Simple Programming Problems

Whenever I'm TA for a introductory CS class where students learn some programming language, I have trouble coming up with good exercises. Problems from <u>Project Euler</u> and the like are usually much too difficult for beginners, especially if they don't have a strong background in mathematics.

This page is a collection of progressively more difficult exercises that are suitable for people who just started learning. It will be extended as I come up with new exercises. Except for the GUI questions, exercises are generally algorithmic and should be solvable without learning any libraries. The difficulty of the exercises of course somewhat depends on the programming language you use. The List exercises for example are more complicated in languages like C that don't have build-in support for lists.

I suppose they are also useful, although much easier, whenever an experienced person wants to learn a new language.

This guide has been translated to Chinese by yifeitao <u>Simple Programming Problems in</u> Chinese

Before you begin

Learning to program means learning how to solve problems using code. Conceptually it is not very difficult to write a program that solves a problem that you can solve yourself. The skill you need to acquire is thinking very precisely about how you solve the problem and breaking it down into steps that are so simple that a computer can execute them. I encourage you to first solve a few instances of a problem by hand and think about what you did to find the solution. For example if the task is sorting lists, sort some short lists yourself. A reasonable method would be to find the smallest element, write it down and cross it out of the original list and repeat this process until you have sorted the whole list. Then you have to teach the computer 1) how to find the smallest element, 2) how to write it down, 3) how to cross it out, and wrap this in a loop. Then continue this task breakdown process until you're confident you know how to write the necessary program.

To make good progress in your programming task, you need to test your work as early and as thoroughly as possible. Everybody makes mistakes while programming and finding mistakes in programs consumes a very large part of a programmer's work-day. Finding a problem in a small and easy piece of code is much simpler than trying to spot it in a large program. This is why you should try to test each sub task you identified during your task-breakdown by itself. Only after you're confident that each part works as you expect you can attempt to plug them together. Make sure you test the complete program as well, errors can creep in in the way the different parts interact. You should try to automate your tests. The easier it is to test your program, the freer you are in experimenting with changes.

The last important point is *how* you express your thoughts as code. In the same way that you can express the same argument in different ways in a normal English essay, you can express the same problem-solving method in different ways in code. Try for brevity. The lines that you don't write are the lines where you can be sure that the don't have bugs. Don't be afraid to Google for idiomatic ways of doing the things you'd like to do (after you tried doing them yourself!). Remember that you don't write the program for the computer, you write it for other humans (maybe a future you!). Choose names that

explain things, add comments where these names don't suffice. Never comment on what the code is doing, only write comments that explain why.

This is a bad example:

```
// This function checks whether a number is even
def f(x):
  // compute x modulo 2 and check whether it is zero
  if modulo(x,2) == 0:
    // the number is even
    return True
else:
    // the number is odd
    return False
```

The exact same idea is much easier to understand if you write it like this:

```
def is_divisible(number, divisor):
    return modulo(number, divisor) == 0

def is_even(number):
    return is divisible(number, 2)
```

Better naming and a better task breakdown make the comments obsolete. Revise your code just as you would revise an essay. Sketch, write, delete, reformulate, ask others what they think. Repeat until only the crispest possible expression of your idea remains. Revisit code you've written a while ago to see whether you can improve it with things you've learned since.

Elementary

- 1. Write a program that prints 'Hello World' to the screen.
- 2. Write a program that asks the user for their name and greets them with their name.
- 3. Modify the previous program such that only the users Alice and Bob are greeted with their names.
- 4. Write a program that asks the user for a number n and prints the sum of the numbers 1 to n
- 5. Modify the previous program such that only multiples of three or five are considered in the sum, e.g. 3, 5, 6, 9, 10, 12, 15 for n=17
- 6. Write a program that asks the user for a number n and gives them the possibility to choose between computing the sum and computing the product of 1,...,n.
- 7. Write a program that prints a multiplication table for numbers up to 12.
- 8. Write a program that prints *all* prime numbers. (Note: if your programming language does not support arbitrary size numbers, printing all primes up to the largest number you can easily represent is fine too.)
- 9. Write a guessing game where the user has to guess a secret number. After every guess the program tells the user whether their number was too large or too small. At the end the number of tries needed should be printed. It counts only as one try if they input the same number multiple times consecutively.

- 10. Write a program that prints the next 20 leap years.
- 11. Write a program that computes the sum of an alternating series where each element of the series is an expression of the form $((-1)^{k+1})/(2*k-1)$ for each value of k from 1 to a million, multiplied by 4. Or, in more mathematical notation

$$4 \cdot \sum_{k=1}^{10^6} \frac{(-1)^{k+1}}{2k-1} = 4 \cdot (1 - 1/3 + 1/5 - 1/7 + 1/9 - 1/11...).$$

Lists, Strings

If your language of choice doesn't have a build in list and/or string type (e.g. you use C), these exercises should also be solvable for arrays. However, some solutions are very different between an array-based list (like C++'s vector) and a pointer based list (like C++'s list), at least if you care about the efficiency of your code. So you might want to either find a library, or investigate how to implement your own linked list if your language doesn't have it.

- 1. Write a function that returns the largest element in a list.
- 2. Write function that reverses a list, preferably in place.
- 3. Write a function that checks whether an element occurs in a list.
- 4. Write a function that returns the elements on odd positions in a list.
- 5. Write a function that computes the running total of a list.
- 6. Write a function that tests whether a string is a palindrome.
- 7. Write three functions that compute the sum of the numbers in a list: using a for-loop, a while-loop and recursion. (Subject to availability of these constructs in your language of choice.)
- 8. Write a function on_all that applies a function to every element of a list. Use it to print the first twenty perfect squares. The perfect squares can be found by multiplying each natural number with itself. The first few perfect squares are 1*1= 1, 2*2=4, 3*3=9, 4*4=16. Twelve for example is not a perfect square because there is no natural number m so that m*m=12. (This question is tricky if your programming language makes it difficult to pass functions as arguments.)
- 9. Write a function that concatenates two lists. [a,b,c], [1,2,3] \rightarrow [a,b,c,1,2,3]
- 10. Write a function that combines two lists by alternatingly taking elements, e.g. [a,b,c], $[1,2,3] \rightarrow [a,1,b,2,c,3]$.
- 11. Write a function that merges two sorted lists into a new sorted list. [1,4,6], [2,3,5] → [1,2,3,4,5,6]. You can do this quicker than concatenating them followed by a sort.
- 12. Write a function that rotates a list by k elements. For example [1,2,3,4,5,6] rotated by two becomes [3,4,5,6,1,2]. Try solving this without creating a copy of the list. How many swap or move operations do you need?
- 13. Write a function that computes the list of the first 100 Fibonacci numbers. The first two Fibonacci numbers are 1 and 1. The n+1-st Fibonacci number can be computed by adding the n-th and the n-1-th Fibonacci number. The first few are therefore 1, 1, 1+1=2, 1+2=3, 2+3=5, 3+5=8.

- 14. Write a function that takes a number and returns a list of its digits. So for 2342 it should return [2,3,4,2].
- 15. Write functions that add, subtract, and multiply two numbers in their digit-list representation (and return a new digit list). If you're ambitious you can implement <u>Karatsuba multiplication</u>. Try <u>different bases</u>. What is the best base if you care about speed? If you couldn't completely solve the prime number exercise above due to the lack of large numbers in your language, you can now use your own library for this task.
- 16. Write a function that takes a list of numbers, a starting base b1 and a target base b2 and interprets the list as a number in base b1 and converts it into a number in base b2 (in the form of a list-of-digits). So for example [2,1,0] in base 3 gets converted to base 10 as [2,1].
- 17. Implement the following sorting algorithms: Selection sort, Insertion sort, Merge sort, Quick sort, Stooge Sort. Check Wikipedia for descriptions.
- 18. Implement binary search.
- 19. Write a function that takes a list of strings an prints them, one per line, in a rectangular frame. For example the list ["Hello", "World", "in", "a", "frame"] gets printed as:

```
*******

* Hello *

* World *

* in *

* a *

* frame *

*******
```

20. Write function that translates a text to Pig Latin and back. English is translated to Pig Latin by taking the first letter of every word, moving it to the end of the word and adding 'ay'. "The quick brown fox" becomes "Hetay uickqay rownbay oxfay".

Intermediate

- 1. Write a program that outputs all possibilities to put + or or nothing between the numbers 1,2,...,9 (in this order) such that the result is 100. For example 1 + 2 + 3 4 + 5 + 6 + 78 + 9 = 100.
- 2. Write a program that takes the duration of a year (in fractional days) for an imaginary planet as an input and produces a leap-year rule that minimizes the difference to the planet's solar year.
- 3. Implement a data structure for graphs that allows modification (insertion, deletion). It should be possible to store values at edges and nodes. It might be easiest to use a dictionary of (node, edgelist) to do this.
- 4. Write a function that generates a DOT representation of a graph.
- 5. Write a program that automatically generates essays for you.
 - 1. Using a sample text, create a directed (multi-)graph where the words of a text are nodes and there is a directed edge between u and v if u is followed by v in your sample text. Multiple occurrences lead to multiple edges.

- 2. Do a random walk on this graph: Starting from an arbitrary node choose a random successor. If no successor exists, choose another random node.
- 6. Write a program that automatically converts English text to Morse code and vice versa.
- 7. Write a program that finds the longest palindromic substring of a given string. Try to be as efficient as possible!
- 8. Think of a good interface for a list. What operations do you typically need? You might want to investigate the list interface in your language and in some other popular languages for inspiration.
- 9. Implement your list interface using a fixed chunk of memory, say an array of size 100. If the user wants to add more stuff to your list than fits in your memory you should produce some kind of error, for example you can throw an exception if your language supports that.
- 10. Improve your previous implementation such that an arbitrary number of elements can be stored in your list. You can for example allocate bigger and bigger chunks of memory as your list grows, copy the old elements over and release the old storage. You should probably also release this memory eventually if your list shrinks enough not to need it anymore. Think about how much bigger the new chunk of memory should be so that your performance won't be killed by allocations. Increasing the size by 1 element for example is a bad idea.
- 11. If you chose your growth right in the previous problem, you typically won't allocate very often. However, adding to a big list sometimes consumes considerable time. That might be problematic in some applications. Instead try allocating new chunks of memory for new items. So when your list is full and the user wants to add something, allocate a new chunk of 100 elements instead of copying all elements over to a new large chunk. Think about where to do the book-keeping about which chunks you have. Different book keeping strategies can quite dramatically change the performance characteristics of your list.
- 12. Implement a binary heap. Once using a list as the base data structure and once by implementing a pointer-linked binary tree. Use it for implementing heap-sort.
- 13. Implement an unbalanced binary search tree.
- 14. Implement a balanced binary search tree of your choice. I like (a,b)-trees best.
- 15. Compare the performance of insertion, deletion and search on your unbalanced search tree with your balanced search tree and a sorted list. Think about good input sequences. If you implemented an (a,b)-tree, think about good values of a and b.

Advanced

- 1. Given two strings, write a program that efficiently finds the longest common subsequence.
- 2. Given an array with numbers, write a program that efficiently answers queries of the form: "Which is the nearest larger value for the number at position i?", where distance is the difference in array indices. For example in the array [1,4,3,2,5,7], the nearest larger value for 4 is 5. After linear time preprocessing you should be able to answer queries in constant time.
- 3. Given two strings, write a program that outputs the shortest sequence of character insertions and deletions that turn one string into the other.
- 4. Write a function that multiplies two matrices together. Make it as efficient as you can and compare the performance to a polished linear algebra library for your

- language. You might want to read about <u>Strassen's algorithm</u> and the effects CPU caches have. Try out different matrix layouts and see what happens.
- 5. Implement a <u>van Emde Boas</u> tree. Compare it with your previous search tree implementations.
- 6. Given a set of d-dimensional rectangular boxes, write a program that computes the volume of their union. Start with 2D and work your way up.

GUI

- Write a program that displays a bouncing ball.
- Write a Memory game.
- Write a Tetris clone

Open Ended

- 1. Write a program that plays Hangman as good as possible. For example you can use a large dictionary like <u>this</u> and select the letter that excludes most words that are still possible solutions. Try to make the program as efficient as possible, i.e. don't scan the whole dictionary in every turn.
- 2. Write a program that plays Rock, Paper, Scissors better than random against a human. Try to exploit that humans are very bad at generating random numbers.
- 3. Write a program that plays Battle Ship against human opponents. It takes coordinates as input and outputs whether that was a hit or not and its own shot's coordinates.

Other Collections

Of course I'm not the first person to come up with the idea of having a list like this.

- John Dalbey's collection
 - Several small problems <u>Programming Practice</u>
 - CPE 101 Projects
- Code Kata
- 99 Lisp Problems, 99 Haskell Problems. Most of these can also be done in other languages.
- Rosetta Code Programming Tasks. These come with solutions in many languages!
- <u>Code Golf Challenges</u>. The goal here is to solve the problem with as few characters as possible.
- SPOJ Problems. This is a list of more than 13000 Problems!
- <u>Code Abbey</u> According to Github user RodionGork, this is less mathy than Project Euler.

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