Experiment 6 Millikan's Oil Drop

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Synopsis

In this experiment we measure the charge of an electron using Millikan's oil drop method.

I. THEORY

Consider a spherical oil droplet of radius r and density ρ falling under the gravitational force. This droplet in air is acted upon by a constant force and soon reaches a terminal velocity given by Stokes' law, $F_n = 6\pi \eta r v_f$, where η is the coefficient of viscosity of air and v_f is the terminal velocity during the fall. The gravitational and buoyancy forces acting on the droplet are balanced by F_n :

$$\frac{4}{3}\pi r^3 \rho g - \frac{4}{3}\pi r^3 \rho_a g = 6\pi \eta r v_f. \tag{1}$$

Here, ρ_a is the density of air. The falling velocity v_f is thus given by

$$v_f = \frac{2}{9} \frac{gr^2}{n} (\rho - \rho_a). \tag{2}$$

If the droplet carries a charge ne and is moving upward with terminal velocity v, under the influence of the applied electric field V/d between the parallel plate electrodes separated by the distance d and potential difference V, the force balance equation is:

$$\frac{4}{3}\pi r^3(\rho - \rho_a)g + 6\pi \eta rv = \frac{Vne}{d}.$$
(3)

Subtracting Eq. (2) from Eq. (4) and solving for ne, we get

$$ne = \frac{6\pi\eta rd}{V}(v_f + v). \tag{4}$$

Dividing Eq. (4) by Eq. (3), gives

$$ne = \frac{4\pi}{3} \frac{gd}{V} (\rho - \rho_a) r^3 \left(1 + \frac{v}{v_f} \right). \tag{5}$$

The Stokes' law used in obtaining Eqs. (1)–(5) assumes that the droplets are moving slowly, that there is no slipping of the medium over the surface of the droplet, that the medium is of quite large extent compared to the size of the droplet, and that the inhomogeneities in the medium are of a size small compared to the size of the droplets. In the present case, all the assumptions except the last one are reasonably valid. The radii of the droplets are of the order of one micron and therefore not much greater than the mean free path of the air molecules. The droplets will tend to fall more quickly in the free space between the air molecules. The expression for the falling velocity v_f , corrected for this effect, on the basis of kinetic theory is

$$v_f = \frac{2}{9} \frac{gr^2}{n} (\rho - \rho_a) \left(1 + \frac{c}{Pr} \right), \tag{6}$$

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where $c = 6.17 \times 10^{-8}$ m of Hg·m is a correction factor and P (in m of Hg) is the atmospheric pressure. Writing

$$\xi = \frac{9\eta}{2g} \frac{v_f}{(\rho - \rho_a)} \tag{7}$$

$$\zeta = \frac{c}{2P},\tag{8}$$

Eq. (6) now reduces to

$$r^2 + 2\zeta r - \xi = 0. \tag{9}$$

The radius of the droplet is given by the positive root of this equation

$$r = -\zeta + \sqrt{\zeta^2 + \xi}.\tag{10}$$

The charge ne may be obtained by first calculating ξ and ζ from Eqs. (7) and (8), then calculating the radius r from Eq. (10) and finally ne from Eq. (5).

Equation (5) above is for the 'Dynamic' method. In the 'Balancing' method, the droplet is kept stationary by adjusting the potential. The upward velocity is thus equal to zero. The final equation for *ne* in the 'Balancing' method is therefore

$$ne = \frac{4\pi}{3} \frac{gd}{V_b} (\rho - \rho_a) r^3, \tag{11}$$

where V_b is the balancing potential.

II. PROCEDURE

- 1. Read the user manual [4].
- 2. Note the atmospheric pressure and the room temperature.
- 3. Switch on the power supply.
- 4. Adjust the leveling screws in the base of the panel and check the level indicator at the top.
- 5. Wait for about ten minutes.
- 6. Fix two horizontal lines on the monitor. These are the preset lines. The rise and fall times of the droplets to move from one line to the other are to be recorded. A good choice is to choose the second line from the top and the last but one line from the bottom. This will leave some room at the top and at the bottom for maneuvering and preventing the droplet from getting lost.
- 7. Press the 'clear key' to make the 'time meter' read zero.
- 8. Spray droplets of oil from the atomizer. One or two squirts are usually sufficient.
- 9. As the droplets drift down, some of them pass through the hole in the upper parallel plate and reach the region in-between the plates where they are illuminated.
- 10. These are viewed by the microscope/camera as unresolved points of diffracted light and the images are transmitted to the monitor screen.
- 11. These droplets drift down slowly under gravitational force.
- 12. Under the influence of the electric field between the plates, the motion of the droplets will get affected if they are charged. If a droplet moves downward more slowly under the influence of the electric force (corresponding to the upper plate at a positive potential), the drop is negatively charged. Its motion can be arrested or even reversed (made to rise) by an increase in the potential. If the downward drifting of the droplet increases under the action of electric force, the droplet is positively charged. Such droplets are ignored in the present set-up.

- 13. Suitable negatively charged droplet is selected. 'Suitable' means that it drifts downward slowly (about 10-15 s free-fall time) under gravitational field indicating that the droplet is not too heavy. Its mass should also not be too small, otherwise it will bounce around due to random collisions with air molecules, *Brownian motion*, and it will be difficult to estimate when the droplet actually crosses a line. A very small droplet may cross a line 10-20 times. It should also be possible to make it rise by applying a voltage of about 500 V indicating that there are only a few charge quanta on the droplet. Fix some value of the voltage.
- 14. This selection is done by concentrating on one or two droplets and removing all others from the field by switching on and switching off the electric field.
- 15. Once a droplet has been chosen, measurements can begin. There are two approaches:
 - (a) Dynamic: Measure the free-fall time with the voltage off and the rise time with some suitable voltage on for the droplet to move between the two above chosen lines on the monitor. For these measurements, follow the procedure below:
 - i. Pull the droplet above the top chosen line on the monitor by adjusting the voltage.
 - ii. Press the 'clear key' to make the 'time meter' read zero.
 - iii. Switch off the voltage, the droplet will begin to fall freely.
 - iv. Start the 'time meter' by pressing the 'start/stop' key when the droplet crosses the top chosen line on the monitor.
 - v. Stop the 'time meter' by pressing the 'start/stop' key again when the droplet crosses the bottom chosen line on the monitor.
 - vi. Stop the downward motion of the droplet by switching on the voltage.
 - vii. Note the fall time from the 'time meter.'
 - viii. Press the 'clear key' to make the 'time meter' read zero.
 - ix. Allow the droplet to come below the bottom line by switching off the voltage.
 - x. Switch on the voltage (its value already fixed earlier), the droplet will begin to rise.
 - xi. Start the 'time meter' when the droplet crosses the chosen bottom line on the monitor.
 - xii. Stop the 'time meter' when the droplet crosses the top chosen line on the monitor.
 - xiii. Stop the upward motion of the droplet by switching off the voltage.
 - xiv. Note the rise time and the voltage.

Repeat these measurements of free-fall time and rise time several times. Take the average of these timings for the free-fall and the rise and note the voltage (kept fixed). Take another suitable droplet if it is there. If not, spray droplets again. Choose a suitable one and proceed as above to get data on several droplets.

(b) Balancing: Measure the free-fall time as in the above 'Dynamic method' for the droplet to move between the two chosen lines on the monitor. Apply the voltage and adjust its value such that the electric force on the droplet just balances other forces on it and the droplet hangs (does not move up or down). The droplet should remain stationary for several minutes. The voltage may have to be adjusted again and again.

Take the average value of these voltages and the average of the free-fall timings. Take another suitable droplet if it is there. If not, spray droplets again. Choose a suitable one and proceed as above to get on several droplets.

16. Note the atmospheric pressure and the room temperature at the end of the experiment as well.

III. OBSERVATIONS

- 1. Distance d between the plates =
- 2. Distance L between the chosen top and bottom lines of the monitor =

A. Dynamic Method

Drop No.	S. No.	Free-fall Time (s)	Rise Time	$egin{array}{c} \mathbf{Mean} \\ \mathbf{Free-fall} \\ \mathbf{Time} \; (t_f) \\ \mathbf{(s)} \end{array}$	$\begin{array}{c} \text{Mean Rise} \\ \text{Time } (t_r \; (\mathbf{s}) \end{array}$	$egin{aligned} \mathbf{Mean} \\ \mathbf{Free-fall} \\ \mathbf{Velocity} \\ (V_f = L/t_f) \\ \mathbf{m/s} \end{aligned}$	Voltage (V)
1							
2							
3							
4							
4							
5							

TABLE I. Data from Dynamic Method

B. Balancing Method

Drop No.	S. No.	Free-fall Time (s)	$egin{array}{c} ext{Mean} \ ext{Free-fall} \ ext{Time} \ (t_f) \ ext{(s)} \end{array}$	$egin{array}{c} ext{Mean Free-fall} \ ext{Velocity} \ (V_f = L/t_f) ext{ m/s} \end{array}$	Balancing Voltage (v)	Final Balancing Voltage (V)
1						
2						
3						
4						
5						

TABLE II. Data from Balancing Method

- 3. Density ρ of the oil =
- 4. Density ρ_a of air =
- 5. Room temperature T =
- 6. Atmospheric pressure P =
- 7. Coefficient of viscosity of air $\eta =$

IV. CALCULATION

A. Common constants

1.
$$C = 4\pi dg(\rho - \rho_a)/3 =$$

2.
$$D = 9\eta/2g(\rho - \rho_a) =$$

3.
$$\zeta = c/2P =$$

4.
$$c =$$

B. Calculation form droplet data

1. Dynamic Method

Drop No.	$\xi(-Dv_f)$	$r(=-\zeta + sqrt\zeta^2 +)$	r^3	$T\left(=1+\frac{t_f}{t_r}\right)$	$ne(=CTr^3/V)$
1.					
2.					
3.					
4.					
5.					

2. Balancing Method

Drop No.	$\xi(-Dv_f)$	$r(=-\zeta + sqrt\zeta^2 +)$	r^3	$ne(=CTr^3/V)$
1.				
2.				
3.				
4.				
5.				

C. Analysis and Treatment

- 1. Identify the minimum value of charge ne on droplets.
- 2. Divide the value of the charge ne on all droplets by its minimum value.

- 3. The result will be numbers close to integers for all droplets.
- 4. Now extrapolate all these numbers.
- 5. Divide the value of charge ne on all droplets by the respective integers.
- 6. This gives the values on the charge of an electron by different droplets.

1. Dynamic Method

ne	ne divided by the lowest	Nearest integer n_{eff}	n_e/n_{eff}
1.			
2.			
3.			
4.			
5.			

2. Balancing Method

ne	ne divided by the lowest	Nearest integer n_{eff}	n_e/n_{eff}
1			
2			
3			
4			
5			

REFERENCES

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