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, Introduction

 $_{8}$ This is a citation test [HK11].

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Overall choices for simplified models

- General topics:
- choice of Dark Matter type: Dirac (unless specified otherwise) and what we might be missing
- MFV and what we might be missing

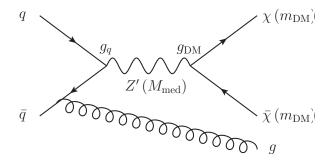


Figure 3.1: The diagram shows the pair production of dark matter particles in association with a parton from the initial state via an s-channel vector or axial-vector mediator. The process if specified by $(M_{\text{med}}, m_{\text{DM}}, g_{\text{DM}}, g_q)$, the mediator and dark matter masses, and the mediator couplings to dark matter and quarks respectively.

Recommended models for all MET+X analyses

Vector and axial vector mediator, s-channel exchange

- There are several matrix element implementations of the s-channel
- vector mediated DM production. This is available in POWHEG,
- MADGRAPH and also MCFM. The implementation in POWHEG
- generates DM pair production with 1 parton at next-to-leading or-
- der (NLO), whilst MADGRAPH and MCFM are at leading order
- (LO). As shown in POWHEG Ref. [HKR13], including NLO correc-23
- tions result in an enhancement in the cross section as compared to
- LO and though this is not significant, it does lead to a substantial
- reduction in the dependence on the choice of the renormalization
- and factorization scale and hence the theoretical uncertainty on the
- signal prediction. Since NLO calculations are available for the pro-
- cess in POWHEG, we recommend to proceed with POWHEG as the
- generator of choice.

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- We consider the case of a dark matter particle that is a Dirac 31
 - fermion and where the production proceeds via the exchange of a
- spin-1 s-channel mediator. We consider the following interactions 33
- between the DM and SM fields including a vector mediator with: 34
 - (a) vector couplings to DM and SM,
- (b) axial-vector couplings to DM and SM.

The corresponding Lagrangians are

$$\mathcal{L}_{\text{vector}} = \sum_{q} g_{q} Z'_{\mu} \bar{q} \gamma^{\mu} q + g_{\text{DM}} Z'_{\mu} \bar{\chi} \gamma^{\mu} \chi \tag{3.1}$$

$$\mathcal{L}_{\text{axial-vector}} = \sum_{q} g_{q} Z'_{\mu} \bar{q} \gamma^{\mu} \gamma^{5} q + g_{\text{DM}} Z'_{\mu} \bar{\chi} \gamma^{\mu} \gamma^{5} \chi \tag{3.2}$$

where the coupling extends over all the quarks and universal cou-

- plings are assumed for all the quarks. It is also possible to consider
- another model in which mixed vector and axial-vector couplings
- are considered, for instance the couplings to the quarks are vector
- whereas those to DM are axial-vector. As a starting point, we con-
- sider only the models with the vector couplings only and axial vector
- couplings only.
- We assume that no additional visible or invisible decays contribute
- to the width of the mediator, this is referred to as the minimal width
- and it is defined as follows for the vector and axial-vector models.

$$\Gamma_{\min} = \Gamma_{\bar{\chi}\chi} + \sum_{q} \Gamma_{\bar{q}q} \tag{3.3}$$

where the individual contributions to this from the partial width are

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$$\Gamma_{\bar{\chi}\chi}^{V} = \frac{g_{\rm DM}^{2} M_{\rm med}}{12\pi} \left(1 + \frac{2m_{\rm DM}^{2}}{M_{\rm med}^{2}} \right) \sqrt{1 - \frac{4m_{\rm DM}^{2}}{M_{\rm med}^{2}}}$$
(3.4)

$$\Gamma_{\bar{q}q}^{V} = \frac{3g_q^2 M_{\text{med}}}{12\pi} \left(1 + \frac{2m_q^2}{M_{\text{med}}^2} \right) \sqrt{1 - \frac{4m_q^2}{M_{\text{med}}^2}}$$
(3.5)

$$\Gamma_{\bar{\chi}\chi}^{A} = \frac{g_{\rm DM}^{2} M_{\rm med}}{12\pi} \left(1 - \frac{4m_{\rm DM}^{2}}{M_{\rm med}^{2}} \right)^{3/2}$$
(3.6)

$$\Gamma_{\bar{q}q}^{A} = \frac{3g_q^2 M_{\text{med}}}{12\pi} \left(1 - \frac{4m_q^2}{M_{\text{med}}^2} \right)^{3/2} . \tag{3.7}$$

Note the color factor 3 in the quark terms. Figure 3.2 shows the min-

50 imal width as a function of mediator mass for both vector and axial-

vector mediators assuming couplings of 1. With this choice of the

couplings, the dominant contribution to the minimal width comes

from the guarks due to the color factor enhancement.

The simplified models described here have four free parameters:

mediator mass M_{med} , Dark Matter mass m_{DM} , coupling of the medi-

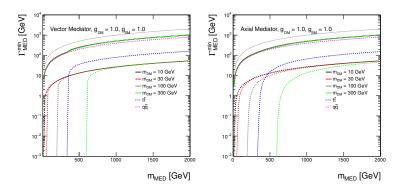
ator to quarks g_q and coupling of the mediator to Dark Matter g_{DM} .

In order to determine an optimal choice of the parameter grid for

presentation of the early Run-2 results, dependencies of the kinematic

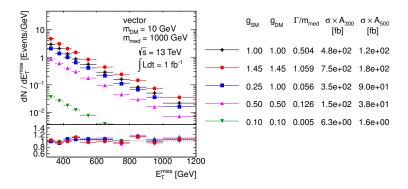
quantities and cross sections on the individual parameters need to be

studied. The following paragraphs list the main observations from



the scans over the parameters that support the final proposal for the parameter grid.

Scan over the couplings Figure 3.3 reveals there are no differences in the shape of the E_T distribution among the samples where the pair of 64 10 GeV Dark Matter particles are produced on-shell from the media-65 tor of 1 TeV, generated with different choice of the coupling strength. The considered coupling values range from 0.1 to 1.45, where the latter value approximates the maximum allowed coupling value, holding $g_q = g_{DM}$, such that $\Gamma_{min} < M_{med}$. Based on similar plots for different choices of mediator and Dark Matter masses, it is concluded that the shapes of kinematic distributions are not altered neither for the on-shell Dark Matter production where $M_{\rm med} > 2m_{\rm DM}$, nor for 72 the off-shell Dark Matter production where $M_{\rm med} < 2m_{\rm DM}$. Only the cross sections change. Differences in kinematic distributions are expected only close to the transition region where both on-shell and off-shell regimes mix.



The only place where special care needs to be taken are extremely heavy and narrow mediators, in other words with low couplings. Figure 3.4 suggests a change in the shape of the E_T distribution for 5 TeV mediator once $\Gamma_{\min}/M_{\mathrm{med}}$ gets down to the order of percent or

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Figure 3.2: Minimal width as a function of mediator mass for vector and axial-vector mediator assuming couplings of 1. The total width is shown as solid lines for Dark Matter masses of 10 GeV, 30 GeV, 100 GeV and 300 GeV in black, red, brown and green, respectively. The individual contributions from Dark Matter are indicated by dotted lines with the same colors. The contribution from all quarks but top is shown as magenta dotted line and the contribution from top quarks only is illustrated by the dotted blue line. The dotted black line shows the extreme case $\Gamma_{\min} = M_{\text{med}}$.

Figure 3.3: Scan over couplings. The E_T distribution is compared for the vector mediator models using the parameters as indicated. Ratios of the normalized distributions with respect to the first one are shown. A_{300} and A_{500} in the table denote the acceptance of the $E_T > 300\,\text{GeV}$ and $E_T > 500\,\text{GeV}$ cut, respectively.

below. This, however, does not come from physics as it is a feature of 81 the generator implementation, where a cutoff for the regions far away 82 from the mediator mass is often used. This is illustrated in Fig. 3.5 showing the invariant mass of the Dark Matter pair in the samples generated for 7 TeV mediator with different coupling strength. In 85 all cases, it is expected to observe a peak around the mediator mass with a tail extending to $m_{\bar{\chi}\chi} \to 0$, significantly enhanced by parton distribution functions at low Bjorken x. For coupling strength 1 and 3, the massive enhancement at $m_{\bar{\chi}\chi} \rightarrow 0$ implies the resonant production at $m_{\bar{\chi}\chi} = 7 \text{ TeV}$ is statistically suppressed such that barely any events are generated there. However, for narrower mediators 91 with couplings below 1, the peak around 7 TeV is clearly visible in the generated sample and the dominant tail at $m_{\bar{\chi}\chi} \to 0$ is artificially cut off, leading to unphysical cross section predictions and kinematic 94 shapes. This explains why the sample with the narrowest mediator in Fig. 3.4 is heavily suppressed in terms of production cross section and also gives different E_T shape. In general, for such extreme parameter choices the EFT model should give the correct answer. In case the simplified model calculation does not reproduce the EFT result, the 99 phase space generation of the simplified model has to be carefully ex-100 amined in order to understand the cause of the problem. Fortunately, this is a rather academic discussion as such extreme corners of the 102 parameter space are not going to be considered for presentation of 103 Run-2 results.

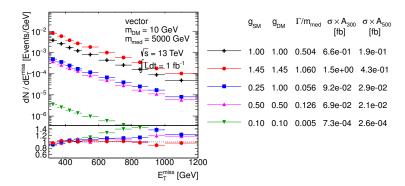


Figure 3.4: Scan over couplings. The E_T distribution is compared for the vector mediator models using the parameters as indicated. Ratios of the normalized distributions with respect to the first one are shown. A_{300} and A_{500} in the table denote the acceptance of the $E_T > 300\,\text{GeV}$ and $E_T > 500\,\text{GeV}$ cut, respectively.

Scan over the Dark Matter mass For the fixed mediator mass and couplings, both the cross section and the kinematic distributions remain similar for different Dark Matter masses as long as $M_{\rm med} > 2m_{\rm DM}$. This is illustrated in Fig. 3.6 on an example of 1 TeV mediator and Dark Matter masses ranging from 10 GeV to 300 GeV. It is observed that the cross section decreases as the Dark Matter mass reaches closer to $M_{\rm med}/2$. Once the Dark Matter pair is produced off-line, the cross section of such simplified model is suppressed and the E_T

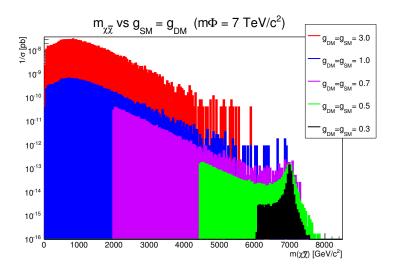


Figure 3.5: Invariant mass of the Dark Matter pair in the samples with $M_{\rm med} = 7 \, \text{TeV}$ and different coupling strengths.

spectrum hardens, as demonstrated with the choice of 1 TeV Dark Matter in the same plot. Figure 3.7 reveals the E_T spectrum hardens further with increasing Dark Matter mass, accompanied by the grad-115 ual decrease of the cross section. From these observations one can 116 conclude:

A coarse binning along $m_{\rm DM}$ is sufficient at $M_{\rm med} \gg 2m_{\rm DM}$.

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- Finer binning is needed in order to capture the changes in the cross section and kinematic quantities close to the production threshold on both sides around $M_{\text{med}} = 2m_{\text{DM}}$.
- Due to the significant cross section suppression of the off-shell 122 Dark Matter pair production, it is not necessary to populate the parameter space $M_{\rm med} \ll 2m_{\rm DM}$ since the LHC is not going to be 124 able to probe the models there. 125

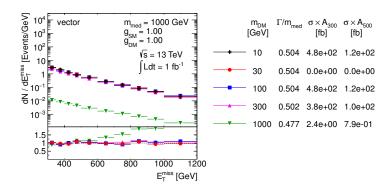


Figure 3.6: Scan over Dark Matter mass. The E_T distribution is compared for the vector mediator models using the parameters as indicated. Ratios of the normalized distributions with respect to the first one are shown. A_{300} and A_{500} in the table denote the acceptance of the $E_T > 300 \,\text{GeV}$ and $E_T > 500 \,\text{GeV}$ cut, respectively.

Scan over the mediator mass Changing the mediator mass for fixed Dark Matter mass and couplings leads to significant differences in

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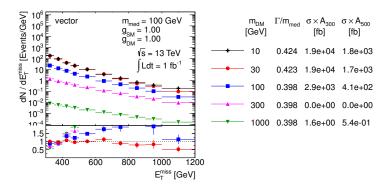


Figure 3.7: Scan over Dark Matter mass. The E_T distribution is compared for the vector mediator models using the parameters as indicated. Ratios of the normalized distributions with respect to the first one are shown. A_{300} and A_{500} in the table denote the acceptance of the $E_T > 300\,\text{GeV}$ and $E_T > 500\,\text{GeV}$ cut, respectively.

cross section and shapes of the kinematic variables for $M_{\rm med} > 2m_{\rm DM}$ as shown in Fig. 3.8. As expected, higher mediator masses lead to harder E_T spectra. On the other hand, the E_T shapes are similar in the off-shell Dark Matter production regime as well as no dramatic differences in cross sections are observed, which is illustrated in Fig. 3.9. Therefore, a coarse binning along $m_{\rm DM}$ is sufficient at $M_{\rm med} \ll 2m_{\rm DM}$.

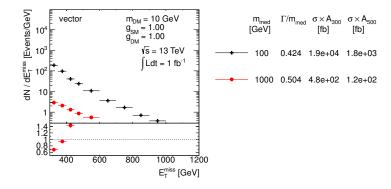


Figure 3.8: Scan over mediator mass. The E_T distribution is compared for the vector mediator models using the parameters as indicated. Ratios of the normalized distributions with respect to the first one are shown. A_{300} and A_{500} in the table denote the acceptance of the $E_T > 300 \, \text{GeV}$ and $E_T > 500 \, \text{GeV}$ cut, respectively.

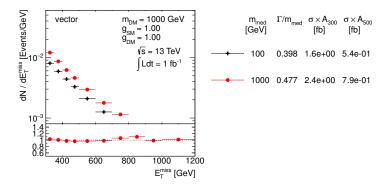


Figure 3.9: Scan over mediator mass. The E_T distribution is compared for the vector mediator models using the parameters as indicated. Ratios of the normalized distributions with respect to the first one are shown. A_{300} and A_{500} in the table denote the acceptance of the $E_T > 300 \, \text{GeV}$ and $E_T > 500 \, \text{GeV}$ cut, respectively.

Proposed parameter grid Based on the observations above, the following proposal is made for the presentation of the early Run-2 results from the LHC:

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- (a) Give results in the $M_{\rm med}$ – $m_{\rm DM}$ plane for a particular choice of the couplings.
- (b) Give results in the g_q – $g_{\rm DM}$ plane for a particular choice of the masses.

We choose to display the results in the M_{med} - m_{DM} plane for the 142 choice of the couplings $g_q = g_{DM} = 1$. In order to motivate the highest mediator mass grid point, the expected sensitivity of Run-2 144 LHC data needs to be taken into account. The expected upper limit 145 at 95% confidence level on the product of cross section, acceptance and efficiency, $\sigma \times A \times \epsilon$, in the final Run-1 ATLAS mono-jet anayl-147 sis [A⁺15] is 51 fb and 7.2 fb for $E_T > 300$ GeV and $E_T > 500$ GeV, respectively. The ATLAS 14 TeV prospects [ATL14] predict twice better sensitivity with the first 5 fb⁻¹ of data already. Given the cross section for V+jets processes increases by roughly factor 2 when go-151 ing from $\sqrt{s} = 8 \text{ TeV}$ to 13 TeV, similar fiducial cross section limits 152 can be expected with the first Run-2 data as from the final Run-1 analysis. The generator level cross section times the acceptance at 154 $E_T > 500 \,\text{GeV}$ for the model with couplings $g_q = g_{\text{DM}} = 1$, light Dark 155 Matter of 10 GeV and 1 TeV vector mediator is at the order of 100 fb, i.e. the early Run-2 mono-jet analysis is going to be sensitive to heavier mediators than this. The value of $\sigma \times A$ at $E_T > 500 \,\text{GeV}$ for 5 TeV 158 vector mediator is at the order of 0.1 fb, therefore this model proba-159 bly lies beyond the reach of the LHC. Based on these arguments, the following M_{med} grid points are chosen, equidistant in the logarithmic 161 scale: 10 GeV, 30 GeV, 100 GeV, 300 GeV, 1000 GeV and 3000 GeV. Given 162 the fact that significant changes in cross section happen around the 163 $M_{\rm med} = 2m_{\rm DM}$ threshold, the $m_{\rm DM}$ grid points are taken at $M_{\rm med}/2$, namely: 5 GeV, 15 GeV, 50 GeV, 150 GeV, 500 GeV and 1500 GeV. The 165 detailed studies of the impact of the parameter changes on the cross 166 section and kinematic distributions presented earlier in this section support removing some of the grid points and rely on interpolation. The optimised grids proposed for the vector and axial-vector media-169 tors are given in Fig. 3.10, containing 24 mass points each. The presentation of the results in the g_q – g_{DM} plane for fixed masses benefits from cross section scaling and is discussed in Sec-172 tion 3.3. 173

3.2 Scalar and pseudoscalar mediator, s-channel exchange

The matrix element implementation of the s-channel spin-o mediated DM production is available in POWHEG with the full top-loop calculation at LO [HR15]. The model assumes Dirac Dark Matter particles and is based on the minimal flavor violation (MFV), which motivates

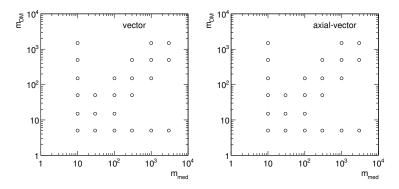


Figure 3.10: Proposed parameter grid for vector and axial-vector mediator in the $M_{\rm med}$ – $m_{\rm DM}$ plane.

Higgs-like Yukawa couplings of the mediator to the Standard Model quarks. No other couplings, such as to leptons, are allowed in this model. The following two cases are considered:

(a) scalar couplings to DM and SM,

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(b) pseudo-scalar couplings to DM and SM with the corresponding Lagrangians written as:

$$\mathcal{L}_{\text{scalar}} = g_q \sum \frac{m_q}{v} (\bar{q}q) S + g_{\text{DM}}(\bar{\chi}\chi) S$$
 (3.8)

$$\mathcal{L}_{\text{pseudo-scalar}} = g_q \sum \frac{m_q}{v} (\bar{q} \gamma^5 q) P + g_{\text{DM}} (\bar{\chi} \gamma^5 \chi) P$$
 (3.9)

(3.10)

where $v=246\,\text{GeV}$ denotes the Higgs vacuum expectation value. We choose to consider minimal mediator width given by Eq. 3.3, where the individual contributions follow from

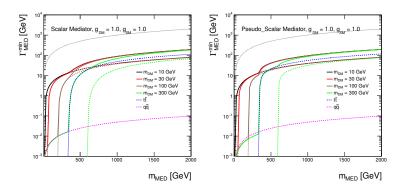
$$\Gamma_{\bar{\chi}\chi}^{S} = \frac{g_{\rm DM}^{2} M_{\rm med}}{8\pi} \left(1 - \frac{4m_{\rm DM}^{2}}{M_{\rm med}^{2}} \right)^{3/2}$$
(3.11)

$$\Gamma_{\bar{q}q}^{S} = \frac{3g_q^2 M_{\text{med}}}{8\pi} \frac{m_q^2}{v^2} \left(1 - \frac{4m_q^2}{M_{\text{med}}^2} \right)^{3/2}$$
(3.12)

$$\Gamma_{\bar{\chi}\chi}^{P} = \frac{g_{\rm DM}^{2} M_{\rm med}}{8\pi} \sqrt{1 - \frac{4m_{\rm DM}^{2}}{M_{\rm med}^{2}}}$$
(3.13)

$$\Gamma_{\bar{q}q}^{P} = \frac{3g_q^2 M_{\text{med}}}{8\pi} \frac{m_q^2}{v^2} \sqrt{1 - \frac{4m_q^2}{M_{\text{med}}^2}} \,. \tag{3.14}$$

The minimal width for scalar and pseudo-scalar mediators with $g_q = g_{\rm DM} = 1$ are shown in Fig. 3.11, illustrating the effect of the Higgs-like Yukawa couplings. For the mediator masses above twice the top quark mass m_t , the minimal width receives the dominant contribution from the top quark. For lighter mediator masses, Dark Matter dominates as the couplings to lighter quarks are Yukawa suppressed. Note that we decide to ignore the partial width coming from gluons through loops as it can be safely neglected [HR15].



Similarly as in the case of the vector and axial-vector mediators, scans in the paramater space are performed also for the scalar and pseudo-scalar mediators in order to decide on the optimised parameter grid for the presentation of Run-2 results. Figures?? show the scans over the couplings, Dark Matter mass and mediator mass and the same conclusions apply as in Section 3.1.

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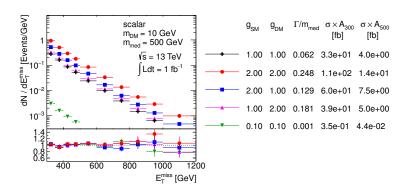
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Since the top quark gives the dominant contribution to the mediator width due to Higgs-like Yukawa couplings, the effect of the top channel opening in the mediator production was studied in addition. Scan over the mediator mass is shown in Fig. 3.16 where the mediator masses 300 GeV and 500 GeV are chosen to be below and above $2m_t$. The off-shell Dark Matter production regime is assumed by taking $m_{\rm DM}=1\,{\rm TeV}$ in order to allow studying solely the effects of the couplings to quarks. No differences in the kinematic distributions are observed and also the cross sections remain similar in this case. Therefore, it is concluded that no significant changes appear for mediator masses around the $2m_t$ threshold.



The optimized parameter grid in the M_{med} - m_{DM} plane for scalar and pseudo-scalar mediators is motivated by similar arguments as in the previous section. Therefore, similar pattern is followed here, taking again $g_q = g_{DM} = 1$. Only the sensitivity to the highest me-

Figure 3.11: Minimal width as a function of mediator mass for scalar and pseudo-scalar mediator assuming couplings of 1. The total width is shown as solid lines for Dark Matter masses of 10 GeV, 30 GeV, 100 GeV and 300 GeV in black, red, brown and green, respectively. The individual contributions from Dark Matter are indicated by dotted lines with the same colors. The contribution from all quarks but top is shown as magenta dotted line and the contribution from top quarks only is illustrated by the dotted blue line. The dotted black line shows the extreme case $\Gamma_{\min} = M_{\text{med}}$.

Figure 3.12: Scan over couplings. The E_T distribution is compared for the scalar mediator models using the parameters as indicated. Ratios of the normalized distributions with respect to the first one are shown. A_{300} and A_{500} in the table denote the acceptance of the $\not\!E_T > 300 \, \text{GeV}$ and $\not\!E_T > 500 \, \text{GeV}$ cut, respectively.

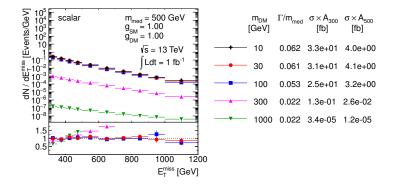


Figure 3.13: Scan over Dark Matter mass. The E_T distribution is compared for the scalar mediator models using the parameters as indicated. Ratios of the normalized distributions with respect to the first one are shown. A_{300} and A_{500} in the table denote the acceptance of the $E_T > 300\,\mathrm{GeV}$ and $E_T > 500\,\mathrm{GeV}$ cut, respectively.

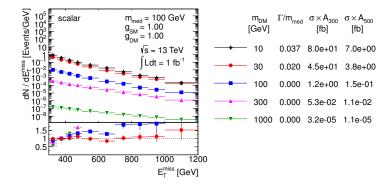


Figure 3.14: Scan over Dark Matter mass. The $\not\! E_T$ distribution is compared for the scalar mediator models using the parameters as indicated. Ratios of the normalized distributions with respect to the first one are shown. A_{300} and A_{500} in the table denote the acceptance of the $\not\! E_T > 300\, {\rm GeV}$ and $\not\! E_T > 500\, {\rm GeV}$ cut, respectively.

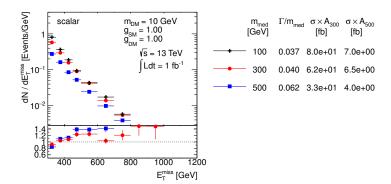


Figure 3.15: Scan over mediator mass. The E_T distribution is compared for the scalar mediator models using the parameters as indicated. Ratios of the normalized distributions with respect to the first one are shown. A_{300} and A_{500} in the table denote the acceptance of the $E_T > 300\,\text{GeV}$ and $E_T > 500\,\text{GeV}$ cut, respectively.

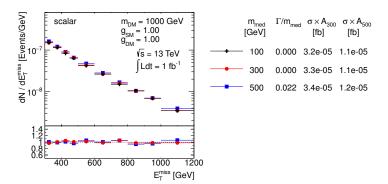


Figure 3.16: Scan over mediator mass. The E_T distribution is compared for the scalar mediator models using the parameters as indicated. Ratios of the normalized distributions with respect to the first one are shown. A_{300} and A_{500} in the table denote the acceptance of the $E_T > 300 \,\text{GeV}$ and $E_T > 500 \,\text{GeV}$ cut, respectively.

diator masses has to be revisited. The generator level cross section 214 times the acceptance at $E_T > 500 \,\text{GeV}$ for the model with couplings 215 $g_q = g_{\rm DM} = 1$, light Dark Matter of 10 GeV and 500 GeV scalar mediator is at the order of 10 fb, i.e. just at the edge of the early Run-2 217 sensitivity. Increasing the mediator mass to 1 TeV pushes the prod-218 uct $\sigma \times A$ down to approximately 0.1 fb, beyond the LHC sensitivity. Therefore, we choose to remove the 3 TeV mediator mass from the grid and present the final grid with 19 mass points only in Fig. 3.17. 221

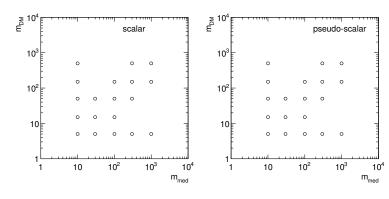


Figure 3.17: Proposed parameter grid for scalar and pseudo-scalar mediator in the M_{med} – m_{DM} plane.

The proposal for the scan in the g_q – g_{DM} plane is described in the 222 following section.

Cross section scaling 3.3

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The aim of the parameter grid optimization is to find out whether 225 certain parts of the parameter space can be omitted and one can rely 226 on the neighboring grid points in order to populate the missing parts. There are two ways of doing this:

- Interpolation is used in-between the grid points that are close enough such that finer granularity is not needed for the presentation purposes, or between the points where smooth or no changes of the results are expected. The latter argument is exactly the one that motivates the reduction of the grid points in the M_{med} – m_{DM} plane.
- Recalculation of the results can be used when the dependencies with respect to the neighboring grid points are known.

The results of the scan over the couplings presented in the previous sections indicate there are no changes in kinematic distributions for different choices of the coupling strengths. This means that the acceptance remains the same in the whole g_q – g_{DM} plane and it is sufficient to perform the detector simulation only for one single grid point. The resulting truth-level selection acceptance and the detector

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reconstruction efficiency can then be applied to all remaining grid points in the g_q – $g_{\rm DM}$ plane where only the generator-level cross section needs to be known. This significantly reduces the computing time as the detector response is by far the most expensive part of the Monte Carlo sample production. However, a further step can be taken if a parameterization of the cross section dependence from one grid point to another exists, in which case the number of generated samples can be reduced even further.

Let us now elaborate on a cross section scaling procedure. The propagator on the s-channel exchange is written in a Breit-Wigner form as $\frac{1}{\sqrt{s}-M_{\rm med}^2+iM_{\rm med}\Gamma}$. The relative size of the center-of-mass energy defined by the two partons entering the hard process and the mediator mass allows to classify the production in the following way:

- off-shell production when $\sqrt{s} \gg M_{\rm med}$ leading to suppressed cross sections,
- on-shell production when $\sqrt{s} \sim M_{
 m med}$ leading to enhanced cross sections,
 - effective field theory (EFT) limit when $\sqrt{s} \ll M_{\rm med}$.

All three categories can be distinguished in Fig. 3.18 showing the upper limit on the interaction scale $M^* \equiv M_{\rm med}/\sqrt{g_q g_{\rm DM}}$ for vector mediator. In the case of the off-shell production and the EFT limit, the first term in the propagator dominates which reduces the dependence on the mediator width. Therefore, in these cases one can approximate the cross section as

$$\sigma \propto g_q^2 g_{\rm DM}^2. \tag{3.15}$$

The on-shell production regime is the most interesting one as it gives the best chances for a discovery at the LHC given the cross section enhancement. The propagator term with the width cannot be neglected in this case and, in the narrow width approximation, one can integrate

$$\int \frac{ds}{(s - M_{\text{med}}^2)^2 + M_{\text{med}}^2 \Gamma^2} = \frac{\pi}{M_{\text{med}} \Gamma}$$
 (3.16)

which further implies the cross section scaling

$$\sigma \propto \frac{g_q^2 g_{\rm DM}^2}{\Gamma}.\tag{3.17}$$

Since $\Gamma \sim g_q^2 + g_{
m DM}^2$, one can simplify this rule in the extreme cases as follows

$$\sigma \propto \frac{g_q^2 g_{\text{DM}}^2}{g_q^2 + g_{\text{DM}}^2} \xrightarrow{g_q \ll g_{\text{DM}}} g_q^2$$
 (3.18)

$$\sigma \propto \frac{g_q^2 g_{\text{DM}}^2}{g_q^2 + g_{\text{DM}}^2} \xrightarrow{g_q \gg g_{\text{DM}}} g_{\text{DM}}^2.$$
 (3.19)

However, it is important to keep in mind that there is no simple scaling rule for how the cross section changes with the Dark Matter mass, mediator mass and the mediator width because PDFs matter in such cases as well. Therefore, the scaling procedure outlined above is expected to work only for fixed masses and fixed mediator width.

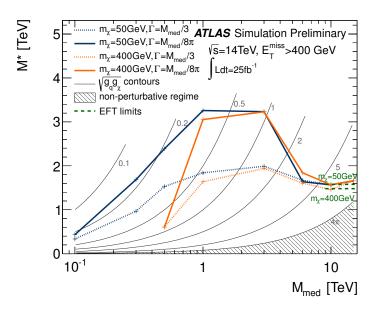


Figure 3.18: Comparison of the 95% CL lower limits on the scale of the interaction of a Z'-like simplified model at 14 TeV, in terms of the mediator mass. Corresponding limits from EFT models are shown on the same plot as green dashed lines to show equivalence between the two models for high mediator masses. Taken from Ref. [ATL14].

Figures 3.19 and 3.20 show the minimal width in the g_q – $g_{\rm DM}$ plane for all vector, axial-vector, scalar and pseudo-scalar mediators for $M_{\rm med}=100\,{\rm GeV}$ and 1000 GeV, respectively, taking $m_{\rm DM}=10\,{\rm GeV}$. The individual colors indicate the lines of constant width along which the cross section scaling works. For vector and axial-vector mediators, the minimal width is predominantly defined by g_q due to the number of quark flavors and the color factor. On the contrary, both the Standard Model and Dark Matter partial width have comparable contributions in case of scalar and pseudo-scalar mediators if the top quark channel is open ($M_{\rm med}>2m_t$). However, mostly $g_{\rm DM}$ defines the minimal width for $M_{\rm med}<2m_t$ due to the Yukawa-suppressed light quark couplings.

The performance of the cross section scaling is demonstrated in Fig. 3.21 where the mass point $M_{\rm med}=1\,{\rm TeV}$ and $m_{\rm DM}=10\,{\rm GeV}$ is chosen and rescaled from the starting point $g_q=g_{\rm DM}=1$ according to Eq. 3.17 to populate the whole $g_q-g_{\rm DM}$ plane. This means the width is not kept constant in this test and this is done in purpose in order to point out deviations from the scaling when the width is altered. For each mass point, the rescaled cross section is compared to the generator cross section and the ratio of the two is plotted. For the given choice of the mass points, the scaling seems to work

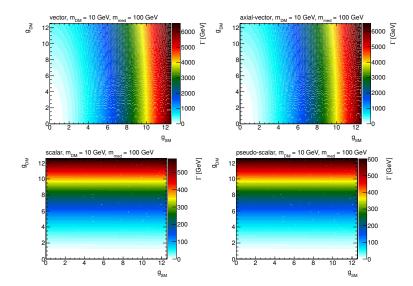


Figure 3.19: Minimal width for vector, axial-vector, scalar and pseudo-scalar mediators as a function of the individual couplings g_q and $g_{\rm DM}$, assuming $M_{\rm med}=100\,{\rm GeV}$ and $m_{\rm DM}=10\,{\rm GeV}$.

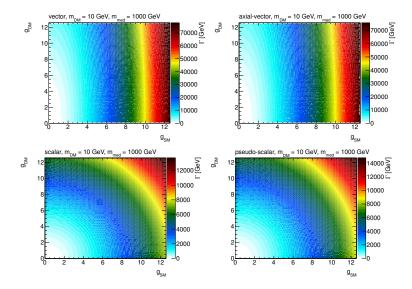


Figure 3.20: Minimal width for vector, axial-vector, scalar and pseudo-scalar mediators as a function of the individual couplings g_q and $g_{\rm DM}$, assuming $M_{\rm med}=1\,{\rm TeV}$ and $m_{\rm DM}=10\,{\rm GeV}$.

²⁸⁹ approximately with the precision of $\sim 20\%$ in the region where $\Gamma_{\min} < M_{\mathrm{med}}$. Constant colors indicate the lines along which the cross section scaling works precisely and there is a remarkable resemblance of the patterns shown in the plots of the mediator width. To prove the scaling along the lines of constant width works, one such line is chosen in Fig. 3.22 for a scalar mediator, defined by $M_{\mathrm{med}} = 300\,\mathrm{GeV},\,m_{\mathrm{DM}} = 100\,\mathrm{GeV},\,g_q = g_{\mathrm{DM}} = 1$, and the rescaled and generated cross sections are found to agree within 3%.

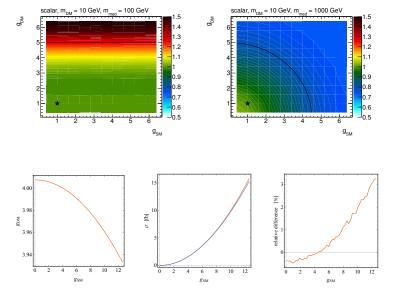


Figure 3.21: Ratio of the rescaled and generated cross sections in the g_q – $g_{\rm DM}$ plane. The point at $g_q=g_{\rm DM}=1$, taken as a reference for the rescaling, is denoted by a star symbol. Scalar model with $M_{\rm med}=100\,{\rm GeV}$ (left) and 1 TeV (right) is plotted for $m_{\rm DM}=10\,{\rm GeV}$. The limiting case $\Gamma_{\rm min}=M_{\rm med}$ is shown as a black line.

Figure 3.22: Scaling along the lines of constant width. The line of constant width for $M_{\rm med}=300\,{\rm GeV}$ and $m_{\rm DM}=100\,{\rm GeV}$, intercepting $g_q=g_{\rm DM}=4$ is shown on left. The generated and rescaled cross sections are compared in the middle, the corresponding ratio is shown on right.

Proposed parameter grid We propose to present the results in the g_q – $g_{\rm DM}$ plane using the following prescription:

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- Since the shapes of kinematic quantities do not change for different couplings, use the acceptance and efficiency for the available $m_{\rm DM}=50\,{\rm GeV},\,M_{\rm med}=300\,{\rm GeV},\,g_q=g_{\rm DM}=1$ grid point from the $M_{\rm med}$ – $m_{\rm DM}$ plane for the scalar and pseudo-scalar mediator. In case of the vector and axial-vector mediator, use the grid point $m_{\rm DM}=50\,{\rm GeV},\,M_{\rm med}=1\,{\rm TeV},\,g_q=g_{\rm DM}=1.$
- Generate additional samples in order to get generator cross sections only. For scalar and pseudo-scalar mediator, choose $m_{\rm DM}=50\,{\rm GeV},\,M_{\rm med}=300\,{\rm GeV}$ with the following values for $g_q=g_{\rm DM}$: 0.1, 2, 3, 4, 5, 6. For vector and axial vector mediator, choose $m_{\rm DM}=50\,{\rm GeV},\,M_{\rm med}=1\,{\rm TeV}$ with the following values for $g_q=g_{\rm DM}$: 0.1, 0.25, 0.5, 0.75, 1.25, 1.5. The upper values are defined by the minimal width reaching the mediator mass.
- Rescale the generator cross sections along the lines of constant width in order to populate the whole g_q – $g_{\rm DM}$ plane.

Rescaling to different mediator width In general there may be an interest to consider larger mediator masses than Γ_{\min} in order to accommodate further couplings of the mediator. The cross section scaling method described above can be used to reinterpret the results presented for the minimal width, since multiplying the width by factor n is equivalent to changing the coupling strength by factor \sqrt{n} , i.e.

$$\sigma(g_q, g_{\rm DM}, n\Gamma_{\rm min}(g_q, g_{\rm DM})) \propto \frac{g_q^2 g_{\rm DM}^2}{\Gamma_{\rm min}(\sqrt{n}g_q, \sqrt{n}g_{\rm DM})}.$$
 (3.20)

The cross section for the sample with couplings g_q and g_{DM} and modified mediator width $\Gamma = n\Gamma_{\min}$ can therefore be rescaled from a sample generated with the minimal width corresponding to the couplings scaled by \sqrt{n} as described in the following formula.

$$\sigma(g_q, g_{\text{DM}}, n\Gamma_{\min}(g_q, g_{\text{DM}})) = \frac{1}{n^2} \sigma(\sqrt{n}g_q, \sqrt{n}g_{\text{DM}}, \Gamma_{\min}(\sqrt{n}g_q, \sqrt{n}g_{\text{DM}}))$$
(3.21)

Advantage of doing this is again in the fact that no event selection and detector response needs to be simulated since the changes in couplings do not have an effect on the shapes of kinematic distributions.

318 3.3.1 POWHEG settings

- This section describes specif settings for the Dark Matter models needed to run the POWHEG generation.
 - The POWHEG implementation allows to generate a single sample that provides sufficient statistics in all mono-jet analysis signal regions. POWHEG generates weighted events and the bornsuppfact parameter is used to set the event suppression factor according to

$$F(k_{\mathrm{T}}) = \frac{k_{\mathrm{T}}^2}{k_{\mathrm{T}}^2 + \mathsf{bornsuppfact}^2} \,. \tag{3.22}$$

- In this way, the events at low \mathbb{E}_T are suppressed and receive higher event weights which ensures higher statistics at high \mathbb{E}_T . We recommend to set bornsuppfact to 1000.
- The bornktmin parameter allows to suppress the low E_T region even further by starting the generation at a certain value of k_T . It is recommended to set this parameter to half the lower analysis E_T cut, therefore the proposed value for bornktmin is 150.
- Set runningwidth to o.

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Set mass_low and mass_high to -1.

- The minimal values for ncall1, itmx1, ncall2, itmx2 are 250000, 5, 1000000, 5 for the DMV model, respectively. In order to increase speed, set foldsci and foldy to 2 and keep foldphi at 1.
- The minimal values for ncall1, itmx1, ncall2, itmx2 are 100000, 5, 100000, 5 for the DMS_tloop model, respectively.
- Allow negative weights for the DMV model by setting withnegweights to 1.
- Since the DMS_tloop model is a leading order process, set L0events
 and bornonly are set to 1 internally.

3.4 Colored scalar mediator, t-channel exchange

An alternative set of simplified models exist where the mediator is exchanged in the t-channel, thereby coupling the quark and dark matter particle directly. Under the assumption that χ is a Standard Model (SM) singlet, the mediating particle, labeled ϕ , is necessarily charged and coloured. This model is parallel to, and partially motivated by, the squark of the MSSM, but in this case the χ is chosen to be Dirac. Following the example of Ref. [PVZ14], the interaction Lagrangian is written as

$$\mathcal{L}_{\text{int}} = g \sum_{i=1,2,3} (\phi_L^i \bar{Q}_L^i + \phi_{uR}^i \bar{u}_R^i + \phi_{dR}^i \bar{d}_R^i) \chi$$
 (3.23)

(Note: [PVZ14] uses only i = 1,2, but I think it's fine to extend this to 3 here.) where Q_L^i , u_R^i and d_R^i are the SM quarks and ϕ_L^i , ϕ_{uR}^i and ϕ_{dR}^i are the corresponding mediators, which (unlike the s-channel mediators) must be heavier than χ . These mediators have SM gauge representations under $(SU(3),SU(2))_Y$ of $(3,2)_{-1/6}$, $(3,1)_{2/3}$ and $(3,1)_{-1/3}$ respectively. Variations of the model previously studied include coupling to the left-handed quarks only [CEHL14, BDSJ+14], to the ϕ_{uR}^i [DNRT13] or ϕ_{dR}^i [PVZ14, A+14b], or some combination [BB13, AWZ14].

Minimal Flavour Violation (MFV) requires that the mediator masses for each flavour be equal; the same logic also applies to the couplings *g*. The available parameters are then

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$$\{m_{\chi}, M_{\phi}, g\}. \tag{3.24}$$

In practice, the third mediator mass and coupling could be separated from the other two, if higher order corrections to the MFV prediction arise due to the large top Yukawa coupling – a common variation is then to define this split between the first two generations and the third, so the parameters are extended to

$$\{m_{\chi}, M_{\phi_{1,2}}, M_{\phi_3}, g_{1,2}, g_3\}.$$
 (3.25)

The width of each mediator is expressed, using the example of decay to an up quark, as

$$\Gamma(\phi_i \to \bar{u}_i \chi) = \frac{g_i^2}{16\pi M_{\phi_i}^3} (M_{\phi_i}^2 - m_{u_i}^2 - m_{\chi}^2) \times \sqrt{M_{\phi_i}^4 + m_{u_i}^4 + m_{\chi}^4 - 2M_{\phi_i}^2 m_{u_i}^2 - 2M_{\phi_i}^2 m_{\chi}^2 - 2m_{u_i}^2 m_{\chi}^2},$$
(3.26)

367 this reduces to

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$$\frac{g_i^2 M_{\phi_i}}{16\pi} \left(1 - \frac{m_{\chi}^2}{M_{\phi_i}^2} \right)^2 \tag{3.27}$$

in the limit $M_{\phi_i}, m_\chi \gg m_{u_i}$.

An interesting point of difference with the s-channel simplified models is that the mediator can radiate a SM object, such as a jet or gauge boson, thus providing three separate mono-X diagrams which must be considered together in calculations. This model can also give a signal in the di-jet + MET channel when, for example, the χ is exchanged in the t-channel and the resulting ϕ pair each decay to a jet + χ .

Specific models for signatures with EW bosons

In this Section, we consider models with a photon, a W boson, a Z boson or a Higgs boson in the final state, accompanied by Dark Matter particles that either couple directly to the boson or are mediated by a new particle. The experimental signature is identified as V+MET.

These models are interesting both as extensions of models where the gluon provides the experimentally detectable signature, and as stand-alone models with final states that cannot be generated by the models in Section 3.

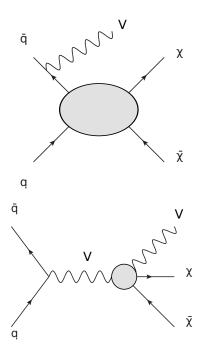


Figure 4.1: Sketch of benchmark models including a contact interaction for V+MET searches, adapted from [NCC⁺14].

The models considered can be divided in three categories:

Models including a contact operator, where the boson is radiated from the initial state

As depicted in the top diagram of Figure 4.1, these models follow

the nomenclature and theory for the EFT benchmarks commonly

used by MET+X searches [GIR⁺10]. These models have been used in past experimental searches [Kha14, Aad14b, K⁺14, Aad14b, A⁺14a, Aad14a], and they will not be described here.

Models including a contact operator, where the boson is directly coupled to DM
Shown in the bottom of Figure 4.1, these models allow for a contact interaction vertex that directly couples the boson to Dark
Matter.

Simplified models where the boson is radiated from the initial state These models follow those already described in Section 3, replacing the initial state gluon with a boson.

V-specific simplified models These models postulate direct couplings
 of new mediators to bosons, e.g. they couple the Higgs boson to a
 new scalar [CDM⁺14].

The following Sections describe the models within these categories, the parameters for each of the benchmark models chosen, the studies towards the choices of the parameters to be scanned, and finally point to the location of their Matrix Element implementation.

8 4.1 Simplified models with ISR boson radiation

Searches in the jet+MET final state are generally more sensitive with 409 respect to final states including bosons, due to the much larger rates 410 of signal events featuring quark or gluon radiation with respect to 411 radiation of bosons [ZBW13], in combination with the low branching 412 ratios if leptons from boson decays are required in the final state. The 413 rates for the Higgs boson radiation is too low for these models to be 414 considered a viable benchmark [CDM⁺14]. However, the presence of photons leptons from W and Z decays and W or Z bosons decaying 416 hadronically allows to reject the background more effectively, making 417 Z/gamma/W+MET searches still worth comparing with searches in the jet+MET final state.

4.1.1 Vector mediator exchanged in the s-channel

The case for searches with W bosons in the final state has so far been strenghtened by the presence of particular choices of couplings between the WIMP and the up and down quarks which enhance W radiation [BT13], in the case of the exchange of a vector mediator in the s-channel. Run-1 searches have considered three sample cases for the product of up and down quark couplings to the mediator $\tilde{\zeta}$:

• No couplings between mediator and either up or down quarks ($\xi = 0$);

- Same coupling between mediator and each of the quark types (ξ = 429 1); 430
- Coupling of opposite sign between mediator and each of the quark 431 types ($\xi = -1$).

The $\xi = -1$ case leads to a large increase in the cross-section of the process, and modifies the spectrum of missing transverse energy or 434 transverse mass used for the searches. The sensitivity of the W+MET 435 search for this benchmark in this case surpasses that of the jet+MET search. However, as shown in Ref. [BCD⁺15], the cross-section in-437 crease is due to the production of longitudinally polarized W bosons, 438 as a consequence of a violation of electroweak gauge symmetries. 439 Unless further particles are introduced (in a fashion similar to the Higgs boson in the Standard Model), choosing a value of $\xi = -1$ 441 for this simplified model will lead to a manifest violation of unitar-442 ity at LHC energies. The simplified model with a vector mediator exchanged in the s-channel model can still be considered as a benchmark for searches with a W boson if $\xi = 1$. We leave the study of 445 further models with cross-section enhancements due to different couplings to up and down quarks for studies beyond the early LHC searches covered in this document. An example of such model is the 448 case of both DM and SM Higgs charged under a new U(1)', with a a 449 small mass mixing between SM Z-boson and the new Zprime. This leads to different effective DM couplings to u_L and d_L , proportional 451 to their coupling to the Z boson, detailed in Appendix B.

The scan in the parameters that characterize this simplified model for EW boson + MET searches follow what already detailed in Section 3.

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As in the case of the jet+MET models, the width does not have a significant impact on the kinematic distributions relevant for those searches. An example of the particle-level analysis acceptance using the generator-level cuts from Ref. [Aad15] for the photon+MET analysis, but raising the photon p_T cut to 150 GeV is shown in Figure 4.2, comparing a width that is set to $\Gamma = M_{med}/3$ to the minimal width (the ratio between the two widths ranges from 1.05 to 1.5 with increasing mediator masses).

Examples of relevant kinematic distributions for selected benchmark points are shown in Fig. 4.9; leading-order cross-sections for the chosen benchmark points are shown in Table ?? [TODO: Insert table of cross-sections].

Colored scalar mediator exchanged in the t-channel

The model parameters with emission of an EW boson follow those in Section 3.

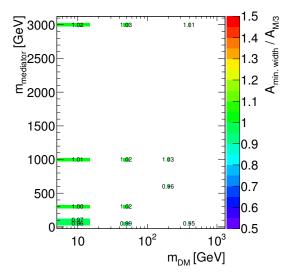


Figure 4.2: Analysis acceptance for the photon+MET analysis when varying the mediator width, in the case of a vector mediator exchanged in the s-channel

Figure 4.4 shows the MET distribution for the hadronic Z+MET final state, with varying dark matter and mediator mass, before any selection. The acceptance for a series of simplified analysis cuts (MET>350 GeV, leading jet $p_T >$ 40 GeV, minimum azimuthal angle between jet and MET > 0.4) applied at the generator level is shown in Figure 4.5.

The parameter scan is still under discussion.

4.1.3 Model implementation

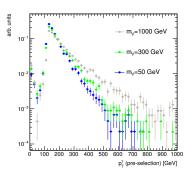
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These models are generated at leading order with MadGraph 2.2.2, and parameter cards can be found on SVN [TODO: Add SVN location]. The parton shower is done using Pythia 8, with a matching scale of... [TODO: To be completed.]

483 4.2 EFT models with direct DM-boson couplings

- [Linda Carpenter and Uli Haisch are rewriting this section. Changes expected:
- change of normalization and Lagrangians to be consistent with [CHH15], linked to notation of [CNS⁺13]
- description of dimension-5 EFTs
- addition of a dimension-5 simplified model]

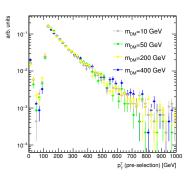
A complete list of effective operators with direct DM/boson couplings for Dirac DM, up to dimension 7, can be found in [CHLR13].



(a) Missing transverse momentum distribution for the photon+MET final state, for different mediator mass choices, for a DM mass of 10 GeV.

1/N dN/dE_T [GeV⁻¹] 0 0 0

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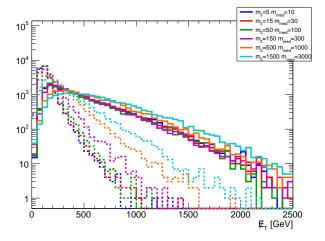


(b) Leading photon transverse momentum distribution for the photon+MET final state, for different DM mass choices, with a mediator mass of 1 TeV.



(c) Missing transverse momentum distribution for the leptonic Z+MET final state, for different mediator mass choices, for a DM mass of 15 GeV

(d) Transverse mass (m_T) for the leptonic W+MET final state.



(e) Missing transverse momentum distribution for the hadronic W+MET final state

Following the notation of [CNS⁺13], the dimension 5 benchmark models from this category have a Lagrangian that includes terms

Figure 4.3: Kinematic distributions relevant for searches with W, Z and photons in the final state, for the simplified model with a vector mediator exchanged in the s-channel.

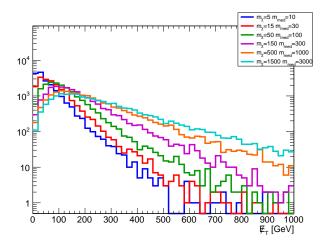


Figure 4.4: Missing transverse momentum distribution for the hadronic Z+MET final state, for the simplified model with a colored scalar mediator exchanged in the t-channel.

t-scalar model acceptance

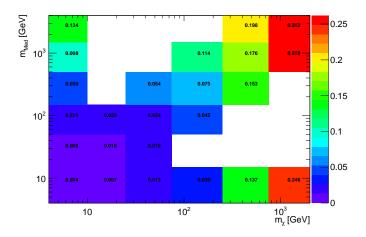


Figure 4.5: Acceptance table for the hadronic Z+MET final state, for the simplified model with a colored scalar mediator exchanged in the *t*-channel.

94 such as:

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$$\frac{m_W^2}{\Lambda_5^3} \bar{\chi} \chi W^{+\mu} W_{\mu}^- + \frac{m_Z^2}{2\Lambda_5^3} \bar{\chi} \chi Z^{\mu} Z_{\mu} . \tag{4.1}$$

where m_Z and m_W are the masses of the Z and W boson, W^μ and Z^μ are the fields of the gauge bosons, χ denote the Dark Matter fields and Λ_5 is the effective field theory scale. This operator induces signatures with MET in conjunction with Z and W bosons at tree level, while at loop level it induces couplings to photon pairs and $Z\gamma$ through W loops. [TODO: Ask Linda to explain this better than I did.]. In these models, a clear relation exists between final states with photons, EW bosons and Higgs boson. [TODO: see if mono-Higgs

studies exist for these operators, include them here].

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The dimension 7 benchmark models include couplings to the kinetic terms of the EW bosons ($F_i^{\mu\nu}$, with $F_i=1,2,3$ being the field strengths of the SM U(1) and SU(2) gauge groups and $\tilde{F}_i^{\mu\nu}$ their dual tensors). The Lagrangian for the scalar coupling of DM and bosons include terms such as the following:

$$\frac{1}{\Lambda_{7,S}^3} \bar{\chi} \chi \sum_{i} k_i F_i^{\mu\nu} F_{\mu\nu}^i + \frac{1}{\Lambda_{7,S}^3} \bar{\chi} \chi \sum_{i} k_i F_i^{\mu\nu} \tilde{F}_{\mu\nu}^i$$
 (4.2)

The Lagrangian with pseudoscalar coupling includes the following terms:

$$\frac{1}{\Lambda_{7,PS}^3} \bar{\chi} \gamma^5 \chi \sum_{i} k_i F_i^{\mu\nu} F_{\mu\nu}^i + \frac{1}{\Lambda_{7,PS}^3} \bar{\chi} \gamma^5 \chi \sum_{i} k_i F_i^{\mu\nu} \tilde{F}_{\mu\nu}^i$$
 (4.3)

The cut-off scales Λ for the separate terms can be related to operators with different Lorentz structure from Ref. [CHLR13]. Given that they do not lead to substantial differences for collider searches as shown in Figure 2 of Ref. [CNS⁺13], they have been denoted as $\Lambda_{7,S}$ for the scalar case and $\Lambda_{7,PS}$ for the pseudoscalar case.

The k_i coefficients for the dimension 7 models are related to the couplings of DM to pairs of gauge bosons by gauge invariance:

$$g_{WW} = \frac{2k_2}{s_{vv}^2 \Lambda_7^3} \tag{4.4}$$

$$g_{ZZ} = \frac{1}{4s_w^2 \Lambda_7^3} \left(\frac{k_1 s_w^2}{c_w^2} + \frac{k_2 c_w^2}{s_w^2} \right) \tag{4.5}$$

$$g_{\gamma\gamma} = \frac{1}{4c_w^2} \frac{k_1 + k_2}{\Lambda_7^3} \tag{4.6}$$

$$g_{Z\gamma} = \frac{1}{2s_w c_w \Lambda_7^3} \left(\frac{k_2}{s_w^2} - \frac{k_1}{c_w^2} \right)$$
 (4.7)

where s_w and c_w are respectively the sine and cosine of the weak mixing angle.

The coefficients k_i determine the relative importance of each of the boson channels, and their correlations. For example, for what concerns searches with W, Z and photons:

- k_2 alone controls the rate of the coupling to W boson pairs;
- If $k_1 = k_2$ contributions from both Z and γ exchange appear;
- If $k_1 = c_w^2/s_w^2 k_2$ the γ exchange is negligible.

The coefficients k_1 and k_2 are related to the coefficients c_1 and c_2 in the equivalent models of Ref. [CHH15] as $k_2 = s_w^2 * c_2$ and $c_2 = c_w^2 * c_1$.

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[TODO: Linda will possibly complete/correct this subsection]

UV completions of such operators where the dominant signature is a single photon or EW boson are possible, for example through the exchange of a W' or a Z'. They are left as benchmarks for future searches as their implementation may require loop diagrams and need further studies beyond the timescale of this Forum.

As shown in Fig. 4.6 kinematics of this model can be approximated by that of a simplified model including a high-mass scalar mediator exchanged in the s-channel. For this reason, the list of benchmark models with direct boson-DM couplings only includes dimension 7 operators.

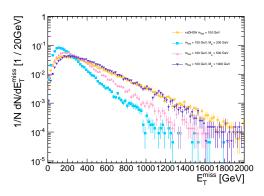


Figure 4.6: Comparison of the missing transverse momentum for the simplified model where a scalar mediator is exchanged in the s-channel and the model including a dimension-5 scalar contact operator, in the leptonic Z+MET final state

The kinematic distributions for dimension-7 scalar and pseudoscalar operators only shows small differences, as shown in Fig. 4.7.



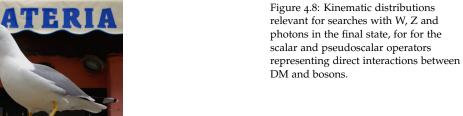
Figure 4.7: Comparison of the missing transverse momentum for the scalar and pseudoscalar operators with direct interaction between DM and photon, in the photon+MET final state

Similarly, the differences in kinematics for the various signatures are negligible when changing the coefficients k_1 and k_2 , as shown in Figure ??. Only the case $k_1 = k_2 = 1$ is generated as benchmark; other cases are left for reinterpretation as they will only need a rescaling of the cross-sections shown in Table ?? [TODO: add tables with cross sections] for the various Dark Matter mass points considered.

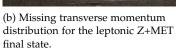
Examples of relevant kinematic distributions for selected benchmark points are shown in Fig. 4.9.



(a) Missing transverse momentum distribution for the photon+MET final









(c) Transverse mass (m_T) for the leptonic W+MET final state.

4.2.1 Specific simplified models

Mono-Higgs, to be completed...



(a) Missing transverse momentum distribution for the photon+MET final state.

Figure 4.9: Kinematic distributions relevant for searches with W, Z and photons in the final state, for the simplified model with a vector mediator exchanged in the s-channel.



(b) Missing transverse momentum distribution for the leptonic Z+MET final state.



(c) Transverse mass (m_T) for the leptonic W+MET final state.



(d) Fat [Insert algorithm] jet mass (m_T) for the the hadronic W+MET final state.

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Specific models for signatures with heavy flavor quarks

- bb+MET models 5.1
- Models with a single b-quark + MET
- tī+MET models

As described in Section 3.2, one of the most simple UV complete extension of the effective field theory approach is the addition of a scalar mediator between DM and SM. A gauge singlet mediator can have tree-level interactions with a singlet DM particle that is either a Dirac or Majorana fermion, or DM that is a scalar itself. The spin-0 mediator can either be a real or complex scalar; a complex scalar contains both scalar and pseudoscalar particles, whereas the real 563 field only contains the scalar particle. In this document we consider only two of the possible choices for this simplified model: one where the interaction with the SM is mediated by a real scalar, and the second where we consider only a light pseudoscalar, assuming that 567 the associated scalar is decoupled from the low-energy spectrum. The kinematics of the two cases is sufficiently different to suggest that further investigation of the complex scalar case is needed but left for 570 future studies.

Couplings to the SM fermions can be arranged by mixing with the SM Higgs. Such models have interesting connections with Higgs 573 physics, and can be viewed as generalizations of the Higgs portal to DM. The most general scalar mediator models will have renormalizable interactions between the SM Higgs and the new scalar ϕ or pseudoscalar a, as well as ϕ/a interactions with electroweak gauge bosons. Such interactions are model dependent, often subject to constraints from electroweak precision tests, and would suggest specialized searches which cannot be generalized to a broad class of models (unlike, for instance, the E_T + jets searches). As a result, for this class of minimal simplified models with spin-0 mediators, we will focus primarily on couplings to fermions and loop-induced couplings to

gluons. Possible couplings to the electroweak sector may also lead to interesting DM phenomenology that can be studied in the context of Higgs Portal DM.

5.3.1 Model and assumption for fermionic DM

Minimal Flavor Violation (MFV) implies that scalar couplings to fermions will be proportional to the fermion mass. However, they can differ for up- and down-type quarks and for charged leptons.

Following the assumption that DM is a fermion χ , which couples to the SM only through a scalar ϕ or pseudoscalar a, the most general tree-level Lagrangians compatible with the MFV assumption are [? ?]:

$$\mathcal{L}_{\text{fermion},\phi} = \mathcal{L}_{\text{SM}} + i\bar{\chi}\partial\chi + m_{\chi}\bar{\chi}\chi + \left|\partial_{\mu}\phi\right|^{2} + \frac{1}{2}m_{\phi}^{2}\phi^{2} + g_{\chi}\phi\bar{\chi}\chi + \frac{\phi}{\sqrt{2}}\sum_{i}\left(g_{u}y_{i}^{u}\bar{u}_{i}u_{i} + g_{d}y_{i}^{d}\bar{d}_{i}d_{i} + g_{\ell}y_{i}^{\ell}\bar{\ell}_{i}\ell_{i}\right), \tag{5.1}$$

$$\mathcal{L}_{\text{fermion},a} = \mathcal{L}_{\text{SM}} + i\bar{\chi}\partial\chi + m_{\chi}\bar{\chi}\chi + \left|\partial_{\mu}a\right|^{2} + \frac{1}{2}m_{a}^{2}a^{2} + ig_{\chi}a\bar{\chi}\gamma_{5}\chi + \frac{ia}{\sqrt{2}}\sum_{i}\left(g_{u}y_{i}^{u}\bar{u}_{i}\gamma_{5}u_{i} + g_{d}y_{i}^{d}\bar{d}_{i}\gamma_{5}d_{i} + g_{\ell}y_{i}^{\ell}\bar{\ell}_{i}\gamma_{5}\ell_{5}\right) \tag{5.2}$$

Here the sums run over the all SM generations; the Yukawa couplings y_i^f are normalized to $y_i^f = \sqrt{2} m_i^f / v$ where $v \simeq 246\,\mathrm{GeV}$ represents the Higgs vacuum expectation value (VEV). We parametrise the DM-mediator coupling as g_χ , without any additional Yukawa structure between the mediator and the dark sector.

The most general Lagrangians including new scalars or pseudoscalars will have a potential containing interactions with the SM Higgs field h. As already stated we only choose a minimal set of interactions that do not include interactions with the Higgs field. Given this simplification, the minimal set of parameters under consideration in

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$$\left\{m_{\chi}, m_{\phi/a}, g_{\chi}, g_{u}, g_{d}, g_{\ell}\right\}. \tag{5.3}$$

The simplest choice of couplings, known as Minimal Simplified Dark Matter model (MSDM) **[TODO: add references]**, is $g_u = g_d = g_\ell$, which is realized in singlet scalar extensions of the SM.

Extending the SM Higgs sector to a two Higgs doublet model implies more complex couplings such as $g_u = \cot \beta$ and $g_d = g_e = \tan \beta$ where $\tan \beta$ denotes the ratio of VEVs of the two Higgs doublets. The case $g_u \neq g_d \neq g_\ell$ requires more additional scalars with potentially large masses, and it is not covered here: for simplicity, we assume universal SM-mediator couplings $g_v = g_u = g_d = g_\ell$ in the remainder of this work.

The expected signal of DM pair production depends on the production rate defined by the dark matter mass m_{χ} , mediator $m_{\phi/a}$, on the couplings g_i and on the branching ration defined by the total decay width of the mediator ϕ/a . We calculate the minimum possible width (assuming only decays into the dark matter and the Standard Model fermions) that is consistent with a given value of $g_{\chi}g_{\rm SM}$. These are given by Eq. (5.4) [BFG15].

$$\Gamma_{\phi,a} = \sum_{f} N_{c} \frac{y_{f}^{2} g_{v}^{2} m_{\phi,a}}{16\pi} \left(1 - \frac{4m_{f}^{2}}{m_{\phi,a}^{2}} \right)^{3/2} + \frac{g_{\chi}^{2} m_{\phi,a}}{8\pi} \left(1 - \frac{4m_{\chi}^{2}}{m_{\phi,a}^{2}} \right)^{3/2} + \frac{\alpha_{s}^{2} y_{t}^{2} g_{v}^{2} m_{\phi,a}^{3}}{32\pi^{3} v^{2}} \left| f_{\phi,a} \left(\frac{4m_{t}^{2}}{m_{\phi,a}^{2}} \right) \right|^{2}$$
(5.4)

where

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$$f_{\phi}(\tau) = \tau \left[1 + (1 - \tau) \operatorname{arctan}^2 \left(\frac{1}{\sqrt{\tau - 1}} \right) \right], \qquad f_a(\tau) = \tau \operatorname{arctan}^2 \left(\frac{1}{\sqrt{\tau - 1}} \right).$$
(5.5)

The first term in each width corresponds to the decay into SM 624 fermions, and the sum runs over all kinematically available fermions, $N_c = 3$ for quarks and $N_c = 1$ for leptons. The second term is the 626 decay into DM, assuming that is kinematically allowed. The factor 627 of two between the decay into SM fermions and into DM is a result of our choice of normalization of the Yukawa couplings due to spin dependencies. The last two terms correspond to decay into gluons. 630 Since we have assumed that $g_v = g_u = g_d = g_\ell$, we have included in 631 the partial decay widths $\Gamma(\phi/a \to gg)$ only the contributions stemming from top loops, which provide the by far largest corrections 633 given that $y_t \gg y_b$ etc. At the loop level the mediators can decay not 634 only to gluons but also to pairs of photons and other final states if kinematical accessible. However the decay rates $\Gamma(\phi/a \rightarrow gg)$ are always larger than the other loop-induced partial widths, and in con-637 sequence the total decay widths $\Gamma_{\phi/a}$ are well approximated by the 638 corresponding sum of the individual partial decay widths involving DM, fermion or gluon pairs. It should be noted that if $m_{\phi/a} > 2m_t$ 640 the total widths of ϕ/a will typically be dominated by the partial widths to top quarks.

5.3.2 Parameter scan

As discussed in Sec. ??, the MFV assumption for spin-0 mediators leads to quark mass dependent Yukawa couplings, and therefore dominant couplings to top quarks. This motivates dedicated DM+ $t\bar{t}$ searches. The benchmark chosen for these searches follows the assumptions mentioned in the previous Section: we consider a Dirac

fermion DM particle, universal couplings to quarks, and minimum mediator width.

The benchmark points scanning the model parameters have been selected to ensure that the kinematic features of the parameter space are sufficiently represented. Detailed studies were performed to identify points in the m_χ , $m_{\phi,a}$, g_χ , g_v (and $\Gamma_{\phi,a}$) parameter space that differ significantly from each other in terms of expected detector acceptance. Because missing transverse momentum is the key observable for searches, the mediator p_T spectra is taken to represent the main kinematics of a model. Another consideration in determining the set of benchmarks is to focus on the phase space where we expect the searches to be sensitive during the 2015 LHC run. Based on a projected integrated luminosity of 30 fb⁻¹ expected for 2015, we disregard model points with a cross section times branching ratio smaller than 0.1 fb.

5.3.3 Parameter scan

The kinematics is most dependent on the masses m_{χ} and $m_{\phi,a}$. Figure 5.1 and 5.2 show typical dependencies for for scalar and pseudoscalar couplings respectively.

The two relevant thresholds that are observed for the variation in the kinematic spectra are $m_{\phi,a}=2m_\chi$ and $m_{\phi,a}=2m_t$. When the mediator mass exceeds both these thresholds then the p_T spectra broadens with larger $m_{\phi,a}$ and the kinematics for ϕ and a are comparable. The mediator p_T spectra changes significantly when crossing these thresholds. In particular, the kinematics are different for an on-shell mediator compared to an off-shell mediator ($m_{\phi,a}<2m_\chi$). Furthermore, the scalar case differs from the pseudoscalar one when $m_\phi<2m_t$. Therefore, it is important to have benchmark points covering both sides of these thresholds with sufficient granularity.

Typically only weak dependencies on width or equivalently couplings are observed (see Fig 5.4), except for large mediator masses of ~ 1.5 TeV or for very small couplings of $\sim 10^{-2}$. These regimes where width effects are significant have production cross sections that are too small to be relevant for 30 fb⁻¹ and are not considered here. However, with the full Run-2 dataset, such models may be within reach. The weak dependence on the typical width values can be understood as the parton distribution function are the dominant effect on mediator production. In other words, for couplings $\sim O(1)$ the width is large enough that the p_T of the mediator is determined mainly by the PDF.

Another case where the width can impact the kinematics is when $m_{\phi,a}$ is slightly larger than $2m_{\chi}$. Here, the width determines the rel-

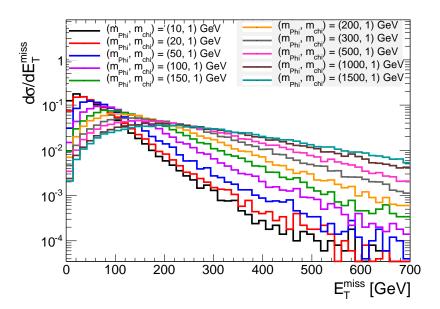


Figure 5.1: Example of the dependence of the kinematics on the scalar mediator mass. The Dark Matter mass is fixed to be 1GeV.

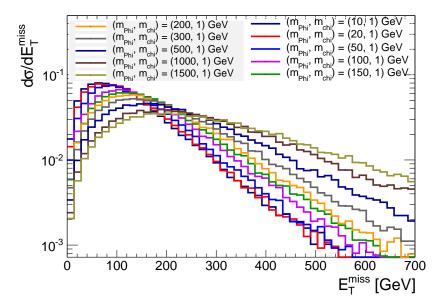


Figure 5.2: Example of the dependence of the kinematics on the pseudoscalar mediator mass. The Dark Matter mass is fixed to be 1GeV.

ative contribution between on-shell and off-shell production. An example is given in Fig. 5.5. In our recommendations we propose to 692 use for semplicity the minimal width, as this is represents the most 693 conservative choice to interpret the LHC results. [TODO: mention

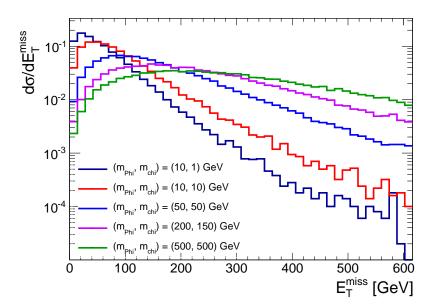


Figure 5.3: Example of the dependence of the kinematic for points of the grid proposed in Tab. ?? close to the $m_{\phi,a} \sim 2m_\chi$ limit.3

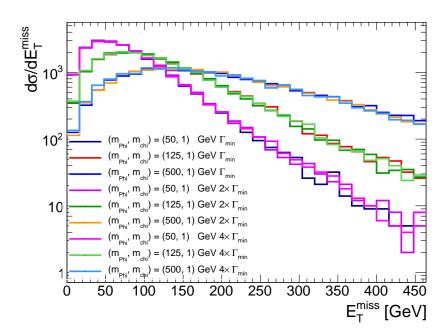


Figure 5.4: Study of the dependence of kinematics on the width of a scalar mediator. The width is increased up to four times the minimal width for each mediator and dark matter mass combination.

695 larger widths too]

Given that the kinematics are similar for all couplings $\sim O(1)$, we recommend to generate only samples with $g_{\chi}=g_v=1$. It follows

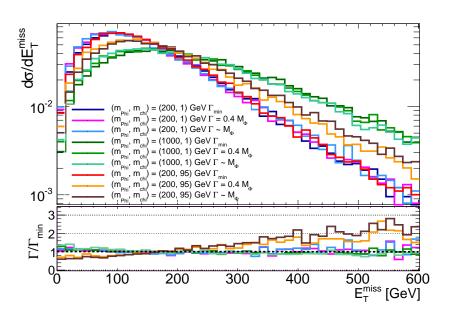


Figure 5.5: Dependence of the dependence of kinematics on the width of a scalar mediator. The width is increased up to the mediator mass. Choices of mediator and dark matter masses such that $m_{\phi,a}$ is slightly larger than $2m_\chi$ is the only case that shows a sizeable variation of the kinematics as a function of the width.

from this that these benchmark points should be a good approximation for non-unity couplings and for $g_\chi \neq g_v$, provided that the sample is rescaled to the appropriate cross section times branching ratio. While a simple scaling function **[CD: which?]** is sufficient for a limited range of coupling values (see Fig. 5.6 for example), we also choose to provide instead a table of cross section times branching ratio values over a large range of couplings to support interpretation of search results (see the Appendix C). The table lists couplings from g=0.1 to g=3.5, where the upper limit is chosen to close to the perturbative limit.

The points for the parameter scan chosen for this model are listed in Table ??, chosen to be harmonized with those for other analyses employing the same scalar model as benchmark. In addition to the considerations discussed in the preceding subsections, very light DM fermions are included ($m_{\chi}=10\,\text{GeV}$) as this is a region where colliders have a complementary sensitivity to current direct detection experiments.

5.4 *Models with a single top—quark + MET*

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[TODO: find a consistent notation for Xnew, M, V and Madgraph model]

A dark matter candidate χ and a new particle M (vector or scalar) are added to the SM, in an effective theory that respects the SU(2)_L ×



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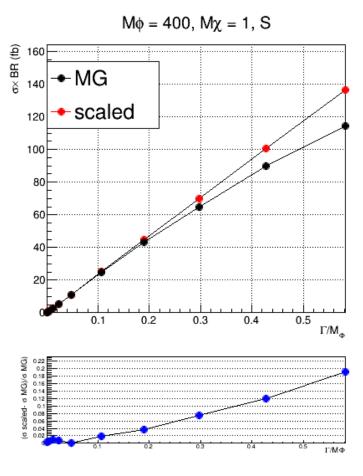


Figure 5.6: An example comparing a simple cross section scaling versus the computation from the generator, for a scalar model with $m_{\phi}=400\,\text{GeV}$ and $m_{\chi}=1\,\text{GeV}$. In this example, the scaling relationship holds for Γ_{ϕ}/m_{ϕ} below 0.2, beyond which finite width effects become important and the simple scaling breaks down.

 $U(1)_Y$ symmetry and produces a single top quark in association with either the DM particle or the new particle (generally called X_{new} when no distinction is made). The full details of these models are described in [AFM11, AAB⁺14, BCDF15].

There are two classes of models based on the monotop production mode: resonant and non-resonant production, as shown in Fig. 5.7.

The following two sections describe the phenomenology leading to these two production mechanisms. Depending on the nature of X_{new} , two main final states might be relevant: monotop production or same-sign top quark pair production. The interplay of these two signatures can largely probe this class of dark matter model, but a detailed study of their complementarity is beyond the scope of this Forum report.

RESONANT PRODUCTION

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In this case, the new particle M is a couloured 2/3-charged scalar ϕ^{\pm} decaying into a top quark and a spin-1/2 invisible particle, χ (in this case X_{new} is the dark matter candidate χ). The dynamics of the new sector is then described by the following Lagrangian:

$$\mathcal{L} = d_i^C \left[(g_{\phi d}^v)^{ij} + (g_{\phi d}^a)^{ij} \gamma^5 \right] d_j \phi^{\pm} + u_k^C \left[(g_{u\chi}^v)^k + (g_{u\chi}^a)^k \gamma^5 \right] \chi \phi^{\pm} \quad (5.6)$$

where u (d) stands for any up-quark (down-quark), the index v (a) stands for vectorial (axial), C means charge conjugate and i, j, k run over the generations (color indices involved in the ϕ^{\pm} -quarks interaction are not explicitly written). The first term leads to the production of the new particle and the last term allows its decay into a up-quark and a non interacting fermion (in particular to the top quark when $(g_{u\chi}^{v/a})^k$ is sizable mainly for k=3). This model is then described by the masses of the new particle m_{ϕ} and the invisible fermion m_{χ} , and the coupling $(g_{\phi d}^{v/a})^{ij}$ and $(g_{u\chi}^{v/a})^k$.

Non-Resonant production

For the non-resonant production, the top quark is produced in association with the new particle (X_{new} is then the new particle and not the dark matter candidate). The new particle can be either a new scalar, interacting with the SM and the DM candidate, or a new vector. For simplicity, we only consider the case of a vector new particle, as the scalar case would involve a mixing with the SM Higgs boson and therefore a larger parameter space.

The dynamics of a case with a vector new particle follows this Lagrangian:

$$\mathcal{L} = \bar{u}_i [(g_{Vu}^v)^{ij} \gamma^\mu + (g_{Vu}^a)^{ij} \gamma^5] u_i V_\mu + \bar{\chi} [g_{Vu}^v \gamma^\mu + g_{Vx}^a \gamma^5] \chi V_\mu$$
 (5.7)

where u stands for any up-quark, the index v (a) stands for vectorial (axial) and i, j, k run over the generations. The first term describes the interaction between the new particle and the up-quarks while the second term leads to the decay the new particle into invisible fermions. The new sector can be defined with the couplings $(g_{Vu}^{v/a})^{ij}$, $g_{V\chi}^{a/v}$ and the masses m_V and m_χ . This model can be probed by two different experimental signatures: monotop and same-sign top quark production.

Figure 5.7: Feynman diagram of leading order processes leading to monotop events: resonant production of t via resonant new particle M decaying into a top quark and $X_{\rm new}$, which is the dark matter fermion χ (left), and s and t channel non-resonant production of a top quark in association with $X_{\rm new}$, which is the new particle M (middle and right).

Model parameters and assumptions

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The models considered as benchmarks for the first LHC searches contain further assumptions in terms of the flavour and chiral structure of the model with respect to the full Lagrangians from equations (5.6) and (5.7). These assumptions lead to limitations in LHC constraints of the parameter space of these models, qualitatively discussed below.

Assumptions in the flavour structure of the models In order to be visible at the LHC in the monotop final state, these models must include a 771 strong coupling between the new particle ϕ and $t\chi$. In the resonant case, the new particle must also couple to light quarks in order to 773 be produced at the LHC, leading to possible constraints from dijet 774 searches. The same kind of assumption exists for the non-resonant 775 production. The new particle M must be produced from a light quark in the initial state, in association with a top quark: this sig-777 nature can mainly probe a high coupling $\left(g_{Vu}^{v/a}\right)_{Vu}^{13} \equiv g_{Vtu}^{v/a}$. Therefore, the sensitivity to other flavour couplings is significantly lower, since V would be produced at a lower rate.

Assumptions in the chiral structure of the models We only consider right-handed quark components, in order to simplify the phenomenology. The representation of the left-handed components under the $SU(2)_L$ symmetry would a coupling to *down*-type quarks, since the effective theory is invariant under $SU(2)_L \times U(1)_Y$ gauge symmetry. Having a coupling between the new particle and *down*-type quarks complicates the collider phenomenology in terms of decay modes. Typically, including the left-handed components of quarks in the lagrangian (5.7) describing the Vtu vertex would lead to

$$\mathcal{L}_{Vtu} = g_{Vtu}^{R} \, \bar{t}_{R} \gamma^{\mu} u_{R} \, V_{\mu} + g_{Vtu}^{L} (\bar{t}_{L} \gamma^{\mu} u_{L} + \bar{b}_{L} \gamma^{\mu} d_{L}) \, V_{\mu}$$
 (5.8)

where $g^{R/L} \equiv 1/2 (g^v \pm g^a)$ couples only to right-handed/lefthanded components. The second term stems from invariance under SU(2)_L rotations, and leads to an additional decay mode $V \to b\bar{d} + \bar{b}d$ (on top of $V \to t\bar{u} + \bar{t}u$ and $V \to \chi\chi$). [Open point: do we just set the 2nd term to zero in this model? Justification?]

IMPLEMENTATION AND NOTATION

the experimental searches are described below.

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This Section describes the notations used in the MadGraph model [Fuk] convention, in term of the ones introduced in the previous Section.

The Madgraph model corresponds to the Lagrangian from [AFM11].

Each coupling constant of this dynamics can be set via the paramater card and the blocks which are relevant for the two models used for

- 1. Resonant scalar model described by the Lagrangian (5.6)
- AQS and BQS: 3×3 matrices (flavour space) fixing the coupling of the scalar ϕ^{\pm} (S stands for scalar) and down-type quarks (Q stands for quarks), written in this note $g_{\phi u}$ or $a_{\rm res}^q$.
 - A12S and B12S: 3×1 matrices (flavour space) fixing the coupling of the fermion χ (12 stands for spin-1/2 fermion) and up-type quarks, written in this note $g_{u\chi}$ or $a_{\rm res}^{1/2}$.
 - particle name: the scalar ϕ^{\pm} is labelled S and the fermion χ is f_{met}
- 2. Non-resonant vectorial model described by the Lagrangian (5.7)
- A1FC and B1FC: 3×3 matrices (flavour space) fixing the coupling of the vector V (1 stands for vector) and up-type quarks, written in this note g_{Vu} or $a_{\text{non-res}}$.
 - particle name: the vector V is labelled v_{met} and the fermion χ doesn't exist
 - the dark matter candidate χ is not implemented (this model assumes BR($V \to \chi \chi$) = 100%)

A means vectorial coupling (g^v) and B means axial coupling (g^a) and these two matrices are taken to be equal according to the chiral assumptions made above. The convention adopted follows [ATL15] in defining a single number $a_{\rm res}$ $(a_{\rm non-res})$ for the resonant (non resonant) model, such as $(a_{\rm res}^q)_{12}=(a_{\rm res}^q)_{21}=(a_{\rm res}^{1/2})_3\equiv a_{\rm res}$ (in order to have d-s-S couplings, and $t-S-f_{met}$ couplings) and $(a_{\rm non-res})_{13}=(a_{\rm non-res})_{31}\equiv a_{\rm non-res}$ (in order to have $v_{met}-t-u$ couplings).

8 PARAMETER SCAN

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[Open point - parameter scan studies go here.]

Which parameters impact the kinematics (this is the only relevant aspect form the experimental point of view)? Some studies would be nice to put in this documents about:

- mediator mass
- mediator width: no effect (or parametrizable effects, plots are
 ready and need to be included)
- which parameters impact our experimental sensitivity? Which plane should be scanned?
- What are the relevant numerical range to explore? First guess would be to follow the mono-top analysis.

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PARAMETER CHOICES AND CROSS SECTIONS

[Open point: update with new numbers]

ATLAS has considered two models, a resonant and a non-resonant production, using only right-handed top quarks in the lepton+jets final state. The signal samples were produced with MADGRAPH5 v1.5.11 interfaced with Pythia 8.175, using the MSTW2008LO Parton Distribution Function (PDF) set (lhapdf ID: 21000). The mass of the top quark was set at 172.5 GeV. Dynamic renormalisation and factorisation scales were used. The *MET* particle mass was varied, and in the case of the resonant model the resonance mass was fixed at 500 GeV:

- Resonant model, MET particle mass: [0,100] GeV in 20 GeV steps
- Non-resonant model, MET particle mass: [0,150] GeV in 25 GeV steps, [200,300] GeV in 50 GeV and [400,1000] GeV in 100 GeV steps

The couplings $a_{\rm res}$ and $a_{\rm non-res}$ are set at a fixed value of 0.2. In addition, two samples are produced for the resonant model for $m(f_{\rm met})=100$ GeV, with coupling strengths fixed at $a_{\rm res}=0.5$ and $a_{\rm res}=1.0$, in order to check the effect of the resonance width on the signal event kinematics. The total width of the resonance varies quadratically with the coupling strength, corresponding to a width of 3.5 GeV, 21.6 GeV, and 86.5 GeV at $a_{\rm res}=0.2$, $a_{\rm res}=0.5$, and $a_{\rm res}=1.0$, respectively.

The number of free parameters is reduced by assuming $(a_{\rm res}^q)_{12} = (a_{\rm res}^q)_{21} = (a_{\rm res}^{1/2})_3 \equiv a_{\rm res}$ for the resonant model and $(a_{\rm non-res})_{13} = (a_{\rm non-res})_{31} \equiv a_{\rm non-res}$ for the non-resonant model, all other elements of these coupling matrices being equal to o. For each model, the coupling parameter $a_{\rm res}$ or $a_{\rm non-res}$ and the masses of the exotic particles are independent.

The cross-sections as well as the width of the resonance for the resonance model are shown in Table 5.1. The cross-section is slowly decreasing when $m(f_{met})$ increases, and the values do not differ by larger than 10%, due to the similarity of the kinematics, in the chosen mass range.

For the non-resonant case, the cross-sections are given in Table 5.2 and are calculated with $a_{\rm non-res}=0.2$. The cross-section diverges when $m(v_{met})$ tends to o GeV. However, when the mass is exactly o GeV the cross-section has a finite value, due to the specificity of the propagator for this massless spin-1 boson.

[Open point: systematic uncertainties]

$m(f_{met})$ [GeV]	σ_{lep} [pb]	σ_{had} [pb]	Γ(Φ) [GeV]
0	1.107	2.214	3.492
20	1.102	2.205	3.491
40	1.089	2.180	3.487
60	1.068	2.137	3.481
80	1.039	2.078	3.472
100	1.001	2.003	3.461
100 ($a_{\rm res} = 0.5$)	6.091	12.13	21.63
100 ($a_{\rm res} = 1.0$	21.77	43.72	86.52

Table 5.1: Theoretical predictions for the product of the production crosssection of the scalar resonance, the branching ratio of its decay into a top quark and the invisible particle, and of the branching ratio of the top quark decay into a semi-leptonic (σ_{lep}) or fully-hadronic (σ_{had}) final state, in the resonance model. Values are given for a resonance of mass 500 GeV and for an effective coupling $a_{\rm res}=0.2$ (except for two masses), as a function of the mass $m(f_{met})$ of the neutral fermion. The total widths $\Gamma(\Phi)$ of the resonance are also shown.

$m(v_{met})$ [GeV]	σ_{lep} [pb]	σ_{had} [pb]
0	96.03	192.4
25	359.0	717.9
50	113.4	226.9
75	59.86	119.5
100	37.45	74.82
125	25.35	50.68
150	18.00	35.96
200	9.662	19.28
250	5.506	11.02
300	3.328	6.656
400	1.372	2.738
500	0.6345	1.270
600	0.3192	0.6354
700	0.1698	0.3383
800	0.09417	0.1883
900	0.05472	0.1091
1000	0.03259	0.06479

Table 5.2: Theoretical predictions for the product of the production cross-section of the invisible vector v_{met} and of a top quark, and of the branching ratio of the top quark decay into a semi-leptonic (σ_{lep}) or fully-hadronic (σ_{had}) final state, in the non-resonance model. Values are given for an effective coupling $a_{\text{non-res}} = 0.2$, as a function of the mass $m(v_{met})$ of the invisible state.

Validity of EFT approach

Effective Field Theories (EFTs) are an extremely useful tool for DM searches at the LHC. Given the current lack of indications about the nature of the DM particle and its interactions, a model independent 874 interpretation of the collider bounds appears mandatory, especially 875 in complementarity with the reinterpretation of the exclusion limits within a choice of simplified models, which cannot exhaust the set 877 of possible completions of an effective Lagrangian. However EFTs 878 must be used with caution at LHC energies, where the energy scale of the interaction is at a scale where the EFT approximation can no longer be assumed to be valid. Here we summarise some methods that can be used to ensure the validity of the EFT approximation. These methods are described in detail in Refs. [BDSMR14?, BDSJ+14, A^{+} 15, RWZ15].

Outline of the procedure described in Refs. [? A^+ 15]

For a tree-level interaction between DM and the Standard Model (SM) via some mediator with mass M, the EFT approximation corresponds to expanding the propagator in powers of $Q_{\rm tr}^2/M^2$, truncating at lowest order, and combining the remaining parameters into a single parameter M_* (also called Λ). For an example scenario with a Z'-type mediator (leading to some combination of operators D5 to D8 in the EFT limit) this corresponds to setting

$$\frac{g_{\text{DM}}g_q}{Q_{\text{tr}}^2 - M^2} = -\frac{g_{\text{DM}}g_q}{M^2} \left(1 + \frac{Q_{\text{tr}}^2}{M^2} + \mathcal{O}\left(\frac{Q_{\text{tr}}^4}{M^4}\right) \right) \simeq -\frac{1}{M_*^2}, \tag{6.1}$$

where $Q_{\rm tr}$ is the momentum carried by the mediator, and $g_{\rm DM}$, g_q are the DM-mediator and quark-mediator couplings respectively. Similar expressions exist for other operators. Clearly the condition that must be satisfied for this approximation to be valid is that $Q_{\rm tr}^2 < M^2 = g_{\rm DM} g_q M_*^2$.

We can use this condition to enforce the validity of the EFT approximation by restricting the signal (after the imposition of the cuts

of the analysis) to events for which $Q_{\rm tr}^2 < M^2$. This truncated signal can then be used to derive the new, truncated limit on M_* as a function of $(m_{\rm DM}, g_{\rm DM} g_g)$.

For the example D5-like operator, $\sigma \propto {M_*}^{-4}$, and so there is a simple rule for converting a rescaled cross section into a rescaled constraint on M_* if the original limit is based on a simple cut-and-count procedure. Defining $\sigma_{\rm EFT}^{\rm cut}$ as the cross section truncated such that all events pass the condition $\sqrt{g_{\rm DM}g_q}M_*^{\rm rescaled} > Q_{\rm tr}$, we have

$$M_*^{\text{rescaled}} = \left(\frac{\sigma_{\text{EFT}}}{\sigma_{\text{EFT}}^{\text{cut}}}\right)^{1/4} M_*^{\text{original}},$$
 (6.2)

which can be solved for $M_*^{\rm rescaled}$ via either iteration or a scan (note that $M_*^{\rm rescaled}$ appears on both the LHS and RHS of the equation). Similar relations exist for a given UV completion of each operator. The details and application of this procedure to ATLAS results can be found in Ref. [A⁺15] for a range of operators. Since this method uses the physical couplings and energy scale $Q_{\rm tr}$, it gives the strongest possible constraints in the EFT limit while remaining robust by ensuring the validity of the EFT approximation.

outline of the procedure described in Ref. [RWZ15]

In [RWZ15] a procedure to extract model independent and consistent bounds within the EFT is described. This procedure can be applied to any effective Lagrangian describing the interactions between the DM and the SM, and provides limits that can be directly reinterpreted in any completion of the EFT.

The range of applicability of the EFT is defined by a mass scale $M_{\rm cut}$, a parameter which marks the upper limit of the range of energy scales at which the EFT can be used reliably, independently of the particular completion of the model. Regardless of the details of the full theory, the energy scale probing the validity of the EFT is less than or equal to the centre-of-mass energy $E_{\rm cm}$, the total invariant mass of the hard final states of the reaction. Therefore, the condition ensuring the validity of the EFT is, by definition of $M_{\rm cut}$,

$$E_{\rm cm} < M_{\rm cut} \,. \tag{6.3}$$

For example, in the specific case of a tree level mediation with a single mediator, M_{cut} can be interpreted as the mass of that mediator.

There are then at least three free parameters describing an EFT: the DM mass $m_{\rm DM}$, the scale M_* of the interaction, and the cutoff scale $M_{\rm cut}$.

We can use the same technique as above to restrict the signal to the events for which $E_{\rm cm} < M_{\rm cut}$, using only these events to derive the exclusion limits on M_* as a function of $(m_{\rm DM}, M_{\rm cut})$. We can also define an *effective coupling strength* $M_{\rm cut} = g_* M_*$, where g_* is a free parameter that substitutes the parameter $M_{\rm cut}$, and therefore derive exclusions on M_* as a function of $(m_{\rm DM}, g_*)$. This allows us to see how much of the theoretically allowed parameter space has been actually tested and how much is still unexplored; For example, in the Z'-type model considered above, g_* is equal to $\sqrt{g_{\rm DM}g_q}$. The resulting plots are shown in [RWZ15] for a particular effective operator.

The advantage of this procedure is that the obtained bounds can be directly and easily recast in any completion of the EFT, by computing the parameters M_* , $M_{\rm cut}$ in the full model as functions of the parameters of the complete theory. On the other hand, the resulting limits will be weaker than those obtained using $Q_{\rm tr}$ and a specific UV completion.

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Appendix: Detailed studies on mono-jet signatures

Appendix: Detailed studies for EW models

B.1 Further W+MET models with possible cross-section enhancements

As pointed out in Ref. [BCD⁺15], the mono-W signature can probe the iso-spin violating interactions of dark matter with quarks. The relevant operators after the electroweak symmetry breaking is

$$\frac{1}{\Lambda^2} \overline{\chi} \gamma_{\mu} \chi \left(\overline{u}_L \gamma^{\mu} u_L + \xi \overline{d}_L \gamma^{\mu} d_L \right) . \tag{B.1}$$

Here, we only keep the left-handed quarks because the right-handed quarks do not radiate a *W*-gauge boson from the weak interaction. As the LHC constraints the cutoff to higher values, it is also important to know the corresponding operators before the electroweak symmetry. At the dimension-six level, the following operator

$$\frac{c_6}{\Lambda^2} \overline{\chi} \gamma_\mu \chi \, \overline{Q}_L \gamma^\mu Q_L \tag{B.2}$$

conserves iso-spin and provides us $\xi=1$ [?]. At the dimension-eight level, new operators appear to induce iso-spin violation and can be

$$\frac{c_8^d}{\Lambda^4} \overline{\chi} \gamma_\mu \chi (H \overline{Q}_L) \gamma^\mu (Q_L H^\dagger) + \frac{c_8^u}{\Lambda^4} \overline{\chi} \gamma_\mu \chi (\tilde{H} \overline{Q}_L) \gamma^\mu (Q_L \tilde{H}^\dagger). \tag{B.3}$$

After inputting the vacuum expectation value of the Higgs field, we have

$$\xi = \frac{c_6 + c_8^d \, v_{\text{EW}}^2 / 2\Lambda^2}{c_6 + c_8^d \, v_{\text{EW}}^2 / 2\Lambda^2}.$$
 (B.4)

- For a nonzero c_6 and $v_{\rm EW} \ll \Lambda$, the iso-spin violation effects are suppressed. On the other hand, the values of c_6 , c_8^d and c_8^u depend on the UV-models.
 - There is one possible UV-model to obtain a zero value for c_6 and non-zero values for c_8^d and c_8^u . One can have the dark matter and the SM Higgs field charged under a new U(1)'. There is a small mass mixing between SM Z-boson and the new Z' with a mixing angle

of $\mathcal{O}(v_{\mathrm{EW}}^2/M_{Z'}^2)$. After integrating out Z', one has different effective dark matter couplings to u_L and d_L fields, which are proportional to their couplings to the Z boson. For this model, we have $c_6=0$ and

$$\xi = \frac{-\frac{1}{2} + \frac{1}{3}\sin^2\theta_W}{\frac{1}{2} - \frac{2}{3}\sin^2\theta_W} \approx -2.7$$
 (B.5)

and order of unity.

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⁹⁴² Appendix: Table of cross sections for $t\bar{t}$ +MET searches

All tables need to be adjusted with right number of significant digits

Coupling (g)	m_{Phi} [GeV]	m_{χ} [GeV]	Γ_{min} [GeV]	σ
0.1	10	1	0.00374318	0.207 ± 0.0006846
0.1	20	1	0.00784569	0.1121 ± 0.0003285
0.1	50	1	0.01987	0.03211 ± 0.0001005
0.1	100	1	0.0398141	$0.007325 \pm 2.416e-05$
0.1	150	1	0.0597437	$0.002396 \pm 7.419e-06$
0.1	200	1	0.0796724	$0.001018 \pm 3.398 \text{e-}06$
0.1	300	1	0.119549	$0.0003394 \pm 1.234e-06$
0.1	500	1	0.310863	$6.802e-05 \pm 2.343e-07$
0.1	1000	1	0.881329	$5.817e-06 \pm 2.356e-08$
0.1	1500	1	1.40417	$8.942e-07 \pm 3.832e-09$
0.1	10	10	0.000100	$1.007e-05 \pm 3.761e-08$
0.1	20	10	0.000100	$3.491e-05 \pm 1.012e-07$
0.1	50	10	0.0153395	0.03212 ± 0.0001037
0.1	100	10	0.0374747	$0.007343 \pm 2.011e-05$
0.1	150	10	0.0581752	$0.002389 \pm 7.654 e\text{-}06$
0.1	200	10	0.0784937	$0.001018 \pm 6.258 e\text{-}06$
0.1	300	10	0.118762	$0.0003373 \pm 1.448e-06$
0.1	500	10	0.310391	$6.773 \text{e-}05 \pm 2.326 \text{e-}07$
0.1	1000	10	0.881093	$5.81e\text{-}06 \pm 2.245e\text{-}08$
0.1	1500	10	1.40401	$8.937e-07 \pm 4.013e-09$
0.1	50	50	0.0000233555	$2.581e-07 \pm 1.214e-09$
0.1	100	50	0.0000492402	1.526e-06 ± 7.038e-09
0.1	150	50	0.0247905	$0.002387 \pm 8.272e\text{-}06$
0.1	200	50	0.051794	$0.00102 \pm 3.216 e\text{-}06$
0.1	300	50	0.100226	$0.0003366 \pm 1.393e-06$
0.1	500	50	0.299052	$6.679 \text{e-}05 \pm 2.406 \text{e-}07$
0.1	1000	50	0.875378	$5.764e-06 \pm 2.472e-08$
0.1	1500	50	1.4002	$8.866e-07 \pm 3.257e-09$

Table C.1 – continued from previous page

Coupling (g)	m_{Phi} [GeV]		Γ_{min} [GeV]	σ
0.1	100	150	0.0000492402	$1.246\text{e-}08 \pm 5.121\text{e-}11$
0.1	150	150	0.0000765167	$1.393e-08 \pm 6.653e-11$
0.1	200	150	0.000106902	$1.693 \text{e-}08 \pm 8.493 \text{e-}11$
0.1	300	150	0.000190543	$7.557\text{e-}08 \pm 2.171\text{e-}10$
0.1	500	150	0.213784	5.063e-05 ± 1.724e-07
0.1	1000	150	0.828844	$5.365 \text{e-}06 \pm 2.028 \text{e-}08$
0.1	1500	150	1.36872	$8.603\text{e-o}7 \pm 3.769\text{e-o}9$
0.1	200	300	0.000106902	$1.415 ext{e-o9} \pm 5.97 ext{e-12}$
0.1	300	300	0.000190543	$1.64e-09 \pm 7.878e-12$
0.1	500	300	0.111924	$3.078\text{e-}09 \pm 1.482\text{e-}11$
0.1	1000	300	0.687162	$3.828e-06 \pm 1.416e-08$
0.1	1500	300	1.26683	$7.579e-07 \pm 3.041e-09$
0.1	500	500	0.111924	$1.784e$ -10 \pm 1.105e-12
0.1	1000	500	0.483444	1.98e-09 \pm 9.199e-12
0.1	1500	500	1.05448	$4.92e ext{-}07 \pm 2.14e ext{-}09$
0.3	10	1	0.0336886	1.876 ± 0.006611
0.3	20	1	0.0706112	1.006 ± 0.003894
0.3	50	1	0.17883	0.2886 ± 0.0009285
0.3	100	1	0.358327	0.06598 ± 0.000182
0.3	150	1	0.537693	0.0214 \pm 6.701e-05
0.3	200	1	0.717052	$0.009216 \pm 3.533 \text{e-}05$
0.3	300	1	1.07594	$0.003044 \pm 1.194e-05$
0.3	500	1	2.79777	$0.0006105 \pm 2.187e-06$
0.3	1000	1	7.93196	$5.256e-05 \pm 2.165e-07$
0.3	1500	1	12.6376	$8.048e-06 \pm 3.473e-08$
0.3	10	10	5.69808	$0.0008143 \pm 3.272e-06$
0.3	20	10	0.0000630938	$0.002836 \pm 9.724e\text{-}06$
0.3	50	10	0.138055	0.2869 ± 0.0008971
0.3	100	10	0.337272	0.06606 ± 0.0002407
0.3	150	10	0.523576	$0.02145 \pm 8.01e-05$
0.3	200	10	0.706443	$0.009222 \pm 2.807e-05$
0.3	300	10	1.06886	$0.003051 \pm 1.001e-05$
0.3	500	10	2.79352	$0.0006115 \pm 2.268e-06$
0.3	1000	10	7.92983	$5.24e-05 \pm 1.964e-07$
0.3	1500	10	12.6361	$8.053e-06 \pm 3.203e-08$
0.3	10	50	5.69808	$1.704e-05 \pm 7.077e-08$
0.3	20	50	0.0000630938	$1.746e-05 \pm 7.383e-08$
0.3	50	50	0.000210199	$2.071e-05 \pm 8.162e-08$
0.3	100	50	0.000443162	$0.0001245 \pm 3.888 \text{e-o7}$
0.3	150	50	0.223114	0.02138 ± 6.22 e-05

Table C.1 – continued from previous page

0.3 200 50 0.466146 0.009186 ± 3.168e-05 0.3 300 50 0.902031 0.003039 ± 1.09e-05 0.3 500 50 2.69146 0.0005971 ± 2.181e-06 0.3 1000 50 7.8784 5.222e-05 ± 1.907e-07 0.3 1500 50 12.6018 7.947e-06 ± 2.996e-08 0.3 100 150 0.000443162 1.004e-06 ± 4.682e-09 0.3 150 150 0.00068865 1.132e-06 ± 4.644e-09 0.3 200 150 0.000962116 1.349e-06 ± 6.834e-09 0.3 300 150 0.00171489 6.08e-06 ± 2.289e-08 0.3 300 150 1.92405 0.000456 ± 2.064e-06 0.3 1000 150 7.45959 4.818e-05 ± 1.84e-07 0.3 1500 150 12.3185 7.796e-06 ± 2.802e-08 0.3 300 0.000962116 1.144e-07 ± 4.635e-10 0.3 300 0.000171489 1.324e-07 ± 6.534e-10 0.3 300 0.00171489 1.324e-07 ± 6.536e-10 0.3 1500 300 1.00732 2.5e-07 ± 1.113e-09 0.3 1500 300 11.4014 6.834e-06 ± 2.623e-08 0.3 500 500 1.00732 1.449e-08 ± 5.536e-11 0.3 1500 500 9.49035 4.374e-06 ± 1.739e-08 0.7 10 1 0.183416 10.2 ± 0.03649 0.7 20 1 0.384439 5.462 ± 0.02022 0.7 50 1 0.97363 1.558 ± 0.004491 0.7 100 1 1.95089 0.3568 ± 0.001143 0.7 150 1 2.92744 0.1161 ± 0.0003685 0.7 200 1 3.90395 0.04995 ± 0.0001494 0.7 300 1 5.85789 0.01649 ± 5.579e-05 0.7 500 1 15.2323 0.003313 ± 1.464e-05 0.7 1500 1 6.88045 4.481e-05 ± 1.885e-07 0.7 150 1 0.000310229 0.02403 ± 0.0001742 0.7 150 1 0.000310229 0.02403 ± 0.0001742 0.7 150 1 0.000310229 0.02403 ± 0.0001742 0.7 150 1 0.000310229 0.02403 ± 0.0001742 0.7 150 1 0.000310229 0.02403 ± 0.0001742 0.7 150 1 0.000310229 0.04984 ± 0.0001855 0.7 200 10 3.84619 0.04984 ± 0.0001855 0.7 200 10 3.84619 0.04984 ± 0.0001855 0.7 200 10 3.84619 0.04984 ± 0.0001855 0.7 200 10 3.84619 0.04984 ± 0.0001855 0.7 500 10 5.81933 0.01649 ± 6.839e-05	Coupling (g)	m_{Phi} [GeV]		Γ_{min} [GeV]	σ
0.3 500 50 2.69146 0.0005971 ± 2.181e-06 0.3 1000 50 7.8784 5.222e-05 ± 1.907e-07 0.3 1500 50 12.6018 7.947e-06 ± 2.996e-08 0.3 150 150 0.000443162 1.004e-06 ± 4.682e-09 0.3 150 150 0.00068865 1.132e-06 ± 4.644e-09 0.3 200 150 0.000962116 1.349e-06 ± 6.834e-06 0.3 300 150 0.00171489 6.08e-06 ± 2.289e-08 0.3 500 150 1.92405 0.000456 ± 2.064e-06 0.3 1000 150 7.45959 4.818e-05 ± 1.84e-07 0.3 1500 150 12.3185 7.796e-06 ± 2.802e-08 0.3 200 300 0.000962116 1.144e-07 ± 4.635e-10 0.3 300 300 0.000962116 1.144e-07 ± 4.635e-10 0.3 300 300 0.00171489 1.324e-07 ± 6.534e-10 0.3 500 300 1.00732 2.5e-07 ± 1.113e-09 0.3 1500 300 11.4014 6.834e-06 ± 2.623e-08 0.3 500 500 1.00732 1.449e-08 ± 5.536e-11 0.3 1500 500 4.35099 1.487e-07 ± 6.617e-10 0.3 1500 500 4.35099 1.487e-07 ± 6.617e-10 0.3 1500 500 9.49035 4.374e-06 ± 1.739e-08 0.7 10 1 0.183416 10.2 ± 0.03649 0.7 20 1 0.384439 5.462 ± 0.02022 0.7 50 1 0.97363 1.558 ± 0.001491 0.7 100 1 1.95089 0.3568 ± 0.0011143 0.7 150 1 2.92744 0.1161 ± 0.0003685 0.7 200 1 3.90395 0.04995 ± 0.0001494 0.7 300 1 5.85789 0.01649 ± 5.579e-05 0.7 500 1 43.1851 0.0002823 ± 1.233e-06 0.7 100 1 43.1851 0.0002823 ± 1.233e-06 0.7 20 10 0.000310229 0.02403 ± 0.0001038 0.7 20 10 0.000343511 0.08347 ± 0.0004742 0.7 50 10 0.751635 1.553 ± 0.004764 0.7 150 10 2.85058 0.1165 ± 0.0004139 0.7 200 10 3.84619 0.04984 ± 0.0001855 0.7 500 10 5.81933 0.01649 ± 6.843e-05 0.7 500 10 5.81933 0.002815 ± 1.129e-06 0.7 500 10 5.81933 0.01649 ± 6.843e-05 0.7 500 10 5.81933 0.0002815 ± 1.129e-06 0.7 500 10 5.81933 0.0002815 ± 1.129e-06	0.3	200	50	0.466146	0.009186 ± 3.168e-05
0.3 1000 50 7.8784 5.222e-05 ± 1.907e-07 0.3 1500 50 12.6018 7.947e-06 ± 2.996e-08 0.3 150 150 0.000443162 1.004e-06 ± 4.682e-09 0.3 150 150 0.00068865 1.132e-06 ± 4.644e-09 0.3 200 150 0.000962116 1.349e-06 ± 6.834e-09 0.3 300 150 0.00171489 6.08e-06 ± 2.289e-08 0.3 500 150 1.92405 0.000456 ± 2.064e-06 0.3 1000 150 7.45959 4.818e-05 ± 1.84e-07 0.3 1500 150 12.3185 7.796e-06 ± 2.802e-08 0.3 200 300 0.000962116 1.144e-07 ± 4.635e-10 0.3 300 300 0.000962116 1.324e-07 ± 6.534e-10 0.3 300 300 0.000171489 1.324e-07 ± 6.534e-10 0.3 300 300 1.00732 2.5e-07 ± 1.113e-09 0.3 1500 300 11.40732 2.5e-07 ± 6.617e-10 0.3 1500 300 11.4014 6.834e-06 ± 2.623e-08 0.3 500 500 1.00732 1.449e-08 ± 5.536e-11 0.3 1500 300 11.00732 1.449e-08 ± 5.536e-11 0.3 1500 500 4.35099 1.487e-07 ± 6.617e-10 0.3 1500 500 9.49035 4.374e-06 ± 1.739e-08 0.7 10 1 0.183416 10.2 ± 0.03649 0.7 20 1 0.384439 5.462 ± 0.02022 0.7 50 1 0.97363 1.558 ± 0.004491 0.7 100 1 1.95089 0.3568 ± 0.001143 0.7 150 1 2.92744 0.1161 ± 0.0003685 0.7 200 1 3.90395 0.04995 ± 0.0001494 0.7 300 1 5.88789 0.01649 ± 5.579e-05 0.7 1500 1 43.1851 0.0002823 ± 1.233e-06 0.7 1500 1 68.8045 4.481e-05 ± 1.885e-07 0.7 150 1 0.000343511 0.08347 ± 0.0004742 0.7 50 10 0.000343511 0.08347 ± 0.0004742 0.7 50 10 0.000343511 0.08347 ± 0.0004794 0.7 150 10 0.000343511 0.08347 ± 0.0004794 0.7 150 10 0.000343511 0.08347 ± 0.0004794 0.7 150 10 1.88666 0.3569 ± 0.0004951 0.7 150 10 5.81933 0.01649 ± 5.579e-05 0.7 150 10 5.81933 0.01649 ± 6.843e-05 0.7 200 10 3.84619 0.04984 ± 0.0001855 0.7 200 10 3.84619 0.04984 ± 0.0001855 0.7 500 10 1.52092 0.003301 ± 1.289e-05 0.7 500 10 15.2092 0.003301 ± 1.289e-05 0.7 500 10 15.2092 0.003301 ± 1.289e-05	0.3	300	50	0.902031	0.003039 ± 1.09e-05
0.3	0.3	500	50	2.69146	0.0005971 \pm 2.181e-06
0.3 150 150 0.000443162 1.004e-06 ± 4.682e-09 0.3 150 150 0.00068865 1.132e-06 ± 4.644e-09 0.3 200 150 0.000962116 1.349e-06 ± 6.834e-09 0.3 300 150 0.00171489 6.08e-06 ± 2.289e-08 0.3 500 150 1.92405 0.000456 ± 2.064e-06 0.3 1000 150 7.45959 4.818e-05 ± 1.84e-07 0.3 1500 150 12.3185 7.796e-06 ± 2.802e-08 0.3 200 300 0.000962116 1.144e-07 ± 4.635e-10 0.3 300 300 0.00171489 1.324e-07 ± 6.534e-10 0.3 300 300 0.00171489 1.324e-07 ± 6.534e-10 0.3 500 300 1.00732 2.5e-07 ± 1.113e-09 0.3 1500 300 1.00732 2.5e-07 ± 1.113e-09 0.3 1500 300 1.00732 1.449e-08 ± 5.536e-11 0.3 1500 500 1.00732 1.449e-08 ± 5.536e-11 0.3 1500 500 4.35099 1.487e-07 ± 6.617e-10 0.3 1500 500 4.35099 1.487e-07 ± 6.617e-10 0.3 1500 500 9.49035 4.374e-06 ± 1.739e-08 0.7 10 1 0.183416 10.2 ± 0.03649 0.7 20 1 0.384439 5.462 ± 0.02022 0.7 50 1 0.97363 1.558 ± 0.004491 0.7 100 1 1.95089 0.3568 ± 0.001143 0.7 150 1 2.92744 0.1161 ± 0.003685 0.7 200 1 3.90395 0.04995 ± 0.0001494 0.7 300 1 5.8789 0.01649 ± 5.579e-05 0.7 500 1 15.2323 0.003313 ± 1.464e-05 0.7 1500 1 68.8045 4.481e-05 ± 1.885e-07 0.7 1500 1 68.8045 4.481e-05 ± 1.885e-07 0.7 150 10 0.000343511 0.08347 ± 0.0004742 0.7 50 10 0.000343511 0.08347 ± 0.0004742 0.7 50 10 0.751635 1.553 ± 0.0004764 0.7 150 10 1.83626 0.3569 ± 0.0001439 0.7 200 10 3.84619 0.04984 ± 0.0001855 0.7 200 10 3.84619 0.04984 ± 0.0001855 0.7 500 10 15.2092 0.003301 ± 1.289e-05	0.3	1000	50	7.8784	5.222e-05 ± 1.907e-07
0.3	0.3	1500	50	12.6018	$7.947e$ -06 \pm 2.996e-08
0.3	0.3	100	150	0.000443162	$1.004\text{e-}06 \pm 4.682\text{e-}09$
0.3	0.3	150	150	0.00068865	$1.132e-06 \pm 4.644e-09$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.3	200	150	0.000962116	$1.349e-06 \pm 6.834e-09$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.3	300	150	0.00171489	$6.08\text{e-}06 \pm 2.289\text{e-}08$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.3	500	150	1.92405	$0.000456 \pm 2.064e-06$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.3	1000	150	7.45959	$4.818e-05 \pm 1.84e-07$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.3	1500	150	12.3185	$7.796\text{e-}06 \pm 2.802\text{e-}08$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.3	200	300	0.000962116	1.144 e-07 \pm 4.635e-10
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.3	300	300	0.00171489	$1.324e ext{-07} \pm 6.534e ext{-10}$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.3	500	300	1.00732	$2.5 ext{e-o7} \pm 1.113 ext{e-o9}$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.3	1000	300	6.18446	$3.439e-05 \pm 1.376e-07$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.3	1500	300	11.4014	$6.834\text{e-}06 \pm 2.623\text{e-}08$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.3	500	500	1.00732	$1.449 \text{e-} 08 \pm 5.536 \text{e-} 11$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.3	1000	500	4.35099	$1.487 e$ -07 \pm 6.617e-10
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.3	1500	500	9.49035	$4.374e\text{-}06 \pm 1.739e\text{-}08$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.7	10	1	0.183416	10.2 ± 0.03649
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.7	20	1	0.384439	5.462 ± 0.02022
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.7	50	1	0.97363	1.558 ± 0.004491
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.7	100	1	1.95089	0.3568 ± 0.001143
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.7	150	1	2.92744	0.1161 ± 0.0003685
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.7	200	1	3.90395	0.04995 ± 0.0001494
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.7	300	1	5.85789	0.01649 \pm 5.579e-05
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.7	500	1	15.2323	$0.003313 \pm 1.464e-05$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.7	1000	1	43.1851	$0.0002823 \pm 1.233e-06$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.7	1500	1	68.8045	$4.481e$ -05 \pm 1.885e-07
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.7	10	10	0.0000310229	0.02403 ± 0.0001038
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.7	20	10	0.000343511	0.08347 ± 0.0004742
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.7	50	10	0.751635	1.553 ± 0.004764
0.720010 3.84619 0.04984 ± 0.0001855 0.730010 5.81933 $0.01649 \pm 6.843e-05$ 0.750010 15.2092 $0.003301 \pm 1.289e-05$ 0.7100010 43.1735 $0.0002815 \pm 1.129e-06$	0.7	100	10	1.83626	0.3569 ± 0.0009501
0.730010 5.81933 $0.01649 \pm 6.843e$ -050.750010 15.2092 $0.003301 \pm 1.289e$ -050.7100010 43.1735 $0.0002815 \pm 1.129e$ -06	0.7	150	10	2.85058	0.1165 ± 0.0004139
0.7 500 10 15.2092 0.003301 \pm 1.289e-05 0.7 1000 10 43.1735 0.0002815 \pm 1.129e-06	0.7	200	10	3.84619	0.04984 ± 0.0001855
0.7 1000 10 43.1735 0.0002815 \pm 1.129e-06	0.7	300	10	5.81933	$0.01649 \pm 6.843 \text{e-}05$
	0.7	500	10	15.2092	$0.003301 \pm 1.289e-05$
	0.7	1000	10	43.1735	$0.0002815 \pm 1.129e\text{-}06$
0.7 1500 10 68.7967 4.491e-05 \pm 2.108e-07	0.7	1500	10	68.7967	$4.491 ext{e-o5} \pm 2.108 ext{e-o7}$

Table C.1 – continued from previous page

Coupling (g)	m_{Phi} [GeV]	m_{χ} [GeV]	Γ_{min} [GeV]	σ
0.7	10	50	0.0000310229	0.000511 ± 1.977e-06
0.7	20	50	0.000343511	$0.0005184 \pm 2.146e-06$
0.7	50	50	0.00114442	$0.0006176 \pm 3.053e-06$
0.7	100	50	0.00241277	$0.003681 \pm 1.333e-05$
0.7	150	50	1.21473	0.1156 ± 0.0003755
0.7	200	50	2.53791	0.04988 ± 0.0001824
0.7	300	50	4.91106	$0.01651 \pm 6.317 e$ -05
0.7	500	50	14.6535	$0.003218 \pm 1.523e-05$
0.7	1000	50	42.8935	$0.0002794 \pm 1.049e-06$
0.7	1500	50	68.6098	$4.46 ext{e-05} \pm 1.989 ext{e-07}$
0.7	100	150	0.00241277	$2.968\text{e-}05 \pm 1.364\text{e-}07$
0.7	150	150	0.00374932	$3.327e-05 \pm 1.594e-07$
0.7	200	150	0.00523819	4.04 e-05 \pm 1.861e-07
0.7	300	150	0.00933663	$0.0001787 \pm 7.694e$ -07
0.7	500	150	10.4754	$0.00243 \pm 1.128 \text{e-}05$
0.7	1000	150	40.6133	$0.0002573 \pm 1.014e-06$
0.7	1500	150	67.0675	$4.239e-05 \pm 1.707e-07$
0.7	100	300	0.00241277	$3.132e-06 \pm 1.547e-08$
0.7	150	300	0.00374932	$3.227e-06 \pm 1.433e-08$
0.7	200	300	0.00523819	$3.393e-06 \pm 1.437e-08$
0.7	300	300	0.00933663	$3.918e\text{-}06 \pm 1.628e\text{-}08$
0.7	500	300	5.4843	$7.383e-06 \pm 2.87e-08$
0.7	1000	300	33.6709	$0.0001801 \pm 7.992e$ -07
0.7	1500	300	62.0745	$3.644e-05 \pm 1.473e-07$
0.7	500	500	5.4843	$4.301e-07 \pm 1.836e-09$
0.7	1000	500	23.6887	$3.684e-06 \pm 2.358e-08$
0.7	1500	500	51.6697	$2.291e-05 \pm 9.843e-08$
1.	10	1	0.374318	20.79 ± 0.08102
1.	20	1	0.784569	11.08 ± 0.0396
1.	50	1	1.987	3.146 ± 0.01331
1.	100	1	3.98141	0.7199 ± 0.002775
1.	150	1	5.97437	0.2354 ± 0.0008189
1.	200	1	7.96724	0.1009 ± 0.0003854
1.	300	1	11.9549	0.03369 ± 0.0001155
1.	500	1	31.0863	$0.006652 \pm 2.898e-05$
1.	1000	1	88.1329	$0.0005705 \pm 2.817e-06$
1.	1500	1	140.417	$9.244e-05 \pm 4.273e-07$
1.	10	10	0.000063312	0.1009 ± 0.00035
1.	20	10	0.000701043	0.3475 ± 0.002265
1.	50	10	1.53395	3.139 ± 0.01028

Table C.1 – continued from previous page

Coupling (g)	m_{Phi} [GeV]		Γ_{min} [GeV]	σ
1.	100	10	3.74747	0.7158 ± 0.002486
1.	150	10	5.81752	0.236 ± 0.0007591
1.	200	10	7.84937	0.1013 ± 0.0003668
1.	300	10	11.8762	0.03374 ± 0.0001403
1.	500	10	31.0391	$0.006631 \pm 2.585e-05$
1.	1000	10	88.1093	$0.0005663 \pm 2.515e-06$
1.	1500	10	140.401	$9.408 ext{e-o5} \pm 4.698 ext{e-o7}$
1.	10	50	0.000063312	$0.00212 \pm 8.815 e\text{-}06$
1.	20	50	0.000701043	$0.002149 \pm 9.604 e$ -06
1.	50	50	0.00233555	$0.002568 \pm 1.017e-05$
1.	100	50	0.00492402	0.01523 ± 5.043 e-05
1.	150	50	2.47905	0.2351 ± 0.0008404
1.	200	50	5.1794	0.09993 ± 0.0003164
1.	300	50	10.0226	0.03349 ± 0.0001351
1.	500	50	29.9052	$0.006402 \pm 2.604e-05$
1.	1000	50	87.5378	$0.0005634 \pm 2.601e-06$
1.	1500	50	140.02	$9.211e-05 \pm 4.909e-07$
1.	100	150	0.00492402	$0.0001247 \pm 5.899 e - 07$
1.	150	150	0.00765167	0.0001387 ± 5.889 e-07
1.	200	150	0.0106902	0.000168 ± 7.656 e-07
1.	300	150	0.0190543	$0.0007464 \pm 2.977e-06$
1.	500	150	21.3784	$0.004856 \pm 1.95 e - 05$
1.	1000	150	82.8844	$0.0005122 \pm 1.98e-06$
1.	1500	150	136.872	$8.662e-05 \pm 3.821e-07$
1.	200	300	0.0106902	$1.422e-05 \pm 6.147e-08$
1.	300	300	0.0190543	$1.626e-05 \pm 6.865e-08$
1.	500	300	11.1924	$3.081e-05 \pm 1.244e-07$
1.	1000	300	68.7162	$0.0003534 \pm 1.392e-06$
1.	1500	300	126.683	$7.258e-05 \pm 3.651e-07$
1.	500	500	11.1924	$1.777e-06 \pm 9.67e-09$
1.	1000	500	48.3444	$1.331e-05 \pm 6.551e-08$
1.	1500	500	105.448	$4.443e-05 \pm 1.988e-07$
1.5	10	1	0.842215	46.59 ± 0.1797
1.5	20	1	1.76528	24.52 ± 0.08387
1.5	50	1	4.47075	6.903 ± 0.02244
1.5	100	1	8.95817	1.577 ± 0.005493
1.5	150	1	13.4423	0.5224 ± 0.002309
1.5	200	1	17.9263	0.2259 ± 0.0008625
1.5	300	1	26.8985	0.07529 ± 0.0003407
1.5	500	1	69.9442	$0.01445 \pm 6.469e-05$
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Table C.1 – continued from previous page

1.5 1000 1 198.299 $0.001234 \pm 5.694e-06$ 1.5 1500 1 315.939 $0.002179 \pm 1.024e-06$ 1.5 10 10 0.000157735 1.763 ± 0.01031 1.5 20 10 0.00157735 1.763 ± 0.01031 1.5 50 10 3.45138 6.906 ± 0.02283 1.5 100 10 8.4318 1.568 ± 0.006489 1.5 150 10 13.0894 0.5162 ± 0.001934 1.5 200 10 17.6611 0.2249 ± 0.0008153 1.5 300 10 26.7214 0.07541 ± 0.0002941 1.5 300 10 26.7214 0.07541 ± 0.0002841 1.5 300 10 198.246 $0.00147 \pm 6.923e-05$ 1.5 1500 10 315.903 $0.002157 \pm 8.805e-07$ 1.5 1500 10 315.903 $0.002157 \pm 8.805e-07$ 1.5 150 10 30.503 0.00157735 0.016	Coupling (g)			Γ_{min} [GeV]	σ
1.5 10 10 0.000142452 0.5117 ± 0.002037 1.5 20 10 0.00157735 1.763 ± 0.01031 1.5 50 10 3.45138 6.906 ± 0.02283 1.5 100 10 8.4318 1.568 ± 0.006489 1.5 150 10 13.0894 0.5162 ± 0.001934 1.5 200 10 17.6611 0.2249 ± 0.0008153 1.5 300 10 26.7214 0.07541 ± 0.0002941 1.5 500 10 69.8379 $0.01447 \pm 6.923e-05$ 1.5 1000 10 198.246 $0.001242 \pm 6.739e-06$ 1.5 1500 10 315.903 $0.0002157 \pm 8.805e-07$ 1.5 100 50 0.00157735 $0.01068 \pm 4.527e-05$ 1.5 10 50 0.00157735 $0.01093 \pm 6.079e-05$ 1.5 10 50 0.011079 0.07677 ± 0.0002445 1.5 10 50 0.011079 0.07677 ± 0.0002445 <td>1.5</td> <td>1000</td> <td>1</td> <td>198.299</td> <td>0.001234 ± 5.694e-06</td>	1.5	1000	1	198.299	0.001234 ± 5.694 e-06
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	1.5	1500	1	315.939	$0.0002179 \pm 1.024e$ -06
1.5 50 10 3.45138 6.906 ± 0.02283 1.5 100 10 8.4318 1.568 ± 0.006489 1.5 150 10 13.0894 0.5162 ± 0.001934 1.5 200 10 17.6611 0.2249 ± 0.0008153 1.5 300 10 26.7214 0.07541 ± 0.002941 1.5 500 10 69.8379 $0.01447 \pm 6.923e-05$ 1.5 1000 10 198.246 $0.001242 \pm 6.739e-06$ 1.5 1500 10 198.246 $0.001242 \pm 6.739e-06$ 1.5 1500 10 315.903 $0.0002157 \pm 8.805e-07$ 1.5 150 10 50 0.00142452 $0.01083 \pm 6.092e-05$ 1.5 150 50 0.00157735 $0.01093 \pm 6.092e-05$ 1.5 10 50 0.0011079 0.07677 ± 0.0002445 1.5 10 50 0.011079 0.07677 ± 0.0002445 1.5 150 50 5.57786	1.5	10	10	0.000142452	0.5117 ± 0.002037
1.5 100 10 8.4318 1.568 ± 0.006489 1.5 150 10 13.0894 0.5162 ± 0.001934 1.5 200 10 17.6611 0.2249 ± 0.0008153 1.5 300 10 26.7214 0.07541 ± 0.0002941 1.5 500 10 69.8379 $0.01447 \pm 6.923e-05$ 1.5 1000 10 198.246 $0.001242 \pm 6.739e-06$ 1.5 1500 10 315.903 $0.0002157 \pm 8.805e-07$ 1.5 10 50 0.000142452 $0.01083 \pm 6.79e-05$ 1.5 10 50 0.00157735 $0.0193 \pm 6.079e-05$ 1.5 10 50 0.0011079 0.07677 ± 0.0002445 1.5 10 50 0.011079 0.07677 ± 0.0002445 1.5 150 50 5.57786 0.5195 ± 0.000511 1.5 150 50 5.57786 0.5195 ± 0.0006711 1.5 150 50 5.25786 0.07353 ± 0.0003291 <td>1.5</td> <td>20</td> <td>10</td> <td>0.00157735</td> <td>1.763 ± 0.01031</td>	1.5	20	10	0.00157735	1.763 ± 0.01031
1.5 150 10 13.0894 0.5162 ± 0.001934 1.5 200 10 17.6611 0.2249 ± 0.0008153 1.5 300 10 26.7214 0.07541 ± 0.0002941 1.5 500 10 69.8379 $0.01447 \pm 6.923e-05$ 1.5 1000 10 198.246 $0.001242 \pm 6.73ge-06$ 1.5 1500 10 315.903 $0.0002157 \pm 8.805e-07$ 1.5 10 50 0.0012452 $0.01083 \pm 6.527e-05$ 1.5 10 50 0.00157735 $0.01093 \pm 6.079e-05$ 1.5 10 50 0.00157735 $0.01093 \pm 6.079e-05$ 1.5 10 50 0.0011279 0.07677 ± 0.0002445 1.5 10 50 0.011079 0.07677 ± 0.0002445 1.5 150 50 0.011079 0.07677 ± 0.0002445 1.5 150 50 0.011079 0.07677 ± 0.0002445 1.5 150 50 0.011079 0.07677 ± 0.00024 1.5 150 50 0.024866 0.0139 ± 0.0002	1.5	50	10	3.45138	6.906 ± 0.02283
1.5 200 10 17.6611 0.2249 ± 0.0008153 1.5 300 10 26.7214 0.07541 ± 0.0002941 1.5 500 10 69.8379 $0.01447 \pm 6.923e-05$ 1.5 1000 10 198.246 $0.001242 \pm 6.739e-06$ 1.5 1500 10 315.903 $0.0002157 \pm 8.805e-07$ 1.5 10 50 0.00015775 $0.01068 \pm 4.527e-05$ 1.5 10 50 0.0015775 $0.01093 \pm 6.079e-05$ 1.5 20 50 0.0015775 $0.01093 \pm 6.079e-05$ 1.5 100 50 0.011079 0.07677 ± 0.0002445 1.5 150 50 0.72866 0.0139 ± 0.00057 1.5 150 50 0.72866 0.01	1.5	100	10	8.4318	1.568 ± 0.006489
1.5 300 10 26.7214 0.07541 ± 0.0002941 1.5 500 10 69.8379 $0.01447 \pm 6.923e-05$ 1.5 1000 10 198.246 $0.001242 \pm 6.739e-06$ 1.5 1500 10 315.903 $0.0002157 \pm 8.805e-07$ 1.5 10 50 0.000157735 $0.01068 \pm 4.527e-05$ 1.5 20 50 0.00157735 $0.01093 \pm 6.079e-05$ 1.5 50 50 0.00525498 $0.01302 \pm 6.649e-05$ 1.5 100 50 0.011079 0.07677 ± 0.0002445 1.5 150 50 5.57786 0.5195 ± 0.001577 1.5 150 50 5.57786 0.5195 ± 0.001577 1.5 150 50 11.6536 0.2195 ± 0.000571 1.5 150 50 16.966 0.0159 ± 0.000671 1.5 150 50 50.25508 0.07353 ± 0.000329 1.5 1500 50 67.2866 $0.01299 \pm 7.038e-06$ 1.5 1500 50 315.045 0.000219	1.5	150	10	13.0894	0.5162 ± 0.001934
1.5 500 10 69.8379 $0.01447 \pm 6.923e-05$ 1.5 1000 10 198.246 $0.001242 \pm 6.739e-06$ 1.5 1500 10 315.903 $0.0002157 \pm 8.805e-07$ 1.5 10 50 0.000157735 $0.01068 \pm 4.527e-05$ 1.5 20 50 0.00157735 $0.01093 \pm 6.079e-05$ 1.5 50 50 0.00525498 $0.01302 \pm 6.649e-05$ 1.5 100 50 0.011079 0.07677 ± 0.0002445 1.5 150 50 5.57786 0.5195 ± 0.001577 1.5 150 50 5.57786 0.5195 ± 0.0001577 1.5 150 50 5.57786 0.5195 ± 0.0001577 1.5 150 50 5.57786 0.5195 ± 0.0006711 1.5 150 50 67.2866 $0.0139 \pm 6.13e-05$ 1.5 150 50 67.2866 $0.0139 \pm 6.13e-05$ 1.5 1500 50 315.045 $0.0002199 \pm 7.038e-06$ 1.5 1500 50 315.045 0.0002	1.5	200	10	17.6611	0.2249 ± 0.0008153
1.5 1000 10 198.246 $0.001242 \pm 6.739e-06$ 1.5 1500 10 315.903 $0.0002157 \pm 8.805e-07$ 1.5 10 50 0.000142452 $0.01068 \pm 4.527e-05$ 1.5 20 50 0.00157735 $0.01093 \pm 6.079e-05$ 1.5 50 50 0.00525498 $0.01302 \pm 6.649e-05$ 1.5 100 50 0.011079 0.07677 ± 0.0002445 1.5 150 50 5.57786 0.5195 ± 0.000577 1.5 200 50 11.6536 0.2195 ± 0.0006711 1.5 300 50 22.5508 0.07353 ± 0.0003291 1.5 500 50 67.2866 $0.0139 \pm 6.13e-05$ 1.5 1000 50 196.96 $0.001209 \pm 7.038e-06$ 1.5 1500 50 315.045 $0.002109 \pm 8.631e-07$ 1.5 1500 50 315.045 $0.002109 \pm 7.038e-06$ 1.5 150 50 0.011079 $0.006295 \pm 3.608e-06$ 1.5 150 150 0.011079 0	1.5	300	10	26.7214	0.07541 ± 0.0002941
1.5 1500 10 315.903 $0.0002157 \pm 8.805e-07$ 1.5 10 50 0.000142452 $0.01068 \pm 4.527e-05$ 1.5 20 50 0.00157735 $0.01093 \pm 6.079e-05$ 1.5 50 50 0.00525498 $0.01302 \pm 6.649e-05$ 1.5 100 50 0.011079 0.07677 ± 0.0002445 1.5 150 50 5.57786 0.5195 ± 0.000577 1.5 200 50 11.6536 0.2195 ± 0.0006711 1.5 300 50 22.5508 0.07353 ± 0.0003291 1.5 500 50 67.2866 $0.0139 \pm 6.13e-05$ 1.5 1000 50 196.96 $0.001209 \pm 7.038e-06$ 1.5 1500 50 315.045 $0.002109 \pm 8.631e-07$ 1.5 1500 50 315.045 $0.002109 \pm 8.631e-07$ 1.5 150 50 0.011079 $0.006295 \pm 3.008e-06$ 1.5 150 150 0.011079 $0.006295 \pm 3.608e-06$ 1.5 150 150 0.0240529 <t< td=""><td>1.5</td><td>500</td><td>10</td><td>69.8379</td><td>$0.01447 \pm 6.923 \text{e-}05$</td></t<>	1.5	500	10	69.8379	$0.01447 \pm 6.923 \text{e-}05$
1.5 10 50 0.000142452 $0.01068 \pm 4.527e-05$ 1.5 20 50 0.00157735 $0.0193 \pm 6.079e-05$ 1.5 50 50 0.00525498 $0.01302 \pm 6.649e-05$ 1.5 100 50 0.011079 0.07677 ± 0.0002445 1.5 150 50 5.57786 0.5195 ± 0.000577 1.5 200 50 11.6536 0.2195 ± 0.0006711 1.5 300 50 22.5508 0.07353 ± 0.0003291 1.5 500 50 67.2866 $0.0139 \pm 6.13e-05$ 1.5 1000 50 196.96 $0.001209 \pm 7.038e-06$ 1.5 1500 50 315.045 $0.002109 \pm 8.631e-05$ 1.5 1500 50 315.045 $0.002109 \pm 8.631e-05$ 1.5 150 150 0.011079 $0.006295 \pm 3.008e-06$ 1.5 150 150 0.0172162 $0.000706 \pm 3.661e-06$ 1.5 150 150 0.0240529 $0.00086 \pm 3.608e-06$ 1.5 300 150 48.1013 <	1.5	1000	10	198.246	$0.001242 \pm 6.739e-06$
1.5 20 50 0.00157735 $0.0193 \pm 6.079e-05$ 1.5 50 50 0.00525498 $0.01302 \pm 6.649e-05$ 1.5 100 50 0.011079 0.07677 ± 0.0002445 1.5 150 50 5.57786 0.5195 ± 0.000577 1.5 200 50 11.6536 0.2195 ± 0.0006711 1.5 300 50 22.5508 0.07353 ± 0.0003291 1.5 500 50 67.2866 $0.0139 \pm 6.13e-05$ 1.5 1000 50 196.96 $0.001209 \pm 7.038e-06$ 1.5 1500 50 315.045 $0.002109 \pm 8.631e-05$ 1.5 150 50 315.045 $0.002109 \pm 8.631e-05$ 1.5 150 150 0.0172162 $0.0002109 \pm 8.631e-06$ 1.5 150 150 0.0172162 $0.000706 \pm 3.661e-06$ 1.5 150 150 0.0240529 $0.0086 \pm 3.608e-06$ 1.5 300 150 0.0428723 $0.003751 \pm 1.304e-05$ 1.5 1500 150 307.963 $0.$	1.5	1500	10	315.903	0.0002157 ± 8.805 e-07
1.55050 0.00525498 $0.01302 \pm 6.649e-05$ 1.5 100 50 0.011079 0.07677 ± 0.0002445 1.5 150 50 5.57786 0.5195 ± 0.001577 1.5 200 50 11.6536 0.2195 ± 0.0006711 1.5 300 50 22.5508 0.07353 ± 0.0003291 1.5 500 50 67.2866 $0.0139 \pm 6.13e-05$ 1.5 1000 50 196.96 $0.001209 \pm 7.038e-06$ 1.5 1500 50 315.045 $0.0002109 \pm 8.631e-07$ 1.5 150 150 0.011079 $0.0006295 \pm 3.008e-06$ 1.5 150 150 0.0172162 $0.000706 \pm 3.661e-06$ 1.5 150 150 0.0240529 $0.00086 \pm 3.608e-06$ 1.5 300 150 0.0240529 $0.00086 \pm 3.608e-06$ 1.5 300 150 0.0428723 $0.003751 \pm 1.304e-05$ 1.5 1500 150 48.1013 $0.01046 \pm 4.013e-05$ 1.5 1500 150 307.963 $0.001072 \pm 4.469e-06$ 1.5 1500 150 307.963 $0.0001931 \pm 1.022e-06$ 1.5 1500 300 0.0240529 $7.176e-05 \pm 3.641e-07$ 1.5 300 300 0.0240529 $7.176e-05 \pm 3.641e-07$ 1.5 500 300 25.183 $0.000155 \pm 6.658e-07$ 1.5 1500 300 285.036 $0.0001529 \pm 7.694e-07$ 1.5 1500 500 285.036 0.000152	1.5	10	50	0.000142452	$0.01068 \pm 4.527 e$ -05
1.510050 0.011079 0.07677 ± 0.0002445 1.515050 5.57786 0.5195 ± 0.001577 1.520050 11.6536 0.2195 ± 0.0006711 1.530050 22.5508 0.07353 ± 0.0003291 1.550050 67.2866 $0.0139 \pm 6.13e-05$ 1.5100050 196.96 $0.001209 \pm 7.038e-06$ 1.5150050 315.045 $0.0002109 \pm 8.631e-07$ 1.5100150 0.011079 $0.0006295 \pm 3.008e-06$ 1.5150150 0.0172162 $0.000706 \pm 3.661e-06$ 1.5200150 0.0240529 $0.00086 \pm 3.608e-06$ 1.5300150 0.0428723 $0.003751 \pm 1.304e-05$ 1.5500150 48.1013 $0.01046 \pm 4.013e-05$ 1.51000150 186.49 $0.001072 \pm 4.469e-06$ 1.51500150 307.963 $0.0001931 \pm 1.022e-06$ 1.5200300 0.0240529 $7.176e-05 \pm 3.641e-07$ 1.5300300 0.0428723 $8.3e-05 \pm 3.627e-07$ 1.5500300 25.183 $0.000155 \pm 6.658e-07$ 1.51500300 285.036 $0.0001529 \pm 7.694e-07$ 1.51500300 285.036 $0.0001529 \pm 7.694e-07$ 1.51500500 237.259 $8.736e-05 \pm 4.269e-07$ 1.51500500 237.259 $8.736e-05 \pm 4.268e-07$ 2.101 1.49727	1.5	20	50	0.00157735	$0.01093 \pm 6.079 \text{e-}05$
1.515050 5.57786 0.5195 ± 0.001577 1.520050 11.6536 0.2195 ± 0.0006711 1.530050 22.5508 0.07353 ± 0.0003291 1.550050 67.2866 $0.0139 \pm 6.13e-05$ 1.5100050 196.96 $0.001209 \pm 7.038e-06$ 1.5150050 315.045 $0.0002109 \pm 8.631e-07$ 1.5100150 0.011079 $0.0006295 \pm 3.008e-06$ 1.5150150 0.0172162 $0.000706 \pm 3.661e-06$ 1.5200150 0.0240529 $0.00086 \pm 3.608e-06$ 1.5300150 0.0428723 $0.003751 \pm 1.304e-05$ 1.51000150 48.1013 $0.01046 \pm 4.013e-05$ 1.51000150 186.49 $0.001072 \pm 4.469e-06$ 1.51500150 307.963 $0.0001931 \pm 1.022e-06$ 1.5200300 0.0240529 $7.176e-05 \pm 3.641e-07$ 1.5300300 0.0428723 $8.3e-05 \pm 3.627e-07$ 1.5500300 25.183 $0.000155 \pm 6.658e-07$ 1.51000300 154.611 $0.0007234 \pm 2.773e-06$ 1.51500300 285.036 $0.0001529 \pm 7.694e-07$ 1.5500500 25.183 $9.099e-06 \pm 4.301e-08$ 1.51500500 25.183 $9.099e-06 \pm 4.301e-08$ 1.51500500 237.259 $8.736e-05 \pm 4.268e-07$ 2.101 1.49727 <td< td=""><td>1.5</td><td>50</td><td>50</td><td>0.00525498</td><td>$0.01302 \pm 6.649e-05$</td></td<>	1.5	50	50	0.00525498	$0.01302 \pm 6.649e-05$
1.520050 11.6536 0.2195 ± 0.0006711 1.530050 22.5508 0.07353 ± 0.0003291 1.550050 67.2866 $0.0139 \pm 6.13e-05$ 1.5100050 196.96 $0.001209 \pm 7.038e-06$ 1.5150050 315.045 $0.0002109 \pm 8.631e-07$ 1.5100150 0.011079 $0.0006295 \pm 3.008e-06$ 1.5150150 0.0172162 $0.000706 \pm 3.661e-06$ 1.5200150 0.0240529 $0.00086 \pm 3.608e-06$ 1.5300150 0.0428723 $0.003751 \pm 1.304e-05$ 1.5500150 48.1013 $0.01046 \pm 4.013e-05$ 1.51000150 186.49 $0.001072 \pm 4.469e-06$ 1.51500150 307.963 $0.0001931 \pm 1.022e-06$ 1.5200300 0.0240529 $7.176e-05 \pm 3.641e-07$ 1.5300300 0.0428723 $8.3e-05 \pm 3.627e-07$ 1.5500300 25.183 $0.000155 \pm 6.658e-07$ 1.51500300 25.183 $0.0001529 \pm 7.694e-07$ 1.5500500 25.183 $9.099e-06 \pm 4.301e-08$ 1.51500500 25.183 $9.099e-06 \pm 4.301e-08$ 1.51500500 237.259 $8.736e-05 \pm 2.699e-07$ 1.51500500 237.259 $8.736e-05 \pm 4.268e-07$ 2.101 1.49727 82.65 ± 0.3408 2.201 3.13828 $43.1 \pm$	1.5	100	50	0.011079	0.07677 ± 0.0002445
1.53005022.5508 0.07353 ± 0.0003291 1.550050 67.2866 $0.0139 \pm 6.13e-05$ 1.5100050 196.96 $0.001209 \pm 7.038e-06$ 1.5150050 315.045 $0.0002109 \pm 8.631e-07$ 1.5100 150 0.011079 $0.0006295 \pm 3.008e-06$ 1.5150 150 0.0172162 $0.000706 \pm 3.661e-06$ 1.5200 150 0.0240529 $0.00086 \pm 3.608e-06$ 1.5300 150 0.0428723 $0.003751 \pm 1.304e-05$ 1.5500 150 48.1013 $0.01046 \pm 4.013e-05$ 1.51000 150 186.49 $0.001072 \pm 4.469e-06$ 1.51500 150 307.963 $0.0001931 \pm 1.022e-06$ 1.5200 300 0.0240529 $7.176e-05 \pm 3.641e-07$ 1.5300 300 0.0428723 $8.3e-05 \pm 3.627e-07$ 1.5500 300 25.183 $0.000155 \pm 6.658e-07$ 1.51500 300 25.183 $0.000155 \pm 6.658e-07$ 1.51500 300 25.183 $0.0001529 \pm 7.694e-07$ 1.51500 300 285.036 $0.0001529 \pm 7.694e-07$ 1.51500 500 25.183 $9.099e-06 \pm 4.301e-08$ 1.51500 500 25.183 $9.099e-06 \pm 4.301e-08$ 1.51500 500 237.259 $8.736e-05 \pm 2.699e-07$ 1.51500 500 237.259 $8.736e-05 \pm 4.268e-07$ 2. <t< td=""><td>1.5</td><td>150</td><td>50</td><td>5.57786</td><td>0.5195 ± 0.001577</td></t<>	1.5	150	50	5.57786	0.5195 ± 0.001577
1.550050 67.2866 $0.0139 \pm 6.13e-05$ 1.5 1000 50 196.96 $0.001209 \pm 7.038e-06$ 1.5 1500 50 315.045 $0.0002109 \pm 8.631e-07$ 1.5 100 150 0.011079 $0.0006295 \pm 3.008e-06$ 1.5 150 150 0.0172162 $0.000706 \pm 3.661e-06$ 1.5 200 150 0.0240529 $0.00086 \pm 3.608e-06$ 1.5 300 150 0.0428723 $0.003751 \pm 1.304e-05$ 1.5 500 150 48.1013 $0.01046 \pm 4.013e-05$ 1.5 1000 150 186.49 $0.001072 \pm 4.469e-06$ 1.5 1500 150 307.963 $0.0001931 \pm 1.022e-06$ 1.5 200 300 0.0240529 $7.176e-05 \pm 3.641e-07$ 1.5 300 300 0.0428723 $8.3e-05 \pm 3.627e-07$ 1.5 500 300 25.183 $0.000155 \pm 6.658e-07$ 1.5 1500 300 25.183 $0.000155 \pm 6.658e-07$ 1.5 1500 300 285.036 $0.0001529 \pm 7.694e-07$ 1.5 500 500 25.183 $9.099e-06 \pm 4.301e-08$ 1.5 1500 500 25.183 $9.099e-06 \pm 4.301e-08$ 1.5 1500 500 237.259 $8.736e-05 \pm 2.699e-07$ 1.5 1500 500 237.259 $8.736e-05 \pm 4.268e-07$ 2. 10 1 1.49727 82.65 ± 0.3408 2. 20 1 3.13828 43.1 ± 0.1487 <td>1.5</td> <td>200</td> <td>50</td> <td>11.6536</td> <td>0.2195 ± 0.0006711</td>	1.5	200	50	11.6536	0.2195 ± 0.0006711
1.5100050196.96 $0.001209 \pm 7.038e-06$ 1.5150050 315.045 $0.0002109 \pm 8.631e-07$ 1.5100150 0.011079 $0.0006295 \pm 3.008e-06$ 1.5150150 0.0172162 $0.000706 \pm 3.661e-06$ 1.5200150 0.0240529 $0.00086 \pm 3.608e-06$ 1.5300150 0.0428723 $0.003751 \pm 1.304e-05$ 1.5500150 48.1013 $0.01046 \pm 4.013e-05$ 1.51000150 186.49 $0.001072 \pm 4.469e-06$ 1.51500150 307.963 $0.0001931 \pm 1.022e-06$ 1.5200300 0.0240529 $7.176e-05 \pm 3.641e-07$ 1.5300300 0.0428723 $8.3e-05 \pm 3.627e-07$ 1.5500300 25.183 $0.000155 \pm 6.658e-07$ 1.51500300 285.036 $0.0001529 \pm 7.694e-07$ 1.51500300 285.036 $0.0001529 \pm 7.694e-07$ 1.51500500 25.183 $9.099e-06 \pm 4.301e-08$ 1.51500500 25.183 $9.099e-06 \pm 4.301e-08$ 1.51500500 237.259 $8.736e-05 \pm 4.268e-07$ 2.101 1.49727 82.65 ± 0.3408 2.201 3.13828 43.1 ± 0.1487	1.5	300	50	22.5508	0.07353 ± 0.0003291
1.5150050315.045 $0.0002109 \pm 8.631e-07$ 1.5100150 0.011079 $0.0006295 \pm 3.008e-06$ 1.5150150 0.0172162 $0.000706 \pm 3.661e-06$ 1.5200150 0.0240529 $0.00086 \pm 3.608e-06$ 1.5300150 0.0428723 $0.003751 \pm 1.304e-05$ 1.5500150 48.1013 $0.01046 \pm 4.013e-05$ 1.51000150 186.49 $0.001072 \pm 4.469e-06$ 1.51500150 307.963 $0.0001931 \pm 1.022e-06$ 1.5200300 0.0240529 $7.176e-05 \pm 3.641e-07$ 1.5300300 0.0428723 $8.3e-05 \pm 3.627e-07$ 1.5500300 25.183 $0.000155 \pm 6.658e-07$ 1.51500300 25.183 $0.000155 \pm 6.658e-07$ 1.51500300 285.036 $0.0001529 \pm 7.694e-07$ 1.5500500 25.183 $9.099e-06 \pm 4.301e-08$ 1.51000500 108.775 $5.335e-05 \pm 2.699e-07$ 1.51500500 237.259 $8.736e-05 \pm 4.268e-07$ 2.101 1.49727 82.65 ± 0.3408 2.201 3.13828 43.1 ± 0.1487	1.5	500	50	67.2866	$0.0139 \pm 6.13e-05$
1.51001500.0110790.0006295 \pm 3.008e-061.51501500.01721620.000706 \pm 3.661e-061.52001500.02405290.00086 \pm 3.608e-061.53001500.04287230.003751 \pm 1.304e-051.550015048.10130.01046 \pm 4.013e-051.51000150186.490.001072 \pm 4.469e-061.51500150307.9630.0001931 \pm 1.022e-061.52003000.02405297.176e-05 \pm 3.641e-071.53003000.04287238.3e-05 \pm 3.627e-071.550030025.1830.000155 \pm 6.658e-071.51000300154.6110.0007234 \pm 2.773e-061.51500300285.0360.0001529 \pm 7.694e-071.550050025.1839.099e-06 \pm 4.301e-081.51000500108.7755.335e-05 \pm 2.699e-071.51500500237.2598.736e-05 \pm 4.268e-072.1011.4972782.65 \pm 0.34082.2013.1382843.1 \pm 0.1487	1.5	1000	50	196.96	$0.001209 \pm 7.038e-06$
1.51501500.01721620.000706 \pm 3.661e-061.52001500.02405290.00086 \pm 3.608e-061.53001500.04287230.003751 \pm 1.304e-051.550015048.10130.01046 \pm 4.013e-051.51000150186.490.001072 \pm 4.469e-061.51500150307.9630.0001931 \pm 1.022e-061.52003000.02405297.176e-05 \pm 3.641e-071.53003000.04287238.3e-05 \pm 3.627e-071.550030025.1830.000155 \pm 6.658e-071.51000300154.6110.0007234 \pm 2.773e-061.51500300285.0360.0001529 \pm 7.694e-071.550050025.1839.099e-06 \pm 4.301e-081.51000500108.7755.335e-05 \pm 2.699e-071.51500500237.2598.736e-05 \pm 4.268e-072.1011.4972782.65 \pm 0.34082.2013.1382843.1 \pm 0.1487	1.5	1500	50	315.045	$0.0002109 \pm 8.631e-07$
1.52001500.02405290.00086 \pm 3.608e-061.53001500.04287230.003751 \pm 1.304e-051.550015048.10130.01046 \pm 4.013e-051.51000150186.490.001072 \pm 4.469e-061.51500150307.9630.0001931 \pm 1.022e-061.52003000.02405297.176e-05 \pm 3.641e-071.53003000.04287238.3e-05 \pm 3.627e-071.550030025.1830.000155 \pm 6.658e-071.51000300154.6110.0007234 \pm 2.773e-061.51500300285.0360.0001529 \pm 7.694e-071.550050025.1839.099e-06 \pm 4.301e-081.51000500108.7755.335e-05 \pm 2.699e-071.51500500237.2598.736e-05 \pm 4.268e-072.1011.4972782.65 \pm 0.34082.2013.1382843.1 \pm 0.1487	1.5	100	150	0.011079	$0.0006295 \pm 3.008e-06$
1.53001500.04287230.003751 \pm 1.304e-051.550015048.10130.01046 \pm 4.013e-051.51000150186.490.001072 \pm 4.469e-061.51500150307.9630.0001931 \pm 1.022e-061.52003000.02405297.176e-05 \pm 3.641e-071.53003000.04287238.3e-05 \pm 3.627e-071.550030025.1830.000155 \pm 6.658e-071.51000300154.6110.0007234 \pm 2.773e-061.51500300285.0360.0001529 \pm 7.694e-071.550050025.1839.099e-06 \pm 4.301e-081.51000500108.7755.335e-05 \pm 2.699e-071.51500500237.2598.736e-05 \pm 4.268e-072.1011.4972782.65 \pm 0.34082.2013.1382843.1 \pm 0.1487	1.5	150	150	0.0172162	$0.000706 \pm 3.661e-06$
1.5500150 48.1013 $0.01046 \pm 4.013e-05$ 1.51000150 186.49 $0.001072 \pm 4.469e-06$ 1.51500150 307.963 $0.0001931 \pm 1.022e-06$ 1.5200300 0.0240529 $7.176e-05 \pm 3.641e-07$ 1.5300300 0.0428723 $8.3e-05 \pm 3.627e-07$ 1.5500300 25.183 $0.000155 \pm 6.658e-07$ 1.51000300 154.611 $0.0007234 \pm 2.773e-06$ 1.51500300 285.036 $0.0001529 \pm 7.694e-07$ 1.5500500 25.183 $9.099e-06 \pm 4.301e-08$ 1.51000500 108.775 $5.335e-05 \pm 2.699e-07$ 1.51500500 237.259 $8.736e-05 \pm 4.268e-07$ 2.101 1.49727 82.65 ± 0.3408 2.201 3.13828 43.1 ± 0.1487	1.5	200	150	0.0240529	$0.00086 \pm 3.608 e\text{-}06$
1.51000150186.49 $0.001072 \pm 4.469e-06$ 1.51500150 307.963 $0.0001931 \pm 1.022e-06$ 1.5200300 0.0240529 $7.176e-05 \pm 3.641e-07$ 1.5300300 0.0428723 $0.000155 \pm 6.658e-07$ 1.5500300 25.183 $0.000155 \pm 6.658e-07$ 1.51000300 154.611 $0.0007234 \pm 2.773e-06$ 1.51500300 285.036 $0.0001529 \pm 7.694e-07$ 1.5500500 25.183 $9.099e-06 \pm 4.301e-08$ 1.51000500 108.775 $5.335e-05 \pm 2.699e-07$ 1.51500500 237.259 $8.736e-05 \pm 4.268e-07$ 2.101 1.49727 82.65 ± 0.3408 2.201 3.13828 43.1 ± 0.1487	1.5	300	150	0.0428723	$0.003751 \pm 1.304e-05$
1.51500150307.9630.0001931 \pm 1.022e-061.52003000.0240529 $7.176e-05 \pm 3.641e-07$ 1.53003000.0428723 $8.3e-05 \pm 3.627e-07$ 1.550030025.1830.000155 \pm 6.658e-071.51000300154.6110.0007234 \pm 2.773e-061.51500300285.0360.0001529 \pm 7.694e-071.550050025.1839.099e-06 \pm 4.301e-081.51000500108.7755.335e-05 \pm 2.699e-071.51500500237.2598.736e-05 \pm 4.268e-072.1011.4972782.65 \pm 0.34082.2013.1382843.1 \pm 0.1487	1.5	500	150	48.1013	$0.01046 \pm 4.013e-05$
1.52003000.0240529 $7.176e-05 \pm 3.641e-07$ 1.53003000.0428723 $8.3e-05 \pm 3.627e-07$ 1.5500300 25.183 0.000155 $\pm 6.658e-07$ 1.51000300 154.611 0.0007234 $\pm 2.773e-06$ 1.51500300 285.036 0.0001529 $\pm 7.694e-07$ 1.5500500 25.183 9.099e-06 $\pm 4.301e-08$ 1.51000500 108.775 $5.335e-05 \pm 2.699e-07$ 1.51500500 237.259 $8.736e-05 \pm 4.268e-07$ 2.101 1.49727 82.65 ± 0.3408 2.201 3.13828 43.1 ± 0.1487	1.5	1000	150	186.49	$0.001072 \pm 4.469e-06$
1.53003000.04287238.3e-05 \pm 3.627e-071.550030025.1830.000155 \pm 6.658e-071.51000300154.6110.0007234 \pm 2.773e-061.51500300285.0360.0001529 \pm 7.694e-071.550050025.1839.099e-06 \pm 4.301e-081.51000500108.7755.335e-05 \pm 2.699e-071.51500500237.2598.736e-05 \pm 4.268e-072.1011.4972782.65 \pm 0.34082.2013.1382843.1 \pm 0.1487	1.5	1500	150	307.963	$0.0001931 \pm 1.022e-06$
1.550030025.1830.000155 \pm 6.658e-071.51000300154.6110.0007234 \pm 2.773e-061.51500300285.0360.0001529 \pm 7.694e-071.550050025.1839.099e-06 \pm 4.301e-081.51000500108.7755.335e-05 \pm 2.699e-071.51500500237.2598.736e-05 \pm 4.268e-072.1011.4972782.65 \pm 0.34082.2013.1382843.1 \pm 0.1487	1.5	200	300		$7.176e-05 \pm 3.641e-07$
1.51000300154.6110.0007234 \pm 2.773e-061.51500300285.0360.0001529 \pm 7.694e-071.550050025.1839.099e-06 \pm 4.301e-081.51000500108.7755.335e-05 \pm 2.699e-071.51500500237.2598.736e-05 \pm 4.268e-072.1011.4972782.65 \pm 0.34082.2013.1382843.1 \pm 0.1487	1.5	300	300	0.0428723	$8.3e-05 \pm 3.627e-07$
1.51500300285.0360.0001529 \pm 7.694e-071.550050025.1839.099e-06 \pm 4.301e-081.51000500 108.775 5.335e-05 \pm 2.699e-071.51500500 237.259 $8.736e$ -05 \pm 4.268e-072.101 1.49727 82.65 ± 0.3408 2.201 3.13828 43.1 ± 0.1487	1.5	500	300	25.183	$0.000155 \pm 6.658e-07$
1.550050025.1839.099e-06 \pm 4.301e-081.51000500 108.775 5.335e-05 \pm 2.699e-071.51500500 237.259 $8.736e-05 \pm 4.268e-07$ 2.101 1.49727 82.65 ± 0.3408 2.201 3.13828 43.1 ± 0.1487	1.5	1000	300	154.611	$0.0007234 \pm 2.773e-06$
1.51000500 108.775 $5.335e-05 \pm 2.699e-07$ 1.51500500 237.259 $8.736e-05 \pm 4.268e-07$ 2.101 1.49727 82.65 ± 0.3408 2.201 3.13828 43.1 ± 0.1487	1.5	1500	300	285.036	$0.0001529 \pm 7.694e$ -07
1.51500500237.2598.736e-05 \pm 4.268e-072.1011.4972782.65 \pm 0.34082.2013.1382843.1 \pm 0.1487	1.5	500	500	25.183	$9.099e-06 \pm 4.301e-08$
2. 10 1 1.49727 82.65 \pm 0.3408 2. 20 1 3.13828 43.1 \pm 0.1487	1.5	1000	500	108.775	$5.335e-05 \pm 2.699e-07$
2. 20 1 3.13828 43.1 ± 0.1487	1.5	1500	500	237.259	$8.736\text{e-}05 \pm 4.268\text{e-}07$
	2.	10	1	1.49727	82.65 ± 0.3408
2. 50 1 7.948 11.84 \pm 0.04278	2.	20	1	3.13828	43.1 ± 0.1487
<u> </u>	2.	50	1	7.948	11.84 ± 0.04278

Table C.1 – continued from previous page

Coupling (g)	m_{Phi} [GeV]		Γ_{min} [GeV]	σ
2.	100	1	15.9256	2.712 ± 0.01209
2.	150	1	23.8975	0.9056 ± 0.004237
2.	200	1	31.869	0.3952 ± 0.001653
2.	300	1	47.8195	0.132 ± 0.0004713
2.	500	1	124.345	0.02461 ± 0.0001101
2.	1000	1	352.532	$0.002071 \pm 1.061e-05$
2.	1500	1	561.669	$0.0003815 \pm 1.4e-06$
2.	10	10	0.000253248	1.627 ± 0.005672
2.	20	10	0.00280417	5.528 ± 0.03152
2.	50	10	6.13579	11.98 ± 0.04005
2.	100	10	14.9899	2.696 ± 0.01091
2.	150	10	23.2701	0.8981 ± 0.004067
2.	200	10	31.3975	0.3921 ± 0.001675
2.	300	10	47.5047	0.1312 ± 0.0005524
2.	500	10	124.156	0.02454 ± 0.0001302
2.	1000	10	352.437	$0.002051 \pm 9.73e-06$
2.	1500	10	561.606	$0.0003797 \pm 1.522e-06$
2.	10	50	0.000253248	0.03397 ± 0.0001354
2.	20	50	0.00280417	0.03452 ± 0.0001623
2.	50	50	0.00934219	0.04088 ± 0.0001623
2.	100	50	0.0196961	0.24 ± 0.0008579
2.	150	50	9.9162	0.8991 ± 0.002903
2.	200	50	20.7176	0.382 ± 0.001411
2.	300	50	40.0903	0.1287 ± 0.0005596
2.	500	50	119.621	0.02328 ± 0.0001255
2.	1000	50	350.151	$0.001995 \pm 1.184 e$ -05
2.	1500	50	560.08	$0.0003671 \pm 1.741e-06$
2.	10	150	0.000253248	0.001822 ± 7.946 e-06
2.	20	150	0.00280417	$0.001842 \pm 8.453 e\text{-}06$
2.	50	150	0.00934219	$0.00187 \pm 8.818 \text{e-}06$
2.	100	150	0.0196961	0.001985 ± 8.101 e-06
2.	150	150	0.0306067	$0.002231 \pm 1.131e-05$
2.	200	150	0.0427607	0.002694 \pm 1.215e-05
2.	300	150	0.0762174	$0.01186 \pm 4.862 e - 05$
2.	500	150	85.5134	$0.01769 \pm 8.02e$ -05
2.	1000	150	331.538	$0.001716 \pm 7.617e-06$
2.	1500	150	547.49	$0.0003242 \pm 1.537e-06$
2.	100	300	0.0196961	$0.0002092 \pm 8.197 e$ -07
2.	150	300	0.0306067	$0.0002152 \pm 8.37e-07$
2.	200	300	0.0427607	$0.0002275 \pm 8.607e$ -07
-				

Table C.1 – continued from previous page

Coupling (g)	m_{Phi} [GeV]		Γ_{min} [GeV]	σ
2.	300	300	0.0762174	0.0002609 ± 1.05e-06
2.	500	300	44.7698	$0.0004931 \pm 2.01e-06$
2.	1000	300	274.865	$0.001119 \pm 5.167e-06$
2.	1500	300	506.731	$0.0002432 \pm 1.053e-06$
2.	300	500	0.0762174	2.367e-05 ± 1.206e-07
2.	500	500	44.7698	$2.871e-05 \pm 1.09e-07$
2.	1000	500	193.378	$0.000131 \pm 5.569 e$ -07
2.	1500	500	421.793	$0.0001323 \pm 5.222e$ -07
2.5	10	1	2.33949	128.4 ± 0.4393
2.5	20	1	4.90356	65.92 ± 0.2248
2.5	50	1	12.4187	17.77 ± 0.0663
2.5	100	1	24.8838	4.051 ± 0.01562
2.5	150	1	37.3398	1.364 ± 0.004927
2.5	200	1	49.7953	0.6008 ± 0.002928
2.5	300	1	74.718	0.2036 ± 0.0008994
2.5	500	1	194.29	0.03629 ± 0.0001865
2.5	1000	1	550.831	$0.002918 \pm 1.235 e$ -05
2.5	1500	1	877.608	$0.0005639 \pm 2.327e-06$
2.5	10	10	0.0003957	3.918 ± 0.0159
2.5	20	10	0.00438152	13.54 ± 0.05349
2.5	50	10	9.58718	18.03 ± 0.06068
2.5	100	10	23.4217	4.025 ± 0.01458
2.5	150	10	36.3595	1.36 ± 0.00698
2.5	200	10	49.0586	0.5979 ± 0.002445
2.5	300	10	74.2262	0.2016 ± 0.0006995
2.5	500	10	193.994	0.03579 ± 0.0001738
2.5	1000	10	550.683	$0.002902 \pm 1.515 e - 05$
2.5	1500	10	877.509	$0.0005651 \pm 2.275e-06$
2.5	10	50	0.0003957	0.08298 ± 0.000365
2.5	20	50	0.00438152	0.08474 ± 0.0003631
2.5	50	50	0.0145972	0.09986 ± 0.000455
2.5	100	50	0.0307751	0.5855 ± 0.001667
2.5	150	50	15.4941	1.359 ± 0.005802
2.5	200	50	32.3712	0.5728 ± 0.002188
2.5	300	50	62.6411	0.1938 ± 0.0008665
2.5	500	50	186.907	0.03384 ± 0.0001589
2.5	1000	50	547.111	$0.002773 \pm 1.645e-05$
2.5	1500	50	875.125	$0.0005349 \pm 3.534e-06$
2.5	10	150	0.0003957	$0.004461 \pm 1.951e-05$
2.5	20	150	0.00438152	0.004473 ± 2.159e-05

Table C.1 – continued from previous page

Coupling (g)	m_{Phi} [GeV]	m_{χ} [GeV]	Γ_{min} [GeV]	σ
2.5	50	150	0.0145972	$0.00451 \pm 1.808 e - 05$
2.5	100	150	0.0307751	$0.00486 \pm 1.984 e\text{-}05$
2.5	150	150	0.0478229	$0.00548 \pm 2.35 \text{e-}05$
2.5	200	150	0.0668136	$0.006545 \pm 2.81\text{e-}05$
2.5	300	150	0.11909	0.02878 ± 0.0001168
2.5	500	150	133.615	0.02572 ± 0.00011
2.5	1000	150	518.027	$0.002339 \pm 1.101e-05$
2.5	1500	150	855.453	$0.0004622 \pm 2.297e\text{-}06$
2.5	100	300	0.0307751	$0.0005104 \pm 2.62e-06$
2.5	150	300	0.0478229	$0.000526 \pm 2.091e$ -06
2.5	200	300	0.0668136	$0.0005503 \pm 2.402e$ -06
2.5	300	300	0.11909	$0.0006368 \pm 2.911e-06$
2.5	500	300	69.9528	$0.001197 \pm 4.697 e$ -06
2.5	1000	300	429.476	$0.001499 \pm 6.445 e$ -06
2.5	1500	300	791.767	$0.0003277 \pm 1.439e-06$
2.5	300	500	0.11909	$5.773 \text{e-}05 \pm 2.645 \text{e-}07$
2.5	500	500	69.9528	$6.973e-05 \pm 3.037e-07$
2.5	1000	500	302.152	$0.0002498 \pm 1.042e$ -06
2.5	1500	500	659.052	$0.000172 \pm 8.531e-07$
3.	10	1	3.36886	185.9 ± 0.8608
3.	20	1	7.06112	92.49 ± 0.3581
3.	50	1	17.883	24.38 ± 0.08507
3.	100	1	35.8327	5.551 ± 0.02275
3.	150	1	53.7693	1.878 ± 0.008801
3.	200	1	71.7052	0.8398 ± 0.004651
3.	300	1	107.594	0.2856 ± 0.001301
3.	500	1	279.777	0.04861 ± 0.0002143
3.	1000	1	793.196	$0.003716 \pm 1.874e-05$
3.	1500	1	1263.76	$0.0007294 \pm 3.217e-06$
3.	10	10	0.000569808	8.181 ± 0.03184
3.	20	10	0.00630938	28.05 ± 0.09412
3.	50	10	13.8055	24.97 ± 0.07128
3.	100	10	33.7272	5.485 ± 0.01916
3.	150	10	52.3576	1.858 ± 0.007406
3.	200	10	70.6443	0.8336 ± 0.003435
3.	300	10	106.886	0.2832 ± 0.001293
3.	500	10	279.352	0.04802 ± 0.0003129
3.	1000	10	792.983	$0.003669 \pm 1.542e-05$
3.	1500	10	1263.61	$0.0007221 \pm 3.036e-06$
3.	10	50	0.000569808	0.1714 ± 0.0007653

Table C.1 – continued from previous page

Coupling (g)	m_{Phi} [GeV]	m_{χ} [GeV]	Γ_{min} [GeV]	σ
3.	20	50	0.00630938	0.1751 ± 0.000689
3.	50	50	0.0210199	0.2073 ± 0.001019
3.	100	50	0.0443162	1.21 ± 0.003153
3.	150	50	22.3114	1.896 ± 0.007571
3.	200	50	46.6146	0.787 ± 0.002939
3.	300	50	90.2031	0.2685 ± 0.001344
3.	500	50	269.146	0.04468 ± 0.0002221
3.	1000	50	787.84	0.003505 ± 1.861 e-05
3.	1500	50	1260.18	$0.0006823 \pm 3.857e\text{-}06$
3.	10	150	0.000569808	$0.009285 \pm 4.234e-05$
3.	20	150	0.00630938	$0.00924 \pm 4.234 e$ -05
3.	50	150	0.0210199	$0.009462 \pm 3.85 \text{e-}05$
3.	100	150	0.0443162	$0.01017 \pm 4.443e-05$
3.	150	150	0.068865	0.01124 \pm 5.221e-05
3.	200	150	0.0962116	$0.01366 \pm 6.834 e$ -05
3.	300	150	0.171489	0.05937 ± 0.0002495
3.	500	150	192.405	0.03448 ± 0.0001467
3.	1000	150	745.959	$0.00288 \pm 1.359 \text{e-}05$
3.	1500	150	1231.85	$0.0005735 \pm 3.925e-06$
3.	50	300	0.0210199	$0.001039 \pm 3.982e-06$
3.	100	300	0.0443162	$0.001056 \pm 4.834e-06$
3.	150	300	0.068865	$0.001096 \pm 4.922e$ -06
3⋅	200	300	0.0962116	$0.001147 \pm 5.869e-06$
3⋅	300	300	0.171489	$0.001327 \pm 6.728e-06$
3⋅	500	300	100.732	$0.00245 \pm 9.636e-06$
3⋅	1000	300	618.446	$0.001853 \pm 7.863e-06$
3⋅	1500	300	1140.14	$0.0003934 \pm 2.083e-06$
3⋅	150	500	0.068865	$0.0001123 \pm 4.327e-07$
3.	200	500	0.0962116	$0.000114 \pm 5.127e-07$
3.	300	500	0.171489	$0.0001206 \pm 5.124e-07$
3.	500	500	100.732	$0.0001447 \pm 6.102e-07$
3.	1000	500	435.099	$0.0004016 \pm 1.656e-06$
3⋅	1500	500	949.035	$0.0002061 \pm 8.548e-07$
3.5	10	1	4.58539	257.5 ± 0.9241
3.5	20	1	9.61097	123.8 ± 0.4645
3.5	50	1	24.3407	31.59 ± 0.09614
3.5	100	1	48.7723	7.04 ± 0.02954
3.5	150	1	73.186	2.417 ± 0.01038
3.5	200	1	97.5987	1.089 ± 0.004308
3.5	300	1	146.447	0.3709 ± 0.001616

Table C.1 – continued from previous page

Coupling (g)	m_{Phi} [GeV]	m_{χ} [GeV]	Γ_{min} [GeV]	σ
3.5	500	1	380.808	0.06035 ± 0.0003762
3.5	1000	1	1079.63	$0.004345 \pm 2.711e-05$
3.5	1500	1	1720.11	$0.0008581 \pm 3.653e-06$
3.5	10	10	0.000775572	15.08 ± 0.0569
3.5	20	10	0.00858777	51.42 ± 0.1478
3.5	50	10	18.7909	32.56 ± 0.1113
3.5	100	10	45.9065	6.963 ± 0.03199
3.5	150	10	71.2646	2.38 ± 0.009493
3.5	200	10	96.1548	1.079 ± 0.004244
3.5	300	10	145.483	0.369 ± 0.001602
3.5	500	10	380.229	0.05978 ± 0.0003017
3.5	1000	10	1079.34	$0.004302 \pm 2.412e-05$
3.5	1500	10	1719.92	$0.0008525 \pm 3.878e-06$
3.5	10	50	0.000775572	0.3176 ± 0.001314
3.5	20	50	0.00858777	0.3229 ± 0.001215
3.5	50	50	0.0286105	0.3857 ± 0.001618
3.5	100	50	0.0603192	2.228 ± 0.00751
3.5	150	50	30.3684	2.477 ± 0.008787
3.5	200	50	63.4476	1.025 ± 0.003864
3.5	300	50	122.776	0.3483 ± 0.001614
3.5	500	50	366.338	0.05534 ± 0.0003035
3.5	1000	50	1072.34	$0.004076 \pm 2.371e-05$
3.5	1500	50	1715.24	$0.0008077 \pm 4.889e-06$
3.5	10	150	0.000775572	$0.01719 \pm 9.115 e-05$
3.5	20	150	0.00858777	$0.01719 \pm 8.334e-05$
3.5	50	150	0.0286105	$0.01754 \pm 8.239e-05$
3.5	100	150	0.0603192	$0.01855 \pm 8.371e-05$
3.5	150	150	0.0937329	0.02099 ± 0.0001038
3.5	200	150	0.130955	0.0252 ± 0.0001138
3.5	300	150	0.233416	0.1096 ± 0.0006465
3.5	500	150	261.885	0.04374 ± 0.0002091
3.5	1000	150	1015.33	$0.00334 \pm 1.751e-05$
3.5	1500	150	1676.69	$0.0006583 \pm 3.614e-06$
3.5	10	300	0.000775572	$0.001925 \pm 9.279e-06$
3.5	20	300	0.00858777	$0.001916 \pm 1.026e-05$
3.5	50	300	0.0286105	0.001918 ± 8.166 e-06
3.5	100	300	0.0603192	$0.001958 \pm 7.426e-06$
3.5	150	300	0.0937329	$0.002036 \pm 8.81e-06$
3.5	200	300	0.130955	$0.002123 \pm 8.379e-06$
3.5	300	300	0.233416	$0.002448 \pm 9.259e-06$

Table C.1 – continued from previous page

Coupling (g)	m_{Phi} [GeV]	m_{χ} [GeV]	Γ_{min} [GeV]	σ
3.5	500	300	137.107	0.004413 ± 2.588e-05
3.5	1000	300	841.774	$0.002184 \pm 1.014e-05$
3.5	1500	300	1551.86	$0.0004471 \pm 2.349e-06$
3.5	10	500	0.000775572	0.0002016 ± 7.906 e-07
3.5	20	500	0.00858777	$0.0002011 \pm 9.138e-07$
3.5	50	500	0.0286105	$0.0002018 \pm 9.929 e$ -07
3.5	100	500	0.0603192	0.0002033 ± 8.104 e-07
3.5	150	500	0.0937329	0.0002067 ± 8.026 e-07
3.5	200	500	0.130955	$0.0002106 \pm 8.439e-07$
3.5	300	500	0.233416	$0.0002225 \pm 9.256e-07$
3.5	500	500	137.107	$0.0002686 \pm 1.162e-06$
3.5	1000	500	592.219	$0.0005877 \pm 2.823e-06$
3.5	1500	500	1291.74	$0.0002318 \pm 1.11e-06$

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