

## Scale mixture 分布

把分布写成  
高斯与另一个更  
简单分布的混  
合体, 方便计算.

- Scale mixture 高斯.

$$\int_0^\infty N(x | \mu, \frac{\delta^2}{r}) \overset{\text{分布}}{Ga}(r | \frac{\nu}{2}, \frac{\nu}{2}) \overset{\text{权重}}{dr}$$

$$= \int_0^\infty \frac{r^{-\frac{1}{2}}}{\sqrt{2\pi}\delta} \exp\left(-\frac{(x-\mu)^2}{2\delta^2} r\right) \frac{(\frac{\nu}{2})^{\frac{\nu}{2}}}{\Gamma(\frac{\nu}{2})} r^{\frac{\nu}{2}-1} \exp\left(-\frac{\nu r}{2}\right) dr.$$

- Laplace 分布

$$f(x) = \frac{1}{4\delta} \exp\left(-\frac{|x-\mu|}{2\delta}\right)$$

$$= \int \frac{1}{2\pi r} \overset{\text{高斯}}{\exp\left(-\frac{1}{2r}(x-\mu)^2\right)} \overset{\text{指数分布}}{\frac{1}{2\delta^2} \exp\left(-\frac{1}{2\delta^2} r\right)} dr$$

- NB 分布

$$\int_0^\infty f_{\text{Poisson}}(k) f_{\text{Gamma}}(r, \frac{1-p}{p}) dr$$

$$= \int_0^\infty \frac{\lambda^k}{k!} e^{-\lambda}.$$



