Contents

```
1 int dfs(int lef, int rig){
1 Data Structure
                     if(lef + 2 == rig){
                   2
3
                      if(num[lef] > num[rig-1]){
return lef;
}
                   5
                      else{
2 Divide and Conquer
                   7
                        return rig-1;
2.1 count inversions . . . . . . . . . . . . . . . . . .
                   8
                   9
2
                     int mid = (lef + rig)/2;
                   10
                     int p1 = dfs(lef, mid);
11
12
                     int p2 = dfs(mid, rig);
13
                     if(num[p1] > num[p2]){
                      return p1;
4 Fnumerate
                     }
                   15
else{
5 Graph
                  2
                  17
                      return p2;
                   18
19 }
1.3 Trie
const int MAXL = ; // 自己填
                   const int MAXC = ;
6 Other
struct Trie {
int nex[MAXL][MAXC];
int len[MAXL];
int sz;
void init() {
memset(nex, 0, sizeof(nex));
memset(len, 0, sizeof(len));
sz = 0;
                   10
11
void insert(const string &str) {
13
                     int p = 0;
for (char c : str) {
                   14
int id = c - 'a';
if (!nex[p][id]) {
                   16
7 Function
                   17
                      nex[p][id] = ++sz;
18
19
                     p = nex[p][id];
}
                   20
21
                     len[p] = str.length();
22
9
                   23
int p = 0;
vector<int> ans;
                  9
                   26
int id = str[i] - 'a';
                   27
if (!nex[p][id]) {
                  28
return ans;
                     }
                   30
                     p = nex[p][id];
                   31
 Data Structure
                   32
                     if (len[p]) {
                   33
                      ans.pb(len[p]);
                   34
```

1.1 BIT

```
1 #define lowbit(k) (k & -k)
  void add(vector<int> &tr, int id, int val) {
    for (; id <= n; id += lowbit(id)) {</pre>
3
      tr[id] += val;
5
    }
6 }
7
  int sum(vector<int> &tr, int id) {
    int ret = 0;
    for (; id >= 1; id -= lowbit(id)) {
10
      ret += tr[id];
11
12
    return ret;
13 }
```

1.2 Segment tree

```
vector<int> find(const string &str, int i) {
       for (; i < str.length(); i++) {</pre>
35
       }
36
       return ans;
```

Divide and Conquer

count inversions

37 }

38 };

```
1 int arr[maxn], buf[maxn];
 int count_inversions(int lef, int rig){ // 逆序數對
2
      if(rig - lef <= 1) return 0;</pre>
3
      int mid = (lef + rig)/2;
```

```
5
       int ans = count_inversions(lef, mid) +
            count_inversions(mid, rig);
       int i = lef, j = mid, k = lef;
7
       while(i < mid || j < rig){</pre>
8
           if(i >= mid) buf[k] = arr[j++];
9
            else if(j >= rig) buf[k] = arr[i++];
10
           else{
11
                if(arr[i] <= arr[j]) buf[k] = arr[i++];</pre>
12
                else{
                    buf[k] = arr[j++];
13
14
                    ans += mid - i;
                }
15
           }
16
           k++;
17
18
       for(int k = lef; k < rig; ++k) arr[k] = buf[k];</pre>
19
20
       return ans;
21 | }
```

3 DP

3.1 Doubling

```
1 /* 倍增 */
2 int LOG = sqrt(N); // 2^LOG >= N
3 vector<int> arr(N);
4 vector<vector<int>> dp(N, vector<int>(LOG));
5 for(int i = 0; i < N; ++i) cin >> arr[i];
6 int L, Q, a, b;
7 cin >> L >> Q;
8 | for(int i = 0; i < N; ++i) 
      dp[i][0] = lower_bound(arr.begin(), arr.end(),
9
           arr[i] + L) - arr.begin();
      if(dp[i][0] == N || arr[i] + L < arr[dp[i][0]])</pre>
10
           dp[i][0] -= 1;
11 }
  for(int i = 1; i < LOG; ++i)</pre>
12
      for(int j = 0; j < N; ++j)
13
           dp[j][i] = dp[dp[j][i - 1]][i - 1];
14
15 for (int i = 0; i < 0; ++i){
16
      cin >> a >> b;
      a--; // 要減減是因為arr的index從0開始但題目從1開始
17
18
      if(a > b) swap(a, b);
19
20
      int ans = 0:
21
       for(int i = LOG - 1; i >= 0; --i){ // 從後往回推
           if(dp[a][i] < b){</pre>
22
23
               ans += (1 << i);
24
               a = dp[a][i];
25
26
      }
      cout << ans + 1 << endl;
27
28 }
```

3.2 Josephus

3.3 LCS

```
1 int LCS(string s1, string s2) {
2 int n1 = s1.size(), n2 = s2.size();
3 int dp[n1+1][n2+1] = {0};
4 // dp[i][j] = s1的前i個字元和s2的前j個字元
5 for (int i = 1; i <= n1; i++) {
```

3.4 LIS

```
1 int LIS(vector<int> &a) { // Longest Increasing
       Subseauence
     vector<int> s;
     for (int i = 0; i < a.size(); i++) {</pre>
3
       if (s.empty() || s.back() < a[i]) {</pre>
5
         s.push_back(a[i]);
6
       } else {
7
         *lower_bound(s.begin(), s.end(), a[i],
8
           [](int x, int y) {return x < y;}) = a[i];
9
       }
    }
10
11
    return s.size();
12 }
```

4 Enumerate

4.1 Halfcut Enumerate

```
1 /* 折半枚舉 */
  void dfs(set<long long int> &s, int depth, int T,
       long long int sum){
       if(depth >= T){
4
          s.insert(sum);
5
           return;
      }
6
      dfs(s, depth + 1, T, sum); // 取或不取的概念
7
      dfs(s, depth + 1, T, sum + A[depth]);
8
9
  }
10
  int main(){
11
       int N, T;
       set<long long int> s1, s2;
12
13
       cin >> N >> T;
       for(int i = 0; i < N; ++i) cin >> A[i];
14
       dfs(s1, 0, N/2, 0); // 折半枚舉
15
       dfs(s2, N/2, N, 0);
16
17
       long long int ans = 0;
18
      for(auto &x : s1){
           auto it = s2.upper_bound(T - x);
19
20
           long long int y = *(--it);
21
           if(x + y \le T) ans = max(ans, x + y);
22
23
       cout << ans << endl;
```

5 Graph

5.1 SPFA

```
8
       dis[s] = 0;
       inqueue[s] = true;
9
10
       cnt[s] = 1;
11
       while(!q.empty()){
12
           int now = q.front();
13
            q.pop();
           inqueue[now] = false;
14
15
            for(auto &e : G[now]){
16
17
                if(dis[e.t] > dis[now] + e.w){
                     dis[e.t] = dis[now] + e.w;
18
                     if(!inqueue[e.t]){
19
20
                         cnt[e.t]++;
                         if(cnt[e.t] > m){
21
22
                              return false;
23
                         inqueue[e.t] = true;
24
25
                         q.push(e.t);
                    }
26
27
                }
           }
28
29
30
       return true;
31 }
```

5.2 Dijkstra

```
1 struct Item{
2
       int u, dis;
3
       // 取路徑最短
       bool operator < (const Item &other) const{</pre>
5
           return dis > other.dis;
6
7 };
8 int dis[maxn];
9 vector < Edge > G[maxn];
10 void dijkstra(int s){
       for(int i = 0; i <= n; i++){</pre>
11
12
           dis[i] = inf;
13
       dis[s] = 0;
14
15
       priority_queue < Item > pq;
16
       pq.push({s, 0});
17
       while(!pq.empty()){
           // 取路徑最短的點
18
           Item now = pq.top();
19
20
           pq.pop();
21
           if(now.dis > dis[now.u]){
               continue;
22
23
           // 鬆弛更新,把與 now.u 相連的點都跑一遍
24
           for(Edge e : G[now.u]){
25
26
               if(dis[e.v] > now.dis + e.w){
27
                   dis[e.v] = now.dis + e.w;
28
                   pq.push({e.v, dis[e.v]});
29
               }
           }
30
31
       }
32 }
```

Floyd Warshall

```
1 void floyd_warshall(){
2
      for(int i = 0; i < n; i++){</pre>
3
         for(int j = 0; j < n; j++){
             G[i][j] = INF;
4
5
6
         G[i][i] = 0;
7
8
      for (int k = 0; k < n; k++){
          嘗試每一個中繼點
9
          for (int i = 0; i < n; i++){ //
              計算每一個 i 點與每一個 j 點
```

```
G[i][j] = min(G[i][j], G[i][k] +
11
                          G[k][j]);
                }
12
13
            }
       }
14
15 }
```

for (int j = 0; j < n; j++){

Disjoint set Kruskal

```
struct Edge{
      int u, v, w;
2
      // 用權重排序 由大到小
3
      bool operator < (const Edge &other) const{</pre>
          return w > other.w;
5
6
7 } edge[maxn];
  // disjoint set
8
  int find(int x){
10
    if(parent[x] < 0){
11
      return x;
    }
12
13
    else{
14
      return parent[x] = find(parent[x]);
15
16 }
  void unite(int a, int b){
17
18
    a = find(a);
19
    b = find(b);
20
    if(a != b){
21
      if(parent[a] < parent[b]){</pre>
22
23
        parent[a] += parent[b];
24
        parent[b] = a;
      }
25
26
27
        parent[b] += parent[a];
28
        parent[a] = b;
29
30
    }
  }
31
  void kruskal(){
32
      memset(parent, -1, sizeof(parent));
33
      sort(edge, edge + m);
34
      int i, j;
35
      for(i = 0, j = 0; i < n - 1 && j < m; i++){
36
          // 如果 u 和 v 的祖先相同, 則 j++
37
               (祖先相同代表會產生環 所以不要)
          while(find(edge[j].u) == find(edge[j].v)) j++;
38
          // 若部會產生環 則讓兩點之間產生橋
39
               (連接兩顆子生成樹)
40
          unite(edge[j].u, edge[j].v);
41
          j++;
42
      }
43 }
```

5.5 KM

```
1 \mid \mathbf{const} \quad \mathbf{int} \quad X = 50;
                      // X的點數,等於Y的點數
2 | const int Y = 50;
                      // Y的點數
3 int adj[X][Y];
                      // 精簡過的adjacency matrix
                      // vertex labeling
  int lx[X], ly[Y];
5 int mx[X], my[Y];
                      //
      X各點的配對對象、Y各點的配對對象
6 int q[X], *qf, *qb; // BFS queue
                      // BFS
7 int p[X];
      parent,交錯樹之偶點,指向上一個偶點
8 bool vx[X], vy[Y]; // 記錄是否在交錯樹上
9 int dy[Y], pdy[Y]; // 表格
10
  void relax(int x){ // relaxation
11
      for (int y=0; y<Y; ++y)</pre>
12
```

```
13
           if (adj[x][y] != 1e9)
                                                              85
                                                                         weight += adj[x][mx[x]];
               if (1x[x] + 1y[y] - adj[x][y] < dy[y]){
                                                              86
14
                                                                     return weight:
15
                   dy[y] = 1x[x] + 1y[y] - adj[x][y];
                                                              87 }
16
                   pdy[y] = x; //
                        記錄好是從哪個樹葉連出去的
17
               }
                                                                5.6 Dinic
18 }
19 | void reweight(){ // 調整權重、調整表格
      int d = 1e9:
                                                              1 // Maximum Flow
20
       for (int y=0; y<Y; ++y) if (!vy[y]) d = min(d,</pre>
                                                              2 const int V = 100, E = 1000;
21
                                                              3|int adj[V]; // adjacency lists,初始化為-1。
           dy[y]);
22
       for (int x=0; x<X; ++x) if ( vx[x]) lx[x] -= d;</pre>
                                                                struct Element {int b, r, next;} e[E*2];
      for (int y=0; y<Y; ++y) if ( vy[y]) ly[y] += d;</pre>
23
                                                              5
                                                                int en = 0;
      for (int y=0; y<Y; ++y) if (!vy[y]) dy[y] -= d;</pre>
24
                                                                void addedge(int a, int b, int c){
25 }
                                                                    e[en] = (Element){b, c, adj[a]}; adj[a] = en++;
26 void augment(int x, int y){ // 擴充路徑
                                                              8
                                                                     e[en] = (Element){a, 0, adj[b]}; adj[b] = en++;
      for (int ty; x != -1; x = p[x], y = ty){
27
                                                              9
                                                                }
           ty = mx[x]; my[y] = x; mx[x] = y;
28
                                                              10 int d[V];
                                                                                 // 最短距離
29
                                                              11
                                                                bool visit[V]; // BFS/DFS visit record
30 }
                                                              12 int q[V];
                                                                                 // queue
                                                              13 int BFS(int s, int t){ // 計算最短路徑,求出容許圖
31 | bool branch1(){ // 延展交錯樹:使用既有的等邊
32
      while (qf < qb)</pre>
                                                                    memset(d, 0x7f, sizeof(d));
33
           for (int x=*qf++, y=0; y<Y; ++y)</pre>
                                                              15
                                                                    memset(visit, false, sizeof(visit));
34
               if (!vy[y] && lx[x] + ly[y] == adj[x][y]){
                                                                     int qn = 0;
                                                              16
                   vy[y] = true;
35
                                                              17
                                                                    d[s] = 0;
36
                   if (my[y] == -1){
                                                                    visit[s] = true;
                                                              18
37
                        augment(x, y);
                                                              19
                                                                    q[qn++] = s;
38
                        return true;
                                                              20
39
                   }
                                                              21
                                                                     for (int qf=0; qf<qn; ++qf){</pre>
                   int z = my[y];
40
                                                              22
                                                                         int a = q[qf];
                   *qb++ = z; p[z] = x; vx[z] = true;
41
                                                                         for (int i = adj[a]; i != -1; i = e[i].next){
                                                              23
                        relax(z);
                                                              24
                                                                             int b = e[i].b;
                                                                             if (e[i].r > 0 && !visit[b]){
42
                                                              25
43
       return false;
                                                                                 d[b] = d[a] + 1;
                                                              26
44 }
                                                              27
                                                                                 visit[b] = true;
                                                                                 q[qn++] = b;
45 bool branch2(){ // 延展交錯樹:使用新添的等邊
                                                              28
       for (int y=0; y<Y; ++y){</pre>
                                                              29
                                                                                 if (b == t) return d[t];
46
                                                                             }
                                                              30
47
           if (!vy[y] && dy[y] == 0){
48
               vy[y] = true;
                                                              31
                                                                         }
               if (my[y] == -1){
49
                                                              32
                                                                    }
                   augment(pdy[y], y);
                                                              33
                                                                     return V;
50
51
                                                              34 }
                   return true;
               }
                                                              35
                                                                int DFS(int a, int df, int s, int t){ //
52
53
               int z = my[y];
                                                                     求出一條最短擴充路徑,並擴充流量
               *qb++ = z; p[z] = pdy[y]; vx[z] = true;
54
                                                                     if (a == t) return df;
                                                              36
                   relax(z);
                                                              37
                                                                     if (visit[a]) return 0;
55
           }
                                                              38
                                                                     visit[a] = true;
56
      }
                                                                     for (int i = adj[a]; i != -1; i = e[i].next){
                                                              39
      return false;
                                                                         int b = e[i].b;
57
                                                              40
58 }
                                                              41
                                                                         if (e[i].r > 0 && d[a] + 1 == d[b]){
59 int Hungarian(){
                                                                             int f = DFS(b, min(df, e[i].r), s, t);
                                                              42
                                                                             if (f){
60
      // 初始化vertex labeling
                                                              43
61
      // memset(lx, 0, sizeof(lx)); // 任意值皆可
                                                              44
                                                                                 e[i].r -= f;
                                                              45
                                                                                 e[i^1].r += f;
62
      memset(ly, 0, sizeof(ly));
63
      for (int x=0; x<X; ++x)</pre>
                                                              46
                                                                                 return f;
                                                                             }
                                                              47
64
           for (int y=0; y<Y; ++y)</pre>
                                                                         }
               lx[x] = max(lx[x], adj[x][y]);
                                                              48
65
                                                                    }
                                                              49
66
                                                              50
                                                                     return 0;
       // X側每一個點,分別建立等邊交錯樹。
67
                                                              51 }
68
      memset(mx, -1, sizeof(mx));
                                                                int dinitz(int s, int t){
                                                              52
69
      memset(my, -1, sizeof(my));
                                                              53
                                                                     int flow = 0;
70
       for (int x=0; x<X; ++x){</pre>
                                                              54
                                                                     while (BFS(s, t) < V)
           memset(vx, false, sizeof(vx));
71
                                                              55
                                                                         while (true){
           memset(vy, false, sizeof(vy));
72
                                                              56
                                                                             memset(visit, false, sizeof(visit));
73
           memset(dy, 0x7f, sizeof(dy));
                                                                             int f = DFS(s, 1e9, s, t);
                                                              57
74
           qf = qb = q;
                                                                             if (!f) break;
                                                              58
75
           *qb++ = x; p[x] = -1; vx[x] = true; relax(x);
                                                              59
                                                                             flow += f:
76
           while (true){
                                                              60
                                                                         }
77
               if (branch1()) break;
                                                                     return flow;
                                                              61
78
               reweight();
                                                              62 3
79
               if (branch2()) break;
           }
80
81
      }
82
      // 計算最大權完美匹配的權重
                                                                      Bipatirate
83
      int weight = 0;
      for (int x=0; x<X; ++x)</pre>
```

 $1 \mid const int maxn = 300 + 5;$

84

```
2 int n, color[maxn];
  vector<vector<int>> v(maxn);
  bool dfs(int s){
       for(auto it : v[s]){
6
           if(color[it] == -1){
                color[it] = 3 - color[s];
7
                if(!dfs(it)){
8
9
                     return false:
10
11
12
           if(color[s] == color[it]){
13
                return false:
           }
14
15
       }
16
       return true;
17 }
18 void isBipatirate(){
19
       bool flag = true;
       for(int i = 1; i <= n; ++i){</pre>
20
21
            if(color[i] == -1){
                color[i] = 1;
22
23
                flag &= dfs(i);
           }
24
25
26
       if(flag){
           cout << "YES" << endl;</pre>
27
28
29
       else{
30
           cout << "NO" << endl;
31
32 }
33 int main(){
34
       while(cin >> n && n){
35
            for(int i = 1; i <= n; ++i) v[i].clear();</pre>
36
            memset(color, -1, sizeof(color));
37
           int a. b:
38
            while(cin >> a >> b && (a || b)){
                v[a].emplace_back(b);
39
40
                v[b].emplace_back(a);
41
           }
42
           isBipatirate();
43
       }
44 }
```

5.8 Hungarian algorithm

```
1 const int maxn = 500+5;
2 int t, N, bn, gn, match[maxn];
3 bool visited[maxn];
  vector<vector<int>> G(maxn);
  struct People{
       int h;
6
7
       string music, sport;
8
       People(){}
9
       People(int h, string music, string sport){
10
           this ->h = h;
11
           this->music = music;
12
           this->sport = sport;
13
14 }lef[maxn], rig[maxn];
15 bool check(People boy, People girl){
16
       if(abs(boy.h - girl.h) <= 40 && boy.music ==</pre>
           girl.music && boy.sport != girl.sport) return
           true:
17
       return false;
18 }
19 bool dfs(int s){
       for(int i = 0; i < G[s].size(); ++i){</pre>
20
21
           int v = G[s][i];
22
           if(visited[v]) continue;
           visited[v] = true;
23
           if(match[v] == -1 || dfs(match[v])){
24
25
                match[v] = s;
26
                return true;
27
           }
       }
28
```

```
29
       return false;
30 }
  int Hungarian(){
31
32
       int cnt = 0;
33
       memset(match, -1, sizeof(match));
       for(int i = 0; i < bn; ++i){</pre>
34
35
           memset(visited, false, sizeof(visited));
36
           if(dfs(i)) cnt++;
37
       }
38
       return cnt;
39 }
40 int main(){
41
       cin >> t;
       while(t--){
42
43
           cin >> N;
           bn = 0, gn = 0;
44
45
            for(int i = 0; i <= N; ++i) G[i].clear();</pre>
46
            int h;
47
            string sex, music, sport;
48
            for(int i = 0; i < N; ++i){</pre>
                cin >> h >> sex >> music >> sport;
49
50
                if(sex == "M") lef[bn++] = People(h,
                     music, sport);
51
                else rig[gn++] = People(h, music, sport);
52
           for(int i = 0; i < bn; ++i){</pre>
53
                for(int j = 0; j < gn; ++j)
55
                     if(check(lef[i], rig[j]))
                         G[i].emplace_back(j);
56
           cout << N - Hungarian() << endl;</pre>
57
58
       }
59 }
```

6 Other

6.1 Bubble Sort Expect Value

```
1 /* 期望值算法:
2| 擲一枚公平的六面骰子, 其每次「點數」的期望值是 3.5
|E(x)| = 1 * 1/6 + 2 * 1/6 + 3 * 1/6 + 4 * 1/6 + 5 *
      1/6 + 6 * 1/6
  = (1 + 2 + 3 + 4 + 5 + 6)/6 = 3.5
5 bubble sort 每兩兩之間交換機率是 1/2
  總共會做 C(n, 2) 次
6
  E(x) = C(n, 2) * 1/2 = (n * (n - 1))/2 * 1/2 */
8 int t, ca = 1;
9
  cin >> t;
  while(t--){
10
      long long int n;
11
12
      cin >> n;
      cout << "Case " << ca++ << ": ";
13
      // 如果 (n * (n - 1)) 可以被 4 整除
14
          代表最後答案會是整數,否則會是分數
15
      if((n * (n - 1)) % 4){
         cout << ( (n * (n - 1)) / 2 ) << "/2"<< endl:
16
17
     }
18
     else{
19
         cout << ((n * (n - 1)) / 2) / 2 << endl;
20
     }
21 3
```

6.2 ORXOR

```
1 /* 如何切區段,之所以要1<<n是為了可以跑000~111
2 i = 0, binary i = 000
3 0 : 1 5 7
4 i = 1, binary i = 001
5 1 : 1 5 7
6 i = 2, binary i = 010, 看得出來切了一刀
7 2 : 1 | 5 7
```

39

40

41

42

43

44

45

46

47

48 }

}

```
8 \mid i = 3, binary i = 011
9 3 : 1 | 5 7
10 | i = 4 , binary i = 100 , 為了要切在 index = 2 , 所以才要 1 << j
11 4 : 1 5 | 7
|12|i = 5, binary i = 101
13 5 : 1 5 | 7
|14|i = 6, binary i = 110
15 6 : 1 | 5 | 7
|i| = 7, binary |i| = 111
17 7 : 1 | 5 | 7
18 可以觀察出來,前兩位 bit 是 1 時代表的意義是切在哪裡*/
19 int n:
20 int num[20+7];
21 memset(num, 0, sizeof(num));
22 cin >> n;
23 for(int i = 1; i <= n; i++){
       cin >> num[i];
24
25 }
26 int mini = 2147483647; // 不知道為甚麼只有 2147483647
       給過
27 // 1 << n = n * 2
28 | for(int i = 0; i < (1 << n); i++){
       int XOR = 0, OR = 0;
29
30
       for(int j = 1; j <= n; j++){</pre>
           OR |= num[j];
31
32
           if((i & (1 << j))){</pre>
               XOR ^= OR;
33
34
               OR = 0;
35
           }
      }
36
37
       XOR ^= OR;
       mini = min(mini, XOR);
38
39 }
40 cout << mini << endl;
```

6.4 X drawing

```
1 long long int n, a, b, p, q, r, s;
2 cin >> n >> a >> b;
  cin >> p >> q >> r >> s;
  for(long long int i = p; i <= q; i++){</pre>
       for(long long int j = r; j <= s; j++){</pre>
           if(abs(i - a) == abs(j - b)){
6
                cout << '#':
           }
8
9
           else{
10
                cout << '.';
11
12
       }
       cout << endl;</pre>
13
14
```

for(int i = 0; i <= N; i++){

cout << "Case " << ca++ << ": " << fixed <<

setprecision(10) << dfs(num) << endl;</pre>

dp[i] = -1;

cin >> num;

Linear_Sieve();

cin >> t;

while(t--){

6.3 Race to 1

37

int ca = 1;

```
1 const int N = 1000000;
2 bool sieve[N+5];
3 vector<int> pri;
4 double dp[N+5];
5 void Linear_Sieve(){ // 線性篩
       for (int i = 2; i < N; i++){
6
7
           if (!sieve[i])
8
               pri.push_back(i);
9
           for (int p: pri){
               if (i * p \ge N){
10
11
                    break;
12
               sieve[i * p] = true;
13
14
               if (i % p == 0){
15
                    break;
16
           }
17
18
       }
19 }
20 double dfs(int n){
21
       if(dp[n] != -1) return dp[n];
22
       dp[n] = 0;
23
       if(n == 1) return dp[n];
24
       int total = 0, prime = 0;
25
       for(int i = 0; i < pri.size() && pri[i] <= n;</pre>
           i++){
           total++:
26
           if(n % pri[i]) continue;
27
28
           prime++;
           dp[n] += dfs(n/pri[i]);
29
30
31
       dp[n] = (dp[n] + total)/prime; // 算期望值
32
       return dp[n];
33 }
34 int main(){
35
       int t;
36
       int num;
```

6.5 Big Mod

```
1 ' ' '
2
  Mod
  pow(x, y, z) = x^y % z
5 # python 如何讀取直到 EOF 用 try except
  try:
7
      while True:
          # input().split() 用空格切開讀取一整行
8
          # map (型態, input().split()) 才能把值全讀成
9
          B, P, M = map(int, input().split())
10
11
          print(pow(B, P, M))
  except EOFError:
12
      exit
13
```

6.6 Crested Ibis vs Monster

```
1 /* dp 背包 - 重量/價值/可重複使用
2 因為這題可以重複使用同一條魔法
3| 所以可以這樣 dp*/
4 int h, n;
5
  cin >> h >> n;
  for(int i = 1; i <= n; i++){</pre>
      cin >> a[i] >> b[i];
8 }
  memset(dp, 0x3f3f3f3f, sizeof(dp));
9
10
  dp[0][0] = 0;
  for(int i = 1; i <= n; i++){</pre>
11
      for(int j = 0; j <= h; j++){</pre>
12
13
          dp[i][j] = min(dp[i-1][j], dp[i][max(0, j -
               a[i])] + b[i]);
14
15 }
16 cout << dp[n][h] << endl;</pre>
```

6.7 dpd Knapsack 1

```
1 // dp 背包 - 時間/數量/價值 - 第幾分鐘符合
2 int N, W;
3 cin >> N >> W;
4 int w[100000+5];
5 int v[100000+5];
6 | for(int i = 0; i < N; i++) {
7
      cin >> w[i] >> v[i];
8 }
9 long long int dp[100000+5];
10 memset(dp, 0, sizeof(dp));
11 for(int i = 0; i < N; i++){
12
      for(int j = W; j >= w[i]; j--){
          dp[j] = max(dp[j], dp[j - w[i]] + v[i]);
13
14
15 }
16 cout << dp[W] << endl;</pre>
```

6.8 Fraction Floor Sum

```
1 / * [N/i] == M
|2| -> M <= N/i < M + 1
3 \rightarrow N/(M+1) < i <= N/M */
4 long long int N;
5 cin >> N;
6 long long int ans = 0;
  for(long long int i = 1; i <= N; i++){</pre>
7
      long long int M = N / i;
9
      long long int n = N / M;
10
      // 總共會有 n - i 個的 [N/i] 值都是 M
      ans += (n - i + 1) * M;
11
      // 更新跳過 以免重複計算
12
13
      i = n;
14 }
15 cout << ans << endl;
```

6.9 Homer Simpson

```
1 // dp 背包 - 時間/數量 - 漢堡
2 int m, n, t;
  while(cin >> m >> n >> t){
       int dp[10000+5];
       memset(dp, -1, sizeof(dp));
       dp[0] = 0;
6
7
       for(int i = m; i <= t; i++){</pre>
          if(dp[i - m] != -1){
8
               dp[i] = max(dp[i], dp[i - m] + 1);
           }
10
11
12
       for(int i = n; i <= t; i++){</pre>
           if(dp[i - n] != -1){
13
               dp[i] = max(dp[i], dp[i - n] + 1);
15
16
       if(dp[t] == -1){ // 時間無法剛好吃滿的時候
17
18
           for(int i = t; i >= 0; i--){
               if(dp[i] != -1){
19
                    cout << dp[i] << " " << t - i << endl;
20
21
22
23
           }
24
25
           cout << dp[t] << endl;</pre>
26
27
28 }
```

6.10 Let Me Count The Ways

```
1 // dp - 時間/數量 - 硬幣排序
2 long long int n, dp[30000+5];
  int coin[] = {1, 5, 10, 25, 50};
  memset(dp, 0, sizeof(dp));
5
  dp[0] = 1;
  for(int i = 0; i < 5; i++){</pre>
       for(int j = coin[i]; j < 30000+5; j++){</pre>
           if(dp[j - coin[i]] != -1){
               dp[j] += dp[j - coin[i]];
9
10
11
       }
12 }
13
  while(cin >> n){
       if(dp[n] == 1){
14
15
           cout << "There is only " << dp[n] << " way to</pre>
                produce " << n << " cents change." <<
16
       }
17
       else{
           cout << "There are " << dp[n] << " ways to</pre>
18
                produce " << n << " cents change." <<</pre>
                end1:
       }
19
20 }
```

6.11 Luggage

```
1 // dp 背包 - 重量/是否成立
2 int t;
3 cin >> t;
  cin.ignore();
 5
  while(t--){
       string str:
 7
       getline(cin , str);
       vector<int> v;
8
 9
       stringstream ss;
       int num, cnt = 0, sum = 0;;
10
       bool dp[4000+5];
11
12
       memset(dp, false, sizeof(dp));
13
       ss << str;
14
       while(ss >> num){
15
           cnt++;
           sum += num;
16
17
           v.emplace_back(num);
18
19
       if(sum & 1){
           cout << "NO" << endl;
20
           continue;
21
22
23
       dp[0] = true;
24
       for(int i = 0; i < v.size(); i++){</pre>
           for(int j = sum; j >= v[i]; j--){
25
                if(dp[j - v[i]]){
                    dp[j] = true;
27
28
           }
29
30
       }
31
       cout << (dp[sum/2] ? "YES" : "NO") << endl;</pre>
32 }
```

6.12 Number of Pairs

```
12
       cin >> n >> 1 >> r;
                                                                    27
                                                                           dp[1][1] = 1;
                                                                           for(int i = 1; i <= r; i++){</pre>
13
       int num:
                                                                    28
                                                                                for(int j = 1; j <= c; j++){</pre>
       for(int i = 0; i < n; i++){</pre>
                                                                    29
14
15
            cin >> num;
                                                                    30
                                                                                    if(mp[i][j]){
16
            v.emplace_back(num);
                                                                    31
                                                                                         continue;
17
                                                                    32
                                                                                    }
       sort(v.begin(), v.end());
                                                                    33
                                                                                    if(i > 1){
18
19
       long long int ans = 0;
                                                                    34
                                                                                         dp[i][j] += dp[i-1][j];
       for(int i = 0; i < n; i++){</pre>
                                                                    35
20
            ans += (upper_bound(v.begin() + i + 1,
                                                                                    if(j > 1){
21
                                                                    36
                 v.end(), r - v[i])
                                                                    37
                                                                                         dp[i][j] += dp[i][j-1];
                 lower_bound(v.begin() + i + 1, v.end(), 1
                                                                    38
                 - v[i]));
                                                                    39
                                                                                }
                                                                    40
22
23
       cout << ans << endl;</pre>
                                                                    41
                                                                           cout << dp[r][c] << endl;</pre>
                                                                    42 }
24 }
```

6.13 SuperSale

```
1 // dp 背包 - 重量/價值/不可重複使用 - 舉重
2 int t;
3 cin >> t;
4 while(t--){
       int n;
       cin >> n;
6
       for(int i = 0; i < n; i++){</pre>
           cin >> edge[i].p >> edge[i].w;
8
9
10
       int g, total = 0;
11
       cin >> g;
       for(int i = 0; i < g; i++){</pre>
12
           int pw, dp[30+5];
13
           cin >> pw;
14
15
           memset(dp, 0, sizeof(dp));
           for(int j = 0; j < n; j++){
16
17
                for(int k = pw; k >= edge[j].w; k--){
                    dp[k] = max(dp[k], dp[k - edge[j].w]
18
                        + edge[j].p);
19
               }
           }
20
21
           total += dp[pw];
22
       cout << total << endl;</pre>
23
24 }
```

6.14 Walking on the Safe Side

```
1 // dp - 地圖更新
2 int t;
3 bool space = false;
4 cin >> t;
  while(t--){
       if(space){
6
7
           cout << endl;</pre>
8
       }
9
       else{
10
           space = true;
       }
11
12
       int r, c;
13
       cin >> r >> c;
       cin.ignore();
14
15
       memset(mp, false, sizeof(mp));
       memset(dp, 0, sizeof(dp));
16
17
       string str;
       for(int i = 0; i < r; i++){</pre>
18
19
           getline(cin, str);
20
            int n, num;
           stringstream ss(str);
21
            ss >> n;
22
23
           while(ss >> num){
24
                mp[n][num] = true;
25
           }
       }
26
```

7 Function

7.1 strstr

```
1 #include <stdio.h>
  #include <string.h>
4
  int main(){
5
  char * c;
  char str1[1005], str2[1005];
6
  scanf("%s %s", str1, str2);
8
  c = strstr(str1, str2);
  if (c != NULL){
9
      printf("Yes\n");
11 }
  else printf("No\n");
13 }
14 // Input : Hello eLl
15 // Output : No
```

7.2 substr

```
1 int main(){
2     string str; //abcdef
3     cin >> str;
4     string tmp;
5     tmp = str.substr(0, 2); //ab
6     str = str.substr(2); //cdef
7     cout << tmp << " " << str;
8     return 0;
9 }</pre>
```

7.3 map set

```
1 | .begin( ) // Return iterator to beginning
2 .end( ) // Return iterator to end
3 | . empty( ) // 檢查是否為空
4 . size( ) // 回傳大小
5 mp.insert(pair<char,int>('a',100))
6 st.insert(100) // 插入key \ value
7 .erase() // 刪掉指定key和他的value
8 .clear( ) // 清空整個 map
  m.find( )
10 cout << "a => " << mymap.find('a')->second << endl;</pre>
      // 找出 map 裡 key
11
          有沒有在裡面,如果有的話會回傳元素所在的iterator,否則何
12 s.count() // 返回某個值元素在 set 的 個數
13 while( !mymap.empty()){
      cout << mymap.begin()->first << " => " <<</pre>
14
          mymap.begin()->second << endl;</pre>
15
      mymap.erase(mymap.begin());
16 }
```

```
17 | for (auto it = mymap.begin(); it != mymap.end(); ++it)
18 | cout << it->first << " => " << it->second << endl;
```

7.4 vector

```
1 | v.erase(v.begin() + 5) //拿掉第六個數
2 | v.erase(v.begin(), v.begin() + 3); //拿掉前三個數
```

7.5 setprecision

```
1 // 將數字的小數部分設定為固定長度
2 cnt = 3.5555;
3 cout << fixed << setprecision(3) << cnt ;
4 // output : 3.555
```

7.6 GCD LCM

```
int gcd(int a, int b){
    return (b == 0 ? a : gcd(b, a % b));
}
int lcm(int a, int b){
    return a * b / gcd(a, b);
}

/* 輾轉相除法 - 求兩數是否互質
如果兩數互質 最終結果其中一方為0時 另一方必為1
若兩數有公因數 最終結果其中一方為0時 另一方必不為1 */
while ( ( num1 %= num2 ) != 0 && ( num2 %= num1 ) !=
    0 );
```

7.7 reverse

```
1 | int a[10] = {0, 1, 2, 3, 4, 5, 6, 7, 8, 9};
2 | reverse(a, a+5) // 轉換0~5
3 | vector<int> v;
5 | reverse(v.begin(), v.end());
6 | string str = "123";
8 | reverse(str.begin(), str.end());
9 | cout << str << endl; //321
```

7.8 CHAR

7.9 sort

```
8 sort(v.begin(), v.end()); //小到大
9
10 int cmp(int a, int b){
11    return a > b;
12 }
13 sort(v.begin(), v.end(), cmp); //大到小
```

7.10 struct

```
1  struct area{
2    int a, b;
3    bool operator < (const area rhs) const{
4        return a > rhs.a || ( a == a && b > rhs.b);
5    }
6    bool operator! = (const area rhs) const{
7        return a != rhs.a || b != rhs.b;
8    }
9  };
```

7.11 deque

```
1 deque <int> que;
2 que.push_back(10);
3 que.push_front(20);
4 que.front()
5 que.back()
6 que.pop_front()
7 que.pop_back()
8 cout << "Element at position 2 : " << que.at(2) << endl;</pre>
```

7.12 python template

```
1 import math
  import operator
3
4
  try:
5
       while(1):
           listx = []
6
           listx.append("...")
           list_s = sorted(listx) # 小到大
           list_s = sorted(listx, reverse = True) #
9
               大到小
           # max(listx)
10
11
           # min(listx)
           # sum(listx)
12
13
           # len(listx)
           dicty = \{\}
14
15
           dicty[key] = "value"
           dicty = sorted(dicty.items()) # by key
16
17
           dicty= sorted(dicty.items(),
               key=operator.itemgetter(1)) # by value
           # EOF 寫法
18
19
           # 階層 math.factorial(3) == 6
           # 絕對值 math.fabs(x)
20
           # 無條件進位 math.ceil(3.1) == 3
21
           # 無條件捨去 math.floor(2.9) == 2
22
23
           # C n 取 k math.comb(n, k)
          # math.gcd
24
25
           # math.lcm
           # e 次 x 幂 math.exp(x)
26
27
  except EOFError:
28
      pass
```