5

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```

1 Data Structure

1.1 Josephus

1.2 BIT

```
1 #define lowbit(k) (k & -k)
2 void add(vector<int> &tr, int id, int val) {
    for (; id <= n; id += lowbit(id)) {</pre>
      tr[id] += val;
5
6 }
7 int sum(vector<int> &tr, int id) {
    int ret = 0;
9
    for (; id >= 1; id -= lowbit(id)) {
10
      ret += tr[id];
    }
11
12
    return ret;
13 }
```

1.3 Segment tree

```
int dfs(int lef, int rig){
    if(lef + 2 == rig){
        if(num[lef] > num[rig-1]){
            return lef;
        }
        else{
        return rig-1;
        }
    }
    int mid = (lef + rig)/2;
```

```
11
         int p1 = dfs(lef, mid);
         int p2 = dfs(mid, rig);
  12
  13
         if(num[p1] > num[p2]){
1 14
              return p1;
  15
1
 16
         else{
  17
              return p2;
  18
  19 }
```

1.4 Trie

```
const int MAXL = ; // 自己填
  const int MAXC = ;
2
  struct Trie {
3
     int nex[MAXL][MAXC];
     int len[MAXL];
     int sz;
     void init() {
       memset(nex, 0, sizeof(nex));
8
       memset(len, 0, sizeof(len));
10
11
12
     void insert(const string &str) {
13
       int p = 0;
       for (char c : str) {
         int id = c - 'a';
15
         if (!nex[p][id]) {
16
17
           nex[p][id] = ++sz;
18
19
         p = nex[p][id];
20
21
       len[p] = str.length();
22
23
     vector<int> find(const string &str, int i) {
24
       int p = 0;
25
       vector<int> ans;
       for (; i < str.length(); i++) {</pre>
26
         int id = str[i] - 'a';
27
28
         if (!nex[p][id]) {
29
           return ans;
30
31
         p = nex[p][id];
         if (len[p]) {
32
33
           ans.pb(len[p]);
34
35
       }
36
       return ans;
    }
37
38 };
```

2 DP

2.1 LCS

```
1 int LCS(string s1, string s2) {
    int n1 = s1.size(), n2 = s2.size();
3
    int dp[n1+1][n2+1] = \{0\};
    // dp[i][j] = s1的前i個字元和s2的前j個字元
    for (int i = 1; i <= n1; i++) {</pre>
5
      for (int j = 1; j \le n2; j++) {
6
        if (s1[i - 1] == s2[j - 1]) {
           dp[i][j] = dp[i - 1][j - 1] + 1;
8
9
        } else {
           dp[i][j] = max(dp[i - 1][j], dp[i][j - 1]);
10
11
12
    }
13
14
    return dp[n1][n2];
15 }
```

2.2 LIS

```
1 int LIS(vector<int> &a) { // Longest Increasing
       Subsequence
    vector<int> s;
2
     for (int i = 0; i < a.size(); i++) {</pre>
       if (s.empty() || s.back() < a[i]) {</pre>
         s.push_back(a[i]);
6
       } else {
7
         *lower_bound(s.begin(), s.end(), a[i],
8
           [](int x, int y) {return x < y;}) = a[i];
9
    }
10
11
    return s.size();
12 }
```

3 Graph

3.1 SPFA

```
1 bool SPFA(int s){
       // 記得初始化這些陣列
       int cnt[1000+5], dis[1000+5];
3
4
       bool inqueue[1000+5];
5
       queue<int> q;
6
7
       q.push(s);
8
       dis[s] = 0;
9
       inqueue[s] = true;
10
       cnt[s] = 1;
11
       while(!q.empty()){
12
           int now = q.front();
13
           q.pop();
           inqueue[now] = false;
14
15
           for(auto &e : G[now]){
16
                if(dis[e.t] > dis[now] + e.w){
17
                    dis[e.t] = dis[now] + e.w;
18
19
                    if(!inqueue[e.t]){
20
                        cnt[e.t]++:
                        if(cnt[e.t] > m){
21
22
                             return false;
23
24
                        inqueue[e.t] = true;
                        q.push(e.t);
25
26
                    }
27
               }
           }
28
29
30
       return true;
31 }
```

3.2 Dijkstra

```
1 struct Item{
2
      int u, dis;
       // 取路徑最短
4
       bool operator < (const Item &other) const{</pre>
5
           return dis > other.dis;
6
7 };
8 int dis[maxn];
9 vector<Edge> G[maxn];
10 void dijkstra(int s){
11
       for(int i = 0; i <= n; i++){
12
           dis[i] = inf;
13
14
       dis[s] = 0;
15
       priority_queue < Item > pq;
16
       pq.push({s, 0});
17
       while(!pq.empty()){
```

```
// 取路徑最短的點
18
19
          Item now = pq.top();
20
          pq.pop();
          if(now.dis > dis[now.u]){
21
22
              continue;
          }
23
          // 鬆弛更新,把與 now.u 相連的點都跑一遍
24
25
          for(Edge e : G[now.u]){
26
              if(dis[e.v] > now.dis + e.w){
                  dis[e.v] = now.dis + e.w;
27
                  pq.push({e.v, dis[e.v]});
28
29
              }
30
          }
31
      }
32 }
```

3.3 Floyd Warshall

```
1 void floyd_warshall(){
       for(int i = 0; i < n; i++){</pre>
2
3
           for(int j = 0; j < n; j++){
               G[i][j] = INF;
5
6
           G[i][i] = 0;
7
       for (int k = 0; k < n; k++){
8
           嘗試每一個中繼點
9
           for (int i = 0; i < n; i++){ //</pre>
               計算每一個 i 點與每一個 j 點
               for (int j = 0; j < n; j++){
10
                   G[i][j] = min(G[i][j], G[i][k] +
11
                        G[k][j]);
12
               }
13
           }
14
      }
15 }
```

3.4 Disjoint set Kruskal

```
1 struct Edge{
       int u, v, w;
2
       // 用權重排序 由大到小
3
       bool operator < (const Edge &other) const{</pre>
           return w > other.w;
       }
  }edge[maxn];
7
  // disjoint set
9
  int find(int x){
    if(parent[x] < 0){
10
11
       return x;
    }
12
13
14
       return parent[x] = find(parent[x]);
15
16 }
  void unite(int a, int b){
17
18
    a = find(a);
    b = find(b);
19
20
21
    if(a != b){
22
       if(parent[a] < parent[b]){</pre>
23
         parent[a] += parent[b];
         parent[b] = a;
24
25
       }
       else{
26
27
         parent[b] += parent[a];
28
         parent[a] = b;
29
30
    }
31 }
32
  void kruskal(){
       memset(parent, -1, sizeof(parent));
33
       sort(edge, edge + m);
34
```

```
35
                                                            55
                                                                       }
      for(i = 0, j = 0; i < n - 1 && j < m; i++){
                                                                   }
                                                            56
36
          // 如果 u 和 v 的祖先相同, 則 j++
                                                            57
                                                                   return false;
37
                                                            58 }
               (祖先相同代表會產生環 所以不要)
                                                            59
                                                               int Hungarian(){
          while(find(edge[j].u) == find(edge[j].v)) j++;
38
                                                            60
                                                                   // 初始化vertex labeling
           // 若部會產生環 則讓兩點之間產生橋
39
                                                                   // memset(lx, 0, sizeof(lx)); // 任意值皆可
                                                            61
               (連接兩顆子生成樹)
                                                            62
                                                                   memset(ly, 0, sizeof(ly));
          unite(edge[j].u, edge[j].v);
40
                                                                   for (int x=0; x<X; ++x)</pre>
                                                            63
41
                                                            64
                                                                       for (int y=0; y<Y; ++y)</pre>
42
      }
                                                                           1x[x] = max(1x[x], adj[x][y]);
                                                            65
43 }
                                                            66
                                                            67
                                                                   // x側每一個點,分別建立等邊交錯樹。
                                                                   memset(mx, -1, sizeof(mx));
                                                            68
  3.5 KM
                                                                   memset(my, -1, sizeof(my));
                                                            69
                                                            70
                                                                   for (int x=0; x<X; ++x){</pre>
                                                            71
                                                                       memset(vx, false, sizeof(vx));
                      // X的點數,等於Y的點數
1 \mid \mathbf{const} \quad \mathbf{int} \quad X = 50;
                                                            72
                                                                       memset(vy, false, sizeof(vy));
                       // Y的點數
2 | const int Y = 50;
                                                                       memset(dy, 0x7f, sizeof(dy));
                                                            73
3 int adj[X][Y];
                       // 精簡過的adjacency matrix
                                                            74
                                                                       qf = qb = q;
4 int 1x[X], 1y[Y];
                       // vertex labeling
                                                            75
                                                                       *qb++ = x; p[x] = -1; vx[x] = true; relax(x);
5 int mx[X], my[Y];
                       //
                                                            76
                                                                       while (true){
       X各點的配對對象、Y各點的配對對象
                                                            77
                                                                           if (branch1()) break;
6 int q[X], *qf, *qb; // BFS queue
                                                                           reweight():
                                                            78
                       // BFS
7 int p[X];
                                                                           if (branch2()) break;
                                                            79
       parent,交錯樹之偶點,指向上一個偶點
                                                                       }
                                                            80
8 bool vx[X], vy[Y]; // 記錄是否在交錯樹上
                                                            81
                                                                   }
9| int dy[Y], pdy[Y]; // 表格
                                                            82
                                                                   // 計算最大權完美匹配的權重
10
                                                            83
                                                                   int weight = 0;
11 void relax(int x){ // relaxation
                                                                   for (int x=0; x<X; ++x)</pre>
                                                            84
12
      for (int y=0; y<Y; ++y)</pre>
                                                                       weight += adj[x][mx[x]];
                                                            85
13
          if (adj[x][y] != 1e9)
                                                            86
                                                                   return weight;
               if (lx[x] + ly[y] - adj[x][y] < dy[y]){
14
                   dy[y] = lx[x] + ly[y] - adj[x][y];
15
16
                   pdy[y] = x; //
                       記錄好是從哪個樹葉連出去的
                                                               3.6 Dinic
17
18 }
19 void reweight(){ // 調整權重、調整表格
                                                             1 // Maximum Flow
                                                             2 | const int V = 100, E = 1000;
      int d = 1e9:
20
21
      for (int y=0; y<Y; ++y) if (!vy[y]) d = min(d,</pre>
                                                             3 int adj[V]; // adjacency lists,初始化為-1。
                                                               struct Element {int b, r, next;} e[E*2];
           dy[y]);
22
      for (int x=0; x<X; ++x) if (vx[x]) 1x[x] -= d;
                                                             5
                                                               int en = 0;
23
      for (int y=0; y<Y; ++y) if ( vy[y]) ly[y] += d;</pre>
                                                               void addedge(int a, int b, int c){
                                                             6
      for (int y=0; y<Y; ++y) if (!vy[y]) dy[y] -= d;</pre>
                                                                   e[en] = (Element){b, c, adj[a]}; adj[a] = en++;
24
25 }
                                                                   e[en] = (Element){a, 0, adj[b]}; adj[b] = en++;
                                                             9 }
26 void augment(int x, int y){ // 擴充路徑
      for (int ty; x != -1; x = p[x], y = ty){
                                                            10 int d[V];
                                                                               // 最短距離
27
                                                                              // BFS/DFS visit record
28
          ty = mx[x]; my[y] = x; mx[x] = y;
                                                               bool visit[V];
29
                                                            12
                                                               int q[V];
                                                                               // queue
                                                               int BFS(int s, int t){ // 計算最短路徑,求出容許圖
30 }
                                                            13
31 | bool branch1(){ // 延展交錯樹:使用既有的等邊
                                                                   memset(d, 0x7f, sizeof(d));
                                                            14
32
      while (qf < qb)</pre>
                                                            15
                                                                   memset(visit, false, sizeof(visit));
          for (int x=*qf++, y=0; y<Y; ++y)</pre>
                                                                   int qn = 0;
33
                                                            16
                                                                   d[s] = 0;
34
               if (!vy[y] \&\& lx[x] + ly[y] == adj[x][y]){
                                                                   visit[s] = true;
                   vy[y] = true;
35
                                                            18
                   if (my[y] == -1){
                                                            19
                                                                   q[qn++] = s;
36
37
                       augment(x, y);
                                                            20
38
                       return true:
                                                            21
                                                                   for (int qf=0; qf<qn; ++qf){</pre>
                                                                       int a = q[qf];
39
                   }
                                                            22
                                                                       for (int i = adj[a]; i != -1; i = e[i].next){
40
                   int z = my[y];
                                                            23
                   *qb++ = z; p[z] = x; vx[z] = true;
41
                                                            24
                                                                           int b = e[i].b;
                       relax(z);
                                                            25
                                                                           if (e[i].r > 0 && !visit[b]){
                                                            26
                                                                               d[b] = d[a] + 1;
42
43
      return false;
                                                            27
                                                                               visit[b] = true;
                                                                               q[qn++] = b;
44 }
                                                            28
                                                                               if (b == t) return d[t];
45 | bool branch2(){ // 延展交錯樹:使用新添的等邊
                                                            29
                                                                           }
46
      for (int y=0; y<Y; ++y){</pre>
                                                            30
                                                            31
                                                                       }
          if (!vy[y] && dy[y] == 0){
47
48
               vy[y] = true;
                                                            32
                                                                   }
                                                                   return V;
                                                            33
49
               if (my[y] == -1){
                                                            34 }
50
                   augment(pdy[y], y);
                                                            35 int DFS(int a, int df, int s, int t){ //
51
                   return true;
                                                                   求出一條最短擴充路徑,並擴充流量
52
               }
53
                                                            36
                                                                   if (a == t) return df;
               int z = my[y];
               *qb++ = z; p[z] = pdy[y]; vx[z] = true;
54
                                                            37
                                                                   if (visit[a]) return 0;
```

visit[a] = true;

38

relax(z);

```
39
       for (int i = adj[a]; i != -1; i = e[i].next){
           int b = e[i].b;
40
            if (e[i].r > 0 && d[a] + 1 == d[b]){
41
                int f = DFS(b, min(df, e[i].r), s, t);
42
43
                if (f){
                    e[i].r -= f;
44
                    e[i^1].r += f;
45
46
                    return f;
                }
47
           }
48
49
       }
50
       return 0;
51 }
52 int dinitz(int s, int t){
53
       int flow = 0;
       while (BFS(s, t) < V)
54
           while (true){
55
56
                memset(visit, false, sizeof(visit));
                int f = DFS(s, 1e9, s, t);
57
58
                if (!f) break;
                flow += f;
59
60
           }
61
       return flow;
62 }
```

4 Other

4.1 Bubble Sort Expect Value

```
1 /* 期望值算法:
  2| 擲一枚公平的六面骰子,其每次「點數」的期望值是 3.5
  |E(x)| = 1 \times 1/6 + 2 \times 1/6 + 3 \times 1/6 + 4 \times 1/6 + 5 \times 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 +
                             1/6 + 6 * 1/6
  |4| = (1 + 2 + 3 + 4 + 5 + 6)/6 = 3.5
  5 bubble sort 每兩兩之間交換機率是 1/2
  6 總共會做 C(n, 2) 次
  7 | E(x) = C(n, 2) * 1/2 = (n * (n - 1))/2 * 1/2 */
  8 int t, ca = 1;
  9 cin >> t;
10 while(t--){
                            long long int n;
11
                            cin >> n;
12
                            cout << "Case " << ca++ << ": ";
13
                             // 如果 (n * (n - 1)) 可以被 4 整除
                                               代表最後答案會是整數,否則會是分數
15
                            if((n * (n - 1)) % 4){
                                             cout << ( (n * (n - 1)) / 2 ) << "/2"<< endl;
16
                           }
17
18
                            else{
19
                                             cout << ( (n * (n - 1)) / 2 ) / 2 << endl;
20
21 | }
```

4.2 Crested Ibis vs Monster

```
1 /* dp 背包 - 重量/價值/可重複使用
2 因為這題可以重複使用同一條魔法
3| 所以可以這樣 dp*/
4 int h, n;
5 cin >> h >> n;
6 for(int i = 1; i <= n; i++){
      cin >> a[i] >> b[i];
7
8 }
9 memset(dp, 0x3f3f3f3f, sizeof(dp));
10 | dp[0][0] = 0;
11 for(int i = 1; i <= n; i++){
      for(int j = 0; j <= h; j++){</pre>
12
          dp[i][j] = min(dp[i-1][j], dp[i][max(0, j -
13
              a[i])] + b[i]);
14
15 }
16 cout << dp[n][h] << endl;</pre>
```

4.3 dpd Knapsack 1

```
1 // dp 背包 - 時間/數量/價值 - 第幾分鐘符合
  int N, W;
3 cin >> N >> W:
  int w[100000+5];
  int v[100000+5];
  for(int i = 0; i < N; i++){
7
      cin >> w[i] >> v[i];
8 }
9
  long long int dp[100000+5];
10
  memset(dp, 0, sizeof(dp));
  for(int i = 0; i < N; i++){
11
12
      for(int j = W; j >= w[i]; j--){
          dp[j] = max(dp[j], dp[j - w[i]] + v[i]);
13
14
15 }
16 cout << dp[W] << endl;</pre>
```

4.4 Fraction Floor Sum

```
/* [N/i] == M
2
  -> M <= N/i < M + 1
  -> N/(M+1) < i <= N/M */
4 long long int N;
  cin >> N;
5
6
  long long int ans = 0;
  for(long long int i = 1; i <= N; i++){</pre>
7
      long long int M = N / i;
      long long int n = N / M;
10
      // 總共會有 n - i 個的 [N/i] 值都是 M
      ans += (n - i + 1) * M;
11
      // 更新跳過 以免重複計算
12
      i = n;
13
14 }
15 cout << ans << endl;
```

4.5 Homer Simpson

```
1 // dp 背包 - 時間/數量 - 漢堡
  int m, n, t;
2
  while(cin >> m >> n >> t){
      int dp[10000+5];
      memset(dp, -1, sizeof(dp));
       dp[0] = 0;
6
       for(int i = m; i <= t; i++){</pre>
           if(dp[i - m] != -1){
8
               dp[i] = max(dp[i], dp[i - m] + 1);
           }
10
11
12
       for(int i = n; i <= t; i++){</pre>
           if(dp[i - n] != -1){
13
               dp[i] = max(dp[i], dp[i - n] + 1);
14
15
16
       if(dp[t] == -1){ // 時間無法剛好吃滿的時候
17
18
           for(int i = t; i >= 0; i--){
19
               if(dp[i] != -1){
                    cout << dp[i] << " " << t - i << endl;
20
21
                    break;
22
23
           }
24
      }
25
       else{
           cout << dp[t] << endl;</pre>
26
27
28 }
```

4.6 Let Me Count The Ways

```
1 // dp - 時間/數量 - 硬幣排序
2 long long int n, dp[30000+5];
3 int coin[] = {1, 5, 10, 25, 50};
4 memset(dp, 0, sizeof(dp));
5|dp[0] = 1;
6 for (int i = 0; i < 5; i++){
      for(int j = coin[i]; j < 30000+5; j++){</pre>
7
8
           if(dp[j - coin[i]] != -1){
9
               dp[j] += dp[j - coin[i]];
           }
10
11
      }
12 }
13 while(cin >> n){
       if(dp[n] == 1){
14
           cout << "There is only " << dp[n] << " way to
15
               produce " << n << " cents change." <<</pre>
16
      }
17
       else{
           cout << "There are " << dp[n] << " ways to</pre>
18
               produce " << n << " cents change." <<</pre>
19
       }
20 }
```

4.7 Luggage

```
1 // dp 背包 - 重量/是否成立
2 int t;
3 cin >> t;
4 cin.ignore();
  while(t--){
       string str:
7
       getline(cin , str);
       vector<int> v;
8
9
       stringstream ss;
       int num, cnt = 0, sum = 0;;
10
11
       bool dp[4000+5];
12
       memset(dp, false, sizeof(dp));
       ss << str;
13
14
       while(ss >> num){
15
           cnt++;
           sum += num;
16
17
           v.emplace_back(num);
18
19
       if(sum & 1){
           cout << "NO" << endl;
20
           continue;
21
       }
22
23
       dp[0] = true;
24
       for(int i = 0; i < v.size(); i++){</pre>
           for(int j = sum; j >= v[i]; j--){
25
                if(dp[j - v[i]]){
26
                    dp[j] = true;
27
28
           }
29
       }
30
31
       cout << (dp[sum/2] ? "YES" : "NO") << endl;</pre>
32 }
```

4.8 Number of Pairs

```
1  /* uper_bound ex:
2  10  20  30  30  40  50
3  upper_bound for element 30 is at index 4
4  lower_bound ex:
5  10  20  30  40  50
6  lower_bound for element 30 at index 2 */
int t;
cin >> t;
while(t--){
int n, l, r;
vector<int> v;
```

```
12
       cin >> n >> 1 >> r;
13
       int num:
14
       for(int i = 0; i < n; i++){</pre>
15
           cin >> num;
16
           v.emplace_back(num);
17
18
       sort(v.begin(), v.end());
19
       long long int ans = 0;
20
       for(int i = 0; i < n; i++){
21
            ans += (upper_bound(v.begin() + i + 1,
                v.end(), r - v[i]) -
                lower_bound(v.begin() + i + 1, v.end(), 1
                - v[i]));
       }
22
23
       cout << ans << endl;</pre>
24 }
```

4.9 ORXOR

```
1 /* 如何切區段,之所以要1<<n是為了可以跑000~111
2|i = 0, binary i = 000
3 0 : 1 5 7
  i = 1, binary i = 001
5 1 : 1 5 7
6 | i = 2 , binary i = 010 , 看得出來切了一刀
  2:1157
|i| = 3, binary |i| = 011
9 3 : 1 | 5 7
10 i = 4, binary i = 100, 為了要切在index=2, 所以才要1<<j
  4:15/7
|12|i = 5, binary i = 101
13 5 : 1 5 / 7
|14| i = 6, binary i = 110
15 6 : 1 | 5 | 7
  i = 7, binary i = 111
17 7 : 1 | 5 | 7
|18| 可以觀察出來,前兩位 bit 是 1 時代表的意義是切在哪裡 */
19 int n;
20 int num[20+7];
21 memset(num, 0, sizeof(num));
22
  cin >> n:
  for(int i = 1; i <= n; i++){</pre>
23
      cin >> num[i];
25 }
26 int mini = 2147483647; // 不知道為甚麼只有 2147483647
      給過
  // 1 << n = n * 2
27
28 for(int i = 0; i < (1 << n); i++){
      int XOR = 0, OR = 0;
29
      for(int j = 1; j <= n; j++){</pre>
30
          OR |= num[j];
31
32
          if((i & (1 << j))){</pre>
              XOR ^= OR;
33
              OR = 0;
34
35
      }
36
37
      XOR ^= OR;
      mini = min(mini, XOR);
38
39 }
40 cout << mini << endl;
```

4.10 Race to 1

```
1 const int N = 1000000;
2 bool sieve[N+5];
3 vector<int> pri;
4 double dp[N+5];
5 void Linear_Sieve(){ // 線性篩
6 for (int i = 2; i < N; i++){
7 if (!sieve[i])
8 pri.push_back(i);
9 for (int p: pri){
10 if (i * p >= N){
```

6

7

8

9

10

11

12

13

14

15

16

17

18

19

20

21

22

23

24

25

26

27

28

29

30

31

32

33

34

35

36

37

38

39

40

41

42 }

3 bool space = false;

if(space){

int r, c;

cin >> r >> c;

cin.ignore();

string str;

}

dp[1][1] = 1;

}

}

cout << endl;</pre>

space = true;

memset(mp, false, sizeof(mp));

memset(dp, 0, sizeof(dp));

for(int i = 0; i < r; i++){</pre>

stringstream ss(str);

for(int i = 1; i <= r; i++){</pre>

if(mp[i][j]){

 $if(i > 1){$

 $if(j > 1){$

cout << dp[r][c] << endl;</pre>

continue:

mp[n][num] = true;

for(int j = 1; j <= c; j++){</pre>

dp[i][j] += dp[i-1][j];

dp[i][j] += dp[i][j-1];

getline(cin, str);

while(ss >> num){

int n, num;

ss >> n;

cin >> t;

}

while(t--){

else{

```
11
                     break;
                }
12
                sieve[i * p] = true;
13
14
                if (i % p == 0){
15
                     break;
16
17
           }
18
19|}
20
  double dfs(int n){
21
       if(dp[n] != -1) return dp[n];
       dp[n] = 0;
22
23
       if(n == 1) return dp[n];
       int total = 0, prime = 0;
24
25
       for(int i = 0; i < pri.size() && pri[i] <= n;</pre>
            i++){
            total++;
26
27
            if(n % pri[i]) continue;
            prime++;
28
29
            dp[n] += dfs(n/pri[i]);
30
31
       dp[n] = (dp[n] + total)/prime; // 算期望值
32
       return dp[n];
33 }
34 int main(){
35
       int t;
       int num;
36
       int ca = 1;
37
       for(int i = 0; i <= N; i++){</pre>
38
39
            dp[i] = -1;
40
41
       Linear_Sieve();
42
       cin >> t;
       while(t--){
43
44
           cin >> num;
45
            cout << "Case " << ca++ << ": " << fixed <<
46
                setprecision(10) << dfs(num) << endl;</pre>
47
       }
48 }
```

4.11 SuperSale

```
1 // dp 背包 - 重量/價值/不可重複使用 - 舉重
2 int t;
  cin >> t;
  while(t--){
      int n;
       cin >> n;
       for(int i = 0; i < n; i++){</pre>
7
8
           cin >> edge[i].p >> edge[i].w;
9
10
      int g, total = 0;
       cin >> g;
11
12
       for(int i = 0; i < g; i++){</pre>
13
           int pw, dp[30+5];
           cin >> pw;
14
           memset(dp, 0, sizeof(dp));
15
16
           for(int j = 0; j < n; j++){
17
                for(int k = pw; k >= edge[j].w; k--){
18
                    dp[k] = max(dp[k], dp[k - edge[j].w]
                        + edge[i].p);
19
               }
           }
20
21
           total += dp[pw];
22
       }
       cout << total << endl;</pre>
23
24 }
```

4.13 X drawing

}

}

```
1 long long int n, a, b, p, q, r, s;
2 cin >> n >> a >> b;
3
  cin >> p >> q >> r >> s;
  for(long long int i = p; i <= q; i++){</pre>
       for(long long int j = r; j <= s; j++){</pre>
           if(abs(i - a) == abs(j - b)){
               cout << '#';
8
           }
           else{
9
10
                cout << '.';
11
12
       }
13
       cout << endl;
14 }
```

4.12 Walking on the Safe Side

```
1 // dp - 地圖更新
2 int t;
```