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### Data Structure

### 1.1 BIT

3.7 Bipatirate

```
1 #define lowbit(k) (k & -k)
  void add(vector<int> &tr, int id, int val) {
    for (; id <= n; id += lowbit(id)) {</pre>
3
       tr[id] += val;
5
    }
6 }
7 int sum(vector<int> &tr, int id) {
    int ret = 0;
    for (; id >= 1; id -= lowbit(id)) {
10
      ret += tr[id];
11
12
    return ret;
13 }
```

# 1.2 Segment tree

```
1 int dfs(int lef, int rig){
      if(lef + 2 == rig){
          if(num[lef] > num[rig-1]){
              return lef;
5
          }
6
          else{
              return rig-1;
```

```
8
              }
   9
  10
          int mid = (lef + rig)/2;
          int p1 = dfs(lef, mid);
  11
  12
          int p2 = dfs(mid, rig);
  13
          if(num[p1] > num[p2]){
  14
              return p1;
         }
  16
         else{
  17
              return p2;
2
  18
  19 }
```

### 1.3 Trie

```
1 const int MAXL = ; // 自己填
     const int MAXC = ;
     struct Trie {
       int nex[MAXL][MAXC];
       int len[MAXL];
       int sz:
   7
       void init() {
         memset(nex, 0, sizeof(nex));
memset(len, 0, sizeof(len));
  8
  9
  10
         sz = 0;
  11
  12
       void insert(const string &str) {
  13
          int p = 0;
          for (char c : str) {
  14
  15
            int id = c - 'a';
  16
            if (!nex[p][id]) {
              nex[p][id] = ++sz;
  17
  18
            p = nex[p][id];
  19
         }
  20
  21
         len[p] = str.length();
  22
  23
       vector<int> find(const string &str, int i) {
  24
         int p = 0;
          vector<int> ans;
8
  26
          for (; i < str.length(); i++) {</pre>
  27
            int id = str[i] -
  28
            if (!nex[p][id]) {
              return ans;
  29
  31
            p = nex[p][id];
  32
            if (len[p]) {
  33
              ans.pb(len[p]);
  34
  35
         }
  36
          return ans;
  37
       }
  38 }:
```

#### 2 DP

8

#### Josephus 2.1

```
1 int josephus (int n, int k) {
     // 有 n 個人圍成一圈, 每 k 個一次
3
     return n > 1 ? (josephus(n-1 , k) + k) % n : 0;
4 }
5 // 回傳最後一人的編號, 0 index
```

## 2.2 LCS

```
1 int LCS(string s1, string s2) {
   int n1 = s1.size(), n2 = s2.size();
   int dp[n1+1][n2+1] = {0};
   // dp[i][j] = s1的前i個字元和s2的前j個字元
```

```
for (int i = 1; i <= n1; i++) {
       for (int j = 1; j <= n2; j++) {</pre>
6
7
         if (s1[i - 1] == s2[j - 1]) {
           dp[i][j] = dp[i - 1][j - 1] + 1;
8
9
         } else {
10
           dp[i][j] = max(dp[i - 1][j], dp[i][j - 1]);
11
12
      }
13
    }
14
    return dp[n1][n2];
15 }
  2.3 LIS
1 int LIS(vector<int> &a) { // Longest Increasing
       Subsequence
2
    vector<int> s;
3
    for (int i = 0; i < a.size(); i++) {</pre>
       if (s.empty() || s.back() < a[i]) {</pre>
         s.push_back(a[i]);
      } else {
         *lower_bound(s.begin(), s.end(), a[i],
7
8
           [](int x, int y) {return x < y;}) = a[i];
9
    }
10
```

# 3 Graph

return s.size();

11

12 }

## 3.1 SPFA

```
1 bool SPFA(int s){
       // 記得初始化這些陣列
3
       int cnt[1000+5], dis[1000+5];
       bool inqueue[1000+5];
       queue < int > q;
6
       q.push(s);
7
8
       dis[s] = 0;
       inqueue[s] = true;
9
10
       cnt[s] = 1;
11
       while(!q.empty()){
12
           int now = q.front();
13
           q.pop();
           inqueue[now] = false;
14
15
16
           for(auto &e : G[now]){
17
                if(dis[e.t] > dis[now] + e.w){
                    dis[e.t] = dis[now] + e.w;
18
                    if(!inqueue[e.t]){
19
20
                        cnt[e.t]++;
                        if(cnt[e.t] > m){
21
22
                             return false;
23
24
                        inqueue[e.t] = true;
25
                        q.push(e.t);
                    }
26
27
               }
           }
28
29
30
       return true;
31 }
```

# 3.2 Dijkstra

```
1 struct Item{
2 int u, dis;
3 // 取路徑最短
4 bool operator < (const Item &other) const{
```

```
5
           return dis > other.dis;
6
7
  };
  int dis[maxn];
8
9
  vector < Edge > G[maxn];
10
  void dijkstra(int s){
       for(int i = 0; i <= n; i++){</pre>
11
12
           dis[i] = inf;
13
14
       dis[s] = 0;
15
       priority_queue<Item> pq;
16
       pq.push({s, 0});
17
       while(!pq.empty()){
           // 取路徑最短的點
18
           Item now = pq.top();
19
20
           pq.pop();
           if(now.dis > dis[now.u]){
21
22
               continue;
23
           }
           // 鬆弛更新,把與 now.u 相連的點都跑一遍
24
25
           for(Edge e : G[now.u]){
               if(dis[e.v] > now.dis + e.w){
26
                   dis[e.v] = now.dis + e.w;
27
28
                   pq.push({e.v, dis[e.v]});
               }
29
30
           }
31
      }
32 }
```

# 3.3 Floyd Warshall

```
1 void floyd_warshall(){
       for(int i = 0; i < n; i++){</pre>
          for(int j = 0; j < n; j++){
3
4
               G[i][j] = INF;
5
          G[i][i] = 0;
6
7
8
      for (int k = 0; k < n; k++){
           嘗試每一個中繼點
9
           for (int i = 0; i < n; i++){ //
               計算每一個 i 點與每一個 j 點
               for (int j = 0; j < n; j++){
10
                   G[i][j] = min(G[i][j], G[i][k] +
11
                       G[k][j]);
               }
12
13
          }
14
      }
15 }
```

# 3.4 Disjoint set Kruskal

```
1 struct Edge{
2
      int u, v, w;
       // 用權重排序 由大到小
3
      bool operator < (const Edge &other) const{</pre>
4
5
           return w > other.w;
6
7
  }edge[maxn];
8
  // disjoint set
9
  int find(int x){
10
    if(parent[x] < 0){
       return x;
11
12
13
    else{
14
       return parent[x] = find(parent[x]);
15
16 }
17
  void unite(int a, int b){
    a = find(a);
18
19
    b = find(b);
20
    if(a != b){
```

```
22
      if(parent[a] < parent[b]){</pre>
                                                            43
                                                                  return false;
        parent[a] += parent[b];
                                                            44 }
23
        parent[b] = a;
24
                                                            45 | bool branch2(){ // 延展交錯樹:使用新添的等邊
      }
25
                                                                  for (int y=0; y<Y; ++y){</pre>
26
      else{
                                                            47
                                                                      if (!vy[y] && dy[y] == 0){
27
        parent[b] += parent[a];
                                                            48
                                                                          vy[y] = true;
        parent[a] = b;
28
                                                                           if (my[y] == -1){
                                                            49
29
                                                            50
                                                                               augment(pdy[y], y);
30
    }
                                                            51
                                                                               return true:
  }
31
                                                            52
32
  void kruskal(){
                                                            53
                                                                           int z = my[y];
      memset(parent, -1, sizeof(parent));
                                                                           *qb++ = z; p[z] = pdy[y]; vx[z] = true;
33
                                                            54
      sort(edge, edge + m);
34
                                                                               relax(z);
      int i, j;
35
                                                            55
                                                                      }
36
      for (i = 0, j = 0; i < n - 1 && j < m; i++){}
                                                                  }
                                                            56
37
          // 如果 u 和 v 的祖先相同, 則 j++
                                                            57
                                                                  return false;
                                                            58 }
               (祖先相同代表會產生環 所以不要)
          while(find(edge[j].u) == find(edge[j].v)) j++;
                                                            59 int Hungarian(){
38
           // 若部會產生環 則讓兩點之間產生橋
                                                            60
                                                                  // 初始化vertex labeling
39
               (連接兩顆子生成樹)
                                                            61
                                                                  // memset(lx, 0, sizeof(lx)); // 任意值皆可
40
          unite(edge[j].u, edge[j].v);
                                                            62
                                                                  memset(ly, 0, sizeof(ly));
                                                                  for (int x=0; x<X; ++x)
                                                            63
41
           j++;
                                                                       for (int y=0; y<Y; ++y)</pre>
                                                            64
42
      }
                                                                          lx[x] = max(lx[x], adj[x][y]);
                                                            65
43 }
                                                            66
                                                            67
                                                                  // x側每一個點,分別建立等邊交錯樹。
                                                            68
                                                                  memset(mx, -1, sizeof(mx));
  3.5 KM
                                                            69
                                                                  memset(my, -1, sizeof(my));
                                                                  for (int x=0; x<X; ++x){</pre>
                                                            70
                                                            71
                                                                      memset(vx, false, sizeof(vx));
                      // X的點數,等於Y的點數
1 const int X = 50;
                                                                      memset(vy, false, sizeof(vy));
                                                            72
                      // Y的點數
2 | const int Y = 50;
                                                                      memset(dy, 0x7f, sizeof(dy));
                                                            73
3 int adj[X][Y];
                      // 精簡過的adjacency matrix
                                                            74
                                                                      qf = qb = q;
4 int 1x[X], 1y[Y];
                      // vertex labeling
                                                            75
                                                                      *qb++ = x; p[x] = -1; vx[x] = true; relax(x);
5 int mx[X], my[Y];
                      //
                                                            76
                                                                      while (true){
       X各點的配對對象、Y各點的配對對象
                                                            77
                                                                           if (branch1()) break;
6 int q[X], *qf, *qb; // BFS queue
                                                            78
                                                                           reweight();
                       // BFS
7 int p[X];
                                                                           if (branch2()) break;
                                                            79
      parent,交錯樹之偶點,指向上一個偶點
                                                                      }
                                                            80
8 bool vx[X], vy[Y]; // 記錄是否在交錯樹上
                                                            81
                                                                  }
9| int dy[Y], pdy[Y]; // 表格
                                                            82
                                                                  // 計算最大權完美匹配的權重
10
                                                            83
                                                                  int weight = 0;
11
  void relax(int x){ // relaxation
                                                            84
                                                                  for (int x=0; x<X; ++x)</pre>
      for (int y=0; y<Y; ++y)</pre>
12
                                                                      weight += adj[x][mx[x]];
                                                            85
          if (adj[x][y] != 1e9)
13
                                                            86
                                                                  return weight;
14
              if (lx[x] + ly[y] - adj[x][y] < dy[y]){
15
                  dy[y] = lx[x] + ly[y] - adj[x][y];
16
                  pdy[y] = x; //
                       記錄好是從哪個樹葉連出去的
                                                              3.6 Dinic
17
              }
18 }
19 void reweight(){ // 調整權重、調整表格
                                                            1 // Maximum Flow
                                                              const int V = 100, E = 1000;
      int d = 1e9;
20
21
      for (int y=0; y<Y; ++y) if (!vy[y]) d = min(d,</pre>
                                                              int adj[V]; // adjacency lists,初始化為-1。
                                                              struct Element {int b, r, next;} e[E*2];
           dy[v]);
22
      for (int x=0; x<X; ++x) if ( vx[x]) lx[x] -= d;</pre>
                                                              int en = 0;
23
      for (int y=0; y<Y; ++y) if ( vy[y]) ly[y] += d;</pre>
                                                              void addedge(int a, int b, int c){
      for (int y=0; y<Y; ++y) if (!vy[y]) dy[y] -= d;</pre>
                                                                  e[en] = (Element)\{b, c, adj[a]\}; adj[a] = en++;
24
25 }
                                                                  e[en] = (Element){a, 0, adj[b]}; adj[b] = en++;
                                                            9 }
  void augment(int x, int y){ // 擴充路徑
26
                                                                               // 最短距離
      for (int ty; x != -1; x = p[x], y = ty){
                                                            10 int d[V]:
27
28
          ty = mx[x]; my[y] = x; mx[x] = y;
                                                            11
                                                              bool visit[V]; // BFS/DFS visit record
                                                                              // queue
29
                                                            12 int q[V];
30 }
                                                              int BFS(int s, int t){ // 計算最短路徑,求出容許圖
                                                            13
31 bool branch1(){ // 延展交錯樹:使用既有的等邊
                                                                  memset(d, 0x7f, sizeof(d));
                                                            14
32
      while (qf < qb)</pre>
                                                            15
                                                                  memset(visit, false, sizeof(visit));
          for (int x=*qf++, y=0; y<Y; ++y)</pre>
                                                                  int qn = 0;
33
                                                            16
                                                                  d[s] = 0;
34
               if (!vy[y] && lx[x] + ly[y] == adj[x][y]){
35
                  vy[y] = true;
                                                            18
                                                                  visit[s] = true;
36
                  if (my[y] == -1){
                                                            19
                                                                  q[qn++] = s;
37
                       augment(x, y);
                                                            20
                       return true;
                                                            21
                                                                  for (int qf=0; qf<qn; ++qf){</pre>
38
                                                            22
                                                                      int a = q[qf];
39
40
                  int z = my[y];
                                                            23
                                                                      for (int i = adj[a]; i != -1; i = e[i].next){
```

24

25

26

int b = e[i].b;

if (e[i].r > 0 && !visit[b]){

d[b] = d[a] + 1;

41

42

\*qb++ = z; p[z] = x; vx[z] = true;

relax(z);

}

```
27
                    visit[b] = true;
                    q[qn++] = b;
28
29
                    if (b == t) return d[t];
30
               }
31
           }
       }
32
33
       return V:
34 }
35 int DFS(int a, int df, int s, int t){ //
       求出一條最短擴充路徑,並擴充流量
       if (a == t) return df;
36
37
       if (visit[a]) return 0;
       visit[a] = true;
38
39
       for (int i = adj[a]; i != -1; i = e[i].next){
           int b = e[i].b;
40
41
           if (e[i].r > 0 && d[a] + 1 == d[b]){
               int f = DFS(b, min(df, e[i].r), s, t);
42
43
               if (f){
44
                    e[i].r -= f;
45
                    e[i^1].r += f;
                    return f;
46
               }
47
           }
48
       }
49
50
       return 0:
51 }
52 int dinitz(int s, int t){
       int flow = 0;
       while (BFS(s, t) < V)
54
55
           while (true){
56
               memset(visit, false, sizeof(visit));
               int f = DFS(s, 1e9, s, t);
57
58
               if (!f) break;
59
               flow += f;
           }
60
61
       return flow;
62 }
```

### 3.7 Bipatirate

```
1 const int maxn = 300 + 5;
2 int n, color[maxn];
3 vector<vector<int>> v(maxn);
4 bool dfs(int s){
5
       for(auto it : v[s]){
            if(color[it] == -1){
6
7
                color[it] = 3 - color[s];
8
                if(!dfs(it)){
9
                     return false;
10
11
12
            if(color[s] == color[it]){
13
                return false:
14
15
16
       return true;
17 }
18
  void isBipatirate(){
19
       bool flag = true;
       for(int i = 1; i <= n; ++i){</pre>
20
21
            if(color[i] == -1){
22
                color[i] = 1;
23
                flag &= dfs(i);
24
           }
25
       if(flag){
26
           cout << "YES" << endl;</pre>
27
28
       else{
29
           cout << "NO" << endl;
30
31
32 }
33 int main(){
       while(cin >> n && n){
34
           for(int i = 1; i <= n; ++i) v[i].clear();</pre>
35
```

```
36
           memset(color, -1, sizeof(color));
37
           int a. b:
38
           while(cin >> a >> b && (a || b)){
               v[a].emplace_back(b);
39
40
                v[b].emplace_back(a);
41
42
           isBipatirate();
43
       }
44 }
```

# 3.8 Hungarian algorithm

```
1 const int maxn = 500+5;
  int t, N, bn, gn, match[maxn];
  bool visited[maxn];
  vector<vector<int>> G(maxn);
  struct People{
       int h;
7
       string music, sport;
8
       People(){}
9
       People(int h, string music, string sport){
10
           this->h = h;
11
           this->music = music;
12
           this->sport = sport;
13
14| }lef[maxn], rig[maxn];
15
  bool check(People boy, People girl){
16
       if(abs(boy.h - girl.h) <= 40 && boy.music ==</pre>
            girl.music && boy.sport != girl.sport) return
            true:
       return false;
17
18
  }
  bool dfs(int s){
19
20
       for(int i = 0; i < G[s].size(); ++i){</pre>
21
           int v = G[s][i];
22
           if(visited[v]) continue;
23
           visited[v] = true;
           if(match[v] == -1 || dfs(match[v])){
24
25
                match[v] = s;
26
                return true;
27
28
       }
29
       return false;
30 }
31
  int Hungarian(){
32
       int cnt = 0;
33
       memset(match, -1, sizeof(match));
       for(int i = 0; i < bn; ++i){</pre>
34
35
           memset(visited, false, sizeof(visited));
36
           if(dfs(i)) cnt++;
37
38
       return cnt;
39 }
40
  int main(){
41
       cin >> t;
42
       while(t--){
43
           cin >> N;
44
           bn = 0, gn = 0;
45
           for(int i = 0; i <= N; ++i) G[i].clear();</pre>
46
           int h:
47
           string sex, music, sport;
           for(int i = 0; i < N; ++i){</pre>
48
                cin >> h >> sex >> music >> sport;
49
                if(sex == "M") lef[bn++] = People(h,
50
                    music, sport);
51
                else rig[gn++] = People(h, music, sport);
52
           for(int i = 0; i < bn; ++i){</pre>
53
54
                for(int j = 0; j < gn; ++j)</pre>
55
                    if(check(lef[i], rig[j]))
                         G[i].emplace_back(j);
56
           cout << N - Hungarian() << endl;</pre>
57
58
       }
59 }
```

# 4 Other

## 4.1 Bubble Sort Expect Value

```
1 /* 期望值算法:
2| 擲一枚公平的六面骰子,其每次「點數」的期望值是 3.5
3 | E(x) = 1 * 1/6 + 2 * 1/6 + 3 * 1/6 + 4 * 1/6 + 5 *
      1/6 + 6 * 1/6
|4| = (1 + 2 + 3 + 4 + 5 + 6)/6 = 3.5
5 bubble sort 每兩兩之間交換機率是 1/2
6| 總共會做 C(n, 2) 次
7 E(x) = C(n, 2) * 1/2 = (n * (n - 1))/2 * 1/2 */
8 int t, ca = 1;
9 cin >> t;
10 while(t--){
11
      long long int n;
12
      cin >> n;
      cout << "Case " << ca++ << ": ";
13
      // 如果 (n * (n - 1)) 可以被 4 整除
14
          代表最後答案會是整數,否則會是分數
      if((n * (n - 1)) % 4){
15
16
         cout << ( (n * (n - 1)) / 2 ) << "/2" << endl;
      }
17
18
      else{
         cout << ( (n * (n - 1)) / 2 ) / 2 << endl;
19
20
21 }
```

### 4.2 ORXOR

```
1 /* 如何切區段,之所以要1<<n是為了可以跑000~111
2 | i = 0, binary i = 000
3 0 : 1 5 7
4 \mid i = 1, binary i = 001
5 1 : 1 5 7
6 i = 2, binary i = 010, 看得出來切了一刀
7 2 : 1 | 5 7
8 i = 3 , binary i = 011
9 3 : 1 | 5 7
10 i = 4, binary i = 100, 為了要切在index=2, 所以才要1<<j
11 4 : 1 5 | 7
|12|i = 5, binary i = 101
13 5 : 1 5 | 7
|14|i = 6, binary i = 110
15 6 : 1 | 5 | 7
|16| i = 7, binary i = 111
17 7 : 1 | 5 | 7
18 可以觀察出來,前兩位 bit 是 1 時代表的意義是切在哪裡*/
19 int n;
20 int num [20+7]:
21 memset(num, 0, sizeof(num));
22 cin >> n;
23 for(int i = 1; i \le n; i++){
24
      cin >> num[i];
25 }
26 int mini = 2147483647; // 不知道為甚麼只有 2147483647
      給過
27 // 1 << n = n * 2
28 for(int i = 0; i < (1 << n); i++){
      int XOR = 0, OR = 0;
29
      for(int j = 1; j <= n; j++){</pre>
30
          OR |= num[j];
31
32
          if((i & (1 << j))){</pre>
              XOR ^= OR;
33
34
              OR = 0;
          }
35
36
      XOR ^= OR;
37
38
      mini = min(mini, XOR);
39 }
40 cout << mini << endl;
```

### 4.3 Race to 1

```
1 const int N = 1000000;
2 bool sieve[N+5];
  vector<int> pri;
4
  double dp[N+5];
  void Linear_Sieve(){ // 線性篩
5
       for (int i = 2; i < N; i++){</pre>
           if (!sieve[i])
               pri.push_back(i);
9
           for (int p: pri){
                if (i * p >= N){
10
11
                    break;
12
                sieve[i * p] = true;
13
               if (i % p == 0){
14
15
                    break;
16
               }
17
           }
18
  }
19
  double dfs(int n){
20
       if(dp[n] != -1) return dp[n];
21
22
       dp[n] = 0:
23
       if(n == 1) return dp[n];
       int total = 0, prime = 0;
24
25
       for(int i = 0; i < pri.size() && pri[i] <= n;</pre>
           i++){
           total++;
26
27
           if(n % pri[i]) continue;
           prime++;
28
29
           dp[n] += dfs(n/pri[i]);
30
       dp[n] = (dp[n] + total)/prime; // 算期望值
31
32
       return dp[n];
33 }
34
  int main(){
35
       int t;
       int num;
36
37
       int ca = 1;
       for(int i = 0; i <= N; i++){
38
39
           dp[i] = -1;
40
       Linear_Sieve();
41
       cin >> t;
42
43
       while(t--){
44
           cin >> num;
45
46
           cout << "Case " << ca++ << ": " << fixed <<
                setprecision(10) << dfs(num) << endl;</pre>
       }
47
48 }
```

### 4.4 X drawing

```
1 long long int n, a, b, p, q, r, s;
2
  cin >> n >> a >> b;
  cin >> p >> q >> r >> s;
3
  for(long long int i = p; i <= q; i++){</pre>
       for(long long int j = r; j <= s; j++){</pre>
           if(abs(i - a) == abs(j - b)){
7
                cout << '#';
           }
9
            else{
                cout << '.';
10
11
       }
12
       cout << endl;</pre>
13
14 3
```

### 4.5 Big Mod

```
1 '''
2 Mod
  pow(x, y, z) = x^y % z
5 # python 如何讀取直到 EOF 用 try except
6 try:
7
      while True:
         # input().split() 用空格切開讀取一整行
8
         # map (型態, input().split()) 才能把值全讀成
9
            int
10
         B, P, M = map(int, input().split())
         print(pow(B, P, M))
11
12 except EOFError:
13
     exit
```

### 4.6 Crested Ibis vs Monster

```
1 /* dp 背包 - 重量/價值/可重複使用
2 因為這題可以重複使用同一條魔法
3| 所以可以這樣 dp*/
4 int h, n;
5 cin >> h >> n;
6 for(int i = 1; i <= n; i++){
      cin >> a[i] >> b[i];
8 }
9 memset(dp, 0x3f3f3f3f, sizeof(dp));
10 | dp[0][0] = 0;
11 for(int i = 1; i <= n; i++){
      for(int j = 0; j <= h; j++){
12
13
          dp[i][j] = min(dp[i-1][j], dp[i][max(0, j -
              a[i])] + b[i]);
14
      }
15 }
16 cout << dp[n][h] << endl;</pre>
```

# 4.7 dpd Knapsack 1

```
1 // dp 背包 - 時間/數量/價值 - 第幾分鐘符合
2 int N, W;
3 cin >> N >> W;
4 int w[100000+5];
5 int v[100000+5];
6 for(int i = 0; i < N; i++){
      cin >> w[i] >> v[i];
7
8 }
9 long long int dp[100000+5];
10 memset(dp, 0, sizeof(dp));
11 for (int i = 0; i < N; i++){
      for(int j = W; j >= w[i]; j--){
12
13
          dp[j] = max(dp[j], dp[j - w[i]] + v[i]);
14
15 }
16 cout << dp[W] << endl;</pre>
```

### 4.8 Fraction Floor Sum

```
1 /* [N/i] == M
|2| -> M <= N/i < M + 1
|3| -> N/(M+1) < i <= N/M */
4 long long int N;
5 cin >> N;
6 long long int ans = 0;
7 for(long long int i = 1; i <= N; i++){
      long long int M = N / i;
9
      long long int n = N / M;
      // 總共會有 n - i 個的 [N/i] 值都是 M
10
      ans += (n - i + 1) * M;
11
      // 更新跳過 以免重複計算
12
      i = n;
13
14 }
15 cout << ans << endl;
```

# 4.9 Homer Simpson

```
1 // dp 背包 - 時間/數量 - 漢堡
  int m, n, t;
3
  while(cin >> m >> n >> t){
       int dp[10000+5];
      memset(dp, -1, sizeof(dp));
       dp[0] = 0;
       for(int i = m; i <= t; i++){</pre>
7
           if(dp[i - m] != -1){
               dp[i] = max(dp[i], dp[i - m] + 1);
9
10
11
12
       for(int i = n; i <= t; i++){</pre>
13
           if(dp[i - n] != -1){
               dp[i] = max(dp[i], dp[i - n] + 1);
14
15
16
       if(dp[t] == -1){ // 時間無法剛好吃滿的時候
17
           for(int i = t; i >= 0; i--){
18
               if(dp[i] != -1){
19
                    cout << dp[i] << " " << t - i << endl;</pre>
20
21
                    break;
               }
22
23
           }
24
25
      else{
           cout << dp[t] << endl;</pre>
26
27
      }
28 }
```

# 4.10 Let Me Count The Ways

```
1 // dp - 時間/數量 - 硬幣排序
2 long long int n, dp[30000+5];
3 int coin[] = {1, 5, 10, 25, 50};
  memset(dp, 0, sizeof(dp));
  dp[0] = 1;
5
  for(int i = 0; i < 5; i++){
       for(int j = coin[i]; j < 30000+5; j++){</pre>
           if(dp[j - coin[i]] != -1){
                dp[j] += dp[j - coin[i]];
9
10
11
12 }
  while(cin >> n){
13
14
       if(dp[n] == 1){
           \operatorname{cout} << "There is only" << \operatorname{dp[n]} << " way to
15
                produce " << n << " cents change." <<
                endl:
16
       }
       else{
17
18
           cout << "There are " << dp[n] << " ways to</pre>
                produce " << n << " cents change." <<
                endl;
19
       }
20 }
```

### 4.11 Luggage

```
1 // dp 背包 - 重量/是否成立
  int t;
3 cin >> t;
  cin.ignore();
  while(t--){
5
      string str:
6
      getline(cin , str);
7
      vector<int> v:
8
9
      stringstream ss;
10
      int num, cnt = 0, sum = 0;;
11
      bool dp[4000+5];
12
      memset(dp, false, sizeof(dp));
      ss << str;
13
```

22

23

24 }

```
14
       while(ss >> num){
15
            cnt++:
16
            sum += num;
            v.emplace_back(num);
17
18
19
       if(sum & 1){
            cout << "NO" << endl;
20
21
            continue;
22
       dp[0] = true;
23
24
       for(int i = 0; i < v.size(); i++){</pre>
            for(int j = sum; j >= v[i]; j--){
25
26
                if(dp[j - v[i]]){
                     dp[j] = true;
27
28
            }
29
       }
30
       cout << (dp[sum/2] ? "YES" : "NO") << endl;</pre>
31
32 }
```

### 4.12 Number of Pairs

```
1 /* uper_bound ex:
2 10 20 30 30 40 50
3 upper_bound for element 30 is at index 4
4 lower_bound ex:
5 10 20 30 40 50
6 lower_bound for element 30 at index 2 */
7 int t;
8 cin >> t;
  while(t--){
9
       int n, 1, r;
10
       vector<int> v;
11
12
       cin >> n >> 1 >> r;
       int num;
13
       for(int i = 0; i < n; i++){</pre>
14
15
           cin >> num;
16
           v.emplace_back(num);
17
       }
       sort(v.begin(), v.end());
18
19
       long long int ans = 0;
       for(int i = 0; i < n; i++){</pre>
20
           ans += (upper_bound(v.begin() + i + 1,
21
                v.end(), r - v[i])
                lower_bound(v.begin() + i + 1, v.end(), 1
                - v[i]));
       }
22
23
       cout << ans << endl;</pre>
24 }
```

### 4.13 SuperSale

```
1 // dp 背包 - 重量/價值/不可重複使用 - 舉重
2 int t;
3 cin >> t;
4 while(t--){
      int n;
      cin >> n;
6
      for(int i = 0; i < n; i++){</pre>
8
           cin >> edge[i].p >> edge[i].w;
9
10
      int g, total = 0;
      cin >> g;
11
12
       for(int i = 0; i < g; i++){
           int pw, dp[30+5];
13
           cin >> pw;
14
15
           memset(dp, 0, sizeof(dp));
           for(int j = 0; j < n; j++){
16
17
               for(int k = pw; k >= edge[j].w; k--){
                   dp[k] = max(dp[k], dp[k - edge[j].w]
18
                       + edge[j].p);
19
               }
           }
20
```

# 4.14 Walking on the Safe Side

total += dp[pw];

cout << total << endl;</pre>

```
1 // dp - 地圖更新
2 int t;
3 bool space = false;
   cin >> t;
   while(t--){
       if(space){
            cout << endl;</pre>
7
8
       else{
10
            space = true;
11
       int r, c;
12
       cin >> r >> c;
13
14
        cin.ignore();
       memset(mp, false, sizeof(mp));
memset(dp, 0, sizeof(dp));
15
16
        string str;
17
        for(int i = 0; i < r; i++){</pre>
18
19
            getline(cin, str);
20
            int n. num:
21
            stringstream ss(str);
22
            ss >> n;
            while(ss >> num){
23
                 mp[n][num] = true;
24
25
       }
26
27
       dp[1][1] = 1;
28
        for(int i = 1; i <= r; i++){</pre>
29
            for(int j = 1; j <= c; j++){</pre>
30
                 if(mp[i][j]){
31
                      continue;
32
33
                 if(i > 1){
                      dp[i][j] += dp[i-1][j];
34
35
                 if(j > 1){
36
37
                      dp[i][j] += dp[i][j-1];
38
            }
39
40
        cout << dp[r][c] << endl;</pre>
41
42 }
```

# **Function**

#### 5.1 strstr

```
1 #include <stdio.h>
2 #include <string.h>
4
  int main(){
  char * c:
  char str1[1005], str2[1005];
  scanf("%s %s", str1, str2);
  c = strstr(str1, str2);
  if (c != NULL){
9
      printf("Yes\n");
10
11 }
12 else printf("No\n");
13 }
14 // Input : Hello eLl
15 // Output : No
```

### 5.2 substr

```
1 int main(){
2     string str; //abcdef
3     cin >> str;
4     string tmp;
5     tmp = str.substr(0, 2); //ab
6     str = str.substr(2); //cdef
7     cout << tmp << " " << str;
8     return 0;
9 }</pre>
```

# 5.3 map set

```
1 | .begin( ) // Return iterator to beginning
2 .end( ) // Return iterator to end
3 .empty() // 檢查是否為空
4 . size( ) // 回傳大小
5 mp.insert(pair<char,int>('a',100))
6 st.insert(100) // 插入key value
7 .erase( ) // 刪掉指定key和他的value
8 .clear( ) // 清空整個 map
9 m.find()
10 cout << "a => " << mymap.find('a')->second << endl;</pre>
      // 找出 map 裡 key
11
          有沒有在裡面,如果有的話會回傳元素所在的iterator,看即傳函的化
12 s.count() // 返回某個值元素在 set 的 個數
13 while( !mymap.empty()){
      cout << mymap.begin()->first << " => " <<
         mymap.begin()->second << endl;</pre>
15
      mymap.erase(mymap.begin());
16 }
17 for (auto it = mymap.begin(); it != mymap.end(); ++it)
      cout << it->first << " => " << it->second << endl;</pre>
```

### 5.4 vector

```
1 | v.erase(v.begin() + 5) //拿掉第六個數
2 | v.erase (v.begin(), v.begin() + 3); //拿掉前三個數
```

### 5.5 setprecision

```
1 // 將數字的小數部分設定為固定長度
2 cnt = 3.5555;
3 cout << fixed << setprecision(3) << cnt ;
4 // output : 3.555
```

## 5.6 GCD LCM

```
int gcd(int a, int b){
    return (b == 0 ? a : gcd(b, a % b));

}
int lcm(int a, int b){
    return a * b / gcd(a, b);

}

/* 輾轉相除法 - 求兩數是否互質

如果兩數互質 最終結果其中一方為0時 另一方必為1

若兩數有公因數 最終結果其中一方為0時 另一方必不為1 */
while ( ( num1 %= num2 ) != 0 && ( num2 %= num1 ) !=
    0 );
```

# 5.7 reverse

```
1 int a[10] = {0, 1, 2, 3, 4, 5, 6, 7, 8, 9};
2 reverse(a, a+5) // 轉換0~5
3
4 vector<int> v;
5 reverse(v.begin(), v.end());
6
7 string str = "123";
8 reverse(str.begin(), str.end());
9 cout << str << endl; //321</pre>
```

### 5.8 CHAR

```
1 isdigit()
2 isalnum() //判斷字母 // 數字
3 isalpha()
4 islower()
5
  isupper()
6 isblank() //判斷是否為空格,或者 tab 健制表符,即
      space 和 \t
  toupper()
8 tolower()
1 priority_queue < int, vector < int >, less < int >> //大到小
2 priority_queue<int, vector<int>, greater<int>>
      //小到大
  int arr[] = {4, 5, 8, 3, 7, 1, 2, 6, 10, 9};
      sort(arr, arr+10);
  vector<int> v;
  sort(v.begin(), v.end()); //小到大
10
  int cmp(int a, int b){
      return a > b;
11
12 }
13 sort(v.begin(), v.end(), cmp); //大到小
```

### 5.10 struct

```
1    struct area{
2        int a, b;
3        bool operator <(const area rhs) const{
4            return a > rhs.a || ( a == a && b > rhs.b);
5        }
6        bool operator!=(const area rhs) const{
7            return a != rhs.a || b != rhs.b;
8        }
9    };
```

# 5.11 deque

```
1 deque <int> que;
2 que.push_back(10);
3 que.push_front(20);
4 que.front()
5 que.back()
6 que.pop_front()
7 que.pop_back()
8 cout << "Element at position 2 : " << que.at(2) << end];</pre>
```

# 5.12 python template

```
1 import math
2 import operator
3
4
5
      while(1):
6
          listx = []
          listx.append("...")
7
          list_s = sorted(listx) # 小到大
8
9
          list_s = sorted(listx, reverse = True) #
              大到小
          # max(listx)
10
          # min(listx)
11
12
          # sum(listx)
          # len(listx)
13
14
          dicty = {}
          dicty[key] = "value"
15
          dicty= sorted(dicty.items()) # by key
16
          dicty= sorted(dicty.items(),
17
              key=operator.itemgetter(1)) # by value
          # EOF寫法
18
          # 階層 math.factorial(3) == 6
19
          # 絕對值 math.fabs(x)
20
          # 無條件進位 math.ceil(3.1) == 3
21
          # 無條件捨去 math.floor(2.9) == 2
22
          # C n 取 k math.comb(n, k)
23
24
          # math.gcd
          # math.lcm
25
          # e 次 x 幂 math.exp(x)
26
27 except EOFError:
28
      pass
```