

Measuring the properties of reionised bubbles with resolved Lyman alpha spectra

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ABSTRACT

Identifying and characterising reionised bubbles enables us to track both their size distribution, which depends on the primary ionising sources, and the relationship between reionisation and galaxy evolution. We demonstrate that spectrally resolved $z \gtrsim 6$ Lyman-alpha ($\text{Ly}\alpha$) emission can constrain properties of reionised regions. Specifically, the distance from a source to a neutral region sets the minimum observable $\text{Ly}\alpha$ velocity offset from systemic. Detection of flux on the blue side of the $\text{Ly}\alpha$ resonance implies the source resides in a large, sufficiently ionised region that photons can escape without significant resonant absorption, and thus constrains both the sizes of and the residual neutral fractions within ionised bubbles. We estimate the extent of the region around galaxies which is optically thin to blue $\text{Ly}\alpha$ photons, analogous to quasar proximity zones, as a function of the source’s ionising photon output and surrounding gas density. This optically thin region is typically $\lesssim 0.3$ pMpc in radius (allowing transmission of flux $\gtrsim -250 \text{ km s}^{-1}$), $\lesssim 10\%$ of the distance to the neutral region. In a proof-of-concept, we demonstrate the $z \approx 6.6$ galaxy COLA1 – with a blue $\text{Ly}\alpha$ peak – likely resides in an ionised region > 0.7 pMpc, with residual neutral fraction $< 10^{-5.5}$. To ionise its own proximity zone we infer COLA1 has a steep UV slope ($\beta < -2.27$), a high ionising photon escape fraction ($f_{\text{esc}} > 0.48$) and moderate line-of-sight gas density ($< 2.61 \times$ the cosmic mean).

Key words: dark ages, reionisation, first stars – galaxies: high-redshift

1 INTRODUCTION

Understanding the process of Hydrogen reionisation is one of the frontiers of astronomy. It occurred neither homogeneously nor instantaneously, as ionising photons propagating from nascent galaxies reionised the most overdense regions first, carving out ionised ‘bubbles’ within the then neutral Universe, gradually reionising the entire intergalactic medium (IGM). Measuring the timeline and topology of reionisation, i.e., studying the redshift evolution and spatial distribution of these ionised regions, is key to understanding how reionisation occurred (e.g., Furlanetto et al. 2004; McQuinn et al. 2007; Mesinger 2016).

A key question is what drove reionisation, that is, where did the ionising photons originate from? Identifying reionised or neutral regions of the IGM not only characterises the topology of reionisation but enables us to address this question by comparing the properties of observed

galaxies in those regions to the local ionisation state (e.g., Beardsley et al. 2015). Regions which reionise early are likely the first overdensities where galaxy formation is accelerated, thus identifying those regions helps to identify the first generations of galaxies.

Mapping reionised bubbles and measuring their size distribution is a goal of future 21 cm intensity experiments. This requires spatial resolution capable of discerning ionised hydrogen gas on scales of < 1 proper Mpc (e.g., Geil et al. 2017). However, sensitivity to these smallest scales is still an observational challenge: it requires large baseline radio telescopes to resolve HI regions (e.g., SKA-low, Koopmans et al. 2015), and detailed spectroscopic follow-up of the galaxies within HII regions to determine their ionising properties. However, estimates of bubble sizes on small scales are currently feasible with Lyman-alpha ($\text{Ly}\alpha$, rest wavelength 1216 Å) spectroscopy of high redshift sources.

Due to its high cross-section for absorption by neutral hydrogen, $\text{Ly}\alpha$ is a sensitive probe of neutral gas. Neutral hydrogen affects both the strength and lineshape of $\text{Ly}\alpha$ (see, e.g., Dijkstra 2014, for a review). With the advent of

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sensitive near-IR spectroscopy, Ly α emission from galaxies and quasars at $z > 6$ has been a particularly powerful probe of reionisation (e.g., Malhotra & Rhoads 2006; Fan et al. 2006; Dijkstra et al. 2011; Treu et al. 2013; Mesinger et al. 2015; Davies et al. 2018; Mason et al. 2018a; Greig et al. 2019). In recent years, the declining flux distribution of Ly α emission from galaxies at $z \gtrsim 6$ has been used to measure the average fraction of the IGM which is neutral at a given redshift (Schenker et al. 2014; Mason et al. 2018a, 2019; Hoag et al. 2019; Whitler et al. 2019).

The lineshape of Ly α also encodes information about neutral hydrogen structures the photons encountered along their path. Within or in close proximity to the emitting galaxy the Ly α spectrum is shaped by resonant scattering with H I that is not necessarily along the line-of-sight (Eide et al. 2018), and typically produces double-peaked emission line profiles due to the high optical depth at line centre (e.g., Neufeld 1990). However, at larger distances, when the probability of scattering back into the line-of-sight becomes negligible, the impact of intervening H I can be treated more simply as absorption. The smooth damping wing, due to $n_{\text{H I}} \gtrsim 10^{-6} \text{ cm}^3$ gas that can be at large distances, is commonly interpreted as a signature of reionisation (e.g., Miralda-Escude 1998). In this case, the optical depth due to damping wing absorption is a function of the distance to the nearest neutral patch and thus could be used to recover the size of ionised bubbles (Malhotra & Rhoads 2006).

Due to the short recombination time at $z \gtrsim 6$ (\sim the age of the universe) even within ‘ionised’ bubbles there can be significant residual neutral gas. The amount of neutral hydrogen depends on the local ionisation field and can lead to resonant absorption on the blue side of the Ly α resonance (e.g., Gunn & Peterson 1965; Zheng et al. 2010; Laursen et al. 2011) – which makes the detection of blue Ly α peaks towards higher redshift increasingly unlikely. In a number of rare sightlines, however, blue Ly α flux has been observed at $z \gtrsim 6$ (Matthee et al. 2018; Songaila et al. 2018; Bosman et al. 2019), implying a low resonant optical depth and thus low residual neutral fraction in reionised regions. In these cases it may be possible to directly measure the properties of individual ionised bubbles.

Here, we demonstrate that $z > 6$ Ly α emission line-shapes encode information about the ionised bubbles their host galaxies reside in. While previous works have shown that Ly α can be visible early in the epoch of reionisation if galaxies reside in ionised bubbles (Haiman 2002; Mason et al. 2018b) we show here that spectroscopic measurements of Ly α emitters enable us to calculate the minimum size of the ionised bubble such that Ly α at a given frequency offset is visible to us. Furthermore, we demonstrate that blue-peaked Ly α lines observed at $z \gtrsim 6$ can be used to constrain the residual neutral gas remaining in reionised bubbles. As a proof-of-concept, we investigate the necessary physical conditions for observing the double-peaked Ly α emitted COLA1 (Hu et al. 2016; Matthee et al. 2018).

This paper is organised as follows: we describe our model for the Ly α optical depth in Section 2 and present our results in Section 3. We discuss our results in Section 4 and present conclusions in Section 5. We use the Planck Collaboration et al. (2015) cosmology: $(\Omega_{\Lambda}, \Omega_{\text{m}}, \Omega_{\text{b}}, n, \sigma_8, H_0) = (0.69, 0.31, 0.048, 0.97, 0.81, 68 \text{ km s}^{-1} \text{ Mpc}^{-1})$. Magnitudes

are in the AB system. Distances, volumes, and densities are proper unless otherwise stated.

2 MODEL

In this section, we describe the two components of our model: the Ly α optical depth as a function of the distance from a galaxy (§ 2.1) and the properties of ionised bubbles (§ 2.2).

2.1 Lyman-alpha optical depth

The Ly α optical depth through hydrogen gas for photon observed at $\lambda_{\text{obs}} = \lambda_{\text{em}}(1 + z_s)$ to a source at redshift z_s , observed at z_{obs} , is given by:

$$\tau_{\alpha}(\lambda_{\text{obs}}) = \int_{z_{\text{obs}}}^{z_s} dz \, c \frac{dt}{dz} x_{\text{H I}}(z) n_{\text{H}}(z) \sigma_{\alpha} \left(\frac{\lambda_{\text{obs}}}{1 + z}, T \right) \quad (1)$$

where n_{H} is the total number density of hydrogen and $x_{\text{H I}}$ is the fraction of hydrogen which is neutral. $\sigma_{\alpha}(\lambda, T)$ is the Ly α scattering cross-section through an ensemble of hydrogen atoms with a Maxwell-Boltzmann velocity distribution, usually expressed as function of the dimensionless frequency $x = (\nu - \nu_{\alpha})/\Delta\nu_{\text{b}}$:

$$\sigma_{\alpha}(x, T) = \sigma_0 \times \phi(x), \quad (2)$$

$$\sigma_0 = \frac{1}{\Delta\nu_{\text{b}} \sqrt{\pi}} \frac{f_{\alpha} \pi e^2}{m_e c} \approx 5.9 \times 10^{-14} \left(\frac{T}{10^4 \text{ K}} \right)^{-1/2} \text{ cm}^2$$

where $f_{\alpha} = 0.416$ is the Ly α oscillator strength, m_e and e are the mass and charge of an electron, and $\phi(x)$ is the Voigt function:

$$\phi(x) = \frac{a_{\text{V}}}{\pi} \int_{-\infty}^{\infty} dy \frac{e^{-y^2}}{(y - x)^2 + a_{\text{V}}^2}. \quad (3)$$

Here, $\nu_{\alpha} \approx 2.46 \times 10^{15} \text{ Hz}$ is the resonant frequency of Ly α , at wavelength $\lambda_{\alpha} \approx 1216 \text{ \AA}$, $\Delta\nu_{\text{b}} = \nu_{\alpha} \sqrt{2k_{\text{B}}T/m_{\text{p}}c^2} \equiv \nu_{\alpha} v_{\text{th}}/c$ is the thermally broadened frequency, and the Voigt parameter $a_{\text{V}} \approx 4.7 \times 10^{-4} (T/10^4 \text{ K})^{-1/2}$. Equation (3) is normalised such that $\int dx \phi(x) = 1$. The cross-section is tightly peaked around the core of the line, but has damping wings which extend out to $> 1000 \text{ km s}^{-1}$ from the line centre (e.g., Dijkstra 2014). We use the approximation for $\phi(x)$ given by Tasitsiomi (2006).

Approximating Equation (3) as a Dirac delta function, and assuming constant $x_{\text{H I}}$, we obtain the Gunn & Peterson (1965) optical depth for blue photons emitted from a source at z_s :

$$\tau_{\text{GP}}(z_s) = \frac{f_{\alpha} \pi e^2}{m_e \nu_{\alpha}} \frac{x_{\text{H I}} n_{\text{H}}(z_s)}{H(z_s)} \approx 4.7 \times 10^5 x_{\text{H I}} \left(\frac{n_{\text{H}}}{\bar{n}_{\text{H}}} \right) \left(\frac{1 + z_s}{8} \right)^{3/2}. \quad (4)$$

We assume that the source galaxy resides inside an ionised region embedded in a neutral homogeneous intergalactic medium at a distance R_{ion} . This is representative of reionisation’s early pre-overlap phases when ionised bubbles grow around sources of ionising photons. However, the assumption of an isolated bubble breaks down as reionisation progresses, meaning our method provides only a lower limit on the bubble size.

We construct the optical depth to a source galaxy by

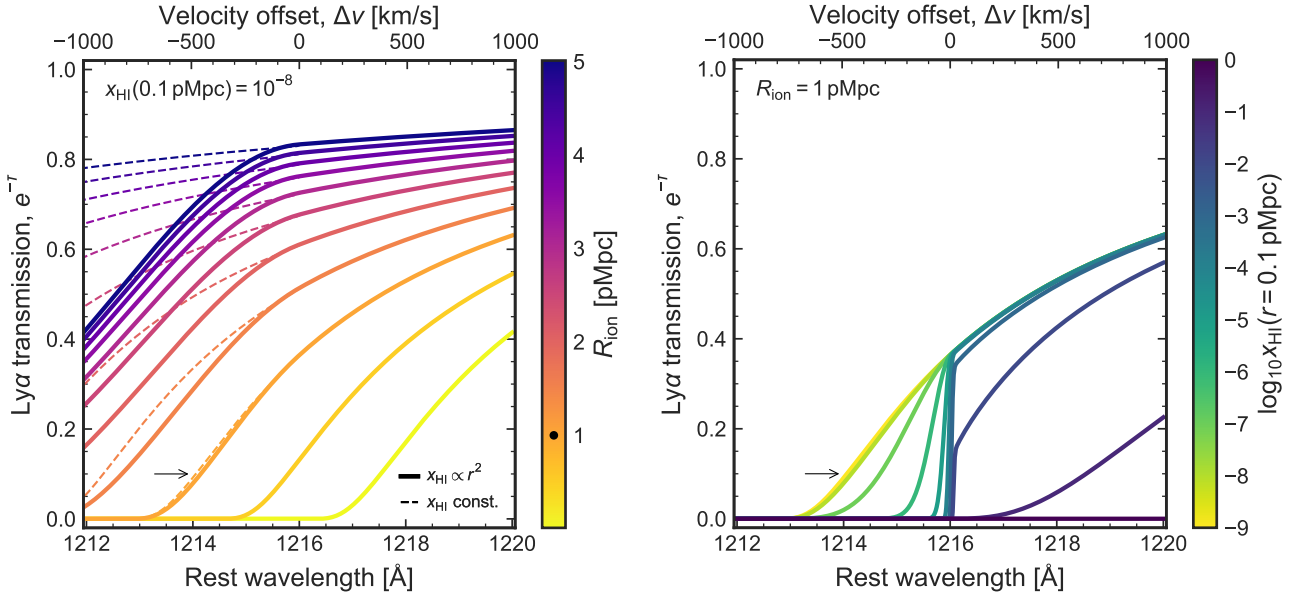


Figure 1. Ly α transmission for a source at $z_s = 7$ using a $x_{\text{HI}} \propto r^{-2}$ profile (solid lines). **Left:** Varying the distance to first neutral patch while fixing $x_{\text{HI}}(r = 0.1 \text{ Mpc}) = 10^{-8}$ ($n_{\text{HI}} \sim 10^{-12} \text{ cm}^{-3}$). For decreasing bubble size, the transmission on the red side of the Ly α line centre decreases, due to the increasing damping wing absorption. However, even in a fully neutral IGM, Ly α can be visible providing it is emitted at $> 200 \text{ km s}^{-1}$. Thin dashed lines show the transmission if $x_{\text{HI}} = 10^{-8}$ is constant inside the ionised region. The small black arrow shows $R_{\text{ion}} = 1 \text{ pMpc}$ to compare with the right panel. **Right:** Changing the residual neutral fraction inside the ionised region while holding the distance to the fully neutral patch, $R_{\text{ion}} = 1 \text{ pMpc}$, fixed. For increasing residual neutral fraction, the transmission on the blue side decreases as the gas becomes optically thick to Ly α photons redshifting to the resonant frequency by $x_{\text{HI}} \gtrsim 10^{-5}$. For higher neutral fractions, the damping wing absorption due to residual neutral gas inside the ionised region also become significant, reducing transmission on the red side of the line.

modelling the two media separately, i.e. breaking the integral into two components: from z_s to z_{ion} and z_{ion} to z_{obs} (following, Haiman 2002; Cen & Haiman 2000; Mesinger et al. 2004). In the ionised bubble we set $T = 10^4 \text{ K}$ (appropriate for photoionised gas at the mean density, e.g., Hui & Gnedin 1997) and $n_{\text{H}}(z) = C_{\text{HI}} \bar{n}_{\text{H}}(z)$. C_{HI} is the clumping factor of ionised hydrogen, $C_{\text{HI}} \equiv \langle n_{\text{HI}}^2 \rangle / \bar{n}_{\text{HI}}^2$, a free parameter which enhances the rate of recombinations, and $\bar{n}_{\text{H}}(z)$ is the cosmic mean hydrogen number density: $\bar{n}_{\text{H}}(z) \approx 1.88 \times 10^{-7} (1+z)^3 \text{ cm}^{-3}$. In the neutral IGM, we set $T = 1 \text{ K}$, assuming gas decouples from the CMB at $z \sim 150$ (Peebles 1993), and $n_{\text{H}}(z) = \bar{n}_{\text{H}}(z)$. Our results are not strongly sensitive to these temperature choices within a physically motivated range ($T < 10^5 \text{ K}$).

The left panel of Figure 1 shows the Ly α transmission, $e^{-\tau(\lambda)}$, as a function of wavelength – commonly expressed as velocity offset, $\Delta v \equiv c(\lambda_{\text{em}}/\lambda_{\alpha} - 1)$ – and ionised bubble radius, assuming the residual neutral fraction inside the ionised bubble is very low ($x_{\text{HI}} = 10^{-8}$ at 0.1 pMpc from the source, assuming $x_{\text{HI}} \propto r^2$ – see § 2.2.2). As the bubble size increases more flux is transmitted on both the blue and red side of the line. Blue photons which redshift into resonance at the edge of bubble or at further distances from the source all encounter fully neutral gas when they reach resonance and are thus absorbed with a high optical depth. Photons which have already redshifted past resonance by the time they reach the neutral gas experience the damping wing absorption, which smoothly suppresses flux to red wavelengths. For very small bubble sizes, the transmission on the blue side is therefore negligible and the transmission

within 200 km s^{-1} of the red side can be very low. Ly α lines observed with low velocity offsets from systemic must reside in large ionised regions.

Note that even in a fully neutral IGM ($R_{\text{ion}} = 0$) Ly α flux can still be transmitted on the red side: it is possible to observe Ly α lines at very high redshifts, providing they emit Ly $\alpha \gtrsim 300 \text{ km s}^{-1}$ from systemic (Dijkstra et al. 2011). Therefore, even at very high redshifts, merely detection of Ly α is not sufficient to identify a reionised bubble: there must be flux $< 300 \text{ km s}^{-1}$.

The right panel of Figure 1 shows the transmission through a bubble of fixed size (1 pMpc), but changing the residual neutral fraction in the ionised region around the source. The damping wing set by R_{ion} acts as an envelope for the maximum possible transmission: for $x_{\text{HI}}(r = 0.1 \text{ pMpc}) < 10^{-8}$, the bubble is fully optically thin and the maximum blue flux allowed given the damping wing shape can be transmitted. As the residual neutral fraction increases, more flux on the blue side of the line is absorbed, with the ionised region becoming optically thick for $x_{\text{HI}}(r = 0.1 \text{ pMpc}) \gtrsim 10^{-6}$ (corresponding to a neutral hydrogen number density of $n_{\text{HI}} \gtrsim 5 \times 10^{-10} \text{ cm}^{-3}$). For $x_{\text{HI}} > 10^{-1}$ the transmission displays a strong damping wing on the red side, though note the transmission in this case is lower than the $R_{\text{ion}} = 0 \text{ Mpc}$ case in the left panel: in the right panel we assume gas in the bubble is heated to 10^4 K , which generates a higher optical depth than the cold neutral IGM.

2.2 Size and residual neutral fraction of ionised bubbles

The optical depth can be calculated for any values of ionised bubble size, R_{ion} , and residual neutral fraction inside the bubble, x_{H} , to estimate those parameters in a model-independent way. In the limiting case of a single ionising source (plus uniform ionising background) we can also estimate those quantities for a physical model.

2.2.1 Size of ionised region

Assuming ionisation by a single source at redshift z_s at the centre of the ionised region, the proper radius of the region can be obtained by solving for the evolution of an ionisation front (e.g., Shapiro & Giroux 1987; Cen & Haiman 2000; Yajima et al. 2018):

$$\frac{dR_{\text{ion}}^3}{dt} = \frac{3f_{\text{esc}}\dot{N}_{\text{ion}}}{4\pi\bar{n}_{\text{H}}(z_s)} - C_{\text{HII}}\bar{n}_{\text{H}}(z_s)\alpha_{\text{B}}(T)R_{\text{ion}}^3 + 3H(z)R_{\text{ion}}^3 \quad (5)$$

where the first term is due to ionisations from a source with ionising photon output \dot{N}_{ion} (in units of s^{-1}) and ionising escape fraction f_{esc} , the second term is due to recombinations – assuming Case B recombination in a clumpy medium with clumping factor C_{HII} . For α_{B} , we use the approximation from Hui & Gnedin (1997) for the hydrogen recombination coefficient as a function of temperature. The third term of Eq. (5) is the expansion of the region due to the Hubble flow.

For constant \dot{N}_{ion} and f_{esc} , and simplified cosmology, Equation (5) can be solved analytically (Shapiro & Giroux 1987). For instance, for a luminous source at $z \lesssim 8$ (when the recombination rate is relatively low), the first term in Equation (5) dominates (Equation 2 of Cen & Haiman 2000), so that

$$R_{\text{ion}} \approx \left(\frac{3f_{\text{esc}}\dot{N}_{\text{ion}}t_{\text{age}}}{4\pi\bar{n}_{\text{H}}(z_s)} \right)^{1/3} \quad (6)$$

where t_{age} is the time since the ionising source has switched on. In reality, due to the Hubble expansion the ionised radius grows more rapidly after $\sim 10^7$ years than Equation (6). Here, we solve Equation (5) numerically.

The source emissivity \dot{N}_{ion} , in s^{-1} can be written as

$$\dot{N}_{\text{ion}}(t) = \int_{\nu_{\text{H}}}^{\infty} d\nu \frac{L_{\nu}(t)}{h\nu} \quad (7)$$

where L_{ν} is the ionising spectrum of the source in $\text{erg s}^{-1} \text{Hz}^{-1}$, which can be approximated as a power-law for hydrogen ionising photons: $L_{\nu} \propto \nu^{-\alpha}$ for $\nu > \nu_{\text{H}}$, where $\nu_{\text{H}} \approx 3.3 \times 10^{15} \text{ Hz}$ is the frequency of hydrogen photoionisation, α is the spectral slope of the ionising continuum, typically $1 \lesssim \alpha \lesssim 2$ for quasars (e.g., Scott et al. 2004; Stevans et al. 2014; Lusso et al. 2015) and galaxies with massive stars (Steidel et al. 2014; Feltre et al. 2016), where stripped stars in binaries can cause the spectral slope to reach ~ 1 (Götberg et al. 2020).

To estimate \dot{N}_{ion} for galaxies we assume the spectrum is a double power law: $L_{\nu} \propto \nu^{-\alpha}$ for $\nu > \nu_{\text{H}}$, and $L_{\nu} \propto \nu^{-\beta}$ for $\nu < \nu_{\text{H}}$. Thus we can estimate \dot{N}_{ion} from a UV magnitude (measured at 1500 \AA) as:

$$\dot{N}_{\text{ion}} \approx 5.2 \times 10^{55} \left(\frac{1+z}{8} \right) \frac{10^{-0.4(M_{\text{UV}}+20)}}{\alpha(1+z)^{\beta+2}} \left(\frac{912}{1500} \right)^{\beta+2} \text{ s}^{-1}$$

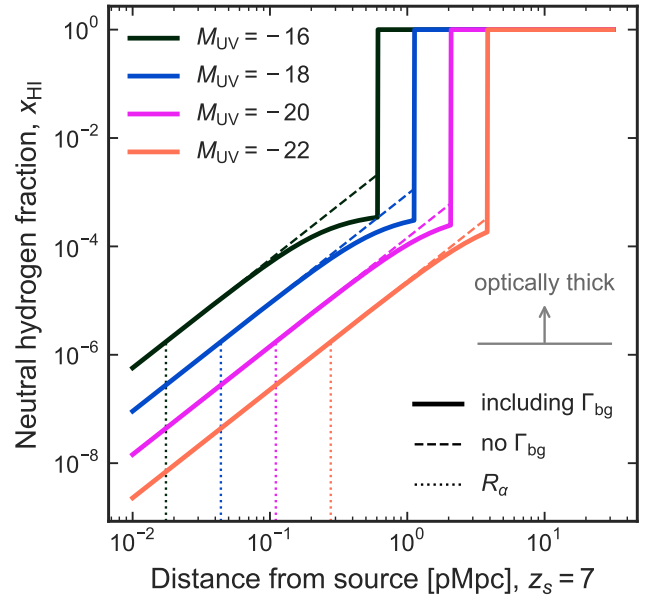


Figure 2. Residual neutral hydrogen fraction inside an ionised region, with (solid lines) and without (dashed lines) including ionising background flux from Khaire & Srianand (2019), as a function of the distance from the source and source UV magnitude. R_{ion} is determined by solving Equation (5). Calculated assuming $f_{\text{esc}} = 1$, $C_{\text{HII}} = 3$, $\beta = -2$, $\alpha = 2$. The dotted vertical lines mark the radius of the optically thin region, R_{α} , defined by $x_{\text{H}} \lesssim 1.6 \times 10^{-6}$ (§ 2.2.3).

(8)

Galaxy spectra typically have a steeper drop-off beyond the HeII ionising limit (54.4 eV), which isn't captured in our simple power-law approximation. However, we note that this has only a small impact on our estimation of \dot{N}_{ion} : for $1 < \alpha < 3$ assuming the spectrum is zero $\nu > \nu_{\text{HeII}}$ produces $> 0.75\dot{N}_{\text{ion}}$ as defined in Equation (8).

2.2.2 Residual neutral fraction of ionised region

Due to the recombination of ionised hydrogen, inside the ionised region there will be some residual neutral fraction. This can be computed by equating the recombination rate to the ionisation rate, assuming ionisation equilibrium. Assuming ionisations due to the central source and some diffuse ionising background, the residual neutral fraction at a proper radius r from the source is (e.g., Mesinger et al. 2004):

$$x_{\text{H}}(r) = C_{\text{HII}}\bar{n}_{\text{H}}(z)\alpha_{\text{B}}(T) \left(\Gamma_{\text{bg}}(z) + \frac{J_s}{4\pi r^2} \right)^{-1}. \quad (9)$$

Here, Γ_{bg} is the hydrogen ionising rate due to the background within the ionised region in s^{-1} , and J_s is the hydrogen ionising emissivity of the central source in $\text{cm}^2 \text{s}^{-1}$. The gas reaches ionisation equilibrium with a characteristic timescale $t_{\text{eq}}^{-1} = \Gamma_{\text{bg}} + J_s/4\pi r^2$, so the bubble will be in ionisation equilibrium within $\sim 10^5$ years assuming constant emissivity (e.g., Davies et al. 2020). Thus Equation (9) holds for sources with ionising populations $> 10^5$ years, which is

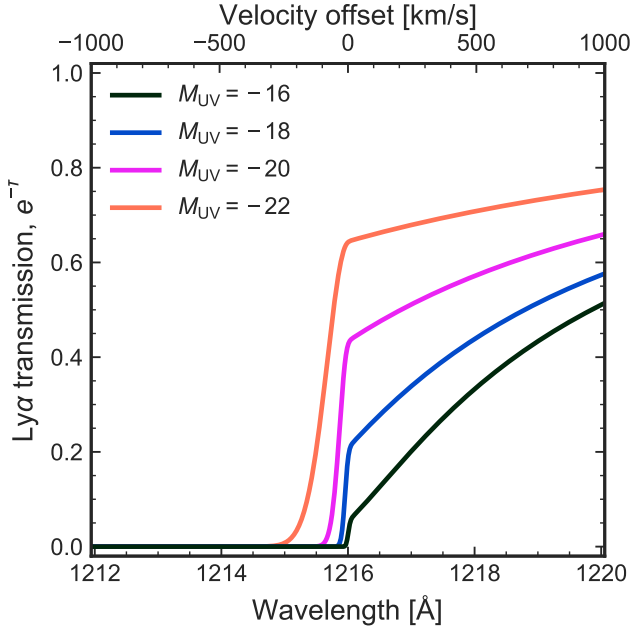


Figure 3. Ly α transmission curves for the models shown in Figure 2, calculating the optical depth as described in § 2.1.

reasonable for massive galaxies at $z \sim 6 - 8$, though may break down for galaxies with short bursts of star formation.

We use the ionising background model by Khaire & Srikanth (2019) but note that it does not significantly impact the residual neutral fraction for bubbles at $z > 6$ as the background is low compared to the local ionisation field, leading to $x_{\text{HII}} \propto r^2$. Strictly, Γ_{bg} accounts for other ionising sources nearby and will therefore vary depending on the density of the environment. We expect $\Gamma_{\text{bg}} \lesssim 6\langle\Gamma_{\text{bg}}\rangle$ based on fluctuations of density and mean free path (Mesinger & Dijkstra 2008; Davies & Furlanetto 2016). For reference $\langle\Gamma_{\text{bg}}(z \sim 7)\rangle \approx 0.2 \times 10^{-12} \text{ s}^{-1}$ in the Khaire & Srikanth (2019) model, and has been measured to be $\lesssim 0.3 \times 10^{-12} \text{ s}^{-1}$ at $z \sim 6$ (Wyithe et al. 2010; Calverley et al. 2011). The source hydrogen ionising emissivity can be expressed as

$$J_s = f_{\text{esc}} \int_{\nu_H}^{\infty} d\nu \frac{L_\nu}{h\nu} \sigma_{\text{ion}}(\nu) \quad (10)$$

with the hydrogen photoionisation rate $\sigma_{\text{ion}} = \sigma_{\text{ion},0}(\nu/\nu_H)^{-3}$, where $\sigma_{\text{ion},0} \approx 6.3 \times 10^{-18} \text{ cm}^2$ (e.g., Draine 2011). Assuming as above an ionising spectrum $L_\nu \propto \nu^{-\alpha}$ yields

$$J_s = f_{\text{esc}} \dot{N}_{\text{ion}} \frac{\alpha}{\alpha + 3} \sigma_{\text{ion},0} \quad (11)$$

where \dot{N}_{ion} is given by Equation (8).

Figure 2 shows some typical neutral fraction profiles inside a HII region. Here, and below, we assume that the neutral fraction is unity outside the HII region at the radius determined by Equation 5. We see that more luminous galaxies produce bubbles which are both larger (Equation 6) and more highly ionised at a fixed distance from the source. Figure 3 shows the Ly α for the same set of models. Only UV bright galaxies are capable of producing a sufficiently large ionised region to allow blue flux to be observed.

2.2.3 Optically thin region within ionised region

Importantly, due to the high resonant cross-section of Ly α (Equation (2)) an ionised bubble can still be optically thick to Ly α . Thus blue Ly α flux can be suppressed by residual neutral gas *within* an ionised bubble. The proper radius at which the bubble becomes optically thick to Ly α is the radius where the Gunn & Peterson (1965) optical depth (Equation (4), using $x_{\text{HII}}(r)$ given by Equation 9) exceeds an optical depth threshold $\tau_{\text{lim}} \sim 2.3$ (i.e. transmission $\sim 10\%$):

$$R_\alpha = \left(\frac{J_s}{4\pi} \right)^{1/2} \left[\frac{C_{\text{HII}}^2 \bar{n}_{\text{H}}^2(z) \alpha_B(T) f_\alpha \pi e^2}{H(z) \tau_{\text{lim}} m_e \nu_\alpha} - \Gamma_{\text{bg}}(z) \right]^{-1/2} \quad (12)$$

$$\approx 0.16 \left(\frac{\tau_{\text{lim}} \dot{N}_{\text{ion}} f_{\text{esc}}}{2.3 \times 5.2 \times 10^{55} \text{ s}^{-1}} \right)^{1/2} \left(\frac{2.5\alpha}{\alpha + 3} \right)^{1/2}$$

$$\times \left(\frac{C_{\text{HII}}}{3} \right)^{-1} \left(\frac{T}{10^4 \text{ K}} \right)^{0.4} \left(\frac{1+z}{8} \right)^{-9/4} \text{ Mpc}$$

where J_s is given by Equation (11). For the latter equality we assumed $\Gamma_{\text{bg}} = 0$, $\alpha_B(T) \approx 2.6 \times 10^{-13} (T/10^4 \text{ K})^{-0.8} \text{ cm}^3 \text{ s}^{-1}$ and used \dot{N}_{ion} for a $M_{\text{UV}} = -20$ galaxy (Equation 8).

This radius corresponds to reaching a neutral hydrogen number density of $n_{\text{HII}} \gtrsim 4.7 \times 10^{-10} (\tau_{\text{lim}}/2.3) [(1+z)/8]^{3/2} \text{ cm}^{-3}$ – or $x_{\text{HII}} \gtrsim 1.6 \times 10^{-6} (C_{\text{HII}}/3)^{-1} (\tau_{\text{lim}}/2.3) [(1+z)/8]^{-3/2}$ – in the ionised region. At higher densities/neutral fractions the gas is optically thick to Ly α photons.

This is analogous to the quasar near/proximity zones described by Bolton & Haehnelt (2007), except here we include the contribution of other, diffuse sources of ionising photons. As discussed in Section 2.2.2 we assume the reionised region is in ionisation equilibrium, which is valid for sources with ionising populations $> 10^5$ years. See Davies et al. (2020) for discussion of the time evolution of such optically thin regions around quasars.

A lower limit on R_α can thus be estimated from the minimum observable blue Ly α velocity offset $\Delta v_\alpha^{\text{min}}$:

$$R_\alpha > \frac{|\Delta v_\alpha^{\text{min}}|}{H(z_s)} \quad (13)$$

Previous works, which assumed ionised bubbles are optically thin to Ly α (e.g., Matthee et al. 2018; Hashimoto et al. 2018) estimated $R_{\text{ion}} > |\Delta v_\alpha^{\text{min}}|/H(z_s)$. From the above, we see this is actually measuring R_α and is an underestimate of R_{ion} . We will show below in Section 3.1 that $R_\alpha \ll R_{\text{ion}}$.

3 RESULTS

3.1 Evolution of optically thin regions around galaxies

The Ly α optical depth (Equation 1) decreases with decreasing redshift, due to the increasing ionising output of sources, and the reducing density of neutral gas due to cosmic expansion. Thus, we expect the optically thin regions around galaxies in reionising bubbles to grow with decreasing redshift, increasing the observable blue flux.

Figure 4 shows the total ionised radius (R_{ion}) and the optically thin radius (R_α) as a function of source redshift, fixing $f_{\text{esc}} = 1$, $C_{\text{HII}} = 3$, $\alpha = 2$, $\beta = -2$. We compare the sizes of the bubbles and proximity zones for sources with different UV luminosities ($M_{\text{UV}} = -16, -18, -20, -22$)

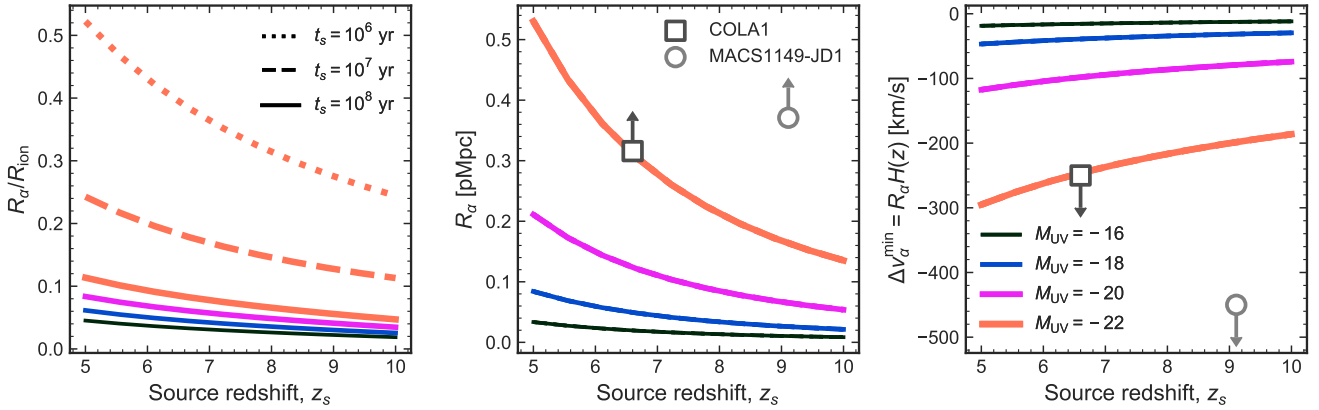


Figure 4. Radii of ionised bubbles and Ly α proximity zones around galaxies as a function of source redshift and age. Note these show optimistic upper limits on the sizes assuming $f_{\text{esc}} = 1$, $C_{\text{HII}} = 3$, $\alpha = 2$, $\beta = -2$. **Left:** Ratio of the Ly α proximity zone (R_α , Equation 12) to the radius of ionised sphere (R_{ion} , Equation 5) for galaxies with $M_{\text{UV}} = -16, -18, -20, -22$ (black, blue, pink, orange lines respectively). We show the time evolution of R_α/R_{ion} for the brightest source. Early on, before the ionisation front can grow significantly, $R_\alpha \sim 0.3 - 0.5 R_{\text{ion}}$, however, for sources > 100 Myr old, $R_\alpha \lesssim 0.1 R_{\text{ion}}$. **Center:** The proper size of the optically thin region R_α in pMpc as a function of source redshift. All lines are the same as the left panel. **Right:** Radius of optically thin region expressed as a Ly α velocity offset, i.e. the maximum Ly α blue peak velocity offset that would be observable from a Ly α emitter inside this ionised region. We also show the observed blue-peaked Ly α emitters COLA1 (Hu et al. 2016; Matthee et al. 2018), MACS1149-JD1 (Hashimoto et al. 2018). NEPLA4 (Songaila et al. 2018) is at the same redshift as COLA1 and has a similar blue peak velocity.

and age ($10^6, 10^7, 10^8$ yrs). Except for very young sources $R_\alpha \lesssim 0.1 R_{\text{ion}}$, R_α does not change in size with age for constant emissivity once ionisation equilibrium is reached. As noted above, previous works, which assumed ionised bubbles are fully ionised when estimating blue peak transmission, underestimated the total extent of the ionised region when using the observed blue Ly α peak. By including recombinations we see the blue Ly α flux only probes the much smaller optically thin region. In the next section, we show that there are model-independent ways to estimate a lower bound on the size of the full ionised region.

3.2 Observable Ly α lines in a mostly neutral medium

Figure 5 shows the minimum Ly α velocity offset observable as a function of the distance to the first neutral region (R_{ion}) and residual neutral fraction in the bubble (x_{HII}). We compute Ly α transmission $e^{\tau(\Delta v)}$ on a grid of R_{ion} and x_{HII} , enabling a model-independent estimate of the properties of an ionised bubble based on Ly α transmission. We show the velocity offsets observable if $> 10\%$ of the flux emitted at that velocity offset is transmitted through the IGM. We choose 10% as assuming an emitted Ly α EW of 200 Å, this transmitted flux should be observable with current facilities.

For small bubbles with high x_{HII} , it is only possible to observe Ly α which is significantly redshifted. Conversely, it is only possible to observe blue Ly α flux if there is a significant distance to the first neutral patch (> 0.5 pMpc) and the HII region is highly ionised ($x_{\text{HII}} < 10^{-5}$).

The two panels in Figure 5 compare the minimum observable Ly α velocity offsets in the case of a homogeneous residual neutral fraction in the bubble ($x_{\text{HII}} = \text{constant}$), approximating reionisation by a uniform ionising background of ultra-faint sources) and in the limiting case of the Ly α emitter as the sole reionising source ($x_{\text{HII}} \propto r^2$, Equation 9),

with the value on the y -axis $x_{\text{HII}}(r = 0.1 \text{ pMpc})$. The trend of increased red-blue visibility with increasing bubble size is the same in both cases.

3.3 The ionised environment around observed blue-peaked Ly α emitters

3.3.1 COLA1

COLA1 is a $z \approx 6.6$ galaxy with a blue Ly α peak with flux up to -250 km s^{-1} from systemic (Hu et al. 2016; Matthee et al. 2018). From Figure 5 we see that this requires it to reside in an ionised region at least 0.7 pMpc to the nearest neutral patch, with a residual neutral fraction $x_{\text{HII}} < 10^{-6}$. Our estimate of the extent of the ionised region is roughly double than that of Matthee et al. (2018), who estimated 0.3 pMpc (2.3 cMpc). This is due to their assumption that the entire bubble is optically thin. As discussed in Section 3.1, with just the minimum observed blue flux velocity we can only calculate R_α (Equation 13), but the total ionised region is much larger.

Figure 6 shows the radius of the proximity zone as a function of source magnitude. We compare R_α to the blue peak velocity offsets from Matthee et al. (2018) and Hashimoto et al. (2018), and vary $f_{\text{esc}} = \{1, 0.2\}$, $C_{\text{HII}} = \{3, 10\}$, $\alpha = \{1, 2\}$ and $\beta = \{-2, -2.5\}$. For COLA1 to ionise its own proximity zone likely requires a high escape fraction, steep UV spectral slope β , and relatively low gas density, whilst the ionising spectral slope makes a negligible impact on the proximity zone size.

To investigate in more detail the necessary conditions for COLA1's blue peak to be observable we perform a Bayesian inference to infer the parameters in Equation (12). We define the likelihood to observe blue Ly α flux at $-250 \pm 60 \text{ km s}^{-1}$ (the minimum observed blue flux, using the instrumental resolution $R \sim 5000$ for the uncertainty), from a galaxy with $M_{\text{UV}} = -21.6 \pm 0.3$ at $z = 6.6$. To observe a

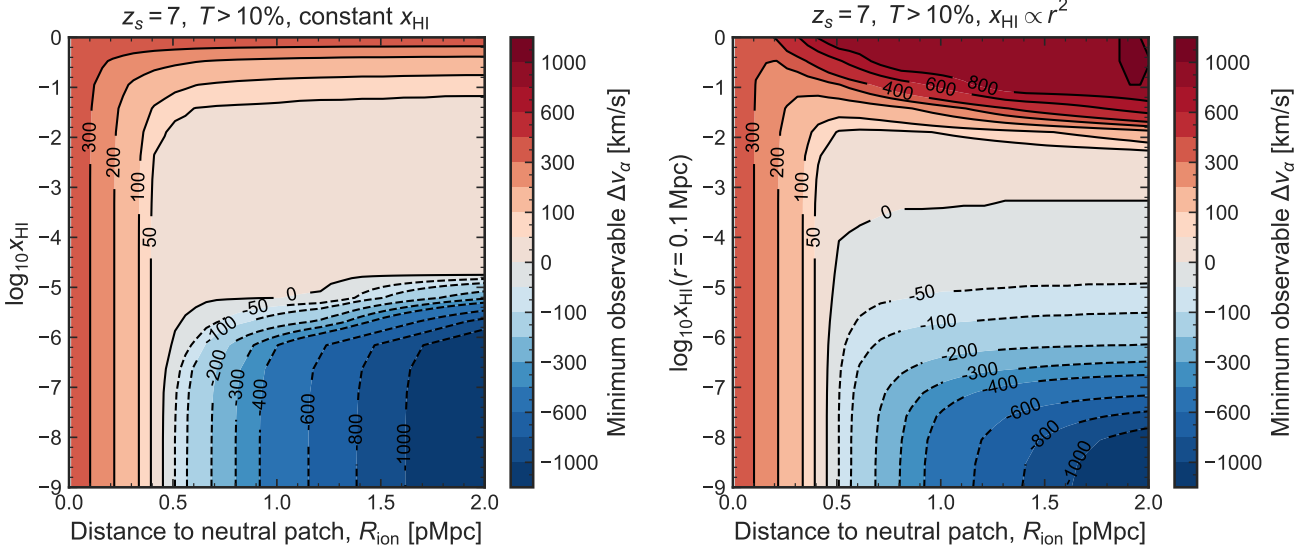


Figure 5. Minimum observable Ly α velocity offset, Δv_α as a function of bubble size and residual neutral fraction, assuming $> 10\%$ transmission on the red or blue sides. **Left** for a constant residual neutral fraction, x_{HI} , inside the ionised bubble. **Right** $x_{\text{HI}} \propto r^2$, with the quoted value at 0.1 Mpc.

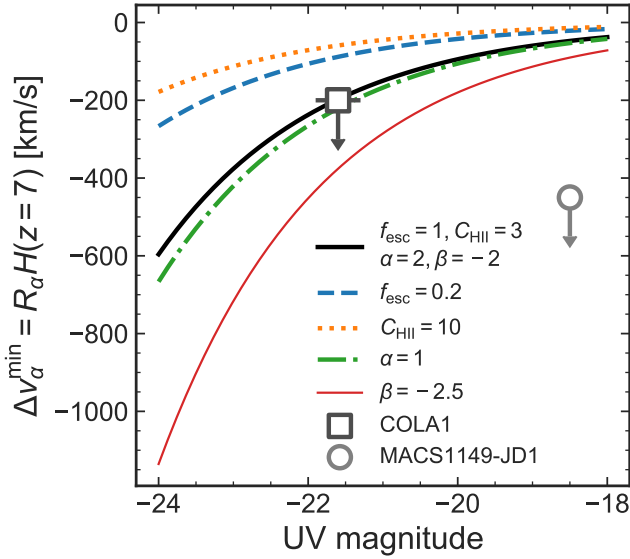


Figure 6. Radius of optically thin region produced by a single source of a given UV magnitude. We show the minimum observable blue-shifted velocity offset from systemic. The black solid line shows a fiducial galaxy model ($f_{\text{esc}} = 1$, $C_{\text{HI}} = 3$, $\alpha = 2$, $\beta = -2$). The other lines show the impact of changing one of these parameters to a more extreme value: $f_{\text{esc}} = 0.2$ (blue dash), $C_{\text{HI}} = 10$ (orange dots), $\alpha = 2$ (green dot-dash), $\beta = -2.5$ (thin red solid).

blue peak at Δv , the proximity zone $R_\alpha > |\Delta v|/H(z)$. The likelihood is:

$$p(R_\alpha \geq |\Delta v|/H(z) | \theta) = \frac{1}{2} \text{erfc} \left(\frac{|\Delta v|/H(z) - R_{\alpha, \text{mod}}(\theta)}{\sqrt{2}\sigma_R} \right) \quad (14)$$

where we have assumed the probability of a proximity

zone having radius R_α , $p(R_\alpha | \theta)$, is a normal distribution with mean $R_{\alpha, \text{mod}}(\theta)$ (Equation 12) and variance $\sigma_R^2 = [\sigma_{\Delta v}/H(z)]^2$. We use uniform priors on the parameters $\theta = [f_{\text{esc}}, C_{\text{HI}}, \alpha, \beta, \Gamma_{\text{bg}}]$: $0 \leq f_{\text{esc}} \leq 1$, $0.2 < C_{\text{HI}} < 10$, $1 \leq \alpha \leq 2.5$, $-3 < \beta < -1$, and $0 < \Gamma_{\text{bg}}/10^{-12} \text{s}^{-1} < 10$. We run two versions of the model: one where we fix the ionising background $\Gamma_{\text{bg}} = 0$ (i.e. assuming COLA1 ionises its proximity zone alone), and one where Γ_{bg} is a free parameter. To estimate the posteriors and the evidence for each model, $Z = \int d\theta p(\theta | R_\alpha)$, we use Dynamic Nested Sampling implemented in **dynesty** (Speagle 2019).

Figure 7 shows the posteriors for these parameters and their median and 16 – 84% credible intervals or 68% upper/lower limits, and the evidence Z . In both cases, gas density is inferred to be relatively low ($\lesssim 2.6 \bar{n}_{\text{H}}$, 1σ), the UV slope β is inferred to be steep ($\beta < -2.27$ 1σ for $\Gamma_{\text{bg}} = 0$) and the spectral slope of the ionising continuum, α , is not well constrained by the proximity zone, due to the smaller range of possible α having a minimal impact on the size of the proximity zone (see Figure 6). In the model without an ionising background, high escape fractions are inferred (> 0.48 , 1σ), while when we include an ionising background there is a degeneracy between high single source f_{esc} and low ionising background, or low f_{esc} and high ionising background. Neither model is strongly preferred, with a Bayes factor $Z_{\text{bg}}/Z_{\text{nobg}} = 1.2$ (e.g., Trotta 2008).

3.3.2 Other $z > 6$ blue peaks

Hashimoto et al. (2018) reported a 4σ detection of a Ly α line in the $z = 9.11$ source MACS1149-JD1. The Ly α line is offset by $-450 \pm 60 \text{ km s}^{-1}$ from their detection of [OIII]88 μm .

Based on Figure 5, if the Ly α comes from the same source as the [OIII], the environment of MACS1149-JD1 must be extremely highly ionised ($> 10^{-6}$) and in a bubble $\gtrsim 1$ pMpc. Figure 6 shows the size of the proximity zones

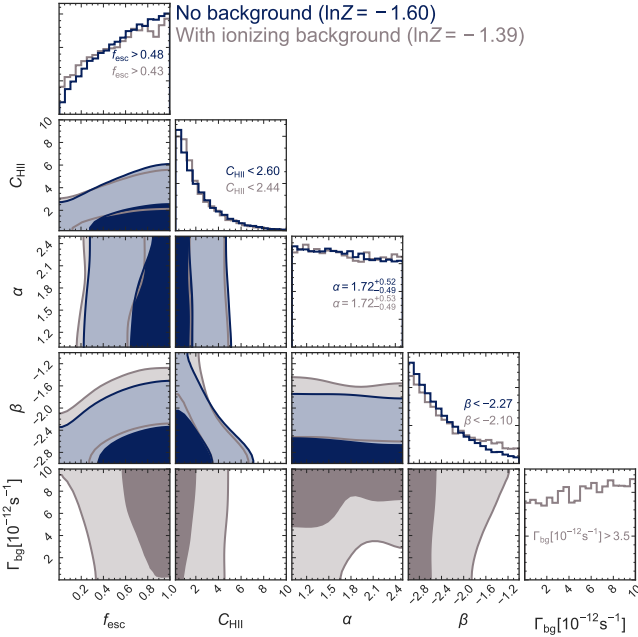


Figure 7. Posterior distributions for f_{esc} , C_{HII} , α , β and Γ_{bg} inferred from the observed maximum blue Ly α peak of COLA1 (-250 km s^{-1}). We show 1σ and 2σ contours of the 2D posteriors, and histograms of marginalised 1D posteriors for the parameters. Blue lines show the model with $\Gamma_{\text{bg}} = 0$, grey lines the model with Γ_{bg} as a free parameter. The likelihood and priors are described in Section 3.3.1.

produced by galaxies of a given M_{UV} . Given the observed faintness of MACS1149-JD1 ($M_{\text{UV}} = 18.5 \pm 0.1$ based on lens modelling and fits to photometry and grism spectroscopy, Hoag et al. 2018), it is impossible for it to produce such a large optically thin region, even with high f_{esc} , steep α and low gas density. We thus agree with a possible interpretation by Hashimoto et al. (2018) that the Ly α emission comes from a different, slightly lower redshift, source compared to the [OIII] emission in MACS1149-JD1.

NEPLA4 (Songaila et al. 2018) is a narrow-band selected Ly α emitter at $z = 6.6$ with blue flux up to $\sim -250 \text{ km s}^{-1}$, similar to COLA1. As the UV continuum is not known we cannot place it on Figure 6.

4 DISCUSSION

4.1 Ly α constraints on bubble properties

Blue Ly α peaks can reveal conditions inside individual reionised bubbles, however we expect blue peaks to be rare at $z > 6$, due to the high IGM opacity (see § 3.1 and e.g., Laursen et al. 2011). By contrast, Ly α lines which are redshifted with respect to systemic may arise more often at high redshift due to outflows, which aids the transmission of photons through the IGM (Dijkstra et al. 2011). Figure 5 demonstrates that the velocity offset of an observed red peak can place lower limits on the size of an ionised region (see also Malhotra & Rhoads 2006).

Not only can a single source place constraints on bubble sizes, with a deep spectroscopic survey in a single field it

could be possible to map an ionised bubble directly. Due to the the ionisation gradient across bubbles the transmission of Ly α will vary radially across a bubble (see Figure 8). As we demonstrate in Figure 5, the observable minimum velocity offset from systemic varies as a function of the distance from the nearest neutral region. Likewise, the transmitted Ly α flux will decrease for sources further from the center of bubbles. If the faint-end of Ly α luminosity function is steep (e.g., $\alpha \sim -2.8$ Drake et al. 2017) at $z \sim 7$, using the luminosity function model by Gronke et al. (2015) (setting $\alpha = -2.8$) we expect ~ 12 Ly α emitting galaxies with a luminosity $L \gtrsim 10^{41} \text{ erg s}^{-1}$ (flux $\gtrsim 1 \times 10^{-19} \text{ erg s}^{-1} \text{ cm}^{-2}$) located within $R_\alpha \sim 0.3 \text{ pMpc}$ (the lower limit on COLA1’s proximity zone – see Figure 4). Note, this estimate does not account for galaxy clustering – if Ly α emitters live in over-dense regions (Ouchi et al. 2017) we expect higher number counts. Within this optically thin region we would expect the fraction of galaxies with blue Ly α peaks to be comparable to those seen at lower redshifts, when the IGM is highly ionised.

With a large near infra-red spectroscopic survey to measure Ly α flux and high S/N resolved lineshapes, as well as systemic redshift from other emission lines (e.g. rest-frame optical lines visible with JWST) it could be possible to directly map ionised bubbles and place constraints on the bubble size distribution during reionisation. These deep measurements will be feasible with 30 m telescope spectroscopy (e.g., E-ELT/MOSAIC is expected to reach $1 \times 10^{-19} \text{ erg s}^{-1} \text{ cm}^{-2}$ in 40 hrs, Evans et al. 2015).

To fully interpret such data requires a more realistic treatment of the neutral gas distribution than the uniform model used here. For example, Gronke et al. (in prep) explores the prevalence of blue Ly α peaks in the cosmological radiative hydrodynamical simulation CoDaII (Ocvirk et al. 2018), and finds large line-of-sight variation in Ly α transmission due to inhomogeneous gas distributions.

While the visibility of blue peaks (or red peaks with small velocity offset) can put lower limits on R_α , measuring the size more accurately is difficult. However, given sufficient spectral quality, it might be possible to detect a sharp cutoff on the blue side of a blue peak – a signature of absorption, since frequency redistribution yields smoother profiles towards the wings (Neufeld 1990). A sharp cutoff would be expected if there is a sharp transition from an optically thin ionised region to one that is optically thick, for example, from galaxies sustaining their own R_α surrounded by homogeneous $10^{-5} \lesssim x_{\text{HII}} \lesssim 10^{-3}$ reionised gas (which may be typical of the IGM at the end of reionisation e.g., Fan et al. 2006). This would enable a direct measurement of R_α and thus tighter constraints on f_{esc} . In contrast, a sharp cutoff of the red peak towards line centre can be due to either the IGM or radiative transfer effects and is commonly found also at low redshifts (e.g., Rivera-Thorsen et al. 2015; Yang et al. 2017), thus, this is harder to use as a measurement for R_α . However, one could use this signature in a statistical sense: intragalactic radiative transfer sets a characteristic correlation between the width and velocity offset of red Ly α peaks (e.g., Neufeld 1990; Verhamme et al. 2018), and this trend should be altered at high- z due to the IGM absorption yielding a flatter slope in the width-offset relation.

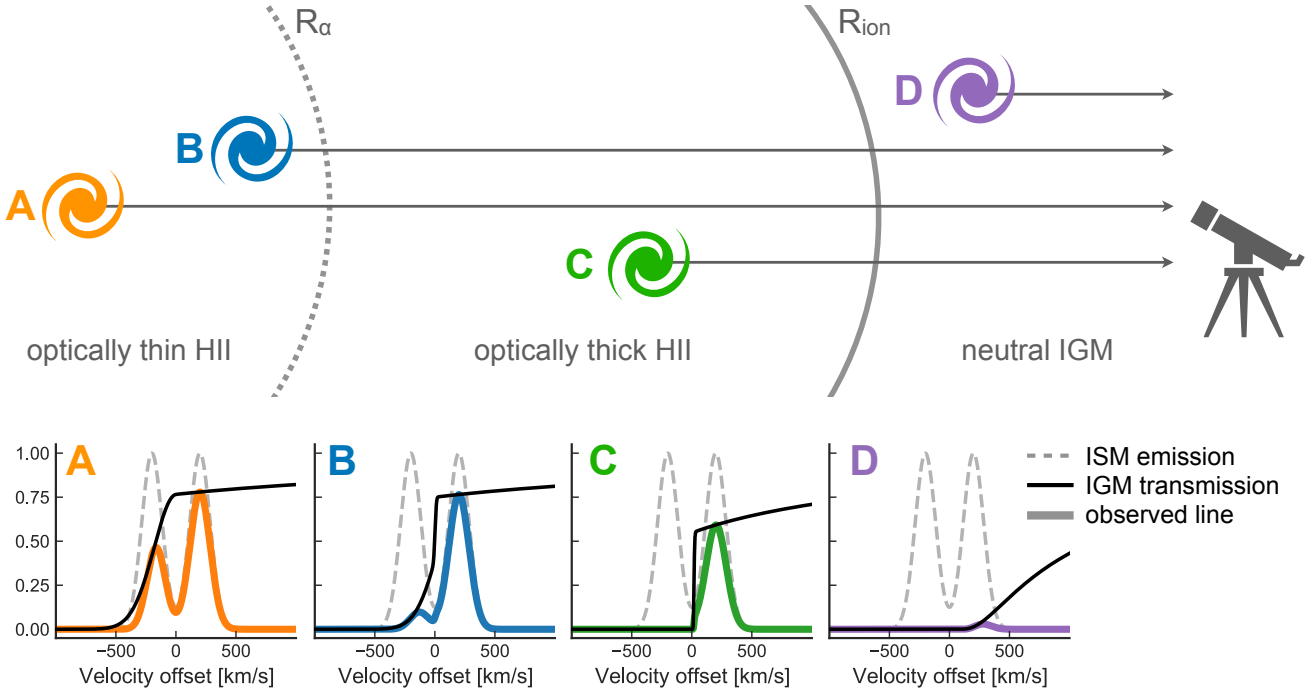


Figure 8. Illustration of IGM attenuation for galaxies at different radial positions from the center of an ionised bubble. We show relative (not to scale) positions and observed line profiles of galaxies: at the center of the bubble, inside the optically thin region (A), close to the edge of the optically thin region (B), and within the optically thick region (C), in the neutral IGM (D). The plots show the observed Ly α emission lines expected if all the galaxies had the same double-peaked emission line emerging from the ISM. Galaxy A can be observed with significant blue flux, whereas galaxies C and D have no observed blue flux. A small fraction of Ly α is still visible from galaxy D, but only at $\Delta v \gtrsim 300 \text{ km s}^{-1}$.

4.2 Impact of resonant absorption on EoR inferences

The increase in the size of the optically thin region means that more blue flux will be observed at lower redshifts, even if the size of the ionised bubble remains the same. The evolving flux distribution of Ly α emission from $z > 6$ galaxies has been used to measure the average neutral hydrogen fraction of the IGM (Mesinger et al. 2015; Mason et al. 2018a), under the assumption that the declining flux is due to damping wing absorption alone. However, an increase in resonant absorption may also account for some of the decrease observed in the Ly α flux distribution at $z > 6$ (see e.g., Bolton & Haehnelt 2013; Mesinger et al. 2015).

Given current constraints on the neutral fraction at the end of reionisation ($z < 6$, Fan et al. 2006), we can ask under what conditions could the increased optical depth due to an increased residual neutral fraction in ionised bubbles cause the observed decline in Ly α emission.

Assuming a double-peaked Gaussian Ly α lineprofile, with red:blue flux ratio $R : 1$, the resulting Ly α transmission fraction through the IGM can be written as:

$$\frac{T(z=7)}{T(z=6)} = \frac{e^{-\tau_{\text{GP}}(z=7)} + R}{e^{-\tau_{\text{GP}}(z=6)} + R} \quad (15)$$

Figure 9 shows this as a function of the relative increase in the average residual neutral fraction between $z \sim 6$ and $z \sim 7$, $x_{\text{H}}(z=7)/x_{\text{H}}(z=6)$. In order to produce a drop in the observed Ly α fraction of $T_7/T_6 \sim 0.5$, either the neutral fraction at $z = 6$ must be $< 10^{-6}$, i.e. not optically thick, or if $x_{\text{H}}(z=6) \sim 10^{-5}$ the blue peak flux must be $\gtrsim 100\times$

stronger than the red peak. Both of these scenarios are unlikely: the $z \sim 6$ Ly α forest is optically thick on average (e.g., Fan et al. 2006, find $x_{\text{H}}(z \sim 6) \gtrsim 10^{-4}$) and the observed Ly α line shapes of galaxies at all redshifts show dominant red peaks (e.g., Trainor et al. 2015; Rivera-Thorsen et al. 2015; Yang et al. 2017; Steidel et al. 2018). Therefore, while the residual neutral fraction in ionised regions will increase between $z \sim 6$ to $z \sim 7$ due to a lower ionising background and increased recombinations, it is unlikely to significantly impact the integrated transmission of Ly α on average, and thus has a small impact on reionisation inferences.

5 CONCLUSIONS

We have used an analytic model to estimate the Ly α optical depth within reionised bubbles and investigate the impact of reionisation on Ly α lineshapes. Our conclusions are as follows:

(i) Both the size of, and residual neutral hydrogen fraction within, reionised bubbles affect the observed lineshape of Ly α emission during reionisation. As such, measurements of the Ly α velocity offset from systemic can provide lower limits on the source's distance to the first large neutral patch along the line of sight, and upper limits on the residual neutral fraction inside its HII bubble.

(ii) Galaxies with Ly α lines observed with low velocity offsets from systemic must reside in large reionised regions. Detecting blue Ly α peaks during reionisation requires the source galaxy live in a $R \gtrsim 0.5 \text{ pMpc}$, and highly ionised

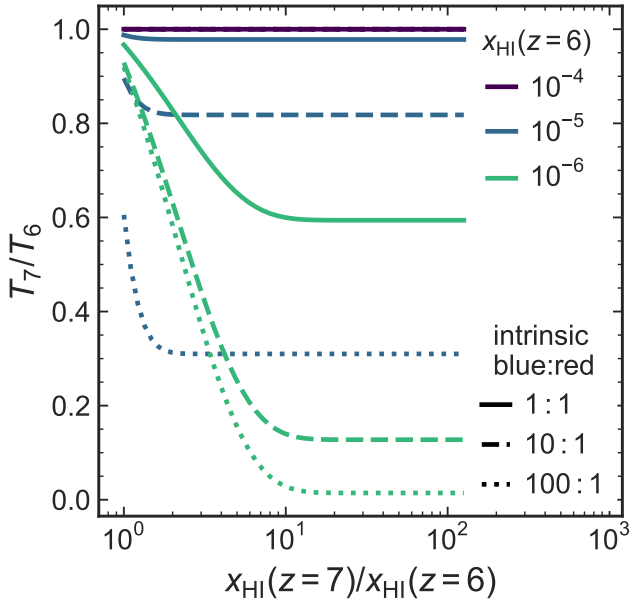


Figure 9. Ly α transmission ratio $z = 7$ to $z = 6$ given by Equation (15), assuming all of the optical depth to Ly α is due to resonant absorption of the blue peak (i.e. no damping wing), as a function of the relative increase in the residual neutral fraction $x_{\text{HI}}(z = 7)/x_{\text{HI}}(z = 6)$. The coloured lines show the ratio for different values of $x_{\text{HI}}(z = 6)$ and the linestyles for different intrinsic blue:red peak ratios. For an increase in residual neutral fraction to explain the drop in Ly α transmission $T_7/T_6 \sim 0.5$ requires the $z \sim 6$ IGM to be highly neutral $x_{\text{HI}} \lesssim 10^{-5}$ and the blue peak to be significantly stronger than the red peak, contrary to observations at $z \lesssim 5$ which show majority of dominant red peaks (e.g., Trainor et al. 2015; Rivera-Thorsen et al. 2015; Yang et al. 2017; Steidel et al. 2018).

($x_{\text{HI}} > 10^{-5}$) bubble. By contrast, Ly α can be detected even from fully neutral regions, providing it was emitted at high velocity offset ($\gtrsim 300 \text{ km s}^{-1}$).

(iii) Around individual galaxies, we predict the regions of low Ly α optical depth – proximity zones – to be typically $< 0.3 \text{ pMpc}$, allowing blue-shifted Ly α to be detected out to $\gtrsim 250 \text{ km s}^{-1}$.

(iv) The observed blue-peaked Ly α emitter COLA1, with blue flux up to -250 km s^{-1} , must reside in a highly ionised region ($x_{\text{HI}} < 10^{-5.5}$) at least 0.7 pMpc from the nearest large scale neutral patch. For COLA1 to have generated its own proximity zone requires it to have a high escape fraction, $f_{\text{esc}} > 0.48$, and steep UV spectral slope, $\beta < -2.27$, and for the total gas density along the line of sight to be relatively low $< 2.61 \bar{n}_{\text{H}}$. Including an ionising background alleviates the need for a high f_{esc} and steep β , but still requires a relatively low gas density.

Detailed measurements of Ly α lineshapes and velocity offsets can be used to constrain the properties of reionised regions, including to place lower limits on ionised bubble sizes. With rest-UV – optical spectroscopy with, e.g., the James Webb Space Telescope (*JWST*) these methods enable direct comparison between galaxy properties and their ionised regions.

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