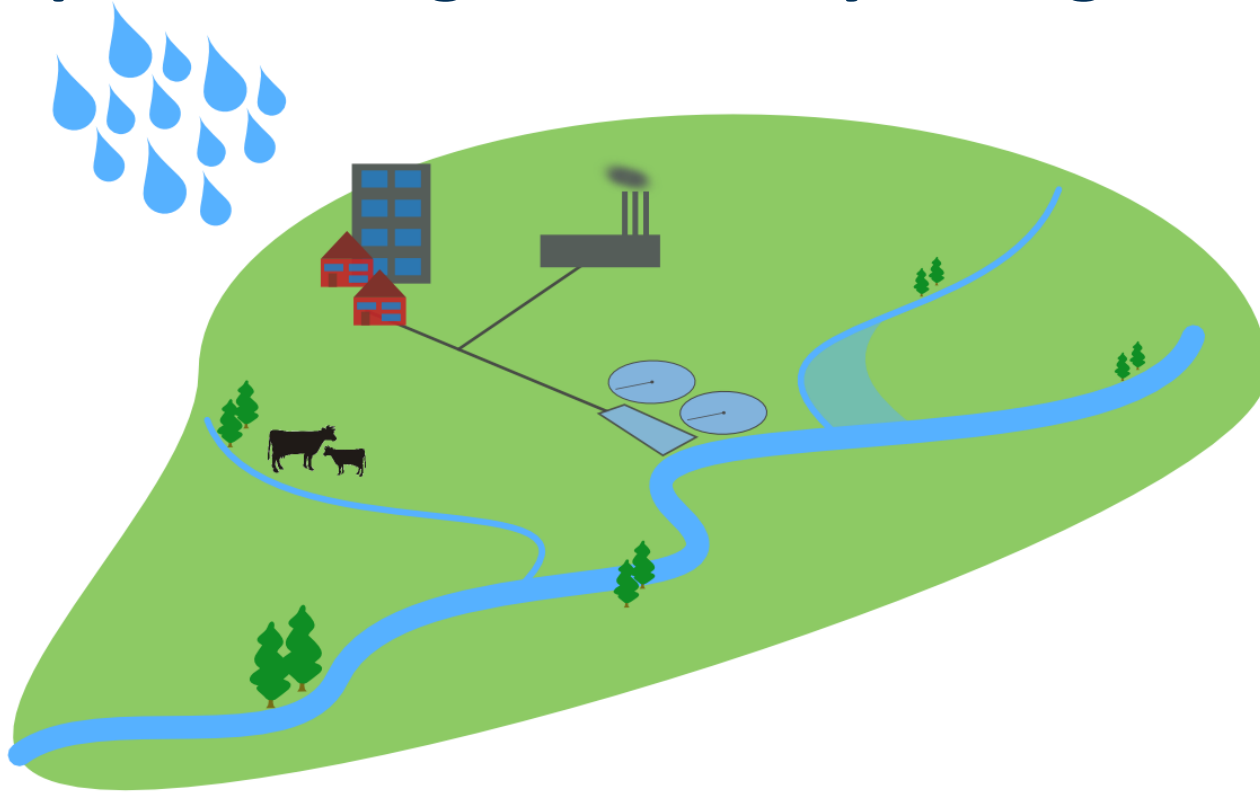


30/05/2012

## Hydrological model structure evaluation

S. Van Hoey, J. Van der Kwast, I. Nopens, P. Seuntjens

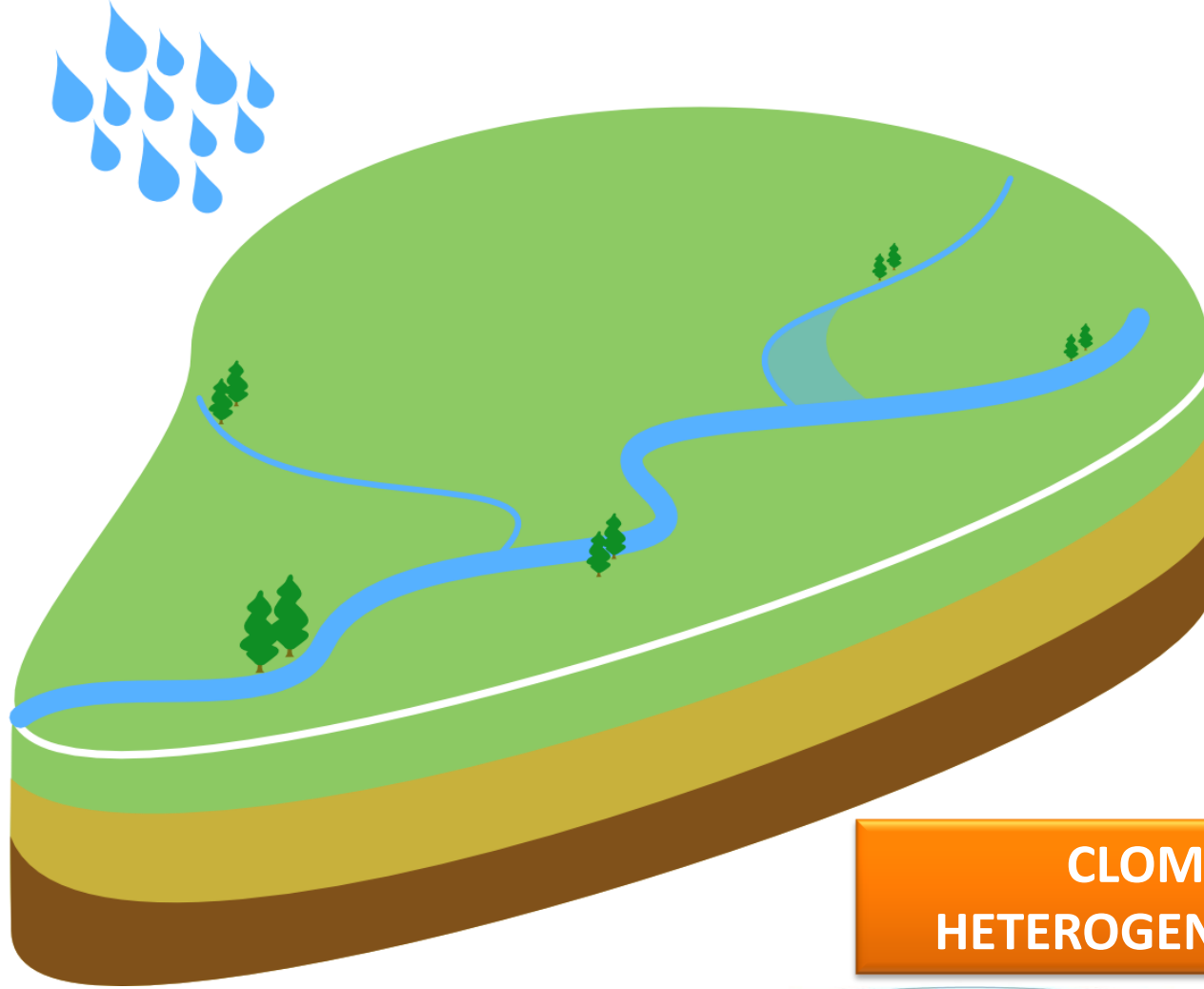
# A priori: Integrated <> Hydrological Modelling



# A priori: Integrated <> Hydrological Modelling

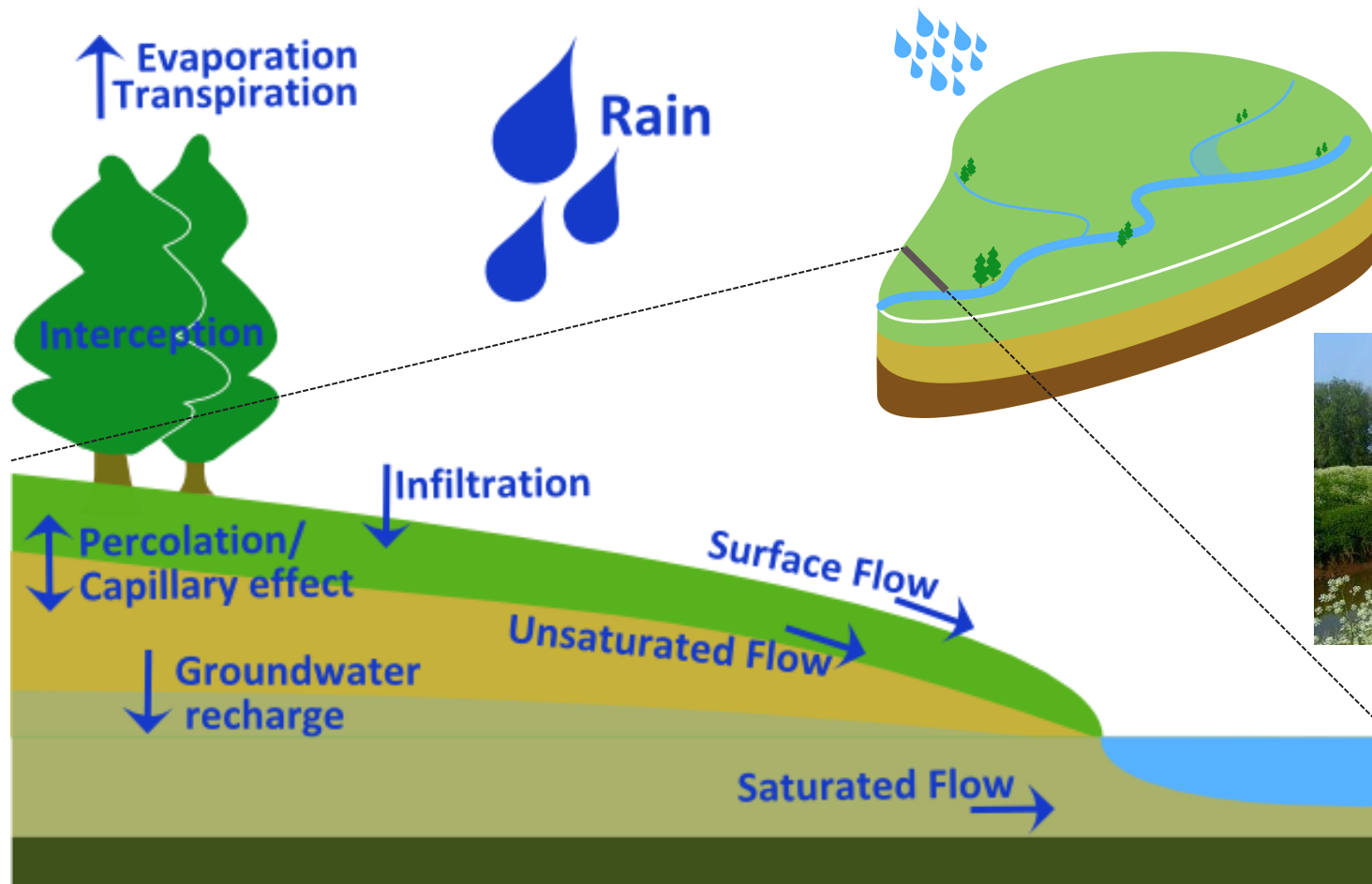


# A priori: Hydrological Catchment Modelling

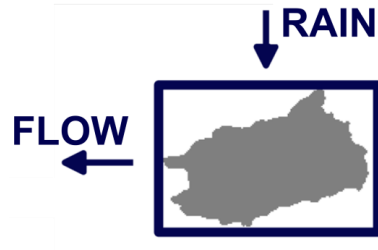


**CLOMPEX AND  
HETEROGENEOUS SYSTEM**

# A priori: Hydrological Catchment Modelling

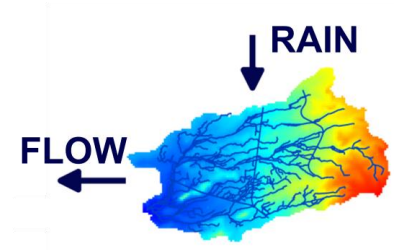


# A priori: Hydrological Catchment Modelling



## LUMPED

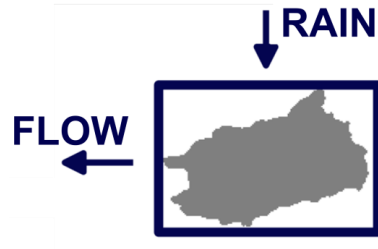
- » No spatial component
- » Set of ODE's
- » Short computation time
- » Describing *Dominant Processes* on catchment level
- » Rainfall-runoff models



## DISTRIBUTED

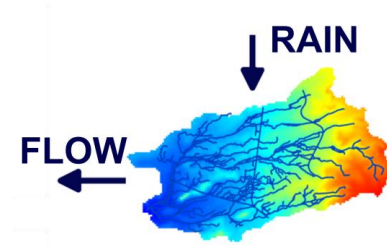
- » Spatially explicit
- » ODE/PDE options
- » Long computation time
- » Water balance on pixel-level + inter-pixel routing component
- » Spatial data-inputs

# A priori: Hydrological Catchment Modelling



## LUMPED

- » No spatial component
- » Set of ODE's
- » Short computation time
- » Describing *Dominant Processes* on catchment level
- » Rainfall-runoff models

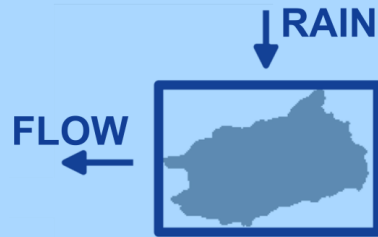


## DISTRIBUTED

- » Spatially explicit
- » ODE/PDE options
- » Long computation time
- » Water balance on pixel-level + inter-pixel routing component
- » Spatial data-inputs

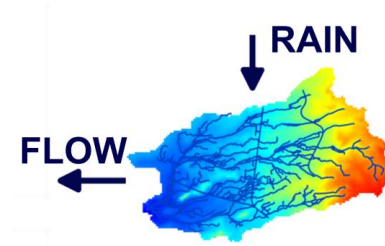
**WHICH processes to include?**  
**HOW to describe these processes?**

# Today: Lumped Hydrological Modelling



## LUMPED

- » No spatial component
- » Set of ODE's
- » Short computation time
- » Describing *Dominant Processes* on catchment level
- » Rainfall-runoff models



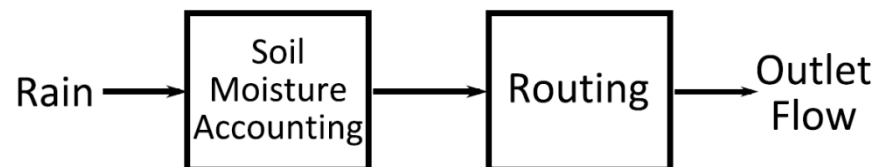
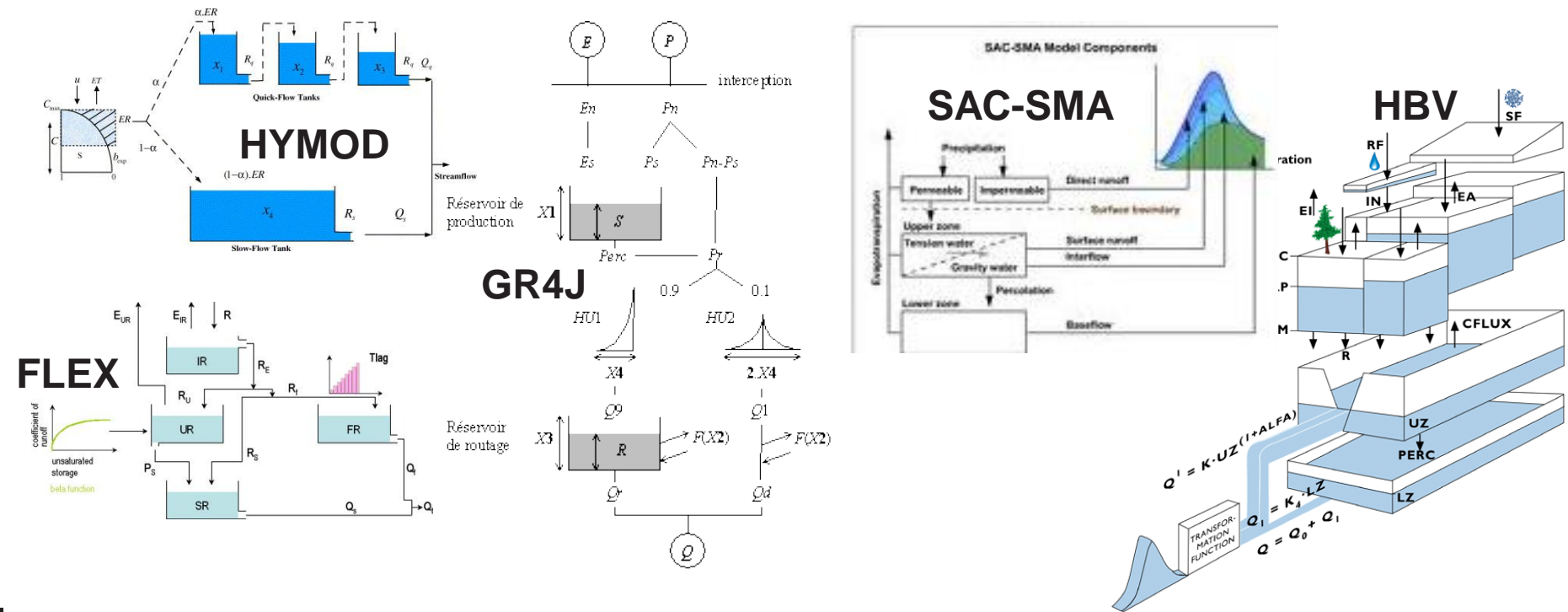
## DISTRIBUTED

- » Spatially explicit
- » ODE/PDE options
- » Long computation time
- » Water balance on pixel-level + inter-pixel routing component
- » Spatial data-inputs

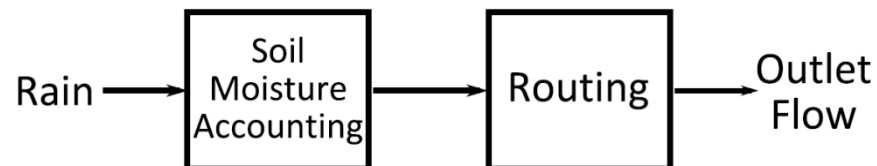
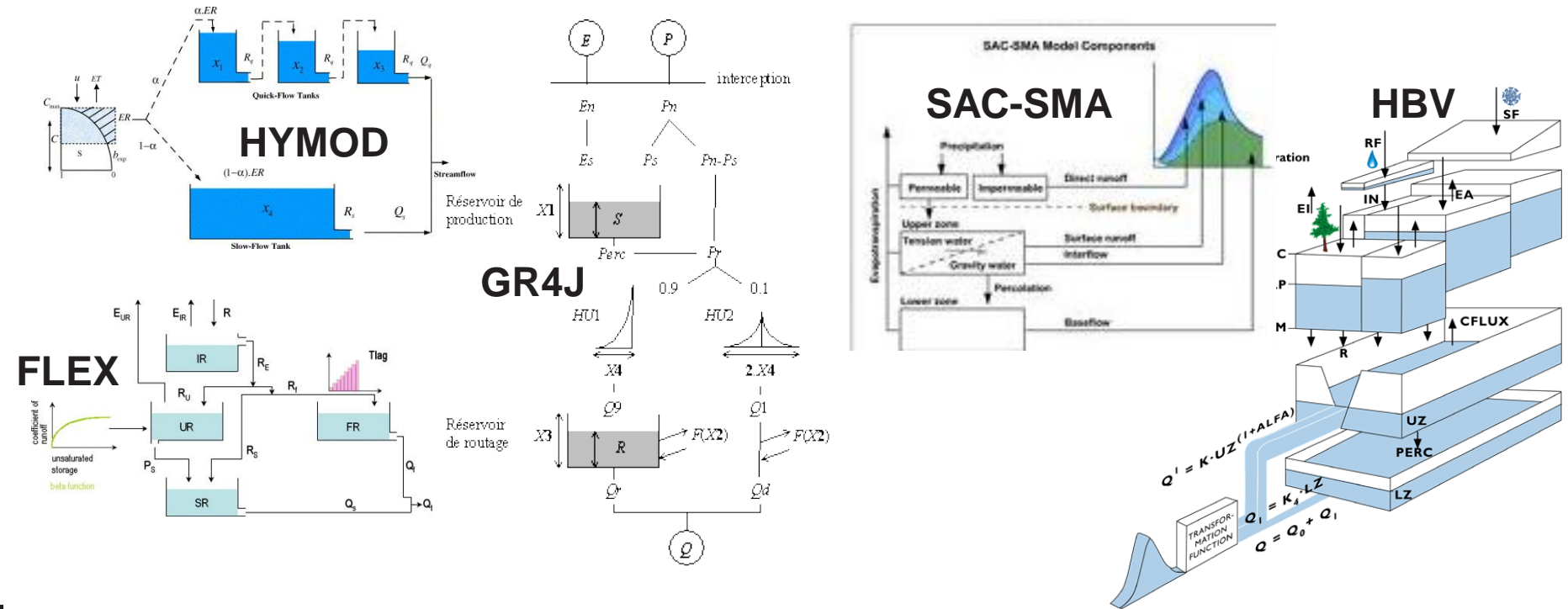
**WHICH processes to include?**  
**HOW to describe these processes?**



# Lumped representations of the catchment

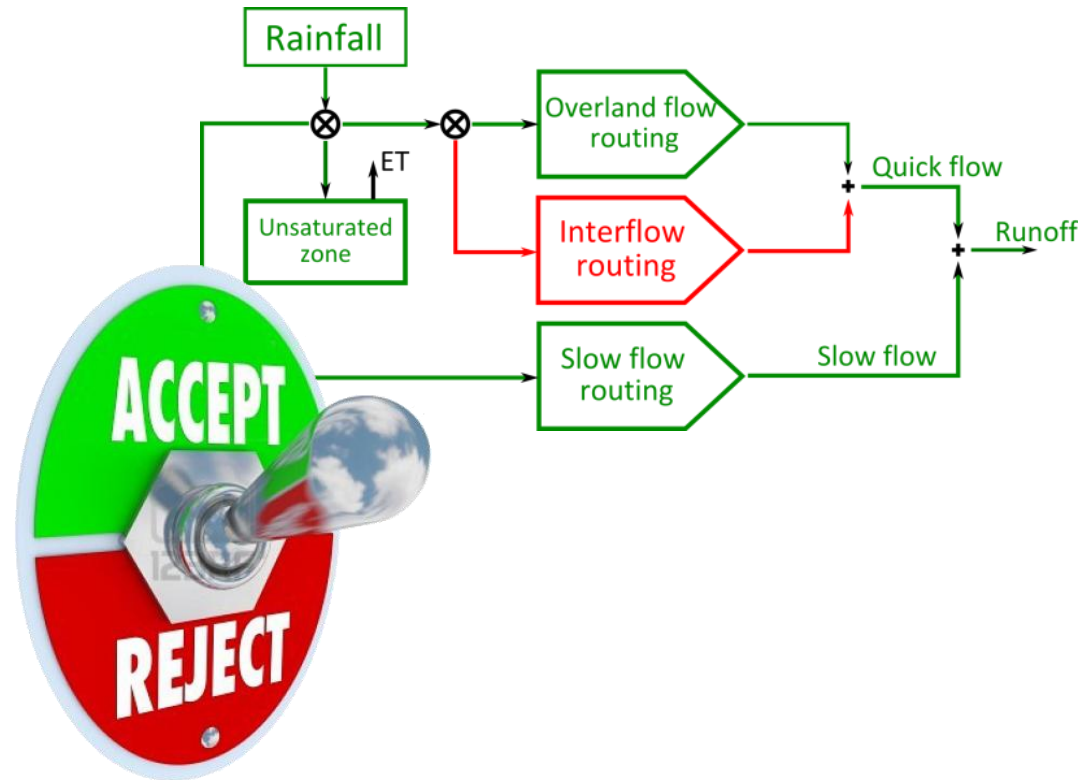
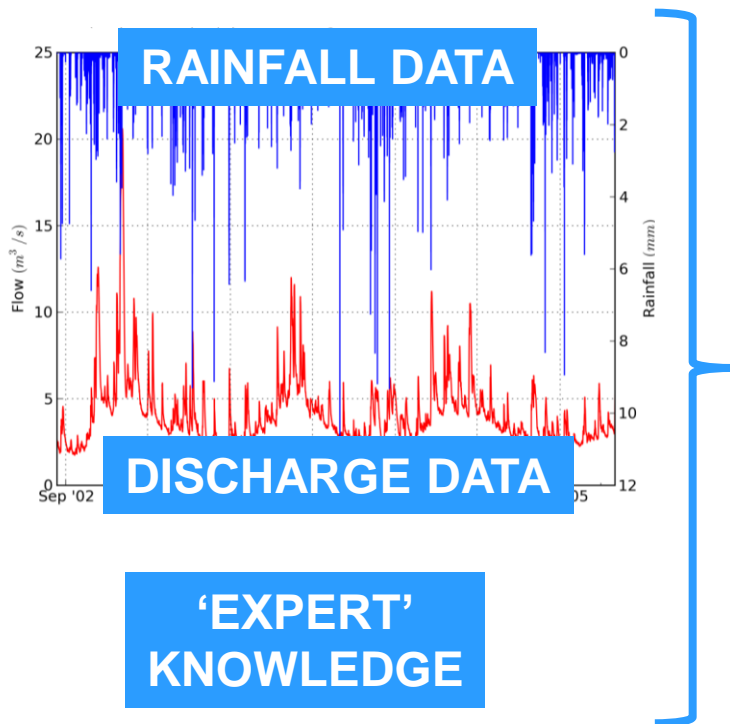


# Lumped representations of the catchment



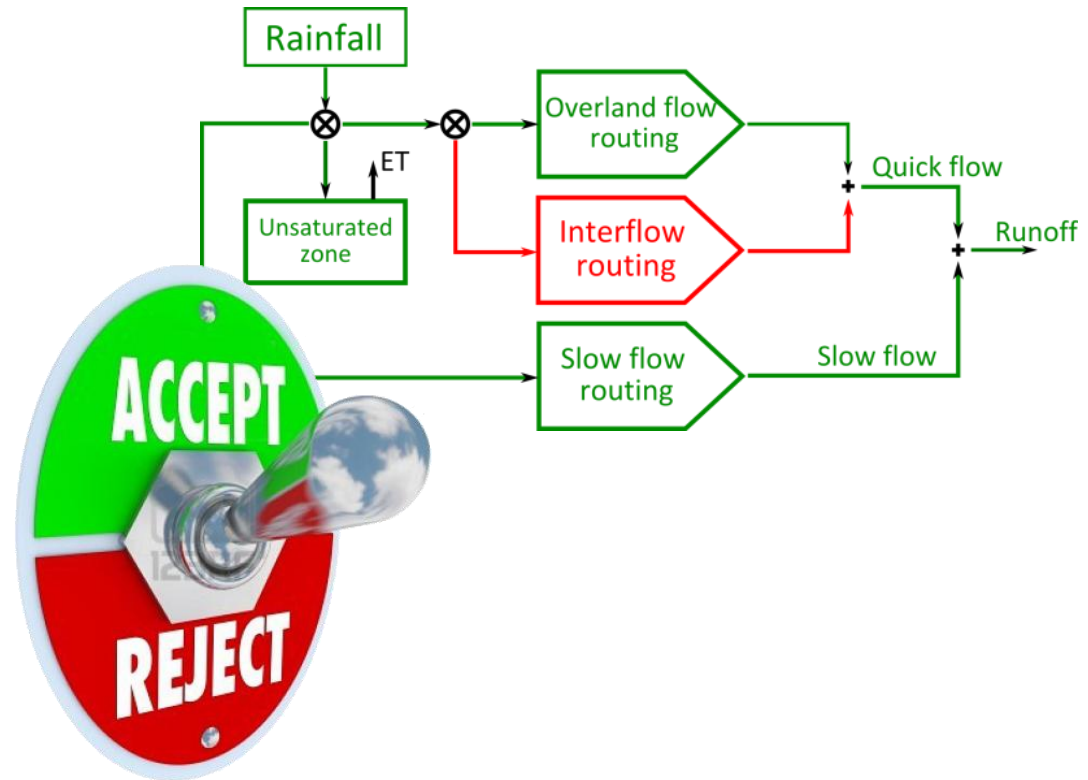
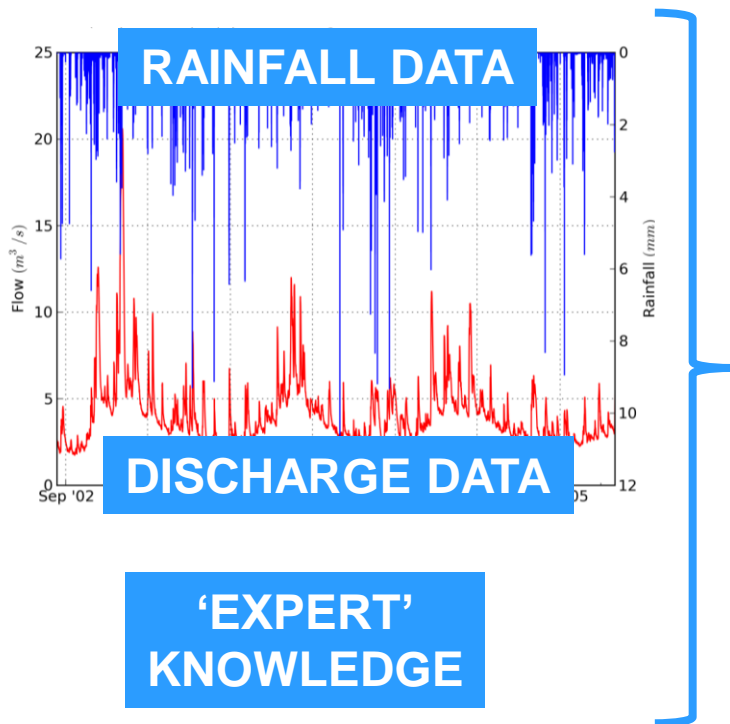
There is no 'one model fits all' -> need for flexibility!

# Wishfull thinking...



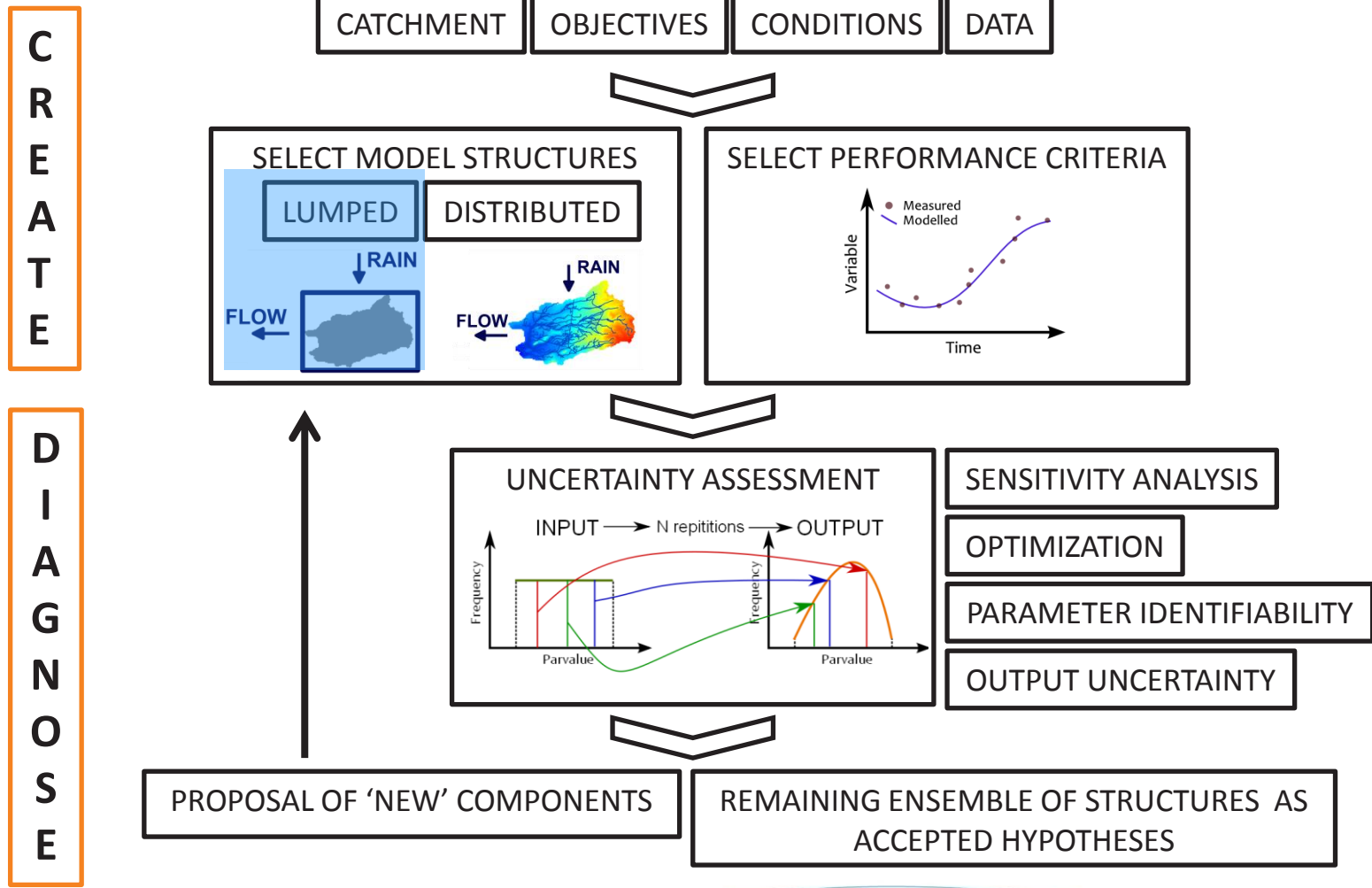
*No one model fits all, but different models fit well  
=> We want the right answer for the right reasons*

# Wishfull thinking...



Can we identify the most suitable model structure?  
Is this suitable structure conditioned by the performance criteria?

# Methodology



# Application

## » Nete catchment

» Belgium, 362km<sup>2</sup>

## » Data

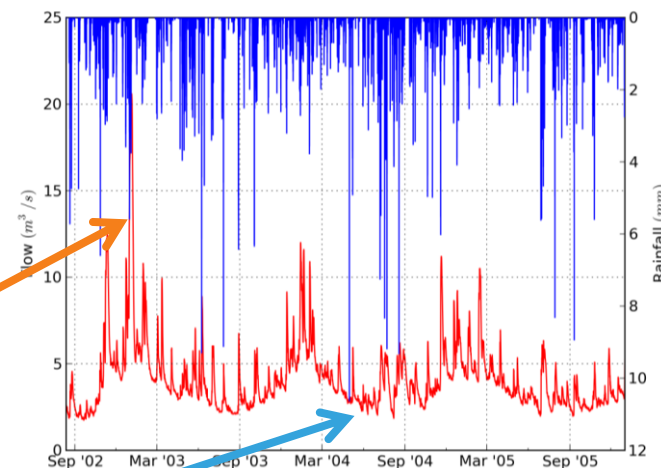
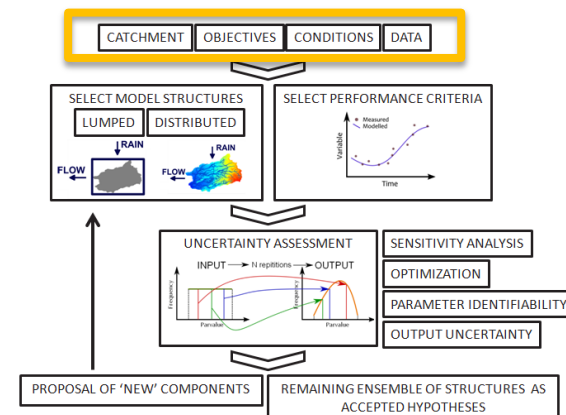
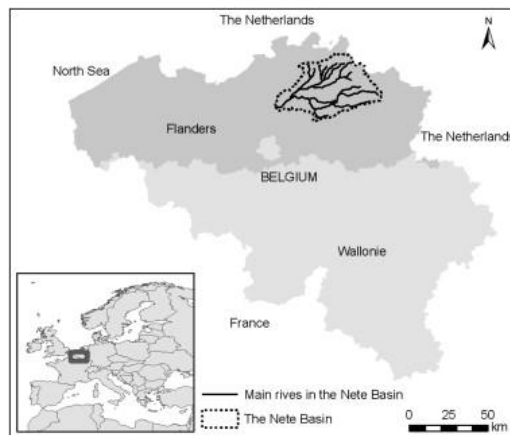
» Rainfall (2002-2008, hourly timestep)

» Flow at outlet (2002-2008, hourly timestep)

» **Objectives:** Understanding in dominant hydrological processes:

» Flood risk in winter: peak discharges

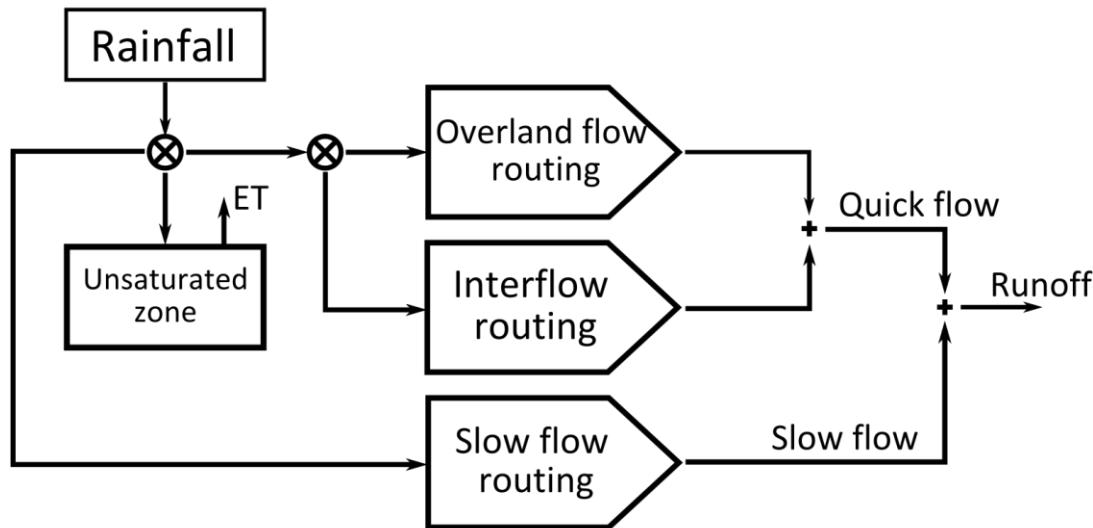
» Water availability in summer: baseflow reproduction



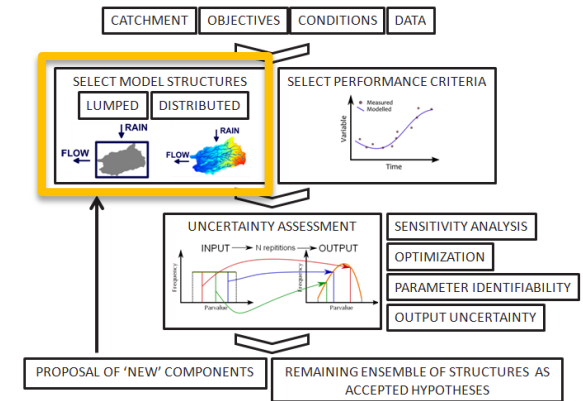
# Model Structure Selection

## LUMPED MODEL

Model structure variations based on VHM model (Willems, P.)



(Clark M.,2008; Willems P.,submitted)

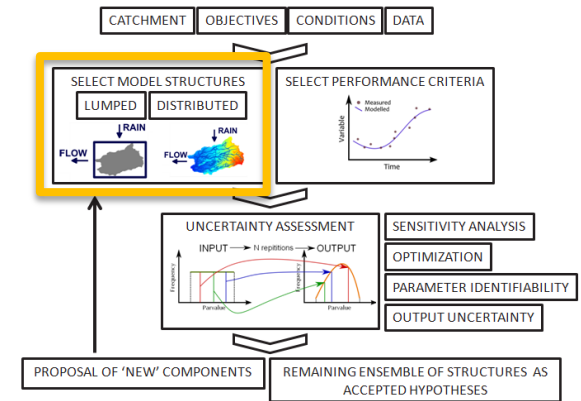
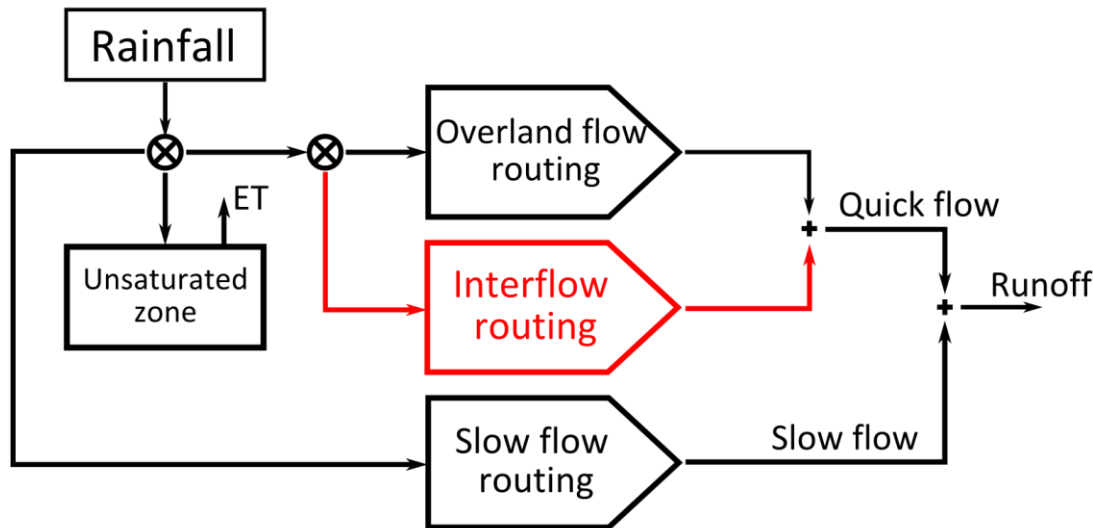
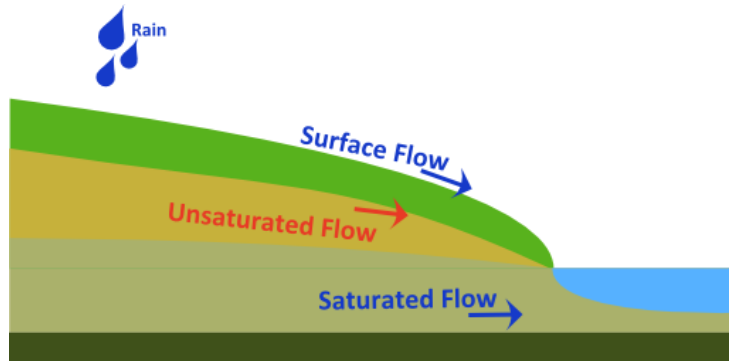


## HYPOTHESES

- » Presence of Interflow?
- » Unsaturated zone: Linear or non-linear?
- » Which combination of linear reservoirs to represent routing?
- » Infiltration excess overland flow dominant?



# Model Structure Selection



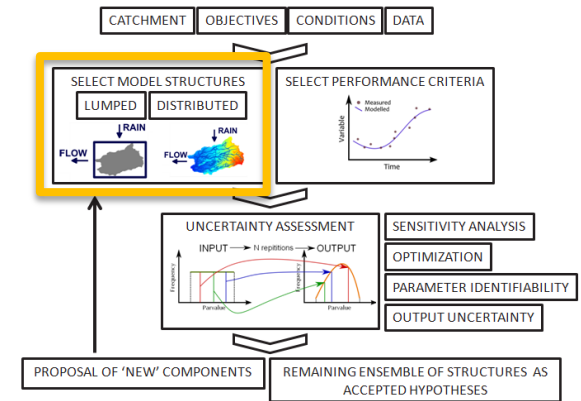
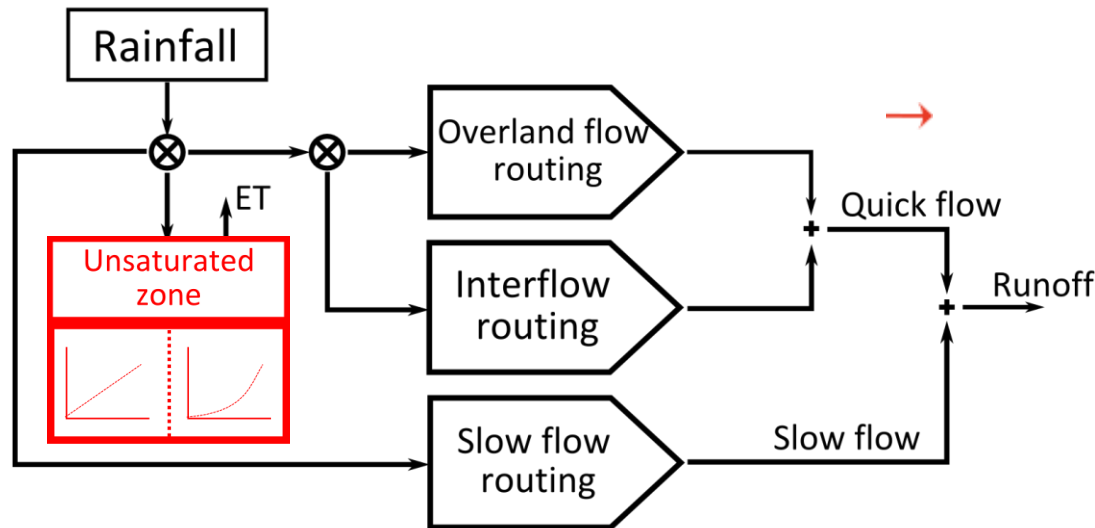
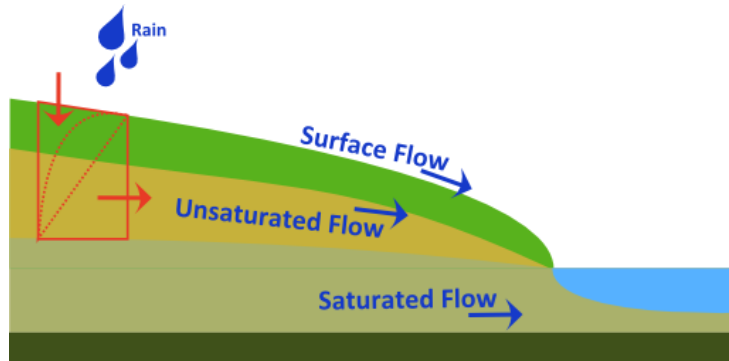
## HYPOTHESES

- » Presence of **Interflow**?
- » Unsaturated zone: Linear or non-linear?
- » Which combination of linear reservoirs to represent routing?
- » Infiltration excess overland flow dominant?

(Clark M.,2008; Willems P.,submitted)



# Model Structure Selection

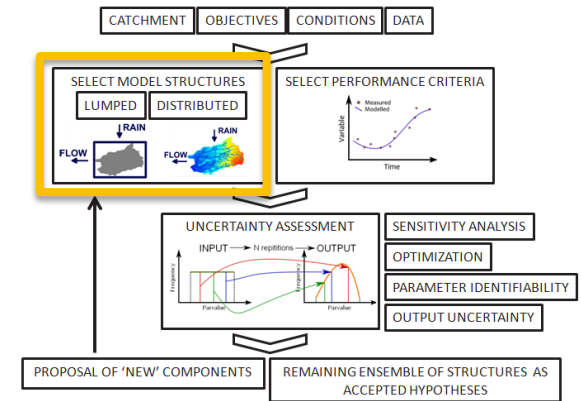
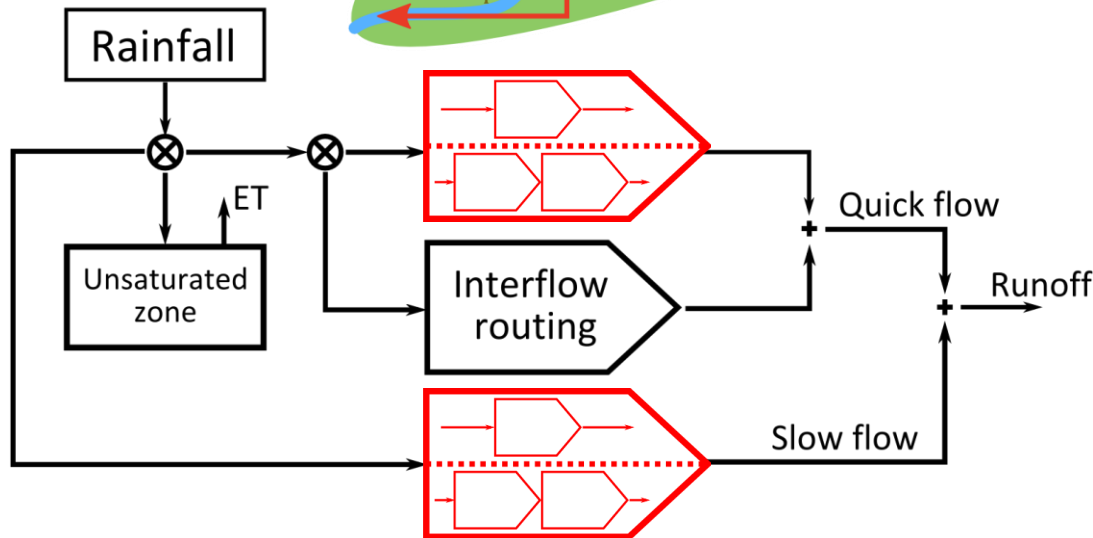


## HYPOTHESES

- » Presence of Interflow?
- » **Unsaturated zone**: Linear or non-linear?
- » Which combination of linear reservoirs to represent routing?
- » Infiltration excess overland flow dominant?

(Clark M.,2008; Willems P.,submitted)

# Model Structure Selection

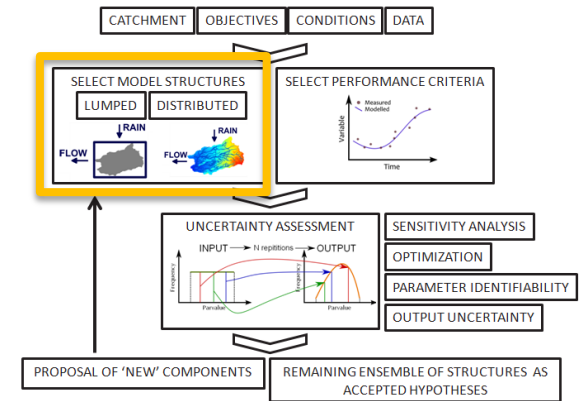
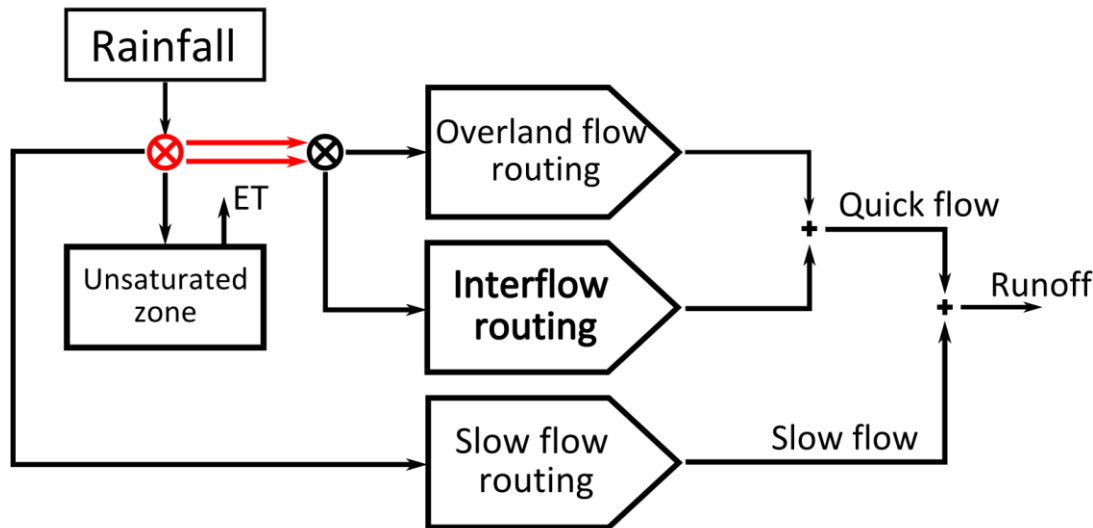
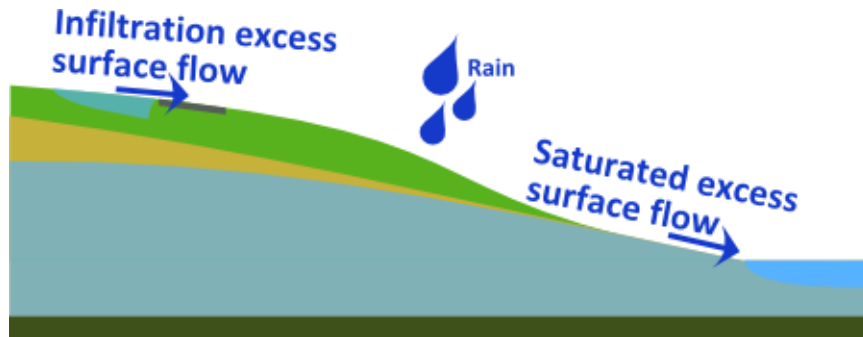


## HYPOTHESES

- » Presence of Interflow?
- » Unsaturated zone: Linear or non-linear?
- » Which combination of **linear reservoirs** to represent routing?
- » Infiltration excess overland flow dominant?

(Clark M.,2008; Willems P.,submitted)

# Model Structure Selection



## HYPOTHESES

- » Presence of Interflow?
- » Unsaturated zone: Linear or non-linear?
- » Which combination of linear reservoirs to represent routing?
- » **Infiltration excess** overland flow dominant?

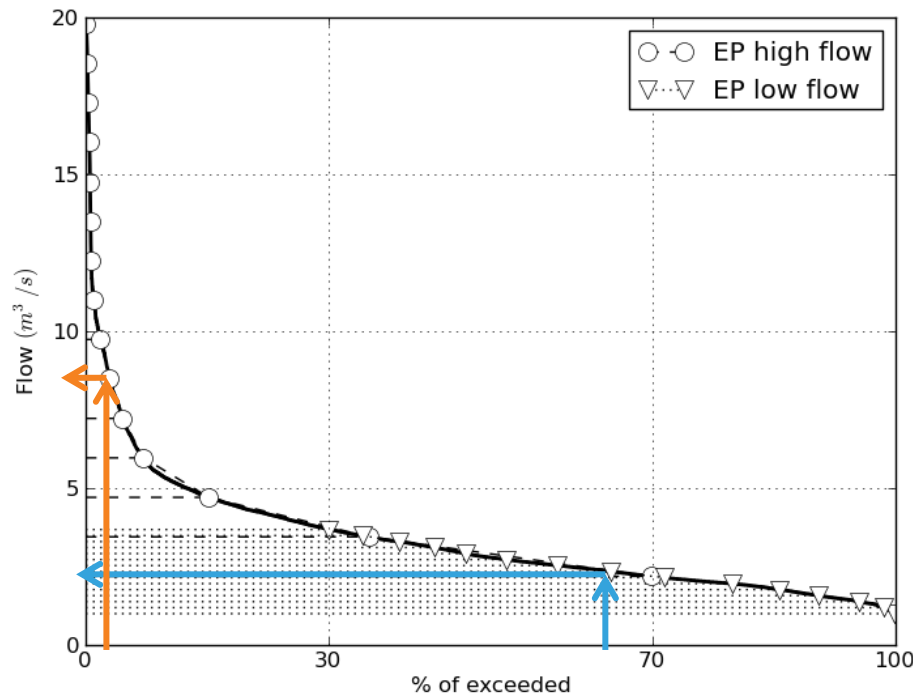
(Clark M.,2008; Willems P.,submitted)

# Performance criteria selection

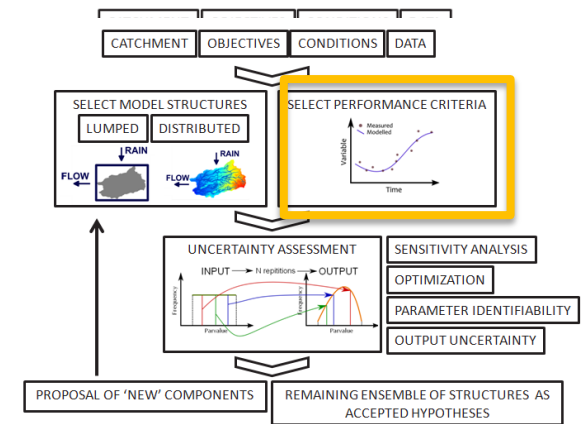
## FLOW DURATION CURVE BASED

» **High flow** and **Low flow**

» In combination with Nash Sutcliffe (NS) criterium: :  $W1*NS + W2*FDC^{err}$



$$NS = 1 - \frac{\sum_{i=1}^N (\hat{x}_i - x_i)^2}{\sum_{i=1}^N (x_i - \bar{x})^2}$$

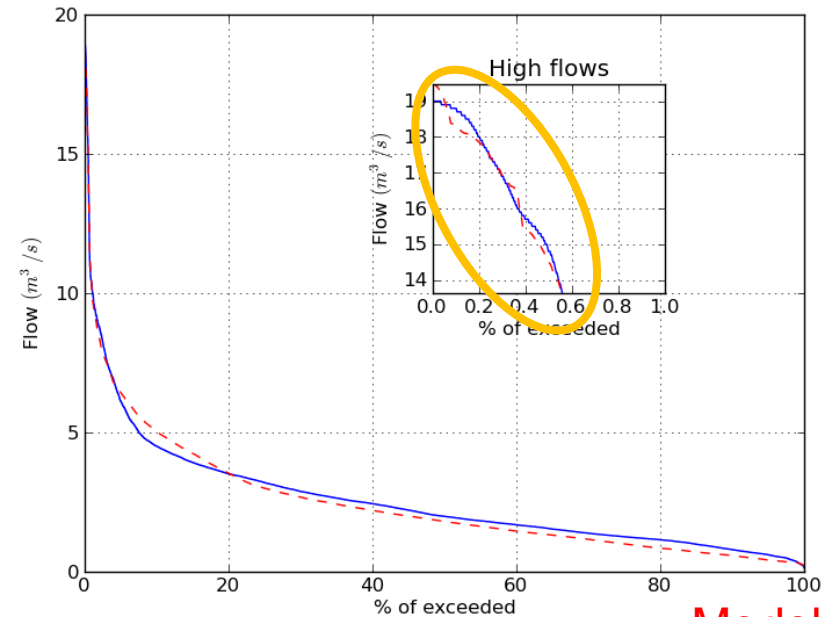
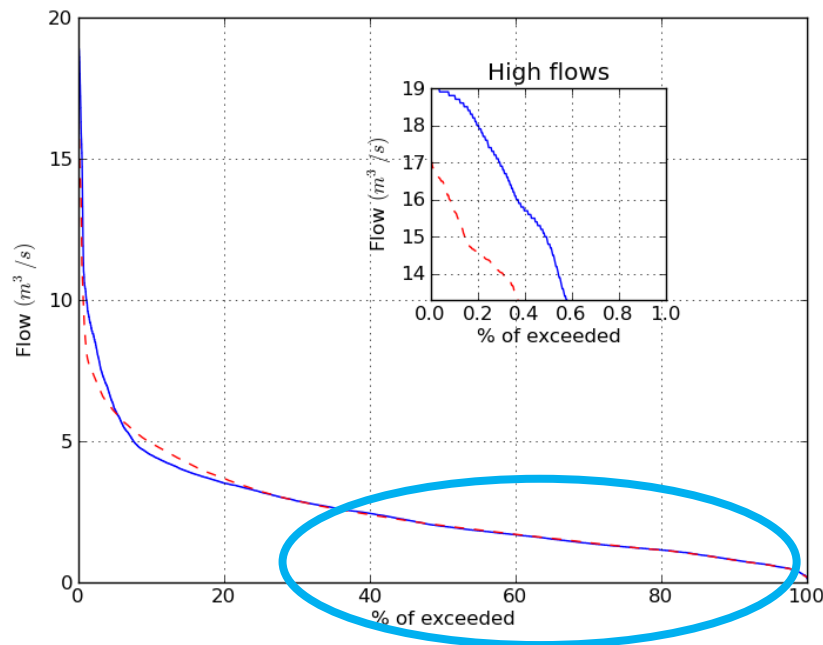
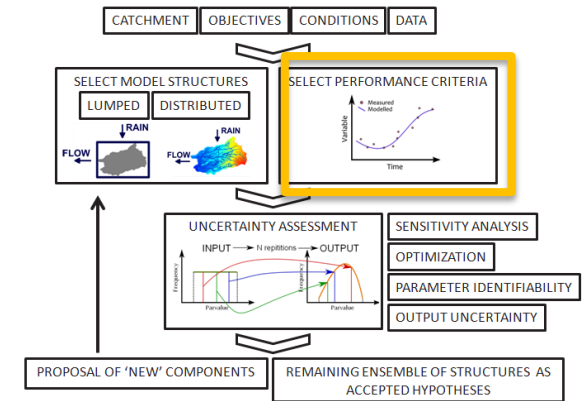


# Performance criteria selection

## FLOW DURATION CURVE BASED

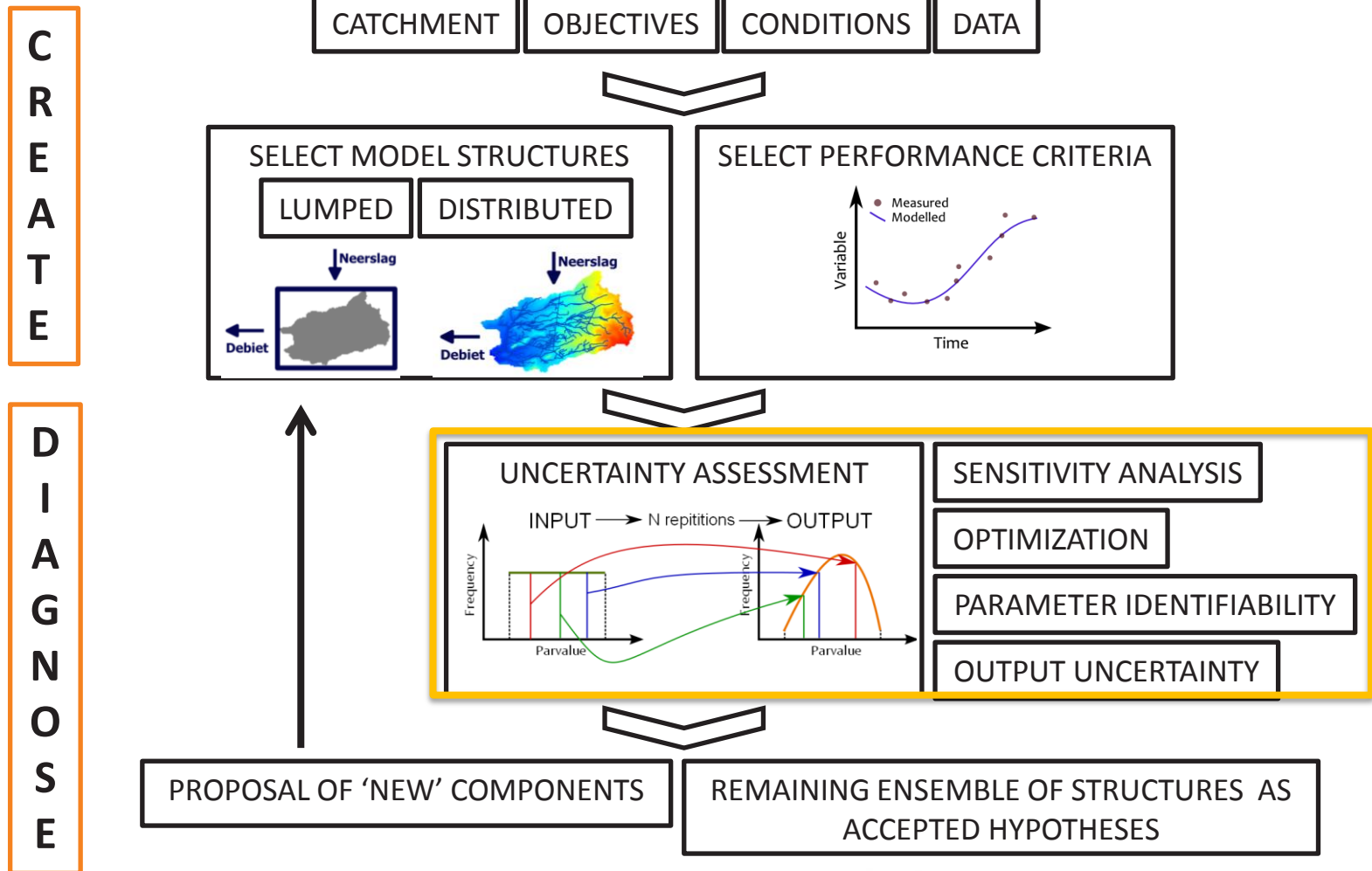
» **High flow** and **Low flow**

» In combination with Nash-Sutcliffe (NS) criterium:  $W1 * NS + W2 * FDC^{err}$



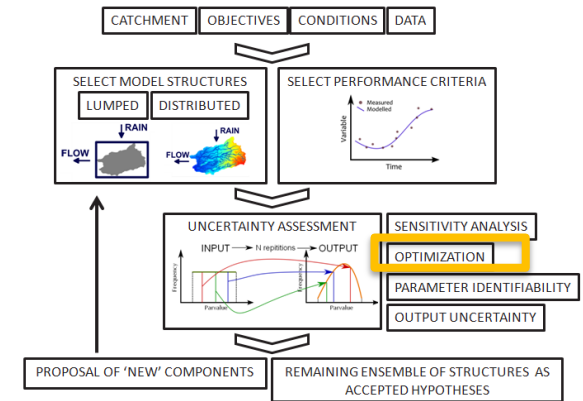
- Model  
- Measured

# Methodology



# Optimization results: 1 structure

	Calibration period					Validation Period				
	NS	lowflow	highflow	NS – FDClow	NS – FDChigh	NS	lowflow	highflow	NS – FDClow	NS – FDChigh
<b>NS</b>	0.85	0.57	0.75	0.85	0.84	0.7	0.51	0.61	0.69	0.67

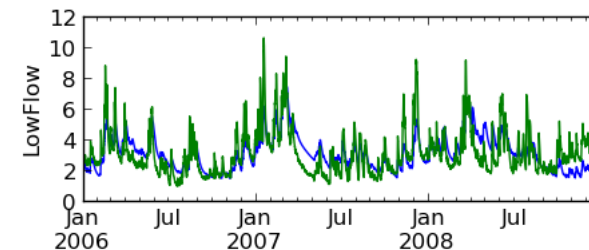
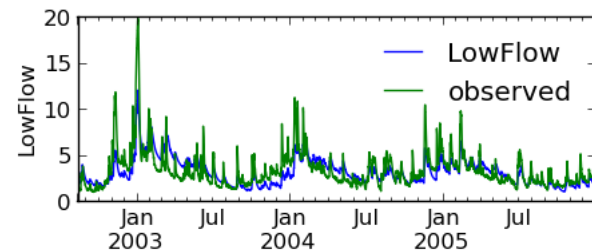
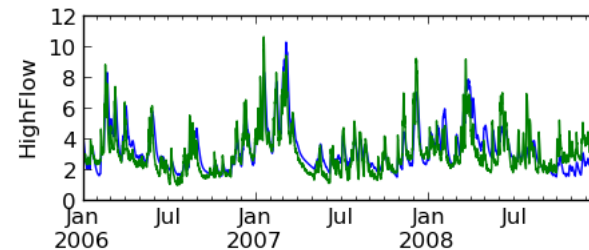
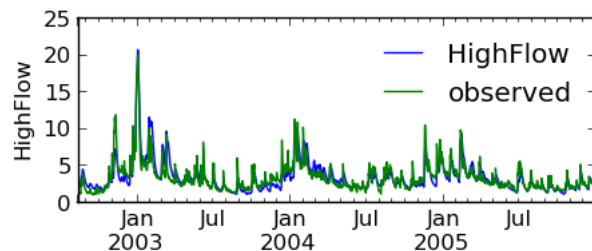
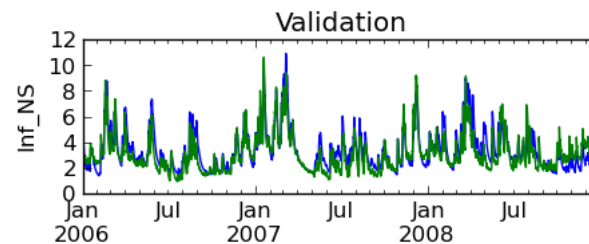
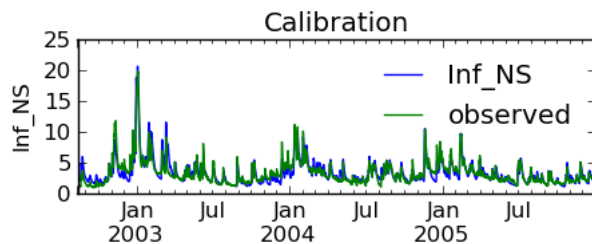


Optimization method used:  
*Shuffled Complex Evolution*

**NS**

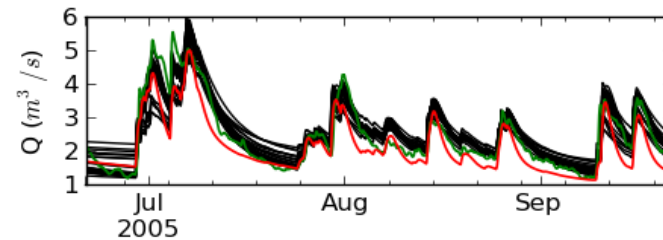
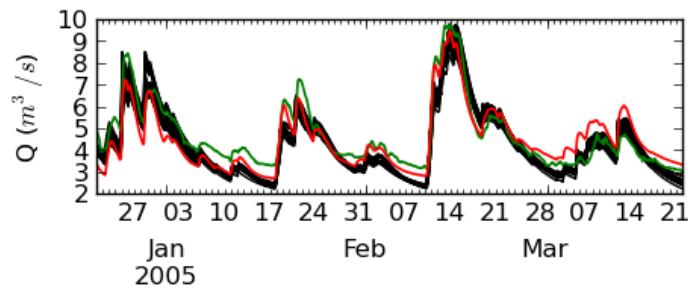
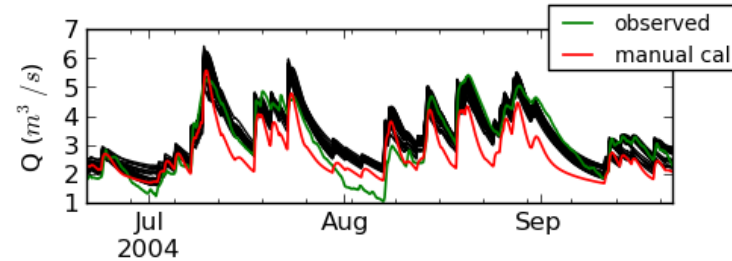
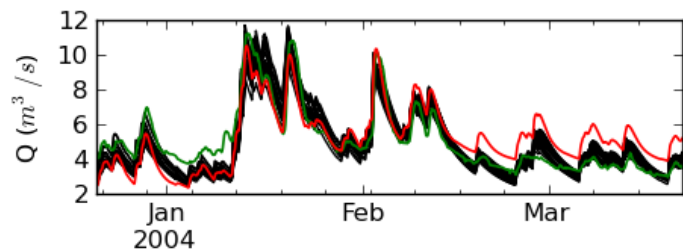
**FDC<sup>err</sup><sub>high</sub>**

**FDC<sup>err</sup><sub>low</sub>**

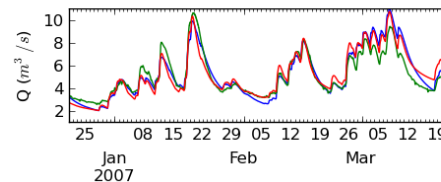
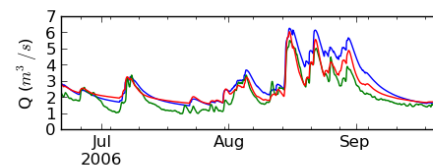




# Optimization results: ensemble



Validation events

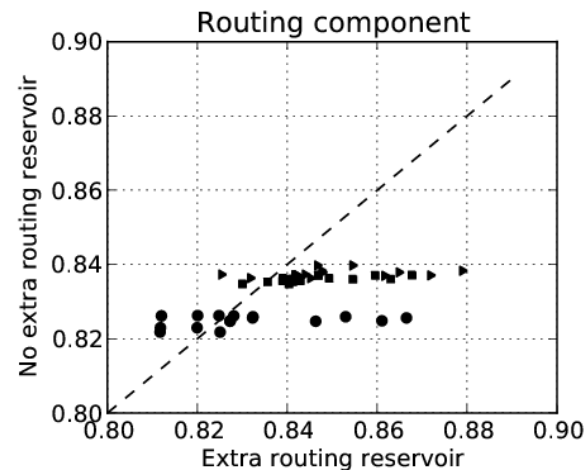
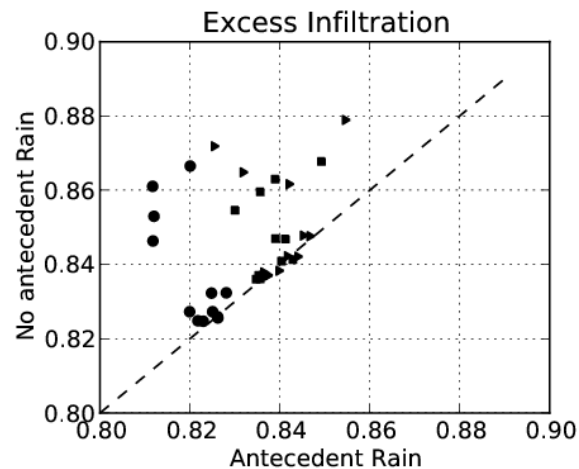
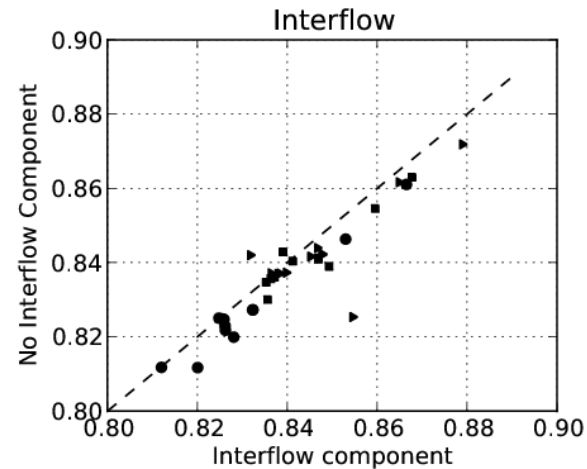
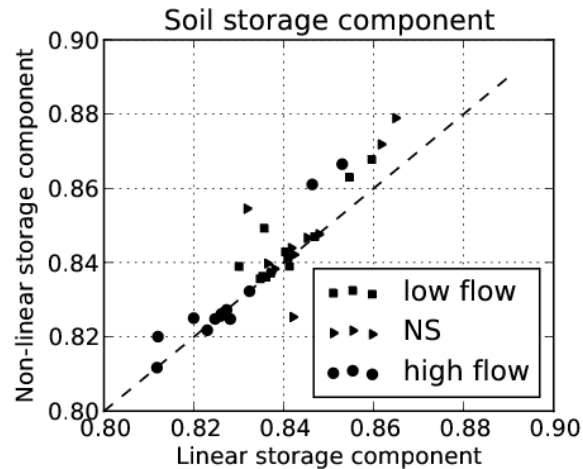


Manual calibration by Vansteenkiste T.  
Based on 'general calibration methodology'  
used at Hydraulics Laboratorium

	Mean of ensemble performance on calibration period
NSE	0.86
R <sup>2</sup>	0.93
MAE	0.56
RMSE	0.77

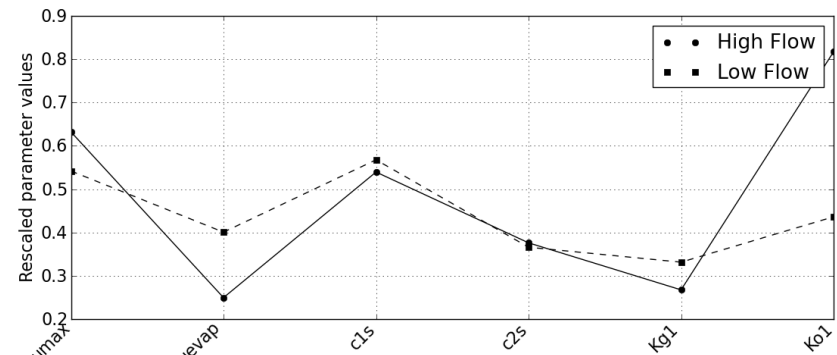
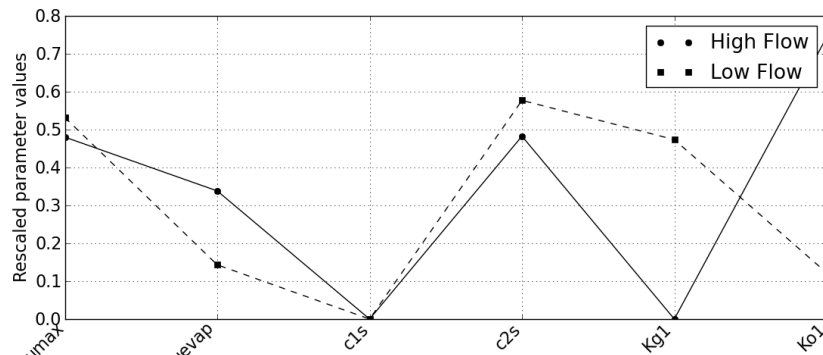
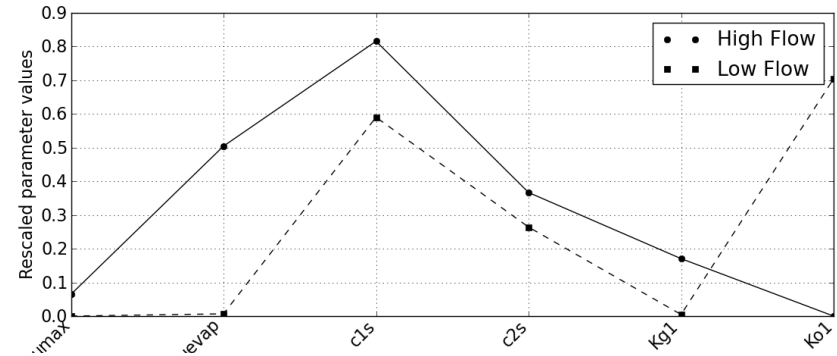
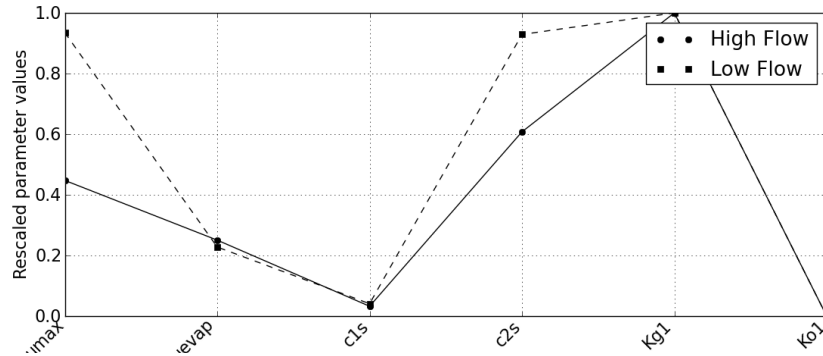


# Optimization: structures are doing well...



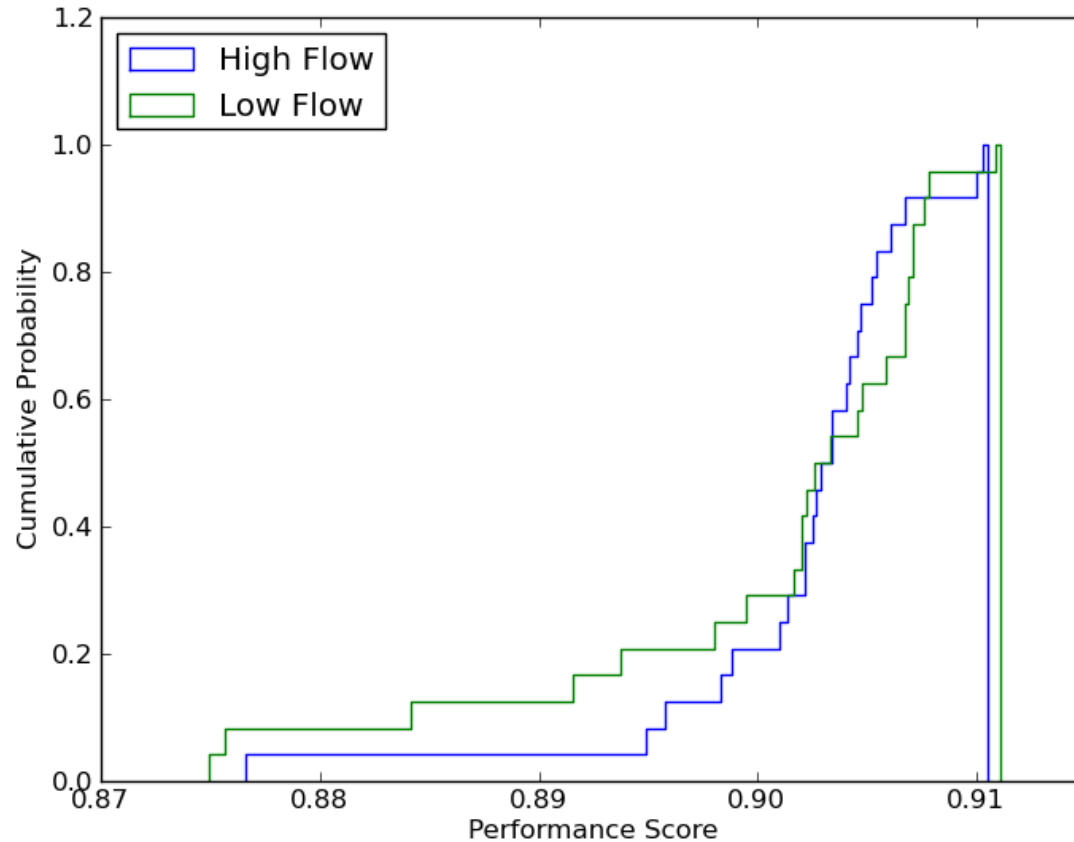
# ... with very different parameter sets.

» Structures able to 'fit' the model -> *overparameterization?, equifinality?*



Optimal parameter set is dependent from the objective used.  
Enough degrees of freedom to 'fit' – overparameterization?

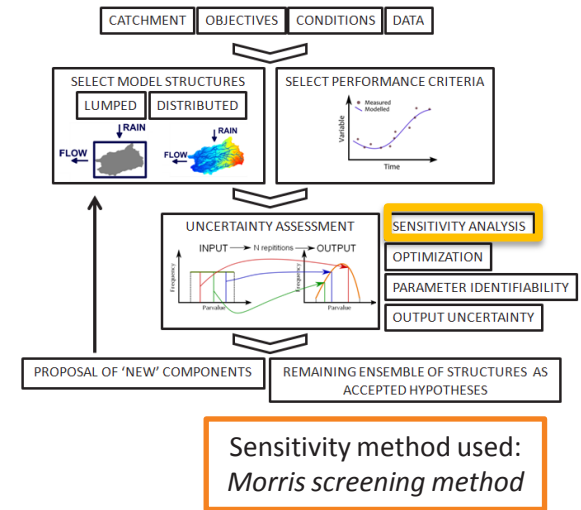
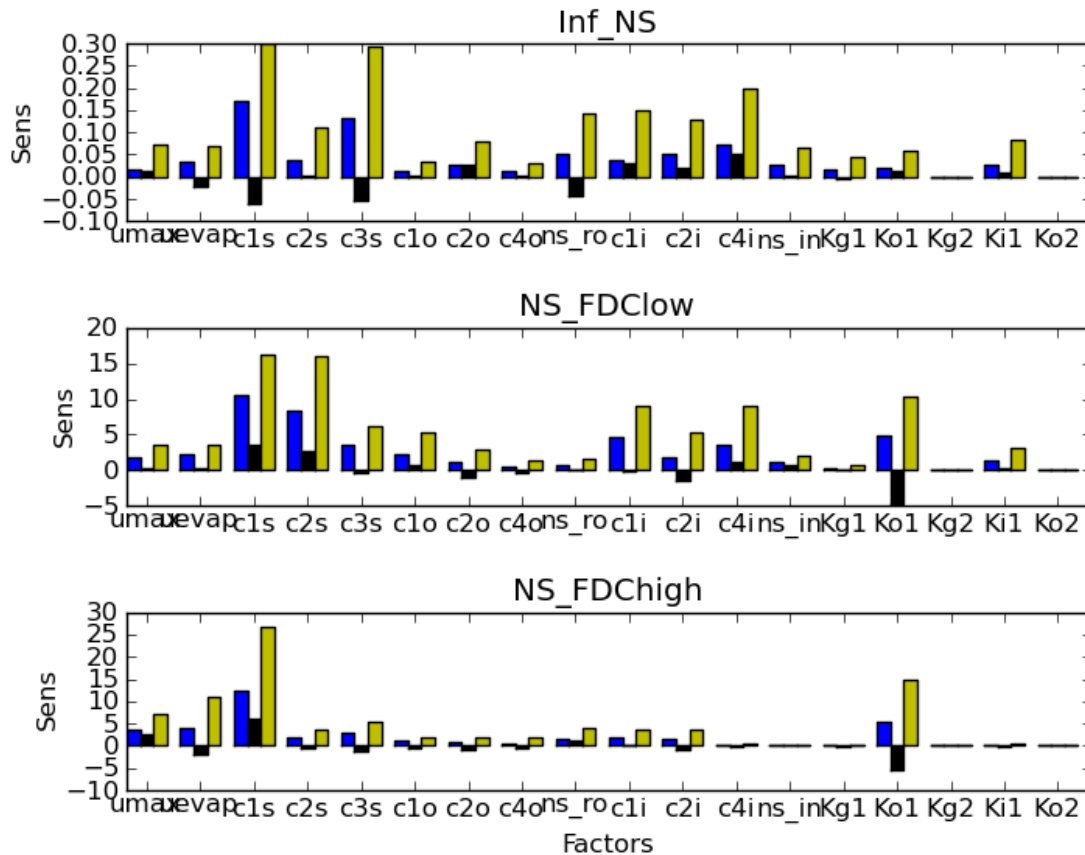
# Objective criteria not conditioning the structure



- » CDF of 24 structures
- » Spread of performance score is measure of discriminating power
- » TWO POSSIBILITIES:
  1. Objective measures not well selected
  2. High similarity of model structures

# Sensitivity Analysis (qualitative)

Based on distribution of Elementary Effects (EE)



» INFLUENCE ON OUTPUT:

» **Blue:** mean of the absolute values of EE

» **Black:** mean of the EE

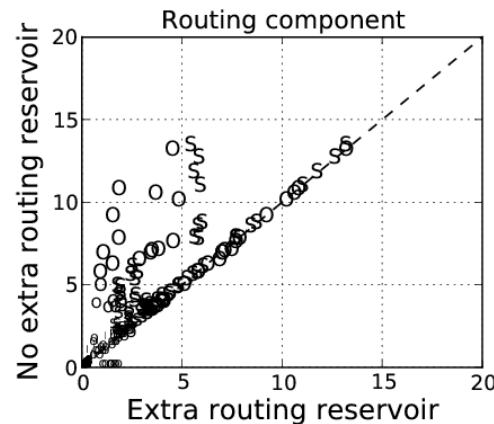
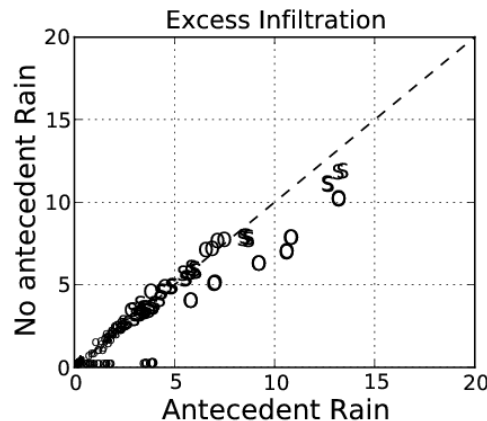
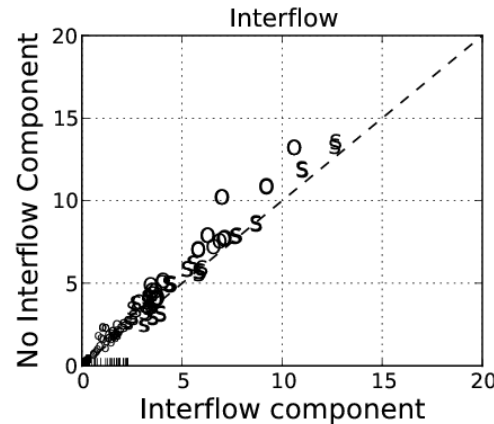
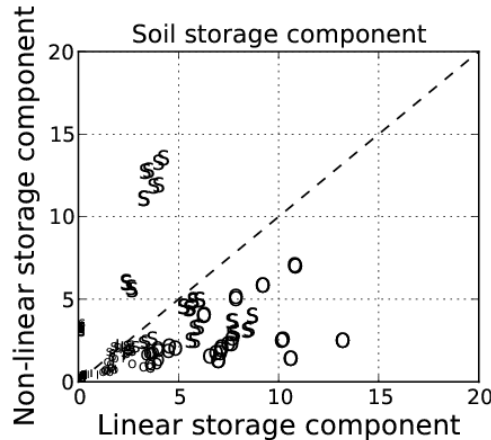
» PARAMETER INTERDEPENDENCE:

» **Yellow:** standard deviation of EE

» High interactions is inherent to the VHM structure used!

**Different parameters sensitive to different objective criteria**

# Sensitivity Analysis (qualitative)



Comparison for **HIGH FLOW** criterium

- » Parameters present in the **overland component** and the **unsaturated soil** always most sensitive
- » When going from **linear to non-linear soil** component the variation in the output is mainly described by the unsaturated zone parameters instead of overland flow parameters → *both sensitive*
- » **Interflow** and **excess infiltration** → *limited effect*
- » **More complex routing** decreases sensitivity + no benefit in performance → *exclude*

**Model structures not diverse enough!**

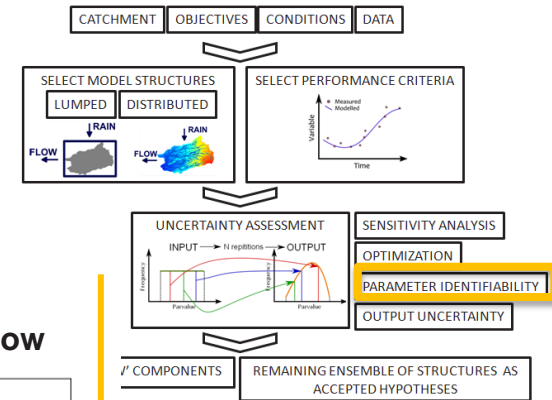
# Identifiability Analysis

## OBJECTIVE CRITERIA

NS

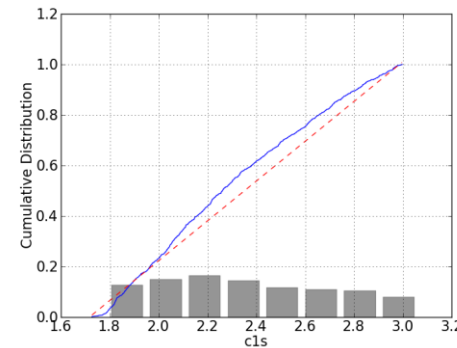
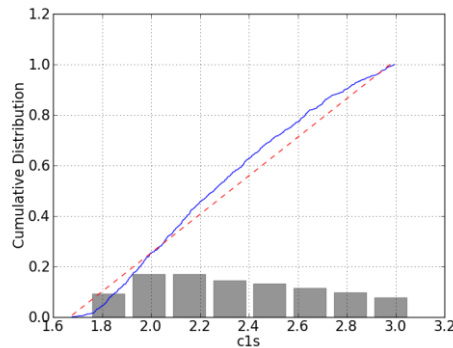
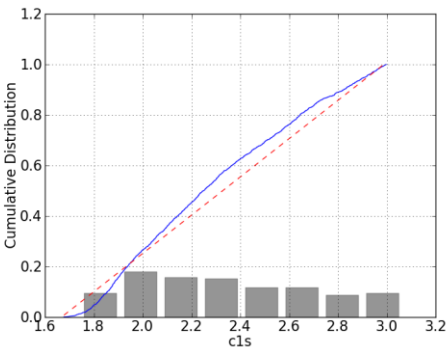
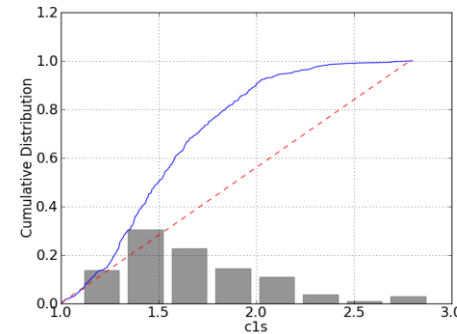
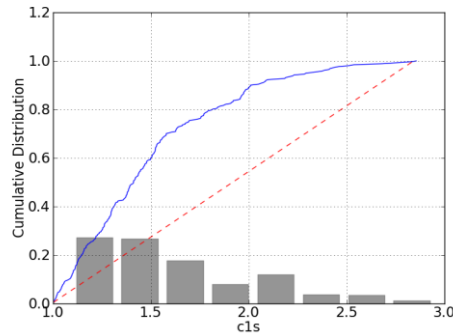
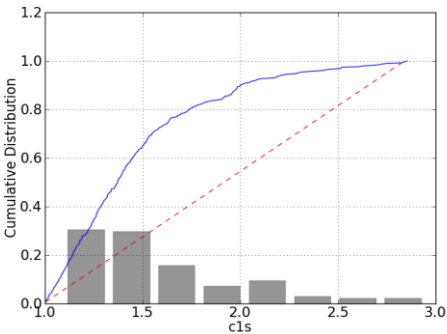
NS &  $FDC^{err}_{high}$

NS &  $FDC^{err}_{low}$



Identifiability method used:  
*GLUE-based identifiability index*  
(Wagener, 2007)

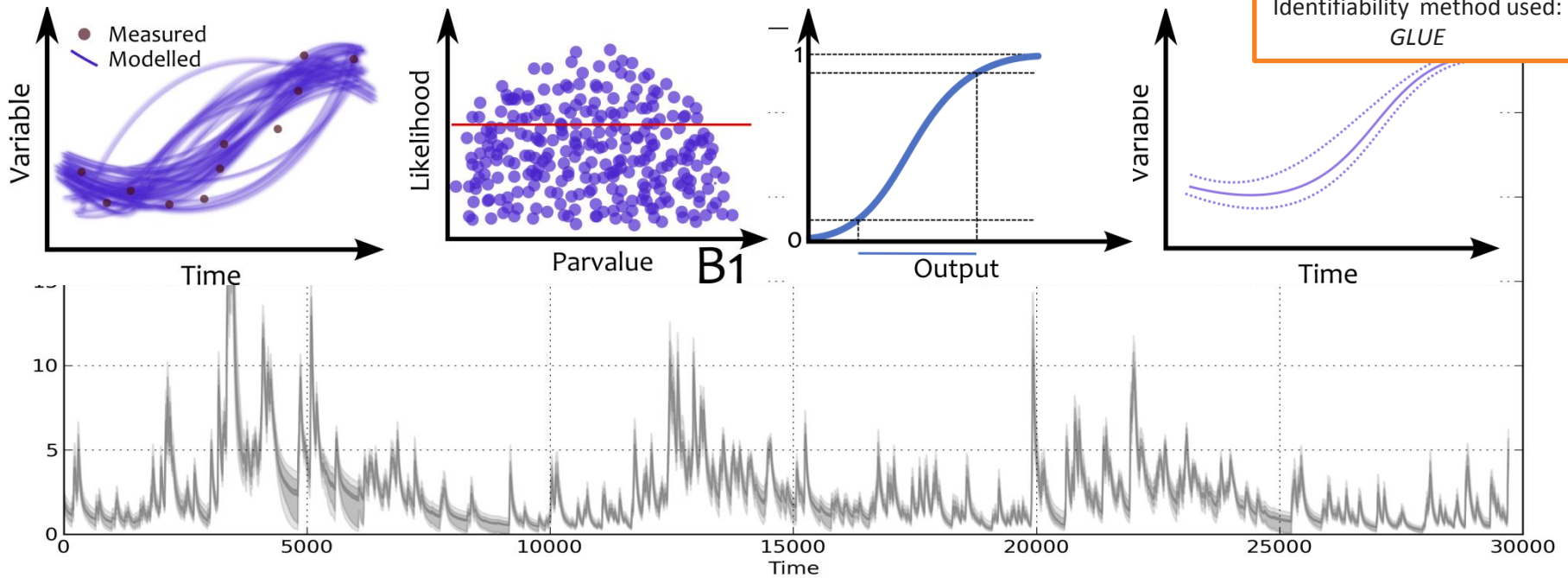
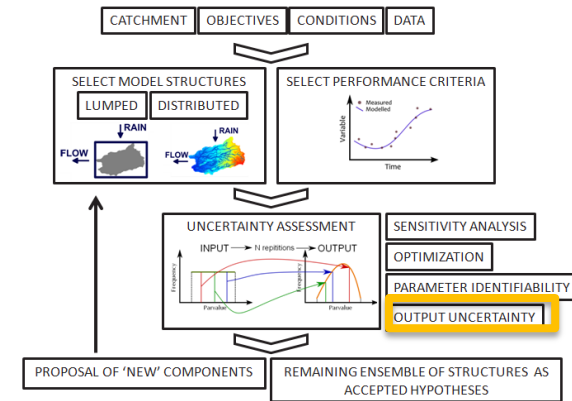
STRUCTURES



Parameter identifiability can be applied as model selection criterion

# Uncertainty Analysis (not in detail)

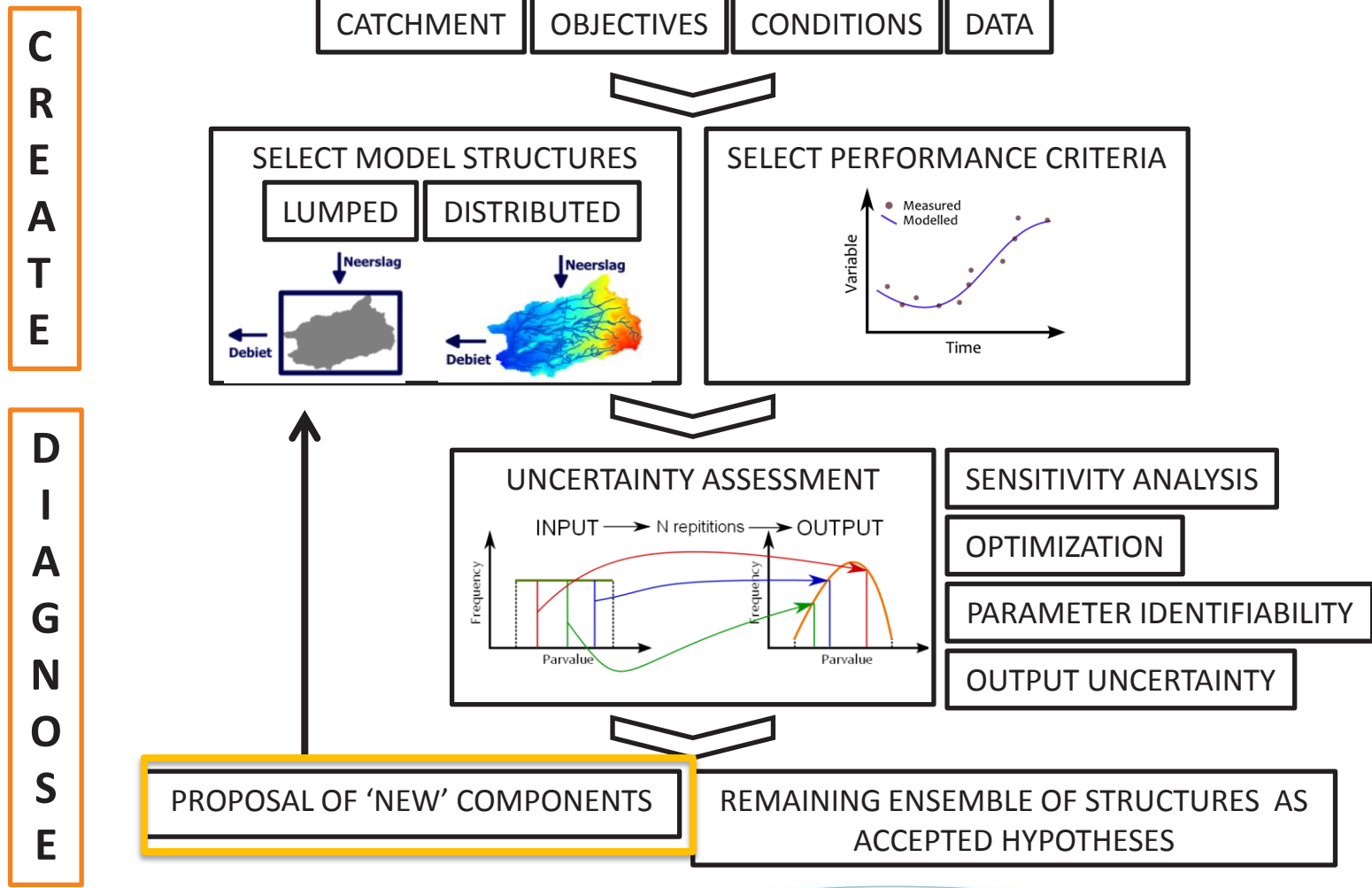
- » Ensemble of accepted **parameter sets** based on limits of acceptance
- » Ensemble of accepted **structures** used based on limits of acceptance
- » Every accepted run weighted by objective criteria



**Model structures not diverse enough!**



# Methodology





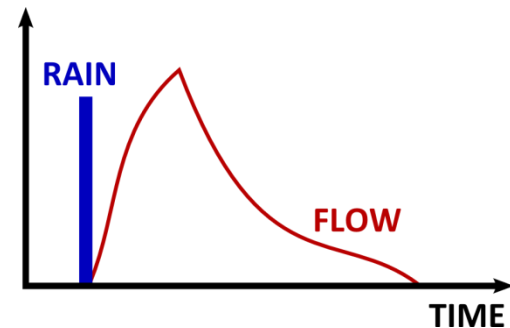
# What have we learned? -> next steps

## More diversity needed in model structures

- » NEW STRUCTURES: PDM and NAM model with completely different configurations compared to VHM-alternatives

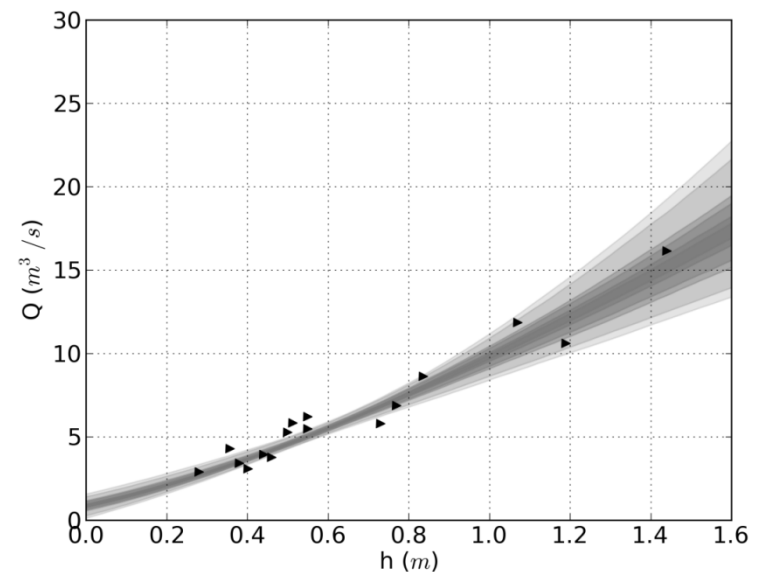
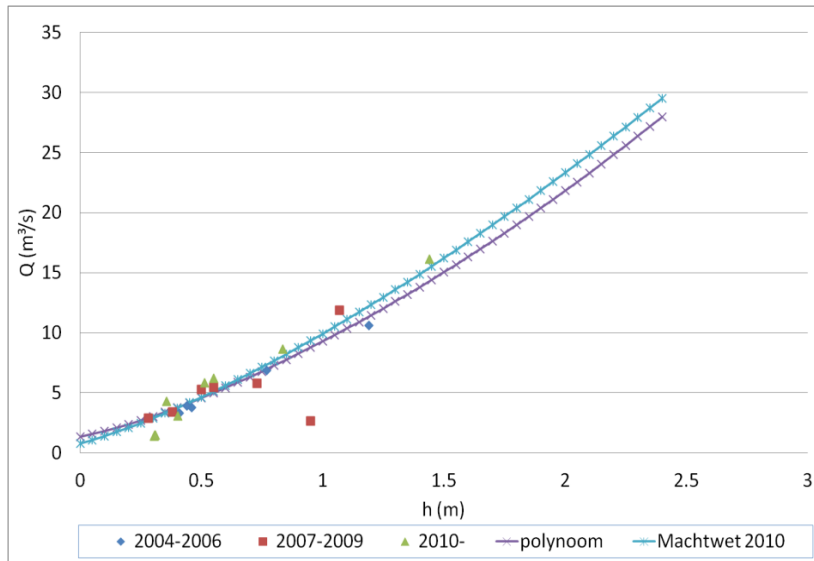
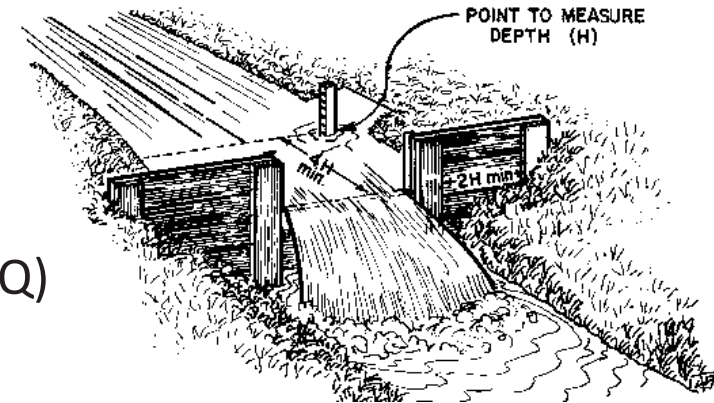
## More diversity needed in objective measures

- » CHECK SPECIFIC PROPERTIES OF THE HYDROGRAPH: check how the structure behaves in rising limb versus falling limb of flow after rain event
- » INCORPORATE FLOW DATA UNCERTAINTY

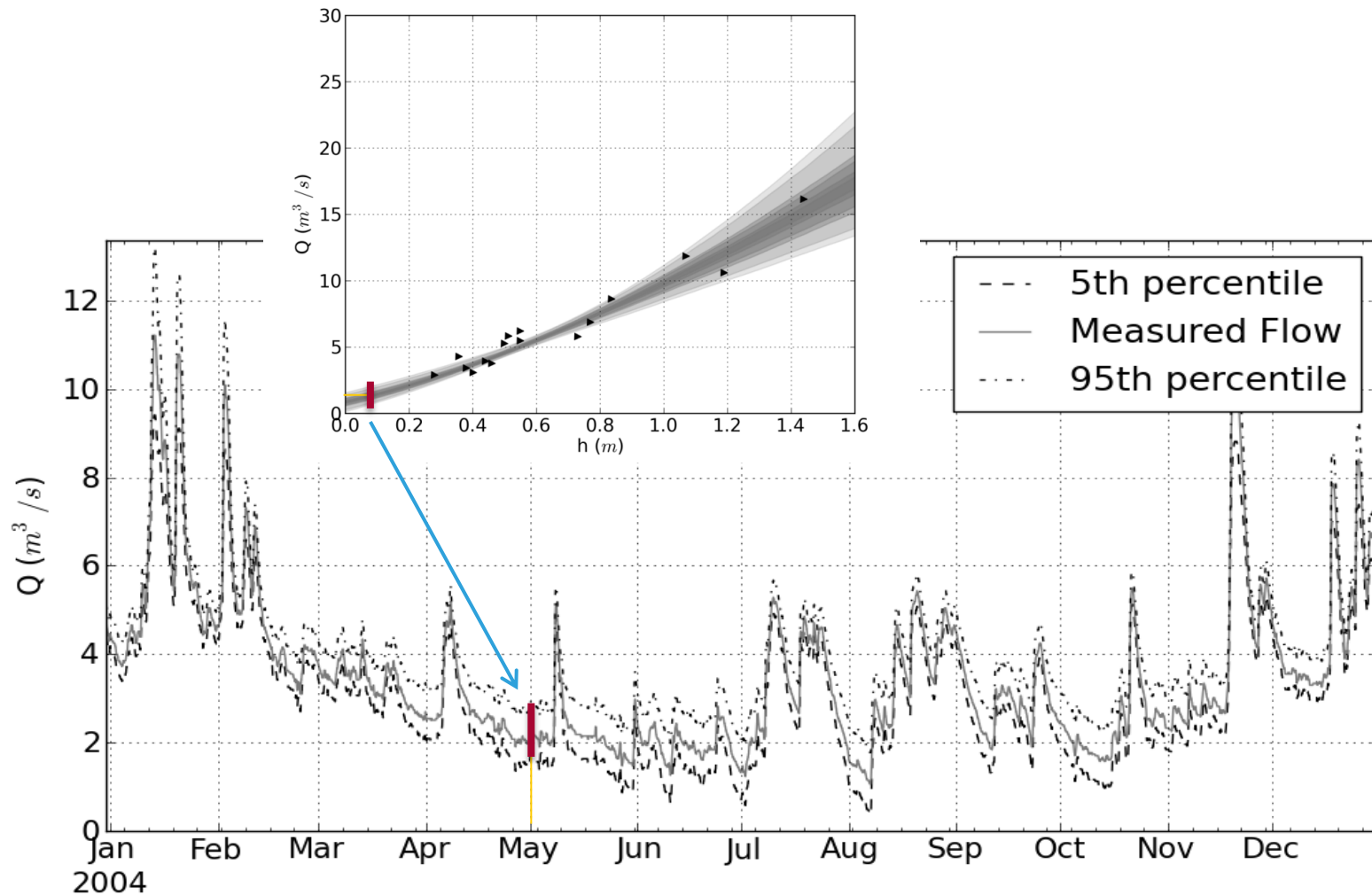


# Flow data uncertainty

- » Flow measured by weir
- » Need control measurements to find relation between measured height (h) and discharge (Q)
- » Power-law:  $Q = a(h + b)^c$
- » Uncertainty envelope derived based on subset of measurements

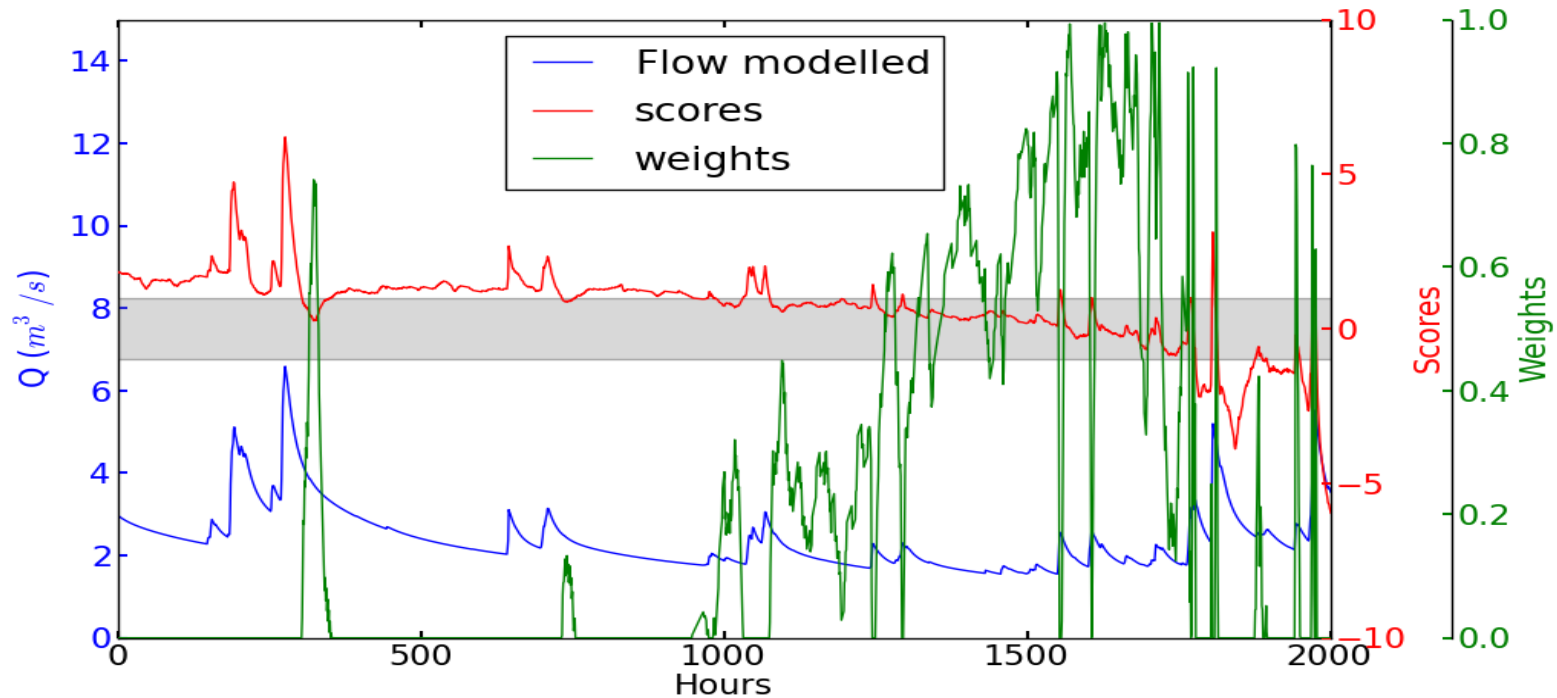
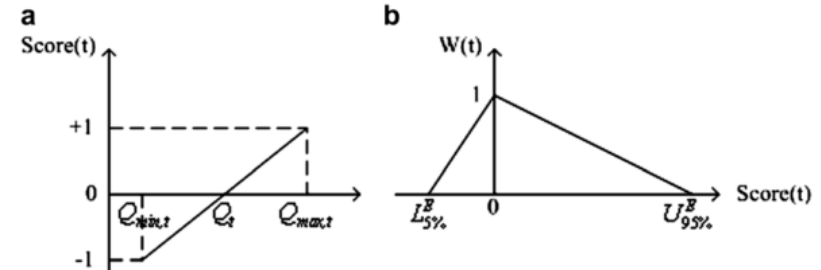


# Q-h uncertainty to Q timeserie uncertainty



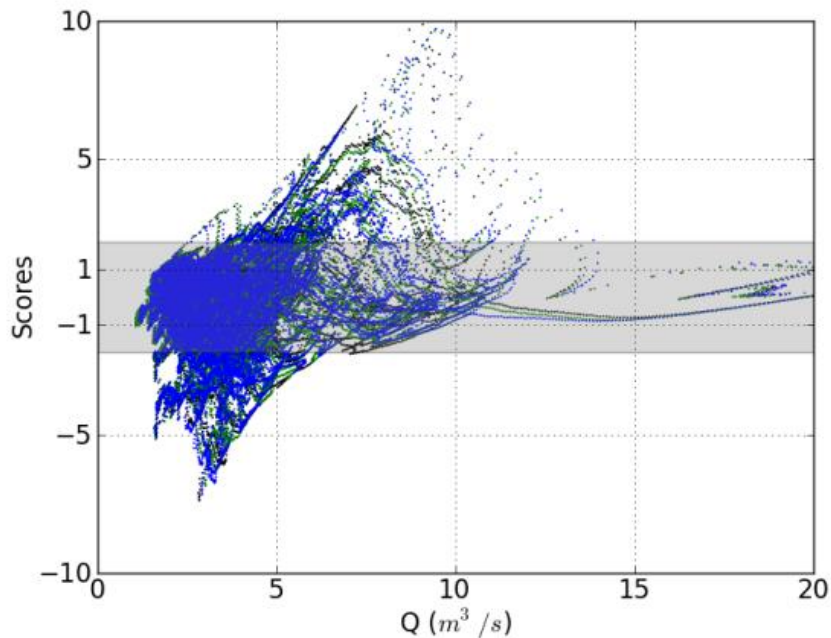
# Q timeserie uncertainty as objective criterion

- » Data uncertainty bounds to evaluate model outputs and weight simulations

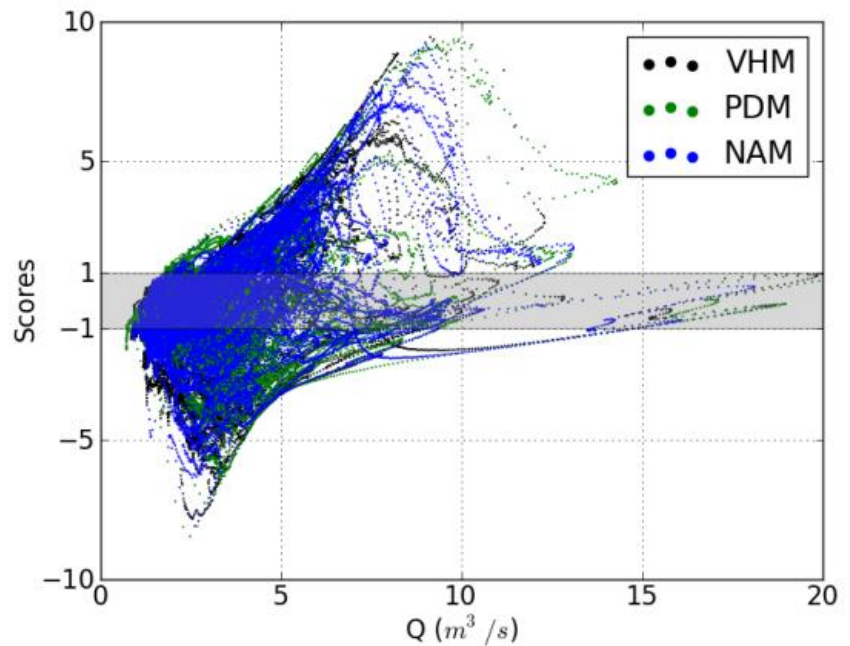


# NAM, PDM and VHM similar failures

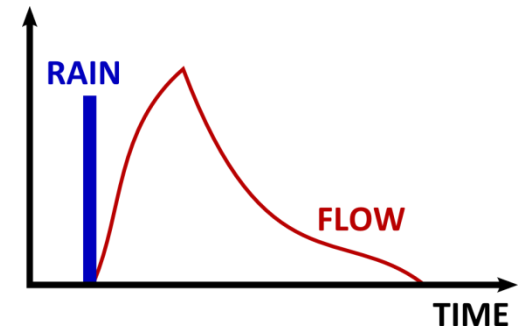
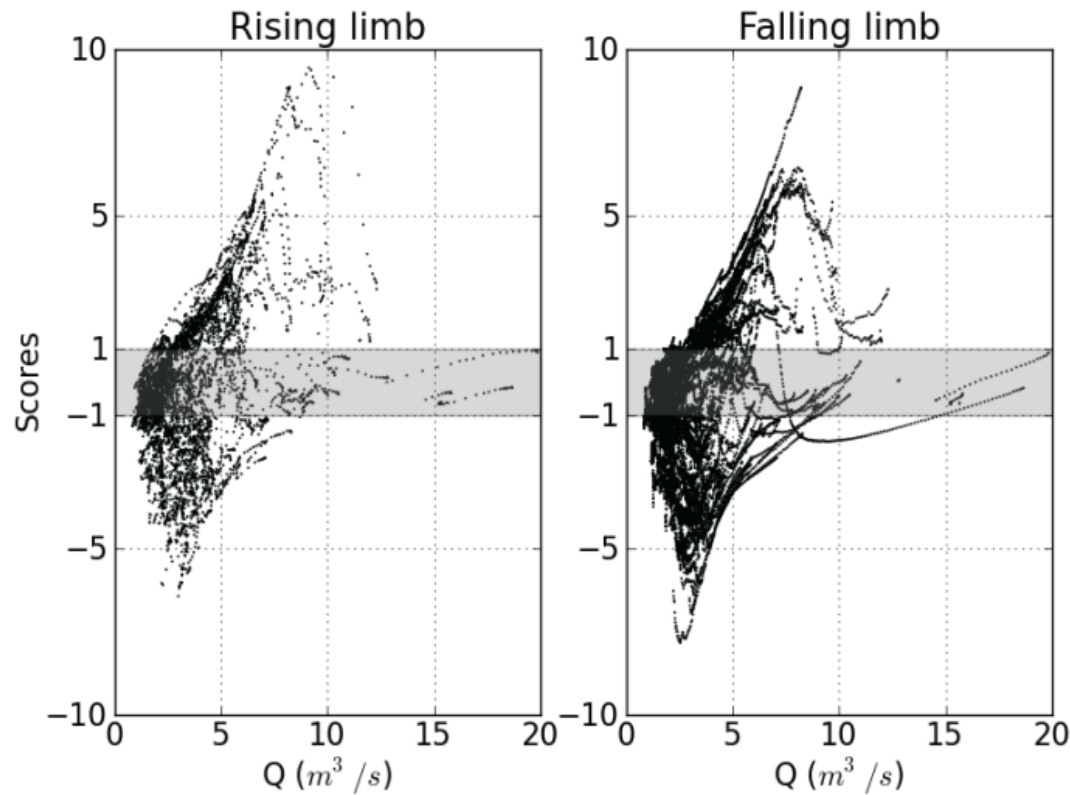
VHM alternatives



cfr. PDM, NAM en VHM



# Failure in rising and falling limb very similar



To be continued...

# Conclusions

- » Shift from *on the shelf* fixed model structure towards case-specific ensemble of behavioural model structures
- » Shift from *classic* (observed-simulated)<sup>2</sup> evaluation towards more rigorous analysis of model outcome
  - » Improvement needed in *discriminating criteria*
- » Model identification *a combined effort* of parameterization and structure identification in uncertainty assessment
- » NOT *Push the button for success* – > tools to interpret model structures!
  - » Learning by modelling!
- » Difficult to discriminate structures as *optimal model structure* based on single streamflow output signal
- » Implementation in **Python** (open source) => open and extendable!