

HOMEWORK 1: RESULTS  
ADINATH M  
18990

PROBLEM 1

Bisection Method

The approximate solution obtained in 1 iteration is 3.0  
The approximate solution obtained in 2 iteration is 2.5  
The approximate solution obtained in 3 iteration is 2.75  
The approximate solution obtained in 4 iteration is 2.875  
The approximate solution obtained in 5 iteration is 2.9375  
The approximate solution obtained in 6 iteration is 2.96875  
The approximate solution obtained in 7 iteration is 2.953125  
The approximate solution obtained in 8 iteration is 2.9453125  
The approximate solution obtained in 9 iteration is 2.94140625  
The approximate solution obtained in 10 iteration is 2.943359375  
The approximate solution obtained in 11 iteration is 2.9423828125  
The root of the equation with relative tolerance of 0.001 is 2.9423828125  
The number of iterations taken to achieve this value is 11

PROBLEM 2

Regula Falsi Method

The approximate solution obtained in 1 iteration is 0.31466533780077094  
The approximate solution obtained in 2 iteration is 0.4467281445913339  
The approximate solution obtained in 3 iteration is 0.4940153365958987  
The approximate solution obtained in 4 iteration is 0.509946140365247  
The approximate solution obtained in 5 iteration is 0.5152010099022495  
The approximate solution obtained in 6 iteration is 0.5169222100105165  
The approximate solution obtained in 7 iteration is 0.5174846767845119  
The approximate solution obtained in 8 iteration is 0.5176683449777301  
The approximate solution obtained in 9 iteration is 0.5177283052714121  
The approximate solution obtained in 10 iteration is 0.5177478783221142  
The approximate solution obtained in 11 iteration is 0.5177542674540466  
The approximate solution obtained in 12 iteration is 0.5177563530081399  
The approximate solution obtained in 13 iteration is 0.5177570337772521  
The approximate solution obtained in 14 iteration is 0.5177572559945329  
The root of the equation with relative tolerance of  $1e-06$  is  
0.5177572559945329  
The number of iterations taken to achieve this value is 14

Secant Method

The approximate solution obtained in 1 iteration is 1  
The approximate solution obtained in 2 iteration is 0.31466533780077094  
The approximate solution obtained in 3 iteration is 0.4467281445913339  
The approximate solution obtained in 4 iteration is 0.5317058606445457  
The approximate solution obtained in 5 iteration is 0.5169044675673677  
The approximate solution obtained in 6 iteration is 0.517747465271495  
The approximate solution obtained in 7 iteration is 0.5177573707542169  
The root of the equation with relative tolerance of  $1e-06$  is  
0.5177573636823997  
The number of iterations taken to achieve this value is 7

PROBLEM 3

Part (a)

#### Newton's Method

The approximate solution obtained in 1 iteration is -0.999999999989999  
The approximate solution obtained in 2 iteration is -0.5306440165880459  
The approximate solution obtained in 3 iteration is -0.588626532134796  
The approximate solution obtained in 4 iteration is -0.5884017768080275  
The approximate solution obtained in 5 iteration is -0.5884017765009962  
The root of the equation with relative tolerance of  $1e-06$  is -  
0.5884017765009962  
The number of iterations taken to achieve this value is 5

#### Secant Method

The approximate solution obtained in 1 iteration is 1  
The approximate solution obtained in 2 iteration is -5.031038733198447  
The approximate solution obtained in 3 iteration is -0.16051867195163716  
The approximate solution obtained in 4 iteration is -0.8298306248059459  
The approximate solution obtained in 5 iteration is -0.5756375739986599  
The approximate solution obtained in 6 iteration is -0.5887103386407785  
The approximate solution obtained in 7 iteration is -0.5884017264778837  
The root of the equation with relative tolerance of  $1e-06$  is -  
0.5884017765009013  
The number of iterations taken to achieve this value is 7

#### Modified Newton's Method

The approximate solution obtained in 1 iteration is -0.24999998448630642  
The approximate solution obtained in 2 iteration is -0.5063051670020028  
The approximate solution obtained in 3 iteration is -0.5871673224050348  
The approximate solution obtained in 4 iteration is -0.5884017630415093  
The approximate solution obtained in 5 iteration is -0.5884017765009962  
The root of the equation with relative tolerance of  $1e-06$  is -  
0.5884017765009962  
The number of iterations taken to achieve this value is 5

#### Part (b)

#### Newton's Method

The approximate solution obtained in 1 iteration is -0.5000000000758279  
The approximate solution obtained in 2 iteration is -0.5445980432020442  
The approximate solution obtained in 3 iteration is -0.5665500114701518  
The approximate solution obtained in 4 iteration is -0.5774827973027736  
The approximate solution obtained in 5 iteration is -0.5829433320632383  
The approximate solution obtained in 6 iteration is -0.5856727315869128  
The approximate solution obtained in 7 iteration is -0.5870372879326275  
The approximate solution obtained in 8 iteration is -0.5877195393880712  
The approximate solution obtained in 9 iteration is -0.5880606595751808  
The approximate solution obtained in 10 iteration is -0.5882312184257134  
The approximate solution obtained in 11 iteration is -0.5883164975579707  
The approximate solution obtained in 12 iteration is -0.5883591370530614  
The approximate solution obtained in 13 iteration is -0.5883804567831225  
The approximate solution obtained in 14 iteration is -0.5883911166438156  
The approximate solution obtained in 15 iteration is -0.5883964465730814  
The approximate solution obtained in 16 iteration is -0.5883991115374445  
The approximate solution obtained in 17 iteration is -0.5884004440195585  
The approximate solution obtained in 18 iteration is -0.5884011102605985  
The approximate solution obtained in 19 iteration is -0.5884014433811142  
The root of the equation with relative tolerance of  $1e-06$  is -  
0.5884014433811142  
The number of iterations taken to achieve this value is 19

#### Secant Method

The approximate solution obtained in 1 iteration is 1

The approximate solution obtained in 2 iteration is -2.2881190998554244  
The approximate solution obtained in 3 iteration is 2.238743416190869  
The approximate solution obtained in 4 iteration is 89.8575728481702  
The approximate solution obtained in 5 iteration is 2.1845228537658143  
The approximate solution obtained in 6 iteration is 2.1329067048947365  
The approximate solution obtained in 7 iteration is 1.0975016534713629  
The approximate solution obtained in 8 iteration is 0.5721631090386814  
The approximate solution obtained in 9 iteration is -4.825995710535452  
The approximate solution obtained in 10 iteration is 0.9142842240213863  
The approximate solution obtained in 11 iteration is 1.2785374631398705  
The approximate solution obtained in 12 iteration is -0.37778460457646224  
The approximate solution obtained in 13 iteration is -0.5676909467640785  
The approximate solution obtained in 14 iteration is -0.5696419554912123  
The approximate solution obtained in 15 iteration is -0.5785633972862619  
The approximate solution obtained in 16 iteration is -0.5819497582858273  
The approximate solution obtained in 17 iteration is -0.5845056072556054  
The approximate solution obtained in 18 iteration is -0.585972680865122  
The approximate solution obtained in 19 iteration is -0.586905570798394  
The approximate solution obtained in 20 iteration is -0.5874758932462881  
The approximate solution obtained in 21 iteration is -0.5878298322527629  
The approximate solution obtained in 22 iteration is -0.5880482304802043  
The approximate solution obtained in 23 iteration is -0.5881832890455403  
The approximate solution obtained in 24 iteration is -0.5882667402907288  
The approximate solution obtained in 25 iteration is -0.5883183204586327  
The approximate solution obtained in 26 iteration is -0.5883501976459747  
The approximate solution obtained in 27 iteration is -0.5883698990719535  
The approximate solution obtained in 28 iteration is -0.5883820751579749  
The approximate solution obtained in 29 iteration is -0.5883896004052459  
The approximate solution obtained in 30 iteration is -0.5883942512597771  
The approximate solution obtained in 31 iteration is -0.5883971256464686  
The approximate solution obtained in 32 iteration is -0.5883989021148505  
The approximate solution obtained in 33 iteration is -0.5884000000326943  
The approximate solution obtained in 34 iteration is -0.5884006785832132  
The root of the equation with relative tolerance of 1e-06 is -  
0.5884010979504936  
The number of iterations taken to achieve this value is 34

#### Modified Newton's Method

The approximate solution obtained in 1 iteration is -0.24999997231022195  
The approximate solution obtained in 2 iteration is -0.5063051437037074  
The approximate solution obtained in 3 iteration is -0.5871673218435971  
The approximate solution obtained in 4 iteration is -0.5884017630429802  
The approximate solution obtained in 5 iteration is -0.5884017765028889  
The root of the equation with relative tolerance of 1e-06 is -  
0.5884017765028889  
The number of iterations taken to achieve this value is 5