

# Semantic Data Mining Using RDF Hypergraphs

1 of 15



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# The definition of hypergraph

(1)

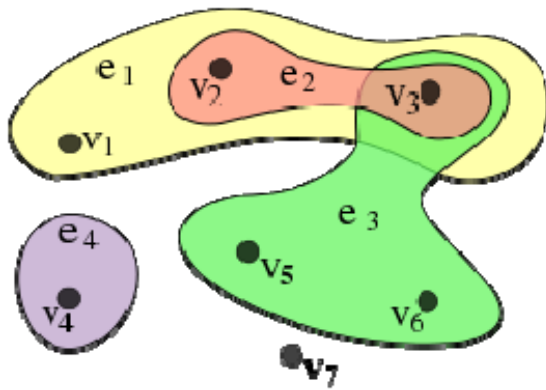
- In a graph, an edge, only two vertices
- In a hypergraph, an edge, more than two vertices.

(2)

- A hypergraph  $HG=(V,E)$
- $V$  : vertex set.
- $V$  : vertex set.
- $e \in E$  is a subset of  $V$ .



# An example of hypergraph



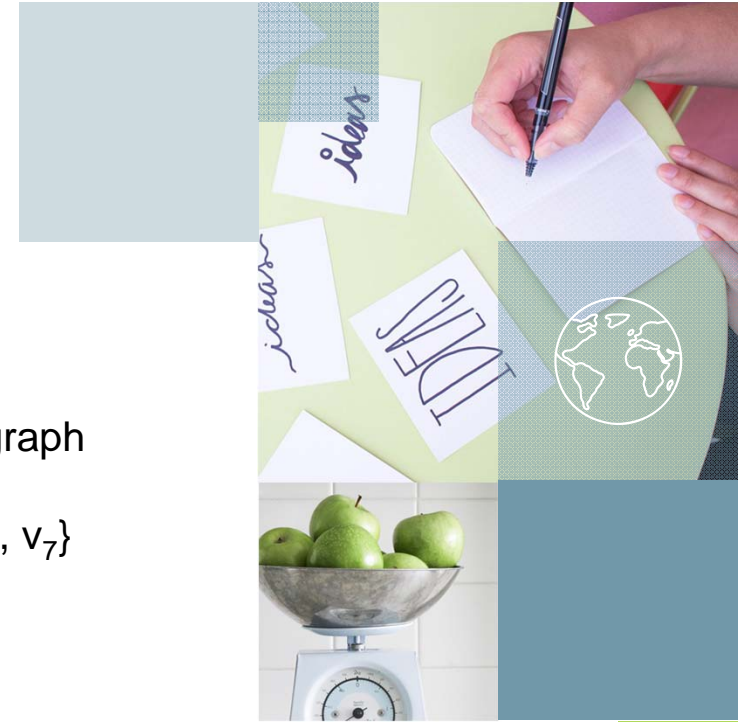
An example of a hypergraph

$$V = \{v_1, v_2, v_3, v_4, v_5, v_6, v_7\}$$

$$E = \{e_1, e_2, e_3, e_4\}$$

$$= \{\{v_1, v_2, v_3\}, \{v_2, v_3\},$$

$$\{v_3, v_5, v_6\}, \{v_4\}\}.$$

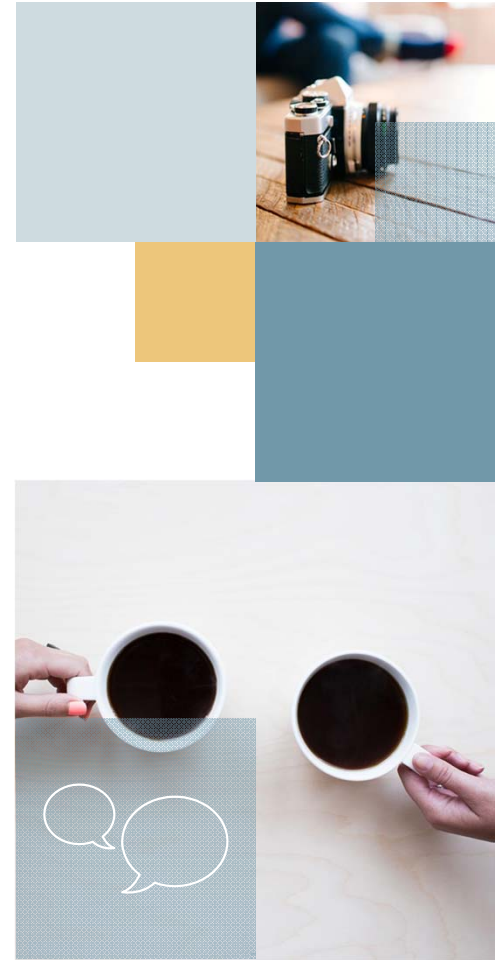


# The application of hypergraph in data mining

Discovering  
semantic  
associations  
between items

Clustering

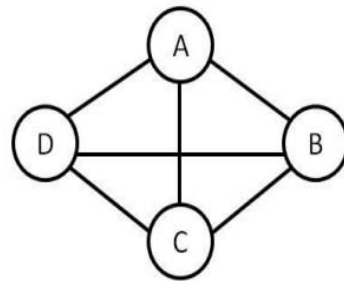
Spatial data  
mining



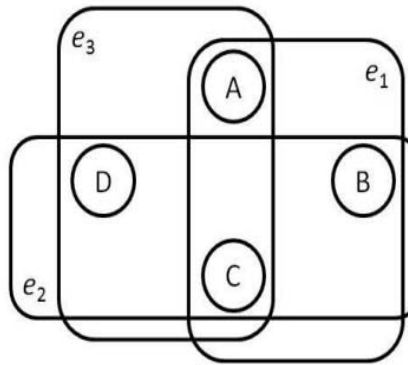
# Why we use hypergraph

	A	B	C	D
$e_1$ :	1	1	1	0
$e_2$ :	0	1	1	1
$e_3$ :	1	0	1	1

(a)



(b)

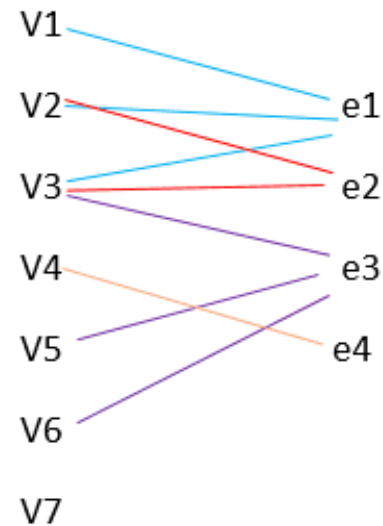
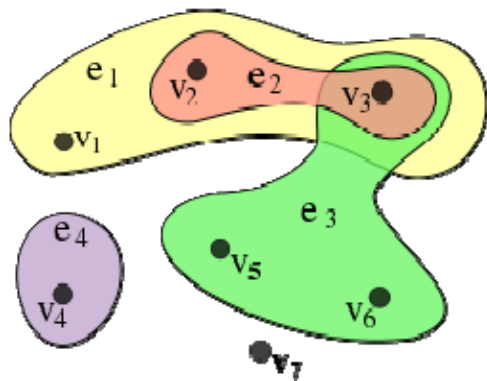


(c)

Figure 1. (a) an example transaction table; (b) the Gaifman graph representation of the table; (c) The hypergraph representation of the table

# How to transform hypergraph to bipartite graph(BG)

- Let  $V$  and  $E$  be the two parts of BG
- $(v_i, e_j)$  are connected with an edge if and only if vertex  $v_i$  is contained in edge  $e_j$  in  $H$

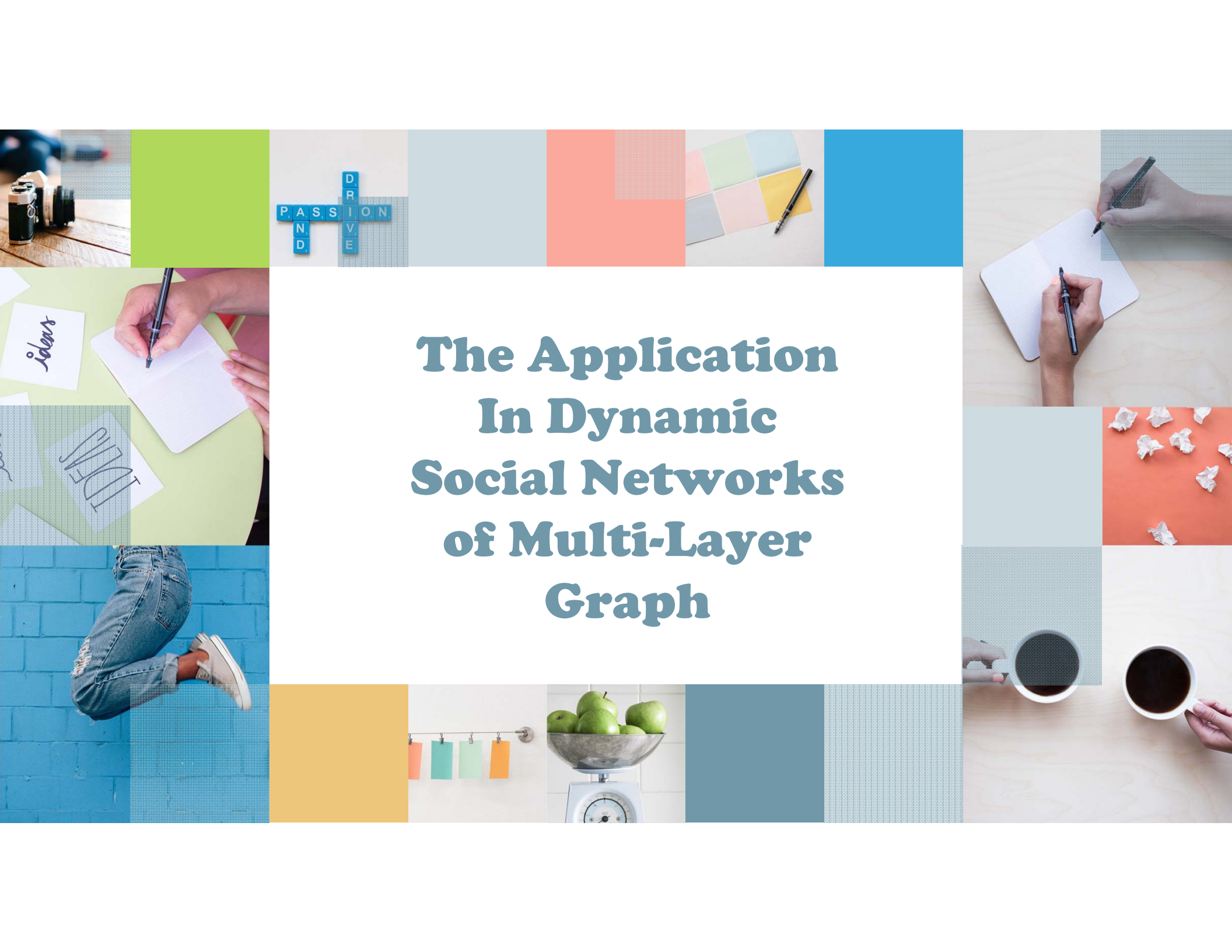


Hypergraph

BG







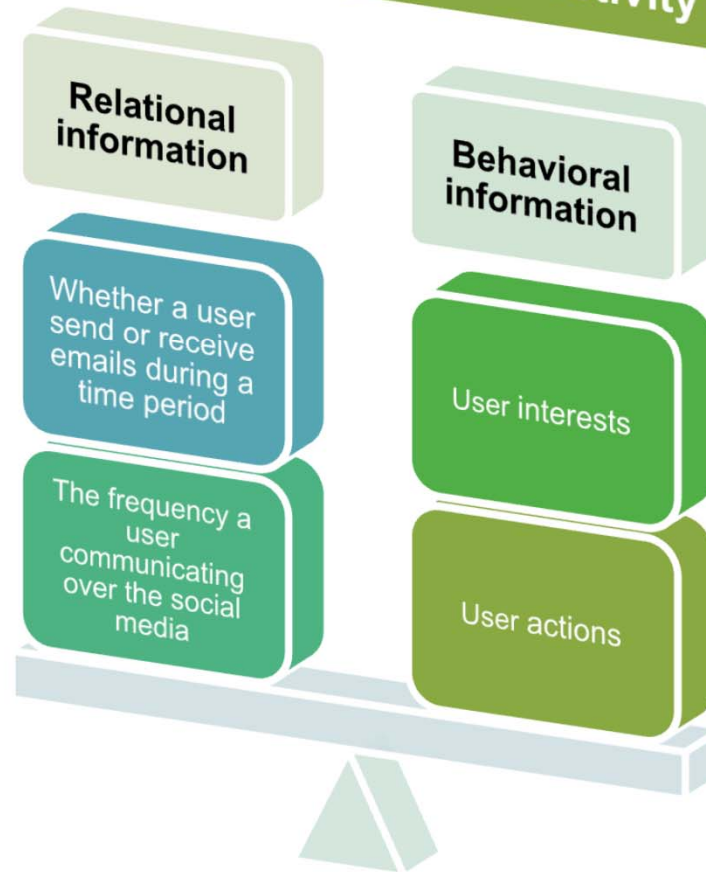
# **The Application In Dynamic Social Networks of Multi-Layer Graph**

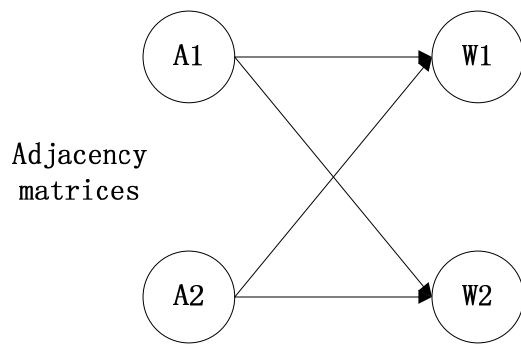
We are married





## Two type of sources in the connectivity information

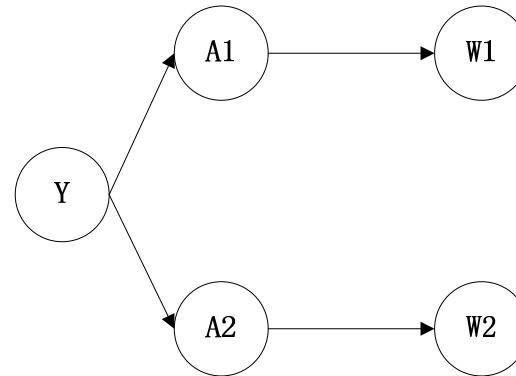




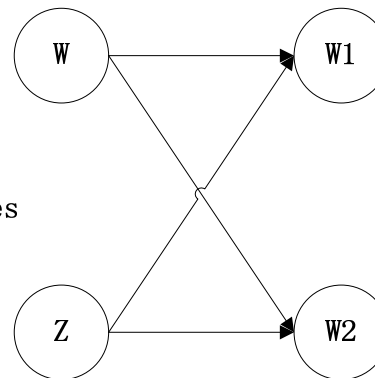
Observed  
matrices



Latent  
Variables



Observed  
matrices

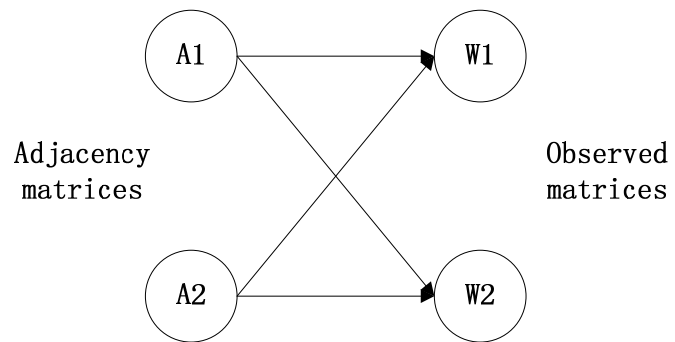


Latent  
Variables

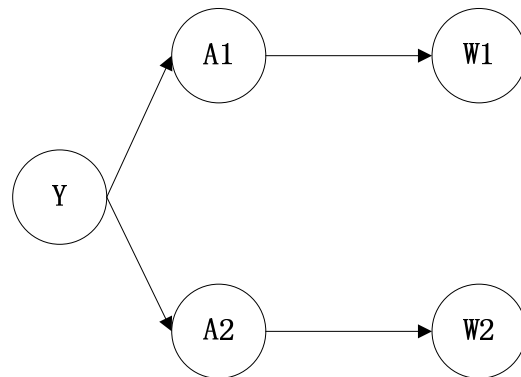
Observed  
matrices

**The evolution of  
solutions of the  
multi-layer graph**

# Hierarchical Latent-variable Model

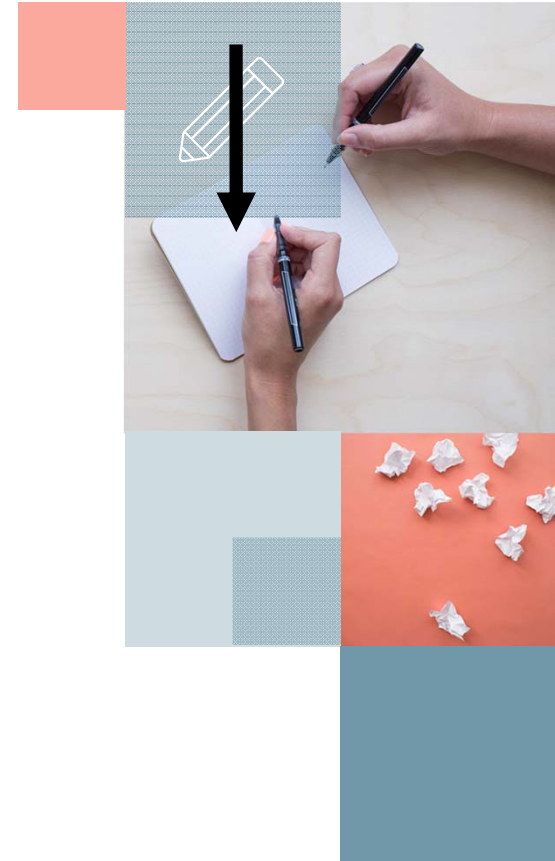


Latent Variables

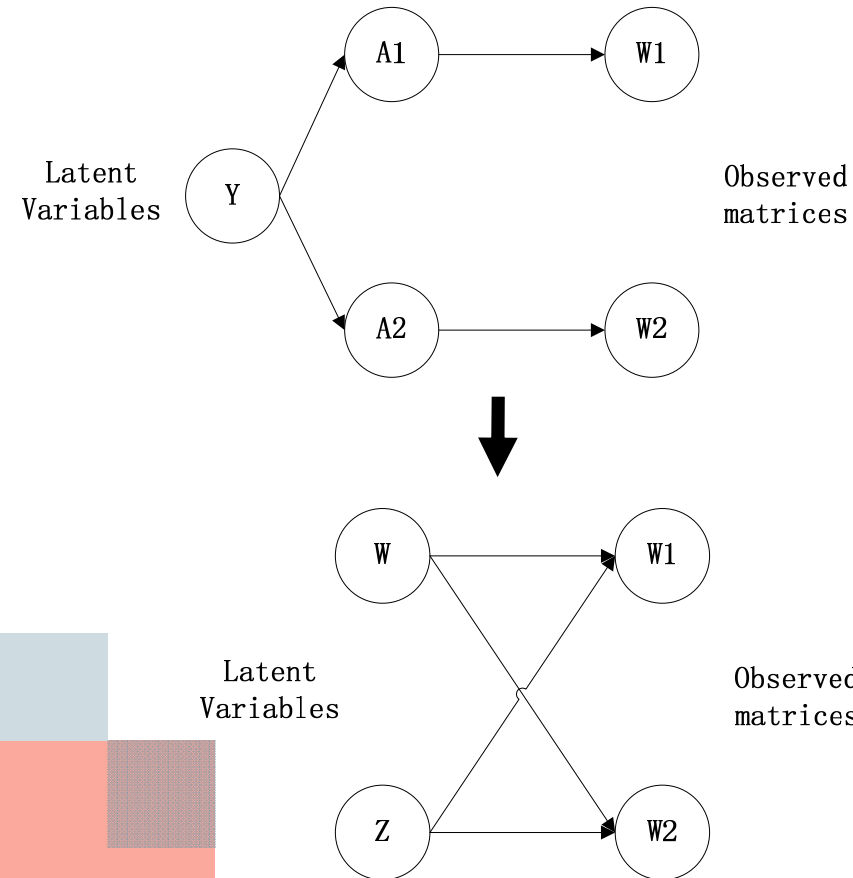


Observed matrices

$$P(Y|W_1, W_2) = \sum_{A_1, A_2} P(Y|A_1, A_2)P(A_1, A_2|W_1, W_2).$$



# Posterior Mixture Model



$$P(Y|W_1, W_2) = \sum_{A_1, A_2} P(Y|A_1, A_2)P(A_1, A_2|W_1, W_2).$$

$$P(W|W_1, W_2) \quad (12)$$

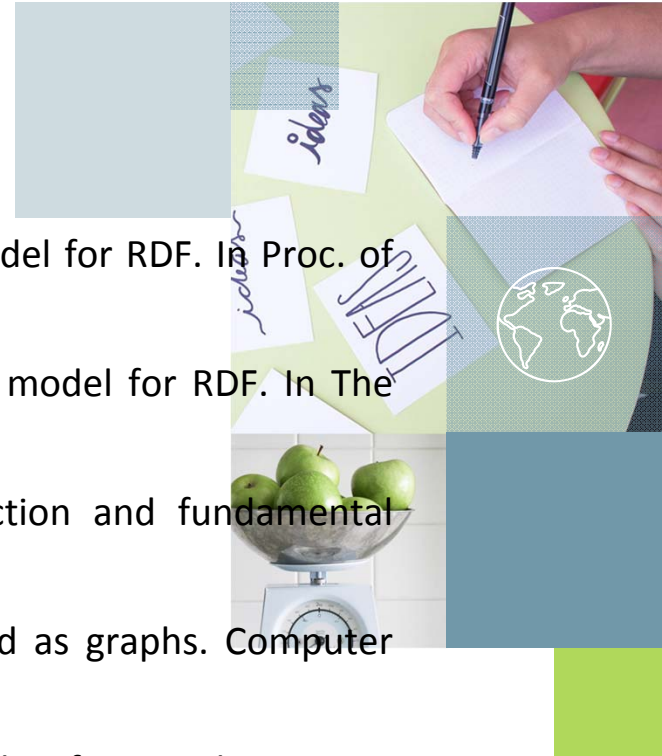
$$= \xi \frac{P(W)P_1(W_1|W)}{P_1(W_1)} + (1 - \xi) \frac{P(W)P_2(W_2|W)}{P_2(W_2)} \quad (13)$$

$$= P(W) [\gamma_1 P_1(W_1|W) + \gamma_2 P_2(W_2|W)], \quad (14)$$

$$\arg \max_W [\gamma_1 P_1(W_1|W) + \gamma_2 P_2(W_2|W)]. \quad (15)$$

## References

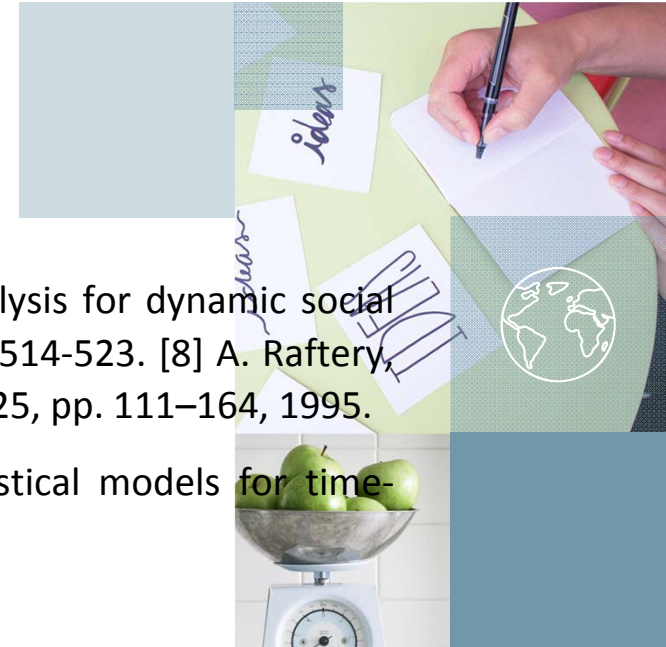
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# Thank You

