

```
#include "llvm/ADT/DenseMap.h"
29
30
     #include "llvm/ADT/DenseSet.h"
     #include "llvm/ADT/STLExtras.h"
31
32
     #include "llvm/ADT/StringExtras.h"
33
     #include "llvm/ADT/iterator range.h"
34
     #include "llvm/Support/Alignment.h"
35
     #include "llvm/Support/Casting.h"
     #include "llvm/Support/ErrorOr.h"
36
37
     #include "tensorflow/compiler/mlir/hlo/include/mlir-hlo/Analysis/shape_component_analysis.h"
38
     #include "tensorflow/compiler/mlir/hlo/include/mlir-hlo/Dialect/mhlo/IR/hlo_ops.h"
39
     #include "tensorflow/compiler/mlir/hlo/include/mlir-hlo/Dialect/mhlo/transforms/rewriters.h"
     #include "tensorflow/compiler/mlir/tfrt/jit/transforms/tf cpurt passes.h"
40
41
42
     namespace tensorflow {
43
     namespace {
44
45
     using llvm::ArrayRef;
46
     using llvm::SmallVector;
47
     using mlir::AffineExpr;
48
49
     using mlir::AffineMap;
50
     using mlir::failure;
     using mlir::FuncOp;
51
     using mlir::FunctionPass;
52
53
     using mlir::Location;
54
     using mlir::LogicalResult;
     using mlir::MLIRContext;
55
     using mlir::OpBuilder;
56
     using mlir::RankedTensorType;
57
58
     using mlir::ShapeComponentAnalysis;
     using mlir::success;
59
60
     using mlir::TypeRange;
     using mlir::Value;
61
62
     using mlir::ValueRange;
63
     using mlir::arith::ConstantIndexOp;
     using mlir::arith::ConstantOp;
64
65
     using mlir::arith::IndexCastOp;
66
67
     namespace linalg = mlir::linalg;
68
     namespace mhlo = mlir::mhlo;
69
     namespace shape = mlir::shape;
70
     namespace tensor = mlir::tensor;
71
72
     #define GEN_PASS_CLASSES
73
     #include "tensorflow/compiler/mlir/tfrt/jit/transforms/tf_cpurt_passes.h.inc"
74
75
76
77
     // Rewrite shape.cstr_broadcastable with constant witness if can prove that
```

```
78
      // shapes are broadcastable from the symbolic shapes.
79
80
      class CstrBroadcastableOpLowering
          : public mlir::OpRewritePattern<shape::CstrBroadcastableOp> {
81
       public:
82
        using Base = OpRewritePattern<shape::CstrBroadcastableOp>;
83
84
85
        explicit CstrBroadcastableOpLowering(MLIRContext* ctx);
86
87
        LogicalResult matchAndRewrite(shape::CstrBroadcastableOp op,
88
                                       mlir::PatternRewriter& rewriter) const override;
89
      };
90
91
      CstrBroadcastableOpLowering::CstrBroadcastableOpLowering(MLIRContext* ctx)
92
          : Base(ctx) {}
93
94
      // Returns true if all of bcasted_shapes can be broadcasted with output_shape.
      bool isKnownBroadcastable(ShapeComponentAnalysis& analysis,
95
                                ValueRange bcasted shapes, Value output shape) {
96
97
        auto output shape dims = analysis.dimensionsForShapeTensor(output shape);
98
        if (!output_shape_dims) return false;
99
        for (Value shape : bcasted shapes) {
          auto shape dims = analysis.dimensionsForShapeTensor(shape);
100
          if (!shape dims) return false;
101
          // Iterate backwards over the smallest input shape.
102
          for (auto zip : llvm::zip(llvm::reverse(*output_shape_dims),
103
104
                                     llvm::reverse(*shape_dims))) {
            const auto& first = std::get<0>(zip);
105
106
            const auto& second = std::get<1>(zip);
107
            // TODO(ezhulenev): What to do with dimensions statically known to be
            // zero?
108
109
            // Numpy can only broadcast [0] with [1], however Tensorflow can broadcast
            // [0] with any dimension size, and produces dimension of size [0].
110
111
            // Currently we'll conservatively return failure and will not proceed with
112
            // a rewrite.
            if (first.isConstant(0) || second.isConstant(0)) return false;
113
            // If either shape has a static one dimension the broadcast will always
114
115
            // succeed.
            if (first.isConstant(1) || second.isConstant(1)) continue;
116
            // Otherwise dims have to be equal.
117
118
            if (first != second) return false;
119
          }
120
        }
121
        return true;
122
      }
123
      LogicalResult CstrBroadcastableOpLowering::matchAndRewrite(
124
125
          shape::CstrBroadcastableOp op, mlir::PatternRewriter& rewriter) const {
126
        ShapeComponentAnalysis shape_component_analysis;
```

```
127
             if (!isKnownBroadcastable(shape component analysis, op.getShapes(),
    128
                                       op.getShapes().front()))
    129
               return failure();
    130
             // Replace constraint with a true witness.
    131
             rewriter.replaceOpWithNewOp<shape::ConstWitnessOp>(op, true);
    132
    133
    134
             return success();
           }
    135
    136
    137
           // Replace shape.broadcast with a shape if it's statically known.
           class BroadcastOpLowering final
    138
               : public mlir::OpRewritePattern<shape::BroadcastOp> {
    139
           public:
    140
    141
            explicit BroadcastOpLowering(MLIRContext* ctx) : OpRewritePattern(ctx) {}
    142
             LogicalResult matchAndRewrite(shape::BroadcastOp op,
    143
    144
                                           mlir::PatternRewriter& rewriter) const override;
    145
           };
    146
    147
           // Returns a shape tensor if the shapes can be broadcasted to a known shape.
    148
           // Will either return one of the shapes or a generated mix of the shapes.
••• 149
           11vm::Optional<Value> simplifyBroadcast(ShapeComponentAnalysis& analysis,
    150
                                                   ValueRange shapes, Location loc,
    151
                                                    OpBuilder* builder) {
             // First find the input shape with the largest rank.
    152
             SmallVector<ArrayRef<ShapeComponentAnalysis::SymbolicDimension>> shapes_found;
    153
             size_t maxRank = 0;
    154
             for (auto shape : llvm::enumerate(shapes)) {
    155
               auto found_shape = analysis.dimensionsForShapeTensor(shape.value());
    156
    157
               if (!found_shape) return {};
               shapes_found.push_back(*found_shape);
    158
               maxRank = std::max(maxRank, found_shape->size());
    159
    160
             }
    161
             SmallVector<const ShapeComponentAnalysis::SymbolicDimension*>
    162
    163
                 joined_dimensions(maxRank);
             SmallVector<std::pair<Value, int64_t>> shape_and_rank_for_dim(maxRank);
    164
             for (auto shape : llvm::enumerate(shapes_found)) {
    165
               for (auto dim : llvm::enumerate(llvm::reverse(shape.value()))) {
    166
    167
                 // 1 dimensions don't contribute to the final result.
    168
                 if (dim.value().isConstant(1)) continue;
                 // If it's not a 1 dimension it will be present in the result. Remember
    169
                 // where it came from.
    170
    171
                 auto index = maxRank - dim.index() - 1;
                 if (!joined_dimensions[index]) {
    172
                   joined_dimensions[index] = &dim.value();
    173
                   shape_and_rank_for_dim[index] =
    174
    175
                       std::make_pair(shapes[shape.index()], shape.value().size());
```

```
176
              continue;
177
178
            // Bail if the dimensions are neither equal nor 1.
            if (*joined_dimensions[index] != dim.value()) return {};
179
          }
180
181
        // If the output is the same as one of the inputs just return that.
182
        if (llvm::is_splat(shape_and_rank_for_dim) &&
183
            shape and rank for dim[0].first) {
184
185
          return shape_and_rank_for_dim[0].first;
186
187
        // Otherwise rematerialize the shape from the pieces we have.
188
        SmallVector<Value> elements;
        for (int i = 0; i != maxRank; ++i) {
189
190
          // 1 dimensions are filtered above, recreate the constant.
191
          if (!shape and rank for dim[i].first) {
            auto one = builder->getIntegerAttr(
192
193
                shapes[0].getType().cast<RankedTensorType>().getElementType(), 1);
194
            elements.push back(builder->create<ConstantOp>(loc, one));
195
            continue;
196
          }
197
          // Extract from one of the shapes, accounting for the reverse indexing
198
          // performed by broadcast.
          Value index = builder->create<ConstantIndexOp>(
199
200
              loc, i - maxRank + shape_and_rank_for_dim[i].second);
201
          elements.push_back(builder->create<tensor::ExtractOp>(
202
              loc, shape_and_rank_for_dim[i].first, index));
203
204
        return Value(builder->create<tensor::FromElementsOp>(loc, elements));
205
      }
206
207
      LogicalResult BroadcastOpLowering::matchAndRewrite(
          shape::BroadcastOp op, mlir::PatternRewriter& rewriter) const {
208
209
        ShapeComponentAnalysis shape_component_analysis;
210
        auto new broadcast = simplifyBroadcast(
211
            shape_component_analysis, op.getShapes(), op.getLoc(), &rewriter);
212
        if (!new_broadcast) return failure();
213
        rewriter.replaceOp(op, {*new_broadcast});
214
        return success();
      }
215
216
217
218
219
      // Rewrite mhlo.dynamic_broadcast_in_dim operation into linalg.generic operation
220
      // if can infer the indexing maps for the operand from the symbolic shapes.
221
      class DynamicBroadcastInDimOpLowering
222
          : public mlir::OpRewritePattern<mhlo::DynamicBroadcastInDimOp> {
223
       public:
224
        using Base = OpRewritePattern<mhlo::DynamicBroadcastInDimOp>;
```

```
225
226
        explicit DynamicBroadcastInDimOpLowering(MLIRContext* ctx);
227
228
        LogicalResult matchAndRewrite(mhlo::DynamicBroadcastInDimOp op,
229
                                      mlir::PatternRewriter& rewriter) const override;
230
      };
231
232
      DynamicBroadcastInDimOpLowering::DynamicBroadcastInDimOpLowering(
          MLIRContext* ctx)
233
234
          : Base(ctx) {}
235
      // Check if broadcasting `from` to `to shape` is statically known to only have
236
      // dimensions that never expand or always expand.
237
238
      11vm::Optional<AffineMap> isNonExpandingBroadcast(
239
          ShapeComponentAnalysis& analysis, Value from, Value to shape) {
        auto in shape = analysis.dimensionsForShape(from);
240
        auto out_shape = analysis.dimensionsForShapeTensor(to_shape);
241
        if (!in shape || !out shape) return {};
242
243
        SmallVector<AffineExpr> input map exprs;
244
245
        size_t rank = out_shape->size();
246
        MLIRContext* ctx = (*out shape)[0].expr.getContext();
247
        size t d = 0;
        auto affine_zero = getAffineConstantExpr(0, ctx);
248
249
        for (auto zip :
             llvm::zip(llvm::reverse(*in_shape), llvm::reverse(*out_shape))) {
250
          const auto& in = std::get<0>(zip);
251
          const auto& out = std::get<1>(zip);
252
          bool extend = in.isConstant(1) && !out.isConstant(1);
253
          input_map_exprs.push_back(extend ? affine_zero
254
255
                                            : getAffineDimExpr(rank - d - 1, ctx));
256
          ++d;
257
          // Bail if this is neither a known expansion nor a known non-expansion.
258
259
          if (!extend && in != out) return {};
260
261
        // Any leading dimensions will be expanded.
262
        input map exprs.resize(in shape->size(), affine zero);
        std::reverse(input_map_exprs.begin(), input_map_exprs.end());
263
        return AffineMap::get(/*dimCount=*/rank,
264
265
                               /*symbolCount=*/0, input_map_exprs, ctx);
266
      }
267
268
      LogicalResult DynamicBroadcastInDimOpLowering::matchAndRewrite(
          mhlo::DynamicBroadcastInDimOp op, mlir::PatternRewriter& rewriter) const {
269
        MLIRContext* ctx = getContext();
270
271
272
        auto in_type = op.operand().getType().dyn_cast<RankedTensorType>();
273
        auto out_type = op.getResult().getType().dyn_cast<RankedTensorType>();
```

```
274
        if (!in type || !out type) return failure();
275
276
        // Check that broadcast is right-aligned (numpy style), so that operand
277
        // dimensions broadcasted to match inner-most dimensions of the output.
278
        auto bcast dims = op.broadcast dimensions().getValues<int64 t>();
279
        auto expected bcast dims = llvm::seq<int64 t>(
            out_type.getRank() - in_type.getRank(), out_type.getRank());
280
        if (!llvm::equal(bcast_dims, expected_bcast_dims)) return failure();
281
282
283
        ShapeComponentAnalysis shape_component_analysis;
284
        auto input_map = isNonExpandingBroadcast(
            shape_component_analysis, op.operand(), op.output_dimensions());
285
        if (!input map) return failure();
286
287
288
        // Resolve dynamic output dimensions for the `linalg.init tensor` operation.
289
        SmallVector<Value> output dyn dimensions;
290
        Location loc = op.getLoc();
291
        int64_t rank = out_type.getRank();
292
        for (size t d = 0; d < rank; ++d) {
          int64_t output_dim = out_type.getShape()[d];
293
294
295
          // Skip static output dimensions, they will be resolved from the shape.
296
          if (output dim >= 0) continue;
297
298
          // Resolve the dynamic size of the output dimension.
          Value output_dyn_dim = rewriter.create<tensor::ExtractOp>(
299
300
              loc, op.output_dimensions(),
              ValueRange{rewriter.create<ConstantIndexOp>(loc, d)});
301
302
303
          // Symbolic shape analysis might have given us an i32 or i64. Cast to index.
304
          if (!output dyn dim.getType().isIndex())
305
            output_dyn_dim = rewriter.create<IndexCastOp>(loc, output_dyn_dim,
306
                                                           rewriter.getIndexType());
307
308
          output dyn dimensions.push back(output dyn dim);
309
        }
310
311
        // Create a linalg.tensor init operation to initialize output.
312
        Value init = rewriter.create<linalg::InitTensorOp>(loc, output_dyn_dimensions,
313
                                                            out_type.getShape(),
314
                                                            out_type.getElementType());
315
        // Output indexing map is an identity with `rank` number of loops.
316
        AffineMap output_map = AffineMap::getMultiDimIdentityMap(rank, ctx);
317
318
319
        // All iterators are parallel.
        SmallVector<llvm::StringRef> iterator_types(rank, "parallel");
320
321
322
        rewriter.replaceOpWithNewOp<linalg::GenericOp>(
```

```
323
           op, /*resultTensorTypes=*/TypeRange{init.getType()},
324
           /*inputs=*/ValueRange{op.operand()},
           /*outputs=*/ValueRange{init},
325
           /*indexingMaps=*/llvm::makeArrayRef({*input_map, output_map}),
326
           /*iteratorTypes=*/iterator_types,
327
           [&](OpBuilder& nested builder, Location nested loc, ValueRange args) {
328
             nested_builder.create<linalg::YieldOp>(nested_loc, args[0]);
329
330
           });
331
332
       return success();
333
     }
334
      // ------ //
335
336
      // Optimize function based on the symbolic shape attributes.
337
      // ------ //
338
339
     struct SymbolicShapeOptimizationPass
340
          : public SymbolicShapeOptimizationBase<SymbolicShapeOptimizationPass> {
341
       SymbolicShapeOptimizationPass() = default;
342
343
       explicit SymbolicShapeOptimizationPass(bool constraints_only) {
344
         this->optimize only constraints = constraints only;
345
       }
346
347
       void runOnFunction() override {
         FuncOp func = getFunction();
348
349
         MLIRContext* ctx = &getContext();
350
         mlir::RewritePatternSet patterns(ctx);
351
352
353
         // Rewrite constraints based on the symbolic shapes.
354
         patterns.insert<CstrBroadcastableOpLowering>(ctx);
         // Rewrite shape.broadcast based on the symbolic shapes.
355
356
         patterns.insert<BroadcastOpLowering>(ctx);
357
358
         // Move broadcasts up across mhlo operations to enable more opportunities
359
         // for constraints and broadcasts optimizations. These patterns are only
360
         // applicable if we do not lower mhlo broadcasts to linalg.generic.
         if (optimize_only_constraints)
361
           mlir::mhlo::PopulateBroadcastsPropagationPatterns(ctx, &patterns);
362
363
364
         // Rewrite broadcasts based on the symbolic shapes if enabled.
         if (!optimize_only_constraints)
365
           patterns.insert<DynamicBroadcastInDimOpLowering>(ctx);
366
367
368
         // Add shape dialect canonicalization patterns to fold shape operations
         // after constraints are replaced with constant witness.
369
         mlir::Dialect* shape_dialect = ctx->getLoadedDialect<shape::ShapeDialect>();
370
         for (auto* op : ctx->getRegisteredOperations()) {
371
```

```
if (op->dialect.getTypeID() == shape_dialect->getTypeID())
372
              op->getCanonicalizationPatterns(patterns, ctx);
373
374
          }
375
          (void)mlir::applyPatternsAndFoldGreedily(func, std::move(patterns));
376
377
        }
378
      };
379
380
      } // namespace
381
382
      std::unique_ptr<FunctionPass> CreateSymbolicShapeOptimizationPass(
          bool constraints_only) {
383
        return std::make_unique<SymbolicShapeOptimizationPass>(constraints_only);
384
      }
385
386
387
      } // namespace tensorflow
```