

2018 春大学物理 C 作业八

第十章 机械波

一、选择题

1.C 2.B 3.D 4.C 5.C 6.C 7.A 8.B 9.C 10.B

二、填空题

1. $a = -0.2\pi^2 \cos(\pi t + \frac{3}{2}\pi x)$ (SI)

2. $y = A \cos[2\pi(\nu t + \frac{x+L}{\lambda}) + \frac{\pi}{2}]$

$t_1 + \frac{L}{\lambda\nu} + \frac{k}{\nu}, \quad k=0, \pm 1, \pm 2, \dots$ [只写 $t_1 + L/(\lambda\nu)$ 也可以]

3. $y_p = 0.2 \cos(\frac{1}{2}\pi t - \frac{1}{2}\pi)$

4. $y = 12.0 \times 10^{-2} \cos(\frac{1}{2}\pi x) \cos 20\pi t$ (SI)

$x = (2k+1) \text{ m}, \quad \text{即 } x = 1 \text{ m}, 3 \text{ m}, 5 \text{ m}, 7 \text{ m}, 9 \text{ m}$

$x = 2k \text{ m}, \quad \text{即 } x = 0 \text{ m}, 2 \text{ m}, 4 \text{ m}, 6 \text{ m}, 8 \text{ m}, 10 \text{ m}$

三、计算题

1. 解:

(1) $y = 0.1 \cos(4\pi t - \frac{2}{10}\pi x) = 0.1 \cos 4\pi(t - \frac{1}{20}x)$ (SI)

(2) $t_1 = T/4 = (1/8) \text{ s}, \quad x_1 = \lambda/4 = (10/4) \text{ m}$ 处质点的位移

$$y_1 = 0.1 \cos 4\pi(T/4 - \lambda/80) \\ = 0.1 \cos 4\pi(1/8 - \frac{1}{8}) = 0.1 \text{ m}$$

(3) 振速 $v = \frac{\partial y}{\partial t} = -0.4\pi \sin 4\pi(t - x/20).$

$t_2 = \frac{1}{2}T = (1/4) \text{ s}, \quad \text{在 } x_1 = \lambda/4 = (10/4) \text{ m}$ 处质点的振速

$$v_2 = -0.4\pi \sin(\pi - \frac{1}{2}\pi) = -1.26 \text{ m/s}$$

2. 解:

(1) 振动方程: $y = A \cos(\omega t + \phi_0) \quad A = 10 \text{ cm},$

$$\omega = 2\pi\nu = \pi \text{ s}^{-1}, \quad \nu = u/\lambda = 0.5 \text{ Hz}$$

初始条件:

$$y(0, 0) = 0$$

$$\dot{y}(0, 0) > 0 \quad \text{得} \quad \phi_0 = -\frac{1}{2}\pi$$

故得原点振动方程: $y = 0.10 \cos(\pi t - \frac{1}{2}\pi)$ (SI)

(2) $x = 150 \text{ cm}$ 处相位比原点落后 $\frac{3}{2}\pi$, 所以

$$y = 0.10 \cos(\pi t - \frac{1}{2}\pi - \frac{3}{2}\pi) = 0.10 \cos(\pi t - 2\pi) \quad (\text{SI})$$

也可写成 $y = 0.10 \cos \pi t$ (SI)