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## 1 Data Structure

### 1.1 BIT

```

1 #define lowbit(k) (k & -k)
2 void add(vector<int> &tr, int id, int val) {
3     for (; id <= n; id += lowbit(id)) {
4         tr[id] += val;
5     }
6 }
7 int sum(vector<int> &tr, int id) {
8     int ret = 0;
9     for (; id >= 1; id -= lowbit(id)) {
10         ret += tr[id];
11     }
12     return ret;
13 }

```

### 1.2 Segment tree

```

1 int dfs(int lef, int rig){
2     if(lef + 2 == rig){
3         if(num[lef] > num[rig-1]){
4             return lef;
5         }
6         else{
7             return rig-1;
8         }
9     }
10    int mid = (lef + rig)/2;
11    int p1 = dfs(lef, mid);
12    int p2 = dfs(mid, rig);
13    if(num[p1] > num[p2]){
14        return p1;
15    }
16    else{
17        return p2;
18    }
19 }

```

### 1.3 Trie

```

5 const int MAXL = ; // 自己填
6 const int MAXC = ;
7 struct Trie {
8     int nex[MAXL][MAXC];
9     int len[MAXL];
10    int sz;
11    void init() {
12        memset(nex, 0, sizeof(nex));
13        memset(len, 0, sizeof(len));
14        sz = 0;
15    }
16    void insert(const string &str) {
17        int p = 0;
18        for (char c : str) {
19            int id = c - 'a';
20            if (!nex[p][id]) {
21                nex[p][id] = ++sz;
22            }
23            p = nex[p][id];
24        }
25        len[p] = str.length();
26    }
27    vector<int> find(const string &str, int i) {
28        int p = 0;
29        vector<int> ans;
30        for (; i < str.length(); i++) {
31            int id = str[i] - 'a';
32            if (!nex[p][id]) {
33                return ans;
34            }
35            p = nex[p][id];
36            if (len[p]) {
37                ans.pb(len[p]);
38            }
39        }
40        return ans;
41    }
42 }

```

## 2 Divide and Conquer

### 2.1 count inversions

```

1 int arr[maxn], buf[maxn];
2 int count_inversions(int lef, int rig){ // 逆序数对
3     if(rig - lef <= 1) return 0;
4     int mid = (lef + rig)/2;

```

```

5   int ans = count_inversions(lef, mid) +
      count_inversions(mid, rig);
6   int i = lef, j = mid, k = lef;
7   while(i < mid || j < rig){
8       if(i >= mid) buf[k] = arr[j++];
9       else if(j >= rig) buf[k] = arr[i++];
10      else{
11          if(arr[i] <= arr[j]) buf[k] = arr[i++];
12          else{
13              buf[k] = arr[j++];
14              ans += mid - i;
15          }
16      }
17      k++;
18  }
19  for(int k = lef; k < rig; ++k) arr[k] = buf[k];
20  return ans;
21 }

```

### 3 DP

#### 3.1 Doubling

```

1  /* 倍增 */
2  int LOG = sqrt(N); // 2^LOG >= N
3  vector<int> arr(N);
4  vector<vector<int>> dp(N, vector<int>(LOG));
5  for(int i = 0; i < N; ++i) cin >> arr[i];
6  int L, Q, a, b;
7  cin >> L >> Q;
8  for(int i = 0; i < N; ++i){
9      dp[i][0] = lower_bound(arr.begin(), arr.end(),
10         arr[i] + L) - arr.begin();
11      if(dp[i][0] == N || arr[i] + L < arr[dp[i][0]])
12         dp[i][0] -= 1;
13  }
14  for(int i = 1; i < LOG; ++i)
15      for(int j = 0; j < N; ++j)
16         dp[j][i] = dp[dp[j][i-1]][i-1];
17  for(int i = 0; i < Q; ++i){
18      cin >> a >> b;
19      a--; // 要減減是因為arr的index從0開始但題目從1開始
20      b--;
21      if(a > b) swap(a, b);
22      int ans = 0;
23      for(int i = LOG - 1; i >= 0; --i){ // 從後往回推
24          if(dp[a][i] < b){
25              ans += (1 << i);
26              a = dp[a][i];
27          }
28      }
29      cout << ans + 1 << endl;
30  }

```

#### 3.2 Josephus

```

1  int josephus (int n, int k) {
2      // 有 n 個人圍成一圈，每 k 個一次
3      return n > 1 ? (josephus(n-1, k) + k) % n : 0;
4  }
5  // 回傳最後一人的編號，0 index

```

#### 3.3 LCS

```

1  int LCS(string s1, string s2) {
2      int n1 = s1.size(), n2 = s2.size();
3      int dp[n1+1][n2+1] = {0};
4      // dp[i][j] = s1的前i個字元和s2的前j個字元
5      for (int i = 1; i <= n1; i++) {

```

```

6      for (int j = 1; j <= n2; j++) {
7          if (s1[i-1] == s2[j-1]) {
8              dp[i][j] = dp[i-1][j-1] + 1;
9          } else {
10             dp[i][j] = max(dp[i-1][j], dp[i][j-1]);
11         }
12     }
13 }
14 return dp[n1][n2];
15 }

```

### 3.4 LIS

```

1  int LIS(vector<int> &a) { // Longest Increasing
      Subsequence
2  vector<int> s;
3  for (int i = 0; i < a.size(); i++) {
4      if (s.empty() || s.back() < a[i]) {
5          s.push_back(a[i]);
6      } else {
7          *lower_bound(s.begin(), s.end(), a[i],
8             [](int x, int y) {return x < y;}) = a[i];
9      }
10 }
11 return s.size();
12 }

```

## 4 Graph

#### 4.1 SPFA

```

1  bool SPFA(int s){
2      // 記得初始化這些陣列
3      int cnt[1000+5], dis[1000+5];
4      bool inqueue[1000+5];
5      queue<int> q;
6
7      q.push(s);
8      dis[s] = 0;
9      inqueue[s] = true;
10     cnt[s] = 1;
11     while(!q.empty()){
12         int now = q.front();
13         q.pop();
14         inqueue[now] = false;
15
16         for(auto &e : G[now]){
17             if(dis[e.t] > dis[now] + e.w){
18                 dis[e.t] = dis[now] + e.w;
19                 if(!inqueue[e.t]){
20                     cnt[e.t]++;
21                     if(cnt[e.t] > m){
22                         return false;
23                     }
24                     inqueue[e.t] = true;
25                     q.push(e.t);
26                 }
27             }
28         }
29     }
30     return true;
31 }

```

#### 4.2 Dijkstra

```

1  struct Item{
2      int u, dis;
3      // 取路徑最短
4      bool operator < (const Item &other) const{
5          return dis > other.dis;

```

```

6     }
7 };
8 int dis[maxn];
9 vector<Edge> G[maxn];
10 void dijkstra(int s){
11     for(int i = 0; i <= n; i++){
12         dis[i] = inf;
13     }
14     dis[s] = 0;
15     priority_queue<Item> pq;
16     pq.push({s, 0});
17     while(!pq.empty()){
18         // 取路徑最短的點
19         Item now = pq.top();
20         pq.pop();
21         if(now.dis > dis[now.u]){
22             continue;
23         }
24         // 鬆弛更新，把與 now.u 相連的點都跑一遍
25         for(Edge e : G[now.u]){
26             if(dis[e.v] > now.dis + e.w){
27                 dis[e.v] = now.dis + e.w;
28                 pq.push({e.v, dis[e.v]});
29             }
30         }
31     }
32 }

```

### 4.3 Floyd Warshall

```

1 void floyd_warshall(){
2     for(int i = 0; i < n; i++){
3         for(int j = 0; j < n; j++){
4             G[i][j] = INF;
5         }
6         G[i][i] = 0;
7     }
8     for (int k = 0; k < n; k++){ // 嘗試每一個中繼點
9         for (int i = 0; i < n; i++){ // 計算每一個i點與每一個j點
10            for (int j = 0; j < n; j++){
11                G[i][j] = min(G[i][j], G[i][k] + G[k][j]);
12            }
13        }
14    }
15 }

```

### 4.4 Disjoint set Kruskal

```

1 struct Edge{
2     int u, v, w;
3     // 用權重排序 由大到小
4     bool operator < (const Edge &other) const{
5         return w > other.w;
6     }
7 }edge[maxn];
8 // disjoint set
9 int find(int x){
10     if(parent[x] < 0){
11         return x;
12     }
13     else{
14         return parent[x] = find(parent[x]);
15     }
16 }
17 void unite(int a, int b){
18     a = find(a);
19     b = find(b);
20     if(a != b){
21         if(parent[a] < parent[b]){
22

```

```

23         parent[a] += parent[b];
24         parent[b] = a;
25     }
26     else{
27         parent[b] += parent[a];
28         parent[a] = b;
29     }
30 }
31 }
32 void kruskal(){
33     memset(parent, -1, sizeof(parent));
34     sort(edge, edge + m);
35     int i, j;
36     for(i = 0, j = 0; i < n - 1 && j < m; i++){
37         // 如果 u 和 v 的祖先相同，則 j++
38         // (祖先相同代表會產生環 所以不要)
39         while(find(edge[j].u) == find(edge[j].v)) j++;
40         // 若部會產生環 則讓兩點之間產生橋
41         // (連接兩顆子生成樹)
42         unite(edge[j].u, edge[j].v);
43         j++;
44     }
45 }

```

### 4.5 KM

```

1 const int X = 50; // x的點數，等於y的點數
2 const int Y = 50; // y的點數
3 int adj[X][Y]; // 精簡過的adjacency matrix
4 int lx[X], ly[Y]; // vertex labeling
5 int mx[X], my[Y]; // x各點的配對對象、y各點的配對對象
6 int q[X], *qf, *qb; // BFS queue
7 int p[X]; // BFS parent，交錯樹之偶點，指向上一個偶點
8 bool vx[X], vy[Y]; // 記錄是否在交錯樹上
9 int dy[Y], pdy[Y]; // 表格
10
11 void relax(int x){ // relaxation
12     for (int y=0; y<Y; ++y)
13         if (adj[x][y] != 1e9)
14             if (lx[x] + ly[y] - adj[x][y] < dy[y]){
15                 dy[y] = lx[x] + ly[y] - adj[x][y];
16                 pdy[y] = x; // 記錄好是從哪個樹葉連出去的
17             }
18 }
19 void reweight(){ // 調整權重、調整表格
20     int d = 1e9;
21     for (int y=0; y<Y; ++y) if (!vy[y]) d = min(d, dy[y]);
22     for (int x=0; x<X; ++x) if (vx[x]) lx[x] -= d;
23     for (int y=0; y<Y; ++y) if (vy[y]) ly[y] += d;
24     for (int y=0; y<Y; ++y) if (!vy[y]) dy[y] -= d;
25 }
26 void augment(int x, int y){ // 擴充路徑
27     for (int ty; x != -1; x = p[x], y = ty){
28         ty = mx[x]; my[y] = x; mx[x] = y;
29     }
30 }
31 bool branch1(){ // 延展交錯樹：使用既有的等邊
32     while (qf < qb)
33         for (int x=*qf++; y=0; y<Y; ++y)
34             if (!vy[y] && lx[x] + ly[y] == adj[x][y]){
35                 vy[y] = true;
36                 if (my[y] == -1){
37                     augment(x, y);
38                     return true;
39                 }
40                 int z = my[y];
41                 *qb++ = z; p[z] = x; vx[z] = true;
42                 relax(z);
43             }
44     return false;
45 }

```

```

44 }
45 bool branch2(){ // 延展交錯樹：使用新添的等邊
46     for (int y=0; y<Y; ++y){
47         if (!vy[y] && dy[y] == 0){
48             vy[y] = true;
49             if (my[y] == -1){
50                 augment(pdy[y], y);
51                 return true;
52             }
53             int z = my[y];
54             *qb++ = z; p[z] = pdy[y]; vx[z] = true;
55             relax(z);
56         }
57     }
58     return false;
59 }
60 int Hungarian(){
61     // 初始化 vertex labeling
62     // memset(lx, 0, sizeof(lx)); // 任意值皆可
63     memset(ly, 0, sizeof(ly));
64     for (int x=0; x<X; ++x){
65         for (int y=0; y<Y; ++y)
66             lx[x] = max(lx[x], adj[x][y]);
67
68     // x側每一個點，分別建立等邊交錯樹。
69     memset(mx, -1, sizeof(mx));
70     memset(my, -1, sizeof(my));
71     for (int x=0; x<X; ++x){
72         memset(vx, false, sizeof(vx));
73         memset(vy, false, sizeof(vy));
74         memset(dy, 0x7f, sizeof(dy));
75         qf = qb = q;
76         *qb++ = x; p[x] = -1; vx[x] = true; relax(x);
77         while (true){
78             if (branch1()) break;
79             reweight();
80             if (branch2()) break;
81         }
82     }
83     // 計算最大權完美匹配的權重
84     int weight = 0;
85     for (int x=0; x<X; ++x)
86         weight += adj[x][mx[x]];
87     return weight;
88 }

```

## 4.6 Dinic

```

1 // Maximum Flow
2 const int V = 100, E = 1000;
3 int adj[V]; // adjacency lists, 初始化為-1。
4 struct Element {int b, r, next;} e[E*2];
5 int en = 0;
6 void addedge(int a, int b, int c){
7     e[en] = (Element){b, c, adj[a]}; adj[a] = en++;
8     e[en] = (Element){a, 0, adj[b]}; adj[b] = en++;
9 }
10 int d[V]; // 最短距離
11 bool visit[V]; // BFS/DFS visit record
12 int q[V]; // queue
13 int BFS(int s, int t){ // 計算最短路徑，求出容許圖
14     memset(d, 0x7f, sizeof(d));
15     memset(visit, false, sizeof(visit));
16     int qn = 0;
17     d[s] = 0;
18     visit[s] = true;
19     q[qn++] = s;
20
21     for (int qf=0; qf<qn; ++qf){
22         int a = q[qf];
23         for (int i = adj[a]; i != -1; i = e[i].next){
24             int b = e[i].b;
25             if (e[i].r > 0 && !visit[b]){
26                 d[b] = d[a] + 1;
27                 visit[b] = true;

```

```

28         q[qn++] = b;
29         if (b == t) return d[t];
30     }
31 }
32 }
33 return V;
34 }
35 int DFS(int a, int df, int s, int t){ //
36     求出一條最短擴充路徑，並擴充流量
37     if (a == t) return df;
38     if (visit[a]) return 0;
39     visit[a] = true;
40     for (int i = adj[a]; i != -1; i = e[i].next){
41         int b = e[i].b;
42         if (e[i].r > 0 && d[a] + 1 == d[b]){
43             int f = DFS(b, min(df, e[i].r), s, t);
44             if (f){
45                 e[i].r -= f;
46                 e[i^1].r += f;
47                 return f;
48             }
49         }
50     }
51     return 0;
52 }
53 int dinitz(int s, int t){
54     int flow = 0;
55     while (BFS(s, t) < V)
56         while (true){
57             memset(visit, false, sizeof(visit));
58             int f = DFS(s, 1e9, s, t);
59             if (!f) break;
60             flow += f;
61         }
62     return flow;
63 }

```

## 4.7 Bipatirate

```

1 const int maxn = 300 + 5;
2 int n, color[maxn];
3 vector<vector<int>> v(maxn);
4 bool dfs(int s){
5     for(auto it : v[s]){
6         if(color[it] == -1){
7             color[it] = 3 - color[s];
8             if(!dfs(it)){
9                 return false;
10            }
11        }
12        if(color[s] == color[it]){
13            return false;
14        }
15    }
16    return true;
17 }
18 void isBipatirate(){
19     bool flag = true;
20     for(int i = 1; i <= n; ++i){
21         if(color[i] == -1){
22             color[i] = 1;
23             flag &= dfs(i);
24         }
25     }
26     if(flag){
27         cout << "YES" << endl;
28     }
29     else{
30         cout << "NO" << endl;
31     }
32 }
33 int main(){
34     while(cin >> n && n){
35         for(int i = 1; i <= n; ++i) v[i].clear();
36         memset(color, -1, sizeof(color));

```

```

37     int a, b;
38     while(cin >> a >> b && (a || b)){
39         v[a].emplace_back(b);
40         v[b].emplace_back(a);
41     }
42     isBipartite();
43 }
44 }

```

## 4.8 Hungarian algorithm

```

1  const int maxn = 500+5;
2  int t, N, bn, gn, match[maxn];
3  bool visited[maxn];
4  vector<vector<int>> G(maxn);
5  struct People{
6      int h;
7      string music, sport;
8      People(){
9          People(int h, string music, string sport){
10             this->h = h;
11             this->music = music;
12             this->sport = sport;
13         }
14     }lef[maxn], rig[maxn];
15     bool check(People boy, People girl){
16         if(abs(boy.h - girl.h) <= 40 && boy.music ==
17             girl.music && boy.sport != girl.sport) return
18             true;
19         return false;
20     }
21     bool dfs(int s){
22         for(int i = 0; i < G[s].size(); ++i){
23             int v = G[s][i];
24             if(visited[v]) continue;
25             visited[v] = true;
26             if(match[v] == -1 || dfs(match[v])){
27                 match[v] = s;
28                 return true;
29             }
30         }
31         return false;
32     }
33     int Hungarian(){
34         int cnt = 0;
35         memset(match, -1, sizeof(match));
36         for(int i = 0; i < bn; ++i){
37             memset(visited, false, sizeof(visited));
38             if(dfs(i)) cnt++;
39         }
40         return cnt;
41     }
42     int main(){
43         cin >> t;
44         while(t--){
45             cin >> N;
46             bn = 0, gn = 0;
47             for(int i = 0; i <= N; ++i) G[i].clear();
48             int h;
49             string sex, music, sport;
50             for(int i = 0; i < N; ++i){
51                 cin >> h >> sex >> music >> sport;
52                 if(sex == "M") lef[bn++] = People(h,
53                     music, sport);
54                 else rig[gn++] = People(h, music, sport);
55             }
56             for(int i = 0; i < bn; ++i){
57                 for(int j = 0; j < gn; ++j)
58                     if(check(lef[i], rig[j]))
59                         G[i].emplace_back(j);
60             }
61             cout << N - Hungarian() << endl;
62         }
63     }

```

## 5 Other

### 5.1 Bubble Sort Expect Value

```

1  /* 期望值算法:
2  擲一枚公平的六面骰子, 其每次「點數」的期望值是 3.5
3   $E(x) = 1 * 1/6 + 2 * 1/6 + 3 * 1/6 + 4 * 1/6 + 5 * 1/6 + 6 * 1/6$ 
4   $= (1 + 2 + 3 + 4 + 5 + 6)/6 = 3.5$ 
5  bubble sort 每兩兩之間交換機率是 1/2
6  總共會做  $C(n, 2)$  次
7   $E(x) = C(n, 2) * 1/2 = (n * (n - 1))/2 * 1/2$ 
8  int t, ca = 1;
9  cin >> t;
10 while(t--){
11     long long int n;
12     cin >> n;
13     cout << "Case " << ca++ << ": ";
14     // 如果  $(n * (n - 1))$  可以被 4 整除
15     // 代表最後答案會是整數, 否則會是分數
16     if((n * (n - 1)) % 4){
17         cout << ( (n * (n - 1)) / 2 ) << "/2" << endl;
18     }
19     else{
20         cout << ( (n * (n - 1)) / 2 ) / 2 << endl;
21     }
22 }

```

### 5.2 ORXOR

```

1  /* 如何切區段, 之所以要  $1 < n$  是為了可以跑 000~111
2  i = 0, binary i = 000
3  0 : 1 5 7
4  i = 1, binary i = 001
5  1 : 1 5 7
6  i = 2, binary i = 010, 看得出來切了一刀
7  2 : 1 | 5 7
8  i = 3, binary i = 011
9  3 : 1 | 5 7
10 i = 4, binary i = 100, 為了要切在 index=2, 所以才要  $1 < n$ 
11 4 : 1 5 | 7
12 i = 5, binary i = 101
13 5 : 1 5 | 7
14 i = 6, binary i = 110
15 6 : 1 | 5 | 7
16 i = 7, binary i = 111
17 7 : 1 | 5 | 7
18 可以觀察出來, 前兩位 bit 是 1 時代表的意義是切在哪裡*/
19 int n;
20 int num[20+7];
21 memset(num, 0, sizeof(num));
22 cin >> n;
23 for(int i = 1; i <= n; i++){
24     cin >> num[i];
25 }
26 int mini = 2147483647; // 不知道為什麼只有 2147483647
27 // 給過
28 //  $1 < n = n * 2$ 
29 for(int i = 0; i < (1 << n); i++){
30     int XOR = 0, OR = 0;
31     for(int j = 1; j <= n; j++){
32         OR |= num[j];
33         if((i & (1 << j))){
34             XOR ^= OR;
35             OR = 0;
36         }
37     }
38     XOR ^= OR;
39     mini = min(mini, XOR);
40 }
41 cout << mini << endl;

```

### 5.3 Race to 1

```

1 const int N = 1000000;
2 bool sieve[N+5];
3 vector<int> pri;
4 double dp[N+5];
5 void Linear_Sieve(){ // 線性篩
6     for (int i = 2; i < N; i++){
7         if (!sieve[i])
8             pri.push_back(i);
9         for (int p: pri){
10             if (i * p >= N){
11                 break;
12             }
13             sieve[i * p] = true;
14             if (i % p == 0){
15                 break;
16             }
17         }
18     }
19 }
20 double dfs(int n){
21     if(dp[n] != -1) return dp[n];
22     dp[n] = 0;
23     if(n == 1) return dp[n];
24     int total = 0, prime = 0;
25     for(int i = 0; i < pri.size() && pri[i] <= n; i++){
26         total++;
27         if(n % pri[i]) continue;
28         prime++;
29         dp[n] += dfs(n/pri[i]);
30     }
31     dp[n] = (dp[n] + total)/prime; // 算期望值
32     return dp[n];
33 }
34 int main(){
35     int t;
36     int num;
37     int ca = 1;
38     for(int i = 0; i <= N; i++){
39         dp[i] = -1;
40     }
41     Linear_Sieve();
42     cin >> t;
43     while(t--){
44         cin >> num;
45
46         cout << "Case " << ca++ << ": " << fixed <<
47             setprecision(10) << dfs(num) << endl;
48     }
}

```

### 5.4 X drawing

```

1 long long int n, a, b, p, q, r, s;
2 cin >> n >> a >> b;
3 cin >> p >> q >> r >> s;
4 for(long long int i = p; i <= q; i++){
5     for(long long int j = r; j <= s; j++){
6         if(abs(i - a) == abs(j - b)){
7             cout << '#';
8         }
9         else{
10             cout << '.';
11         }
12     }
13     cout << endl;
14 }

```

### 5.5 Big Mod

```

1 '''
2 Mod
3 pow(x, y, z) = x^y % z
4 '''
5 # python 如何讀取直到 EOF 用 try except
6 try:
7     while True:
8         # input().split() 用空格切開讀取一整行
9         # map (型態, input().split()) 才能把值全讀成
10             int
11             B, P, M = map(int, input().split())
12             print(pow(B, P, M))
13 except EOFError:
14     exit

```

### 5.6 Crested Ibis vs Monster

```

1 /* dp 背包 - 重量/價值/可重複使用
2 因為這題可以重複使用同一條魔法
3 所以可以這樣 dp*/
4 int h, n;
5 cin >> h >> n;
6 for(int i = 1; i <= n; i++){
7     cin >> a[i] >> b[i];
8 }
9 memset(dp, 0x3f3f3f3f, sizeof(dp));
10 dp[0][0] = 0;
11 for(int i = 1; i <= n; i++){
12     for(int j = 0; j <= h; j++){
13         dp[i][j] = min(dp[i-1][j], dp[i][max(0, j -
14             a[i])] + b[i]);
15     }
16 }
17 cout << dp[n][h] << endl;

```

### 5.7 dpd Knapsack 1

```

1 // dp 背包 - 時間/數量/價值 - 第幾分鐘符合
2 int N, W;
3 cin >> N >> W;
4 int w[100000+5];
5 int v[100000+5];
6 for(int i = 0; i < N; i++){
7     cin >> w[i] >> v[i];
8 }
9 long long int dp[100000+5];
10 memset(dp, 0, sizeof(dp));
11 for(int i = 0; i < N; i++){
12     for(int j = W; j >= w[i]; j--){
13         dp[j] = max(dp[j], dp[j - w[i]] + v[i]);
14     }
15 }
16 cout << dp[W] << endl;

```

### 5.8 Fraction Floor Sum

```

1 /* [N/i] == M
2 -> M <= N/i < M + 1
3 -> N/(M+1) < i <= N/M */
4 long long int N;
5 cin >> N;
6 long long int ans = 0;
7 for(long long int i = 1; i <= N; i++){
8     long long int M = N / i;
9     long long int n = N / M;
10     // 總共會有 n - i 個的 [N/i] 值都是 M
11     ans += (n - i + 1) * M;
12     // 更新跳過 以免重複計算
13     i = n;
14 }
15 cout << ans << endl;

```

## 5.9 Homer Simpson

```

1 // dp 背包 - 時間/數量 - 漢堡
2 int m, n, t;
3 while(cin >> m >> n >> t){
4     int dp[10000+5];
5     memset(dp, -1, sizeof(dp));
6     dp[0] = 0;
7     for(int i = m; i <= t; i++){
8         if(dp[i - m] != -1){
9             dp[i] = max(dp[i], dp[i - m] + 1);
10        }
11    }
12    for(int i = n; i <= t; i++){
13        if(dp[i - n] != -1){
14            dp[i] = max(dp[i], dp[i - n] + 1);
15        }
16    }
17    if(dp[t] == -1){ // 時間無法剛好吃滿的時候
18        for(int i = t; i >= 0; i--){
19            if(dp[i] != -1){
20                cout << dp[i] << " " << t - i << endl;
21                break;
22            }
23        }
24    }
25    else{
26        cout << dp[t] << endl;
27    }
28 }

```

## 5.10 Let Me Count The Ways

```

1 // dp - 時間/數量 - 硬幣排序
2 long long int n, dp[30000+5];
3 int coin[] = {1, 5, 10, 25, 50};
4 memset(dp, 0, sizeof(dp));
5 dp[0] = 1;
6 for(int i = 0; i < 5; i++){
7     for(int j = coin[i]; j < 30000+5; j++){
8         if(dp[j - coin[i]] != -1){
9             dp[j] += dp[j - coin[i]];
10        }
11    }
12 }
13 while(cin >> n){
14     if(dp[n] == 1){
15         cout << "There is only " << dp[n] << " way to
16             produce " << n << " cents change." <<
17             endl;
18     }
19     else{
20         cout << "There are " << dp[n] << " ways to
21             produce " << n << " cents change." <<
22             endl;
23     }
24 }

```

## 5.11 Luggage

```

1 // dp 背包 - 重量/是否成立
2 int t;
3 cin >> t;
4 cin.ignore();
5 while(t--){
6     string str;
7     getline(cin, str);
8     vector<int> v;
9     stringstream ss;
10    int num, cnt = 0, sum = 0;
11    bool dp[4000+5];
12    memset(dp, false, sizeof(dp));
13    ss << str;

```

```

14    while(ss >> num){
15        cnt++;
16        sum += num;
17        v.emplace_back(num);
18    }
19    if(sum & 1){
20        cout << "NO" << endl;
21        continue;
22    }
23    dp[0] = true;
24    for(int i = 0; i < v.size(); i++){
25        for(int j = sum; j >= v[i]; j--){
26            if(dp[j - v[i]]){
27                dp[j] = true;
28            }
29        }
30    }
31    cout << (dp[sum/2] ? "YES" : "NO") << endl;
32 }

```

## 5.12 Number of Pairs

```

1 /* upper_bound ex:
2 10 20 30 30 40 50
3 upper_bound for element 30 is at index 4
4 lower_bound ex:
5 10 20 30 40 50
6 lower_bound for element 30 at index 2 */
7 int t;
8 cin >> t;
9 while(t--){
10    int n, l, r;
11    vector<int> v;
12    cin >> n >> l >> r;
13    int num;
14    for(int i = 0; i < n; i++){
15        cin >> num;
16        v.emplace_back(num);
17    }
18    sort(v.begin(), v.end());
19    long long int ans = 0;
20    for(int i = 0; i < n; i++){
21        ans += (upper_bound(v.begin() + i + 1,
22            v.end(), r - v[i]) -
23            lower_bound(v.begin() + i + 1, v.end(), l
24            - v[i]));
25    }
26    cout << ans << endl;
27 }

```

## 5.13 SuperSale

```

1 // dp 背包 - 重量/價值/不可重複使用 - 舉重
2 int t;
3 cin >> t;
4 while(t--){
5     int n;
6     cin >> n;
7     for(int i = 0; i < n; i++){
8         cin >> edge[i].p >> edge[i].w;
9     }
10    int g, total = 0;
11    cin >> g;
12    for(int i = 0; i < g; i++){
13        int pw, dp[30+5];
14        cin >> pw;
15        memset(dp, 0, sizeof(dp));
16        for(int j = 0; j < n; j++){
17            for(int k = pw; k >= edge[j].w; k--){
18                dp[k] = max(dp[k], dp[k - edge[j].w]
19                    + edge[j].p);
20            }
21        }
22    }

```

```

21     total += dp[pw];
22 }
23 cout << total << endl;
24 }

```

## 5.14 Walking on the Safe Side

```

1 // dp - 地圖更新
2 int t;
3 bool space = false;
4 cin >> t;
5 while(t--){
6     if(space){
7         cout << endl;
8     }
9     else{
10         space = true;
11     }
12     int r, c;
13     cin >> r >> c;
14     cin.ignore();
15     memset(mp, false, sizeof(mp));
16     memset(dp, 0, sizeof(dp));
17     string str;
18     for(int i = 0; i < r; i++){
19         getline(cin, str);
20         int n, num;
21         stringstream ss(str);
22         ss >> n;
23         while(ss >> num){
24             mp[n][num] = true;
25         }
26     }
27     dp[1][1] = 1;
28     for(int i = 1; i <= r; i++){
29         for(int j = 1; j <= c; j++){
30             if(mp[i][j]){
31                 continue;
32             }
33             if(i > 1){
34                 dp[i][j] += dp[i-1][j];
35             }
36             if(j > 1){
37                 dp[i][j] += dp[i][j-1];
38             }
39         }
40     }
41     cout << dp[r][c] << endl;
42 }

```

## 6 Function

### 6.1 strstr

```

1 #include <stdio.h>
2 #include <string.h>
3
4 int main(){
5     char * c;
6     char str1[1005], str2[1005];
7     scanf("%s %s", str1, str2);
8     c = strstr(str1, str2);
9     if (c != NULL){
10         printf("Yes\n");
11     }
12     else printf("No\n");
13 }
14 // Input : Hello eLl
15 // Output : No

```

### 6.2 substr

```

1 int main(){
2     string str; //abcdef
3     cin >> str;
4     string tmp;
5     tmp = str.substr(0, 2); //ab
6     str = str.substr(2); //cdef
7     cout << tmp << " " << str;
8     return 0;
9 }

```

### 6.3 map set

```

1 .begin( ) // Return iterator to beginning
2 .end( ) // Return iterator to end
3 .empty( ) // 檢查是否為空
4 .size( ) // 回傳大小
5 mp.insert(pair<char,int>('a',100))
6 st.insert(100) // 插入key、value
7 .erase( ) // 刪掉指定key和他的value
8 .clear( ) // 清空整個 map
9 m.find( )
10 cout << "a => " << mymap.find('a')->second << endl;
11 // 找出 map 裡 key
12 // 有沒有在裡面，如果有的話會回傳元素所在的iterator，否則傳空
13 s.count() // 返回某個值元素在set的個數
14 while( !mymap.empty()){
15     cout << mymap.begin()->first << " => " <<
16         mymap.begin()->second << endl;
17     mymap.erase(mymap.begin());
18 }
19 for (auto it = mymap.begin(); it != mymap.end(); ++it)
20     cout << it->first << " => " << it->second << endl;

```

### 6.4 vector

```

1 v.erase(v.begin() + 5) //拿掉第六個數
2 v.erase (v.begin(), v.begin() + 3); //拿掉前三個數

```

### 6.5 setprecision

```

1 // 將數字的小數部分設定為固定長度
2 cnt = 3.5555;
3 cout << fixed << setprecision(3) << cnt ;
4 // output : 3.555

```

### 6.6 GCD LCM

```

1 int gcd(int a, int b){
2     return (b == 0 ? a : gcd(b, a % b));
3 }
4 int lcm(int a, int b){
5     return a * b / gcd(a, b);
6 }
7
8 /* 輾轉相除法 - 求兩數是否互質
9 如果兩數互質 最終結果其中一方為0時 另一方必為1
10 若兩數有公因數 最終結果其中一方為0時 另一方必不為1 */
11 while ( ( num1 % num2 ) != 0 && ( num2 % num1 ) != 0 );

```



## 6.7 reverse

```
1 int a[10] = {0, 1, 2, 3, 4, 5, 6, 7, 8, 9};
2 reverse(a, a+5) // 轉換 0~5
3
4 vector<int> v;
5 reverse(v.begin(), v.end());
6
7 string str = "123";
8 reverse(str.begin(), str.end());
9 cout << str << endl; //321
```

## 6.8 CHAR

```
1 isdigit()
2 isalnum() //判斷字母 // 數字
3 isalpha()
4 islower()
5 isupper()
6 isblank() //判斷是否為空格，或者 tab 健制表符，即
   space 和 \t
7 toupper()
8 tolower()
```

## 6.9 sort

```
1 priority_queue<int, vector<int>, less<int>> //大到小
2 priority_queue<int, vector<int>, greater<int>>
   //小到大
3
4 int arr[] = {4, 5, 8, 3, 7, 1, 2, 6, 10, 9};
5 sort(arr, arr+10);
6
7 vector<int> v;
8 sort(v.begin(), v.end()); //小到大
9
10 int cmp(int a, int b){
11     return a > b;
12 }
13 sort(v.begin(), v.end(), cmp); //大到小
```

## 6.10 struct

```
1 struct area{
2     int a, b;
3     bool operator<(const area rhs) const{
4         return a > rhs.a || (a == a && b > rhs.b);
5     }
6     bool operator!=(const area rhs) const{
7         return a != rhs.a || b != rhs.b;
8     }
9 };
```

## 6.11 deque

```
1 deque<int> que;
2 que.push_back(10);
3 que.push_front(20);
4 que.front()
5 que.back()
6 que.pop_front()
7 que.pop_back()
8 cout << "Element at position 2 : " << que.at(2) <<
   endl;
```

## 6.12 python template

```
1 import math
2 import operator
3
4 try:
5     while(1):
6         listx = []
7         listx.append("...")
8         list_s = sorted(listx) # 小到大
9         list_s = sorted(listx, reverse = True) #
           大到小
10        # max(listx)
11        # min(listx)
12        # sum(listx)
13        # len(listx)
14        dicty = {}
15        dicty[key] = "value"
16        dicty= sorted(dicty.items()) # by key
17        dicty= sorted(dicty.items(),
           key=operator.itemgetter(1)) # by value
18        # EOF寫法
19        # 階層 math.factorial(3) == 6
20        # 絕對值 math.fabs(x)
21        # 無條件進位 math.ceil(3.1) == 3
22        # 無條件捨去 math.floor(2.9) == 2
23        # C n 取 k math.comb(n, k)
24        # math.gcd
25        # math.lcm
26        # e 次 x 冪 math.exp(x)
27 except EOFError:
28     pass
```