#### Contents 10 int mid = (lef + rig)/2;int p1 = dfs(lef, mid); 11 12 int p2 = dfs(mid, rig); 1 13 if(num[p1] > num[p2]){ 1 Data Structure 14 return p1; 1 } 1.2 Segment tree . . . . . . . . . . . . . . . 15 else{ 16 17 return p2; 18 1 19 Graph 1.3 Trie const int MAXC = ; struct Trie { 4 Other int len[MAXL]; 6 int sz; void init() { 9 10 sz = 0;11 } 12 13 int p = 0; 14 6 15 6 6 16 17 5 Function } 18 19 p = nex[p][id]; 20 21 22 23 24 int p = 0; 25 vector<int> ans; 8 26 28 29 return ans: 30 } Data Structure p = nex[p][id]; 31 32 **if** (len[p]) { 33 1.1 BIT 34 35 36

```
1 #define lowbit(k) (k & -k)
2 void add(vector<int> &tr, int id, int val) {
    for (; id <= n; id += lowbit(id)) {</pre>
3
       tr[id] += val;
    }
5
6 }
7 int sum(vector<int> &tr, int id) {
    int ret = 0;
    for (; id >= 1; id -= lowbit(id)) {
      ret += tr[id];
10
11
12
    return ret;
13 }
```

## 1.2 Segment tree

```
1 int dfs(int lef, int rig){
2
      if(lef + 2 == rig){
3
          if(num[lef] > num[rig-1]){
               return lef;
5
          }
6
          else{
7
               return rig-1;
8
          }
      }
```

```
const int MAXL = ; // 自己填
    int nex[MAXL][MAXC];
      memset(nex, 0, sizeof(nex));
      memset(len, 0, sizeof(len));
    void insert(const string &str) {
      for (char c : str) {
         int id = c - 'a';
        if (!nex[p][id]) {
          nex[p][id] = ++sz;
      len[p] = str.length();
    vector<int> find(const string &str, int i) {
      for (; i < str.length(); i++) {</pre>
         int id = str[i] - 'a';
         if (!nex[p][id]) {
          ans.pb(len[p]);
       return ans;
    }
37
38 };
```

#### 2 DP

#### 2.1 Josephus

```
1 int josephus (int n, int k) {
     // 有 n 個人圍成一圈,每 k 個一次
     return n > 1 ? (josephus(n-1 , k) + k) % n : 0;
3
4 }
5 // 回傳最後一人的編號, 0 index
```

#### 2.2 LCS

```
1 int LCS(string s1, string s2) {
   int n1 = s1.size(), n2 = s2.size();
3
   int dp[n1+1][n2+1] = \{0\};
    // dp[i][j] = s1的前i個字元和s2的前j個字元
   for (int i = 1; i <= n1; i++) {</pre>
5
     for (int j = 1; j <= n2; j++) {</pre>
```

```
if (s1[i - 1] == s2[j - 1]) {
    dp[i][j] = dp[i - 1][j - 1] + 1;
} else {
    dp[i][j] = max(dp[i - 1][j], dp[i][j - 1]);
}

return dp[n1][n2];
}
```

## 2.3 LIS

```
1 int LIS(vector<int> &a) { // Longest Increasing
       Subseauence
     vector<int> s;
    for (int i = 0; i < a.size(); i++) {</pre>
3
       if (s.empty() || s.back() < a[i]) {</pre>
5
         s.push_back(a[i]);
6
       } else {
         *lower_bound(s.begin(), s.end(), a[i],
7
           [](int x, int y) {return x < y;}) = a[i];
9
    }
10
11
    return s.size();
12 }
```

# 3 Graph

## 3.1 SPFA

```
1 bool SPFA(int s){
       // 記得初始化這些陣列
       int cnt[1000+5], dis[1000+5];
3
4
       bool inqueue[1000+5];
5
       queue<int> q;
6
7
       q.push(s);
8
       dis[s] = 0;
9
       inqueue[s] = true;
10
       cnt[s] = 1;
       while(!q.empty()){
11
12
           int now = q.front();
           q.pop();
13
14
           inqueue[now] = false;
15
           for(auto &e : G[now]){
16
17
                if(dis[e.t] > dis[now] + e.w){
                    dis[e.t] = dis[now] + e.w;
18
19
                    if(!inqueue[e.t]){
20
                        cnt[e.t]++;
                        if(cnt[e.t] > m){
21
22
                             return false;
23
24
                        inqueue[e.t] = true;
25
                        q.push(e.t);
26
               }
27
28
           }
29
30
       return true;
31 }
```

# 3.2 Dijkstra

```
1 struct Item{
2    int u, dis;
3    // 取路徑最短
4    bool operator < (const Item &other) const{
5    return dis > other.dis;
6 }
```

```
8 int dis[maxn];
  vector<Edge> G[maxn];
10 void dijkstra(int s){
11
      for(int i = 0; i \le n; i++){
           dis[i] = inf;
12
13
14
      dis[s] = 0;
15
      priority_queue < Item > pq;
16
       pq.push({s, 0});
17
       while(!pq.empty()){
           // 取路徑最短的點
18
           Item now = pq.top();
19
20
           pq.pop();
           if(now.dis > dis[now.u]){
21
22
               continue;
           }
23
           // 鬆弛更新,把與 now.u 相連的點都跑一遍
24
           for(Edge e : G[now.u]){
25
26
               if(dis[e.v] > now.dis + e.w){
27
                   dis[e.v] = now.dis + e.w;
28
                   pq.push({e.v, dis[e.v]});
               }
29
           }
30
      }
31
32 }
```

# 3.3 Floyd Warshall

```
void floyd_warshall(){
2
       for(int i = 0; i < n; i++){</pre>
           for(int j = 0; j < n; j++){</pre>
3
               G[i][j] = INF;
5
6
           G[i][i] = 0;
7
      for (int k = 0; k < n; k++){
8
           嘗試每一個中繼點
9
           for (int i = 0; i < n; i++){ //</pre>
               計算每一個 i 點與每一個 j 點
               for (int j = 0; j < n; j++){
10
                    G[i][j] = min(G[i][j], G[i][k] +
11
                        G[k][j]);
               }
12
13
           }
      }
14
15
  }
```

## 3.4 Disjoint set Kruskal

```
struct Edge{
2
       int u, v, w;
       // 用權重排序 由大到小
3
       bool operator < (const Edge &other) const{</pre>
5
           return w > other.w;
       }
6
7
  }edge[maxn];
8
  // disjoint set
  int find(int x){
10
    if(parent[x] < 0){
11
       return x;
12
13
    else{
14
       return parent[x] = find(parent[x]);
15
16
  }
17
  void unite(int a, int b){
    a = find(a):
18
19
    b = find(b);
20
21
    if(a != b){
       if(parent[a] < parent[b]){</pre>
22
         parent[a] += parent[b];
23
```

3

```
45 bool branch2(){ // 延展交錯樹:使用新添的等邊
24
        parent[b] = a;
                                                                   for (int y=0; y<Y; ++y){</pre>
      }
25
                                                            46
26
                                                            47
                                                                       if (!vy[y] && dy[y] == 0){
         parent[b] += parent[a];
                                                                           vy[y] = true;
27
                                                            48
                                                                           if (my[y] == -1){
28
         parent[a] = b;
                                                            49
29
                                                            50
                                                                               augment(pdy[y], y);
    }
                                                            51
                                                                               return true;
30
31 }
                                                            52
  void kruskal(){
                                                                           int z = my[y];
32
                                                            53
      memset(parent, -1, sizeof(parent));
                                                                           *qb++ = z; p[z] = pdy[y]; vx[z] = true;
33
34
      sort(edge, edge + m);
                                                                               relax(z):
                                                                       }
35
      int i, j;
                                                            55
36
      for (i = 0, j = 0; i < n - 1 && j < m; i++){}
                                                                   }
                                                            56
                                                            57
                                                                   return false;
           // 如果 u 和 v 的祖先相同, 則 j++
37
                                                            58
               (祖先相同代表會產生環 所以不要)
                                                              int Hungarian(){
          while(find(edge[j].u) == find(edge[j].v)) j++;
                                                            59
38
                                                                   // 初始化vertex labeling
                                                            60
           // 若部會產生環 則讓兩點之間產生橋
39
                                                                   // memset(lx, 0, sizeof(lx)); // 任意值皆可
                                                            61
               (連接兩顆子生成樹)
                                                                   memset(ly, 0, sizeof(ly));
                                                            62
           unite(edge[j].u, edge[j].v);
40
                                                            63
                                                                   for (int x=0; x<X; ++x)</pre>
41
           j++;
                                                                       for (int y=0; y<Y; ++y)</pre>
                                                            64
42
                                                            65
                                                                           lx[x] = max(lx[x], adj[x][y]);
43 }
                                                            66
                                                                   // X側每一個點,分別建立等邊交錯樹。
                                                            67
                                                                   memset(mx, -1, sizeof(mx));
                                                            68
  3.5 KM
                                                                   memset(my, -1, sizeof(my));
                                                            69
                                                            70
                                                                   for (int x=0; x<X; ++x){</pre>
                                                            71
                                                                       memset(vx, false, sizeof(vx));
1 \mid \mathbf{const} \quad \mathbf{int} \quad X = 50;
                      // X的點數,等於Y的點數
                                                                       memset(vy, false, sizeof(vy));
                                                            72
2 | const int Y = 50;
                       // Y的點數
                                                                       memset(dy, 0x7f, sizeof(dy));
                                                            73
                       // 精簡過的adjacency matrix
3 int adj[X][Y];
                                                            74
                                                                       qf = qb = q;
4 int 1x[X], 1y[Y];
                       // vertex labeling
                                                            75
                                                                       *qb++ = x; p[x] = -1; vx[x] = true; relax(x);
5 int mx[X], my[Y];
                       //
                                                            76
                                                                       while (true){
       X各點的配對對象、Y各點的配對對象
                                                            77
                                                                           if (branch1()) break;
6 int q[X], *qf, *qb; // BFS queue
                                                            78
                                                                           reweight():
                       // BFS
7 int p[X];
                                                            79
                                                                           if (branch2()) break;
       parent,交錯樹之偶點,指向上一個偶點
                                                            80
8 bool vx[X], vy[Y]; // 記錄是否在交錯樹上
                                                            81
                                                                   }
9| int dy[Y], pdy[Y]; // 表格
                                                                   // 計算最大權完美匹配的權重
                                                            82
10
                                                                   int weight = 0;
                                                            83
11 void relax(int x){ // relaxation
                                                            84
                                                                   for (int x=0; x<X; ++x)</pre>
12
      for (int y=0; y<Y; ++y)</pre>
                                                                       weight += adj[x][mx[x]];
                                                            85
          if (adj[x][y] != 1e9)
13
                                                            86
                                                                   return weight;
               if (lx[x] + ly[y] - adj[x][y] < dy[y]){
                                                            87 }
14
                   dy[y] = 1x[x] + 1y[y] - adj[x][y];
15
16
                   pdy[y] = x; //
                       記錄好是從哪個樹葉連出去的
                                                               3.6 Dinic
17
18 }
19 void reweight(){ // 調整權重、調整表格
                                                             1 // Maximum Flow
                                                             2 | const int V = 100, E = 1000;
20
      int d = 1e9;
21
      for (int y=0; y<Y; ++y) if (!vy[y]) d = min(d,
                                                             3 int adj[V]; // adjacency lists,初始化為-1。
                                                               struct Element {int b, r, next;} e[E*2];
           dy[v]);
22
      for (int x=0; x<X; ++x) if ( vx[x]) lx[x] -= d;</pre>
                                                             5
                                                               int en = 0;
      for (int y=0; y<Y; ++y) if ( vy[y]) ly[y] += d;</pre>
                                                               void addedge(int a, int b, int c){
23
                                                             6
24
      for (int y=0; y<Y; ++y) if (!vy[y]) dy[y] -= d;</pre>
                                                                   e[en] = (Element){b, c, adj[a]}; adj[a] = en++;
25 }
                                                                   e[en] = (Element){a, 0, adj[b]}; adj[b] = en++;
                                                             9 }
26 void augment(int x, int y){ // 擴充路徑
27
      for (int ty; x != -1; x = p[x], y = ty){
                                                            10 int d[V];
                                                                               // 最短距離
                                                               bool visit[V]; // BFS/DFS visit record
28
           ty = mx[x]; my[y] = x; mx[x] = y;
                                                                               // queue
                                                            12 int q[V];
29
                                                            13 int BFS(int s, int t){ // 計算最短路徑,求出容許圖
30 }
31 bool branch1(){ // 延展交錯樹:使用既有的等邊
                                                            14
                                                                   memset(d, 0x7f, sizeof(d));
32
      while (qf < qb)</pre>
                                                            15
                                                                   memset(visit, false, sizeof(visit));
           for (int x=*qf++, y=0; y<Y; ++y)</pre>
                                                                   int qn = 0;
33
                                                            16
               if (!vy[y] && lx[x] + ly[y] == adj[x][y]){
34
                                                            17
                                                                   d[s] = 0;
                                                                   visit[s] = true;
                   vy[y] = true;
35
                                                            18
36
                   if (my[y] == -1){
                                                            19
                                                                   q[qn++] = s;
37
                       augment(x, y);
                                                            20
38
                       return true;
                                                            21
                                                                   for (int qf=0; qf<qn; ++qf){</pre>
39
                   }
                                                            22
                                                                       int a = q[qf];
                   int z = my[y];
                                                            23
                                                                       for (int i = adj[a]; i != -1; i = e[i].next){
40
41
                   *qb++ = z; p[z] = x; vx[z] = true;
                                                            24
                                                                           int b = e[i].b;
                       relax(z);
                                                            25
                                                                           if (e[i].r > 0 && !visit[b]){
```

26

27

28

d[b] = d[a] + 1;

visit[b] = true;

q[qn++] = b;

42

43

44 }

return false;

```
29
                    if (b == t) return d[t];
               }
30
31
           }
32
       }
33
       return V;
34 }
35 int DFS(int a, int df, int s, int t){ //
       求出一條最短擴充路徑,並擴充流量
       if (a == t) return df;
36
37
       if (visit[a]) return 0;
38
       visit[a] = true;
39
       for (int i = adj[a]; i != -1; i = e[i].next){
           int b = e[i].b;
40
41
           if (e[i].r > 0 && d[a] + 1 == d[b]){
               int f = DFS(b, min(df, e[i].r), s, t);
42
43
               if (f){
44
                    e[i].r -= f;
                    e[i^1].r += f;
45
46
                    return f;
47
               }
           }
48
       }
49
50
       return 0;
51 }
52 int dinitz(int s, int t){
       int flow = 0;
53
       while (BFS(s, t) < V)
54
55
           while (true){
               memset(visit, false, sizeof(visit));
56
57
               int f = DFS(s, 1e9, s, t);
58
               if (!f) break;
               flow += f;
59
60
           }
61
       return flow;
62 }
```

# 4 Other

## 4.1 Bubble Sort Expect Value

```
1 /* 期望值算法:
  2 | 擲一枚公平的六面骰子,其每次「點數」的期望值是 3.5
  |E(x)| = 1 \times 1/6 + 2 \times 1/6 + 3 \times 1/6 + 4 \times 1/6 + 5 \times 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 + 1/6 +
                               1/6 + 6 * 1/6
   |4| = (1 + 2 + 3 + 4 + 5 + 6)/6 = 3.5
  5 bubble sort 每兩兩之間交換機率是 1/2
  6| 總共會做 C(n, 2) 次
  7 E(x) = C(n, 2) * 1/2 = (n * (n - 1))/2 * 1/2 */
  8 int t, ca = 1;
  9 cin >> t;
10 while(t--){
11
                            long long int n;
                            cin >> n;
12
                            cout << "Case " << ca++ << ": ";
13
14
                             // 如果 (n * (n - 1)) 可以被 4 整除
                                               代表最後答案會是整數,否則會是分數
                            if((n * (n - 1)) % 4){
15
                                              cout << ( (n * (n - 1)) / 2 ) << "/2" << endl;
16
                            }
17
18
                            else{
19
                                              cout << ((n * (n - 1)) / 2) / 2 << endl;
20
21 }
```

## 4.2 ORXOR

```
1 /* 如何切區段,之所以要1<<n是為了可以跑000~111
2 i = 0, binary i = 000
3 0 : 1 5 7
4 i = 1, binary i = 001
5 1 : 1 5 7
```

```
6 | i = 2, binary i = 010, 看得出來切了一刀
  2:1157
|i| = 3, binary |i| = 011
9 3 : 1 | 5 7
10 i = 4, binary i = 100, 為了要切在index=2, 所以才要1<<j
  4:15/7
  i = 5, binary i = 101
12
13 5 : 1 5 / 7
|14| i = 6, binary i = 110
15
  6:1|5|7
  i = 7, binary i = 111
17 7 : 1 | 5 | 7
18| 可以觀察出來,前兩位 bit 是 1 時代表的意義是切在哪裡*/
19 int n;
20 int num[20+7];
  memset(num, 0, sizeof(num));
21
  cin >> n;
  for(int i = 1; i <= n; i++){</pre>
23
24
      cin >> num[i];
25 }
26 int mini = 2147483647; // 不知道為甚麼只有 2147483647
      給過
  // 1 << n = n * 2
27
28
  for(int i = 0; i < (1 << n); i++){</pre>
      int XOR = 0, OR = 0;
29
30
      for(int j = 1; j <= n; j++){
31
          OR |= num[j];
32
          if((i & (1 << j))){</pre>
33
              XOR ^= OR;
              OR = 0;
34
35
          }
36
      XOR ^= OR;
37
38
      mini = min(mini, XOR);
39 }
40 cout << mini << endl;
```

#### 4.3 Race to 1

```
1 const int N = 1000000;
  bool sieve[N+5];
3
  vector<int> pri;
  double dp[N+5];
  void Linear_Sieve(){ // 線性篩
      for (int i = 2; i < N; i++){
           if (!sieve[i])
               pri.push_back(i);
           for (int p: pri){
10
               if (i * p >= N){
11
                    break;
12
13
               sieve[i * p] = true;
14
               if (i % p == 0){
15
                    break;
16
               }
17
           }
18
      }
19
  double dfs(int n){
20
21
       if(dp[n] != -1) return dp[n];
22
       dp[n] = 0;
       if(n == 1) return dp[n];
23
       int total = 0, prime = 0;
24
       for(int i = 0; i < pri.size() && pri[i] <= n;</pre>
25
           i++){
26
           total++;
27
           if(n % pri[i]) continue;
28
           prime++;
           dp[n] += dfs(n/pri[i]);
29
      }
30
31
       dp[n] = (dp[n] + total)/prime; // 算期望值
32
       return dp[n];
33
  }
34
  int main(){
      int t;
35
```

```
36
       int num;
       int ca = 1;
37
       for(int i = 0; i <= N; i++){</pre>
38
            dp[i] = -1;
39
40
41
       Linear_Sieve();
       cin >> t;
42
43
       while(t--){
            cin >> num;
44
45
46
            cout << "Case " << ca++ << ": " << fixed <<
                 setprecision(10) << dfs(num) << endl;</pre>
47
       }
48 }
```

# 4.4 X drawing

```
1 long long int n, a, b, p, q, r, s;
2 cin >> n >> a >> b;
3 cin >> p >> q >> r >> s;
4 for(long long int i = p; i <= q; i++){
       for(long long int j = r; j <= s; j++){</pre>
6
           if(abs(i - a) == abs(j - b)){
                cout << '#';
7
           }
8
           else{
9
10
                cout << '.';
11
           }
12
13
       cout << endl;</pre>
14 }
```

# 4.5 Big Mod

```
1 '''
2 Mod
3 \mid pow(x, y, z) = x^y \% z
5 # python 如何讀取直到 EOF 用 try except
6 try:
7
      while True:
          # input().split() 用空格切開讀取一整行
8
9
          # map (型態, input().split()) 才能把值全讀成
             int
          B, P, M = map(int, input().split())
10
11
          print(pow(B, P, M))
12 except EOFError:
     exit
13
```

## 4.6 Crested Ibis vs Monster

```
1 /* dp 背包 - 重量/價值/可重複使用
2 因為這題可以重複使用同一條魔法
3| 所以可以這樣 dp*/
4 int h, n;
5 cin >> h >> n;
6 for(int i = 1; i <= n; i++){
      cin >> a[i] >> b[i];
8 }
9 memset(dp, 0x3f3f3f3f, sizeof(dp));
10 | dp[0][0] = 0;
11 for(int i = 1; i <= n; i++){
      for(int j = 0; j <= h; j++){</pre>
12
          dp[i][j] = min(dp[i-1][j], dp[i][max(0, j -
13
              a[i])] + b[i]);
14
      }
16 cout << dp[n][h] << endl;</pre>
```

## 4.7 dpd Knapsack 1

```
1 // dp 背包 - 時間/數量/價值 - 第幾分鐘符合
2 int N, W;
3 cin >> N >> W:
  int w[100000+5];
  int v[100000+5];
  for(int i = 0; i < N; i++){
7
      cin >> w[i] >> v[i];
  }
8
  long long int dp[100000+5];
9
10
  memset(dp, 0, sizeof(dp));
  for(int i = 0; i < N; i++){
11
12
      for(int j = W; j >= w[i]; j--){
13
          dp[j] = max(dp[j], dp[j - w[i]] + v[i]);
14
15 }
16 cout << dp[W] << endl;</pre>
```

### 4.8 Fraction Floor Sum

```
1 / * [N/i] == M
2
  -> M <= N/i < M + 1
|3| -> N/(M+1) < i <= N/M */
4 long long int N;
  cin >> N;
5
6
  long long int ans = 0;
  for(long long int i = 1; i <= N; i++){</pre>
7
      long long int M = N / i;
9
      long long int n = N / M;
10
      // 總共會有 n - i 個的 [N/i] 值都是 M
      ans += (n - i + 1) * M;
11
      // 更新跳過 以免重複計算
12
13
      i = n;
14 }
15 cout << ans << endl;
```

# 4.9 Homer Simpson

```
1 // dp 背包 - 時間/數量 - 漢堡
  int m, n, t;
3
  while(cin >> m >> n >> t){
      int dp[10000+5];
5
      memset(dp, -1, sizeof(dp));
       dp[0] = 0;
6
7
       for(int i = m; i <= t; i++){</pre>
           if(dp[i - m] != -1){
8
               dp[i] = max(dp[i], dp[i - m] + 1);
           }
10
11
12
       for(int i = n; i <= t; i++){</pre>
           if(dp[i - n] != -1){
13
               dp[i] = max(dp[i], dp[i - n] + 1);
14
15
16
       if(dp[t] == -1){ // 時間無法剛好吃滿的時候
17
18
           for(int i = t; i >= 0; i--){
19
               if(dp[i] != -1){
                    cout << dp[i] << " " << t - i << endl;
20
21
22
23
           }
24
      }
       else{
25
26
           cout << dp[t] << endl;</pre>
27
28 }
```

## 4.10 Let Me Count The Ways

```
1 // dp - 時間/數量 - 硬幣排序
2 long long int n, dp[30000+5];
3 int coin[] = {1, 5, 10, 25, 50};
4 memset(dp, 0, sizeof(dp));
5|dp[0] = 1;
6 for (int i = 0; i < 5; i++){
      for(int j = coin[i]; j < 30000+5; j++){</pre>
           if(dp[j - coin[i]] != -1){
9
               dp[j] += dp[j - coin[i]];
10
11
      }
12 }
13 while(cin >> n){
      if(dp[n] == 1){
14
           cout << "There is only " << dp[n] << " way to
15
               produce " << n << " cents change." <<</pre>
16
       }
17
       else{
           cout << "There are " << dp[n] << " ways to</pre>
18
               produce " << n << " cents change." <<
      }
19
20 }
```

# 4.11 Luggage

```
1 // dp 背包 - 重量/是否成立
2 int t;
3 cin >> t;
4 cin.ignore();
  while(t--){
       string str;
       getline(cin , str);
8
       vector<int> v;
       stringstream ss;
9
       int num, cnt = 0, sum = 0;;
10
       bool dp[4000+5];
11
12
       memset(dp, false, sizeof(dp));
       ss << str;
13
14
       while(ss >> num){
15
           cnt++;
           sum += num;
16
17
           v.emplace_back(num);
18
19
       if(sum & 1){
           cout << "NO" << endl;
20
           continue;
21
22
23
       dp[0] = true;
24
       for(int i = 0; i < v.size(); i++){</pre>
           for(int j = sum; j >= v[i]; j--){
25
                if(dp[j - v[i]]){
26
                    dp[j] = true;
27
28
           }
29
       }
30
31
       cout << (dp[sum/2] ? "YES" : "NO") << endl;</pre>
32 }
```

### 4.12 Number of Pairs

```
12
       cin >> n >> 1 >> r;
       int num;
13
14
       for(int i = 0; i < n; i++){</pre>
15
            cin >> num;
16
            v.emplace_back(num);
17
18
       sort(v.begin(), v.end());
19
       long long int ans = 0;
20
       for(int i = 0; i < n; i++){</pre>
            ans += (upper_bound(v.begin() + i + 1,
21
                v.end(), r - v[i]) -
                lower_bound(v.begin() + i + 1, v.end(), 1
                 - v[i]));
       }
22
23
       cout << ans << endl;</pre>
24 }
```

# 4.13 SuperSale

```
1 // dp 背包 - 重量/價值/不可重複使用 - 舉重
  int t;
  cin >> t;
  while(t--){
      int n;
6
       cin >> n;
7
       for(int i = 0; i < n; i++){
           cin >> edge[i].p >> edge[i].w;
8
9
10
       int g, total = 0;
11
       cin >> g;
       for(int i = 0; i < g; i++){
12
           int pw, dp[30+5];
13
           cin >> pw;
14
15
           memset(dp, 0, sizeof(dp));
           for(int j = 0; j < n; j++){</pre>
16
17
               for(int k = pw; k >= edge[j].w; k--){
                   dp[k] = max(dp[k], dp[k - edge[j].w]
18
                        + edge[j].p);
19
               }
20
21
           total += dp[pw];
22
       cout << total << endl;</pre>
23
24 }
```

## 4.14 Walking on the Safe Side

```
1 // dp - 地圖更新
2 int t;
3 bool space = false;
  cin >> t;
  while(t--){
       if(space){
           cout << endl;</pre>
8
       }
9
       else{
10
           space = true;
11
12
       int r, c;
13
       cin >> r >> c;
14
       cin.ignore();
15
       memset(mp, false, sizeof(mp));
       memset(dp, 0, sizeof(dp));
16
17
       string str;
       for(int i = 0; i < r; i++){</pre>
18
19
           getline(cin, str);
20
           int n, num;
21
           stringstream ss(str);
22
           ss >> n;
23
           while(ss >> num){
24
                mp[n][num] = true;
25
26
       }
```

```
27
        dp[1][1] = 1;
        for(int i = 1; i <= r; i++){</pre>
28
29
             for(int j = 1; j <= c; j++){</pre>
                 if(mp[i][j]){
30
31
                      continue;
32
                 }
                 if(i > 1){
33
34
                      dp[i][j] += dp[i-1][j];
                 }
35
                  if(j > 1){
36
37
                      dp[i][j] += dp[i][j-1];
                 }
38
39
            }
        }
40
41
        cout << dp[r][c] << endl;</pre>
42 }
```

# **Function**

### 5.1 strstr

```
1 #include <stdio.h>
2 #include <string.h>
4 int main(){
5 char * c;
6 char str1[1005], str2[1005];
7 scanf("%s %s", str1, str2);
8 c = strstr(str1, str2);
9 if (c != NULL){
       printf("Yes\n");
10
11 }
12 else printf("No\n");
13 }
14 // Input : Hello eLl
15 // Output : No
```

## 5.2 substr

```
1 int main(){
2
      string str; //abcdef
      cin >> str;
3
      string tmp;
5
      tmp = str.substr(0, 2); //ab
6
      str = str.substr(2); //cdef
      cout << tmp << " " << str;
7
      return 0;
```

## 5.3 map set

```
1 .begin( ) // Return iterator to beginning
2 .end( ) // Return iterator to end
3 | .empty( ) // 檢查是否為空
4 . size( ) // 回傳大小
5 mp.insert(pair<char,int>('a',100))
6 st.insert(100) // 插入key \ value
7 .erase() // 刪掉指定key和他的value
8 .clear( ) // 清空整個 map
9 m.find( )
10 cout << "a => " << mymap.find('a')->second << endl;</pre>
      // 找出 map 裡 key
11
          有沒有在裡面,如果有的話會回傳元素所在的iterator 2 priority_queue<int, vector<int>, greater<int>>
12 s.count() // 返回某個值元素在 set 的 個數
13 while( !mymap.empty()){
      cout << mymap.begin()->first << " => " <<
14
          mymap.begin()->second << endl;</pre>
15
      mymap.erase(mymap.begin());
16 }
```

```
17 for (auto it = mymap.begin(); it != mymap.end(); ++it)
      cout << it->first << " => " << it->second << endl;</pre>
```

## 5.4 vector

```
1 | v.erase(v.begin() + 5) //拿掉第六個數
2 v.erase (v.begin(), v.begin() + 3); //拿掉前三個數
```

# 5.5 setprecision

```
1 // 將數字的小數部分設定為固定長度
2 cnt = 3.5555;
3 cout << fixed << setprecision(3) << cnt ;</pre>
4 // output : 3.555
```

#### 5.6 GCD LCM

```
1 int gcd(int a, int b){
     return (b == 0 ? a : gcd(b, a % b));
2
 }
3
  int lcm(int a, int b){
5
     return a * b / gcd(a, b);
6 }
7
  /* 輾轉相除法 - 求兩數是否互質
9 如果兩數互質 最終結果其中一方為0時 另一方必為1
10 若兩數有公因數 最終結果其中一方為 0時 另一方必不為 1 */
 while ( ( num1 %= num2 ) != 0 && ( num2 %= num1 ) !=
     0);
```

## 5.7 reverse

```
1 int a[10] = {0, 1, 2, 3, 4, 5, 6, 7, 8, 9};
 reverse(a, a+5) // 轉換0~5
 vector<int> v;
4
 reverse(v.begin(), v.end());
7
 string str = "123";
8 reverse(str.begin(), str.end());
9 cout << str << endl; //321
```

## 5.8 CHAR

```
1 isdigit()
2 isalnum() //判斷字母 // 數字
3 isalpha()
4 islower()
5 isupper()
6 isblank() //判斷是否為空格,或者 tab 健制表符,即
     space 和 \t
 toupper()
8 tolower()
```

# 5.9 sort

```
1 priority_queue<int, vector<int>, less<int>> //大到小
     //小到大
 int arr[] = {4, 5, 8, 3, 7, 1, 2, 6, 10, 9};
5
     sort(arr, arr+10);
7 vector<int> v;
```

```
8 | sort(v.begin(), v.end()); //小到大
9 | int cmp(int a, int b){
11     return a > b;
12     }
13 | sort(v.begin(), v.end(), cmp); //大到小
```

## 5.10 struct

```
1  struct area{
2    int a, b;
3    bool operator <(const area rhs) const{
4       return a > rhs.a || ( a == a && b > rhs.b);
5    }
6    bool operator!=(const area rhs) const{
7       return a != rhs.a || b != rhs.b;
8    }
9  };
```

## 5.11 deque

```
1 deque <int> que;
2 que.push_back(10);
3 que.push_front(20);
4 que.front()
5 que.back()
6 que.pop_front()
7 que.pop_back()
8 cout << "Element at position 2 : " << que.at(2) << end1;</pre>
```

## 5.12 python template

```
1 import math
2 import operator
3
4
  try:
      while(1):
5
          listx = []
6
7
          listx.append("...")
          list_s = sorted(listx) # 小到大
9
          list_s = sorted(listx, reverse = True) #
               大到小
10
           # max(listx)
          # min(listx)
11
          # sum(listx)
12
13
          # len(listx)
          dicty = \{\}
14
          dicty[key] = "value"
15
          dicty= sorted(dicty.items()) # by key
16
          dicty= sorted(dicty.items(),
17
               key = operator.itemgetter(1)) # by value
          # EOF寫法
18
          # 階層 math.factorial(3) == 6
19
          # 絕對值 math.fabs(x)
20
          # 無條件進位 math.ceil(3.1) == 3
21
          # 無條件捨去 math.floor(2.9) == 2
22
23
          # C n 取 k math.comb(n, k)
          # math.gcd
24
          # math.lcm
25
           # e 次 x 幂 math.exp(x)
26
27 except EOFError:
28
      pass
```