

Model

- in general I want to estimate something like

$$\Delta C_{it} = \theta(X_{it})R_{it} + g(X_{it}, W_{it}) + \epsilon_{it}$$

$$R_{it} = h(X_{it}, W_{it}) + u_{it}$$

- individual level fixed effect is NOT necessary because looking at first difference of C_{it}
- what about seasonality?

Seasonality

- in linear model use dummies or demean by period averages
- demeaning approach not valid in semi-parametric approach because this

$$\begin{aligned}\Delta C_{it} - \frac{1}{N} \sum_{i=1}^N \Delta C_{it} &= \theta(X_{it})R_{it} - \frac{1}{N} \sum_{i=1}^N \theta(X_{it})R_{it} \\ &\quad + g(X_{it}, W_{it}) - \frac{1}{N} \sum_{i=1}^N g(X_{it}, W_{it}) \\ &\quad + \epsilon_{it}\end{aligned}\tag{1}$$

Seasonality

- is not feasible: unnecessarily hard to interpret and estimate - inference results no longer valid because I would have to adjust the whole estimator (and thus covariance matrix)
- however, just demeaning data results in

$$\begin{aligned}\Delta \hat{C}_{it} &= \theta(\hat{X}_{it})\hat{R}_{it} + g(\hat{X}_{it}, \hat{W}_{it}) + \epsilon_{it} \\ \hat{R}_{it} &= h(\hat{X}_{it}, \hat{W}_{it}) + u_{it}\end{aligned}$$

- where $\hat{X} = X_{it} - \frac{1}{N} \sum_{t=1}^N X_{it}$
- which is only equal to (1) if $g(\cdot, \cdot)$ and $h(\cdot, \cdot)$ are linear and θ doesn't depend on X_{it}

Seasonality

- for individual level fixed effects econML docs suggest to simply throw the OneHotEncoded dummies into the estimator
- is this a feasible option for the monthly dummies, too? After all, why shouldn't it be?
- when throwing them in actually also able to catch interactions between month and observables - maybe having children plays a larger role in winter etc...