

```
In [1]: # ANOVA Monofactorial
```

```
# 1. Carga inicial de datos:
```

```
if(!require(psych)){install.packages("psych")}
if(!require(FSA)){install.packages("FSA")}
if(!require(Rmisc)){install.packages("Rmisc")}
if(!require(ggplot2)){install.packages("ggplot2")}
if(!require(car)){install.packages("car")}
if(!require(multcompView)){install.packages("multcompView")}
if(!require(multcompView)){install.packages("multcomp")}
if(!require(lsmmeans)){install.packages("lsmmeans")}
if(!require(rcompanion)){install.packages("rcompanion")}
```

```
Datos <- ("
```

| Algoritmo | Ejecucion | Puntaje |
|-----------|-----------|---------|
| 'ERA' | '1' | 45033 |
| 'ERA' | '2' | 46623 |
| 'ERA' | '3' | 43845 |
| 'ERA' | '4' | 48849 |
| 'ERA' | '5' | 45471 |
| 'ERA' | '6' | 47132 |
| 'ERA' | '7' | 46175 |
| 'ERA' | '8' | 44015 |
| 'ERA' | '9' | 46189 |
| 'ERA' | '10' | 48499 |
| 'ERA' | '11' | 42445 |
| 'ERA' | '12' | 49155 |
| 'ERA' | '13' | 48019 |
| 'ERA' | '14' | 49068 |
| 'ERA' | '15' | 42040 |
| 'ERA' | '16' | 42538 |
| 'ERA' | '17' | 44734 |
| 'ERA' | '18' | 49899 |
| 'ERA' | '19' | 47471 |
| 'ERA' | '20' | 42966 |
| 'ERA' | '21' | 42895 |
| 'ERA' | '22' | 49284 |
| 'ERA' | '23' | 45463 |
| 'ERA' | '24' | 48812 |
| 'ERA' | '25' | 43817 |
| 'ERA' | '26' | 42326 |
| 'ERA' | '27' | 43323 |
| 'ERA' | '28' | 43482 |
| 'ERA' | '29' | 44474 |
| 'ERA' | '30' | 48576 |
| 'ERA' | '31' | 42984 |
| 'ERA' | '32' | 42914 |
| 'ERA' | '33' | 48492 |
| 'ERA' | '34' | 44776 |
| 'ERA' | '35' | 48997 |
| 'ERA' | '36' | 42966 |
| 'ERA' | '37' | 42632 |
| 'ERA' | '38' | 48334 |
| 'ERA' | '39' | 45233 |
| 'ERA' | '40' | 43456 |
| 'ERA' | '41' | 46802 |
| 'ERA' | '42' | 45332 |
| 'ERA' | '43' | 43422 |
| 'ERA' | '44' | 46946 |
| 'ERA' | '45' | 42401 |
| 'ERA' | '46' | 43473 |
| 'ERA' | '47' | 45527 |
| 'ERA' | '48' | 42785 |
| 'ERA' | '49' | 47040 |
| 'ERA' | '50' | 46662 |
| 'ERA' | '51' | 49270 |
| 'ERA' | '52' | 45591 |
| 'ERA' | '53' | 46501 |
| 'ERA' | '54' | 48277 |
| 'ERA' | '55' | 47178 |
| 'ERA' | '56' | 47658 |
| 'ERA' | '57' | 49259 |
| 'ERA' | '58' | 46043 |
| 'ERA' | '59' | 46578 |

| | | |
|-------|------|-------|
| 'ERA' | '60' | 45165 |
| 'CFS' | '1' | 42906 |
| 'CFS' | '2' | 43517 |
| 'CFS' | '3' | 42032 |
| 'CFS' | '4' | 41393 |
| 'CFS' | '5' | 42820 |
| 'CFS' | '6' | 44951 |
| 'CFS' | '7' | 41741 |
| 'CFS' | '8' | 45950 |
| 'CFS' | '9' | 42535 |
| 'CFS' | '10' | 44958 |
| 'CFS' | '11' | 44690 |
| 'CFS' | '12' | 40945 |
| 'CFS' | '13' | 44157 |
| 'CFS' | '14' | 44550 |
| 'CFS' | '15' | 42781 |
| 'CFS' | '16' | 43145 |
| 'CFS' | '17' | 43578 |
| 'CFS' | '18' | 44312 |
| 'CFS' | '19' | 45834 |
| 'CFS' | '20' | 44558 |
| 'CFS' | '21' | 42529 |
| 'CFS' | '22' | 44373 |
| 'CFS' | '23' | 46034 |
| 'CFS' | '24' | 42572 |
| 'CFS' | '25' | 41411 |
| 'CFS' | '26' | 45356 |
| 'CFS' | '27' | 44186 |
| 'CFS' | '28' | 43339 |
| 'CFS' | '29' | 45815 |
| 'CFS' | '30' | 43666 |
| 'CFS' | '31' | 45324 |
| 'CFS' | '32' | 45427 |
| 'CFS' | '33' | 41425 |
| 'CFS' | '34' | 43171 |
| 'CFS' | '35' | 40805 |
| 'CFS' | '36' | 41931 |
| 'CFS' | '37' | 40793 |
| 'CFS' | '38' | 41542 |
| 'CFS' | '39' | 45018 |
| 'CFS' | '40' | 41054 |
| 'CFS' | '41' | 44277 |
| 'CFS' | '42' | 45672 |
| 'CFS' | '43' | 46409 |
| 'CFS' | '44' | 43394 |
| 'CFS' | '45' | 43966 |
| 'CFS' | '46' | 46300 |
| 'CFS' | '47' | 46196 |
| 'CFS' | '48' | 42279 |
| 'CFS' | '49' | 45212 |
| 'CFS' | '50' | 43758 |
| 'CFS' | '51' | 43222 |
| 'CFS' | '52' | 41552 |
| 'CFS' | '53' | 41354 |
| 'CFS' | '54' | 45633 |
| 'CFS' | '55' | 44274 |
| 'CFS' | '56' | 41765 |
| 'CFS' | '57' | 45777 |
| 'CFS' | '58' | 45205 |
| 'CFS' | '59' | 42317 |
| 'CFS' | '60' | 41959 |
| 'ULE' | '1' | 45512 |
| 'ULE' | '2' | 42095 |
| 'ULE' | '3' | 41297 |
| 'ULE' | '4' | 43138 |
| 'ULE' | '5' | 40823 |
| 'ULE' | '6' | 43642 |
| 'ULE' | '7' | 40638 |
| 'ULE' | '8' | 44984 |
| 'ULE' | '9' | 43633 |
| 'ULE' | '10' | 42653 |
| 'ULE' | '11' | 41374 |
| 'ULE' | '12' | 41558 |
| 'ULE' | '13' | 41849 |
| 'ULE' | '14' | 45989 |
| 'ULE' | '15' | 42002 |

| | | |
|-------------|------|-------|
| 'ULE' | '16' | 44388 |
| 'ULE' | '17' | 41622 |
| 'ULE' | '18' | 42974 |
| 'ULE' | '19' | 44685 |
| 'ULE' | '20' | 44343 |
| 'ULE' | '21' | 43707 |
| 'ULE' | '22' | 45049 |
| 'ULE' | '23' | 42358 |
| 'ULE' | '24' | 40590 |
| 'ULE' | '25' | 45059 |
| 'ULE' | '26' | 40714 |
| 'ULE' | '27' | 42034 |
| 'ULE' | '28' | 45881 |
| 'ULE' | '29' | 40350 |
| 'ULE' | '30' | 41908 |
| 'ULE' | '31' | 41146 |
| 'ULE' | '32' | 40614 |
| 'ULE' | '33' | 40719 |
| 'ULE' | '34' | 40340 |
| 'ULE' | '35' | 42265 |
| 'ULE' | '36' | 45164 |
| 'ULE' | '37' | 44624 |
| 'ULE' | '38' | 45495 |
| 'ULE' | '39' | 44174 |
| 'ULE' | '40' | 40461 |
| 'ULE' | '41' | 44851 |
| 'ULE' | '42' | 45542 |
| 'ULE' | '43' | 42928 |
| 'ULE' | '44' | 45616 |
| 'ULE' | '45' | 45940 |
| 'ULE' | '46' | 45587 |
| 'ULE' | '47' | 45573 |
| 'ULE' | '48' | 41625 |
| 'ULE' | '49' | 40204 |
| 'ULE' | '50' | 43319 |
| 'ULE' | '51' | 41055 |
| 'ULE' | '52' | 40471 |
| 'ULE' | '53' | 43741 |
| 'ULE' | '54' | 43889 |
| 'ULE' | '55' | 40335 |
| 'ULE' | '56' | 40163 |
| 'ULE' | '57' | 45193 |
| 'ULE' | '58' | 40631 |
| 'ULE' | '59' | 40973 |
| 'ULE' | '60' | 42638 |
| 'Monotonic' | '1' | 32490 |
| 'Monotonic' | '2' | 39163 |
| 'Monotonic' | '3' | 32927 |
| 'Monotonic' | '4' | 38382 |
| 'Monotonic' | '5' | 33590 |
| 'Monotonic' | '6' | 39663 |
| 'Monotonic' | '7' | 32283 |
| 'Monotonic' | '8' | 32621 |
| 'Monotonic' | '9' | 37613 |
| 'Monotonic' | '10' | 37005 |
| 'Monotonic' | '11' | 35527 |
| 'Monotonic' | '12' | 39317 |
| 'Monotonic' | '13' | 32426 |
| 'Monotonic' | '14' | 36812 |
| 'Monotonic' | '15' | 32478 |
| 'Monotonic' | '16' | 35713 |
| 'Monotonic' | '17' | 37565 |
| 'Monotonic' | '18' | 32738 |
| 'Monotonic' | '19' | 38524 |
| 'Monotonic' | '20' | 33706 |
| 'Monotonic' | '21' | 39618 |
| 'Monotonic' | '22' | 34218 |
| 'Monotonic' | '23' | 35823 |
| 'Monotonic' | '24' | 35597 |
| 'Monotonic' | '25' | 39642 |
| 'Monotonic' | '26' | 33650 |
| 'Monotonic' | '27' | 33173 |
| 'Monotonic' | '28' | 33812 |
| 'Monotonic' | '29' | 38799 |
| 'Monotonic' | '30' | 36139 |
| 'Monotonic' | '31' | 32847 |

```

'Monotonic'      '32'      39100
'Monotonic'      '33'      35042
'Monotonic'      '34'      38256
'Monotonic'      '35'      39075
'Monotonic'      '36'      36629
'Monotonic'      '37'      35159
'Monotonic'      '38'      38597
'Monotonic'      '39'      34461
'Monotonic'      '40'      35573
'Monotonic'      '41'      38843
'Monotonic'      '42'      34925
'Monotonic'      '43'      33918
'Monotonic'      '44'      33043
'Monotonic'      '45'      36867
'Monotonic'      '46'      33323
'Monotonic'      '47'      38749
'Monotonic'      '48'      39796
'Monotonic'      '49'      37803
'Monotonic'      '50'      38739
'Monotonic'      '51'      36559
'Monotonic'      '52'      38500
'Monotonic'      '53'      35794
'Monotonic'      '54'      39715
'Monotonic'      '55'      38674
'Monotonic'      '56'      35441
'Monotonic'      '57'      34091
'Monotonic'      '58'      32393
'Monotonic'      '59'      32975
'Monotonic'      '60'      38212
")

# Lectura de Los datos
Data <- read.table(textConnection(Datos), header=TRUE)
# Ordenar Los datos segun Los ingresamos
Data$Algoritmo <- factor(Data$Algoritmo, levels = unique(Data$Algoritmo))

# 2. Lectura de datos / Verificación de Lectura

library(psych)
headTail(Data)
str(Data)
summary(Data)
rm(Datos)

# 3. Resumen organizado

Summarize(Puntaje ~ Algoritmo, data = Data, digits = 4)

# 4. Diagrama de cajas

M <- tapply(Data$Puntaje, INDEX = Data$Algoritmo, FUN = mean)
boxplot(Puntaje ~ Algoritmo, data = Data)
points(M, col = "red", pch = "+", cex = 2)

# 5. Información de promedios e intervalos de confianza

Sum <- groupwiseMean(Puntaje ~ Algoritmo, data = Data, conf = 0.95, digits = 3, traditional = FALSE, percent
Sum

# 6. Gráficos de promedios e intervalos de confianza

library(ggplot2)
ggplot(Sum,
  aes(x = Algoritmo, y = Mean)) +
  geom_errorbar(aes(ymin = Percentile.lower,
    ymax = Percentile.upper),
    width = 0.05, size = 0.5) +
  geom_point(shape = 15,
    size = 4) +
  theme_bw() +
  theme(axis.title = element_text(face = "bold")) +
  ylab("Puntaje promedio, s")

# Validacion de supuestos de ANOVA
# Supuesto de normalidad y homocedasticidad

```

```

# 7. Modelo Lineal

model <- lm(Puntaje ~ Algoritmo, data = Data)
summary(model)

# 8. Histograma de residuos

X <- residuals(model)
library(rcompanion)
dev.new()
# Para evitar error "figure margins too large"
windows.options(width = 10, height = 8)
plotNormalHistogram(X)
# Los residuos son normales

# 9. Dispersión de residuos

plot(fitted(model), residuals(model))
# La dispersion es la misma

# 10. Gráficos del modelo lineal

plot(model)

# Se cumplen los supuestos

# 11. ANOVA

library(car)
Anova(model, type = "II")

# P-Value < alpha -> Se rechaza H0

# -----

# Ajuste de promedios | Mínimos cuadrados | Post-Hoc

# 1. Separación de promedios

library(multcompView)
library(lsmeans)
marginal <- lsmeans(model, ~ Algoritmo)
pairs(marginal, adjust="tukey")

# 2. Visión compacta

library(multcomp)
CLD <- cld(marginal, alpha=0.05, Letters = letters, adjust = "tukey")
CLD

# Ordenamos los niveles para imprimirlos
CLD$Algoritmo <- factor(CLD$Algoritmo, levels = c("ERA", "CFS", "ULE", "Monotonic"))
# Removemos espacios en blanco
CLD$.group <- gsub(" ", "", CLD$.group)

# Era estadísticamente distinto a CFS, ULE y Monotonic
# CFS y ULE estadísticamente equivalentes.
# Monotonic estadísticamente distinto a CFS, ULE y Monotonic

library(ggplot2)
ggplot(CLD,
  aes( x = Algoritmo,
        y = lsmean,
        label = .group)) +
  geom_point(shape = 15, size = 4) +
  geom_errorbar(aes(ymin = lower.CL,
                    ymax = upper.CL),
                width = 0.2,
                size = 0.7) +
  theme_bw() +
  theme(axis.title = element_text(face = "bold"),
        axis.text = element_text(face = "bold"),
        plot.caption = element_text(hjust = 0)) +
  ylab("Promedio del mínimo cuadrado \n
        Tiempo de ejecución") +

```

```
geom_text(nudge_x = c(0,0,0),  
          nudge_y = c(1100, 1100, 1100),  
          color = "black")
```

Loading required package: psych

Loading required package: FSA

FSA v0.9.4. See citation('FSA') if used in publication.
Run fishR() for related website and fishR('IFAR') for related book.

Attaching package: 'FSA'

The following object is masked from 'package:psych':

headtail

Loading required package: Rmisc

Loading required package: lattice

Loading required package: plyr

Attaching package: 'plyr'

The following object is masked from 'package:FSA':

mapvalues

Loading required package: ggplot2

Attaching package: 'ggplot2'

The following objects are masked from 'package:psych':

%+%, alpha

Loading required package: car

Loading required package: carData

Registered S3 methods overwritten by 'car':

| | |
|--------------|------|
| method | from |
| hist.boot | FSA |
| confint.boot | FSA |

Attaching package: 'car'

The following object is masked from 'package:FSA':

bootCase

The following object is masked from 'package:psych':

logit

Loading required package: multcompView

Loading required package: lsmeans

Loading required package: emmeans

The 'lsmeans' package is now basically a front end for 'emmeans'.
Users are encouraged to switch the rest of the way.
See help('transition') for more information, including how to
convert old 'lsmeans' objects and scripts to work with 'emmeans'.

Loading required package: rcompanion

Attaching package: 'rcompanion'

The following object is masked from 'package:psych':

phi

A data.frame: 9 × 3

| | Algoritmo | Ejecucion | Puntaje |
|-----|-----------|-----------|---------|
| | <fct> | <chr> | <chr> |
| 1 | ERA | 1 | 45033 |
| 2 | ERA | 2 | 46623 |
| 3 | ERA | 3 | 43845 |
| 4 | ERA | 4 | 48849 |
| ... | NA | ... | ... |
| 237 | Monotonic | 57 | 34091 |
| 238 | Monotonic | 58 | 32393 |
| 239 | Monotonic | 59 | 32975 |
| 240 | Monotonic | 60 | 38212 |

'data.frame': 240 obs. of 3 variables:

```
$ Algoritmo: Factor w/ 4 levels "ERA","CFS","ULE",...: 1 1 1 1 1 1 1 1 1 1 ...
$ Ejecucion: int 1 2 3 4 5 6 7 8 9 10 ...
$ Puntaje : int 45033 46623 43845 48849 45471 47132 46175 44015 46189 48499 ...

  Algoritmo Ejecucion Puntaje
ERA      :60  Min.   : 1.00  Min.   :32283
CFS      :60  1st Qu.:15.75  1st Qu.:40071
ULE      :60  Median :30.50  Median :42858
Monotonic:60  Mean   :30.50  Mean   :42080
          3rd Qu.:45.25  3rd Qu.:45172
          Max.   :60.00  Max.   :49899
```

A data.frame: 4 × 9

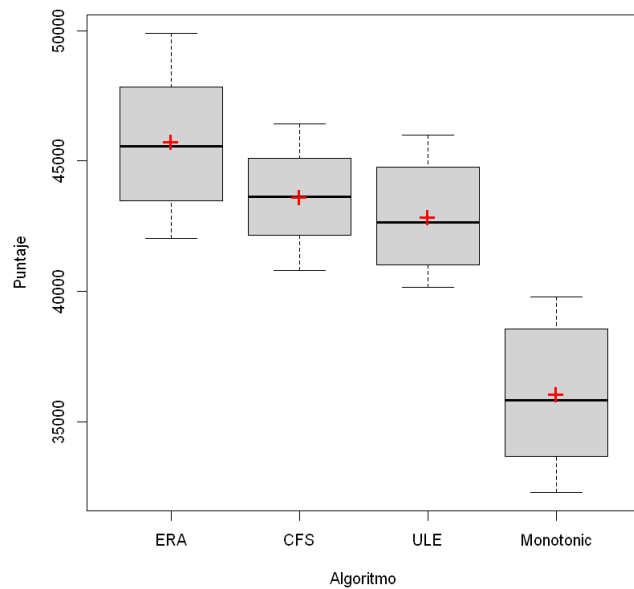
| Algoritmo | n | mean | sd | min | Q1 | median | Q3 | max |
|-----------|-------|----------|----------|-------|----------|---------|----------|-------|
| <fct> | <dbl> | <dbl> | <dbl> | <dbl> | <dbl> | <dbl> | <dbl> | <dbl> |
| ERA | 60 | 45755.20 | 2343.695 | 42040 | 43468.75 | 45559.0 | 47748.25 | 49899 |
| CFS | 60 | 43627.42 | 1664.518 | 40793 | 42217.25 | 43622.0 | 45064.75 | 46409 |
| ULE | 60 | 42868.75 | 1929.409 | 40163 | 41034.50 | 42645.5 | 44726.50 | 45989 |
| Monotonic | 60 | 36068.55 | 2503.939 | 32283 | 33692.00 | 35808.5 | 38542.25 | 39796 |

A data.frame: 4 × 6

| Algoritmo | n | Mean | Conf.level | Percentile.lower | Percentile.upper |
|-----------|-------|-------|------------|------------------|------------------|
| <fct> | <int> | <dbl> | <dbl> | <dbl> | <dbl> |
| ERA | 60 | 45800 | 0.95 | 45200 | 46300 |
| CFS | 60 | 43600 | 0.95 | 43200 | 44000 |
| ULE | 60 | 42900 | 0.95 | 42400 | 43400 |
| Monotonic | 60 | 36100 | 0.95 | 35400 | 36700 |

Warning message:

```
"Using `size` aesthetic for lines was deprecated in ggplot2 3.4.0.
i Please use `linewidth` instead."
```

Call:
lm(formula = Puntaje ~ Algoritmo, data = Data)

Residuals:

| | | | | |
|-------|-------|--------|------|------|
| Min | 1Q | Median | 3Q | Max |
| -3786 | -1948 | -190 | 1923 | 4144 |

Coefficients:

| | Estimate | Std. Error | t value | Pr(> t) |
|--------------------|----------|------------|---------|--------------|
| (Intercept) | 45755.2 | 275.8 | 165.899 | < 2e-16 *** |
| AlgoritmoCFS | -2127.8 | 390.0 | -5.455 | 1.23e-07 *** |
| AlgoritmoULE | -2886.4 | 390.0 | -7.400 | 2.37e-12 *** |
| AlgoritmoMonotonic | -9686.6 | 390.0 | -24.835 | < 2e-16 *** |

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 2136 on 236 degrees of freedom
Multiple R-squared: 0.7458, Adjusted R-squared: 0.7425
F-statistic: 230.8 on 3 and 236 DF, p-value: < 2.2e-16
A anova: 2 x 4

| | Sum Sq | Df | F value | Pr(>F) |
|------------------|------------|-------|----------|--------------|
| | <dbl> | <dbl> | <dbl> | <dbl> |
| Algoritmo | 3159675063 | 3 | 230.7698 | 6.959249e-70 |
| Residuals | 1077095280 | 236 | NA | NA |

| contrast | estimate | SE | df | t.ratio | p.value |
|-----------------|----------|-----|-----|---------|---------|
| ERA - CFS | 2128 | 390 | 236 | 5.455 | <.0001 |
| ERA - ULE | 2886 | 390 | 236 | 7.400 | <.0001 |
| ERA - Monotonic | 9687 | 390 | 236 | 24.835 | <.0001 |
| CFS - ULE | 759 | 390 | 236 | 1.945 | 0.2122 |
| CFS - Monotonic | 7559 | 390 | 236 | 19.380 | <.0001 |
| ULE - Monotonic | 6800 | 390 | 236 | 17.435 | <.0001 |

P value adjustment: tukey method for comparing a family of 4 estimates

```
Loading required package: mvtnorm

Loading required package: survival

Loading required package: TH.data

Loading required package: MASS

Attaching package: 'TH.data'

The following object is masked from 'package:MASS':

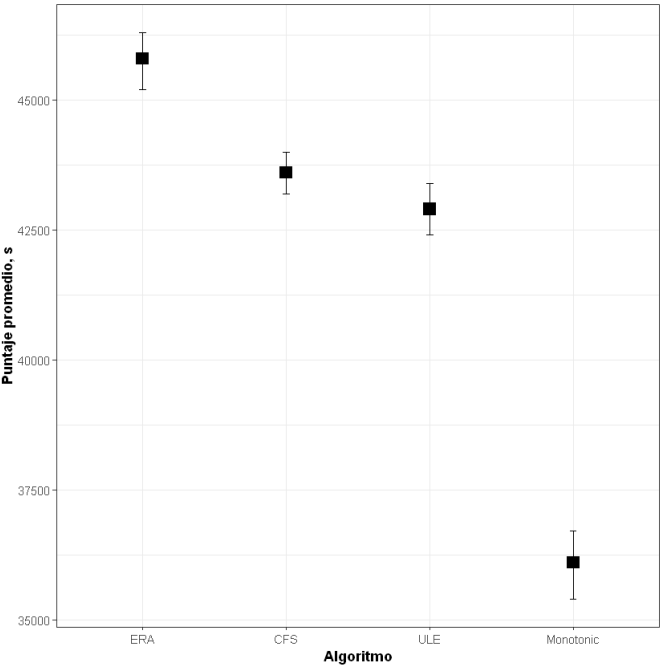
    geyser

Note: adjust = "tukey" was changed to "sidak"
because "tukey" is only appropriate for one set of pairwise comparisons
```

A summary_emm: 4 × 7

| | Algoritmo | lsmean | SE | df | lower.CL | upper.CL | .group |
|---|-----------|----------|----------|-------|----------|----------|--------|
| | <fct> | <dbl> | <dbl> | <dbl> | <dbl> | <dbl> | <chr> |
| 4 | Monotonic | 36068.55 | 275.8007 | 236 | 35376.27 | 36760.83 | a |
| 3 | ULE | 42868.75 | 275.8007 | 236 | 42176.47 | 43561.03 | b |
| 2 | CFS | 43627.42 | 275.8007 | 236 | 42935.14 | 44319.69 | b |
| 1 | ERA | 45755.20 | 275.8007 | 236 | 45062.92 | 46447.48 | c |

Warning message in y + params\$y:
"longer object length is not a multiple of shorter object length"



```
In [ ]:
```