfect collinearity. So, we need to remove one some of them to break collinearlity. We will drop some similiar columns to reduce collinearlity.

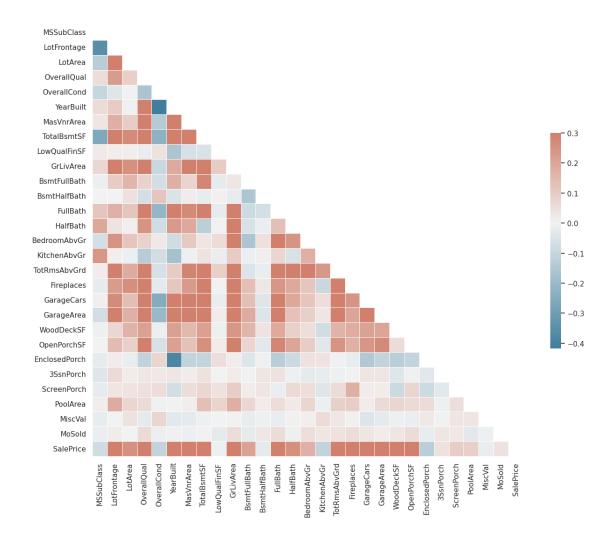
```
feature
                            VIF
26
          MiscVal
                       1.028216
23
        3SsnPorch
                       1.038339
     LowQualFinSF
8
                       1.083549
25
         PoolArea
                       1.111718
     BsmtHalfBath
11
                       1.145886
24
      ScreenPorch
                       1.180588
    {\tt EnclosedPorch}
22
                       1.278575
6
       MasVnrArea
                       1.873677
21
      OpenPorchSF
                       1.883200
20
       WoodDeckSF
                       1.929193
10
     BsmtFullBath
                       2.286867
2
          LotArea
                       2.581617
13
                       2.912953
         HalfBath
17
       Fireplaces
                       2.956167
0
       MSSubClass
                       4.758017
27
            MoSold
                       6.698663
      LotFrontage
                      17.349513
1
7
      TotalBsmtSF
                     23.104223
12
         FullBath
                     23.299146
19
       GarageArea
                     31.193014
4
      OverallCond
                     32.654841
28
        SalePrice
                      32.980410
14
     {\tt BedroomAbvGr}
                      33.041393
18
       GarageCars
                     40.016892
     KitchenAbvGr
                     50.211861
15
9
        GrLivArea
                     67.231348
3
      OverallQual
                     78.184658
16
     {\tt TotRmsAbvGrd}
                      84.253237
5
        YearBuilt
                    147.374043
```

3.1.2 Correlation Matrix

[527]: correlation_matrix = train_df.select_dtypes(include = ['float', 'int64']).corr()
 print(correlation_matrix['SalePrice'].sort_values(ascending=False))
 correlation_matrix_plot(correlation_matrix)

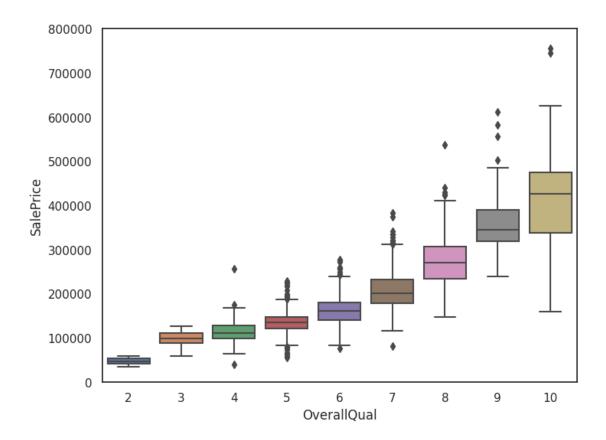
SalePrice 1.000000 OverallQual 0.783546 GrLivArea 0.711706 GarageCars 0.640154 GarageArea 0.607535 TotalBsmtSF0.602042 FullBath 0.569313 TotRmsAbvGrd 0.551821 YearBuilt 0.504297 MasVnrArea 0.465811 Fireplaces 0.445434 LotFrontage 0.327835 OpenPorchSF 0.322786 WoodDeckSF 0.305983 HalfBath 0.258175 LotArea 0.254757 BsmtFullBath 0.209695 BedroomAbvGr 0.169266 ScreenPorch 0.096624 PoolArea 0.091881 3SsnPorch 0.042159 MoSold 0.041310 LowQualFinSF -0.009992 MiscVal -0.016990 BsmtHalfBath -0.030175 MSSubClass -0.079599 OverallCond -0.108627 KitchenAbvGr -0.111408 EnclosedPorch -0.127385

Name: SalePrice, dtype: float64



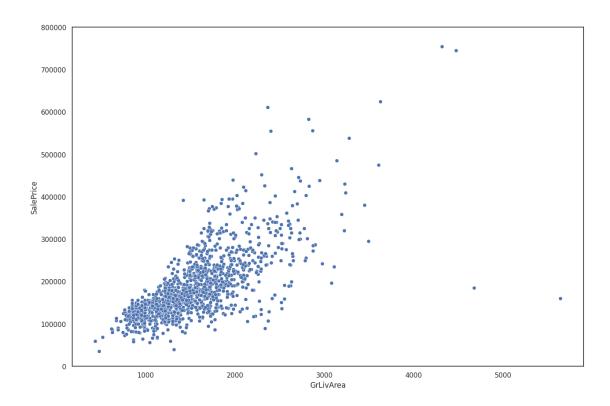
We can see that there are some features like OverallQual, GrLivArea, GarageCars, GarageArea, TotalBsmtSF has strong positive correlation with SalePrice.

```
[528]: var = 'OverallQual'
data = pd.concat([train_df['SalePrice'], train_df[var]], axis=1)
f, ax = plt.subplots(figsize=(8, 6))
fig = sns.boxplot(x=var, y="SalePrice", data=data)
fig.axis(ymin=0, ymax=800000);
```

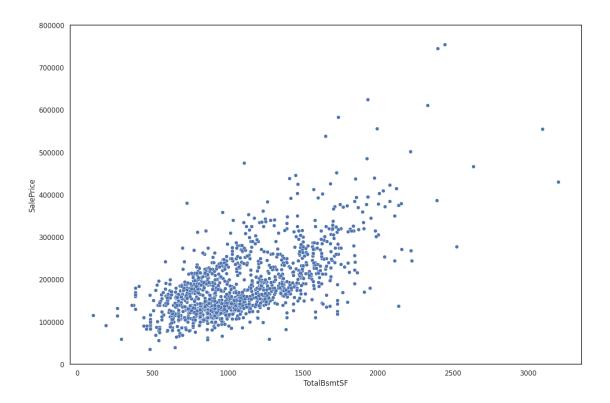


OverallQual and SalePrice seem to have linear correlation. It seems that higher quality demands higher prices.

```
[529]: var = 'GrLivArea'
data = pd.concat([train_df['SalePrice'], train_df[var]], axis=1)
f, ax = plt.subplots(figsize=(15, 10))
fig = sns.scatterplot(x=var, y="SalePrice", data=data)
fig.axis(ymin=0, ymax=800000);
```



GrLivArea and SalePrice seem to have linear relationship but there are outliers at the bottom right. There are outliers which suggest largest GrLivArea with low prices. We can remove them.



3.1.3 Chi-squared test

I will use a statistical test, chi-squared tests to for categorial features.

```
[532]: def chi2_test(df):
    X = df[df.select_dtypes(include = ['object']).columns]

    chi2_data = pd.DataFrame()
    chi2_data["feature"] = X.columns
    chi2s = []
    pvalues = []
    for col in X.columns:
        # For categorical feature
        chi2, p_value, _, _ = stats.chi2_contingency(pd.crosstab(df[col], u))

        chi2s.append(chi2)
        pvalues.append(p_value)

        chi2_data['chi2'] = chi2s
        chi2_data['p_value'] = pvalues
        return chi2_data
```

```
[533]: chi2data = chi2_test(train_df)
print(chi2data.sort_values(by = 'p_value'))
```

```
feature
                             chi2
                                        p_value
17
                                   1.294357e-42
        ExterQual
                     2811.486875
37
         SaleType
                     6386.934740
                                   1.067397e-40
28
       Electrical
                     3423.789697
                                   4.270613e-34
21
         BsmtCond
                     2653.607777
                                   1.604465e-31
38
    SaleCondition
                     4065.333763
                                   6.030287e-30
                                   1.878083e-28
1
           Street
                     1088.427302
0
         MSZoning
                     3276.414434
                                   1.221275e-25
29
      KitchenQual
                     2502.096429
                                   3.361517e-22
         BsmtQual
20
                     2496.248240
                                   7.214869e-22
       GarageQual
34
                     3031.992059
                                   4.999571e-14
         LotShape
2
                     2329.826900
                                   2.219481e-13
33
     GarageFinish
                     1548.351856
                                   2.725970e-09
     Neighborhood
7
                    15694.784597
                                   4.342533e-07
22
     BsmtExposure
                     2162.762636
                                   7.021146e-07
27
       CentralAir
                      779.355259
                                   1.020573e-05
       Foundation
19
                     2662.532706
                                   3.994538e-03
32
       GarageType
                     3225.220808
                                   4.418462e-02
5
        LotConfig
                     2584.013322
                                   5.716175e-02
14
      Exterior1st
                     8173.908469
                                   1.350918e-01
16
       MasVnrType
                     1285.856431
                                   1.579424e-01
25
          Heating
                                   3.088582e-01
                     1883.884503
3
      LandContour
                     1864.807573
                                   4.254058e-01
11
       HouseStyle
                     4301.299244
                                   6.021399e-01
6
        LandSlope
                     1210.727292
                                   6.908929e-01
31
      FireplaceQu
                     2380.592378
                                   9.043710e-01
       Condition2
9
                     4161.107640
                                   9.631585e-01
23
     BsmtFinType1
                     2948.777393
                                   9.653176e-01
26
        HeatingQC
                     2299.034333
                                   9.939671e-01
18
        ExterCond
                     1700.233233
                                   9.951670e-01
15
      Exterior2nd
                     8889.192245
                                   9.976803e-01
35
       GarageCond
                     2214.156382
                                   9.999257e-01
       PavedDrive
36
                     1053.710015
                                   9.999410e-01
10
         BldgType
                     2188.463916
                                   9.999859e-01
24
     BsmtFinType2
                     2679.205844
                                   1.000000e+00
12
        RoofStyle
                     2549.501436
                                   1.000000e+00
30
       Functional
                     2747.202868
                                   1.000000e+00
8
       Condition1
                     3885.476519
                                   1.000000e+00
13
         RoofMatl
                     2794.703218
                                   1.000000e+00
        Utilities
                      221.832709
                                   1.000000e+00
```

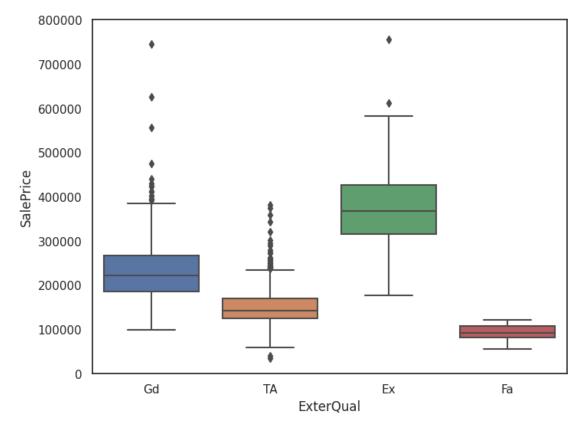
I will remove the features which has p_value is closer to 1 because which is unlikely to have relation with the target variable.

```
[534]: cols_to_remove = chi2_data[chi2_data['p_value'] > 0.65]['feature']
```

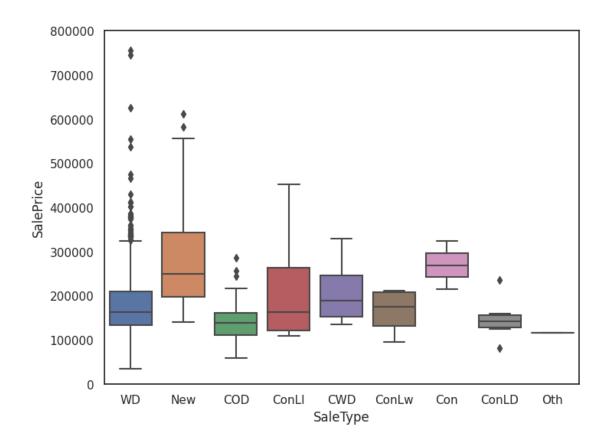
```
[535]: print(f'These are the features which have p_value closer to 1 {cols_to_remove.
        ⇔values}')
      These are the features which have p_value closer to 1 ['Utilities' 'LandSlope'
      'Condition1' 'Condition2' 'BldgType' 'RoofStyle'
       'RoofMatl' 'Exterior2nd' 'ExterCond' 'BsmtFinType1' 'BsmtFinType2'
       'HeatingQC' 'Functional' 'GarageCond' 'PavedDrive']
[536]: train_df = train_df.drop(columns = cols_to_remove, axis = 1)
[537]: train_df.columns
[537]: Index(['MSSubClass', 'MSZoning', 'LotFrontage', 'LotArea', 'Street',
              'LotShape', 'LandContour', 'LotConfig', 'Neighborhood', 'HouseStyle',
              'OverallQual', 'OverallCond', 'YearBuilt', 'Exterior1st', 'MasVnrType',
              'MasVnrArea', 'ExterQual', 'Foundation', 'BsmtQual', 'BsmtCond',
              'BsmtExposure', 'TotalBsmtSF', 'Heating', 'CentralAir', 'Electrical',
              'LowQualFinSF', 'GrLivArea', 'BsmtFullBath', 'BsmtHalfBath', 'FullBath',
              'HalfBath', 'BedroomAbvGr', 'KitchenAbvGr', 'KitchenQual',
              'TotRmsAbvGrd', 'Fireplaces', 'FireplaceQu', 'GarageType',
              'GarageFinish', 'GarageCars', 'GarageArea', 'GarageQual', 'WoodDeckSF',
              'OpenPorchSF', 'EnclosedPorch', '3SsnPorch', 'ScreenPorch', 'PoolArea',
              'MiscVal', 'MoSold', 'SaleType', 'SaleCondition', 'SalePrice'],
             dtype='object')
[538]: chi2data = chi2_test(train_df)
      print(chi2data.sort_values(by = 'p_value'))
                feature
                                 chi2
                                            p_value
                          2811.486875 1.294357e-42
      9
              ExterQual
      22
               SaleType
                          6386.934740
                                       1.067397e-40
      16
             Electrical
                          3423.789697
                                       4.270613e-34
               BsmtCond
                          2653.607777
                                       1.604465e-31
      12
      23 SaleCondition
                          4065.333763 6.030287e-30
      1
                 Street
                          1088.427302 1.878083e-28
      0
               MSZoning
                          3276.414434 1.221275e-25
      17
            KitchenQual
                          2502.096429 3.361517e-22
      11
               BsmtQual
                          2496.248240 7.214869e-22
      21
             GarageQual
                          3031.992059
                                       4.999571e-14
      2
               LotShape
                          2329.826900 2.219481e-13
           GarageFinish
      20
                          1548.351856
                                       2.725970e-09
      5
           Neighborhood 15694.784597 4.342533e-07
      13
           BsmtExposure
                          2162.762636
                                       7.021146e-07
      15
             CentralAir
                                       1.020573e-05
                          779.355259
      10
             Foundation
                          2662.532706
                                       3.994538e-03
      19
             GarageType
                          3225.220808 4.418462e-02
      4
              LotConfig
                          2584.013322 5.716175e-02
      7
            Exterior1st
                          8173.908469 1.350918e-01
```

```
MasVnrType
                          1285.856431 1.579424e-01
      14
                Heating
                          1883.884503 3.088582e-01
      3
            LandContour
                          1864.807573 4.254058e-01
      6
             HouseStyle
                          4301.299244
                                       6.021399e-01
            FireplaceQu
                          2380.592378 9.043710e-01
      18
[539]: var = 'ExterQual'
      data = pd.concat([train_df['SalePrice'], train_df[var]], axis=1)
      f, ax = plt.subplots(figsize=(8, 6))
      fig = sns.boxplot(x=var, y="SalePrice", data=data)
      fig.axis(ymin=0, ymax=800000);
```

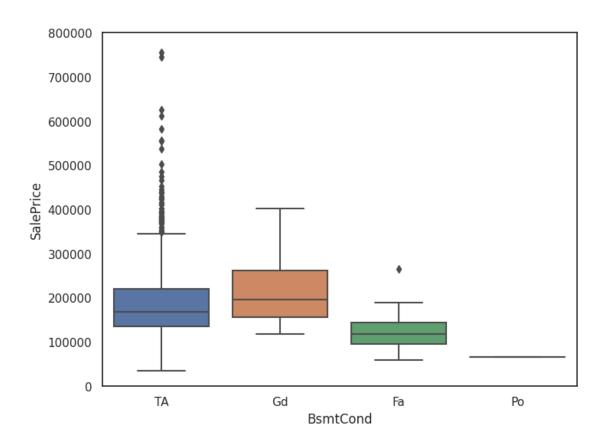
8



```
[540]: var = 'SaleType'
       data = pd.concat([train_df['SalePrice'], train_df[var]], axis=1)
       f, ax = plt.subplots(figsize=(8, 6))
       fig = sns.boxplot(x=var, y="SalePrice", data=data)
       fig.axis(ymin=0, ymax=800000);
```



```
[541]: var = 'BsmtCond'
data = pd.concat([train_df['SalePrice'], train_df[var]], axis=1)
f, ax = plt.subplots(figsize=(8, 6))
fig = sns.boxplot(x=var, y="SalePrice", data=data)
fig.axis(ymin=0, ymax=800000);
```



2]: t	rain_df.head	()							
2]:	MSSubClass	MSZoning	LotFrontage	Lo	tArea	Street	LotShape	LandContour	\
0	60	RL	65.0)	8450	Pave	Reg	Lvl	
1	20	RL	80.0)	9600	Pave	Reg	Lvl	
2	60	RL	68.0)	11250	Pave	IR1	Lvl	
3	70	RL	60.0)	9550	Pave	IR1	Lvl	
4	60	RL	84.0)	14260	Pave	IR1	Lvl	
	LotConfig N	eighborhood	HouseStyle	·	OpenI	PorchSF	Enclosed	lPorch ∖	
0	Inside	CollgCr	2Story	·	_	61		0	
1	FR2	Veenker	1Story	·		0		0	
2	Inside	CollgCr	2Story	·		42		0	
3	Corner	Crawfor	2Story	·		35		272	
4	FR2	NoRidge	2Story	·		84		0	
	3SsnPorch	ScreenPorch	PoolArea	Misc	Val Mo	oSold S	aleType Sa	aleCondition	\
0	0	0	0		0	2	WD	Normal	
1	0	0	0		0	5	WD	Normal	
2	0	0	0		0	9	WD	Normal	
3	0	0	0		0	2	WD	Abnorml	

4 0 0 0 0 12 WD Normal

SalePrice

- 0 208500
- 1 181500
- 2 223500
- 3 140000
- 4 250000

[5 rows x 53 columns]

EDA Summary

- We have analyse the data using Correlation Matrix, Variance Inflation Factor (VIF) and statistical test, Chi-squared test to remove features which might not helpful for modelling.
- Now, we have left with 53 features.

4 Modelling

4.0.1 Model Choices

•

XGBoost

 XGBoost is an optimized gradient boosting library designed for speed and performance, often used for supervised learning tasks.

•

CatBoost

- CatBoost is a gradient boosting library that excels in handling categorical features and aims for ease of use with robust, out-of-the-box performance.

4.0.2 Evaluation Metrics

We will use the following metric - RMSE (Root Mean Squared Error) is a measure of the average magnitude of the model's errors, treating all errors equally, regardless of their direction or size.

4.0.3 Experiments

My experiments are the following: 1. Train XGBoost 2. Hyperparameter Tuning (XGBoost) 3. Train CatBoost 4. Hyperparameter Tuning (CatBoost)

4.0.4 Feature Engineering

Label Encoding I will transform the categorical into numerical format using label encoding.

[543]: train_cate_df = train_df.copy()

```
[544]: cate_cols = train_cate_df.select_dtypes(include = ['object']).columns
       for c in cate_cols:
           lbl = LabelEncoder()
           lbl.fit(list(train_cate_df[c].values))
           train_cate_df[c] = lbl.transform(list(train_cate_df[c].values))
       print('Shape all_data: {}'.format(train_cate_df.shape))
      Shape all_data: (1336, 53)
[545]: train_cate_df[cate_cols].head()
[545]:
                             LotShape
                                        LandContour
                                                      LotConfig
                                                                  Neighborhood
          MSZoning
                     Street
                  3
                                                   3
                  3
                          1
                                     3
                                                   3
                                                               2
                                                                             24
       1
                  3
                                                                              5
       2
                          1
                                     0
                                                   3
                                                               4
       3
                  3
                          1
                                     0
                                                   3
                                                               0
                                                                              6
                  3
                          1
                                     0
                                                   3
                                                               2
                                                                             15
          HouseStyle Exterior1st
                                     MasVnrType ExterQual
                                                                 Heating
                                                                          CentralAir
       0
                                 11
       1
                    2
                                  7
                                               1
                                                           3
                                                                       0
                                                                                    1
                                                             ...
                    5
                                                           2
       2
                                 11
                                               1
                                                                       0
                                                                                    1
       3
                    5
                                 12
                                               2
                                                           3
                                                                       0
                                                                                    1
                    5
                                                           2
                                                                                    1
                                 11
                                               1
                                                                       0
                                                                              GarageQual
          Electrical
                       KitchenQual
                                     FireplaceQu
                                                   GarageType
                                                               GarageFinish
       0
                    4
                                                                                        4
                                                1
                                                            1
                    4
                                  3
                                                4
                                                            1
                                                                            1
                                                                                        4
       1
       2
                    4
                                  2
                                                4
                                                            1
                                                                            1
                                                                                        4
       3
                    4
                                  2
                                                2
                                                            5
                                                                            2
                                                                                        4
                    4
                                  2
                                                4
                                                             1
                                                                            1
          SaleType SaleCondition
       0
       1
                  8
                                  4
       2
                  8
       3
                  8
                                  0
                  8
       [5 rows x 24 columns]
[546]: train_df.columns
[546]: Index(['MSSubClass', 'MSZoning', 'LotFrontage', 'LotArea', 'Street',
               'LotShape', 'LandContour', 'LotConfig', 'Neighborhood', 'HouseStyle',
```

'OverallQual', 'OverallCond', 'YearBuilt', 'Exterior1st', 'MasVnrType',

```
'MasVnrArea', 'ExterQual', 'Foundation', 'BsmtQual', 'BsmtCond',
'BsmtExposure', 'TotalBsmtSF', 'Heating', 'CentralAir', 'Electrical',
'LowQualFinSF', 'GrLivArea', 'BsmtFullBath', 'BsmtHalfBath', 'FullBath',
'HalfBath', 'BedroomAbvGr', 'KitchenAbvGr', 'KitchenQual',
'TotRmsAbvGrd', 'Fireplaces', 'FireplaceQu', 'GarageType',
'GarageFinish', 'GarageCars', 'GarageArea', 'GarageQual', 'WoodDeckSF',
'OpenPorchSF', 'EnclosedPorch', '3SsnPorch', 'ScreenPorch', 'PoolArea',
'MiscVal', 'MoSold', 'SaleType', 'SaleCondition', 'SalePrice'],
dtype='object')
```

```
[611]: train_all = train_cate_df.copy()
```

4.0.5 Evaluation Metrics

Two helper functions to evaluate the performace using Cross Validation RMSLE and RMSE.

4.1 Model Training

4.1.1 XGBoost

Data Preparation

```
[614]: print(f' Training Features {X_train.shape}')
    print(f' Training Target {y_train.shape}')
    print(f' Test Feature {X_test.shape}')
    print(f' Test Target {y_test.shape}')
```

```
Training Features (1068, 52)
Training Target (1068,)
```

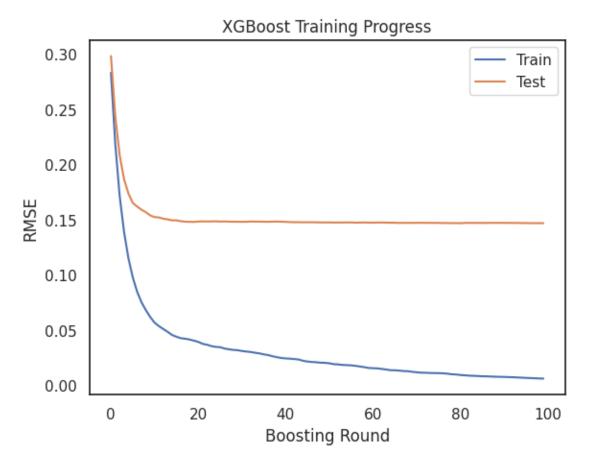
```
Train
[615]: model_xgb = xgb.XGBRegressor(colsample_bytree=0.4603, gamma=0.0468,
                                    learning_rate=0.05, max_depth=3,
                                    min_child_weight=1.7817, n_estimators=2200,
                                    reg_alpha=0.4640, reg_lambda=0.8571,
                                    subsample=0.5213, silent=1,
                                    random_state = 7, nthread = -1)
[620]: n_{folds} = 5
       score = rmsle_cv(model_xgb, X_train, y_train, n_folds)
       print("XGBoost score: {:.4f} ({:.4f})\n".format(score.mean(), score.std()))
      XGBoost score: 0.1213 (0.0177)
[621]: model_xgb.fit(X_train, y_train)
[621]: XGBRegressor(base_score=None, booster=None, callbacks=None,
                    colsample bylevel=None, colsample bynode=None,
                    colsample_bytree=0.4603, device=None, early_stopping_rounds=None,
                    enable categorical=False, eval metric=None, feature types=None,
                    gamma=0.0468, grow_policy=None, importance_type=None,
                    interaction constraints=None, learning rate=0.05, max bin=None,
                    max_cat_threshold=None, max_cat_to_onehot=None,
                    max_delta_step=None, max_depth=3, max_leaves=None,
                    min_child_weight=1.7817, missing=nan, monotone_constraints=None,
                    multi_strategy=None, n_estimators=2200, n_jobs=None, nthread=-1,
                    num_parallel_tree=None, ...)
[616]: dtrain = xgb.DMatrix(X_train, label=y_train)
       dtest = xgb.DMatrix(X_test, label=y_test)
       params = {'objective': 'reg:squarederror', 'eval_metric': 'rmse'}
       evals = [(dtrain, 'train'), (dtest, 'eval')]
       evals result = {}
       bst = xgb.train(params, dtrain, num_boost_round=100, evals=evals,_
        ⇔evals result=evals result)
      [0]
              train-rmse:0.28336
                                       eval-rmse:0.29853
      [1]
              train-rmse:0.21821
                                       eval-rmse:0.24315
      [2]
              train-rmse:0.17152
                                       eval-rmse:0.20865
      [3]
              train-rmse:0.13899
                                       eval-rmse:0.18680
              train-rmse:0.11514
      [4]
                                      eval-rmse:0.17384
```

Test Feature (268, 52) Test Target (268,)

```
[5]
                                  eval-rmse:0.16528
        train-rmse: 0.09780
[6]
        train-rmse:0.08468
                                  eval-rmse:0.16199
[7]
        train-rmse:0.07520
                                  eval-rmse:0.15914
[8]
        train-rmse:0.06801
                                  eval-rmse:0.15688
[9]
        train-rmse:0.06178
                                  eval-rmse:0.15393
                                  eval-rmse:0.15242
[10]
        train-rmse:0.05669
[11]
        train-rmse:0.05350
                                  eval-rmse:0.15214
        train-rmse:0.05091
[12]
                                  eval-rmse:0.15095
[13]
        train-rmse:0.04834
                                  eval-rmse:0.15036
[14]
        train-rmse:0.04550
                                  eval-rmse:0.14948
[15]
        train-rmse:0.04392
                                  eval-rmse:0.14954
[16]
        train-rmse:0.04261
                                  eval-rmse:0.14870
[17]
        train-rmse:0.04212
                                  eval-rmse:0.14831
[18]
        train-rmse:0.04142
                                  eval-rmse:0.14815
[19]
        train-rmse:0.04037
                                  eval-rmse:0.14808
[20]
        train-rmse: 0.03930
                                  eval-rmse:0.14843
[21]
        train-rmse:0.03749
                                  eval-rmse:0.14857
[22]
        train-rmse:0.03668
                                  eval-rmse:0.14845
[23]
        train-rmse:0.03546
                                  eval-rmse:0.14855
Γ241
        train-rmse:0.03474
                                  eval-rmse:0.14860
[25]
        train-rmse:0.03447
                                  eval-rmse:0.14841
[26]
        train-rmse:0.03324
                                  eval-rmse:0.14850
[27]
        train-rmse:0.03257
                                  eval-rmse:0.14835
[28]
        train-rmse:0.03199
                                  eval-rmse:0.14826
[29]
        train-rmse:0.03174
                                  eval-rmse:0.14825
[30]
        train-rmse:0.03100
                                  eval-rmse:0.14821
[31]
        train-rmse:0.03053
                                  eval-rmse:0.14821
[32]
        train-rmse:0.03010
                                  eval-rmse:0.14848
[33]
        train-rmse:0.02943
                                  eval-rmse:0.14835
[34]
        train-rmse:0.02882
                                  eval-rmse:0.14835
        train-rmse:0.02795
[35]
                                  eval-rmse:0.14826
[36]
        train-rmse:0.02732
                                  eval-rmse:0.14820
[37]
        train-rmse:0.02626
                                  eval-rmse:0.14834
[38]
        train-rmse:0.02540
                                  eval-rmse:0.14841
[39]
        train-rmse:0.02467
                                  eval-rmse:0.14829
                                  eval-rmse:0.14814
[40]
        train-rmse:0.02428
[41]
        train-rmse:0.02401
                                  eval-rmse:0.14792
[42]
        train-rmse:0.02372
                                  eval-rmse:0.14782
[43]
        train-rmse:0.02326
                                  eval-rmse:0.14784
[44]
        train-rmse:0.02211
                                  eval-rmse:0.14776
[45]
                                  eval-rmse:0.14776
        train-rmse:0.02145
[46]
        train-rmse:0.02102
                                  eval-rmse:0.14774
[47]
        train-rmse:0.02083
                                  eval-rmse:0.14772
[48]
        train-rmse:0.02037
                                  eval-rmse:0.14758
[49]
        train-rmse:0.02028
                                  eval-rmse:0.14762
        train-rmse:0.01987
[50]
                                  eval-rmse:0.14762
[51]
        train-rmse:0.01908
                                  eval-rmse:0.14752
[52]
        train-rmse:0.01885
                                  eval-rmse:0.14756
```

```
[53]
        train-rmse:0.01840
                                 eval-rmse:0.14759
[54]
        train-rmse:0.01821
                                 eval-rmse:0.14756
[55]
        train-rmse:0.01799
                                 eval-rmse:0.14761
[56]
        train-rmse:0.01756
                                 eval-rmse:0.14742
[57]
        train-rmse:0.01697
                                 eval-rmse:0.14749
[58]
                                 eval-rmse:0.14756
        train-rmse:0.01637
[59]
        train-rmse:0.01563
                                 eval-rmse:0.14745
[60]
        train-rmse:0.01542
                                 eval-rmse:0.14742
[61]
        train-rmse:0.01526
                                 eval-rmse:0.14752
[62]
        train-rmse:0.01474
                                 eval-rmse:0.14753
[63]
        train-rmse:0.01421
                                 eval-rmse:0.14745
        train-rmse:0.01360
[64]
                                 eval-rmse:0.14737
[65]
        train-rmse:0.01351
                                 eval-rmse:0.14733
[66]
        train-rmse:0.01324
                                 eval-rmse:0.14717
[67]
        train-rmse:0.01281
                                 eval-rmse:0.14720
[68]
        train-rmse:0.01270
                                 eval-rmse:0.14720
[69]
        train-rmse:0.01212
                                 eval-rmse:0.14725
[70]
        train-rmse:0.01172
                                 eval-rmse:0.14722
        train-rmse:0.01136
                                 eval-rmse:0.14729
[71]
[72]
        train-rmse:0.01128
                                 eval-rmse:0.14726
                                 eval-rmse:0.14722
[73]
        train-rmse:0.01107
[74]
        train-rmse:0.01098
                                 eval-rmse:0.14720
[75]
        train-rmse:0.01093
                                 eval-rmse:0.14717
                                 eval-rmse:0.14708
[76]
        train-rmse:0.01076
[77]
        train-rmse:0.01046
                                 eval-rmse:0.14708
        train-rmse:0.00991
[78]
                                 eval-rmse:0.14700
[79]
        train-rmse:0.00972
                                 eval-rmse:0.14699
[80]
        train-rmse:0.00925
                                 eval-rmse:0.14692
[81]
        train-rmse:0.00896
                                 eval-rmse:0.14715
[82]
        train-rmse:0.00865
                                 eval-rmse:0.14719
        train-rmse:0.00850
                                 eval-rmse:0.14719
[83]
[84]
        train-rmse:0.00833
                                 eval-rmse:0.14715
[85]
        train-rmse:0.00807
                                 eval-rmse:0.14714
[86]
        train-rmse:0.00804
                                 eval-rmse:0.14719
[87]
        train-rmse:0.00785
                                 eval-rmse:0.14720
        train-rmse:0.00768
                                 eval-rmse:0.14724
[88]
[89]
        train-rmse:0.00761
                                 eval-rmse:0.14726
[90]
        train-rmse:0.00751
                                 eval-rmse:0.14717
        train-rmse:0.00735
[91]
                                 eval-rmse:0.14718
[92]
        train-rmse:0.00724
                                 eval-rmse:0.14717
[93]
        train-rmse:0.00703
                                 eval-rmse:0.14712
[94]
        train-rmse:0.00685
                                 eval-rmse:0.14707
[95]
        train-rmse:0.00663
                                 eval-rmse:0.14707
[96]
        train-rmse:0.00648
                                 eval-rmse:0.14697
[97]
        train-rmse:0.00630
                                 eval-rmse:0.14696
[98]
        train-rmse:0.00614
                                 eval-rmse:0.14697
[99]
        train-rmse:0.00599
                                 eval-rmse:0.14694
```

```
[617]: plt.plot(evals_result['train']['rmse'], label='Train')
   plt.plot(evals_result['eval']['rmse'], label='Test')
   plt.xlabel('Boosting Round')
   plt.ylabel('RMSE')
   plt.title('XGBoost Training Progress')
   plt.legend()
   plt.show()
```



Evaluate

```
[8]: xgb_train_pred = model_xgb.predict(X_train)
print(f'XGBoost Train RMSE {rmse(y_train, xgb_train_pred)}')

xgb_pred = model_xgb.predict(X_test)
print(f'XGBoost Test RMSE {rmse(y_test, xgb_pred)}')
```

XGBoost Train RMSE 0.09 XGBoost Test RMSE 0.12

4.1.2 XGBoost with Hyperparameter Tuning

```
[624]: param grid = {
           'n_estimators': [100, 200, 300],
           'learning_rate': [0.01, 0.05, 0.1],
           'max_depth': [3, 4, 5],
           'subsample': [0.7, 0.8, 0.9],
           'colsample_bytree': [0.7, 0.8, 0.9]
       }
       xgb_model = xgb.XGBRegressor()
       grid_search = GridSearchCV(estimator=xgb_model, param_grid=param_grid, cv=3)
       grid_search.fit(X_train, y_train)
[624]: GridSearchCV(cv=3,
                    estimator=XGBRegressor(base_score=None, booster=None,
                                            callbacks=None, colsample_bylevel=None,
                                            colsample bynode=None,
                                            colsample bytree=None, device=None,
                                            early_stopping_rounds=None,
                                            enable categorical=False, eval metric=None,
                                            feature_types=None, gamma=None,
                                            grow_policy=None, importance_type=None,
                                            interaction_constraints=None,
                                            learning rate=None, m...
                                            max_cat_to_onehot=None, max_delta_step=None,
                                            max_depth=None, max_leaves=None,
                                            min_child_weight=None, missing=nan,
                                            monotone_constraints=None,
                                            multi_strategy=None, n_estimators=None,
                                            n_jobs=None, num_parallel_tree=None,
                                            random_state=None, ...),
                    param_grid={'colsample_bytree': [0.7, 0.8, 0.9],
                                 'learning rate': [0.01, 0.05, 0.1],
                                 'max_depth': [3, 4, 5],
                                 'n_estimators': [100, 200, 300],
                                 'subsample': [0.7, 0.8, 0.9]})
[625]: best_parameters = grid_search.best_params_
       best_score = grid_search.best_score_
       print(f"Best Parameters: {best_parameters}")
       print(f"Best Score: {best_score}")
       best_model = grid_search.best_estimator_
      Best Parameters: {'colsample_bytree': 0.8, 'learning_rate': 0.1, 'max_depth': 3,
      'n_estimators': 200, 'subsample': 0.9}
```

Best Score: 0.9012268726566676

```
[626]: best_xgb_model = xgb.XGBRegressor(**best_parameters)
       best_xgb_model.fit(X_train, y_train)
[626]: XGBRegressor(base_score=None, booster=None, callbacks=None,
                    colsample_bylevel=None, colsample_bynode=None,
                    colsample_bytree=0.8, device=None, early_stopping_rounds=None,
                    enable categorical=False, eval metric=None, feature types=None,
                    gamma=None, grow_policy=None, importance_type=None,
                    interaction constraints=None, learning rate=0.1, max bin=None,
                    max_cat_threshold=None, max_cat_to_onehot=None,
                    max_delta_step=None, max_depth=3, max_leaves=None,
                    min_child_weight=None, missing=nan, monotone_constraints=None,
                    multi_strategy=None, n_estimators=200, n_jobs=None,
                    num_parallel_tree=None, random_state=None, ...)
 [3]: xgb_train_pred = best_xgb_model.predict(X_train)
       print(f'XGBoost Train RMSE {rmse(y_train, xgb_train_pred)}')
       xgb_pred = best_xgb_model.predict(X_test)
       print(f'XGBoost Test RMSE {rmse(y_test, xgb_pred)}')
      XGBoost Train RMSE 0.06
      XGBoost Test RMSE 0.13
      4.1.3 CatBoost
      Data Preparation
[549]: train clone = train df.copy()
       float cols = train clone.select dtypes(include = ['float64']).columns
       train_clone[float_cols] = train_clone[float_cols].astype(int)
[559]: | train_clone["SalePrice"] = np.log1p(train_clone["SalePrice"])
       train_clone = pd.get_dummies(train_clone)
       X = train_clone.drop(columns = ['SalePrice'], axis = 1)
       y = train_clone['SalePrice']
       X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.2,_
        →random_state=32)
       categorical_features_names = list(X.columns)
[561]: train_pool = Pool(X_train,
                         label=y train,
                         cat_features=categorical_features_names)
```

Train

```
[563]: model = CatBoostRegressor(custom_metric= ['R2', 'RMSE'], learning_rate=0.01, u depth = 10, n_estimators=5000)
model.fit(train_pool, eval_set=test_pool, verbose=1000, plot=True)
```

MetricVisualizer(layout=Layout(align_self='stretch', height='500px'))

```
learn: 0.0416175
                               test: 0.0417206 best: 0.0417206 (0)
0:
                                                                      total:
18.2ms
       remaining: 1m 30s
1000: learn: 0.0112569
                               test: 0.0232236 best: 0.0232236 (1000)
                                                                      total:
16.6s
       remaining: 1m 6s
2000: learn: 0.0070376
                               test: 0.0228457 best: 0.0228457 (2000) total:
35.6s remaining: 53.3s
3000: learn: 0.0046750
                               test: 0.0227822 best: 0.0227815 (2955) total:
53.8s remaining: 35.8s
4000:
       learn: 0.0029821
                              test: 0.0227638 best: 0.0227635 (3998) total:
1m 12s remaining: 18.1s
                               test: 0.0227434 best: 0.0227428 (4873) total:
4999:
       learn: 0.0020532
1m 31s remaining: Ous
bestTest = 0.02274284214
bestIteration = 4873
```

Shrink model to first 4874 iterations.

[563]: <catboost.core.CatBoostRegressor at 0x7f6cd1f807d0>

Evaluate

```
[4]: cat_train_pred = model.predict(X_train)
    print(f'CatBoost Train RMSE {rmse(y_train, xgb_train_pred)}')

cat_pred = model.predict(X_test)
    print(f'CatBoost Test RMSE {rmse(y_test, xgb_pred)}')
```

CatBoost Train RMSE 9.53 CatBoost Test RMSE 9.57

4.1.4 CatBoost with Hyperparameter Tuning

```
[593]: param_grid = {
    'iterations': [500, 1000],
    'learning_rate': [0.01, 0.1, 0.2],
    'depth': [4, 6, 8],
```

```
'12_leaf_reg': [1, 3, 5, 7, 9]
       }
[594]: grid search = GridSearchCV(estimator=CatBoostRegressor(),
                                   param_grid=param_grid,
                                   cv=5,
                                   n_{jobs=-1},
                                   verbose=0)
       grid_search.fit(X_train, y_train, verbose=0)
[594]: GridSearchCV(cv=5,
                    estimator=<catboost.core.CatBoostRegressor object at
       0x7f6cd1f3b710>,
                    n_{jobs=-1},
                    param_grid={'depth': [4, 6, 8], 'iterations': [500, 1000],
                                 'l2_leaf_reg': [1, 3, 5, 7, 9],
                                 'learning_rate': [0.01, 0.1, 0.2]})
[595]: best_parameters = grid_search.best_params_
       best_score = grid_search.best_score_
       print(f"Best Parameters: {best_parameters}")
       print(f"Best Score: {best_score}")
      Best Parameters: {'depth': 4, 'iterations': 500, '12_leaf_reg': 5,
      'learning_rate': 0.1}
      Best Score: 0.8861827658601926
[596]: best model = CatBoostRegressor(**best parameters)
       best_model.fit(X_train, y_train)
      0:
              learn: 0.3532770
                                       total: 702us
                                                        remaining: 350ms
      1:
              learn: 0.3335623
                                       total: 1.18ms
                                                       remaining: 295ms
      2:
              learn: 0.3157700
                                       total: 1.61ms
                                                        remaining: 268ms
                                       total: 2.08ms
      3:
              learn: 0.2988716
                                                       remaining: 257ms
                                       total: 2.57ms
      4:
              learn: 0.2846018
                                                        remaining: 255ms
      5:
              learn: 0.2707849
                                       total: 3.08ms
                                                       remaining: 253ms
      6:
              learn: 0.2595443
                                       total: 3.63ms
                                                       remaining: 256ms
      7:
              learn: 0.2493907
                                       total: 4.32ms
                                                       remaining: 266ms
      8:
              learn: 0.2391028
                                       total: 5ms
                                                       remaining: 273ms
              learn: 0.2283552
                                       total: 5.7ms
      9:
                                                       remaining: 279ms
              learn: 0.2197443
                                       total: 6.38ms
                                                       remaining: 284ms
      10:
              learn: 0.2123077
                                       total: 7.06ms
                                                        remaining: 287ms
      11:
      12:
              learn: 0.2046252
                                       total: 7.72ms
                                                        remaining: 289ms
      13:
              learn: 0.1984473
                                       total: 8.38ms
                                                       remaining: 291ms
      14:
              learn: 0.1922836
                                       total: 9.03ms
                                                       remaining: 292ms
      15:
              learn: 0.1870114
                                       total: 9.67ms
                                                        remaining: 293ms
              learn: 0.1821393
                                       total: 10.3ms
                                                       remaining: 293ms
      16:
```

```
17:
        learn: 0.1774804
                                                   remaining: 294ms
                                  total: 11ms
18:
        learn: 0.1737408
                                  total: 11.6ms
                                                   remaining: 295ms
19:
        learn: 0.1708838
                                  total: 12.3ms
                                                   remaining: 295ms
20:
        learn: 0.1669691
                                  total: 12.9ms
                                                   remaining: 295ms
                                  total: 13.6ms
                                                   remaining: 295ms
21:
        learn: 0.1636378
                                                   remaining: 295ms
22:
        learn: 0.1612121
                                  total: 14.2ms
23:
        learn: 0.1585342
                                  total: 14.8ms
                                                   remaining: 294ms
24:
        learn: 0.1556037
                                  total: 15.5ms
                                                   remaining: 294ms
25:
        learn: 0.1533850
                                  total: 16.1ms
                                                   remaining: 294ms
26:
        learn: 0.1506163
                                  total: 16.8ms
                                                   remaining: 294ms
27:
        learn: 0.1485598
                                  total: 17.5ms
                                                   remaining: 294ms
28:
        learn: 0.1469492
                                  total: 18.1ms
                                                   remaining: 294ms
        learn: 0.1454045
29:
                                  total: 18.7ms
                                                   remaining: 293ms
30:
        learn: 0.1435952
                                  total: 19.3ms
                                                   remaining: 293ms
31:
        learn: 0.1418491
                                  total: 19.9ms
                                                   remaining: 292ms
32:
                                                   remaining: 291ms
        learn: 0.1402668
                                  total: 20.5ms
33:
        learn: 0.1387257
                                  total: 21.1ms
                                                   remaining: 289ms
34:
        learn: 0.1374522
                                  total: 21.7ms
                                                   remaining: 288ms
                                  total: 22.3ms
                                                   remaining: 288ms
35:
        learn: 0.1357729
36:
        learn: 0.1344421
                                  total: 22.9ms
                                                   remaining: 287ms
                                  total: 23.5ms
                                                   remaining: 286ms
37:
        learn: 0.1333160
38:
        learn: 0.1321481
                                  total: 24.1ms
                                                   remaining: 285ms
39:
        learn: 0.1312513
                                  total: 24.7ms
                                                   remaining: 284ms
                                  total: 25.3ms
                                                   remaining: 283ms
40:
        learn: 0.1305290
41:
        learn: 0.1293697
                                  total: 25.8ms
                                                   remaining: 282ms
42:
        learn: 0.1285745
                                  total: 26.4ms
                                                   remaining: 281ms
                                  total: 27ms
43:
        learn: 0.1276534
                                                   remaining: 280ms
44:
        learn: 0.1267059
                                  total: 27.6ms
                                                   remaining: 279ms
45:
        learn: 0.1258917
                                  total: 28.1ms
                                                   remaining: 278ms
46:
        learn: 0.1252225
                                  total: 28.7ms
                                                   remaining: 276ms
                                  total: 29.2ms
47:
        learn: 0.1249795
                                                   remaining: 275ms
48:
        learn: 0.1238678
                                  total: 29.8ms
                                                   remaining: 274ms
49:
        learn: 0.1230530
                                  total: 30.3ms
                                                   remaining: 273ms
50:
        learn: 0.1226434
                                  total: 30.9ms
                                                   remaining: 272ms
51:
        learn: 0.1223813
                                  total: 31.4ms
                                                   remaining: 271ms
52:
        learn: 0.1215163
                                  total: 32ms
                                                   remaining: 270ms
53:
        learn: 0.1208749
                                  total: 32.6ms
                                                   remaining: 269ms
54:
        learn: 0.1206409
                                  total: 33.1ms
                                                   remaining: 268ms
55:
        learn: 0.1199707
                                  total: 33.6ms
                                                   remaining: 267ms
56:
        learn: 0.1192999
                                  total: 34.1ms
                                                   remaining: 265ms
57:
                                  total: 34.7ms
        learn: 0.1186356
                                                   remaining: 264ms
                                                   remaining: 268ms
58:
        learn: 0.1184167
                                  total: 35.9ms
59:
        learn: 0.1178437
                                  total: 36.4ms
                                                   remaining: 267ms
60:
        learn: 0.1175393
                                  total: 36.8ms
                                                   remaining: 265ms
61:
        learn: 0.1173410
                                  total: 37.3ms
                                                   remaining: 264ms
        learn: 0.1169933
62:
                                  total: 37.8ms
                                                   remaining: 262ms
63:
        learn: 0.1163097
                                  total: 38.3ms
                                                   remaining: 261ms
64:
        learn: 0.1158097
                                  total: 38.7ms
                                                   remaining: 259ms
```

```
65:
        learn: 0.1150863
                                  total: 39.2ms
                                                   remaining: 258ms
66:
        learn: 0.1147983
                                  total: 39.7ms
                                                   remaining: 256ms
67:
        learn: 0.1145866
                                  total: 40.1ms
                                                   remaining: 255ms
        learn: 0.1144449
                                  total: 40.5ms
                                                   remaining: 253ms
68:
                                                   remaining: 252ms
69:
        learn: 0.1141551
                                  total: 41ms
                                                   remaining: 250ms
70:
        learn: 0.1135066
                                  total: 41.4ms
71:
        learn: 0.1128975
                                  total: 41.9ms
                                                   remaining: 249ms
                                  total: 42.4ms
72:
        learn: 0.1126441
                                                   remaining: 248ms
73:
        learn: 0.1122858
                                  total: 42.8ms
                                                   remaining: 247ms
74:
        learn: 0.1116962
                                  total: 43.3ms
                                                   remaining: 245ms
75:
        learn: 0.1110930
                                  total: 43.7ms
                                                   remaining: 244ms
76:
        learn: 0.1109695
                                  total: 44.2ms
                                                   remaining: 243ms
77:
        learn: 0.1103540
                                  total: 44.6ms
                                                   remaining: 242ms
78:
        learn: 0.1094938
                                  total: 45ms
                                                   remaining: 240ms
79:
        learn: 0.1092652
                                  total: 45.5ms
                                                   remaining: 239ms
80:
                                                   remaining: 237ms
        learn: 0.1090595
                                  total: 45.9ms
81:
        learn: 0.1085171
                                  total: 46.3ms
                                                   remaining: 236ms
82:
        learn: 0.1077989
                                  total: 46.8ms
                                                   remaining: 235ms
        learn: 0.1076079
                                  total: 47.2ms
                                                   remaining: 234ms
83:
84:
        learn: 0.1069775
                                  total: 47.6ms
                                                   remaining: 233ms
                                  total: 48.1ms
85:
        learn: 0.1064349
                                                   remaining: 231ms
86:
        learn: 0.1059226
                                  total: 48.5ms
                                                   remaining: 230ms
87:
        learn: 0.1058087
                                  total: 48.9ms
                                                   remaining: 229ms
88:
        learn: 0.1050220
                                  total: 49.3ms
                                                   remaining: 228ms
89:
        learn: 0.1048879
                                  total: 49.7ms
                                                   remaining: 226ms
90:
        learn: 0.1043749
                                  total: 50.1ms
                                                   remaining: 225ms
                                  total: 50.5ms
                                                   remaining: 224ms
91:
        learn: 0.1039485
92:
        learn: 0.1034659
                                  total: 50.9ms
                                                   remaining: 223ms
93:
        learn: 0.1031671
                                  total: 51.3ms
                                                   remaining: 222ms
94:
        learn: 0.1030035
                                  total: 51.7ms
                                                   remaining: 220ms
                                  total: 52.1ms
95:
        learn: 0.1028822
                                                   remaining: 219ms
96:
        learn: 0.1024266
                                  total: 52.5ms
                                                   remaining: 218ms
97:
        learn: 0.1019823
                                  total: 52.9ms
                                                   remaining: 217ms
        learn: 0.1018539
                                  total: 53.3ms
                                                   remaining: 216ms
98:
                                                   remaining: 215ms
99:
        learn: 0.1014201
                                  total: 53.7ms
100:
        learn: 0.1009559
                                  total: 54.1ms
                                                   remaining: 214ms
101:
        learn: 0.1008594
                                  total: 54.4ms
                                                   remaining: 212ms
102:
        learn: 0.1004201
                                  total: 54.8ms
                                                   remaining: 211ms
                                  total: 55.2ms
103:
        learn: 0.1003303
                                                   remaining: 210ms
104:
        learn: 0.0999516
                                  total: 55.6ms
                                                   remaining: 209ms
105:
        learn: 0.0995629
                                  total: 56ms
                                                   remaining: 208ms
                                                   remaining: 207ms
106:
        learn: 0.0993895
                                  total: 56.4ms
107:
        learn: 0.0993185
                                  total: 56.8ms
                                                   remaining: 206ms
                                                   remaining: 205ms
108:
        learn: 0.0988826
                                  total: 57.2ms
109:
        learn: 0.0987320
                                  total: 57.6ms
                                                   remaining: 204ms
                                                   remaining: 203ms
110:
        learn: 0.0983850
                                  total: 58ms
111:
        learn: 0.0983180
                                  total: 58.4ms
                                                   remaining: 202ms
112:
        learn: 0.0982401
                                  total: 58.7ms
                                                   remaining: 201ms
```

```
113:
        learn: 0.0977169
                                  total: 59.1ms
                                                   remaining: 200ms
114:
        learn: 0.0976547
                                  total: 59.5ms
                                                   remaining: 199ms
115:
        learn: 0.0972780
                                  total: 59.9ms
                                                   remaining: 198ms
                                                   remaining: 197ms
116:
        learn: 0.0971918
                                  total: 60.3ms
                                  total: 60.7ms
117:
        learn: 0.0970033
                                                   remaining: 196ms
                                                   remaining: 196ms
118:
        learn: 0.0966939
                                  total: 61.1ms
119:
        learn: 0.0964549
                                  total: 61.4ms
                                                   remaining: 195ms
120:
        learn: 0.0961597
                                  total: 61.8ms
                                                   remaining: 194ms
121:
        learn: 0.0960808
                                  total: 62.2ms
                                                   remaining: 193ms
122:
        learn: 0.0957279
                                  total: 62.6ms
                                                   remaining: 192ms
123:
        learn: 0.0955350
                                  total: 63ms
                                                   remaining: 191ms
124:
        learn: 0.0954149
                                  total: 63.4ms
                                                   remaining: 190ms
125:
        learn: 0.0953553
                                  total: 63.8ms
                                                   remaining: 189ms
126:
        learn: 0.0950943
                                  total: 64.2ms
                                                   remaining: 188ms
127:
        learn: 0.0950252
                                  total: 64.6ms
                                                   remaining: 188ms
128:
        learn: 0.0949109
                                  total: 65ms
                                                   remaining: 187ms
129:
        learn: 0.0946060
                                  total: 65.4ms
                                                   remaining: 186ms
130:
        learn: 0.0942875
                                  total: 65.8ms
                                                   remaining: 185ms
                                  total: 66.2ms
                                                   remaining: 184ms
131:
        learn: 0.0940258
132:
        learn: 0.0937458
                                  total: 66.6ms
                                                   remaining: 184ms
133:
        learn: 0.0934459
                                  total: 66.9ms
                                                   remaining: 183ms
134:
        learn: 0.0932635
                                  total: 67.3ms
                                                   remaining: 182ms
135:
        learn: 0.0929438
                                  total: 67.7ms
                                                   remaining: 181ms
136:
        learn: 0.0928105
                                  total: 68.1ms
                                                   remaining: 181ms
137:
        learn: 0.0926397
                                  total: 68.5ms
                                                   remaining: 180ms
        learn: 0.0923935
                                  total: 68.9ms
                                                   remaining: 179ms
138:
                                                   remaining: 178ms
139:
        learn: 0.0921275
                                  total: 69.3ms
140:
        learn: 0.0918719
                                  total: 69.7ms
                                                   remaining: 177ms
141:
        learn: 0.0916759
                                  total: 70.1ms
                                                   remaining: 177ms
142:
        learn: 0.0916132
                                  total: 70.5ms
                                                   remaining: 176ms
143:
        learn: 0.0915631
                                  total: 70.9ms
                                                   remaining: 175ms
144:
        learn: 0.0913864
                                  total: 71.2ms
                                                   remaining: 174ms
145:
        learn: 0.0913475
                                  total: 71.6ms
                                                   remaining: 174ms
        learn: 0.0912906
                                  total: 72ms
                                                   remaining: 173ms
146:
147:
        learn: 0.0910730
                                  total: 72.4ms
                                                   remaining: 172ms
148:
        learn: 0.0908739
                                  total: 72.8ms
                                                   remaining: 171ms
149:
        learn: 0.0906041
                                  total: 73.2ms
                                                   remaining: 171ms
150:
        learn: 0.0905606
                                  total: 73.6ms
                                                   remaining: 170ms
151:
        learn: 0.0902892
                                  total: 74ms
                                                   remaining: 169ms
152:
        learn: 0.0902149
                                  total: 74.4ms
                                                   remaining: 169ms
                                  total: 74.8ms
153:
        learn: 0.0901736
                                                   remaining: 168ms
                                                   remaining: 167ms
154:
        learn: 0.0899191
                                  total: 75.2ms
155:
                                  total: 75.5ms
                                                   remaining: 167ms
        learn: 0.0896080
156:
        learn: 0.0893897
                                  total: 75.9ms
                                                   remaining: 166ms
157:
        learn: 0.0893508
                                  total: 76.3ms
                                                   remaining: 165ms
158:
        learn: 0.0891106
                                  total: 76.7ms
                                                   remaining: 165ms
159:
        learn: 0.0887889
                                  total: 77.1ms
                                                   remaining: 164ms
160:
        learn: 0.0885169
                                  total: 77.5ms
                                                   remaining: 163ms
```

```
learn: 0.0882941
161:
                                  total: 77.9ms
                                                   remaining: 163ms
162:
        learn: 0.0882435
                                  total: 78.3ms
                                                   remaining: 162ms
163:
        learn: 0.0881556
                                  total: 78.7ms
                                                   remaining: 161ms
                                  total: 79.1ms
                                                   remaining: 161ms
164:
        learn: 0.0881075
165:
        learn: 0.0877820
                                  total: 79.5ms
                                                   remaining: 160ms
                                                   remaining: 159ms
166:
        learn: 0.0877044
                                  total: 79.9ms
167:
        learn: 0.0875062
                                  total: 80.3ms
                                                   remaining: 159ms
168:
        learn: 0.0872990
                                  total: 80.6ms
                                                   remaining: 158ms
169:
        learn: 0.0870951
                                  total: 81ms
                                                   remaining: 157ms
170:
        learn: 0.0870520
                                  total: 81.5ms
                                                   remaining: 157ms
171:
        learn: 0.0869653
                                  total: 81.9ms
                                                   remaining: 156ms
172:
        learn: 0.0866681
                                  total: 82.2ms
                                                   remaining: 155ms
173:
        learn: 0.0866180
                                  total: 82.6ms
                                                   remaining: 155ms
174:
        learn: 0.0864357
                                  total: 83ms
                                                   remaining: 154ms
175:
        learn: 0.0862041
                                  total: 83.4ms
                                                   remaining: 154ms
176:
        learn: 0.0859825
                                  total: 83.8ms
                                                   remaining: 153ms
177:
        learn: 0.0857469
                                  total: 84.2ms
                                                   remaining: 152ms
178:
        learn: 0.0855579
                                  total: 84.6ms
                                                   remaining: 152ms
                                  total: 85ms
                                                   remaining: 151ms
179:
        learn: 0.0853386
180:
        learn: 0.0852988
                                  total: 85.4ms
                                                   remaining: 151ms
181:
        learn: 0.0851989
                                  total: 85.8ms
                                                   remaining: 150ms
182:
        learn: 0.0851686
                                  total: 86.2ms
                                                   remaining: 149ms
183:
        learn: 0.0850590
                                  total: 86.6ms
                                                   remaining: 149ms
184:
        learn: 0.0847544
                                  total: 86.9ms
                                                   remaining: 148ms
185:
        learn: 0.0846113
                                  total: 87.3ms
                                                   remaining: 147ms
        learn: 0.0842964
                                  total: 87.7ms
                                                   remaining: 147ms
186:
                                  total: 88.1ms
187:
        learn: 0.0841541
                                                   remaining: 146ms
188:
        learn: 0.0839727
                                  total: 88.5ms
                                                   remaining: 146ms
189:
        learn: 0.0837707
                                  total: 88.9ms
                                                   remaining: 145ms
190:
        learn: 0.0836764
                                  total: 89.3ms
                                                   remaining: 144ms
191:
        learn: 0.0836000
                                  total: 89.7ms
                                                   remaining: 144ms
192:
        learn: 0.0834713
                                  total: 90.1ms
                                                   remaining: 143ms
193:
        learn: 0.0834224
                                  total: 90.5ms
                                                   remaining: 143ms
194:
        learn: 0.0833579
                                  total: 90.9ms
                                                   remaining: 142ms
195:
        learn: 0.0833009
                                  total: 91.3ms
                                                   remaining: 142ms
                                  total: 91.7ms
196:
        learn: 0.0830016
                                                   remaining: 141ms
197:
        learn: 0.0828059
                                  total: 92.1ms
                                                   remaining: 140ms
198:
        learn: 0.0825121
                                  total: 92.5ms
                                                   remaining: 140ms
199:
        learn: 0.0824780
                                  total: 92.8ms
                                                   remaining: 139ms
200:
        learn: 0.0824052
                                  total: 93.2ms
                                                   remaining: 139ms
201:
                                  total: 93.6ms
        learn: 0.0822494
                                                   remaining: 138ms
202:
        learn: 0.0820717
                                  total: 94ms
                                                   remaining: 138ms
203:
        learn: 0.0817942
                                                   remaining: 137ms
                                  total: 94.4ms
204:
        learn: 0.0815523
                                  total: 94.8ms
                                                   remaining: 136ms
                                                   remaining: 136ms
205:
        learn: 0.0813970
                                  total: 95.2ms
206:
        learn: 0.0811631
                                  total: 95.6ms
                                                   remaining: 135ms
207:
        learn: 0.0810690
                                  total: 96ms
                                                   remaining: 135ms
208:
        learn: 0.0809741
                                  total: 96.4ms
                                                   remaining: 134ms
```

```
209:
        learn: 0.0809444
                                  total: 96.8ms
                                                   remaining: 134ms
210:
        learn: 0.0807871
                                  total: 97.1ms
                                                   remaining: 133ms
211:
        learn: 0.0806855
                                  total: 97.5ms
                                                   remaining: 132ms
212:
        learn: 0.0806029
                                  total: 97.9ms
                                                   remaining: 132ms
213:
        learn: 0.0804003
                                  total: 98.3ms
                                                   remaining: 131ms
                                                   remaining: 131ms
214:
        learn: 0.0803776
                                  total: 98.7ms
215:
        learn: 0.0802203
                                  total: 99.1ms
                                                   remaining: 130ms
        learn: 0.0800418
216:
                                  total: 99.5ms
                                                   remaining: 130ms
217:
        learn: 0.0798038
                                  total: 99.9ms
                                                   remaining: 129ms
218:
        learn: 0.0796512
                                  total: 100ms
                                                   remaining: 129ms
219:
        learn: 0.0795124
                                  total: 101ms
                                                   remaining: 128ms
220:
        learn: 0.0792978
                                  total: 101ms
                                                   remaining: 128ms
        learn: 0.0792084
221:
                                  total: 101ms
                                                   remaining: 127ms
222:
        learn: 0.0791783
                                  total: 102ms
                                                   remaining: 126ms
223:
        learn: 0.0789725
                                  total: 102ms
                                                   remaining: 126ms
224:
        learn: 0.0788076
                                  total: 103ms
                                                   remaining: 125ms
225:
        learn: 0.0786858
                                  total: 103ms
                                                   remaining: 125ms
226:
        learn: 0.0786158
                                  total: 103ms
                                                   remaining: 124ms
                                                   remaining: 124ms
227:
        learn: 0.0784174
                                  total: 104ms
228:
        learn: 0.0783451
                                  total: 104ms
                                                   remaining: 123ms
229:
        learn: 0.0782373
                                  total: 105ms
                                                   remaining: 123ms
230:
        learn: 0.0781315
                                  total: 105ms
                                                   remaining: 122ms
231:
        learn: 0.0779739
                                  total: 105ms
                                                   remaining: 122ms
232:
        learn: 0.0778122
                                  total: 106ms
                                                   remaining: 121ms
233:
        learn: 0.0777659
                                  total: 106ms
                                                   remaining: 121ms
234:
        learn: 0.0776276
                                  total: 106ms
                                                   remaining: 120ms
235:
        learn: 0.0774570
                                  total: 107ms
                                                   remaining: 120ms
236:
        learn: 0.0772552
                                  total: 107ms
                                                   remaining: 119ms
237:
        learn: 0.0771638
                                  total: 108ms
                                                   remaining: 118ms
238:
        learn: 0.0770942
                                  total: 108ms
                                                   remaining: 118ms
239:
        learn: 0.0769152
                                  total: 108ms
                                                   remaining: 117ms
240:
        learn: 0.0767690
                                  total: 109ms
                                                   remaining: 117ms
241:
        learn: 0.0766074
                                  total: 109ms
                                                   remaining: 116ms
242:
        learn: 0.0764837
                                  total: 110ms
                                                   remaining: 116ms
243:
        learn: 0.0764639
                                  total: 110ms
                                                   remaining: 115ms
244:
        learn: 0.0762655
                                  total: 110ms
                                                   remaining: 115ms
245:
        learn: 0.0761176
                                  total: 111ms
                                                   remaining: 114ms
246:
        learn: 0.0759723
                                  total: 111ms
                                                   remaining: 114ms
247:
        learn: 0.0758935
                                  total: 112ms
                                                   remaining: 113ms
248:
        learn: 0.0758147
                                  total: 112ms
                                                   remaining: 113ms
249:
        learn: 0.0756756
                                  total: 112ms
                                                   remaining: 112ms
250:
        learn: 0.0755715
                                  total: 113ms
                                                   remaining: 112ms
251:
        learn: 0.0755328
                                  total: 113ms
                                                   remaining: 111ms
252:
        learn: 0.0754021
                                  total: 114ms
                                                   remaining: 111ms
                                                   remaining: 110ms
253:
        learn: 0.0753742
                                  total: 114ms
254:
        learn: 0.0751955
                                  total: 114ms
                                                   remaining: 110ms
255:
        learn: 0.0751103
                                  total: 115ms
                                                   remaining: 109ms
256:
        learn: 0.0750341
                                  total: 115ms
                                                   remaining: 109ms
```

```
257:
        learn: 0.0750179
                                  total: 116ms
                                                   remaining: 108ms
258:
        learn: 0.0749516
                                  total: 116ms
                                                   remaining: 108ms
259:
        learn: 0.0748211
                                  total: 116ms
                                                   remaining: 107ms
260:
        learn: 0.0746904
                                  total: 117ms
                                                   remaining: 107ms
261:
        learn: 0.0745694
                                  total: 117ms
                                                   remaining: 106ms
                                                   remaining: 106ms
262:
        learn: 0.0745494
                                  total: 118ms
263:
        learn: 0.0744222
                                  total: 118ms
                                                   remaining: 105ms
264:
        learn: 0.0742872
                                  total: 118ms
                                                   remaining: 105ms
265:
        learn: 0.0742418
                                  total: 119ms
                                                   remaining: 104ms
                                  total: 119ms
266:
        learn: 0.0741839
                                                   remaining: 104ms
267:
        learn: 0.0741687
                                  total: 119ms
                                                   remaining: 103ms
268:
        learn: 0.0741068
                                  total: 120ms
                                                   remaining: 103ms
269:
        learn: 0.0739354
                                  total: 120ms
                                                   remaining: 102ms
270:
        learn: 0.0738229
                                  total: 121ms
                                                   remaining: 102ms
271:
        learn: 0.0736866
                                  total: 121ms
                                                   remaining: 101ms
272:
        learn: 0.0736678
                                  total: 121ms
                                                   remaining: 101ms
273:
        learn: 0.0734981
                                  total: 122ms
                                                   remaining: 100ms
274:
        learn: 0.0734131
                                  total: 122ms
                                                   remaining: 100ms
                                  total: 123ms
                                                   remaining: 99.5ms
275:
        learn: 0.0732944
276:
        learn: 0.0731585
                                  total: 123ms
                                                   remaining: 99ms
277:
        learn: 0.0729876
                                  total: 123ms
                                                   remaining: 98.5ms
278:
        learn: 0.0727894
                                  total: 124ms
                                                   remaining: 98ms
279:
        learn: 0.0727753
                                  total: 124ms
                                                   remaining: 97.5ms
                                  total: 125ms
280:
        learn: 0.0726864
                                                   remaining: 97.1ms
281:
        learn: 0.0726689
                                  total: 125ms
                                                   remaining: 96.6ms
282:
        learn: 0.0725333
                                  total: 125ms
                                                   remaining: 96.1ms
283:
                                                   remaining: 95.6ms
        learn: 0.0723920
                                  total: 126ms
284:
        learn: 0.0723054
                                  total: 126ms
                                                   remaining: 95.1ms
285:
        learn: 0.0720663
                                  total: 127ms
                                                   remaining: 94.7ms
286:
        learn: 0.0719297
                                  total: 127ms
                                                   remaining: 94.2ms
        learn: 0.0719163
287:
                                  total: 127ms
                                                   remaining: 93.7ms
288:
        learn: 0.0718037
                                  total: 128ms
                                                   remaining: 93.2ms
                                  total: 128ms
289:
        learn: 0.0717358
                                                   remaining: 92.7ms
290:
        learn: 0.0717158
                                  total: 128ms
                                                   remaining: 92.3ms
                                                   remaining: 91.8ms
291:
        learn: 0.0716435
                                  total: 129ms
292:
        learn: 0.0715163
                                  total: 129ms
                                                   remaining: 91.3ms
293:
        learn: 0.0714223
                                  total: 130ms
                                                   remaining: 90.8ms
294:
        learn: 0.0713620
                                  total: 130ms
                                                   remaining: 90.3ms
295:
        learn: 0.0712594
                                  total: 130ms
                                                   remaining: 89.9ms
296:
        learn: 0.0710767
                                  total: 131ms
                                                   remaining: 89.4ms
297:
        learn: 0.0709328
                                  total: 131ms
                                                   remaining: 88.9ms
298:
                                                   remaining: 88.5ms
        learn: 0.0708359
                                  total: 132ms
299:
        learn: 0.0708209
                                  total: 132ms
                                                   remaining: 88ms
300:
        learn: 0.0707996
                                  total: 132ms
                                                   remaining: 87.5ms
301:
        learn: 0.0706146
                                  total: 133ms
                                                   remaining: 87ms
302:
        learn: 0.0705911
                                  total: 133ms
                                                   remaining: 86.5ms
303:
        learn: 0.0705168
                                  total: 134ms
                                                   remaining: 86.1ms
304:
        learn: 0.0705051
                                  total: 134ms
                                                   remaining: 85.6ms
```

```
305:
        learn: 0.0704226
                                  total: 134ms
                                                   remaining: 85.1ms
306:
        learn: 0.0703633
                                  total: 135ms
                                                   remaining: 84.7ms
307:
        learn: 0.0702203
                                  total: 135ms
                                                   remaining: 84.2ms
        learn: 0.0701049
                                                   remaining: 83.7ms
308:
                                  total: 135ms
309:
        learn: 0.0700562
                                  total: 136ms
                                                   remaining: 83.3ms
                                  total: 136ms
                                                   remaining: 82.8ms
310:
        learn: 0.0700418
311:
        learn: 0.0699061
                                  total: 137ms
                                                   remaining: 82.3ms
        learn: 0.0698217
312:
                                  total: 137ms
                                                   remaining: 81.8ms
313:
        learn: 0.0696523
                                  total: 137ms
                                                   remaining: 81.4ms
314:
        learn: 0.0695029
                                  total: 138ms
                                                   remaining: 80.9ms
315:
        learn: 0.0693740
                                  total: 138ms
                                                   remaining: 80.5ms
316:
        learn: 0.0693117
                                  total: 139ms
                                                   remaining: 80ms
317:
        learn: 0.0691794
                                  total: 139ms
                                                   remaining: 79.5ms
318:
        learn: 0.0691165
                                  total: 139ms
                                                   remaining: 79.1ms
319:
        learn: 0.0690282
                                  total: 140ms
                                                   remaining: 78.6ms
320:
        learn: 0.0688543
                                  total: 140ms
                                                   remaining: 78.2ms
321:
        learn: 0.0687697
                                  total: 141ms
                                                   remaining: 77.7ms
                                  total: 141ms
322:
        learn: 0.0686841
                                                   remaining: 77.2ms
                                  total: 141ms
                                                   remaining: 76.8ms
323:
        learn: 0.0686084
324:
        learn: 0.0685948
                                  total: 142ms
                                                   remaining: 76.3ms
                                  total: 142ms
325:
        learn: 0.0685114
                                                   remaining: 75.9ms
326:
        learn: 0.0684991
                                  total: 143ms
                                                   remaining: 75.4ms
327:
        learn: 0.0684779
                                  total: 143ms
                                                   remaining: 74.9ms
328:
        learn: 0.0683988
                                  total: 143ms
                                                   remaining: 74.5ms
329:
        learn: 0.0682340
                                  total: 144ms
                                                   remaining: 74ms
330:
        learn: 0.0681769
                                  total: 144ms
                                                   remaining: 73.6ms
                                                   remaining: 73.1ms
331:
        learn: 0.0680506
                                  total: 144ms
332:
        learn: 0.0679364
                                  total: 145ms
                                                   remaining: 72.7ms
333:
        learn: 0.0679113
                                  total: 146ms
                                                   remaining: 72.6ms
334:
        learn: 0.0677760
                                  total: 146ms
                                                   remaining: 72.1ms
335:
        learn: 0.0677520
                                  total: 147ms
                                                   remaining: 71.7ms
336:
        learn: 0.0676131
                                  total: 147ms
                                                   remaining: 71.2ms
                                  total: 148ms
337:
        learn: 0.0675030
                                                   remaining: 70.8ms
        learn: 0.0674325
                                  total: 148ms
                                                   remaining: 70.3ms
338:
                                                   remaining: 69.9ms
339:
        learn: 0.0672879
                                  total: 148ms
340:
        learn: 0.0671885
                                  total: 149ms
                                                   remaining: 69.4ms
341:
        learn: 0.0669832
                                  total: 149ms
                                                   remaining: 69ms
342:
        learn: 0.0669060
                                  total: 150ms
                                                   remaining: 68.5ms
343:
        learn: 0.0667714
                                  total: 150ms
                                                   remaining: 68ms
344:
        learn: 0.0667460
                                  total: 150ms
                                                   remaining: 67.6ms
345:
        learn: 0.0666137
                                  total: 151ms
                                                   remaining: 67.1ms
                                                   remaining: 66.7ms
346:
        learn: 0.0665646
                                  total: 151ms
347:
        learn: 0.0664999
                                  total: 152ms
                                                   remaining: 66.2ms
348:
        learn: 0.0664293
                                  total: 152ms
                                                   remaining: 65.8ms
349:
        learn: 0.0663663
                                  total: 152ms
                                                   remaining: 65.3ms
350:
        learn: 0.0662911
                                  total: 153ms
                                                   remaining: 64.9ms
351:
        learn: 0.0661880
                                  total: 153ms
                                                   remaining: 64.4ms
352:
        learn: 0.0660287
                                  total: 154ms
                                                   remaining: 64ms
```

```
353:
        learn: 0.0659336
                                  total: 154ms
                                                   remaining: 63.5ms
354:
        learn: 0.0658213
                                  total: 154ms
                                                   remaining: 63.1ms
355:
        learn: 0.0657013
                                  total: 155ms
                                                   remaining: 62.6ms
        learn: 0.0655707
                                                   remaining: 62.2ms
356:
                                  total: 155ms
357:
        learn: 0.0655565
                                  total: 156ms
                                                   remaining: 61.7ms
                                                   remaining: 61.2ms
358:
        learn: 0.0655011
                                  total: 156ms
359:
        learn: 0.0653639
                                  total: 156ms
                                                   remaining: 60.8ms
360:
        learn: 0.0652716
                                  total: 157ms
                                                   remaining: 60.4ms
361:
        learn: 0.0652601
                                  total: 157ms
                                                   remaining: 59.9ms
362:
        learn: 0.0651766
                                  total: 158ms
                                                   remaining: 59.5ms
                                                   remaining: 59ms
363:
        learn: 0.0651568
                                  total: 158ms
364:
        learn: 0.0650111
                                  total: 158ms
                                                   remaining: 58.6ms
365:
        learn: 0.0649914
                                  total: 159ms
                                                   remaining: 58.1ms
366:
        learn: 0.0648867
                                  total: 159ms
                                                   remaining: 57.7ms
                                                   remaining: 57.2ms
367:
        learn: 0.0647691
                                  total: 160ms
368:
        learn: 0.0646332
                                  total: 160ms
                                                   remaining: 56.8ms
369:
        learn: 0.0646237
                                  total: 160ms
                                                   remaining: 56.3ms
370:
        learn: 0.0645225
                                  total: 161ms
                                                   remaining: 55.9ms
        learn: 0.0643725
                                                   remaining: 55.4ms
371:
                                  total: 161ms
372:
        learn: 0.0642983
                                  total: 162ms
                                                   remaining: 55ms
373:
        learn: 0.0642885
                                  total: 162ms
                                                   remaining: 54.5ms
374:
        learn: 0.0641988
                                  total: 162ms
                                                   remaining: 54.1ms
375:
        learn: 0.0640445
                                  total: 163ms
                                                   remaining: 53.7ms
376:
        learn: 0.0639296
                                  total: 163ms
                                                   remaining: 53.2ms
377:
        learn: 0.0638441
                                  total: 163ms
                                                   remaining: 52.8ms
378:
        learn: 0.0636968
                                  total: 164ms
                                                   remaining: 52.3ms
379:
        learn: 0.0636285
                                  total: 164ms
                                                   remaining: 51.9ms
380:
        learn: 0.0635146
                                  total: 165ms
                                                   remaining: 51.4ms
381:
        learn: 0.0634862
                                  total: 165ms
                                                   remaining: 51ms
382:
        learn: 0.0634776
                                  total: 165ms
                                                   remaining: 50.5ms
383:
        learn: 0.0634538
                                  total: 166ms
                                                   remaining: 50.1ms
384:
        learn: 0.0633181
                                  total: 166ms
                                                   remaining: 49.6ms
385:
        learn: 0.0632090
                                  total: 167ms
                                                   remaining: 49.2ms
        learn: 0.0631678
                                  total: 167ms
                                                   remaining: 48.8ms
386:
387:
        learn: 0.0631024
                                  total: 167ms
                                                   remaining: 48.3ms
388:
        learn: 0.0629520
                                  total: 168ms
                                                   remaining: 47.9ms
389:
        learn: 0.0629237
                                  total: 168ms
                                                   remaining: 47.4ms
390:
        learn: 0.0629132
                                  total: 169ms
                                                   remaining: 47ms
391:
        learn: 0.0628938
                                  total: 169ms
                                                   remaining: 46.5ms
392:
        learn: 0.0627817
                                  total: 169ms
                                                   remaining: 46.1ms
393:
        learn: 0.0627630
                                  total: 170ms
                                                   remaining: 45.7ms
394:
                                                   remaining: 45.2ms
        learn: 0.0627186
                                  total: 170ms
395:
        learn: 0.0626612
                                  total: 170ms
                                                   remaining: 44.8ms
396:
        learn: 0.0624649
                                  total: 171ms
                                                   remaining: 44.3ms
397:
        learn: 0.0624555
                                  total: 171ms
                                                   remaining: 43.9ms
398:
        learn: 0.0622719
                                  total: 172ms
                                                   remaining: 43.5ms
399:
        learn: 0.0621624
                                  total: 172ms
                                                   remaining: 43ms
400:
        learn: 0.0620698
                                  total: 172ms
                                                   remaining: 42.6ms
```

```
401:
        learn: 0.0619857
                                  total: 173ms
                                                   remaining: 42.1ms
402:
        learn: 0.0618966
                                  total: 173ms
                                                   remaining: 41.7ms
403:
        learn: 0.0618416
                                  total: 174ms
                                                   remaining: 41.3ms
404:
        learn: 0.0617317
                                  total: 174ms
                                                   remaining: 40.8ms
405:
        learn: 0.0616471
                                  total: 174ms
                                                   remaining: 40.4ms
                                  total: 175ms
                                                   remaining: 39.9ms
406:
        learn: 0.0615278
407:
        learn: 0.0614422
                                  total: 175ms
                                                   remaining: 39.5ms
        learn: 0.0614084
408:
                                  total: 176ms
                                                   remaining: 39.1ms
409:
        learn: 0.0613949
                                  total: 176ms
                                                   remaining: 38.6ms
410:
        learn: 0.0613085
                                  total: 176ms
                                                   remaining: 38.2ms
411:
        learn: 0.0611664
                                  total: 177ms
                                                   remaining: 37.8ms
412:
        learn: 0.0611203
                                  total: 177ms
                                                   remaining: 37.3ms
413:
        learn: 0.0610671
                                  total: 178ms
                                                   remaining: 36.9ms
414:
        learn: 0.0609378
                                  total: 178ms
                                                   remaining: 36.4ms
                                                   remaining: 36ms
415:
        learn: 0.0608414
                                  total: 178ms
416:
        learn: 0.0607825
                                  total: 179ms
                                                   remaining: 35.6ms
417:
        learn: 0.0607278
                                  total: 179ms
                                                   remaining: 35.1ms
418:
        learn: 0.0605999
                                  total: 180ms
                                                   remaining: 34.7ms
        learn: 0.0604808
                                  total: 180ms
                                                   remaining: 34.3ms
419:
420:
        learn: 0.0604245
                                  total: 180ms
                                                   remaining: 33.8ms
421:
        learn: 0.0603501
                                  total: 181ms
                                                   remaining: 33.4ms
422:
        learn: 0.0602624
                                  total: 181ms
                                                   remaining: 33ms
423:
        learn: 0.0601689
                                  total: 182ms
                                                   remaining: 32.5ms
424:
        learn: 0.0600350
                                  total: 182ms
                                                   remaining: 32.1ms
425:
        learn: 0.0599535
                                  total: 182ms
                                                   remaining: 31.7ms
                                                   remaining: 31.2ms
426:
        learn: 0.0599454
                                  total: 183ms
427:
        learn: 0.0599039
                                  total: 183ms
                                                   remaining: 30.8ms
428:
        learn: 0.0597689
                                  total: 183ms
                                                   remaining: 30.4ms
429:
        learn: 0.0597066
                                  total: 184ms
                                                   remaining: 29.9ms
430:
        learn: 0.0596721
                                  total: 184ms
                                                   remaining: 29.5ms
431:
        learn: 0.0596171
                                  total: 185ms
                                                   remaining: 29.1ms
432:
        learn: 0.0594849
                                  total: 185ms
                                                   remaining: 28.6ms
433:
        learn: 0.0593782
                                  total: 185ms
                                                   remaining: 28.2ms
                                  total: 186ms
434:
        learn: 0.0593612
                                                   remaining: 27.7ms
435:
        learn: 0.0592721
                                  total: 186ms
                                                   remaining: 27.3ms
436:
        learn: 0.0592573
                                  total: 186ms
                                                   remaining: 26.9ms
437:
        learn: 0.0590963
                                  total: 187ms
                                                   remaining: 26.4ms
438:
        learn: 0.0589709
                                  total: 187ms
                                                   remaining: 26ms
439:
        learn: 0.0588972
                                  total: 188ms
                                                   remaining: 25.6ms
440:
        learn: 0.0588460
                                  total: 188ms
                                                   remaining: 25.2ms
441:
                                  total: 188ms
        learn: 0.0587844
                                                   remaining: 24.7ms
442:
                                                   remaining: 24.3ms
        learn: 0.0586860
                                  total: 189ms
443:
                                  total: 189ms
                                                   remaining: 23.9ms
        learn: 0.0586775
444:
        learn: 0.0585845
                                  total: 190ms
                                                   remaining: 23.4ms
                                                   remaining: 23ms
445:
        learn: 0.0585538
                                  total: 190ms
446:
        learn: 0.0584986
                                  total: 190ms
                                                   remaining: 22.6ms
447:
        learn: 0.0584351
                                  total: 191ms
                                                   remaining: 22.1ms
448:
        learn: 0.0583892
                                  total: 191ms
                                                   remaining: 21.7ms
```

```
449:
        learn: 0.0582947
                                  total: 192ms
                                                   remaining: 21.3ms
450:
        learn: 0.0581681
                                  total: 192ms
                                                   remaining: 20.9ms
451:
        learn: 0.0580522
                                  total: 192ms
                                                   remaining: 20.4ms
452:
        learn: 0.0579769
                                                   remaining: 20ms
                                  total: 193ms
453:
        learn: 0.0579641
                                  total: 193ms
                                                   remaining: 19.6ms
                                                   remaining: 19.1ms
454:
        learn: 0.0579129
                                  total: 194ms
455:
        learn: 0.0578812
                                  total: 194ms
                                                   remaining: 18.7ms
456:
        learn: 0.0577979
                                  total: 194ms
                                                   remaining: 18.3ms
457:
        learn: 0.0576452
                                  total: 195ms
                                                   remaining: 17.9ms
458:
        learn: 0.0575459
                                  total: 195ms
                                                   remaining: 17.4ms
459:
        learn: 0.0574926
                                  total: 195ms
                                                   remaining: 17ms
460:
        learn: 0.0574239
                                  total: 196ms
                                                   remaining: 16.6ms
461:
                                  total: 196ms
        learn: 0.0573261
                                                   remaining: 16.1ms
462:
        learn: 0.0573016
                                  total: 197ms
                                                   remaining: 15.7ms
                                                   remaining: 15.3ms
463:
        learn: 0.0572923
                                  total: 197ms
464:
        learn: 0.0571525
                                  total: 198ms
                                                   remaining: 14.9ms
465:
        learn: 0.0571299
                                  total: 198ms
                                                   remaining: 14.4ms
466:
        learn: 0.0571070
                                  total: 198ms
                                                   remaining: 14ms
                                  total: 199ms
                                                   remaining: 13.6ms
467:
        learn: 0.0570410
468:
        learn: 0.0569051
                                  total: 199ms
                                                   remaining: 13.2ms
469:
        learn: 0.0568072
                                  total: 200ms
                                                   remaining: 12.7ms
470:
        learn: 0.0567259
                                  total: 200ms
                                                   remaining: 12.3ms
471:
        learn: 0.0566775
                                  total: 200ms
                                                   remaining: 11.9ms
472:
        learn: 0.0566140
                                  total: 201ms
                                                   remaining: 11.5ms
473:
        learn: 0.0565948
                                  total: 201ms
                                                   remaining: 11ms
474:
        learn: 0.0565817
                                  total: 202ms
                                                   remaining: 10.6ms
475:
        learn: 0.0564952
                                  total: 202ms
                                                   remaining: 10.2ms
476:
        learn: 0.0564860
                                  total: 202ms
                                                   remaining: 9.76ms
477:
        learn: 0.0563526
                                  total: 203ms
                                                   remaining: 9.33ms
478:
        learn: 0.0563435
                                  total: 203ms
                                                   remaining: 8.9ms
479:
        learn: 0.0562452
                                  total: 203ms
                                                   remaining: 8.48ms
480:
        learn: 0.0561724
                                  total: 204ms
                                                   remaining: 8.05ms
481:
        learn: 0.0560920
                                  total: 204ms
                                                   remaining: 7.63ms
482:
        learn: 0.0559455
                                  total: 205ms
                                                   remaining: 7.2ms
483:
        learn: 0.0558619
                                  total: 205ms
                                                   remaining: 6.78ms
484:
        learn: 0.0557850
                                  total: 205ms
                                                   remaining: 6.35ms
485:
        learn: 0.0557517
                                  total: 206ms
                                                   remaining: 5.93ms
486:
        learn: 0.0557035
                                  total: 206ms
                                                   remaining: 5.5ms
487:
        learn: 0.0555446
                                  total: 207ms
                                                   remaining: 5.08ms
488:
        learn: 0.0554460
                                  total: 207ms
                                                   remaining: 4.66ms
489:
                                  total: 207ms
        learn: 0.0553907
                                                   remaining: 4.23ms
490:
        learn: 0.0553813
                                  total: 208ms
                                                   remaining: 3.81ms
491:
        learn: 0.0552869
                                  total: 208ms
                                                   remaining: 3.38ms
492:
        learn: 0.0552775
                                  total: 209ms
                                                   remaining: 2.96ms
                                                   remaining: 2.54ms
493:
        learn: 0.0552221
                                  total: 209ms
494:
        learn: 0.0551432
                                  total: 209ms
                                                   remaining: 2.11ms
495:
        learn: 0.0550586
                                  total: 210ms
                                                   remaining: 1.69ms
496:
        learn: 0.0550073
                                  total: 210ms
                                                   remaining: 1.27ms
```

```
497:
              learn: 0.0549060
                                      total: 211ms
                                                      remaining: 845us
      498:
              learn: 0.0548913
                                      total: 211ms
                                                       remaining: 422us
              learn: 0.0548346
      499:
                                      total: 211ms
                                                       remaining: Ous
[596]: <catboost.core.CatBoostRegressor at 0x7f6cc009afd0>
 [7]: cat_train_pred = best_model.predict(X_train)
      print(f'CatBoost Train RMSE {rmse(y_train, xgb_train_pred)}')
      cat_pred = best_model.predict(X_test)
      print(f'CatBoost Test RMSE {rmse(y_test, xgb_pred)}')
      CatBoost Train RMSE 0.04
      CatBoost Test RMSE 0.12
```

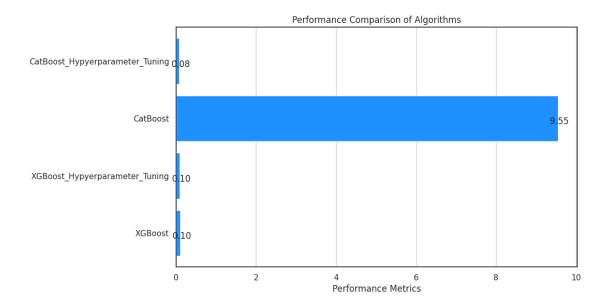
5 Result Analysis

Performance Comparison

```
[637]: result = {
           'XGBoost': [0.09, 0.12],
           'XGBoost_Hypyerparameter_Tuning': [0.06,0.13],
           'CatBoost': [9.53, 9.57],
           'CatBoost_Hypyerparameter_Tuning': [0.04,0.12],
       }
       labels = list(result.keys())
       values = [np.mean(v) for v in result.values()]
       plt.figure(figsize=(10, 6))
       bars = plt.barh(labels, values, color='dodgerblue')
       for bar in bars:
           plt.text(bar.get_width() - 0.2, bar.get_y() + bar.get_height()/2 - 0.1,

¬f"{bar.get_width():.2f}")

       plt.xlabel('Performance Metrics')
       plt.title('Performance Comparison of Algorithms')
       plt.grid(axis='x')
       plt.show()
```



I have run experiments on XGBoost and CatBoost which both have strong benefits in both categorical and numerical data. - Without Hyperparameter Tuning, - XGBoost achieves training RMSE 0.09 and testing RMSE 0.12. The model can be improved with better hyperparameters. - CatBoost achieves training RMSE 9.53 and testing RMSE 9.57, which is relatively higher than XGBoost. The model is underfitting. - With Hyperparameter Tuning, - XGBoost has slightly lower training RMSE 0.06 but testing RMSE 0.13. The model is overfit and doesn't seem to generalize on the training data. It might have been memorizing it. - CatBoost achieves significantly higher performance than the one without tuning. CatBoost training RMSE 0.04 and testing RMSE 0.12.

```
Let's compare the prediction and ground truth.

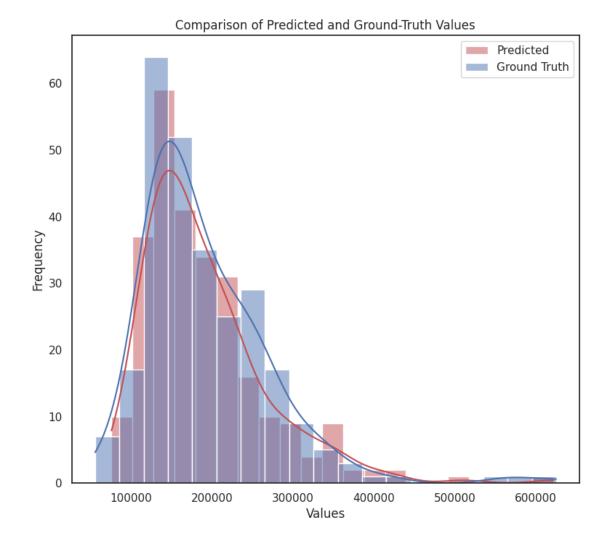
[642]: predictions = best_model.predict(X_test)
    predictions = np.expm1(predictions)

[644]: y_test_reversed = np.expm1(y_test)

[650]: plt.figure(figsize=(9, 8))
    sns.histplot(predictions, kde=True, label='Predicted', color='r')
    sns.histplot(y_test_reversed, kde=True, label='Ground Truth', color='b')

plt.xlabel('Values')
    plt.ylabel('Frequency')
    plt.title('Comparison of Predicted and Ground-Truth Values')
    plt.legend()

# Show the plot
    plt.show()
```



The plot shows that the trend of prediction is similar to the ground truth.

6 Conclusion and Further Work

In the future, I want to use K-nearest neighbors to replace missing values so that we do not need to drop many data points. I will perform more hyperparameter tuning. I also want to explore with different supervised learning algorithms. I want see the performance of simple linear regression.