



**Computer session: yield prediction,
simulation of the genotype \times environment
interaction with an Excel version of APSIM**

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*Training course
Environment & Traits*

Light-limited conditions

$$\Delta \text{Biomass (g/m}^2\text{/day)} = Q \times \text{LI} \times \text{RUE} \quad [1]$$

where Q = incident radiation (MJ/m²/day)

LI = light intercepted by the canopy (MJ/m²/day)

RUE = radiation use efficiency (g/MJ)

$$\text{LI} = (1 - e^{-k \cdot \text{LAI}})$$

where LAI = canopy leaf area index (m² leaf/m² ground area)

k = light extinction coefficient

Water-limited conditions

$$\Delta \text{Biomass (g/m}^2\text{/day)} = T \times TE \quad [2]$$

where T = crop transpiration (mm/day)

TE = transpiration efficiency (g/m²/mm)

$$TE = TE_c / (vpd/10)$$

where vpd = vapour pressure deficit of the atmosphere (hPa), and

TE_c = transpiration efficiency coefficient (Pa)

10 = conversion from hPa to Pa ($\times 100$) and g/g to g/m²/mm ($\div 1000$)

Balance between potential crop water supply and crop water use

Non limiting water supply

When water supply is non limiting, equating [1] and [2] gives the potential transpiration:

$$\Delta \text{Biomass} = Q \times \text{LI} \times \text{RUE} \quad [1]$$

$$\Delta \text{Biomass} = T \times \text{TE} \quad [2]$$

$$T = \text{Potential Demand} = Q \cdot (1 - e^{-k \cdot \text{LAI}}) \cdot \text{RUE} / (\text{TE}_c / (\text{vpd}/10)) \quad [3]$$

In which we find some analogies with the Penman Monteith equation :

$$J_w = \frac{s(\phi_n) + \rho_a c_p \text{VPD}_{air} g_a}{\lambda [s + \gamma (1 + g_a / g_s)]}$$

Balance between potential crop water supply and crop water use

Limiting water supply

Available Soil Water (mm): $ASW = sw - ll$

where sw = soil water content

ll = lower limit of soil water content

Root Depth (cm) = $DAS * \text{Root Growth Rate}$

where DAS = days after sowing

Root Growth Rate (cm / day)

Potential Supply by a layer (PS_{layer}) = $\%RootOccupancy * ASW * kl$

where kl = extraction rate constant from the crop

Potential Supply = $\sum PS_{layer}$

$\sum PS_{layer}$ equals crop transpiration (T) when water supply is limiting

Balance between potential crop water supply and crop water use

How to derive potential supply:

Extraction of soil water from a layer can be described by an exponential decay of volumetric soil water content (q , cm^3/cm^3) with time (t , days) -

$$\theta = (\theta_u - \theta_l).e^{-kl.t}$$

where θ_u and θ_l are water content at ul and ll, respectively.

$$\begin{aligned}\text{So, } d\theta/dt &= -kl.(\theta_u - \theta_l).e^{-kl.t} \\ &= -kl.\theta\end{aligned}$$

Balance between potential crop water supply and crop water use

Summing over successive days:

T is determined via equation [3] or [4] depending on whether the day was light (demand) or water (supply) limited:

Transpiration = Minimum(Potential Supply, Potential Demand)

The ratio of Potential Supply to Potential Demand (S/D) can be used as an indicator:

S/D < 1 means water-limited conditions

S/D ≥ 1 means light-limited conditions

Biomass increment is then evaluated using [1] or [2] (depending on S/D)