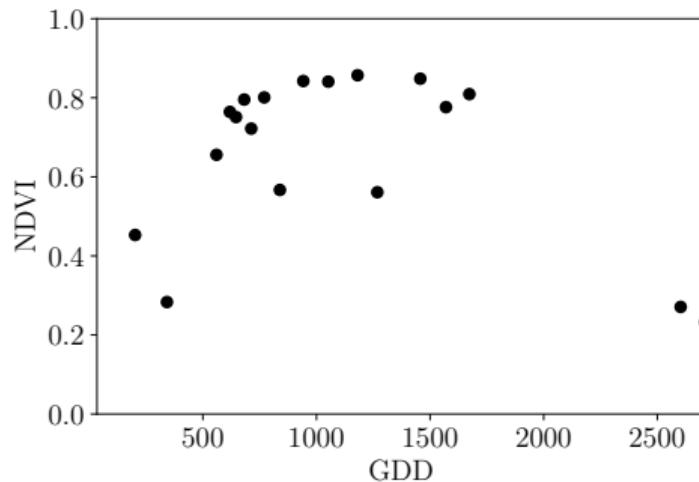
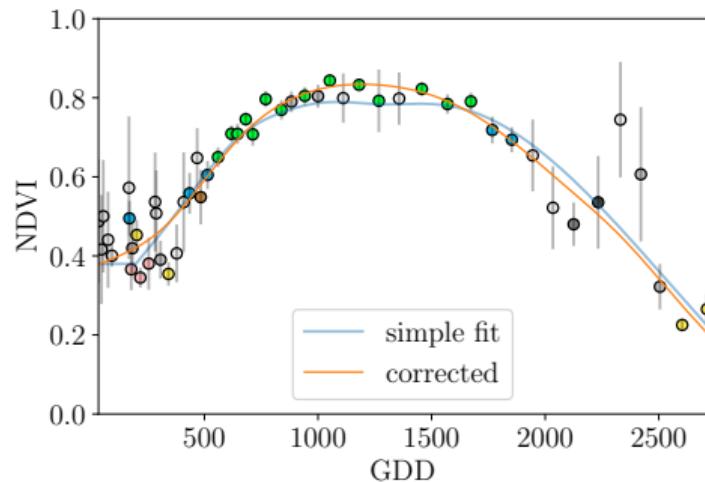


How to get ...

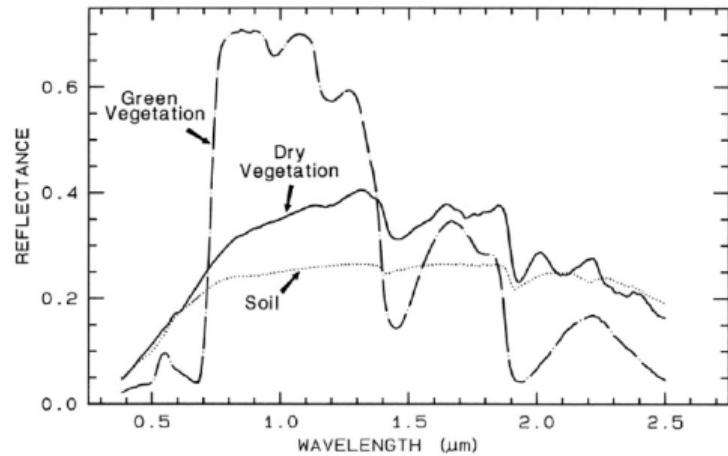
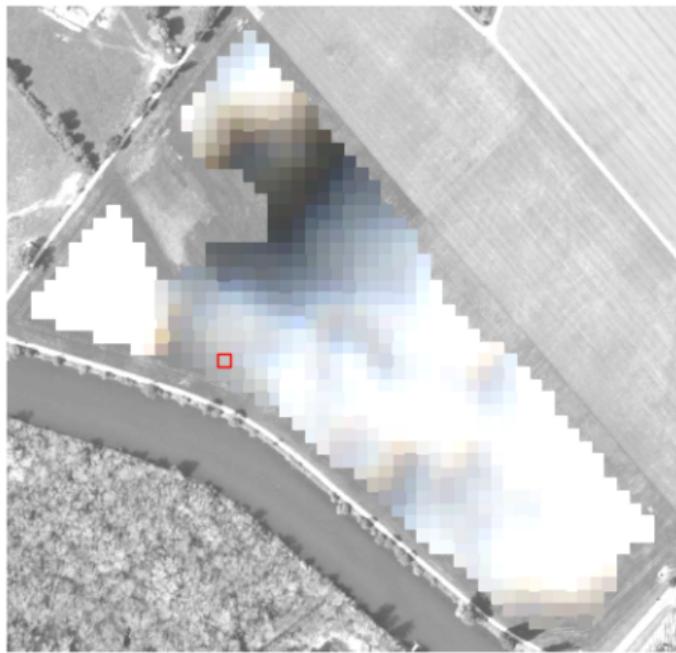
from ...



to ...



NDVI From S2 Images



$$\text{NDVI} = \frac{(\text{NIR} - \text{Red})}{(\text{NIR} + \text{Red})}$$

⁰ Spectral Reflectances https://www.researchgate.net/figure/Reflectance-spectra-of-photosynthetic-green-vegetation-non-photosynthetic-dry_fig4_236677371

Scene Classification Layer (SCL)

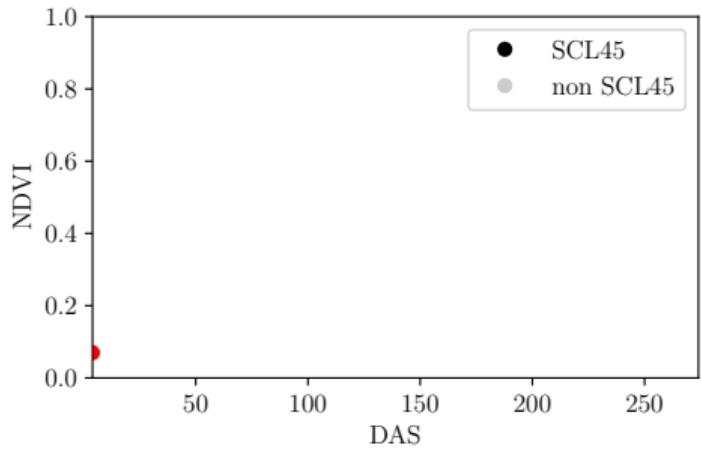


| Color | No. Class |
|-------------|---------------------------------|
| Black | 0: Missing Data |
| Red | 1: Saturated or defective pixel |
| Dark grey | 2: Dark features / Shadows |
| Brown | 3: Cloud shadows |
| Green | 4: Vegetation |
| Yellow | 5: Bare soils |
| Blue | 6: Water |
| Medium grey | 7: Cloud low probability |
| Light grey | 8: Cloud medium probability |
| White | 9: Cloud high probability |
| Cyan | 10: Thin cirrus cloud |
| Pink | 11: Snow or ice |

Sentinel 2 Image + NDVI Time Series



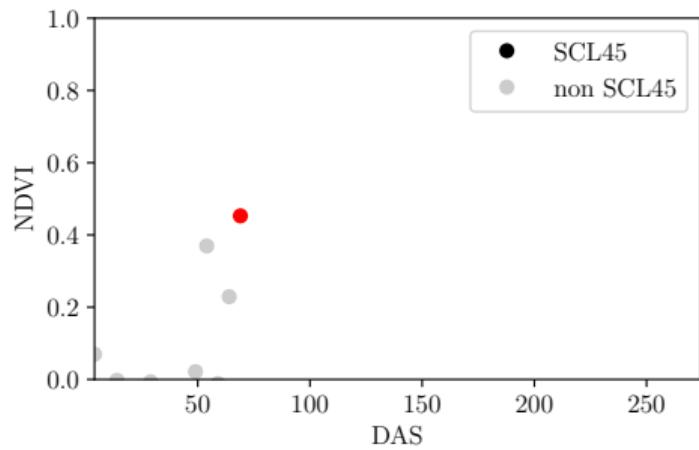
→ Cloud high probability



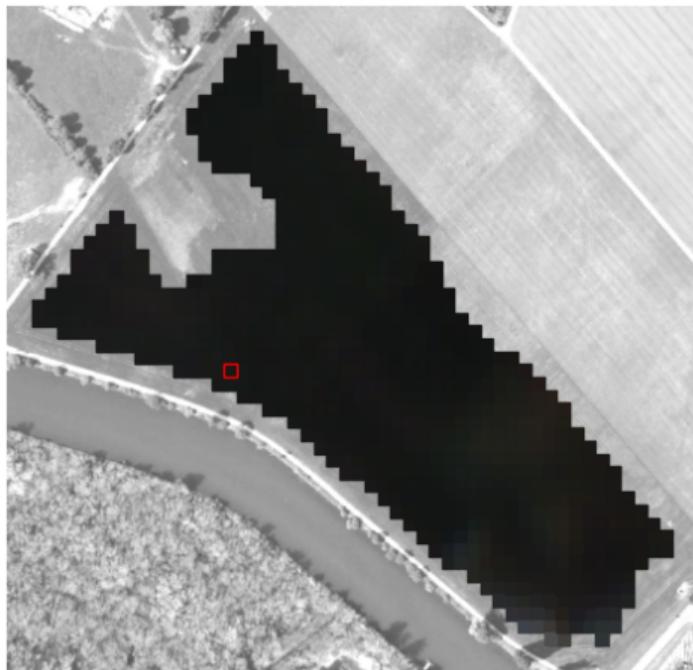
Sentinel 2 Image + NDVI Time Series



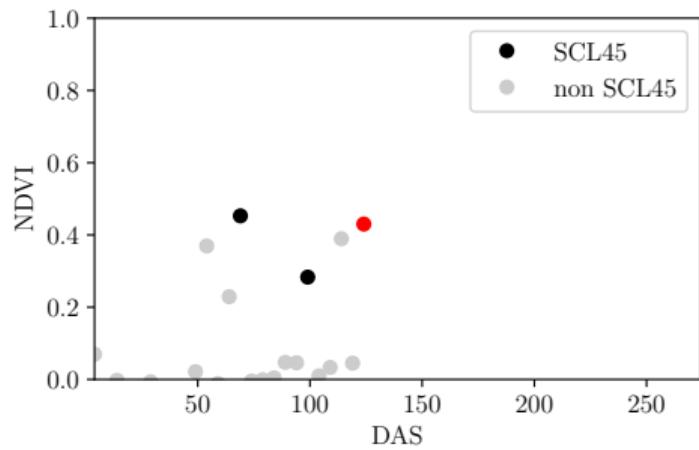
→ Bare soils



Sentinel 2 Image + NDVI Time Series



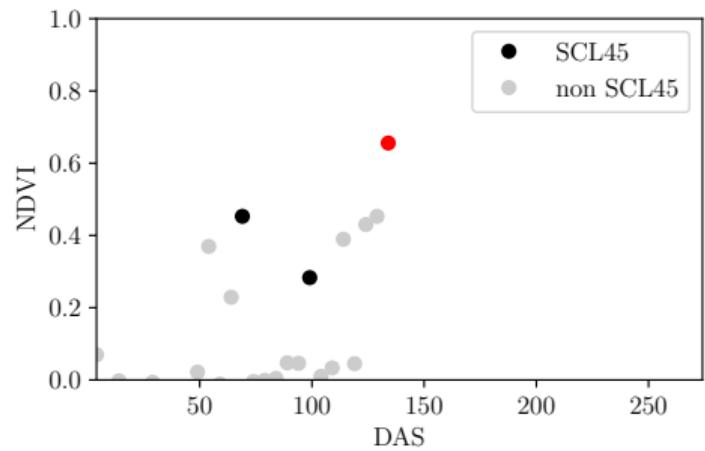
→ Cloud shadows



Sentinel 2 Image + NDVI Time Series



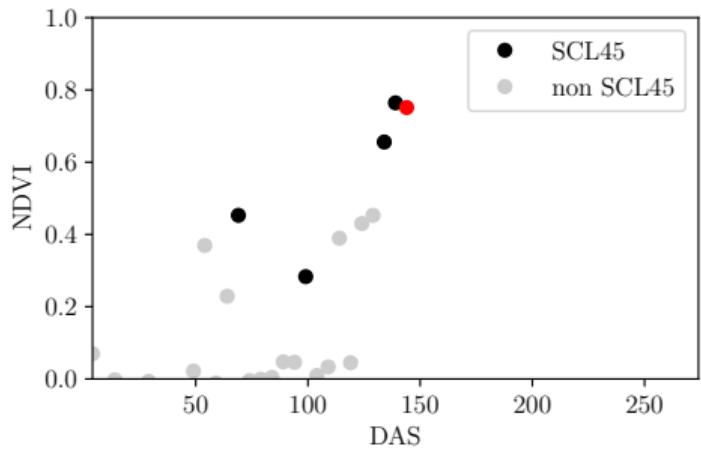
→ Vegetation



Sentinel 2 Image + NDVI Time Series



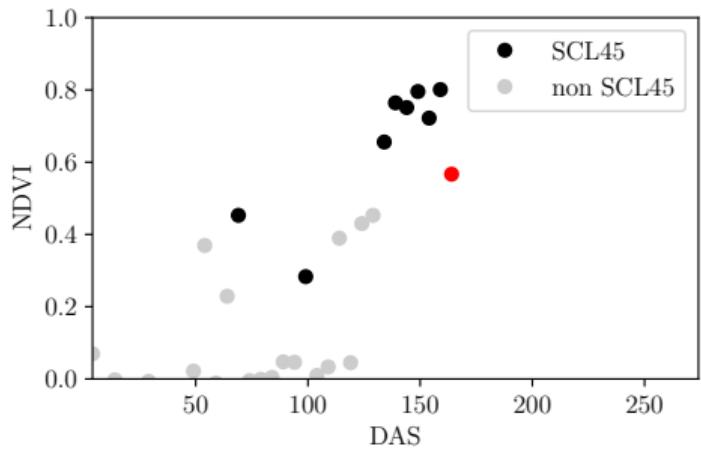
→ Vegetation



Sentinel 2 Image + NDVI Time Series



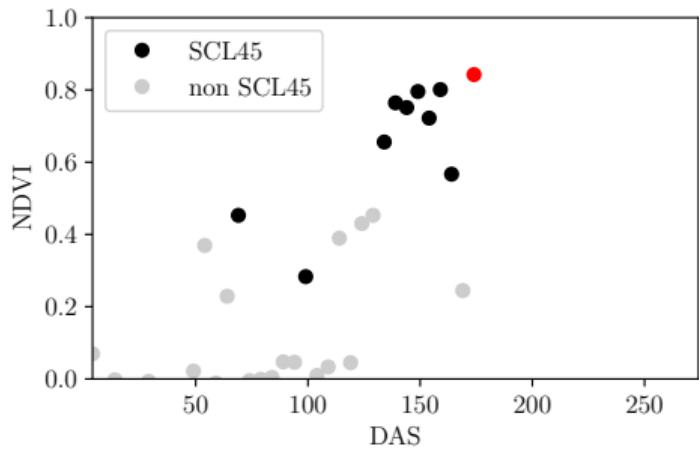
→ Vegetation



Sentinel 2 Image + NDVI Time Series



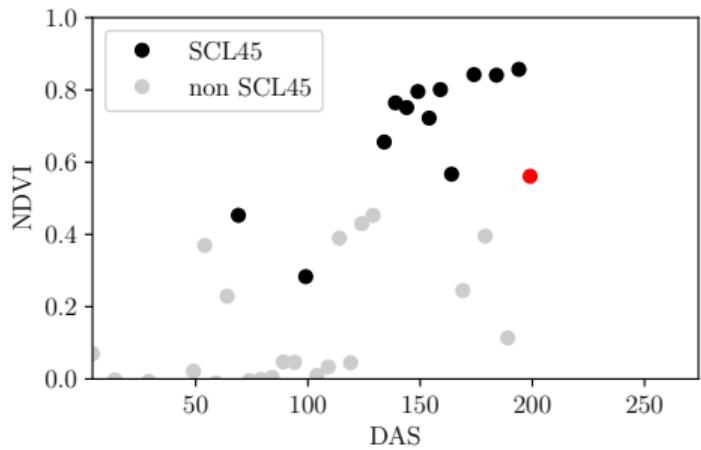
→ Vegetation



Sentinel 2 Image + NDVI Time Series



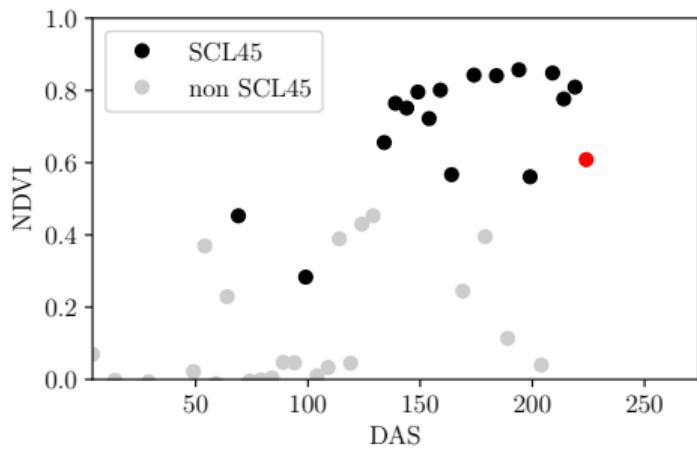
→ Vegetation



Sentinel 2 Image + NDVI Time Series



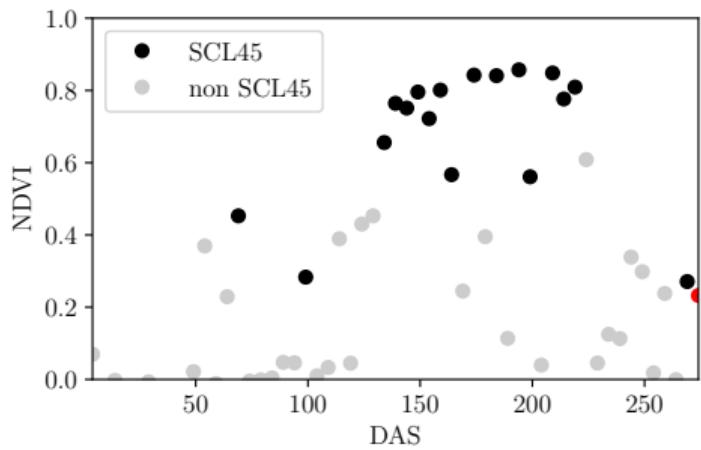
→ Thin cirrus cloud



Sentinel 2 Image + NDVI Time Series

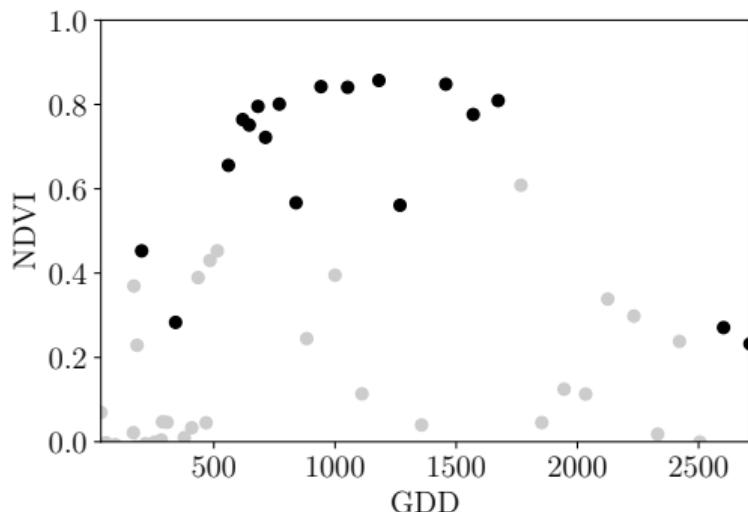
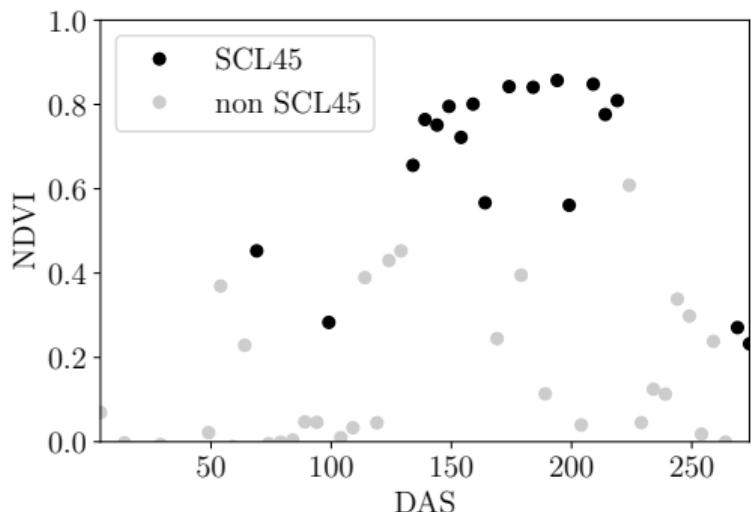


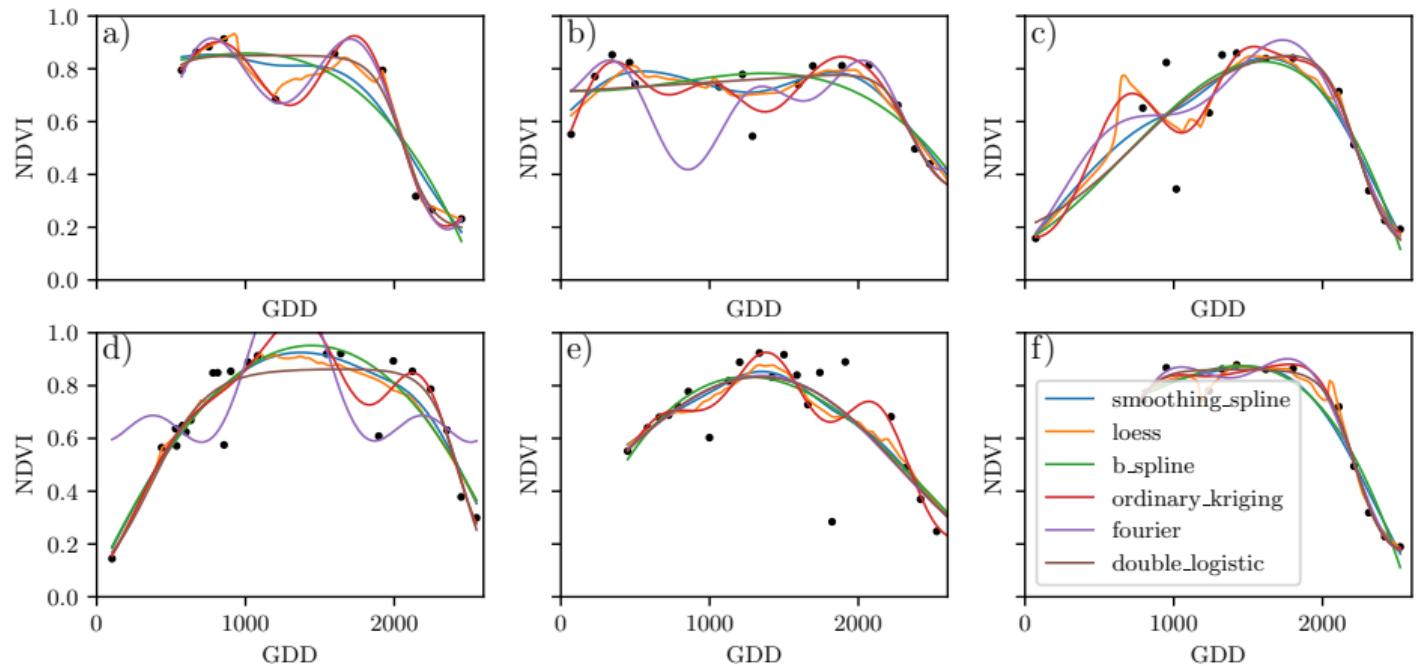
→ Bare soils



Timescale Transformation: DAS vs GDD

$$GDD_n := \sum_{i=0}^n \max(T_i - T_{base}, 0). \quad (1)$$

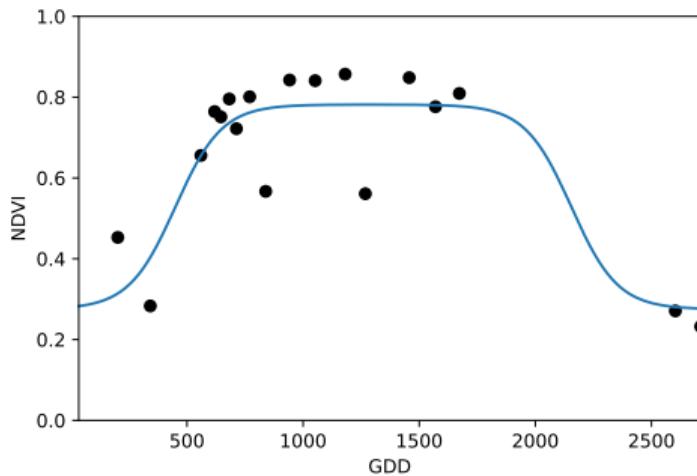




Double Logistic Approximation

Curve fully determined by parameters (no data)

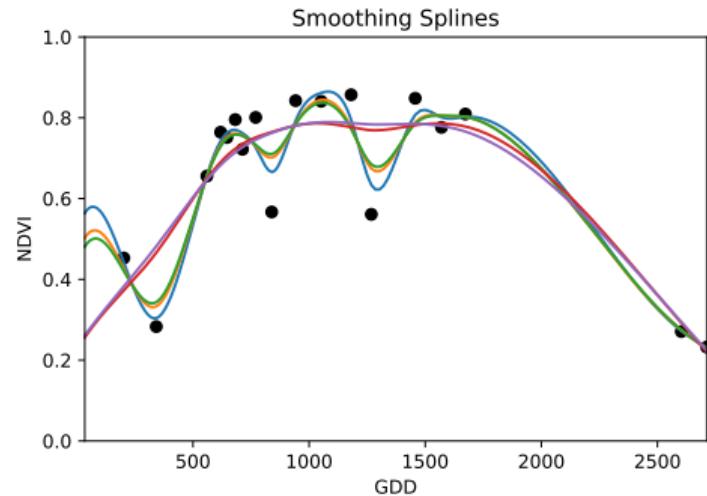
$$NDVI(t) = f(a, b, c, d, e)$$



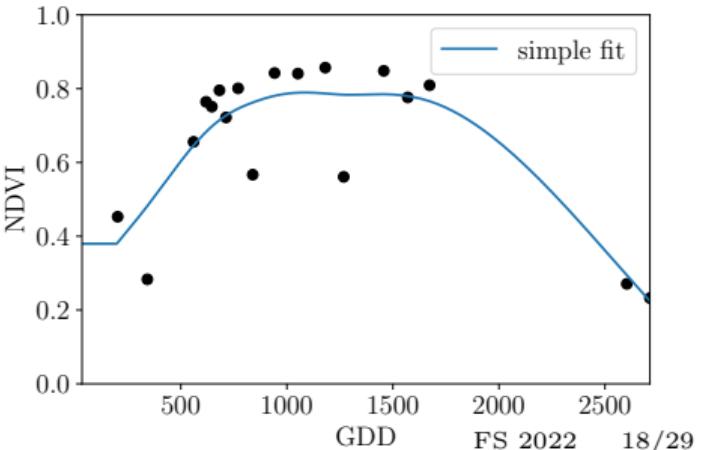
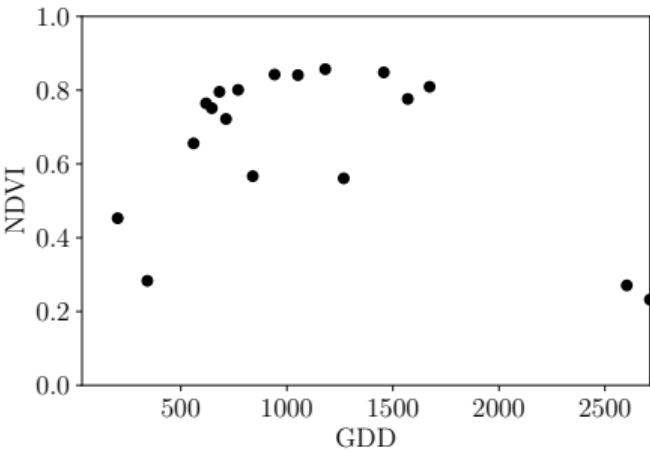
Smoothing Splines

$$\widehat{NDVI} := \operatorname{argmin}_{f \in \mathcal{F}} \underbrace{\sum_{i=1}^n (Y_i - f(x_i))^2}_{\text{sum of squares}} + \lambda \underbrace{\int f''(x)^2 dx}_{\text{smoothness}}$$

Similar to the Whittaker (but more general)

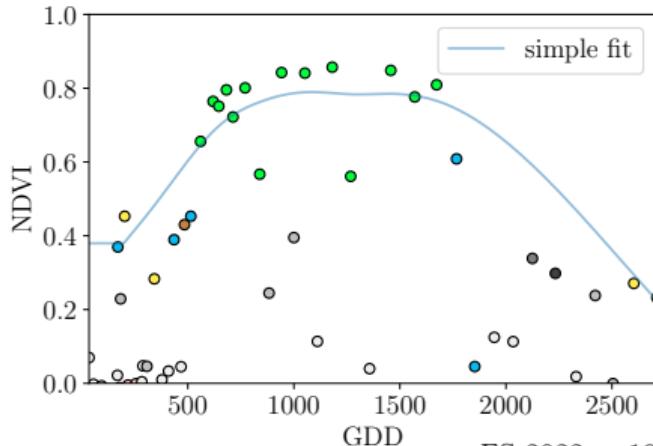
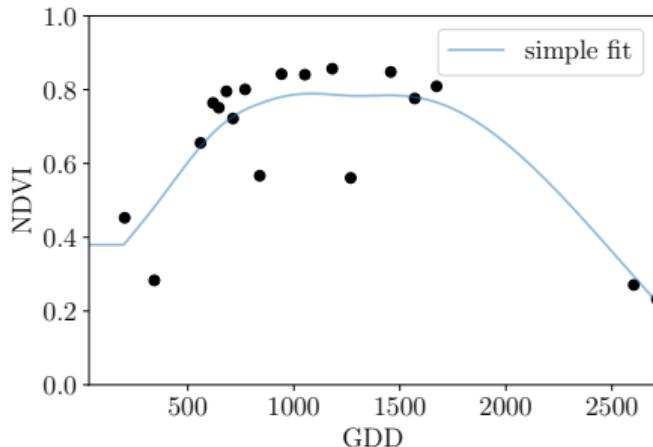


1. Interpolation



2. Other SCL-Classes

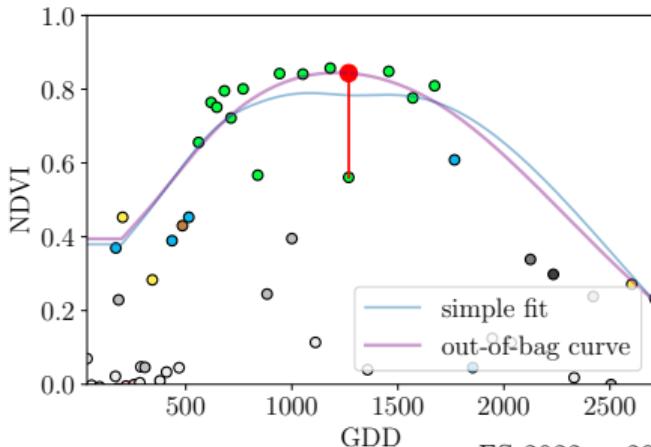
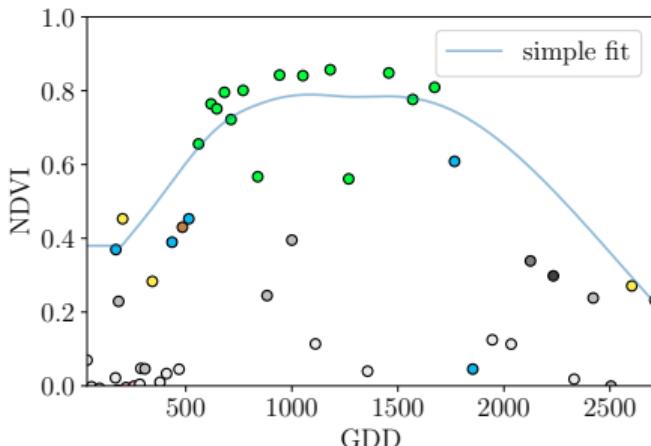
| Color | No. | Class |
|------------|-----|------------------------------|
| Black | 0: | Missing Data |
| Red | 1: | Saturated or defective pixel |
| Dark grey | 2: | Dark features / Shadows |
| Brown | 3: | Cloud shadows |
| Green | 4: | Vegetation |
| Yellow | 5: | Bare soils |
| Blue | 6: | Water |
| Grey | 7: | Cloud low probability |
| Light grey | 8: | Cloud medium probability |
| Cyan | 9: | Cloud high probability |
| Light blue | 10: | Thin cirrus cloud |
| Pink | 11: | Snow or ice |



3. Correction

- get “true” NDVI
- get table:

| | | | | |
|---------|----------|-----------|--------|---------|
| “truth” | observed | scl-class | B2-B10 | weather |
| “truth” | observed | scl-class | B2-B10 | weather |
| ... | ... | ... | ... | ... |

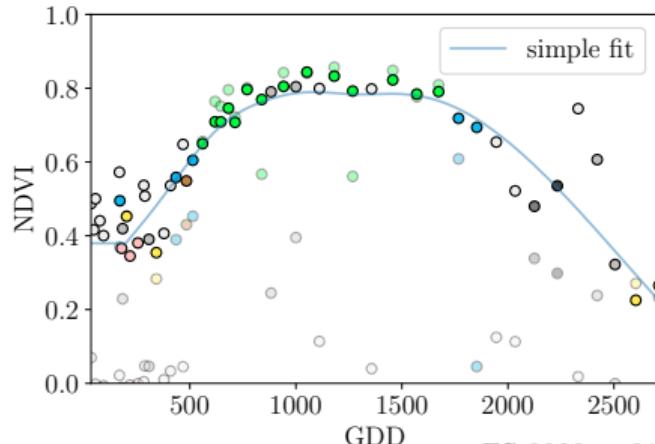
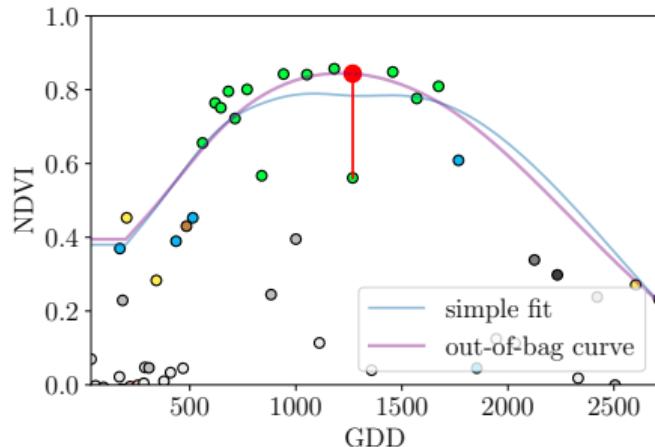


3. Correction

- get “true” NDVI
- get table:

| | | | | |
|---------|----------|-----------|--------|---------|
| “truth” | observed | scl-class | B2-B10 | weather |
| “truth” | observed | scl-class | B2-B10 | weather |
| ... | ... | ... | ... | ... |

- Statistical model
- predict/correct NDVI
- weather – yes or no?

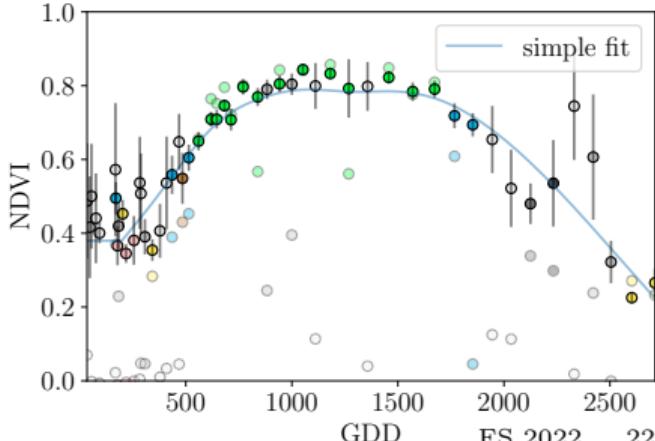
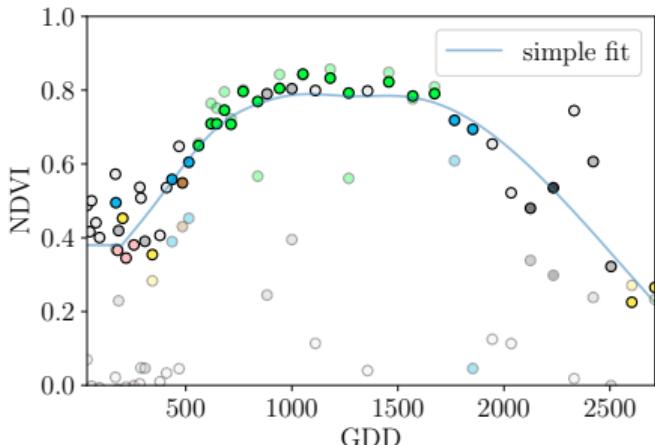


4. Uncertainty Estimation

- Table with residuals:

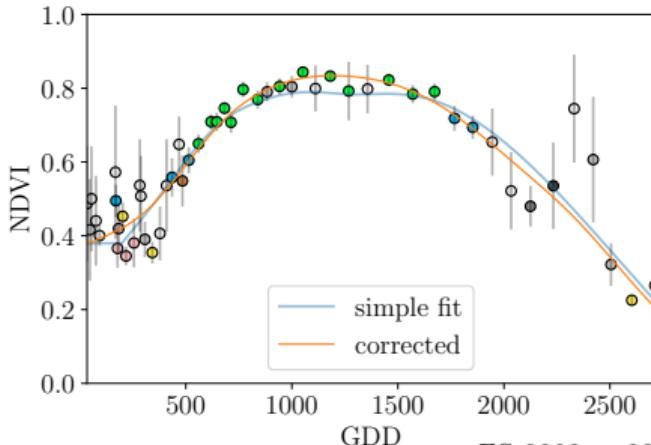
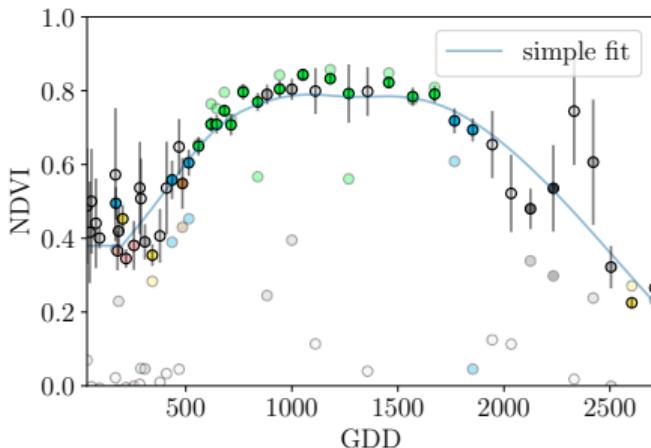
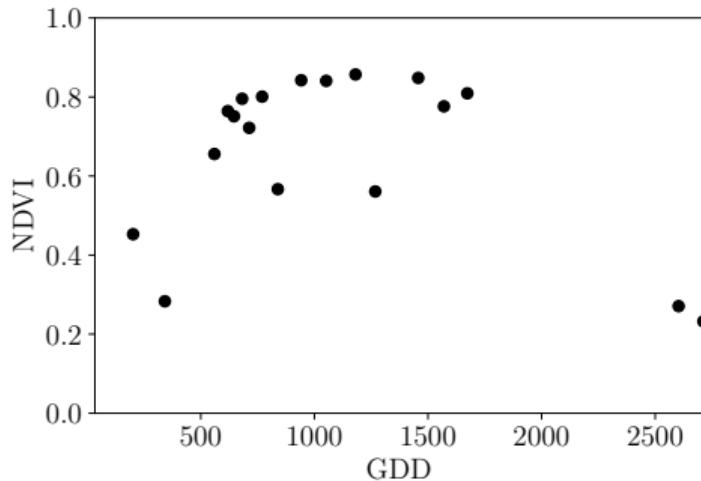
| residuals | observed | scl-class | B2-B10 | weather |
|-----------|----------|-----------|--------|---------|
| residuals | observed | scl-class | B2-B10 | weather |
| : | : | : | : | : |
| | | | | |

- Statistical model
- predict residuals
- $weights = \frac{1}{|residual|}$

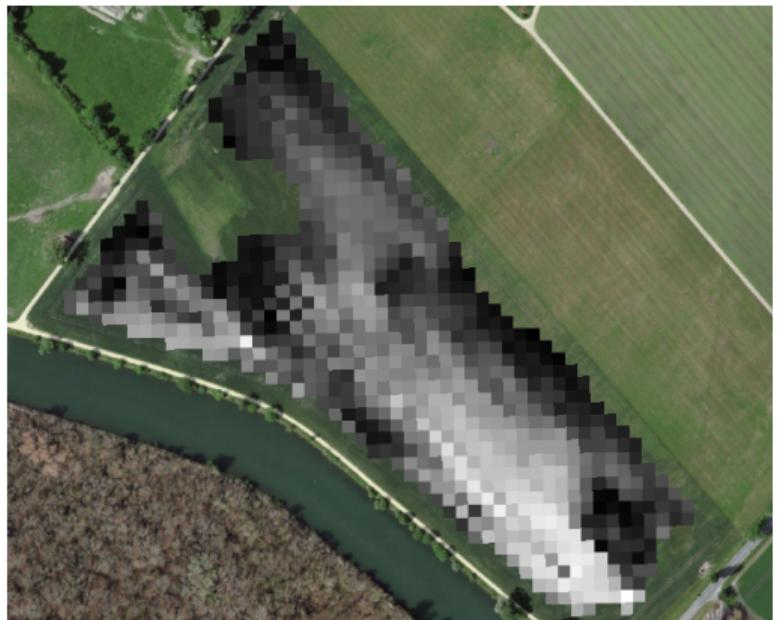
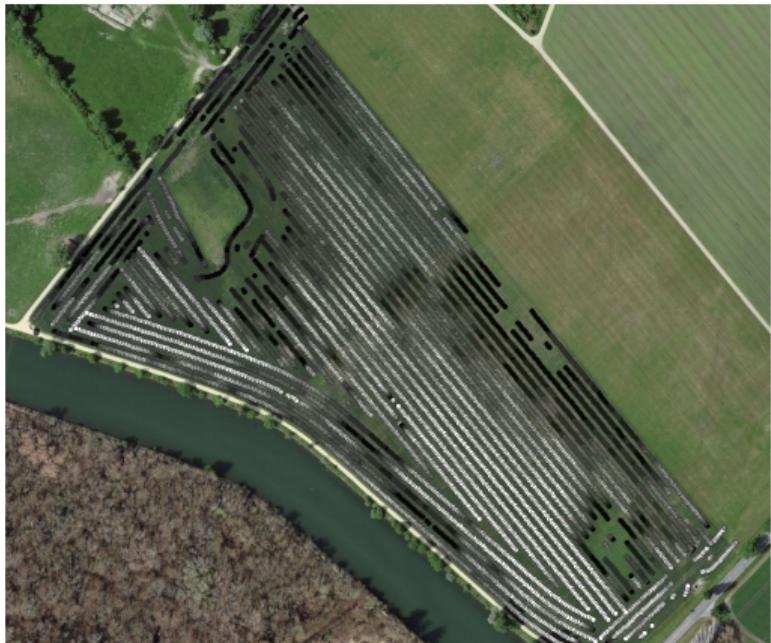


5. Robust Fit to Corrected NDVI

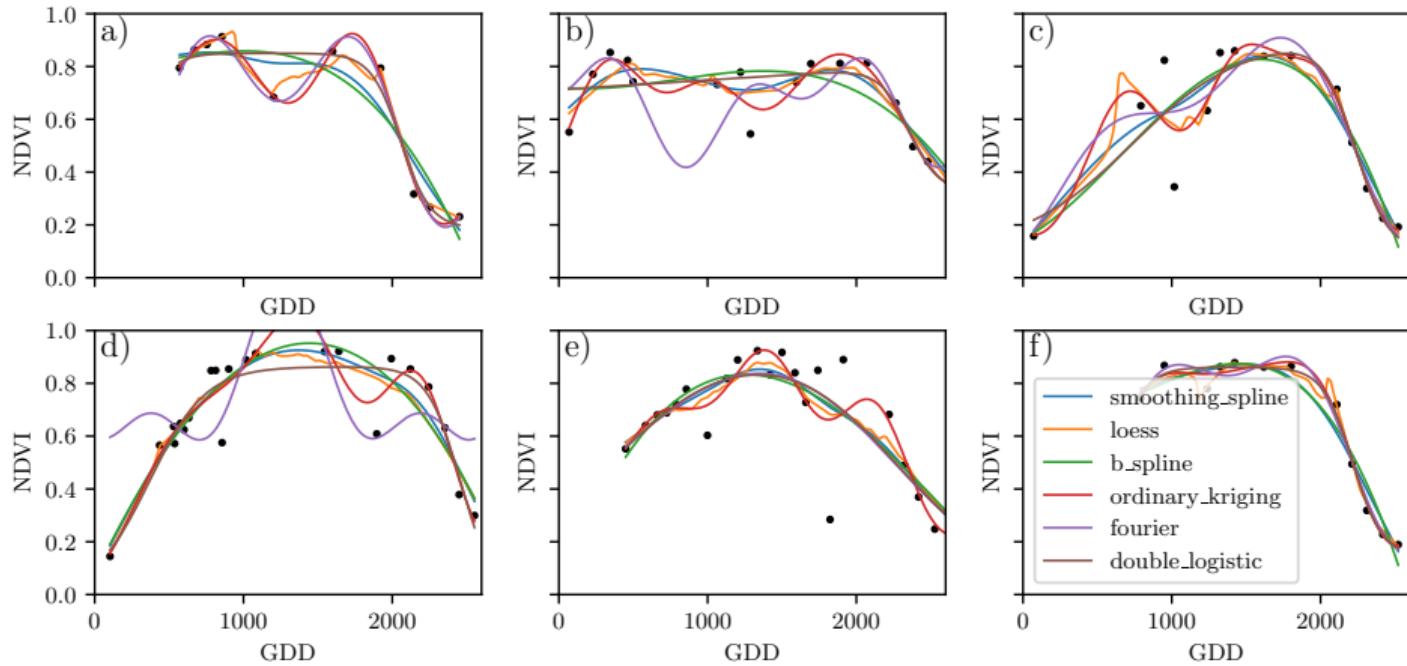
Reminder: Original Situation



Yield Mapping Data



Robustifying



Results

| | RF | OLS-SCL | OLS-all | MARS | GAM | LASSO | no correction |
|-------------------|-------|---------|---------|-------|-------|-------|---------------|
| SS | 0.676 | 0.736 | 0.726 | 0.731 | 0.729 | 0.731 | 0.703 |
| SS ^{rob} | 0.676 | 0.724 | 0.709 | 0.704 | 0.715 | 0.716 | 0.705 |
| DL | 0.672 | 0.692 | 0.691 | 0.691 | 0.702 | 0.701 | 0.667 |
| DL ^{rob} | 0.667 | 0.685 | 0.690 | 0.719 | 0.704 | 0.697 | 0.669 |

R-Package Provided

```
library(CorrectTimeSeries)
data(timeseries_list) # load NDVI-TS data

# Train RF
# Add "true" NDVI (or generally the response), by Out-Of-Bag estimation
timeseries_list <- lapply(timeseries_list, function(df) {
  df$oob_ndvi <- OOB_est(df$gdd, df$ndvi_observed) # gdd is the time-axis
  df})
# Train correction model
formula <- "oob_ndvi ~ B02+B03+B04+B05+B06+B07+B08+B8A+B11+B12+scl_class"
RF <- train_RF_with_formula(formula, timeseries_list, robustify=TRUE)
# ADD CORRECTION
timeseries_list <- lapply(timeseries_list, function(df) {
  df$corrected_ndvi <- randomForest:::predict.randomForest(RF, df)
  df})

# Get interpolation for each timeseries
lapply(timeseries_list, function(df){
  ss <- smoothing_spline(df$gdd, df$corrected_ndvi)
  predict(ss, 1:1000)$y})
```



Thank You !

APPENDIX: OLS^{SCL}

$$\begin{aligned} \text{NDVI}_{\text{corr}} = & 0.711 \text{NDVI}_{\text{observed}} + 0.215 \mathbb{1}_{SCL=2} + 0.237 \mathbb{1}_{SCL=3} + 0.210 \mathbb{1}_{SCL=4} \\ & + 0.116 \mathbb{1}_{SCL=5} + 0.162 \mathbb{1}_{SCL=6} + 0.327 \mathbb{1}_{SCL=7} + 0.474 \mathbb{1}_{SCL=8} \\ & + 0.575 \mathbb{1}_{SCL=9} + 0.306 \mathbb{1}_{SCL=10} + 0.512 \mathbb{1}_{SCL=11} \end{aligned}$$

$$\widehat{\text{abs}}(\text{NDVI}_{\text{true}} - \text{NDVI}_{\text{corr}}) = -0.133 \text{NDVI}_{\text{observed}} + 0.186 \mathbb{1}_{SCL=2} + 0.185 \mathbb{1}_{SCL=3} \\ + 0.146 \mathbb{1}_{SCL=4} + 0.089 \mathbb{1}_{SCL=5} + 0.167 \mathbb{1}_{SCL=6} \\ + 0.203 \mathbb{1}_{SCL=7} + 0.181 \mathbb{1}_{SCL=8} + 0.173 \mathbb{1}_{SCL=9} \\ + 0.180 \mathbb{1}_{SCL=10} + 0.172 \mathbb{1}_{SCL=11}$$