

## Contents

### 1 Graph Theory

- 1.1 DFS . . . . .
- 1.2 BFS . . . . .
- 1.3 Disjoint Set and Kruskal . . . . .

### 2 Number Theory

- 2.1 thm . . . . .

## 1 Graph Theory

### 1.1 DFS

```

1 vector<int> G[N];
2 bitset<N> vis;
3 void dfs(int s) {
4     vis[s] = 1;
5     for (int t : G[s]) {
6         if (!vis[t])
7             dfs(t);
8     }
9 }

```

### 1.2 BFS

```

1 vector<int> G[N];
2 bitset<N> vis;
3 void bfs(int s) {
4     queue<int> q;
5     q.push(s);
6     vis[s] = 1;
7     while (!q.empty()) {
8         int v = q.front();
9         q.pop();
10        for (int t : G[v]) {
11            if (!vis[t]) {
12                q.push(t);
13                vis[t] = 1;
14            }
15        }
16    }
17 }

```

### 1.3 Disjoint Set and Kruskal

```

1 struct Edge{
2     int u, v, w;
3     // bool operator < (const Edge &rhs) const {
4         // return w < rhs.w; }
5 };
6 vector<int> parent;
7 vector<Edge> E;
8
9 bool cmp(Edge edge1, Edge edge2){
10    return edge2.w > edge1.w;
11 }
12
13 int find(int x){
14     if(parent[x] < 0){
15         return x;
16     }
17     return parent[x] = find(parent[x]);
18 }
19
20 bool Uni(int a, int b){
21     a = find(a);
22     b = find(b);
23     if(a == b){

```

```

24         return false;
25     }
26     if(parent[a] > parent[b]){
27         swap(a, b);
28     }
29     parent[a] = parent[a] + parent[b];
30     parent[b] = a;
31     return true;
32 }
33
34 void Kruskal() {
35
36     int cost = 0;
37
38     sort(E.begin(), E.end()); // sort by w
39     // sort(E.begin(), E.end(), cmp);
40
41     // two edge in the same tree or not
42     for (auto it: E){
43         int s = Find(it.s);
44         int t = Find(it.t);
45         if (Uni(it.s, it.t)){
46             cost = cost + it.w;
47         }
48     }
49 }
50
51 int main(){
52
53     // create N space and initial -1
54     parent = vector<int> (N, -1);
55
56     for(i = 0; i < M; i++){
57         cin >> u >> v >> w;
58         E.push_back({u, v, w});
59     }
60
61     Kruskal();
62
63     return 0;
64 }

```

## 2 Number Theory

### 2.1 thm

- 中文測試

$$\sum_{i=1}^n i^2 = \frac{n(n+1)(2n+1)}{6}$$