

Multicast for coordination

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based on cdk5.net

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 - ❓ *delivery guarantees* e.g. can't make a guarantee if multicast is implemented as multiple sends and the sender fails. Can also do ordering

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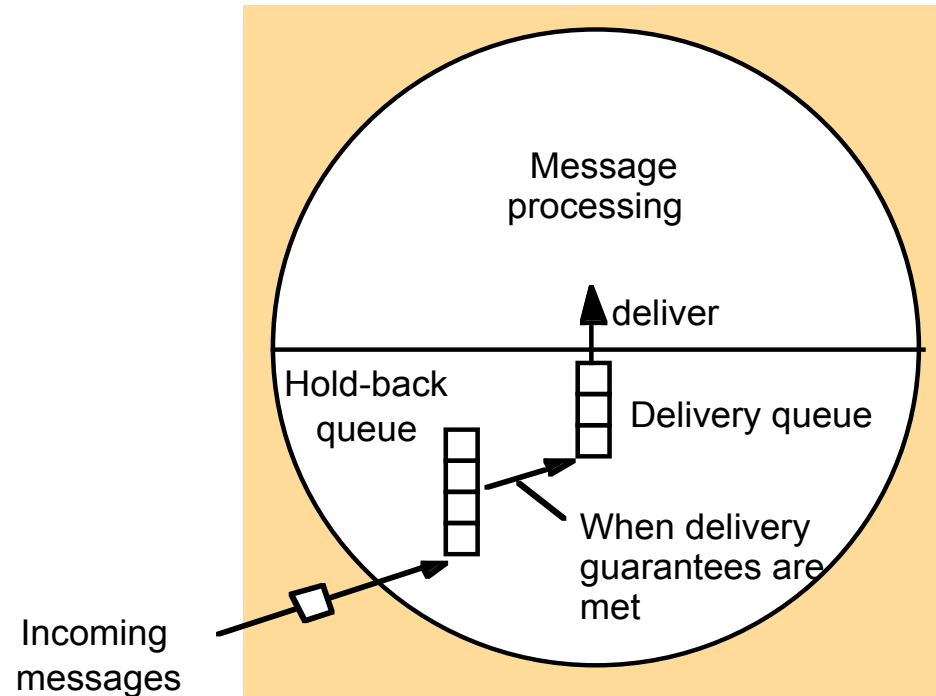
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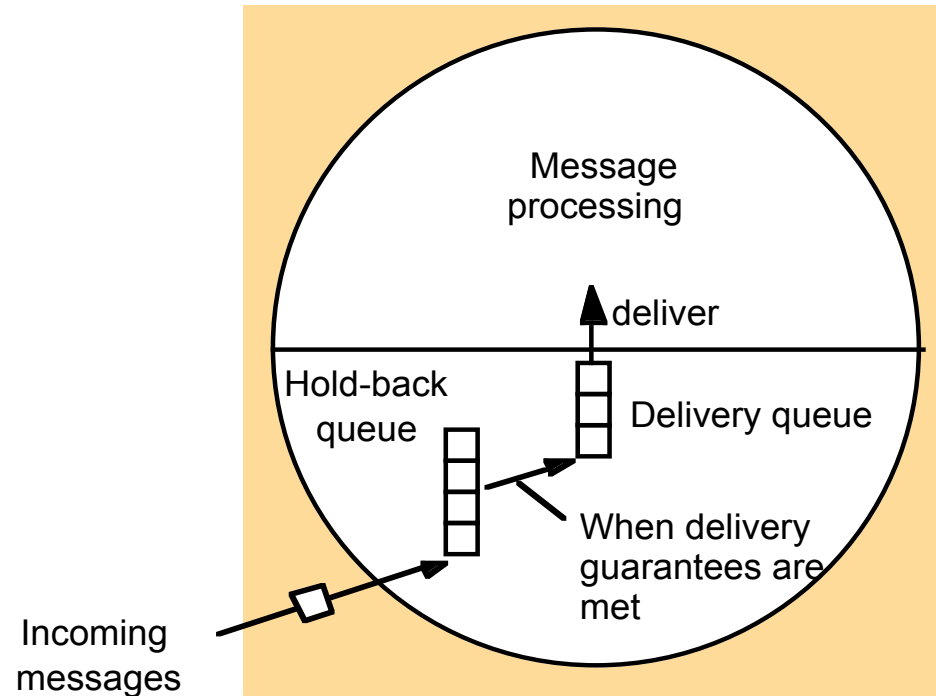
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 - ❓ IP packets may not arrive in sender order, group members can receive messages in different orders

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- [?] We assume there is no falsification of the origin and destination of messages

Open and closed groups

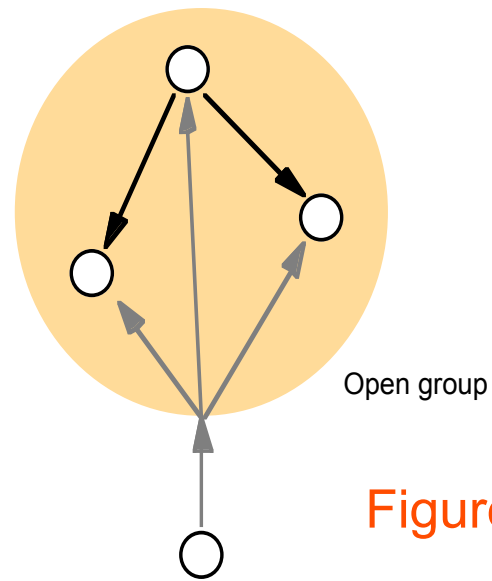
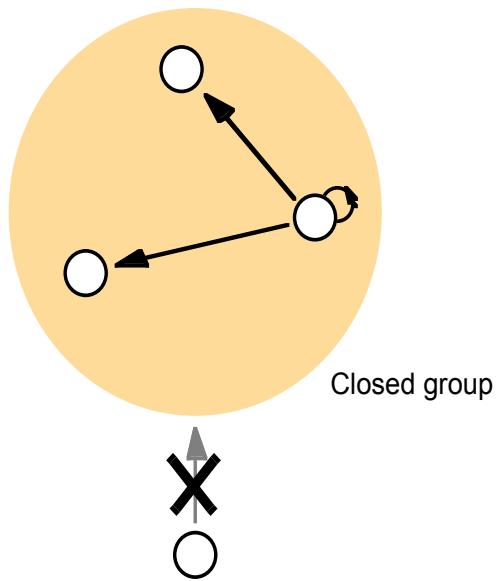


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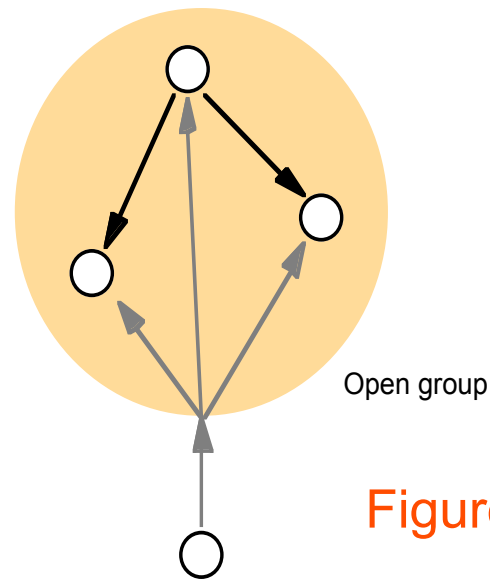
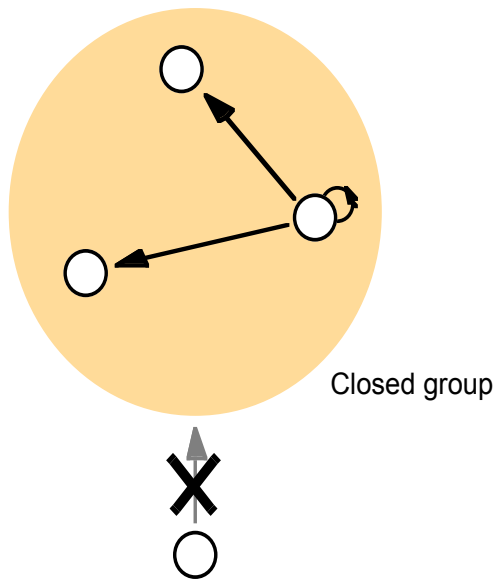


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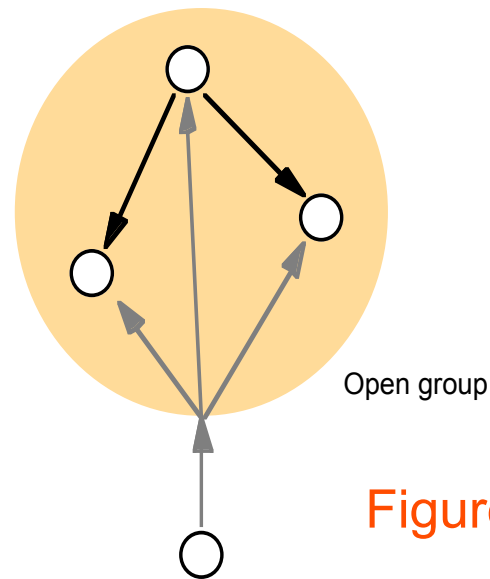
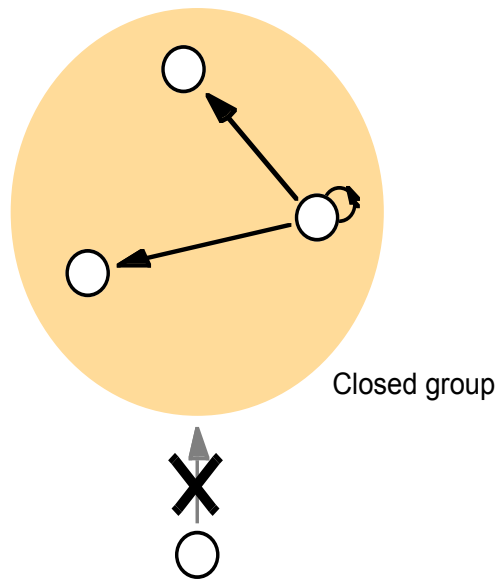


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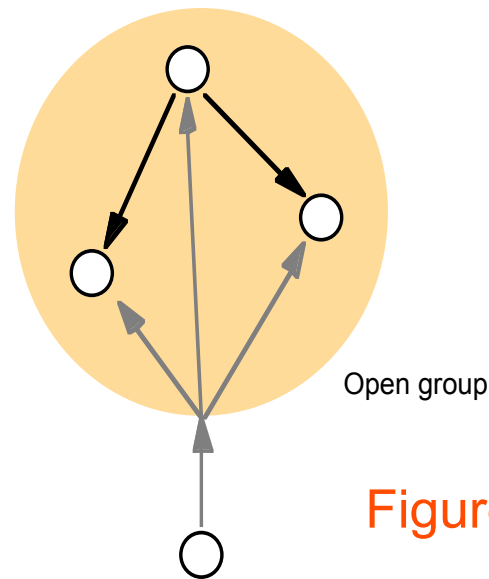
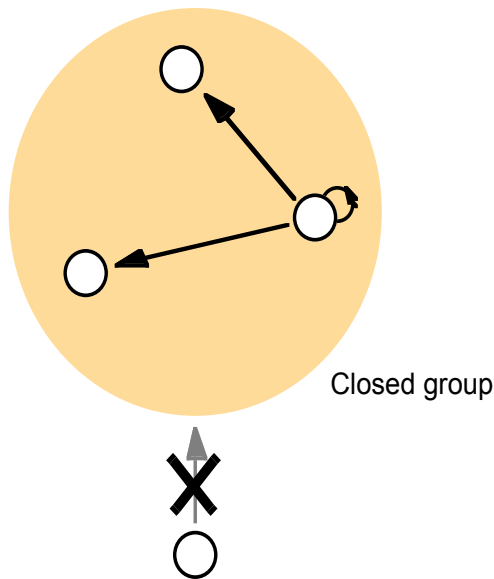


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- ♦ by use checksums, reject duplicates (e.g. due to retries).
- ♦ If considering malicious users in the system model, use security techniques

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A practical implementation of Basic Multicast may be achieved over IP multicast

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- [?] If the sender crashes, then a message may be delivered to some members of the group but not others.

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Reliable multicast

- ❑ The protocol is correct even if the multicaster crashes
- ❑ it satisfies criteria for *validity*, *integrity* and *agreement*
- ❑ it provides operations *R-multicast* and *R-deliver*
- ❑ *Integrity* - a correct process, p delivers m at most once.
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validity - simplify by choosing sender as the one process

agreement - all or nothing - atomicity, even if multicaster crashes

 processes can belong to several closed groups

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On initialization

Received := {};

Figure 11.10

For process p to R-multicast message m to group g

B-multicast(g, m); // $p \in g$ is included as a destination

On B-deliver(m) at process q with $g = \text{group}(m)$

if ($m \notin \text{Received}$)

then

Received := *Received* \cup {*m*};

if ($q \neq p$) then B-multicast(g, m); end if

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Integrity - because the reliable 1-1 channels used for *B-multicast* guarantee integrity

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What can you say about the performance of this algorithm?

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Is this algorithm correct in an asynchronous system?
algorithm?

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Reliable multicast can be implemented efficiently over IP multicast by holding back messages until every member can receive them.

Reliable multicast over IP multicast

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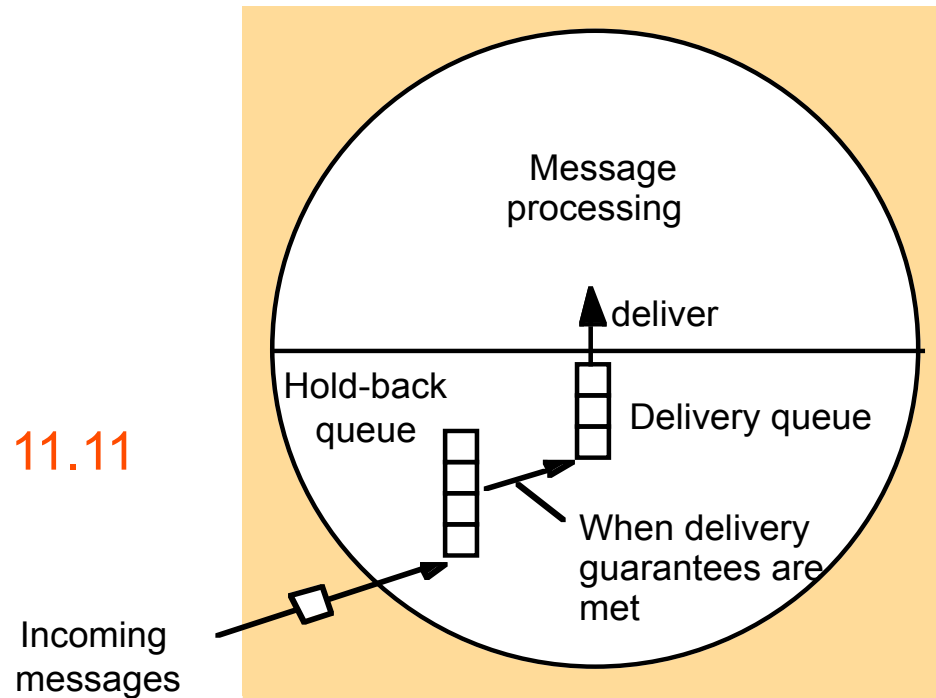
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♦ puts new message in hold-back queue for later delivery

The hold-back queue for arriving multicast messages

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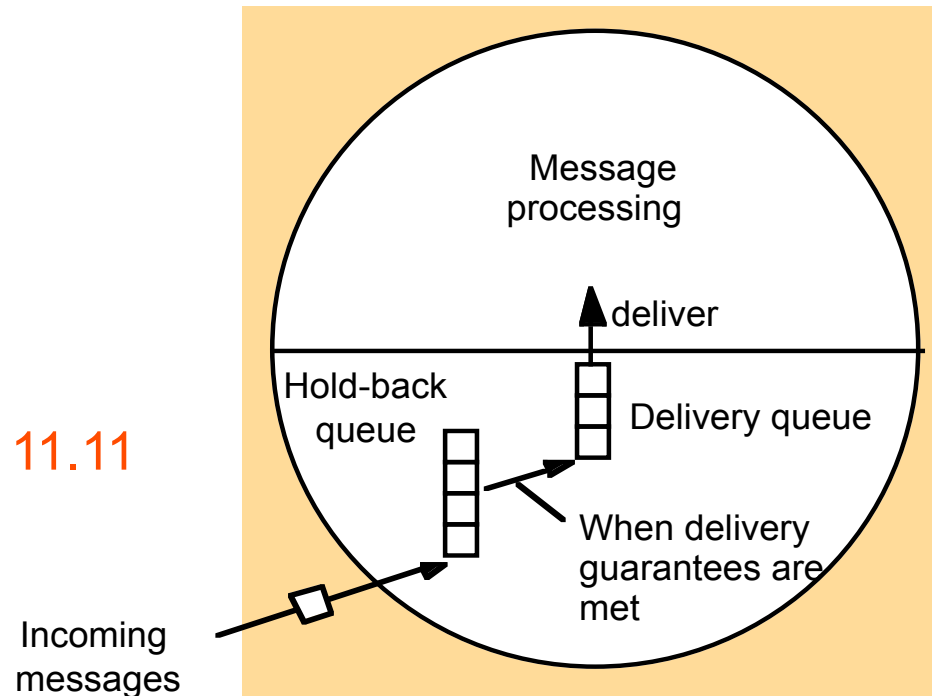
Figure 11.11



The hold-back queue for arriving multicast messages

- ?** The hold back queue is not necessary for reliability as in the implementation using IP multicast, but it simplifies the protocol, allowing sequence numbers to represent sets of messages. Hold-back queues are also used for ordering protocols.

Figure 11.11



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They must keep copies of messages they have delivered so that they can re-transmit them to others.
- ❑ discarding of copies of messages that are no longer needed :
 - ❑ when piggybacked acknowledgements arrive, note which processes have received messages. When all processes in g have the message, discard it.
 - ❑ problem of a process that stops sending - use 'heartbeat' messages.

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❓ Ordering is expensive in delivery latency and bandwidth consumption

Total, FIFO and causal ordering of multicast messages

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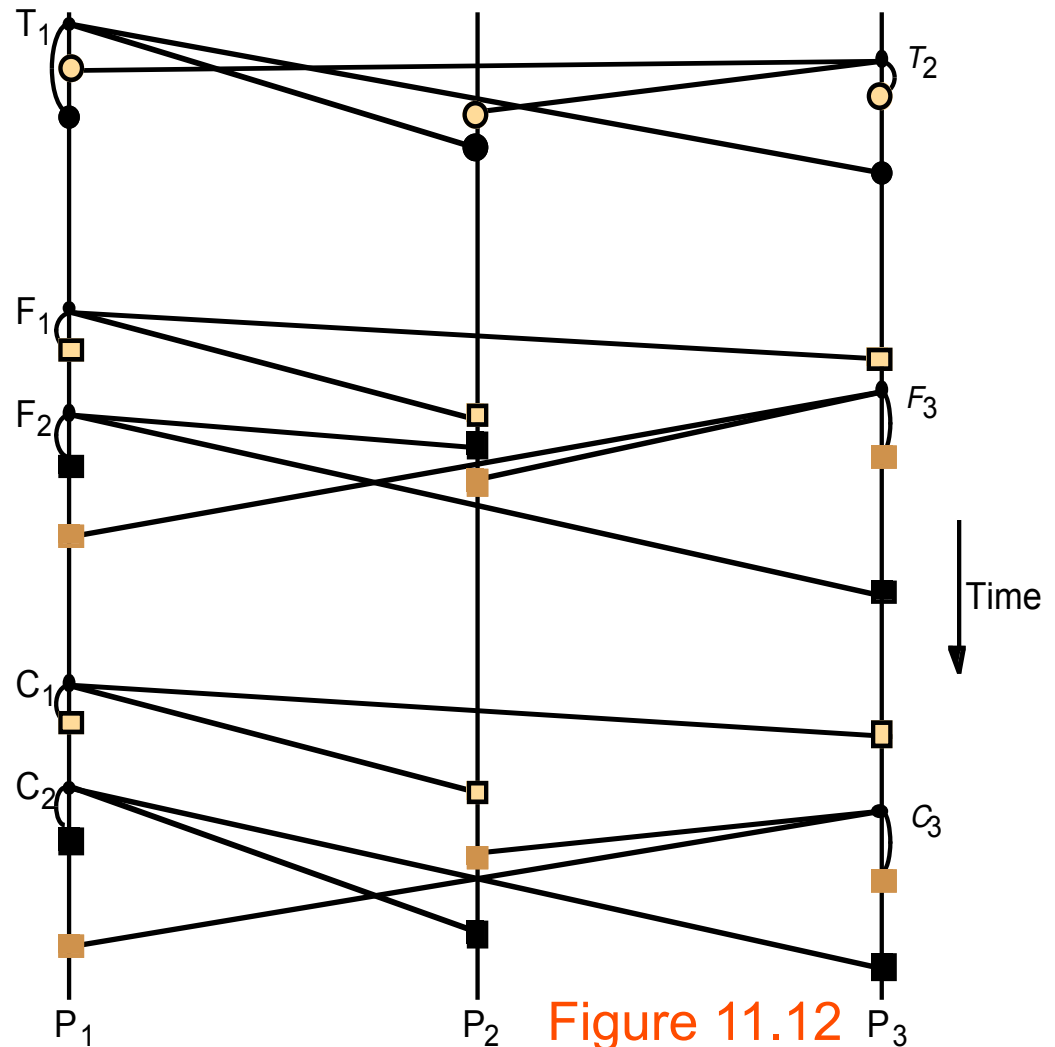


Figure 11.12

Total, FIFO and causal ordering of multicast messages

Notice the consistent ordering of totally ordered messages T_1 and T_2 . They are opposite to real time. The order can be arbitrary it need not be FIFO or causal

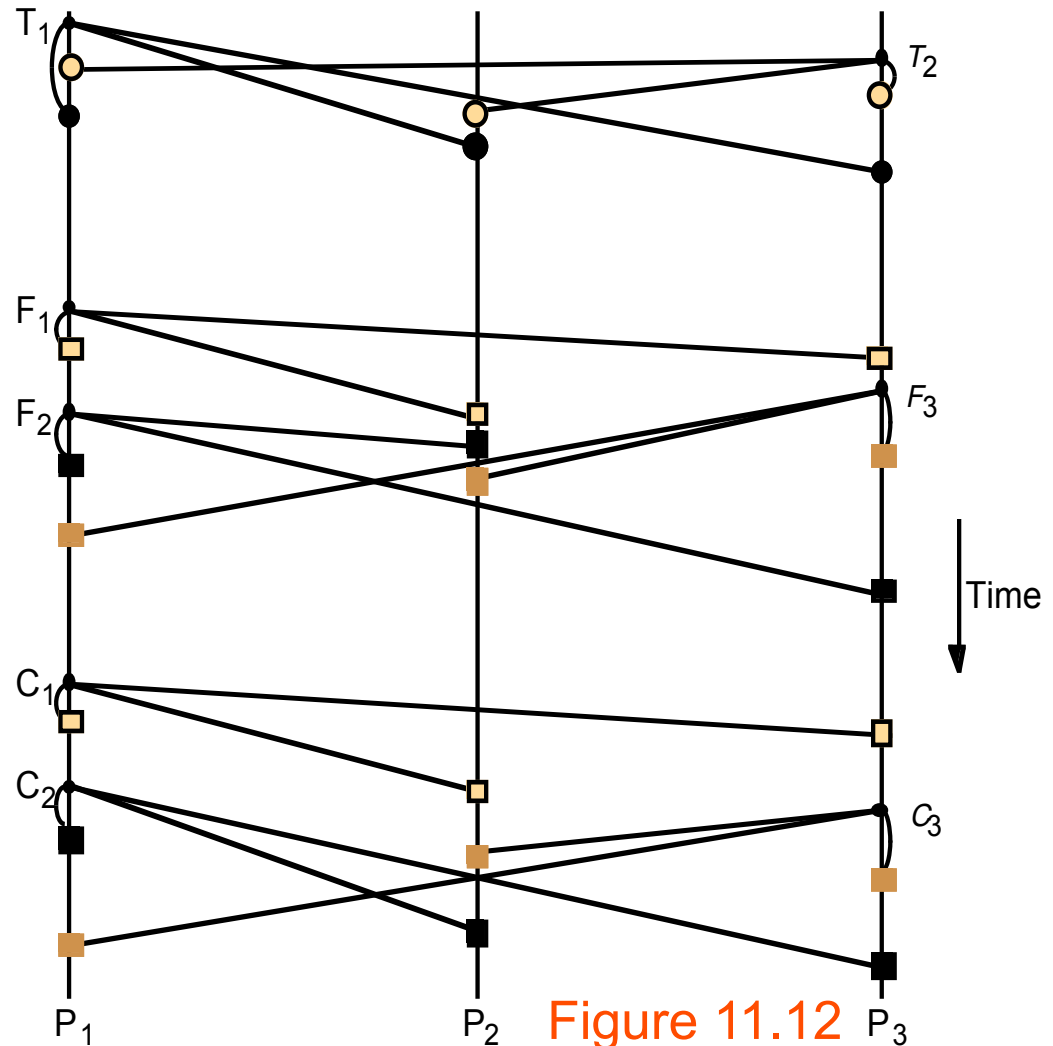
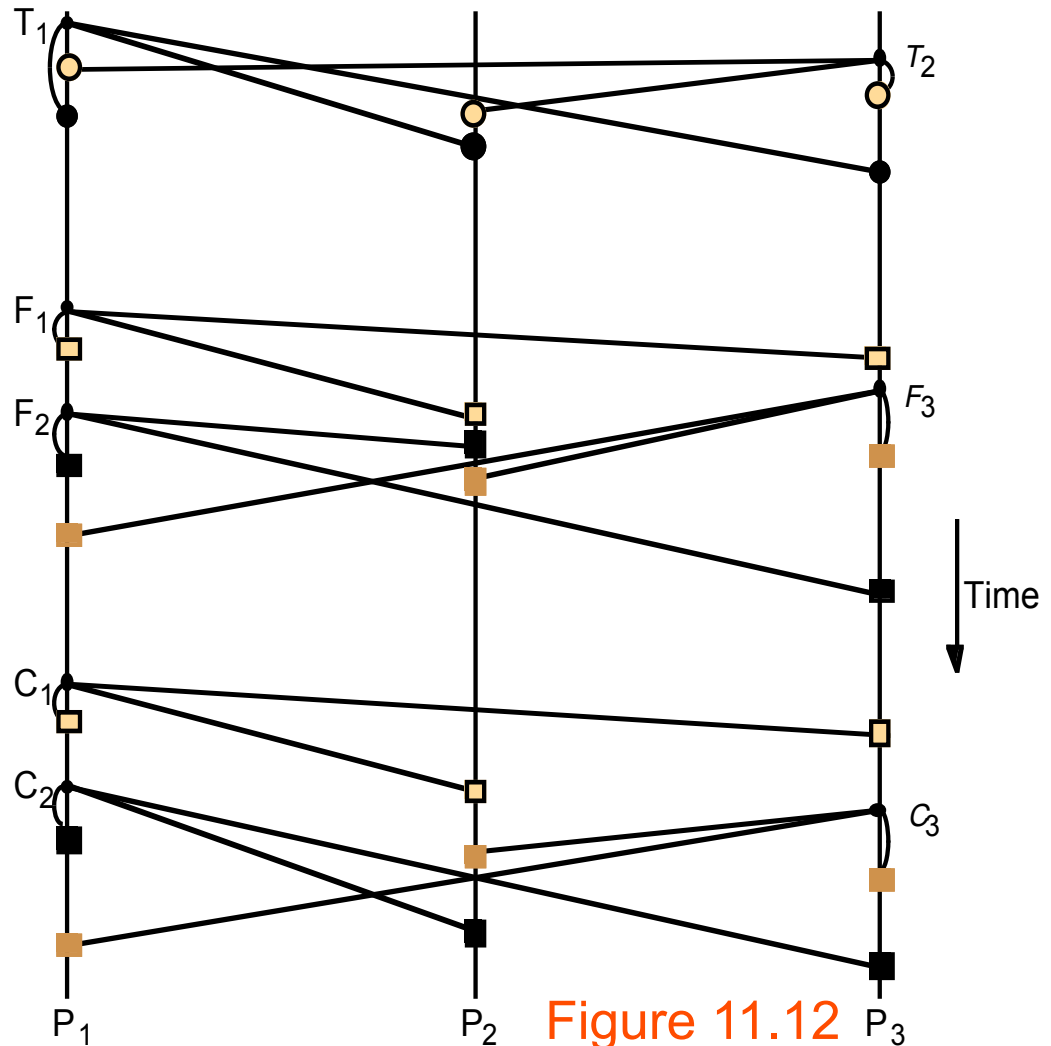


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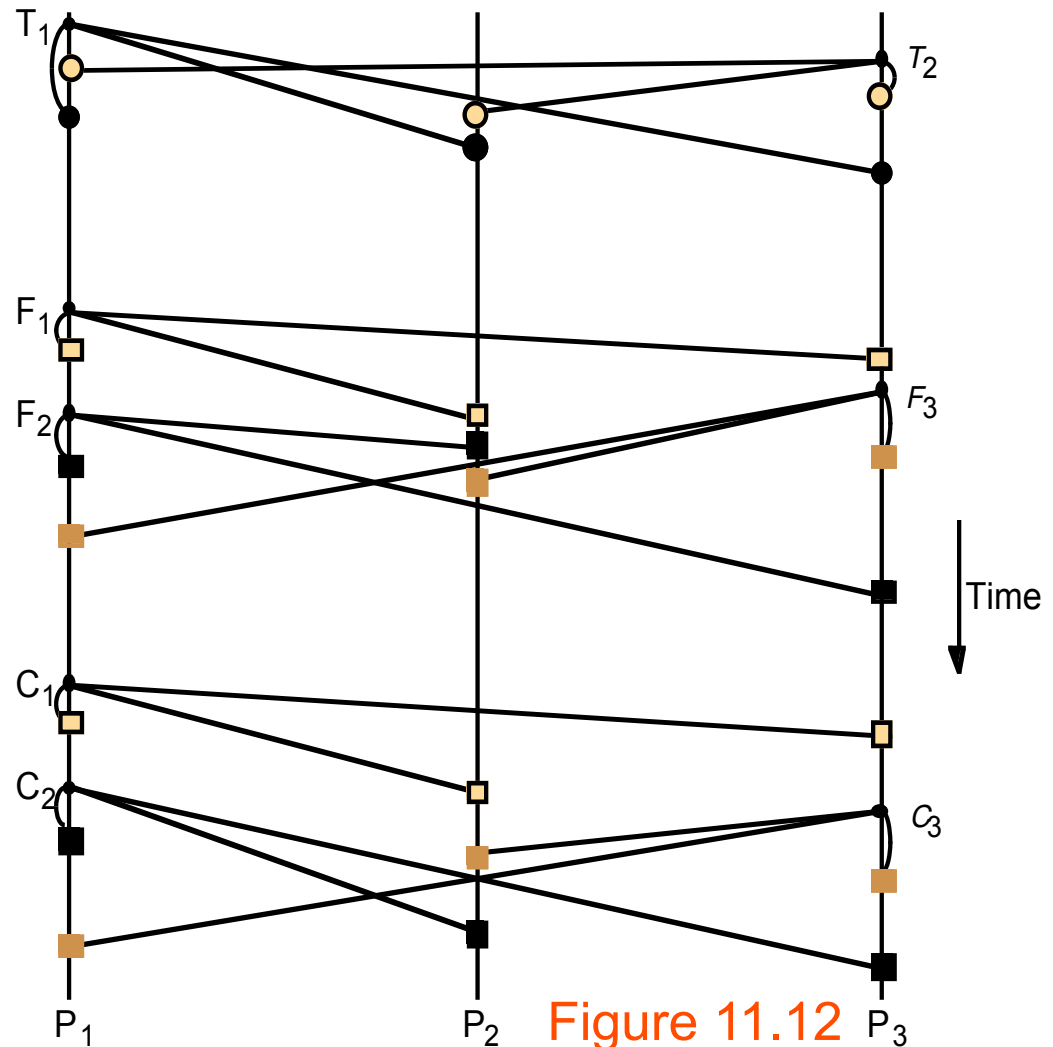


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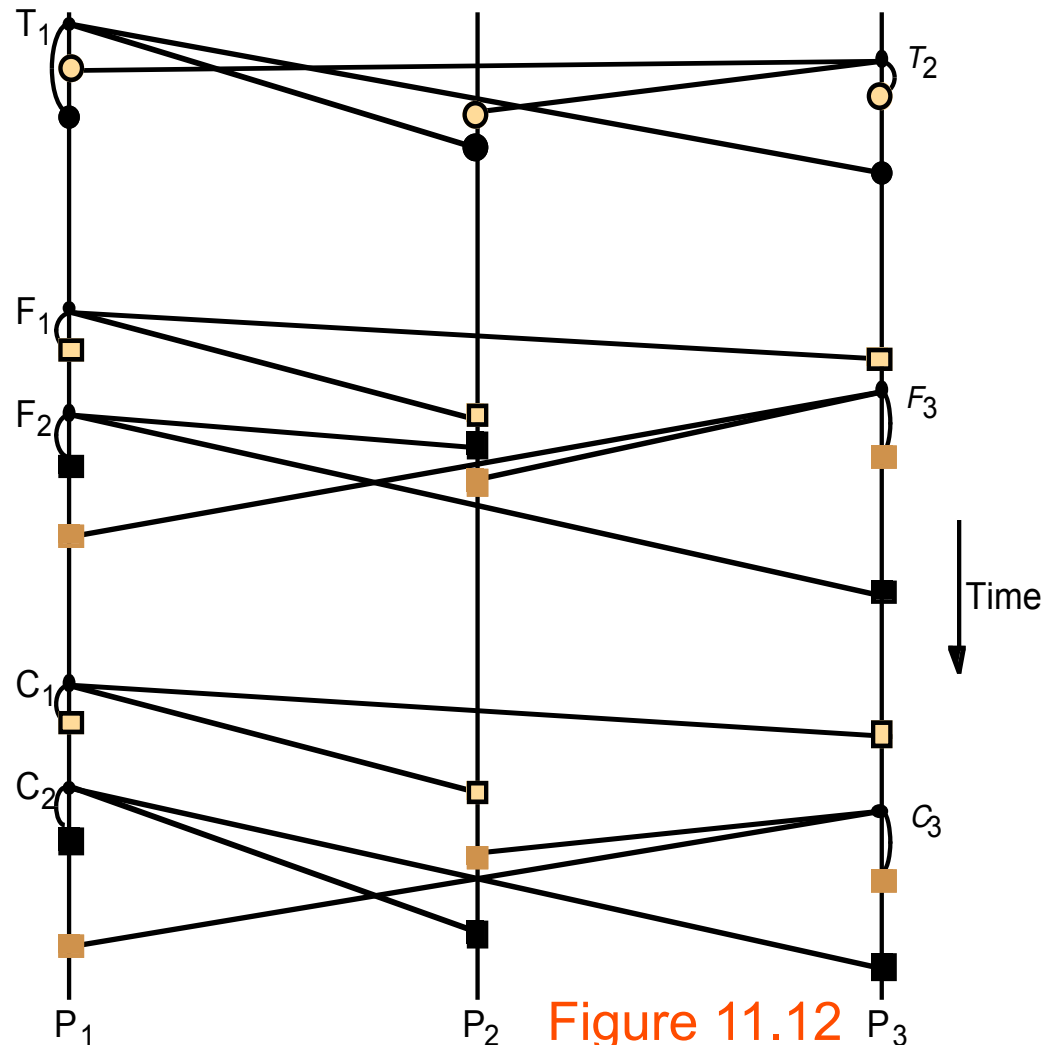


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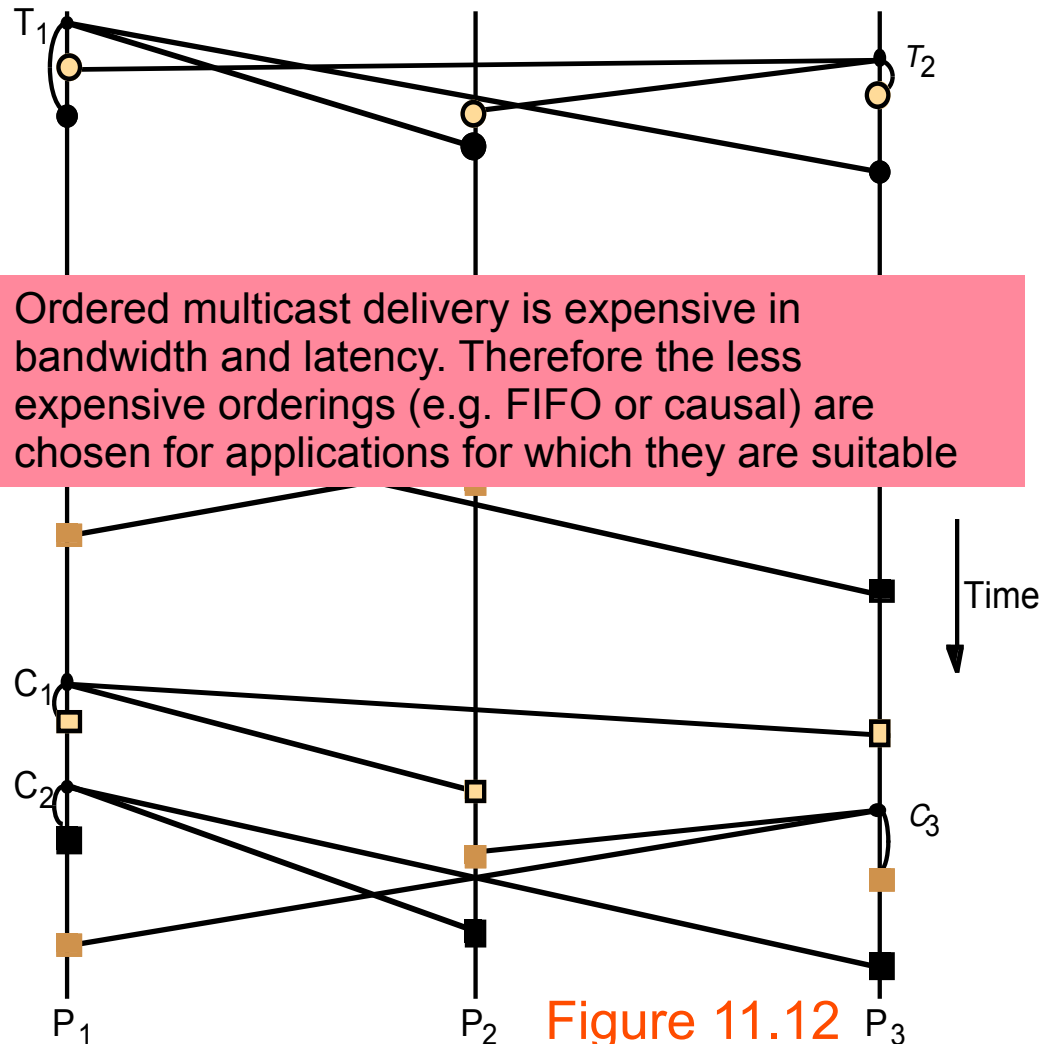


Figure 11.12

Display from a bulletin board program

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Bulletin board <i>os.interesting</i>		
Item	From	Subject
23	A.Hanlon	Mach
24	G.Joseph	Microkernels
25	A.Hanlon	Re: Microkernels
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27	M.Walker	Re: Mach
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- ❑ Require reliable multicast - so that all members receive messages

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Display from a bulletin board program

- ? Users run bulletin board applications which multicast messages
- ? One multicast group per topic (e.g. *os.interesting*)
- ? Require reliable multicast - so that all members receive messages
- ? Ordering:

Bulletin board <i>os.interesting</i>		
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Implementation of FIFO ordering over basic multicast

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- [?] if $S > R^q_g + 1$ then p places message in hold-back queue until intervening messages have been delivered. (note that *B-multicast* does eventually deliver messages unless the sender crashes)

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 1. using a sequencer (only for non-overlapping groups)
 2. the processes in a group collectively agree on a sequence number for each message

Total ordering using a sequencer

Total ordering using a sequencer

1. Algorithm for group member p

On initialization: $r_g := 0$;

To TO-multicast message m to group g

$B\text{-multicast}(g \cup \{\text{sequencer}(g)\}, \langle m, i \rangle)$;

On $B\text{-deliver}(\langle m, i \rangle)$ with $g = \text{group}(m)$

Place $\langle m, i \rangle$ in hold-back queue;

On $B\text{-deliver}(m_{\text{order}} = \langle \text{"order"}, i, S \rangle)$ with $g = \text{group}(m_{\text{order}})$

wait until $\langle m, i \rangle$ in hold-back queue and $S = r_g$;

$TO\text{-deliver}$ m ; // (after deleting it from the hold-back queue)

$r_g = S + 1$;

2. Algorithm for sequencer of g

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Total ordering using a sequencer

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B-deliver order message, get g and S and i from order message

wait till $\langle m, i \rangle$ in queue and $S = r_g$,

TO-deliver m and set r_g to $S+1$

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Discussion of sequencer protocol

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What are the potential problems with using a single sequencer?

Discussion of sequencer protocol

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What are the potential problems with using a single sequencer?

Kaashoek's protocol uses hardware-based multicast

The sender transmits one message to sequencer, then the sequencer multicasts the sequence number and the message but IP multicast is not as reliable as B-multicast so the sequencer stores messages in its history buffer for retransmission on request

members notice messages are missing by inspecting sequence numbers

What can the sequencer do about its history buffer becoming full?

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members notice messages are missing by inspecting sequence numbers

Members piggyback on their messages the latest sequence number they have seen

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What happens when some member stops multicasting?

seen

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Members that do not multicast send heartbeat messages (with a sequence number)

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The ISIS algorithm for total ordering

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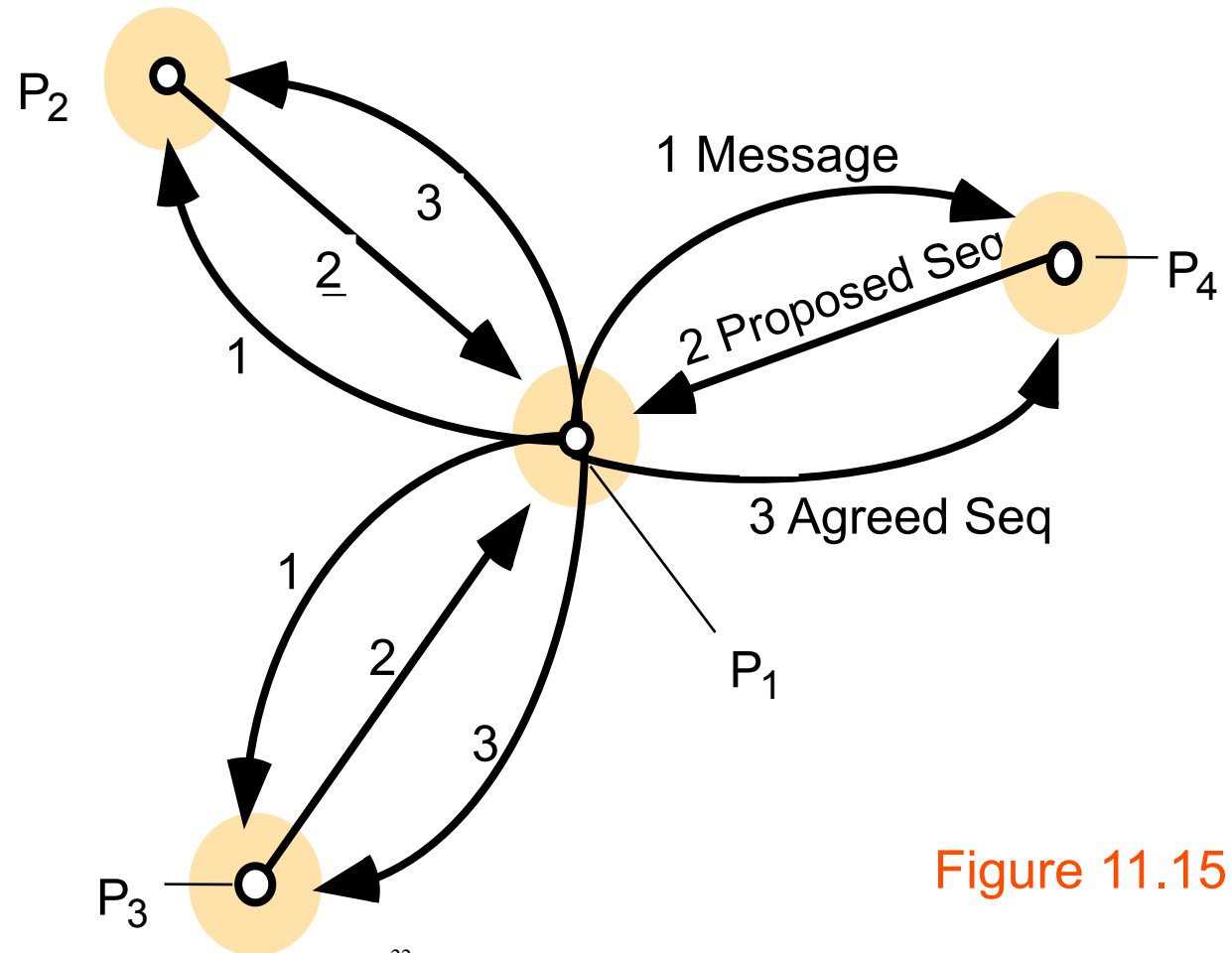


Figure 11.15

The ISIS algorithm for total ordering

1. the process P_1 B-multicasts a message to members of the group

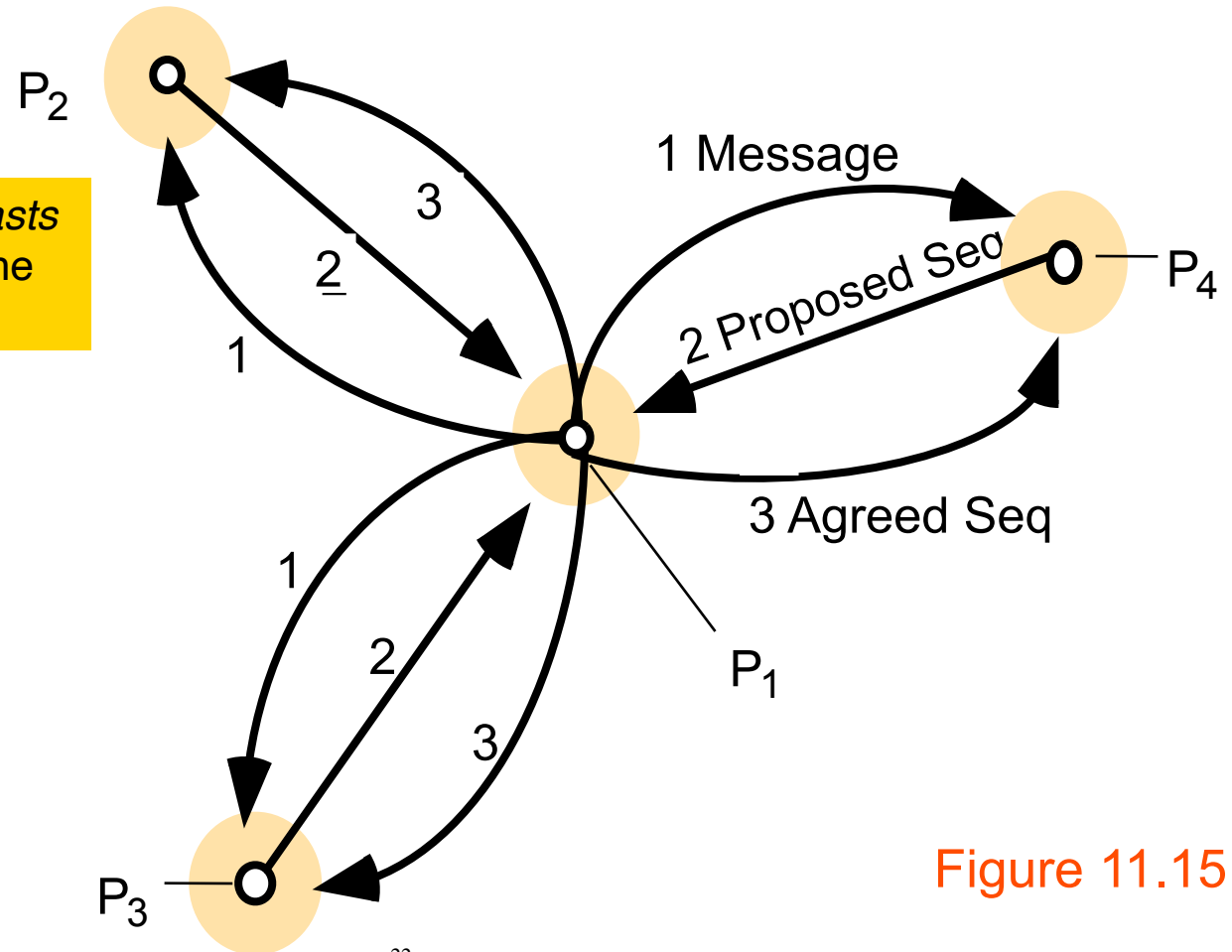
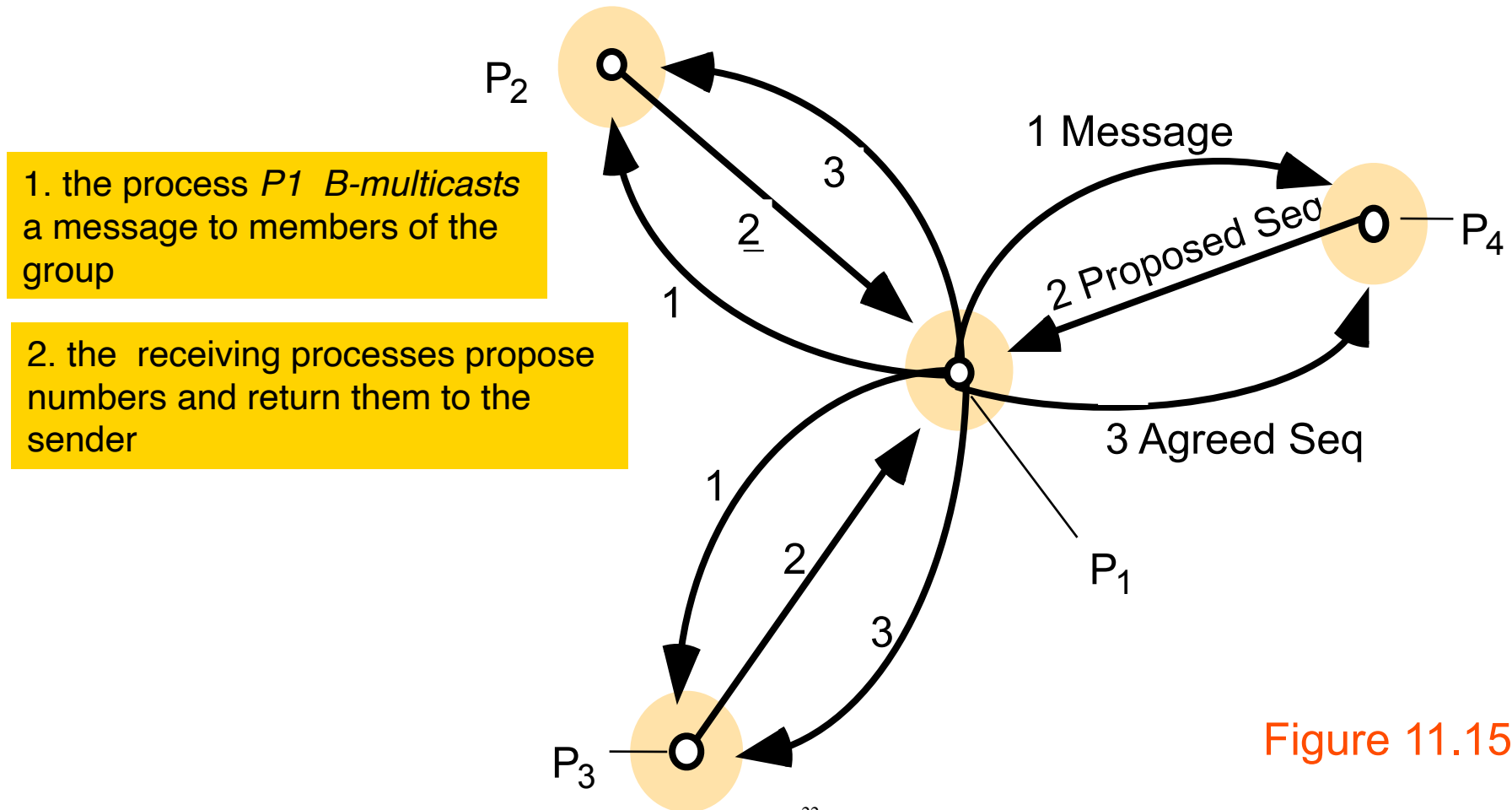


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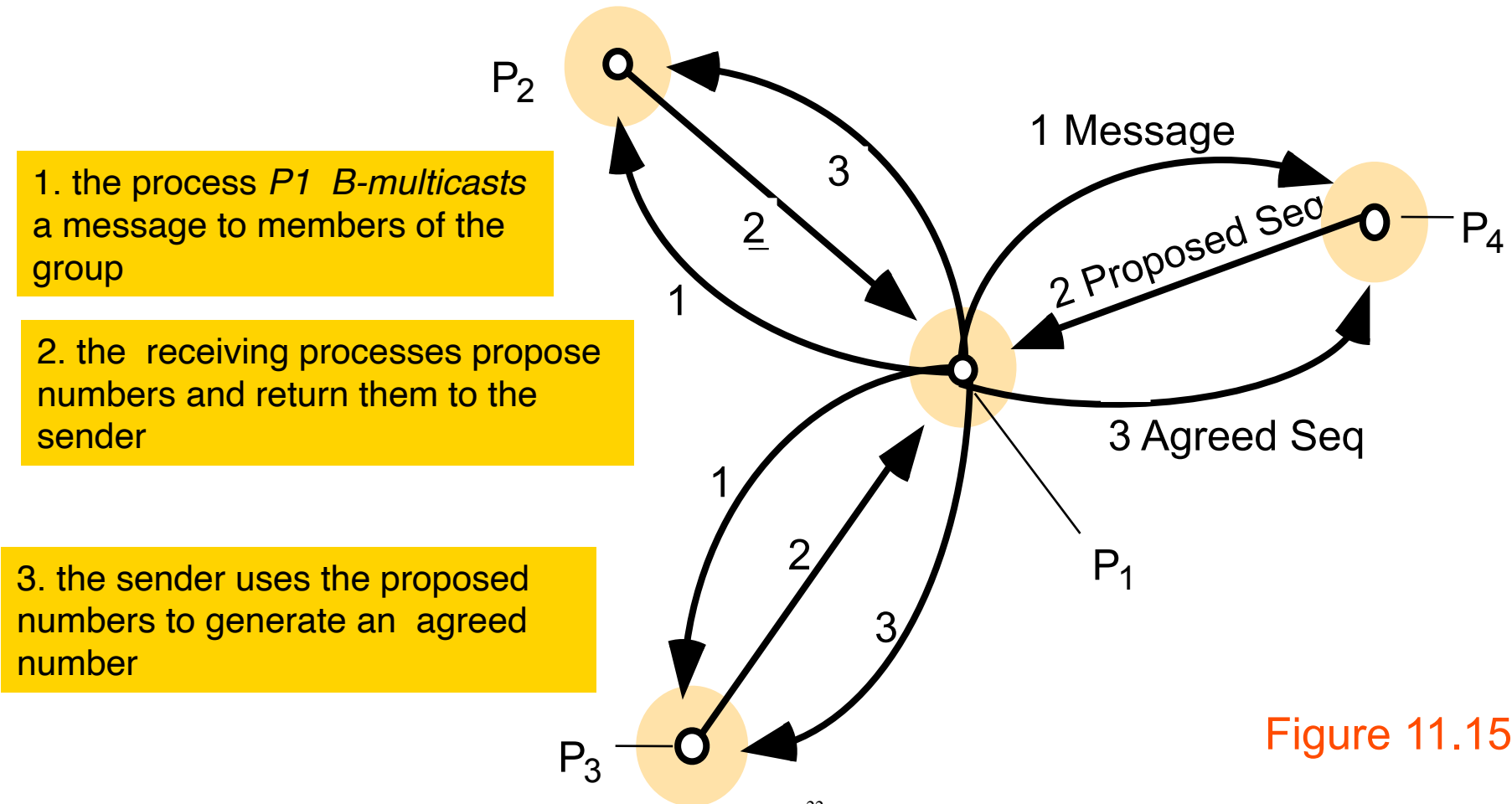


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The ISIS algorithm for total ordering

? this protocol is for open or closed groups

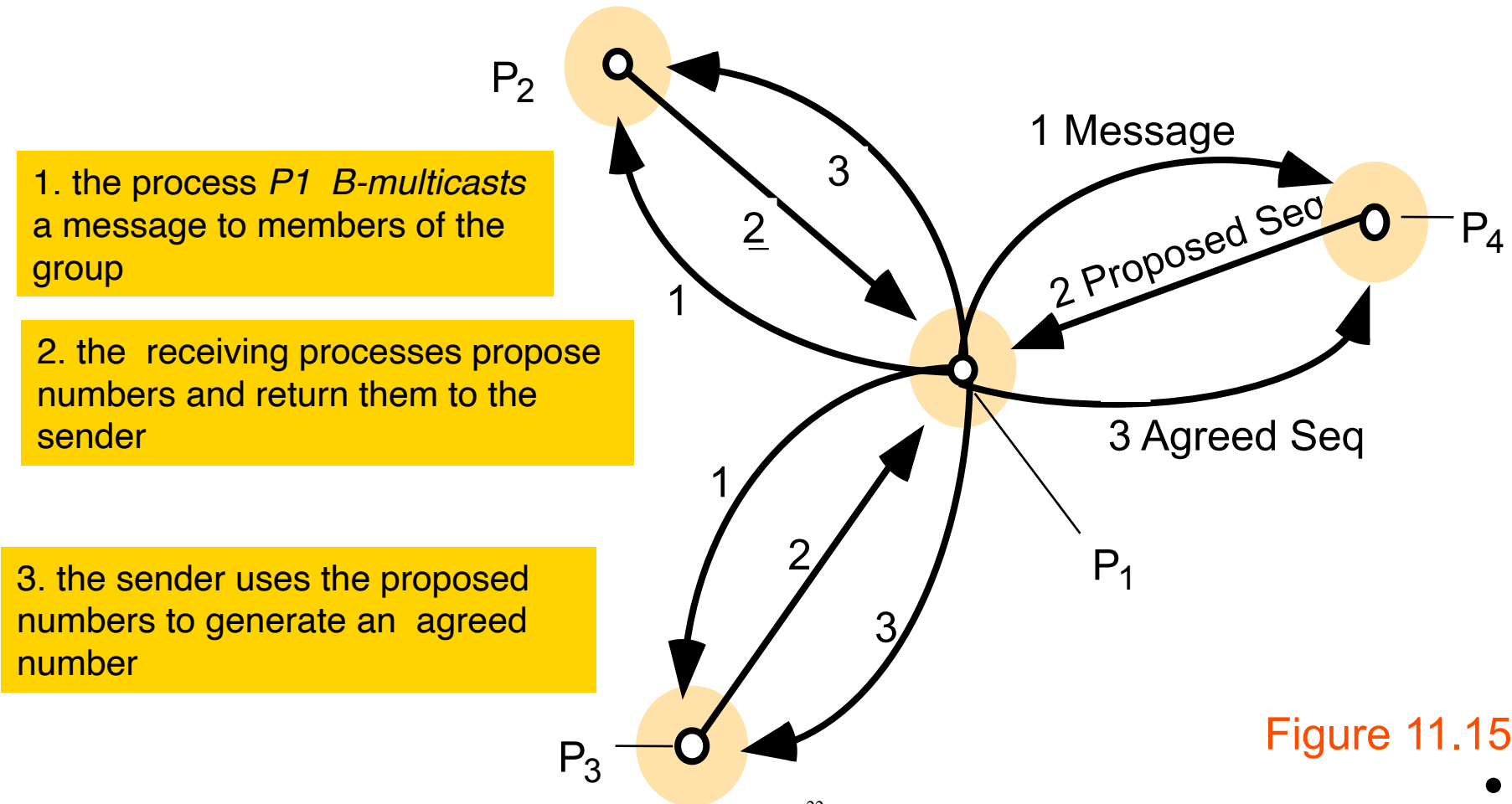


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- [?] 3. p collects all the proposed sequence numbers and selects the largest as the next agreed sequence number, a .
It *B-multicasts* $\langle i, a \rangle$ to g . Recipients set $A^q_g := \text{Max}(A^q_g, a)$, attach a to the message and re-order hold-back queue.

Discussion of ordering in ISIS protocol

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 Hold-back queue

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- ☐ when the message at the front has an agreed id, it is transferred to the delivery queue
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[?] Latency

- [?] 3 messages are sent in sequence, therefore it has a higher latency than sequencer method**
- [?] this ordering may not be causal or FIFO**

Causally ordered multicast

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- ❓ We present an algorithm of Birman 1991 for causally ordered multicast in non-overlapping, closed groups. It uses the *happened before* relation (on multicast messages only)
 - ❓ that is, ordering imposed by one-to-one messages is not taken into account

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 - ❓ that is, ordering imposed by one-to-one messages is not taken into account
- ❓ It uses vector timestamps - that count the number of multicast messages from each process that happened before the next message to be multicast

Causal ordering using vector timestamps

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Algorithm for group member p_i ($i = 1, 2, \dots, N$)

On initialization

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To CO-multicast message m to group g

$V_i^g[i] := V_i^g[i] + 1$;

$B\text{-multicast}(g, \langle V_i^g, m \rangle)$;

On $B\text{-deliver}(\langle V_j^g, m \rangle)$ from p_j , with $g = \text{group}(m)$

place $\langle V_j^g, m \rangle$ in hold-back queue;

wait until $V_j^g[j] = V_i^g[j] + 1$ and $V_j^g[k] \leq V_i^g[k]$ ($k \neq j$);

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Figure
11.16

Causal ordering using vector timestamps

each process has its own vector timestamp

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Figure
11.16

Causal ordering using vector timestamps

each process has its own vector timestamp

Algorithm for group member p_i

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$V_i^g[j] := 0 \ (j = 1, 2, \dots, N);$

To CO-multicast message m to group g

$V_i^g[i] := V_i^g[i] + 1;$

$B\text{-multicast}(g, \langle V_i^g, m \rangle);$

On B-deliver($\langle V_j^g, m \rangle$) from process p_j

place $\langle V_j^g, m \rangle$ in hold-back queue

wait until $V_j^g[j] = V_i^g[j] + 1$ and $V_j^g[k] \leq V_i^g[k] \ (k \neq j);$

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Note: a process can immediately *CO-deliver* to itself its own messages (not shown)

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- ❓ If we combine it with the sequencer algorithm we get total and causal ordering