

## Introduction to Neural Networks

**Day 1**; 13th April 2024

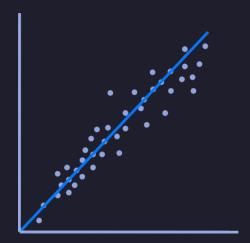
**Learning & Exploration in AI Practices** 



## Regression vs Classification

## 01

<b>D</b> . 4	
Regression	Classification
Predict continuous values	Predicts discrete values
Linear and Non-Linear Regression	Binary or Multi-Class Classifier
Maps input/s to continuous output variable	Maps input/s to discrete output variable
Linear Regression, etc.	Logistic Regression, etc.
Find best fit line	Find decision boundary







## **Loss Functions**

$$L = \frac{1}{2n} \sum_{i=1}^{n} (y_i - y_{predicted_i})^2$$

**RMSE Loss** 

$$L = -(\hat{y} \cdot \log(y) + (1 - \hat{y}) \cdot \log(1 - y))$$
  
Binary Cross Entropy Loss

Loss functions are a method of evaluating how well your algorithm models your dataset.

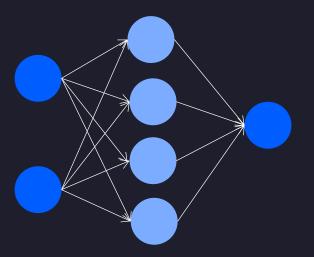
If your predictions are totally off, your loss function will output a higher number. If they're pretty good, it'll output a lower number.



### What is a Neural Network?

Neural network is a type of machine learning model inspired by the human brain. Just like our brains, a neural network is made up of *neurons*.

Neural networks, and brains both receive input, have a layered structure, and are formed of simple computation units.





## Why do we need them?

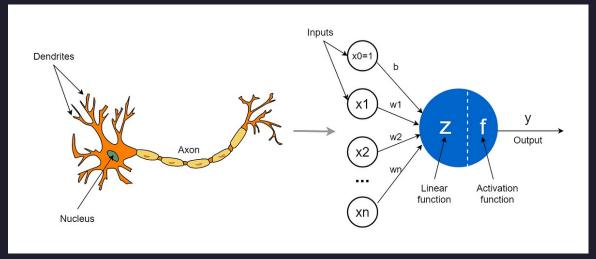
- 1 Learns complex patterns in data that humans struggle to identify.
- **Extracts "hidden" features** from raw data, eliminating the need for us to do so.
- 3 Multi-dimensionality!



## A single perceptron model

#### Simplest form of a neural network.

- Consists of a single neuron with adjustable weights.
- The weighted sum of the inputs is applied to the threshold function.
- Finally, we get a binary output classifying inputs into one of the two classes.

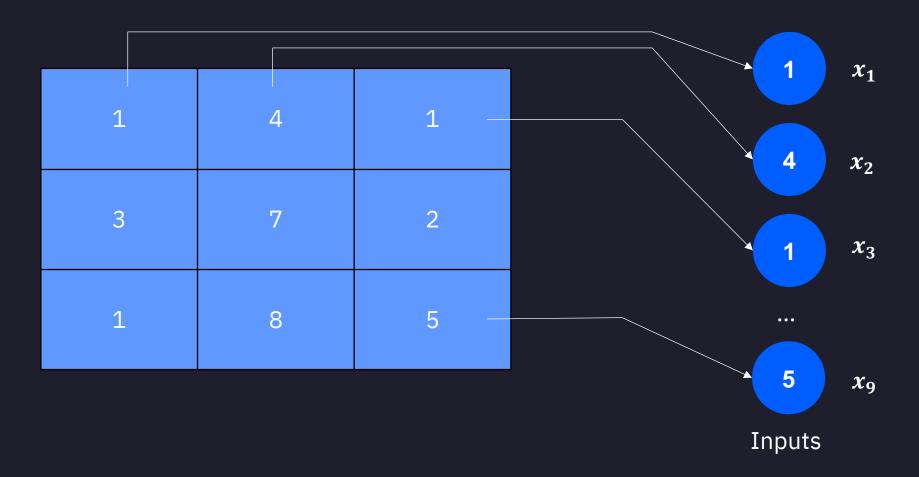


Source: The Concept of Artificial Neurons (Perceptrons) in Neural Networks by Rukshan Pramoditha | Towards Data Science



## Inputs







## Weights & Biases

#### Weights

Weights are like the "strength" of the connections between the input values and the perceptron.

Each input has a weight associated with it.

Higher weights = more influence lower weights = less influence.

#### Bias

The bias is a single number added to the weighted sum of the inputs.

The bias can shift the activation of the perceptron up or down, making it more or less likely to "fire".

It acts as a threshold.



### **Activation Function**

#### What?

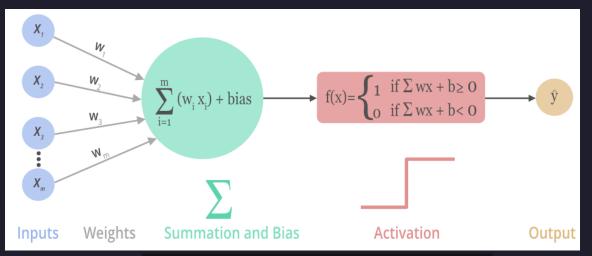
They decide whether a neuron should be activated or not.

#### When?

Applied to every linear function within the neural network.

#### Why?

They help convert inputs from the input space to the output space.



Source: Understanding Activation Functions in Depth | Geeks for Geeks

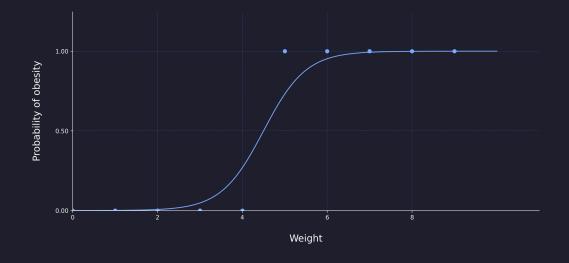


## **Common Activation Functions**

#### Sigmoid

Squashes input values to a range between 0 and 1.

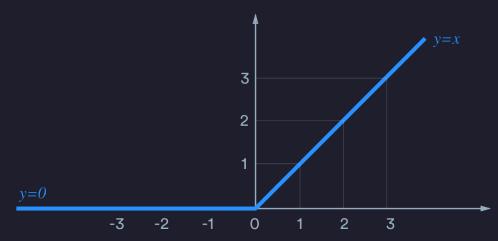
$$f(x) = \frac{1}{1 + e^{-x}}$$



#### **ReLU (Rectified Linear Unit)**

Returns the input directly if it is positive; otherwise zero.

$$f(x) = \max(0, x)$$





## All together.

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$$z = x_1. w_1 + x_2. w_2 + \dots + x_n. w_n + b$$
  
=  $\sum_{i=0}^{n} x_i. w_i + b$   
=  $x^T. w + b$ 

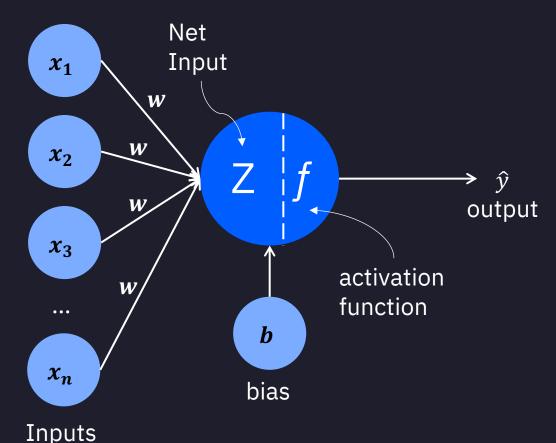
$$\hat{y} = \sigma(z)$$

$$\hat{y} = \begin{cases} 0, z \le 0 \\ z, z > 0 \end{cases}$$

z = Net input

 $\sigma = Activation function(ReLU)$ 

 $\hat{y} = Predicted output$ 





#### Loss

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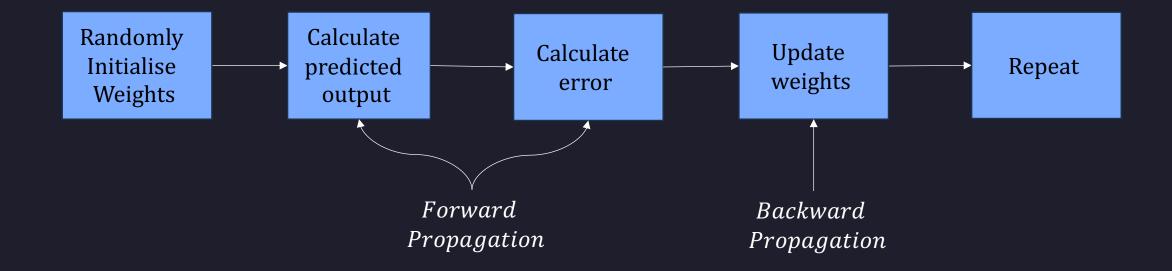
$$\hat{y}(p) = \begin{cases} 0, z \le 0 \\ 1, z > 0 \end{cases} \quad predicted output$$

$$y(p) = desired output$$

$$e(p) = \hat{y}(p) - y(p)$$
  
= error aka loss

Cost = J = 
$$\frac{1}{2n} \sum_{i=1}^{n} (e(i))^2$$
  $L = -(\hat{y} \cdot \log(y) + (1 - \hat{y}) \cdot \log(1 - y))$ 





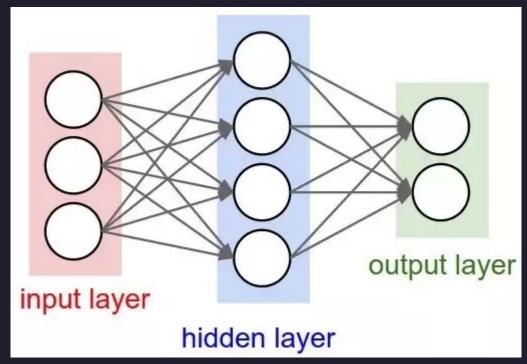


# An extension: Multi-Layered Neural Networks



## Multi-Layered Neural Networks 14

They not only contain *multiple* neurons, but also *multiple layers*.



Source: https://compphysics.github.io/MachineLearning/doc/pub/cnn/html/cnn.html

Input Layer: This is the input that is fed into the neural network

Hidden Layers: Perform all the necessary calculations.

Output Layer: Predicts out final output.

Fully connected: Every neuron in one layer is connected to every neuron in the next layer and has its own sets of weights and bias.

## Number of neurons in each layer 15

#### Input Layer

- Neurons = input size
- Input = grayscale image of size 28x28 pixels.
- Input layer = 784 neurons (28 x 28).

#### Hidden Layer

- Layers = you decide
- Neurons = up to you too!
- Complex problems require more hidden layers.

#### **Output Layer**

- Neurons = no. of classes
- Input = circle, square or triangle.
- No. of neurons = 3



## Inferencing Forward Propagation



## **Forward Propagation**

Forward propagation is where input data is fed through a network, in a forward direction, to generate an output. The data is accepted by hidden layers and processed (by the activation functions), and moves to the successive layer.

Let's look at an example of a small neural network...



### **A Small Neural Network**

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$$w = 2$$

$$x = -2$$

$$b = 8$$

$$y = 2$$

$$z = wx + b$$

$$y = g(z) = z$$

$$J(w,b) = \frac{1}{2}(y - y_{actual})^2$$

$$\vec{x} \longrightarrow b \longrightarrow y$$

## **Backward Propagation Computing Gradients**



The **gradient** is a fancy word for derivative, or the rate of change of a function. It's a vector (a direction to move) that:

- Points in the direction of greatest increase of a function
- Is zero at a local maximum or local minimum (because there is no single direction of increase)

So the gradient tells us how sensitive the model is to a change in that weight



## What does the gradient tell us?

Let a cost function 
$$J(w) = w^2$$
.  
Say  $w = 3$ ,  $J(w) = 3^2 = 9$ 

If we increase w by a tiny amount  $\epsilon = 0.001$ , how does J(w) change?

$$w = 3 + 0.001$$
 (If w \(\tau 0.001\))  
 $J(w) = w^2 = 9.006001$  (then  $J(w) \(\tau 6 \ * 0.001\))$ 

$$\frac{dJ(w)}{dw} = 2w = 6$$



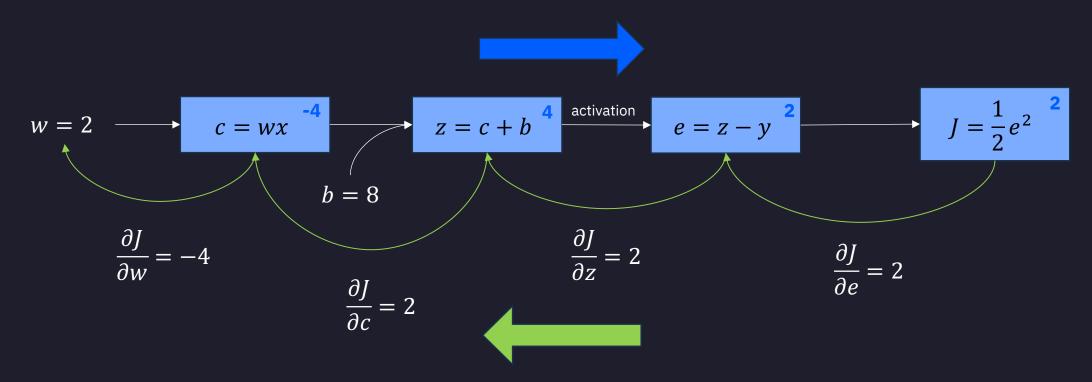
## Optimizing the gradient

## **22**

$$w_{n+1} = w_n - \alpha \frac{\partial J(w,b)}{\partial w}$$
Learning Rate



## Back to our small neural network 23



$$w = 2$$
$$x = -2$$

b = 8

y = 2

The above is using the **chain rule**.

Let's take a look: <a href="https://xnought.github.io/backprop-explainer/">https://xnought.github.io/backprop-explainer/</a>



Everything "configurable" before training.

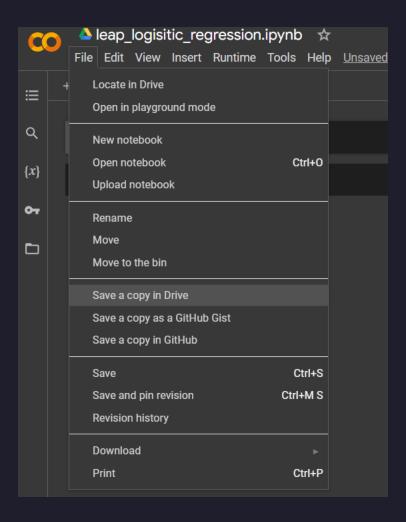
- Number of neurons per hidden layer
- Number of hidden layers
- Which algorithm to use for optimizing gradients
- Activation functions for every neuron
- Learning rate
- •



### Let's make our own!

## **25**

- Go to <u>leap-ai.tech</u>.
- Click the Colab Notebook for Day 1.
- Go to File->Save a copy in Drive!





In a *fully connected neural network*, there is an exponential increase in the number of parameters.

#### Example:

- Input layer of 784 neurons (28x28 pixel grayscale image)
- Hidden layer also with 784 neurons
- 784 neurons x 784 weights per neuron = 614,656 weights
- Plus 784 biases
- Total parameters: 615,440

All this for just one layer! Oh no!

Now imagine the layer count for higher resolutions and RBG images.



# The Solution? Convolutional Neural Networks.



## It's time to TEST you.





## See you tomorrow for the CNN Project!





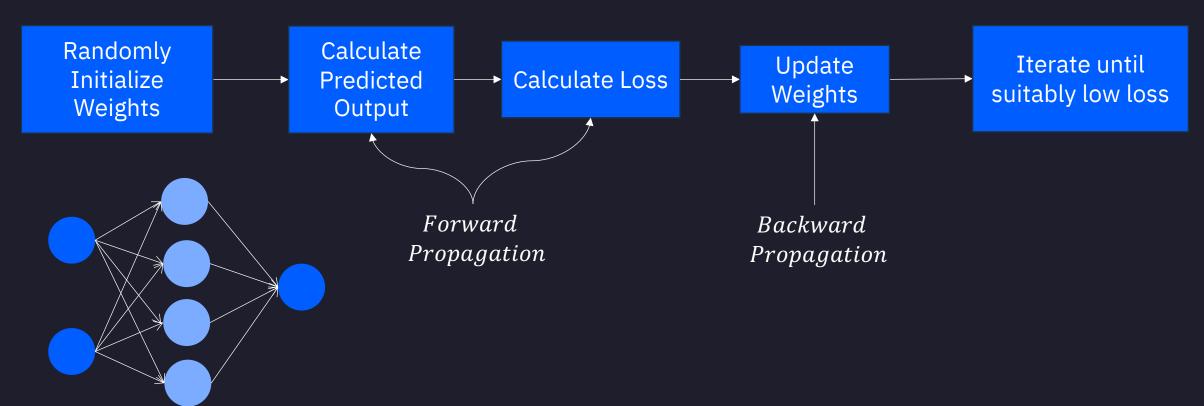
## Convolutional Neural Networks

**Day 2**; 14th April 2024

**Learning & Exploration in AI Practices** 



## Recap on Neural Networks





## Remember the problem?

In a fully connected neural network, there is an **exponential increase** in the number of parameters.

A huge number of parameters (600,000+) for only a 28x28 input image! Imagine how this will scale. This leads to **overfitting** due to too many parameters.

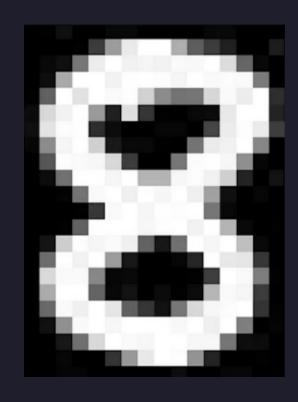
The solution was Convolutional Neural Networks (CNNs).

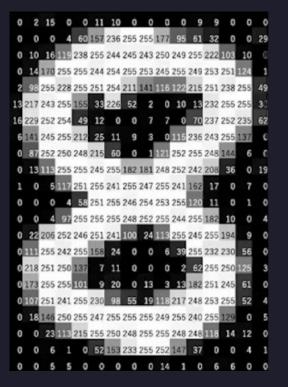


## Before that, Let's meet the Dataset



Computers C using a Matrix of numbers.

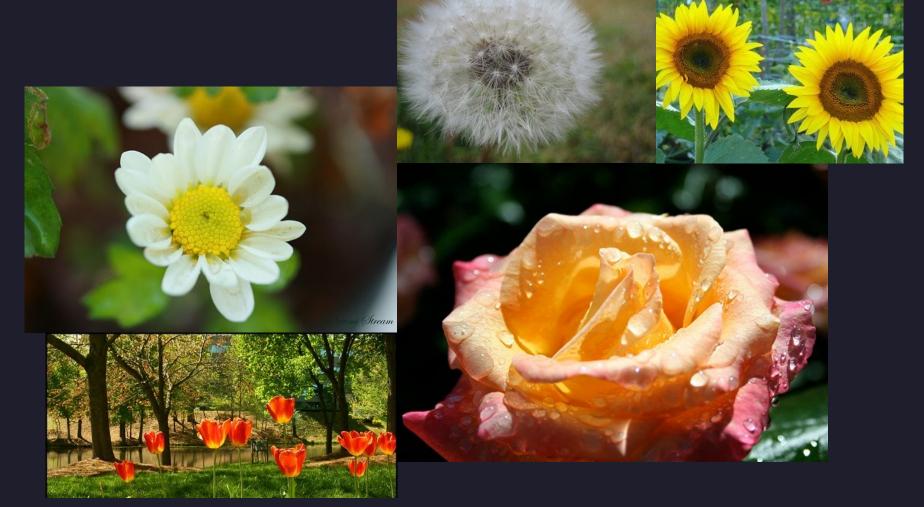






#### The dataset we will use.







#### The dataset we will use.

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We are using a dataset of Flower Images from Kaggle.

The dataset has about **500 labeled images** for each of **5 classes**:

Daisy, Dandelion, Rose, Sunflower, and Tulips.

Let's explore this data.



#### Why the split?

We need to make a **test** set out of our dataset.

- All available data is not used for training.
- Testing always on unseen, 'new' data.
- Can check model performance in the "general" case!

Train 0.8 Test 0.2



#### Things to keep in mind.

For Public Datasets, keep in mind:

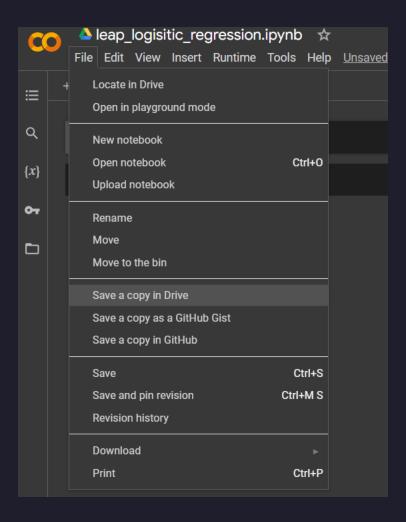
- Understand Data: Analyze dataset structure and check for data imbalance. Explore your dataset!
- Preprocess: Remove duplicates, handle missing values, outliers, and normalize data into one standard format.
- Ethical Use: Adhere to data policies, respect privacy, and follow ethical guidelines.



#### Let's explore and clean!

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- Go to leap-ai.tech.
- Click the Colab Notebook for Day 2.
- Go to File->Save a copy in Drive!





## CNN

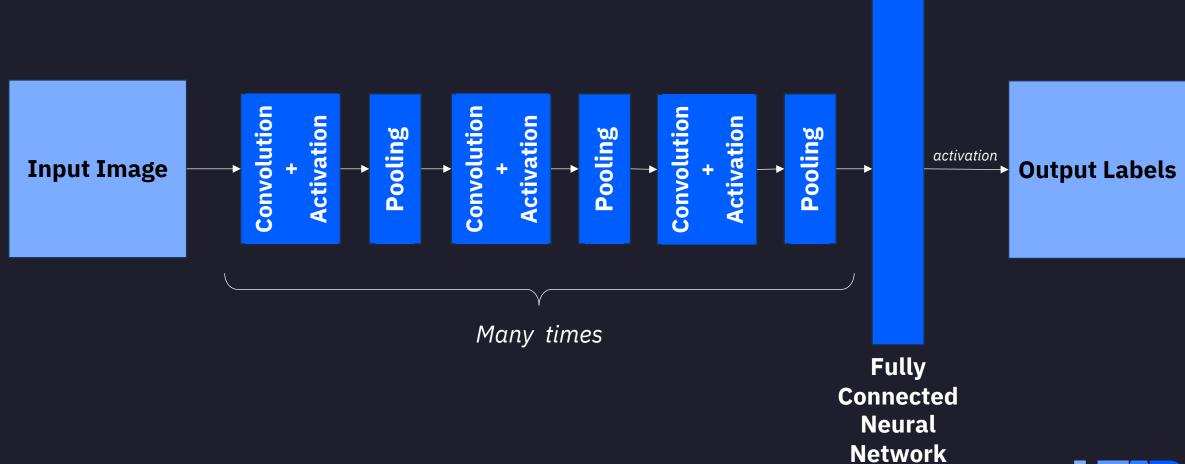




Source: "Chris" X.com/@gtx281



## CNNs for Classification: Outline 11





## **12**



Source: <a href="https://www.youtube.com/watch?v=KuXjwB4LzSA">https://www.youtube.com/watch?v=KuXjwB4LzSA</a>

Convolution is a method to "highlight" features in an image. It "filters" the image and discards unnecessary information.



Convolution mathematically combines two matrices (images) using a sliding window (kernel).

Naturally, you can see how it might need **padding** when it is applied near edges.

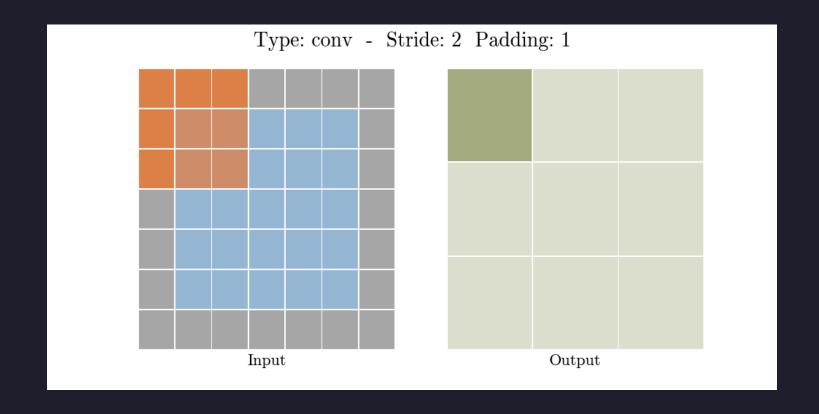
**Stride** can also be used to "skip" a few regions. This makes our output even smaller!



					_	
1,	1,0	1,	0	0		
0,	1,	1,0	1	0	4	
0,	0,×0	1,	1	1		
0	0	1	1	0		
0	1	1	0	0		
	lr	nag	e	Convolved Feature		



## **15**





As a function of input size,

$$Output \, Size = \frac{W - F - 2P}{S} + 1$$

- **W** is the input size
  - **F** is the filter size
  - **P** is the padding (usually auto-defined!)
  - **S** is the stride
- Also, S = 1 and P = (F 1)/2 ensure Input Size = Output Size.

This was all in the two dimensions of the image. What about the spatial arrangement?



## How are they connected within? 17

• Each neuron is connected to a **local region** instead of all the neurons in the previous layer. This is a hyperparameter called "filter size."

Example: Let input size be 32x32x3.

Then, connectivity with **5x5x3** filter size: Each neuron has **75 weights** and of course, 1 bias parameter. Number of neurons will be **32x32x3**.

• **Depth**: The number of filters to use per layer! Changing this will change the output dimension in the depth dimension.

Example: Let input size be 32x32x3.

Now, I have a layer with **depth=12** and **stride=1**. Output size will be 32x32x12! **12288 neurons** 

#### But, the problem was numbers...

Input=32x32x3, depth=12, stride=1, filter=5x5x3 leads to: 12288 neurons, each with 76 parameters... 9,33,888 parameters

The solution: **Depth Slices** 

A 32x32x12 output has 12 "depth" slices.

Neurons in the same depth slice use the same weights and biases.

So, with the same parameters above, new shapes:

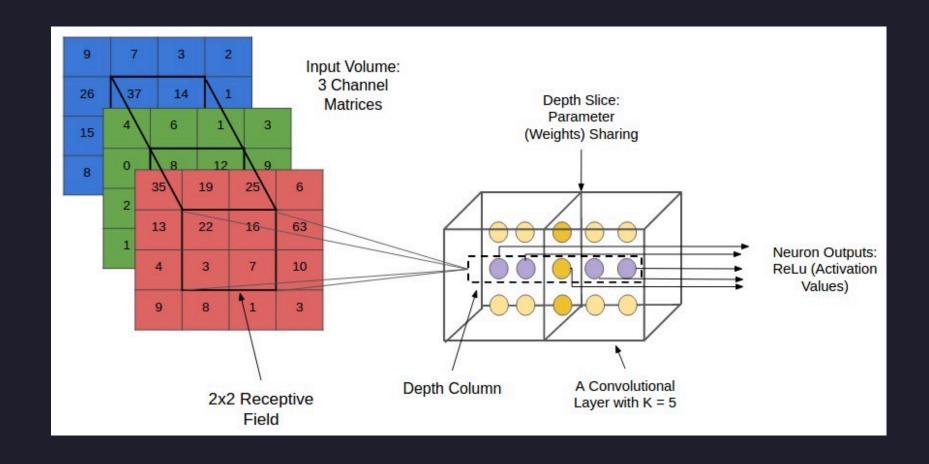
Still 12288 neurons, but parameters are only 5x5x3x12 + 12 = 912.

Based on the assumption that a feature at  $(x_1, y_1)$  is also useful at  $(x_2, y_2)$ .

Why is this reasonable? When can it fail?

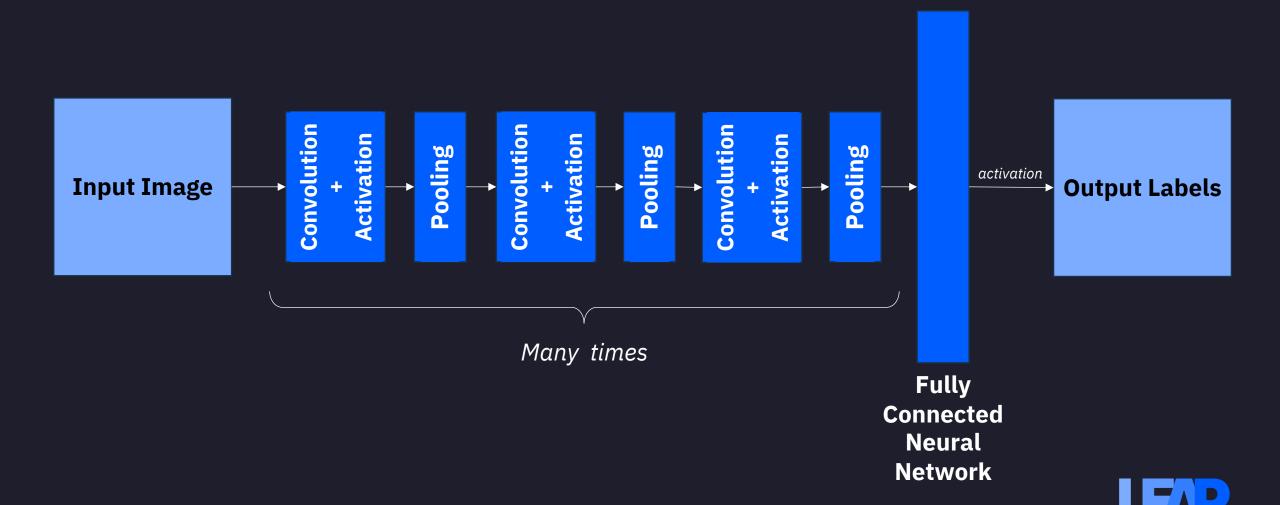
### Illustrative Specimen

## 19





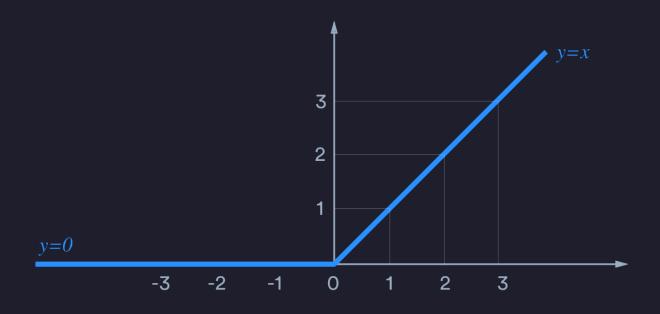
## CNNs for Classification: Outline 20



#### **Part Two: Activation Function**

After the convolution, the output goes through an activation function. Do you remember why this was?

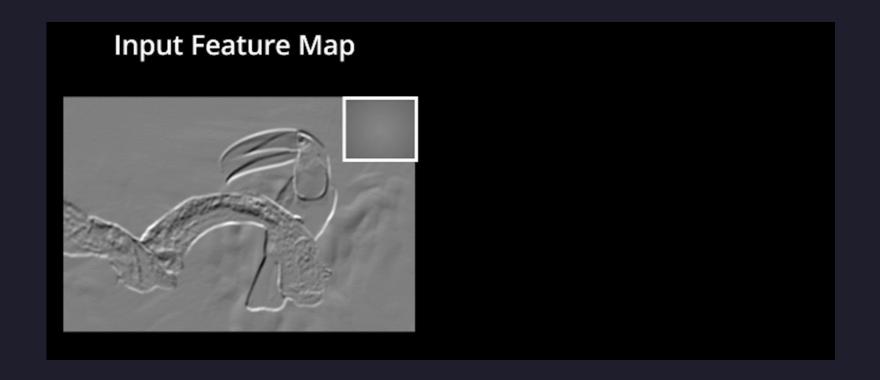
A common function used is **ReLU** (**Rectified Linear Unit**).



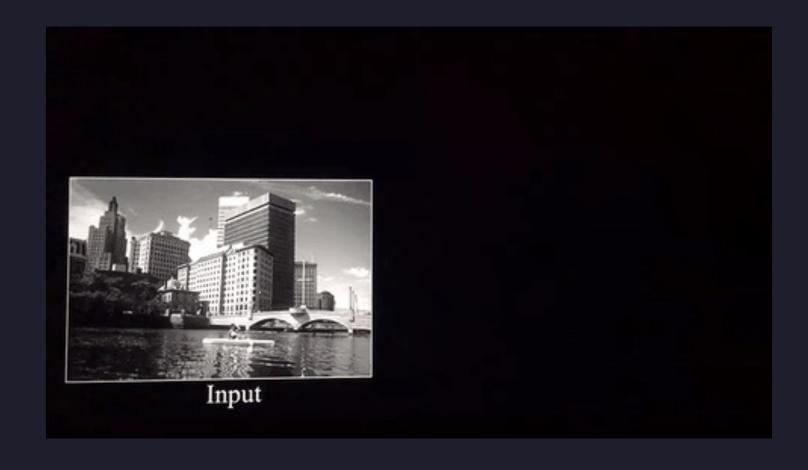


#### **Part Two: Activation Function**

## 22

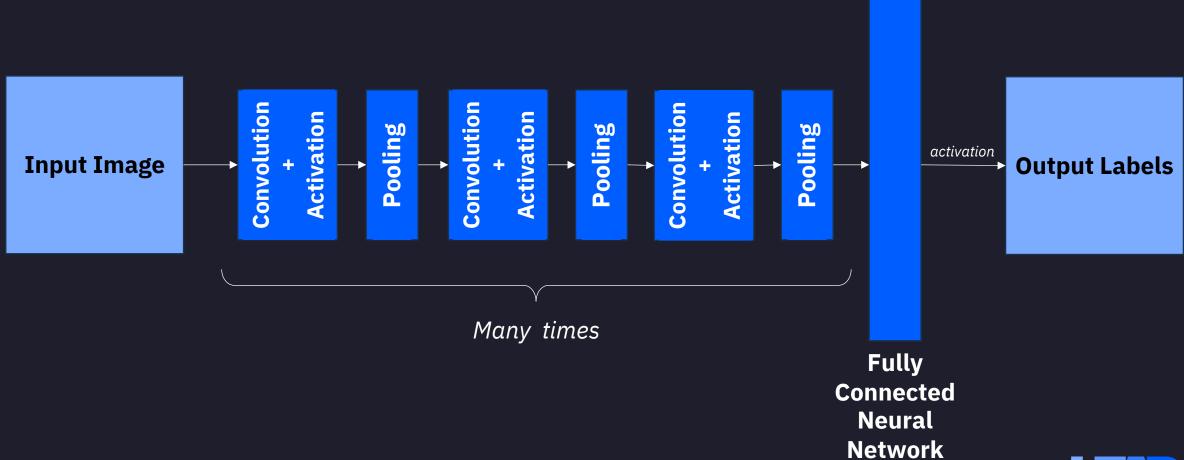








## CNNs for Classification: Outline 24





A method to reduce size of the image to **compress** the data to a smaller scale, while **preserving** the broader and more general patterns created by applying the kernel. Also reduces parameters!

Also works based on a sliding window.

Types: MeanPool, MaxPool, SumPool, etc.

Common: F=3, S=2 and F=2, S=2.

It might be that future CNNs will feature very few to no pooling layers.



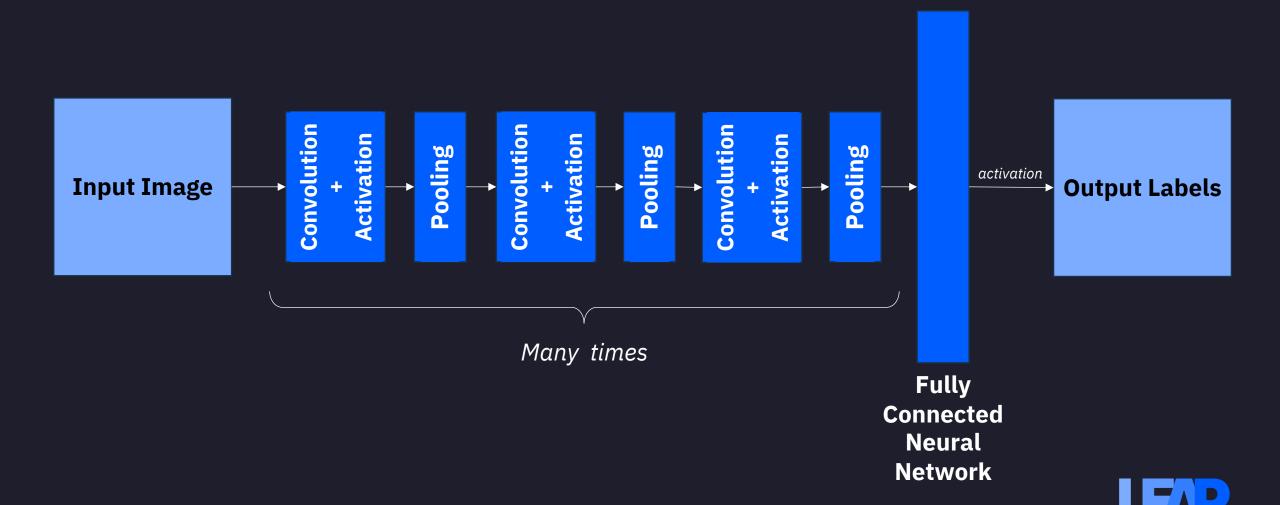
#### **An Illustrative**

## **26**

	Inp	out				
7	3	5	2		Output	
8	7	1	6	maxpool	8	6
4	9	3	9		9	9
0	8	4	5			



## CNNs for Classification: Outline 27



## Part Four: Fully Connected Network

Once we go through a few Conv + Pooling layer groups, we flatten the image into a **1-Dimensional array**.

It then goes into a Neural Network which can have several layers. This is a "simple" ML Model that uses the features we have extracted using convolution as input to give our desired Classification outputs. We saw this yesterday.



- Input layer should be divisible by 2 many times. Can you think of why?
- Use small filters for the Conv layers. Maximum 5x5! Use a Stride of 1, leaving downsizing to Pool layers only!
- F=2, S=2 for the Pooling layers!

Can you see how all the above makes our lives easier?



#### We really like TESTING you.



#### All Talk, No Play?

Let's design our own Convolutional Network.



# Testing (the model this time)



#### **Confusion Matrix**

Instances where the model Instances where the model incorrectly predicts the positive correctly predicts the negative class (1) when the actual class class (0) when the actual class is negative (0). Also known as a **Predicted Classes** is indeed negative (0). Type I error or false alarm. -ve +ve **TN** - True Negative **FP** - False Positive Actual Classes TN FP -ve **FN** - False Negative **TP** - True Positive TP +ve FN Instances where the Instances where the

model incorrectly predicts
the negative class (0)
when the actual class is
positive (1). Also known as
a Type II error or miss.

Instances where the model correctly predicts the positive class (1) when the actual class is indeed positive (1).



#### **Evaluation Metrics**

**Accuracy** is a metric used to evaluate classification models. It measures the ratio of correctly predicted instances to the total instances.

$$Accuracy = \frac{Number\ of\ Correct\ Predictions}{Total\ Number\ of\ Predictions}$$

**For example,** If you have 100 instances in your dataset and your model correctly predicts 85 of them, the accuracy would be 85%.



#### Other Evaluation Metrics

$$\frac{\textbf{Precision}}{All \text{ "true" predictions}} = \frac{\textit{True Positives}}{\textit{True Positives} + \textit{False Positives}}$$

**F1 Score** = Harmonic Mean(Precision, Recall) = 
$$2 * \frac{Precision \ X \ Recall}{Precision + Recall}$$

Refer to the post-workshop content for a detailed explanation.





#### And we are done!

**P.S.** Check out the Post Workshop Content!



