CS423: Probabilistic Programming Basics of Clojure and tiny bit of Anglican

Hongseok Yang KAIST Does anyone use Clojure, Scheme, or Lisp?

Does anyone use Clojure, Scheme, or Lisp?

What are the cons and pros of such a lang.?

Clojure

- Re-design of Scheme for Java virtual machine, with concurrency in mind.
- Untyped.
- Highly expressive.
- Cousin language for Anglican, the probabilistic programming language used in this course.

Learning outcome

- Can write simple Clojure programs with recursion, loop, list, and map.
- Can write simple Anglican programs with no conditioning, and perform inference.
- All by copy-paste-modify programming.

I. Prefix instead of infix notation:

$$(+ 3 3)$$
, not $3+3$

2. Use let to bind variables to values.

```
(let [x (* 3 3) y (* 4 4)] (+ x y))
```

3. Anonymous function using fn:

```
(let [f (fn [x] (* x x))] (+ (f 3) (f 4)))
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4. Separate function definition:

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(defn f [n] ...)
```

E.g.

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E.g.

Recursion allowed

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E.g.

Recursion allowed

n² + 5²

```
Lecture2 — vi sum.clj — 55×14
× ...me/Work/Teaching/2017-18/ProbProg18/Lectures/Lecture2 - vi sum.clj
                                                ...k/Teaching/2017-18/ProbProg18/Lectures/Lecture2 - java · lein repl
     lecture2)
(defn sq [x] (* x x))
(defn g [n]
   (if (= n 0)
      (+ (sq n) (g (- n 1)))))
                                                                                      All
sum.clj
                                                             1,1
"sum.clj" 9L, 101C written
```

[Q] Write a program that computes $1^2 + 2^2 + ... + 5^2$.

NB: I installed leiningen. Then, I ran "lein repl". You can install Clojure and run "clj" instead.

```
Lecture2 — java 4 lein repl — 55×14
                                        × ...k/Teaching/2017-18/ProbProg18/Lectures/Lecture2 — java • lein repl
 ...me/Work/Teaching/2017-18/ProbProg18/Lectures/Lecture2 — vi sum.clj
user=> (load-file "sum.clj")
#'lecture2/g
user=> (lecture2/g 100)
338350
user=> (lecture2/g 1000)
333833500
user=> (lecture2/g 10000)
StackOverflowError clojure.lang.Numbers$LongOps.combi
ne (Numbers.java:419)
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```

No StackOverflow.

5. Tail recursion.



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Not tail recursive

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```
(defn g [n r]
  (if (= n 0)
  r
  (g (- n 1)
        (+ n r))))
```

Tail recursive.

5. Tail recursion. 1) Use accumulator.

Not tail recursive

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Tail recursive. Acc. r

5. Tail recursion. I) Use accumulator. 2) Inform the compiler using loop and recur.

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```
      (defn f [n]
      (defn g [n r]

      (if (= n 0)
      (if (= n 0)

      (defn f [N]
      r

      (loop [n N r 0]
      (g (- n 1)

      (if (= n 0)
      (+ n r))))

      (defn f [N] (g N 0))

      Tail recursive. Acc. r
```

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```
      (defn f [n]
      (if (= n 0)

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      (if (= n 0)

      r
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      (defn f [N]
      r

      (loop [n N r 0]
      (f (- n 1)

      (if (= n 0)
      (f (- n 1)

      (recur (- n 1)
      (defn f [N] (g N 0))

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      (defn f [N]
      r

      (loop [n N r 0]
      (g (- n 1)

      (if (= n 0)
      (+ n r))))

      (defn f [N] (g N 0))

      Tail recursive. Acc.r
```

```
Lecture2 - vi sum_loop.clj - 55×14
 ...Work/Teaching/2017-18/ProbProg18/Lectures/Lecture2 — java • lein repl × .../Teaching/2017-18/ProbProg18/Lecture9 — vi sum_loop.clj
 ns lecture2b)
(defn sq [x] (* x x))
(defn g [n]
   (loop [i n r 0]
      (if (= i 0)
         (recur (- i 1) (+ (sq i) r))))
sum_loop.clj [+]
                                                          11,0-1
                                                                                 All
```

```
Lecture2 — java ∢ lein repl — 55×14
  × ...Work/Teaching/2017-18/ProbProg18/Lectures/Lecture2 — java • lein repl
                                           .../Teaching/2017-18/ProbProg18/Lectures/Lecture2 — vi sum_loop.clj
 ruser=> (load-file "sum_loop.clj")
  #'lecture2b/g
 user=> (lecture2b/g 100)
  338350
 user=> (lecture2b/g 1000)
  333833500
  user=> (lecture2b/g 10000)
  333383335000
  [user=> (lecture2b/g 100000)
  33333833350000
  user=> (lecture2b/g 1000000)
  3333333333500000
sı user=>
```

[Q] Write a Clojure function that takes $n \ge 2$ and computes the n-th Fibonacci number F_n :

$$F_1 = I$$
, $F_2 = I$, $F_{n+2} = F_n + F_{n+1}$

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Exercise 2: Random Fibonacci sequence R_n

$$R_1 = I$$
, $R_2 = I$,

 $R_{n+2} = R_n + R_{n+1}$ or $R_{n+1} - R_n$, each with prob. 1/2

[Q] What does the distribution of R_n look like?

I. Define an Anglican query using defquery.

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query name

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```
query name
(defquery baby-rfib [n]
  (let [b (sample (flip 0.5))
                                      arguments
        new-n (if b n (+ n 1))]
    (loop [i 2 r0 1 r1 1]
      (if (= i new-n)
                                     query body
          (recur (+ i 1)
                  (+ r0 r1)))))
```

Creating and sampling from distribution object

ery using defquery.

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(if (= i n)
r1
(def
                            ))))
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```
(defquery rfib [n]
       (loop [i 2 r0 1 r1 1]
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                          ))))
                    (+ r0 r1))))))/
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(defquery rfib [n]
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(if (= i n)
(det
           (let [b (sample (flip 0.5))
                  r2 (if b (+ r1 r0) (- r1 r0))]
             (recur (+ i 1)
                     r2)))))
                   (+ r0 r1)))))/
```

2. Perform inference using doquery.

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(doquery:importance rfib [20])
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Chooses an inference algorithm.

2. Perform inference using doquery.

query name, arguments

(doquery:importance rfib [20])



Clojure keyword.
Chooses an inference algorithm.

query name,

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2. Perform inference using doquery.

(doquery :importance rfib [20])

Clojure keyword.

Chooses an inference algorithm.

Returns a lazy infinite list of samples.

Only a finite prefix used.

2. Perform inference using doquery.

```
(let [s (doquery :importance rfib [20])]
  (take 2 s))
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```
( {:log-weight 0.0,
    :result 1,
    :predict []}

{:log-weight 0.0,
    :result -17,
    :predict []} )
```

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List

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List of maps

2. Perform inference using doquery.

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(let [s (doquery :importance rfib [20])]
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List
of maps
with three keys

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• To move on, we need to understand map and list datatypes of Clojure.

- To move on, we need to understand map and list datatypes of Clojure.
- Two key questions:
 - I. How to construct a datatype?
 - 2. How to destruct (or decompose) it?

Map in Clojure

I. Constructed using {..} or assoc typically.

```
{:a 0, :b 1, 3 10},
(assoc {:a 0, :b 1} 3 10)
```

2. Accessed (or destructed) by get & keyword.

```
(get {:a 0, :b 1, 3 10} 3)
(get {:a 0, :b 1, 3 10} :a)
(:a {:a 0, :b 1, 3 10})
```

List in Clojure

I. Created using list and conj typically.

```
(list 1 2 3), (conj (list 2 3) 1)
```

2. Destructed by first, rest, and take.

```
(first (list 1 2 3)),
  (rest (list 1 2 3)),
  (take 2 (list 1 2 3))
```

List in Clojure

3. Changed using map and filter.

```
(map inc (list 1 2 3)),
  (map + (list 1 2 3) (list 10 11 12))
(filter (fn [x] (>= x 2)) (list 1 2 3))
```

4. reduce.

```
(reduce + 0.0 (list 1 2 3 4))
```

5. drop, empty?, many other functions. Google.

List in Clojure

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(reduce + 0.0 (list 1 2 3 4))
```

5. drop, empty?, many other functions. Google.

[Q] Write a program that computes $1^2 + 2^2 + ... + n^2$.

```
(def sq [x] (* x x))
(defn f [n]
  (reduce + 0.0 (map sq (range 0 (inc n)))))
```

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```
(map inc (list 1 2 3)),
  (map + (list 1 2 3) (list 10 11 12))
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[Q] Write a program that computes $1^2 + 2^2 + ... + n^2$.

- Map: {...}, assoc, get, and access by keyword.
- List: list, conj, first, rest, take, map, filter, reduce, drop, empty?, etc.

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Core functions

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Masters' tools.

Core functions

- Map: {...}, assoc, get, and access by keyword.
- List: list, conj, first, rest, take, map, filter, reduce, drop, empty?, etc.

[QI] Write a fun. rev that reverses a list.

[Q2] Write a fun. conc that concatenates two lists.

```
(defn rev [1]
  (reduce conj (list) l))
```

- Map: {...}, assoc, get, and access by keyword.
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```
(defn rev [1]
  (reduce conj (list) l))

(defn conc [l1 l2]
  (reduce conj l2 (rev l1))
```

- Map: {..}, assoc, get, and access by keyword.
- List: list, conj, first, rest, take, map, filter, reduce, drop, empty?, etc.

[QI] Write a fun. rev that reverses a list.

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- I. Define an Anglican query using defquery.
- 2. Perform inference using doquery.

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(let [s (doquery :importance rfib [20])]
  (take 2 s))
```

```
( {:log-weight 0.0,
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    {:log-weight 0.0,
        :result -17,
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```

List
of maps
with three keys

3. Pick :result entries and analyse them.

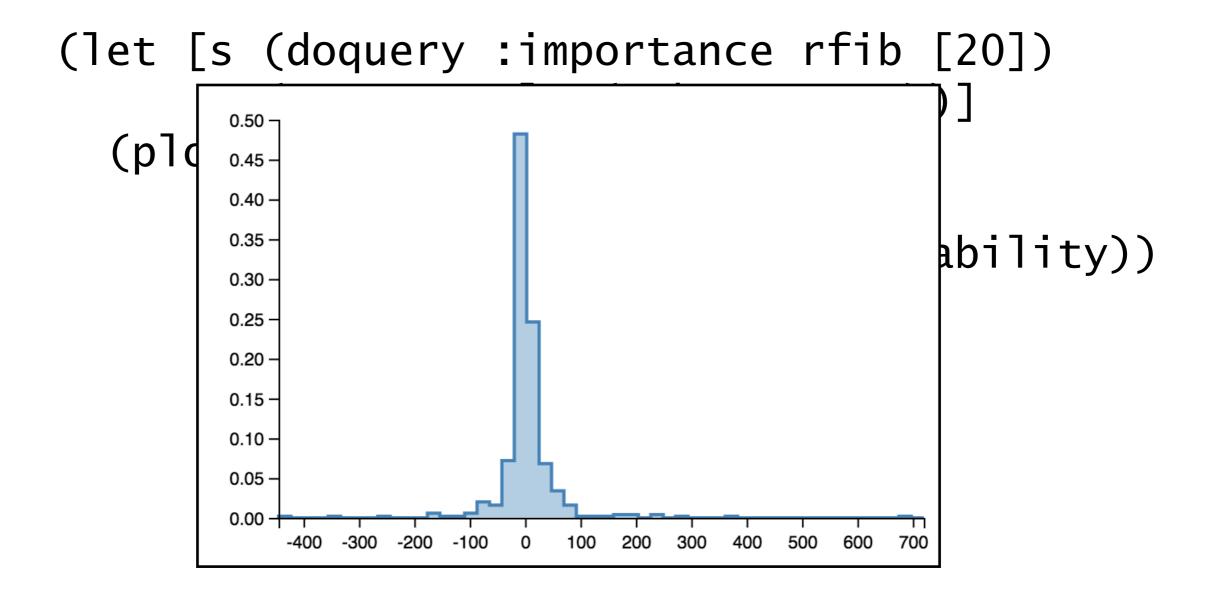
(doquery:importance rfib [20])

3. Pick :result entries and analyse them.

```
(let [s (doquery :importance rfib [20])
    r (map :result (take 1000 s))]
```

3. Pick :result entries and analyse them.

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[Q1] Compute the average of generated R_{20} using 1000 samples. This is called empirical mean.

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```
(let [s (doquery :importance rfib [20])
    r (map :result (take 1000 s))]
    (/ (reduce + 0.0 r) 1000.0))
```

[Q1] Compute the average of generated R_{20} using 1000 samples. This is called empirical mean.

3. Pick :result entries and analyse them.

```
(let [s (doquery :importance rfib [20])
    r (map :result (take 1000 s))]
    (/ (reduce + 0.0 r) 1000.0))
```

[Q1] Compute the average of generated R_{20} using 1000 samples. This is called empirical mean. [Q2] Compute the variance of generated R_{20} .

3. Pick :result entries and analyse them.

```
(let [s (doquery :importance rfib [20])
    r (map :result (take 1000 s))
    m (/ (reduce + 0.0 r) 1000.0)
    f (fn [x] (Math/pow (- x m) 2))]
    (/ (reduce + 0.0 (map f r)) 1000.0))
```

[Q1] Compute the average of generated R_{20} using 1000 samples. This is called empirical mean. [Q2] Compute the variance of generated R_{20} .

Exercise 3:

[Part I] Generate a list of Fibonacci numbers (list $F_1 F_2 ... F_n$) for a given n.

[Part 2] Generate a list of indices $0 \le 10000$ such that i is the sum of digits of F_i .

Assume get-digits for converting a number to a list of its digits. (get-digits 23)=(list 2 3).

Assume range. (range 16) = (list 12345).

Part I

Part 2

```
(defn ck [fibn-and-i]
  (let [fibn (first fibn-and-i)
             (second fibn-and-i)]
    (= (reduce + 0 (get-digits fibn))
       i)))
(def idx-fib-seq
  (map (fn [s i] (list s i))
       (fib 10000)
       (range 1 10001)))
(def indices
  (map second (filter ck idx-fib-seq)))
```

Topics covered

- Functions, recursion, loop, list, and map in Clojure.
- defquery, and doquery in Anglican.

Announcement

- I. Homework 0 in the course webpage.
 - It will teach you how to use Gorilla and to try examples in the web browser.
- 2. Form a group and tell us by the midnight of 30 March 2020 (Monday).