Version 0.1 DRAFT	
ATLAS+CMS DARK MATTER FORUM RE TIONS	COMMENDA-
Author/contributor list to be added as document is finalized.	
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, Introduction

 $_{8}$ This is a citation test [HK11].

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Overall choices for simplified models

- General topics:
- choice of Dark Matter type: Dirac (unless specified otherwise) and what we might be missing
- MFV and what we might be missing

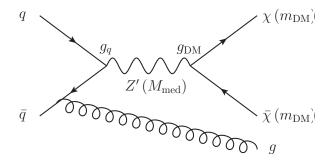


Figure 3.1: The diagram shows the pair production of dark matter particles in association with a parton from the initial state via an s-channel vector or axial-vector mediator. The process if specified by $(M_{\rm med}, m_{\rm DM}, g_{\rm DM}, g_{\rm q})$, the mediator and dark matter masses, and the mediator couplings to dark matter and quarks respectively.

Recommended models for all MET+X analyses

3.1 Vector and axial vector mediator, s-channel exchange

- 8 There are several matrix element implementations of the s-channel
- vector mediated DM production. This is available in POWHEG,
- 20 MADGRAPH and also MCFM. The implementation in POWHEG
- generates DM pair production with 1 parton at next-to-leading or-
- der (NLO), whilst MADGRAPH and MCFM are at leading order
- ²³ (LO). As shown in POWHEG Ref. [HKR13], including NLO correc-
- tions result in an enhancement in the cross section as compared to
- LO and though this is not significant, it does lead to a substantial
- reduction in the dependence on the choice of the renormalization
- and factorization scale and hence the theoretical uncertainty on the
- signal prediction. Since NLO calculations are available for the pro-
- 29 cess in POWHEG, we recommend to proceed with POWHEG as the
- 30 generator of choice.

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- We consider the case of a dark matter particle that is a Dirac
- fermion and where the production proceeds via the exchange of a
- spin-1 s-channel mediator. We consider the following interactions
- between the DM and SM fields including a vector mediator with:
 - (a) vector couplings to DM and SM,
- (b) axial-vector couplings to DM and SM.

The corresponding Lagrangians are

$$\mathcal{L}_{\text{vector}} = \sum_{q} g_{q} Z'_{\mu} \bar{q} \gamma^{\mu} q + g_{\text{DM}} Z'_{\mu} \bar{\chi} \gamma^{\mu} \chi \tag{3.1}$$

$$\mathcal{L}_{\text{axial-vector}} = \sum_{q} g_{q} Z'_{\mu} \bar{q} \gamma^{\mu} \gamma^{5} q + g_{\text{DM}} Z'_{\mu} \bar{\chi} \gamma^{\mu} \gamma^{5} \chi \tag{3.2}$$

where the coupling extends over all the quarks and universal cou-

- plings are assumed for all the quarks. It is also possible to consider
- another model in which mixed vector and axial-vector couplings
- are considered, for instance the couplings to the quarks are vector
- whereas those to DM are axial-vector. As a starting point, we con-
- sider only the models with the vector couplings only and axial vector
- couplings only.
- We assume that no additional visible or invisible decays contribute
- to the width of the mediator, this is referred to as the minimal width
- and it is defined as follows for the vector and axial-vector models.

$$\Gamma_{\min} = \Gamma_{\bar{\chi}\chi} + \sum_{q} \Gamma_{\bar{q}q} \tag{3.3}$$

- where the individual contributions to this from the partial width are
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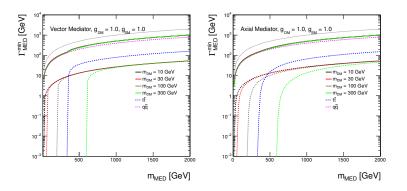
$$\Gamma_{\bar{\chi}\chi}^{V} = \frac{g_{\rm DM}^{2} M_{\rm med}}{12\pi} \left(1 + \frac{2m_{\rm DM}^{2}}{M_{\rm med}^{2}} \right) \sqrt{1 - \frac{4m_{\rm DM}^{2}}{M_{\rm med}^{2}}}$$
(3.4)

$$\Gamma_{\bar{q}q}^{V} = \frac{3g_{q}^{2}M_{\text{med}}}{12\pi} \left(1 + \frac{2m_{q}^{2}}{M_{\text{med}}^{2}}\right) \sqrt{1 - \frac{4m_{q}^{2}}{M_{\text{med}}^{2}}}$$
(3.5)

$$\Gamma_{\bar{\chi}\chi}^{A} = \frac{g_{\rm DM}^{2} M_{\rm med}}{12\pi} \left(1 - \frac{4m_{\rm DM}^{2}}{M_{\rm med}^{2}} \right)^{3/2}$$
(3.6)

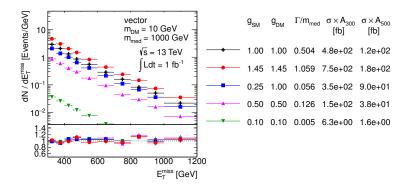
$$\Gamma_{\bar{q}q}^{A} = \frac{3g_{q}^{2}M_{\text{med}}}{12\pi} \left(1 - \frac{4m_{q}^{2}}{M_{\text{med}}^{2}}\right)^{3/2}.$$
(3.7)

- Note the color factor 3 in the quark terms. Figure 3.2 shows the min-
- 50 imal width as a function of mediator mass for both vector and axial-
- vector mediators assuming couplings of 1. With this choice of the
- 52 couplings, the dominant contribution to the minimal width comes
- from the quarks due to the color factor enhancement.
- The simplified models described here have four free parameters:
- mediator mass M_{med} , Dark Matter mass m_{DM} , coupling of the medi-
- ator to quarks g_q and coupling of the mediator to Dark Matter g_{DM} .
- 57 In order to determine an optimal choice of the parameter grid for
- presentation of the early Run-2 results, dependencies of the kinematic
- 59 quantities and cross sections on the individual parameters need to be
- studied. The following paragraphs list the main observations from



the scans over the parameters that support the final proposal for the parameter grid.

Scan over the couplings Figure 3.3 reveals there are no differences in the shape of the E_T distribution among the samples where the pair of 64 10 GeV Dark Matter particles are produced on-shell from the media-65 tor of 1 TeV, generated with different choice of the coupling strength. The considered coupling values range from 0.1 to 1.45, where the latter value approximates the maximum allowed coupling value, holding $g_q = g_{DM}$, such that $\Gamma_{min} < M_{med}$. Based on similar plots for different choices of mediator and Dark Matter masses, it is concluded that the shapes of kinematic distributions are not altered neither for the on-shell Dark Matter production where $M_{\rm med} > 2m_{\rm DM}$, nor for 72 the off-shell Dark Matter production where $M_{\rm med} < 2m_{\rm DM}$. Only the cross sections change. Differences in kinematic distributions are expected only close to the transition region where both on-shell and off-shell regimes mix.



The only place where special care needs to be taken are extremely heavy and narrow mediators, in other words with low couplings. Figure 3.4 suggests a change in the shape of the E_T distribution for 5 TeV mediator once $\Gamma_{\min}/M_{\mathrm{med}}$ gets down to the order of percent or

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Figure 3.2: Minimal width as a function of mediator mass for vector and axial-vector mediator assuming couplings of 1. The total width is shown as solid lines for Dark Matter masses of 10 GeV, 30 GeV, 100 GeV and 300 GeV in black, red, brown and green, respectively. The individual contributions from Dark Matter are indicated by dotted lines with the same colors. The contribution from all quarks but top is shown as magenta dotted line and the contribution from top quarks only is illustrated by the dotted blue line. The dotted black line shows the extreme case $\Gamma_{\min} = M_{\text{med}}$.

Figure 3.3: Scan over couplings. The E_T distribution is compared for the vector mediator models using the parameters as indicated. Ratios of the normalized distributions with respect to the first one are shown. A_{300} and A_{500} in the table denote the acceptance of the $E_T > 300\,\text{GeV}$ and $E_T > 500\,\text{GeV}$ cut, respectively.

below. This, however, does not come from physics as it is a feature of the generator implementation, where a cutoff for the regions far away 82 from the mediator mass is often used. This is illustrated in Fig. 3.5 showing the invariant mass of the Dark Matter pair in the samples generated for 7 TeV mediator with different coupling strength. In 85 all cases, it is expected to observe a peak around the mediator mass with a tail extending to $m_{\bar{\chi}\chi} \to 0$, significantly enhanced by parton distribution functions at low Bjorken x. For coupling strength 1 and 3, the massive enhancement at $m_{\bar{\chi}\chi} \to 0$ implies the resonant production at $m_{\bar{\chi}\chi} = 7 \text{ TeV}$ is statistically suppressed such that barely any events are generated there. However, for narrower mediators 91 with couplings below 1, the peak around 7 TeV is clearly visible in the generated sample and the dominant tail at $m_{\bar{\chi}\chi} \to 0$ is artificially cut off, leading to unphysical cross section predictions and kinematic 94 shapes. This explains why the sample with the narrowest mediator in Fig. 3.4 is heavily suppressed in terms of production cross section and also gives different E_T shape. In general, for such extreme parameter choices the EFT model should give the correct answer. [TODO: add results of ongoing study.]

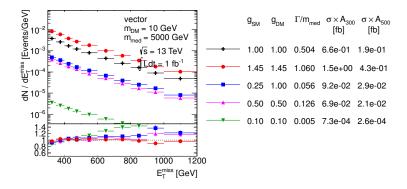


Figure 3.4: Scan over couplings. The E_T distribution is compared for the vector mediator models using the parameters as indicated. Ratios of the normalized distributions with respect to the first one are shown. A_{300} and A_{500} in the table denote the acceptance of the $E_T > 300 \,\text{GeV}$ and $E_T > 500 \,\text{GeV}$ cut, respectively.

Scan over the Dark Matter mass For the fixed mediator mass and couplings, both the cross section and the kinematic distributions remain similar for different Dark Matter masses as long as $M_{\text{med}} > 2m_{\text{DM}}$. 102 This is illustrated in Fig. 3.6 on an example of 1 TeV mediator and 103 Dark Matter masses ranging from 10 GeV to 300 GeV. It is observed that the cross section decreases as the Dark Matter mass reaches 105 closer to $M_{\rm med}/2$. Once the Dark Matter pair is produced off-shell, 106 the cross section of such simplified model is suppressed and the E_T 107 spectrum hardens, as demonstrated with the choice of 1 TeV Dark Matter in the same plot. Figure 3.7 reveals the E_T spectrum hardens 109 further with increasing Dark Matter mass, accompanied by the grad-110 ual decrease of the cross section. From these observations one can conclude:

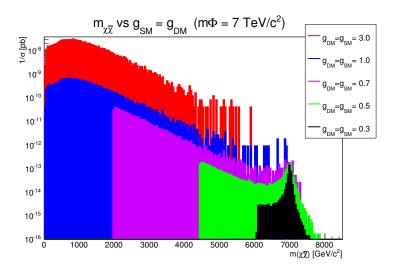


Figure 3.5: Invariant mass of the Dark Matter pair in the samples with $M_{\rm med} = 7 \, \text{TeV}$ and different coupling strengths.

A coarse binning along $m_{\rm DM}$ is sufficient at $M_{\rm med} \gg 2m_{\rm DM}$. 113

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- Finer binning is needed in order to capture the changes in the cross section and kinematic quantities close to the production threshold on both sides around $M_{\text{med}} = 2m_{\text{DM}}$.
- Due to the significant cross section suppression of the off-shell Dark Matter pair production, it is not necessary to populate the parameter space $M_{\rm med} \ll 2m_{\rm DM}$ since the LHC is not going to be able to probe the models there.

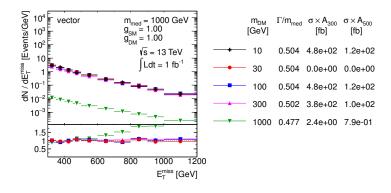


Figure 3.6: Scan over Dark Matter mass. The E_T distribution is compared for the vector mediator models using the parameters as indicated. Ratios of the normalized distributions with respect to the first one are shown. A_{300} and A_{500} in the table denote the acceptance of the $\not\!E_T > 300 \,\text{GeV}$ and $\not\!E_T > 500 \,\text{GeV}$ cut, respectively.

Scan over the mediator mass Changing the mediator mass for fixed Dark Matter mass and couplings leads to significant differences in cross section and shapes of the kinematic variables for $M_{\text{med}} > 2m_{\text{DM}}$ as shown in Fig. 3.8. As expected, higher mediator masses lead to harder E_T spectra. On the other hand, the E_T shapes are similar in the off-shell Dark Matter production regime as well as no dramatic differences in cross sections are observed, which is illustrated

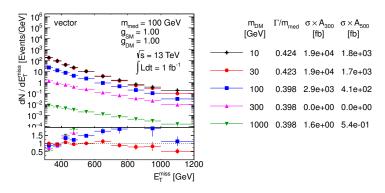


Figure 3.7: Scan over Dark Matter mass. The E_T distribution is compared for the vector mediator models using the parameters as indicated. Ratios of the normalized distributions with respect to the first one are shown. A_{300} and A_{500} in the table denote the acceptance of the $E_T > 300\,\text{GeV}$ and $E_T > 500\,\text{GeV}$ cut, respectively.

in Fig. 3.9. Therefore, a coarse binning along $m_{\rm DM}$ is sufficient at $M_{\rm med} \ll 2m_{\rm DM}.$

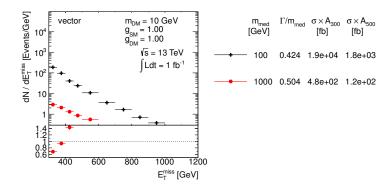


Figure 3.8: Scan over mediator mass. The E_T distribution is compared for the vector mediator models using the parameters as indicated. Ratios of the normalized distributions with respect to the first one are shown. A_{300} and A_{500} in the table denote the acceptance of the $E_T > 300\,\text{GeV}$ and $E_T > 500\,\text{GeV}$ cut, respectively.

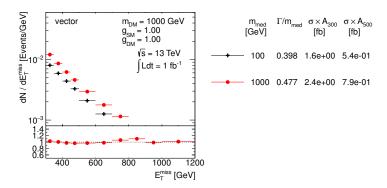


Figure 3.9: Scan over mediator mass. The E_T distribution is compared for the vector mediator models using the parameters as indicated. Ratios of the normalized distributions with respect to the first one are shown. A_{300} and A_{500} in the table denote the acceptance of the $E_T > 300$ GeV and $E_T > 500$ GeV cut, respectively.

Proposed parameter grid Based on the observations above, the following proposal is made for the presentation of the early Run-2 results from the LHC:

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- (a) Give results in the $M_{\rm med}$ – $m_{\rm DM}$ plane for a particular choice of the couplings.
- (b) Give results in the g_q – g_{DM} plane for a particular choice of the masses.

We choose to display the results in the M_{med} - m_{DM} plane for the 137 choice of the couplings $g_q = g_{DM} = 1$. In order to motivate the high-138 est mediator mass grid point, the expected sensitivity of Run-2 LHC data needs to be taken into account. The expected upper limit at 95% 140 confidence level on the product of cross section, acceptance and effi-141 ciency, $\sigma \times A \times \epsilon$, in the final Run-1 ATLAS mono-jet analysis [A⁺15] 142 is 51 fb and 7.2 fb for $E_T > 300 \,\text{GeV}$ and $E_T > 500 \,\text{GeV}$, respectively. The ATLAS 14 TeV prospects [ATL14] predict twice better sensitiv-144 ity with the first 5 fb⁻¹ of data already. Given the cross section for 145 V+jets processes increases by roughly a factor 2 when going from $\sqrt{s}=8\,\text{TeV}$ to 13 TeV, similar fiducial cross section limits can be ex-147 pected with the first Run-2 data as from the final Run-1 analysis. The 148 generator level cross section times the acceptance at $E_T > 500 \,\text{GeV}$ for the model with couplings $g_q = g_{DM} = 1$, light Dark Matter of 10 GeV 150 and 1 TeV vector mediator is at the order of 100 fb, i.e. the early Run-2 151 mono-jet analysis is going to be sensitive to heavier mediators than 152 this. The value of $\sigma \times A$ at $E_T > 500 \,\text{GeV}$ for 5 TeV vector mediator 153 is at the order of 0.1 fb, therefore this model probably lies beyond the 154 reach of the LHC. Based on these arguments, the following M_{med} 155 grid points are chosen, roughly equidistant in the logarithmic scale: 156 10 GeV, 20 GeV, 50 GeV, 100 GeV, 200 GeV, 300 GeV, 500 GeV, 1000 GeV and 2000 GeV. Given the fact that significant changes in cross section 158 happen around the $M_{\text{med}} = 2m_{\text{DM}}$ threshold, the m_{DM} grid points 159 are taken at approximately $M_{\rm med}/2$, namely: 10 GeV, 50 GeV, 150 GeV, 500 GeV and 1000 GeV. Points on the on-shell diagonal are always 161 chosen to be 5 GeV away from the threshold, to avoid numerical in-162 stabilities in the event generation. The detailed studies of the impact 163 of the parameter changes on the cross section and kinematic distributions presented earlier in this section support removing some of 165 the grid points and rely on interpolation. The optimised grids pro-166 posed for the vector and axial-vector mediators are given in Table. 3.1, containing 29 mass points each. One point at very high mediator mass (5 TeV) is added for each of the DM masses scanned, to aid the 169 reinterpretation of results in terms of contact interaction operators (EFTs).

m_{DM} (GeV)		m _{med} (GeV)								
1	10	20	50	100	200	300	500	1000	2000	5000
10	10	15	50	100						5000
50	10		50	95	200	300				5000
150	10				200	295	500			5000
500	10						500	995	2000	5000
1000	10							1000	1995	5000

Table 3.1: Simplified model benchmarks for s-channel simplified models (spin-1 mediators decaying to Dirac DM fermions in the V and A case, taking the minimum width for $g_q = g_{DM} = 1$)

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The presentation of the results in the g_q – g_{DM} plane for fixed masses benefits from cross section scaling and is discussed in Section 3.3.

3.2 Scalar and pseudoscalar mediator, s-channel exchange

One of the most simple UV complete extensions of the effective field 176 theory approach is the addition of a scalar/pseudoscalar mediator between DM and SM. A gauge singlet mediator can have tree-level 178 interactions with a singlet DM particle that is either a Dirac or Majo-179 rana fermion, or DM that is a scalar itself. The spin-0 mediator can either be a real or complex scalar; a complex scalar contains both 181 scalar and pseudoscalar particles, whereas the real field only con-182 tains the scalar particle. In this document we consider only two of 183 the possible choices for this simplified model: one where the interac-184 tion with the SM is mediated by a real scalar, and the second where 185 we consider only a light pseudoscalar, assuming that the associated 186 scalar is decoupled from the low-energy spectrum. The kinematics 187 of the two cases is sufficiently different to suggest that further investigation of the complex scalar case is needed but left for future 189 studies. 190

Couplings to the SM fermions can be arranged by mixing with the SM Higgs. Such models have interesting connections with Higgs physics, and can be viewed as generalizations of the Higgs portal to DM. The most general scalar mediator models will have renormalizable interactions between the SM Higgs and the new scalar ϕ or pseudoscalar a, as well as ϕ/a interactions with electroweak gauge bosons. Such interactions are model dependent, often subject to constraints from electroweak precision tests, and would suggest specialized searches which cannot be generalized to a broad class of models (unlike, for instance, the E_T + jets searches). As a result, for this class of minimal simplified models with spin-0 mediators, we will focus primarily on couplings to fermions and loop-induced couplings to gluons.

Minimal Flavor Violation (MFV) implies that scalar couplings to fermions will be proportional to the fermion mass. However, they can differ for up- and down-type quarks and for charged leptons.

Following the assumption that DM is a fermion χ , which couples to the SM only through a scalar ϕ or pseudoscalar a, the most general tree-level Lagrangians compatible with the MFV assumption

are [CRTW14, ADR $^+$ 14, BFG15]:

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$$\mathcal{L}_{\text{fermion},\phi} = \mathcal{L}_{\text{SM}} + i\bar{\chi}\partial\chi + m_{\chi}\bar{\chi}\chi + \left|\partial_{\mu}\phi\right|^{2} + \frac{1}{2}m_{\phi}^{2}\phi^{2} + g_{\chi}\phi\bar{\chi}\chi + \frac{\phi}{\sqrt{2}}\sum_{i}\left(g_{u}y_{i}^{u}\bar{u}_{i}u_{i} + g_{d}y_{i}^{d}\bar{d}_{i}d_{i} + g_{\ell}y_{i}^{\ell}\bar{\ell}_{i}\ell_{i}\right), \quad (3.8)$$

$$\mathcal{L}_{\text{fermion},a} = \mathcal{L}_{\text{SM}} + i\bar{\chi}\partial\chi + m_{\chi}\bar{\chi}\chi + \left|\partial_{\mu}a\right|^{2} + \frac{1}{2}m_{a}^{2}a^{2} + ig_{\chi}a\bar{\chi}\gamma_{5}\chi + \frac{ia}{\sqrt{2}}\sum_{i}\left(g_{u}y_{i}^{u}\bar{u}_{i}\gamma_{5}u_{i} + g_{d}y_{i}^{d}\bar{d}_{i}\gamma_{5}d_{i} + g_{\ell}y_{i}^{\ell}\bar{\ell}_{i}\gamma_{5}\ell_{3}\right)$$

Here the sums run over the all SM generations; the Yukawa couplings y_i^f are normalized to $y_i^f = \sqrt{2} m_i^f / v$ where $v \simeq 246\,\mathrm{GeV}$ represents the Higgs vacuum expectation value (VEV). We parametrise the DM-mediator coupling as g_χ , without any additional Yukawa structure between the mediator and the dark sector.

As already stated we only choose a minimal set of interactions that do not include interactions with the Higgs field. For simplicity, we also assume universal SM-mediator couplings $g_v = g_u = g_d = g_\ell$

Given these simplifications, the minimal set of parameters under consideration is

$$\left\{m_{\chi}, m_{\phi/a}, g_{\chi}, g_{\mathbf{q}}\right\}. \tag{3.10}$$

The matrix element implementation of the s-channel spin-o mediated DM production is available in POWHEG with the full top-loop calculation at LO [HR15].

We choose to consider minimal mediator width given by Eq. 3.3, where the individual contributions follow from

$$\Gamma_{\bar{\chi}\chi}^{S} = \frac{g_{\rm DM}^2 M_{\rm med}}{8\pi} \left(1 - \frac{4m_{\rm DM}^2}{M_{\rm med}^2} \right)^{3/2}$$
(3.11)

$$\Gamma_{\bar{q}q}^{S} = \frac{3g_{q}^{2}M_{\text{med}}}{8\pi} \frac{m_{q}^{2}}{v^{2}} \left(1 - \frac{4m_{q}^{2}}{M_{\text{med}}^{2}}\right)^{3/2}$$
(3.12)

$$\Gamma_{\bar{\chi}\chi}^{P} = \frac{g_{\rm DM}^{2} M_{\rm med}}{8\pi} \sqrt{1 - \frac{4m_{\rm DM}^{2}}{M_{\rm med}^{2}}}$$
(3.13)

$$\Gamma_{\bar{q}q}^{P} = \frac{3g_{q}^{2}M_{\text{med}}}{8\pi} \frac{m_{q}^{2}}{v^{2}} \sqrt{1 - \frac{4m_{q}^{2}}{M_{\text{med}}^{2}}} . \tag{3.14}$$

The minimal width for scalar and pseudo-scalar mediators with $g_{\rm q}=g_{\rm DM}=1$ are shown in Fig. 3.10, illustrating the effect of the Higgs-like Yukawa couplings. For the mediator masses above twice the top quark mass m_t , the minimal width receives the dominant contribution from the top quark. For lighter mediator masses, Dark Matter dominates as the couplings to lighter quarks are Yukawa

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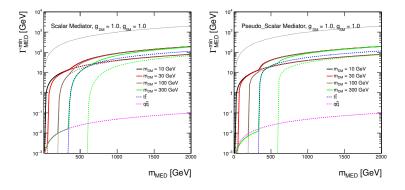
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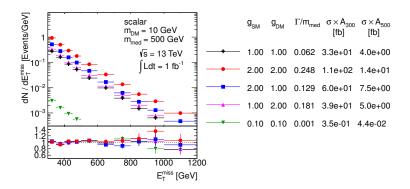
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suppressed. Note that we decide to ignore the partial width coming from gluons through loops as it can be safely neglected [HR15].

Similarly as in the case of the vector and axial-vector mediators, scans in the parameter space are performed also for the scalar and pseudo-scalar mediators in order to decide on the optimised parameter grid for the presentation of Run-2 results. Figures 3.11- 3.15 show the scans over the couplings, Dark Matter mass and mediator mass and the same conclusions apply as in Section 3.1.

Since the top quark gives the dominant contribution to the mediator width due to Higgs-like Yukawa couplings, the effect of the top channel opening in the mediator production was studied in addition. Scan over the mediator mass is shown in Fig. 3.15 where the mediator masses 300 GeV and 500 GeV are chosen to be below and above $2m_t$. The off-shell Dark Matter production regime is assumed by taking $m_{\rm DM}=1\,{\rm TeV}$ in order to allow studying solely the effects of the couplings to quarks. No differences in the kinematic distributions are observed and also the cross sections remain similar in this case. Therefore, it is concluded that no significant changes appear for mediator masses around the $2m_t$ threshold.



The optimized parameter grid in the M_{med} – m_{DM} plane for scalar and pseudo-scalar mediators is motivated by similar arguments as

Figure 3.10: Minimal width as a function of mediator mass for scalar and pseudo-scalar mediator assuming couplings of 1. The total width is shown as solid lines for Dark Matter masses of 10 GeV, 30 GeV, 100 GeV and 300 GeV in black, red, brown and green, respectively. The individual contributions from Dark Matter are indicated by dotted lines with the same colors. The contribution from all quarks but top is shown as magenta dotted line and the contribution from top quarks only is illustrated by the dotted blue line. The dotted black line shows the extreme case $\Gamma_{\min} = M_{\text{med}}$.

Figure 3.11: Scan over couplings. The E_T distribution is compared for the scalar mediator models using the parameters as indicated. Ratios of the normalized distributions with respect to the first one are shown. A_{300} and A_{500} in the table denote the acceptance of the $E_T > 300\,\text{GeV}$ and $E_T > 500\,\text{GeV}$ cut, respectively.

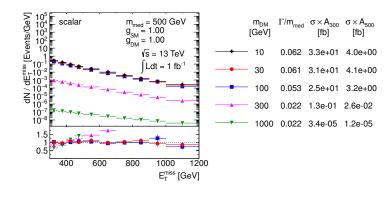


Figure 3.12: Scan over Dark Matter mass. The E_T distribution is compared for the scalar mediator models using the parameters as indicated. Ratios of the normalized distributions with respect to the first one are shown. A_{300} and A_{500} in the table denote the acceptance of the $E_T > 300 \,\text{GeV}$ and $E_T > 500 \,\text{GeV}$ cut, respectively.

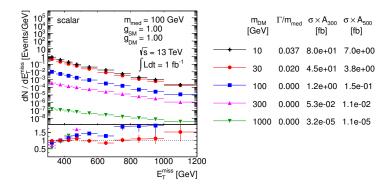


Figure 3.13: Scan over Dark Matter mass. The E_T distribution is compared for the scalar mediator models using the parameters as indicated. Ratios of the normalized distributions with respect to the first one are shown. A_{300} and A_{500} in the table denote the acceptance of the $E_T > 300 \,\text{GeV}$ and $E_T > 500 \,\text{GeV}$ cut, respectively.

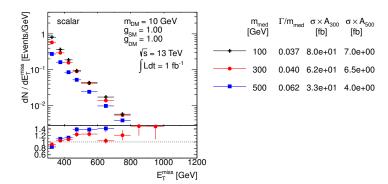


Figure 3.14: Scan over mediator mass. The E_T distribution is compared for the scalar mediator models using the parameters as indicated. Ratios of the normalized distributions with respect to the first one are shown. A_{300} and A_{500} in the table denote the acceptance of the $E_T > 300 \,\text{GeV}$ and $E_T > 500 \,\text{GeV}$ cut, respectively.

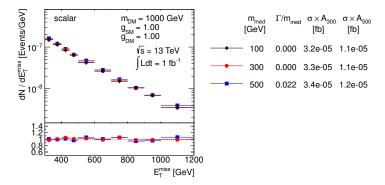


Figure 3.15: Scan over mediator mass. The E_T distribution is compared for the scalar mediator models using the parameters as indicated. Ratios of the normalized distributions with respect to the first one are shown. A_{300} and A_{500} in the table denote the acceptance of the $E_T > 300\,\mathrm{GeV}$ and $E_T > 500\,\mathrm{GeV}$ cut, respectively.

in the previous section. Therefore, a similar pattern is followed here, 251 taking again $g_q = g_{DM} = 1$. Only the sensitivity to the highest me-252 diator masses has to be revisited. The generator level cross section times the acceptance at $E_T > 500 \,\text{GeV}$ for the model with couplings 254 $g_q = g_{DM} = 1$, light Dark Matter of 10 GeV and 500 GeV scalar me-255 diator is at the order of 10 fb, i.e. just at the edge of the early Run-2 sensitivity. Increasing the mediator mass to 1 TeV pushes the product $\sigma \times A$ down to approximately 0.1 fb, beyond the LHC sensitivity. 258 Therefore, we choose to remove the 2 TeV mediator mass from the grid and present the final grid with 26 mass points only in Fig. 3.2. One point at very high mediator mass (5 TeV) is added for each of 261 the DM masses scanned, to aid the reinterpretation of results in terms of contact interaction operators (EFTs).

$m_{\rm DM}$ (GeV)		m _{med} (GeV)							
1	10	20	50	100	200	300	500	1000	5000
10	10	15	50	100					5000
50	10		50	95	200	300			5000
150	10				200	295	500		5000
500	10						500	995	5000
1000	10							1000	5000

Table 3.2: Simplified model benchmarks for s—channel simplified models (spino mediators decaying to Dirac DM fermions in the scalar and pseudoscalar case, taking the minimum width for $g_q = g_{DM} = 1$)

The proposal for the scan in the g_q – $g_{\rm DM}$ plane is described in the following section.

3.3 Cross section scaling

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The aim of the parameter grid optimization is to find out whether certain parts of the parameter space can be omitted and one can rely on the neighboring grid points in order to populate the missing parts.

There are two ways of doing this:

- Interpolation is used in-between the grid points that are close enough such that finer granularity is not needed for the presentation purposes, or between the points where smooth or no changes of the results are expected. The latter argument is exactly the one that motivates the reduction of the grid points in the M_{med}-m_{DM} plane.
- Recalculation of the results can be used when the dependencies with respect to the neighboring grid points are known.

The results of the scan over the couplings presented in the previous sections indicate there are no changes in kinematic distributions for different choices of the coupling strengths. This means that the

acceptance remains the same in the whole g_q – g_{DM} plane and it is 282 sufficient to perform the detector simulation only for one single grid 283 point. The resulting truth-level selection acceptance and the detector reconstruction efficiency can then be applied to all remaining grid 285 points in the g_q – g_{DM} plane where only the generator-level cross sec-286 tion needs to be known. This significantly reduces the computing time as the detector response is by far the most expensive part of the Monte Carlo sample production. However, a further step can be 289 taken if a parameterization of the cross section dependence from one grid point to another exists, in which case the number of generated samples can be reduced even further. 292

Let us now elaborate on a cross section scaling procedure. The propagator on the s-channel exchange is written in a Breit-Wigner form as $\frac{1}{\sqrt{s}-M_{\rm med}^2+iM_{\rm med}\Gamma}$. The relative size of the center-of-mass energy defined by the two partons entering the hard process and the mediator mass allows to classify the production in the following way:

- off-shell production when $\sqrt{s} \gg M_{\rm med}$ leading to suppressed cross sections,
- on-shell production when $\sqrt{s} \sim M_{
 m med}$ leading to enhanced cross sections,
 - effective field theory (EFT) limit when $\sqrt{s} \ll M_{\rm med}$.

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All three categories can be distinguished in Fig. 3.16 showing the upper limit on the interaction scale $M^* \equiv M_{\rm med}/\sqrt{g_{\rm q}g_{\rm DM}}$ for vector mediator. In the case of the off-shell production and the EFT limit, the first term in the propagator dominates which reduces the dependence on the mediator width. Therefore, in these cases one can approximate the cross section as

$$\sigma \propto g_{\rm q}^2 g_{\rm DM}^2. \tag{3.15}$$

The on-shell production regime is the most interesting one as it gives the best chances for a discovery at the LHC given the cross section enhancement. The propagator term with the width cannot be neglected in this case and, in the narrow width approximation, one can integrate

$$\int \frac{ds}{(s - M_{\rm med}^2)^2 + M_{\rm med}^2 \Gamma^2} = \frac{\pi}{M_{\rm med} \Gamma}$$
 (3.16)

which further implies the cross section scaling

$$\sigma \propto \frac{g_q^2 g_{\rm DM}^2}{\Gamma}.\tag{3.17}$$

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Since $\Gamma \sim g_{\rm q}^2 + g_{\rm DM}^2$, one can simplify this rule in the extreme cases as follows

$$\sigma \propto \frac{g_{q}^{2}g_{DM}^{2}}{g_{q}^{2} + g_{DM}^{2}} \xrightarrow{g_{q} \ll g_{DM}} g_{q}^{2}$$

$$\sigma \propto \frac{g_{q}^{2}g_{DM}^{2}}{g_{q}^{2} + g_{DM}^{2}} \xrightarrow{g_{q} \gg g_{DM}} g_{DM}^{2}.$$
(3.18)

$$\sigma \propto \frac{g_{\rm q}^2 g_{\rm DM}^2}{g_{\rm q}^2 + g_{\rm DM}^2} \xrightarrow{g_{\rm q} \gg g_{\rm DM}} g_{\rm DM}^2 .$$
 (3.19)

However, it is important to keep in mind that there is no simple scaling rule for how the cross section changes with the Dark Matter mass, mediator mass and the mediator width because PDFs matter in such cases as well. Therefore, the scaling procedure outlined above is expected to work only for fixed masses and fixed mediator width.

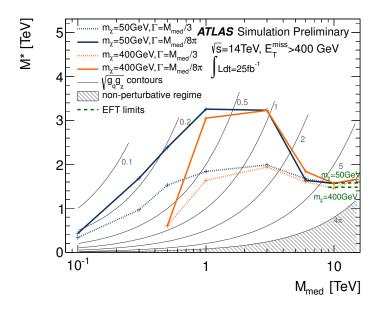


Figure 3.16: Comparison of the 95% CL lower limits on the scale of the interaction of a Z'-like simplified model at 14 TeV, in terms of the mediator mass. Corresponding limits from EFT models are shown on the same plot as green dashed lines to show equivalence between the two models for high mediator masses. Taken from Ref. [ATL14].

Figures 3.17 and 3.18 show the minimal width in the g_q – g_{DM} plane for all vector, axial-vector, scalar and pseudo-scalar mediators for $M_{\rm med} = 100 \,\text{GeV}$ and 1000 GeV, respectively, taking $m_{\rm DM} = 10 \,\text{GeV}$. The individual colors indicate the lines of constant width along which the cross section scaling works. For vector and axial-vector mediators, the minimal width is predominantly defined by g_q due to the number of quark flavors and the color factor. On the contrary, both the Standard Model and Dark Matter partial width have comparable contributions in case of scalar and pseudo-scalar mediators if the top quark channel is open $(M_{\text{med}} > 2m_t)$. However, mostly $g_{\rm DM}$ defines the minimal width for $M_{\rm med} < 2m_t$ due to the Yukawasuppressed light quark couplings.

The performance of the cross section scaling is demonstrated in Fig. 3.19 where the mass point $M_{\text{med}} = 1 \text{ TeV}$ and $m_{\text{DM}} = 10 \text{ GeV}$

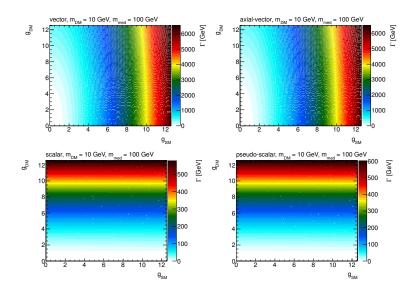


Figure 3.17: Minimal width for vector, axial-vector, scalar and pseudo-scalar mediators as a function of the individual couplings g_q and g_{DM} , assuming $M_{\text{med}} = 100 \,\text{GeV}$ and $m_{\text{DM}} = 10 \,\text{GeV}$.

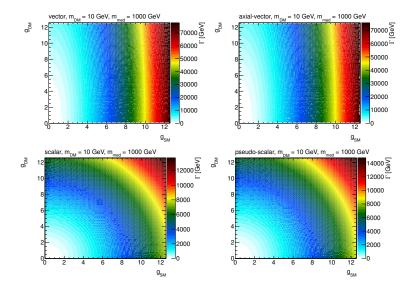


Figure 3.18: Minimal width for vector, axial-vector, scalar and pseudo-scalar mediators as a function of the individual couplings $g_{\rm q}$ and $g_{\rm DM}$, assuming $M_{\rm med}=1\,{\rm TeV}$ and $m_{\rm DM}=10\,{\rm GeV}.$

is chosen and rescaled from the starting point $g_q = g_{DM} = 1$ 324 according to Eq. 3.17 to populate the whole g_q – g_{DM} plane. This 325 means the width is not kept constant in this test and this is done in purpose in order to point out deviations from the scaling when 327 the width is altered. For each mass point, the rescaled cross sec-328 tion is compared to the generator cross section and the ratio of the two is plotted. For the given choice of the mass points, the scaling seems to work approximately with the precision of $\sim 20\%$ in the re-331 gion where $\Gamma_{\min} < M_{\text{med}}$. Constant colors indicate the lines along 332 which the cross section scaling works precisely and there is a remarkable resemblance of the patterns shown in the plots of the mediator 334 width. To prove the scaling along the lines of constant width works, 335 one such line is chosen in Fig. 3.20 for a scalar mediator, defined by $M_{\text{med}} = 300 \,\text{GeV}$, $m_{\text{DM}} = 100 \,\text{GeV}$, $g_{\text{q}} = g_{\text{DM}} = 1$, and the rescaled 337 and generated cross sections are found to agree within 3%.

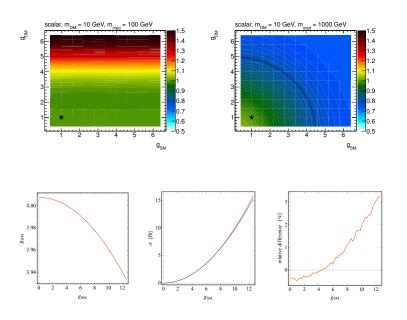


Figure 3.19: Ratio of the rescaled and generated cross sections in the g_q – $g_{\rm DM}$ plane. The point at $g_q=g_{\rm DM}=1$, taken as a reference for the rescaling, is denoted by a star symbol. Scalar model with $M_{\rm med}=100\,{\rm GeV}$ (left) and 1 TeV (right) is plotted for $m_{\rm DM}=10\,{\rm GeV}$. The limiting case $\Gamma_{\rm min}=M_{\rm med}$ is shown as a black line.

Figure 3.20: Scaling along the lines of constant width. The line of constant width for $M_{\rm med}=300\,{\rm GeV}$ and $m_{\rm DM}=100\,{\rm GeV}$, intercepting $g_{\rm q}=g_{\rm DM}=4$ is shown on left. The generated and rescaled cross sections are compared in the middle, the corresponding ratio is shown on right.

Proposed parameter grid We propose to present the results in the g_q – $g_{\rm DM}$ plane using the following prescription:

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- Since the shapes of kinematic quantities do not change for different couplings, use the acceptance and efficiency for the available $m_{\rm DM}=50\,{\rm GeV},\,M_{\rm med}=300\,{\rm GeV},\,g_{\rm q}=g_{\rm DM}=1$ grid point from the $M_{\rm med}$ – $m_{\rm DM}$ plane for the scalar and pseudo-scalar mediator. In case of the vector and axial-vector mediator, use the grid point $m_{\rm DM}=50\,{\rm GeV},\,M_{\rm med}=1\,{\rm TeV},\,g_{\rm q}=g_{\rm DM}=1.$
- Generate additional samples in order to get generator cross sections only. For scalar and pseudo-scalar mediator, choose $m_{\rm DM} =$

50 GeV, $M_{\rm med} = 300$ GeV with the following values for $g_{\rm q} = g_{\rm DM}$: 0.1, 2, 3, 4, 5, 6. For vector and axial vector mediator, choose $m_{\rm DM} = 50$ GeV, $M_{\rm med} = 1$ TeV with the following values for $g_{\rm q} = g_{\rm DM}$: 0.1, 0.25, 0.5, 0.75, 1.25, 1.5. The upper values are defined by the minimal width reaching the mediator mass.

• Rescale the generator cross sections along the lines of constant width in order to populate the whole g_q – g_{DM} plane.

Rescaling to different mediator width In general there may be an interest to consider larger mediator masses than Γ_{\min} in order to accommodate further couplings of the mediator. The cross section scaling method described above can be used to reinterpret the results presented for the minimal width, since multiplying the width by factor n is equivalent to changing the coupling strength by factor \sqrt{n} , i.e.

$$\sigma(g_{\rm q}, g_{\rm DM}, n\Gamma_{\rm min}(g_{\rm q}, g_{\rm DM})) \propto \frac{g_{\rm q}^2 g_{\rm DM}^2}{\Gamma_{\rm min}(\sqrt{n}g_{\rm q}, \sqrt{n}g_{\rm DM})}. \tag{3.20}$$

The cross section for the sample with couplings g_q and g_{DM} and modified mediator width $\Gamma = n\Gamma_{\min}$ can therefore be rescaled from a sample generated with the minimal width corresponding to the couplings scaled by \sqrt{n} as described in the following formula.

$$\sigma(g_{\rm q}, g_{\rm DM}, n\Gamma_{\rm min}(g_{\rm q}, g_{\rm DM})) = \frac{1}{n^2} \sigma(\sqrt{n}g_{\rm q}, \sqrt{n}g_{\rm DM}, \Gamma_{\rm min}(\sqrt{n}g_{\rm q}, \sqrt{n}g_{\rm DM}))$$
(3.21)

Advantage of doing this is again in the fact that no event selection and detector response needs to be simulated since the changes in couplings do not have an effect on the shapes of kinematic distributions.

360 3.3.1 POWHEG settings

This section describes specific settings for the Dark Matter models needed to run the POWHEG generation.

 The POWHEG implementation allows to generate a single sample that provides sufficient statistics in all mono-jet analysis signal regions. POWHEG generates weighted events and the bornsuppfact parameter is used to set the event suppression factor according to

$$F(k_{\mathrm{T}}) = \frac{k_{\mathrm{T}}^2}{k_{\mathrm{T}}^2 + \mathsf{bornsuppfact}^2} \,. \tag{3.22}$$

In this way, the events at low E_T are suppressed and receive higher event weights which ensures higher statistics at high E_T . We recommend to set bornsuppfact to 1000.

- The bornktmin parameter allows to suppress the low E_T region even further by starting the generation at a certain value of k_T . It is recommended to set this parameter to half the lower analysis E_T cut, therefore the proposed value for bornktmin is 150.
- Set runningwidth to o.
- Set mass_low and mass_high to -1.
- The minimal values for ncall1, itmx1, ncall2, itmx2 are 250000, 5, 1000000, 5 for the DMV model, respectively. In order to increase speed, set foldsci and foldy to 2 and keep foldphi at 1.
- The minimal values for ncall1, itmx1, ncall2, itmx2 are 100000, 5, 100000, 5 for the DMS_tloop model, respectively.
- Allow negative weights for the DMV model by setting withnegweights to 1.
- Since the DMS_tloop model is a leading order process, set L0events
 and bornonly are set to 1 internally.

3.4 Colored scalar mediator, t-channel exchange

An alternative set of simplified models exist where the mediator is exchanged in the t-channel, thereby coupling the quark and dark matter particle directly. Under the assumption that χ is a Standard Model (SM) singlet, the mediating particle, labeled ϕ , is necessarily charged and coloured. This model is parallel to, and partially motivated by, the squark of the MSSM, but in this case the χ is chosen to be Dirac. Following the example of Ref. [PVZ14], the interaction Lagrangian is written as

$$\mathcal{L}_{\text{int}} = g \sum_{i=1,2,3} (\phi_L^i \bar{Q}_L^i + \phi_{uR}^i \bar{u}_R^i + \phi_{dR}^i \bar{d}_R^i) \chi$$
 (3.23)

(Note: [PVZ14] uses only i = 1,2, but I think it's fine to extend this to 3 here.) where Q_L^i , u_R^i and d_R^i are the SM quarks and ϕ_L^i , ϕ_{uR}^i and ϕ_{dR}^i are the corresponding mediators, which (unlike the s-channel mediators) must be heavier than χ . These mediators have SM gauge representations under $(SU(3),SU(2))_Y$ of $(3,2)_{-1/6}$, $(3,1)_{2/3}$ and $(3,1)_{-1/3}$ respectively. Variations of the model previously studied include coupling to the left-handed quarks only [CEHL14, BDSJ+14], to the ϕ_{uR}^i [DNRT13] or ϕ_{dR}^i [PVZ14, A+14b], or some combination [BB13, AWZ14].

Minimal Flavour Violation (MFV) requires that the mediator masses for each flavour be equal; the same logic also applies to the

 $_{101}$ couplings g. The available parameters are then

$$\{m_{\chi}, M_{\phi}, g\}.$$
 (3.24)

In practice, the third mediator mass and coupling could be separated from the other two, if higher order corrections to the MFV prediction arise due to the large top Yukawa coupling – a common variation is then to define this split between the first two generations and the third, so the parameters are extended to

$$\{m_{\chi}, M_{\phi_{12}}, M_{\phi_3}, g_{1,2}, g_3\}.$$
 (3.25)

The width of each mediator is expressed, using the example of decay to an up quark, as

$$\Gamma(\phi_i \to \bar{u}_i \chi) = \frac{g_i^2}{16\pi M_{\phi_i}^3} (M_{\phi_i}^2 - m_{u_i}^2 - m_{\chi}^2) \times \sqrt{M_{\phi_i}^4 + m_{u_i}^4 + m_{\chi}^4 - 2M_{\phi_i}^2 m_{u_i}^2 - 2M_{\phi_i}^2 m_{\chi}^2 - 2m_{u_i}^2 m_{\chi}^2},$$
(3.26)

this reduces to

$$\frac{g_i^2 M_{\phi_i}}{16\pi} \left(1 - \frac{m_{\chi}^2}{M_{\phi_i}^2} \right)^2 \tag{3.27}$$

in the limit M_{ϕ_i} , $m_\chi \gg m_{u_i}$.

An interesting point of difference with the s-channel simplified models is that the mediator can radiate a SM object, such as a jet or gauge boson, thus providing three separate mono-X diagrams which must be considered together in calculations. This model can also give a signal in the di-jet + MET channel when, for example, the χ is exchanged in the t-channel and the resulting ϕ pair each decay to a jet + χ .

Specific models for signatures with EW bosons

In this Section, we consider models with a photon, a W boson, a

Z boson or a Higgs boson in the final state, accompanied by Dark

Matter particles that either couple directly to the boson or are medi-

ated by a new particle. The experimental signature is identified as

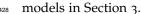
424 V+MET.

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These models are interesting both as extensions of models where the gluon provides the experimentally detectable signature, and as stand-alone models with final states that cannot be generated by the



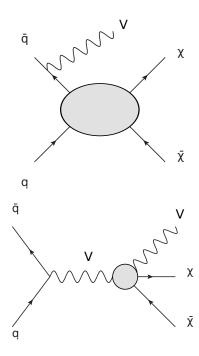


Figure 4.1: Sketch of benchmark models including a contact interaction for V+MET searches, adapted from [NCC⁺14].

The models considered can be divided in three categories:

430 Models including a contact operator, where the boson is radiated from the initial state

As depicted in the top diagram of Figure 4.1, these models follow

the nomenclature and theory for the EFT benchmarks commonly

used by MET+X searches [GIR⁺10]. These models have been used in past experimental searches [Kha14, Aad14b, K⁺14, Aad14b, A⁺14a, Aad14a], and they will not be described here.

Models including a contact operator, where the boson is directly coupled to DM
Shown in the bottom of Figure 4.1, these models allow for a contact interaction vertex that directly couples the boson to Dark
Matter.

Simplified models where the boson is radiated from the initial state These models follow those already described in Section 3, replacing the initial state gluon with a boson.

V-specific simplified models These models postulate direct couplings
 of new mediators to bosons, e.g. they couple the Higgs boson to a
 new scalar [CDM+14].

The following Sections describe the models within these categories, the parameters for each of the benchmark models chosen, the studies towards the choices of the parameters to be scanned, and finally point to the location of their Matrix Element implementation.

50 4.1 Simplified models with ISR boson radiation

Searches in the jet+MET final state are generally more sensitive with 451 respect to final states including bosons, due to the much larger rates 452 of signal events featuring quark or gluon radiation with respect to 453 radiation of bosons [ZBW13], in combination with the low branching ratios if leptons from boson decays are required in the final state. The 455 rates for the Higgs boson radiation is too low for these models to be considered a viable benchmark [CDM⁺14]. However, the presence of photons leptons from W and Z decays and W or Z bosons decaying hadronically allows to reject the background more effectively, making 459 Z/gamma/W+MET searches still worth comparing with searches in the jet+MET final state.

462 4.1.1 Vector mediator exchanged in the s-channel

The case for searches with W bosons in the final state has so far been strenghtened by the presence of particular choices of couplings between the WIMP and the up and down quarks which enhance W radiation [BT13], in the case of the exchange of a vector mediator in the s-channel. Run-1 searches have considered three sample cases for the product of up and down quark couplings to the mediator ξ :

• No couplings between mediator and either up or down quarks ($\xi = 0$);

- Same coupling between mediator and each of the quark types ($\xi = 1$);
- Coupling of opposite sign between mediator and each of the quark types ($\xi=-1$).

The $\xi = -1$ case leads to a large increase in the cross-section of the process, and modifies the spectrum of missing transverse energy or 476 transverse mass used for the searches. The sensitivity of the W+MET 477 search for this benchmark in this case surpasses that of the jet+MET search. However, as shown in Ref. [BCD⁺15], the cross-section increase is due to the production of longitudinally polarized W bosons, 480 as a consequence of a violation of electroweak gauge symmetries. 481 Unless further particles are introduced (in a fashion similar to the Higgs boson in the Standard Model), choosing a value of $\xi = -1$ 483 for this simplified model will lead to a manifest violation of unitar-484 ity at LHC energies. The simplified model with a vector mediator exchanged in the s-channel model can still be considered as a benchmark for searches with a W boson if $\xi = 1$. We leave the study of 487 further models with cross-section enhancements due to different couplings to up and down quarks for studies beyond the early LHC searches covered in this document. An example of such model is the 490 case of both DM and SM Higgs charged under a new U(1)', with a a small mass mixing between SM Z-boson and the new Zprime. This leads to different effective DM couplings to u_L and d_L , proportional 493 to their coupling to the Z boson, detailed in Appendix B. 494

The scan in the parameters that characterize this simplified model for EW boson + MET searches follow what already detailed in Section 3.

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As in the case of the jet+MET models, the width does not have a significant impact on the kinematic distributions relevant for those searches. An example of the particle-level analysis acceptance using the generator-level cuts from Ref. [Aad15] for the photon+MET analysis, but raising the photon p_T cut to 150 GeV is shown in Figure 4.2, comparing a width that is set to $\Gamma = M_{med}/3$ to the minimal width (the ratio between the two widths ranges from 1.05 to 1.5 with increasing mediator masses).

Examples of relevant kinematic distributions for selected benchmark points are shown in Fig. 4.9; leading-order cross-sections for the chosen benchmark points are shown in Table ?? [TODO: Insert table of cross-sections].

4.1.2 Colored scalar mediator exchanged in the t-channel

The model parameters with emission of an EW boson follow those in Section 3.

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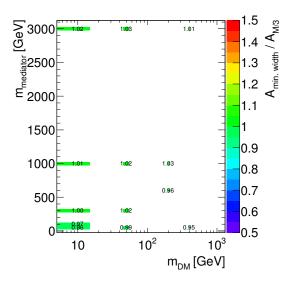


Figure 4.2: Analysis acceptance for the photon+MET analysis when varying the mediator width, in the case of a vector mediator exchanged in the *s*-channel

Figure 4.4 shows the MET distribution for the hadronic Z+MET final state, with varying dark matter and mediator mass, before any selection. The acceptance for a series of simplified analysis cuts (MET>350 GeV, leading jet p_T > 40 GeV, minimum azimuthal angle between jet and MET > 0.4) applied at the generator level is shown in Figure 4.5.

The parameter scan is still under discussion.

20 4.1.3 Model implementation

These models are generated at leading order with MadGraph 2.2.2, and parameter cards can be found on SVN [TODO: Add SVN location]. The parton shower is done using Pythia 8, with a matching scale of... [TODO: To be completed.]

525 4.2 EFT models with direct DM-boson couplings

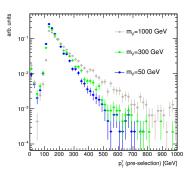
[Linda Carpenter and Uli Haisch are rewriting this section. Changes expected:

- change of normalization and Lagrangians to be consistent with [CHH15], linked to notation of [CNS⁺13]
- description of dimension-5 EFTs
- addition of a dimension-5 simplified model]

A complete list of effective operators with direct DM/boson couplings for Dirac DM, up to dimension 7, can be found in [CHLR13].

Figure 4.3: Kinematic distributions relevant for searches with W, Z and photons in the final state, for the simplified model with a vector mediator

exchanged in the s-channel.

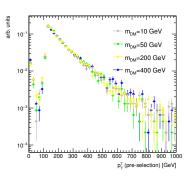


(a) Missing transverse momentum distribution for the photon+MET final state, for different mediator mass choices, for a DM mass of 10 GeV.

1/N dN/dE_T ** [GeV⁻¹] 10

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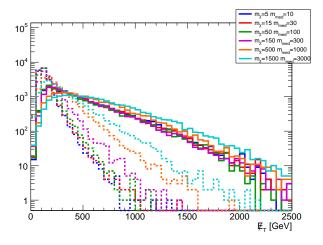


(b) Leading photon transverse momentum distribution for the photon+MET final state, for different DM mass choices, with a mediator mass of 1 TeV.



(c) Missing transverse momentum distribution for the leptonic Z+MET final state, for different mediator mass choices, for a DM mass of 15 GeV

(d) Transverse mass (m_T) for the leptonic W+MET final state.



(e) Missing transverse momentum distribution for the hadronic W+MET final

Following the notation of [CNS+13], the dimension 5 benchmark models from this category have a Lagrangian that includes terms

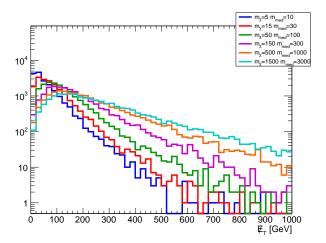


Figure 4.4: Missing transverse momentum distribution for the hadronic Z+MET final state, for the simplified model with a colored scalar mediator exchanged in the t-channel.

t-scalar model acceptance

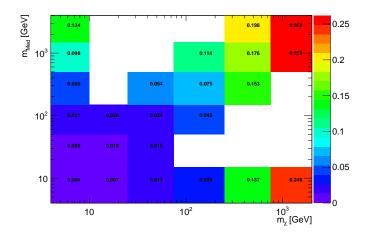


Figure 4.5: Acceptance table for the hadronic Z+MET final state, for the simplified model with a colored scalar mediator exchanged in the *t*-channel.

such as:

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$$\frac{m_W^2}{\Lambda_5^3} \bar{\chi} \chi W^{+\mu} W_{\mu}^- + \frac{m_Z^2}{2\Lambda_5^3} \bar{\chi} \chi Z^{\mu} Z_{\mu} . \tag{4.1}$$

where m_Z and m_W are the masses of the Z and W boson, W^μ and Z^μ are the fields of the gauge bosons, χ denote the Dark Matter fields and Λ_5 is the effective field theory scale. This operator induces signatures with MET in conjunction with Z and W bosons at tree level, while at loop level it induces couplings to photon pairs and $Z\gamma$ through W loops. [TODO: Ask Linda to explain this better than I did.]. In these models, a clear relation exists between final states with photons, EW bosons and Higgs boson. [TODO: see if mono-Higgs

studies exist for these operators, include them here].

The dimension 7 benchmark models include couplings to the kinetic terms of the EW bosons ($F_i^{\mu\nu}$, with $F_i=1,2,3$ being the field strengths of the SM U(1) and SU(2) gauge groups and $\tilde{F}_i^{\mu\nu}$ their dual tensors). The Lagrangian for the scalar coupling of DM and bosons include terms such as the following:

$$\frac{1}{\Lambda_{7,S}^3} \bar{\chi} \chi \sum_{i} k_i F_i^{\mu\nu} F_{\mu\nu}^i + \frac{1}{\Lambda_{7,S}^3} \bar{\chi} \chi \sum_{i} k_i F_i^{\mu\nu} \tilde{F}_{\mu\nu}^i$$
 (4.2)

The Lagrangian with pseudoscalar coupling includes the following terms:

$$\frac{1}{\Lambda_{7PS}^3} \bar{\chi} \gamma^5 \chi \sum_{i} k_i F_i^{\mu\nu} F_{\mu\nu}^i + \frac{1}{\Lambda_{7PS}^3} \bar{\chi} \gamma^5 \chi \sum_{i} k_i F_i^{\mu\nu} \tilde{F}_{\mu\nu}^i$$
(4.3)

The cut-off scales Λ for the separate terms can be related to operators with different Lorentz structure from Ref. [CHLR13]. Given that they do not lead to substantial differences for collider searches as shown in Figure 2 of Ref. [CNS⁺13], they have been denoted as $\Lambda_{7,S}$ for the scalar case and $\Lambda_{7,PS}$ for the pseudoscalar case.

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The k_i coefficients for the dimension 7 models are related to the couplings of DM to pairs of gauge bosons by gauge invariance:

$$g_{WW} = \frac{2k_2}{s_{v_1}^2 \Lambda_7^3} \tag{4.4}$$

$$g_{ZZ} = \frac{1}{4s_w^2 \Lambda_7^3} \left(\frac{k_1 s_w^2}{c_w^2} + \frac{k_2 c_w^2}{s_w^2} \right)$$
 (4.5)

$$g_{\gamma\gamma} = \frac{1}{4c_w^2} \frac{k_1 + k_2}{\Lambda_7^3} \tag{4.6}$$

$$g_{Z\gamma} = \frac{1}{2s_w c_w \Lambda_7^3} \left(\frac{k_2}{s_w^2} - \frac{k_1}{c_w^2} \right)$$
 (4.7)

where s_w and c_w are respectively the sine and cosine of the weak mixing angle.

The coefficients k_i determine the relative importance of each of the boson channels, and their correlations. For example, for what concerns searches with W, Z and photons:

- k_2 alone controls the rate of the coupling to W boson pairs;
- If $k_1 = k_2$ contributions from both Z and γ exchange appear;
- If $k_1 = c_w^2/s_w^2 k_2$ the γ exchange is negligible.

The coefficients k_1 and k_2 are related to the coefficients c_1 and c_2 in the equivalent models of Ref. [CHH15] as $k_2 = s_w^2 * c_2$ and c_3 0 c_4 1 c_5 2 c_5 3 c_6 4 c_7 5 c_8 5 c_8 5 c_9 6 c_9 7 c_9 8 c_9 9 c_9 9

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[TODO: Linda will possibly complete/correct this subsection]

UV completions of such operators where the dominant signature is a single photon or EW boson are possible, for example through the exchange of a W' or a Z'. They are left as benchmarks for future searches as their implementation may require loop diagrams and need further studies beyond the timescale of this Forum.

As shown in Fig. 4.6 kinematics of this model can be approximated by that of a simplified model including a high-mass scalar mediator exchanged in the s-channel. For this reason, the list of benchmark models with direct boson-DM couplings only includes dimension 7 operators.

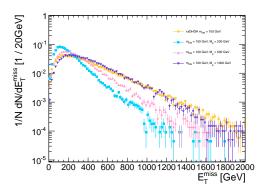


Figure 4.6: Comparison of the missing transverse momentum for the simplified model where a scalar mediator is exchanged in the s-channel and the model including a dimension-5 scalar contact operator, in the leptonic Z+MET final state

The kinematic distributions for dimension-7 scalar and pseudoscalar operators only shows small differences, as shown in Fig. 4.7.



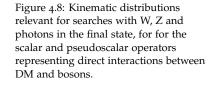
Figure 4.7: Comparison of the missing transverse momentum for the scalar and pseudoscalar operators with direct interaction between DM and photon, in the photon+MET final state

Similarly, the differences in kinematics for the various signatures are negligible when changing the coefficients k_1 and k_2 , as shown in Figure ??. Only the case $k_1 = k_2 = 1$ is generated as benchmark; other cases are left for reinterpretation as they will only need a rescaling of the cross-sections shown in Table ?? [TODO: add tables with cross sections] for the various Dark Matter mass points considered.

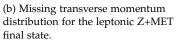
Examples of relevant kinematic distributions for selected benchmark points are shown in Fig. 4.9.



(a) Missing transverse momentum distribution for the photon+MET final









(c) Transverse mass (m_T) for the leptonic W+MET final state.

- 4.2.1 Specific simplified models
- Mono-Higgs, to be completed...



(a) Missing transverse momentum distribution for the photon+MET final state.

Figure 4.9: Kinematic distributions relevant for searches with W, Z and photons in the final state, for the simplified model with a vector mediator exchanged in the s-channel.



(b) Missing transverse momentum distribution for the leptonic Z+MET final state.



(c) Transverse mass (m_T) for the leptonic W+MET final state.



(d) Fat [Insert algorithm] jet mass (m_T) for the the hadronic W+MET final state.

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Specific models for signatures with heavy flavor quarks

96 5.1 t̄t+MET models

As described in Section 3.2, a model with a scalar/pseudoscalar particle mediating the DM-SM interactions is one of the simplest UV completions of our EFT models.

The expected signal of DM pair production depends on the production rate defined by the dark matter mass m_{χ} , mediator $m_{\phi/a}$, on the couplings g_i and on the branching ration defined by the total decay width of the mediator ϕ/a . We calculate the minimum possible width (assuming only decays into the dark matter and the Standard Model fermions) that is consistent with a given value of $g_{\chi}g_{\rm SM}$. These are given by Eq. (5.1) [BFG15].

$$\Gamma_{\phi,a} = \sum_{f} N_{c} \frac{y_{f}^{2} g_{v}^{2} m_{\phi,a}}{16\pi} \left(1 - \frac{4m_{f}^{2}}{m_{\phi,a}^{2}} \right)^{3/2} + \frac{g_{\chi}^{2} m_{\phi,a}}{8\pi} \left(1 - \frac{4m_{\chi}^{2}}{m_{\phi,a}^{2}} \right)^{3/2} + \frac{\alpha_{s}^{2} y_{t}^{2} g_{v}^{2} m_{\phi,a}^{3}}{32\pi^{3} v^{2}} \left| f_{\phi,a} \left(\frac{4m_{t}^{2}}{m_{\phi,a}^{2}} \right) \right|^{2}$$
(5.1)

where

$$f_{\phi}(au) = au \left[1 + (1 - au) \operatorname{arctan}^2 \left(\frac{1}{\sqrt{ au - 1}} \right) \right], \qquad f_a(au) = au \operatorname{arctan}^2 \left(\frac{1}{\sqrt{ au - 1}} \right).$$
(5.2)

The first term in each width corresponds to the decay into SM fermions, and the sum runs over all kinematically available fermions, $N_c=3$ for quarks and $N_c=1$ for leptons. The second term is the decay into DM, assuming that is kinematically allowed. The factor of two between the decay into SM fermions and into DM is a result of our choice of normalization of the Yukawa couplings due to spin dependencies. The last two terms correspond to decay into gluons. Since we have assumed that $g_v=g_u=g_d=g_\ell$, we have included in the partial decay widths $\Gamma(\phi/a\to gg)$ only the contributions stemming from top loops, which provide the by far largest corrections

given that $y_t\gg y_b$ etc. At the loop level the mediators can decay not only to gluons but also to pairs of photons and other final states if kinematical accessible. However the decay rates $\Gamma(\phi/a\to gg)$ are always larger than the other loop-induced partial widths, and in consequence the total decay widths $\Gamma_{\phi/a}$ are well approximated by the corresponding sum of the individual partial decay widths involving DM, fermion or gluon pairs. It should be noted that if $m_{\phi/a}>2m_t$ the total widths of ϕ/a will typically be dominated by the partial widths to top quarks.

5.1.1 Parameter scan

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As discussed in Sec. 3.2, the MFV assumption for spin-0 mediators leads to quark mass dependent Yukawa couplings, and therefore dominant couplings to top quarks. This motivates dedicated DM+ $t\bar{t}$ searches. The benchmark chosen for these searches follows the assumptions mentioned in the previous Section: we consider a Dirac fermion DM particle, universal couplings to quarks, and minimum mediator width.

The benchmark points scanning the model parameters have been selected to ensure that the kinematic features of the parameter space are sufficiently represented. Detailed studies were performed to identify points in the $m_{\rm DM}$, $m_{\phi,a}$, $g_{\rm DM}$, g_v (and $\Gamma_{\phi,a}$) parameter space that differ significantly from each other in terms of expected detector acceptance. Because missing transverse momentum is the key observable for searches, the mediator p_T spectra is taken to represent the main kinematics of a model. Another consideration in determining the set of benchmarks is to focus on the phase space where we expect the searches to be sensitive during the 2015 LHC run. Based on a projected integrated luminosity of 30 fb⁻¹ expected for 2015, we disregard model points with a cross section times branching ratio smaller than 0.1 fb.

5.1.2 Parameter scan

The kinematics is most dependent on the masses $m_{\rm DM}$ and $m_{\phi,a}$.

Figure 5.1 and 5.2 show typical dependencies for scalar and pseudoscalar couplings respectively.

The two relevant thresholds that are observed for the variation in the kinematic spectra are $m_{\phi,a}=2m_{\rm DM}$ and $m_{\phi,a}=2m_t$. When the mediator mass exceeds both these thresholds then the p_T spectra broadens with larger $m_{\phi,a}$ and the kinematics for ϕ and a are comparable. The mediator p_T spectra changes significantly when crossing these thresholds. In particular, the kinematics are different for an on-shell mediator compared to an off-shell mediator $(m_{\phi,a}<2m_{\rm DM})$.

- Furthermore, the scalar case differs from the pseudoscalar one when
- $m_{\phi} < 2m_t$. Therefore, it is important to have benchmark points cover-
- ing both sides of these thresholds with sufficient granularity.

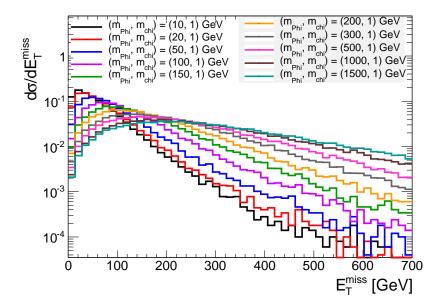


Figure 5.1: Example of the dependence of the kinematics on the scalar mediator mass. The Dark Matter mass is fixed to be 1GeV.

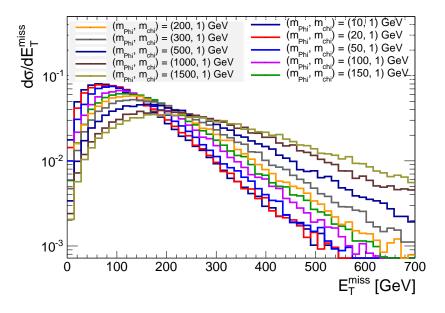


Figure 5.2: Example of the dependence of the kinematics on the pseudoscalar mediator mass. The Dark Matter mass is fixed to be 1GeV.

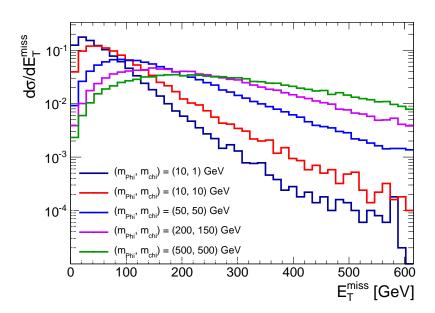


Figure 5.3: Example of the dependence of the kinematic for points of the grid proposed in Tab. 3.2 close to the $m_{\phi,a} \sim 2m_\chi$ limit.3

Typically only weak dependencies on width or equivalently couplings are observed (see Fig 5.4), except for large mediator masses of ~ 1.5 TeV or for very small couplings of $\sim 10^{-2}$. These regimes where width effects are significant have production cross sections that are too small to be relevant for $30\,\mathrm{fb}^{-1}$ and are not considered here. However, with the full Run-2 dataset, such models may be within reach. The weak dependence on the typical width values can be understood as the parton distribution function are the dominant effect on mediator production. In other words, for couplings $\sim O(1)$ the width is large enough that the p_T of the mediator is determined mainly by the PDF.

Another case where the width can impact the kinematics is when $m_{\phi,a}$ is slightly larger than $2m_{\chi}$. Here, the width determines the relative contribution between on-shell and off-shell production. An example is given in Fig. 5.5. In our recommendations we propose to use for simplicity the minimal width, as this is represents the most conservative choice to interpret the LHC results. **[TODO: mention**]

larger widths too]

Given that the kinematics are similar for all couplings $\sim O(1)$, we recommend to generate only samples with $g_{\rm DM}=g_v=1$. It follows from this that these benchmark points should be a good approximation for non-unity couplings and for $g_{\rm DM} \neq g_v$, provided that the sample is rescaled to the appropriate cross section times branching ratio. While a simple scaling function **[CD: which?]** is sufficient for

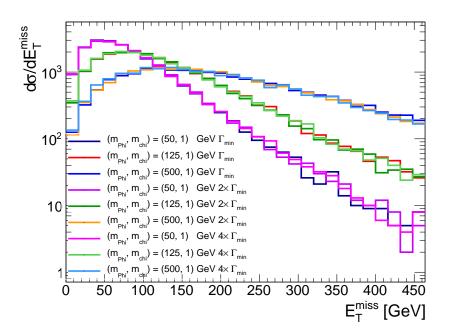


Figure 5.4: Study of the dependence of kinematics on the width of a scalar mediator. The width is increased up to four times the minimal width for each mediator and dark matter mass combination.

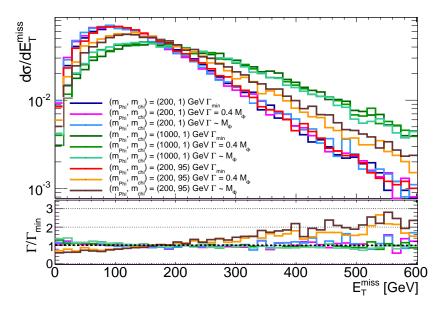


Figure 5.5: Dependence of the dependence of kinematics on the width of a scalar mediator. The width is increased up to the mediator mass. Choices of mediator and dark matter masses such that $m_{\phi,a}$ is slightly larger than $2m_{\chi}$ is the only case that shows a sizeable variation of the kinematics as a function of the width.

- a limited range of coupling values (see Fig. 5.6 for example), we also
- choose to provide instead a table of cross section times branching
- ratio values over a large range of couplings to support interpretation

of search results (see the Appendix C). The table lists couplings from g=0.1 to g=3.5, where the upper limit is chosen to close to the perturbative limit.

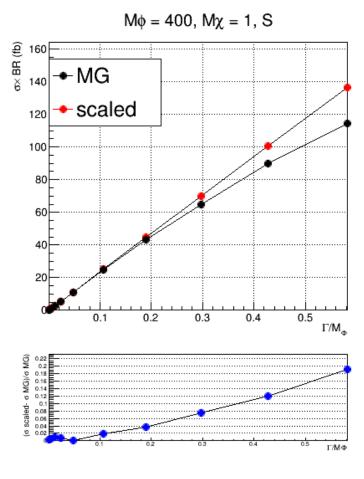


Figure 5.6: An example comparing a simple cross section scaling versus the computation from the generator, for a scalar model with $m_{\phi}=400\,\mathrm{GeV}$ and $m_{\mathrm{DM}}=1\,\mathrm{GeV}$. In this example, the scaling relationship holds for Γ_{ϕ}/m_{ϕ} below 0.2, beyond which finite width effects become important and the simple scaling breaks down.

The points for the parameter scan chosen for this model are listed in Table 3.2, chosen to be harmonized with those for other analyses employing the same scalar model as benchmark. Based on the sensitivity considerations above, DM masses are only simulated up to 500 GeV, leading to a total of 24 benchmark points.

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In addition to the considerations discussed in the preceding subsections, very light DM fermions are included ($m_{\rm DM}=10\,{\rm GeV}$) as this is a region where colliders have a complementary sensitivity to current direct detection experiments.

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Validity of EFT approach

Effective Field Theories (EFTs) are an extremely useful tool for DM searches at the LHC. Given the current lack of indications about the nature of the DM particle and its interactions, a model independent 705 interpretation of the collider bounds appears mandatory, especially in complementarity with the reinterpretation of the exclusion limits within a choice of simplified models, which cannot exhaust the set of possible completions of an effective Lagrangian. However EFTs 709 must be used with caution at LHC energies, where the energy scale of the interaction is at a scale where the EFT approximation can no longer be assumed to be valid. Here we summarise some methods 712 that can be used to ensure the validity of the EFT approximation. These methods are described in detail in Refs. [BDSMR14?, BDSJ+14, A^{+} 15, RWZ15].

6.1 Outline of the procedure described in Refs. [? A^+ 15]

For a tree-level interaction between DM and the Standard Model (SM) via some mediator with mass M, the EFT approximation corresponds to expanding the propagator in powers of $Q_{\rm tr}^2/M^2$, truncating at lowest order, and combining the remaining parameters into a single parameter M_* (also called Λ). For an example scenario with a Z'-type mediator (leading to some combination of operators D5 to D8 in the EFT limit) this corresponds to setting

$$\frac{g_{\text{DM}}g_q}{Q_{\text{tr}}^2 - M^2} = -\frac{g_{\text{DM}}g_q}{M^2} \left(1 + \frac{Q_{\text{tr}}^2}{M^2} + \mathcal{O}\left(\frac{Q_{\text{tr}}^4}{M^4}\right) \right) \simeq -\frac{1}{{M_*}^2}, \tag{6.1}$$

where $Q_{\rm tr}$ is the momentum carried by the mediator, and $g_{\rm DM}$, g_q are the DM-mediator and quark-mediator couplings respectively. Similar expressions exist for other operators. Clearly the condition that must be satisfied for this approximation to be valid is that $Q_{\rm tr}^2 < M^2 = g_{\rm DM} g_q M_*^2$.

We can use this condition to enforce the validity of the EFT approximation by restricting the signal (after the imposition of the cuts

of the analysis) to events for which $Q_{\rm tr}^2 < M^2$. This truncated signal can then be used to derive the new, truncated limit on M_* as a function of $(m_{\rm DM}, g_{\rm DM} g_g)$.

For the example D5-like operator, $\sigma \propto {M_*}^{-4}$, and so there is a simple rule for converting a rescaled cross section into a rescaled constraint on M_* if the original limit is based on a simple cut-and-count procedure. Defining $\sigma^{\rm cut}_{\rm EFT}$ as the cross section truncated such that all events pass the condition $\sqrt{g_{\rm DM}g_q}M_*^{\rm rescaled}>Q_{\rm tr}$, we have

$$M_*^{\text{rescaled}} = \left(\frac{\sigma_{\text{EFT}}}{\sigma_{\text{EFT}}^{\text{cut}}}\right)^{1/4} M_*^{\text{original}},$$
 (6.2)

which can be solved for $M_*^{\rm rescaled}$ via either iteration or a scan (note that $M_*^{\rm rescaled}$ appears on both the LHS and RHS of the equation). Similar relations exist for a given UV completion of each operator. The details and application of this procedure to ATLAS results can be found in Ref. [A $^+$ 15] for a range of operators. Since this method uses the physical couplings and energy scale $Q_{\rm tr}$, it gives the strongest possible constraints in the EFT limit while remaining robust by ensuring the validity of the EFT approximation.

6.2 Outline of the procedure described in Ref. [RWZ15]

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In [RWZ15] a procedure to extract model independent and consistent bounds within the EFT is described. This procedure can be applied to any effective Lagrangian describing the interactions between the DM and the SM, and provides limits that can be directly reinterpreted in any completion of the EFT.

The range of applicability of the EFT is defined by a mass scale $M_{\rm cut}$, a parameter which marks the upper limit of the range of energy scales at which the EFT can be used reliably, independently of the particular completion of the model. Regardless of the details of the full theory, the energy scale probing the validity of the EFT is less than or equal to the centre-of-mass energy $E_{\rm cm}$, the total invariant mass of the hard final states of the reaction. Therefore, the condition ensuring the validity of the EFT is, by definition of $M_{\rm cut}$,

$$E_{\rm cm} < M_{\rm cut} \,. \tag{6.3}$$

For example, in the specific case of a tree level mediation with a single mediator, M_{cut} can be interpreted as the mass of that mediator.

There are then at least three free parameters describing an EFT: the DM mass $m_{\rm DM}$, the scale M_* of the interaction, and the cutoff scale $M_{\rm cut}$.

We can use the same technique as above to restrict the signal to the events for which $E_{\rm cm} < M_{\rm cut}$, using only these events to derive the exclusion limits on M_* as a function of $(m_{\rm DM}, M_{\rm cut})$. We can also define an *effective coupling strength* $M_{\rm cut} = g_* M_*$, where g_* is a free parameter that substitutes the parameter $M_{\rm cut}$, and therefore derive exclusions on M_* as a function of $(m_{\rm DM}, g_*)$. This allows us to see how much of the theoretically allowed parameter space has been actually tested and how much is still unexplored; For example, in the Z'-type model considered above, g_* is equal to $\sqrt{g_{\rm DM}g_q}$. The resulting plots are shown in [RWZ15] for a particular effective operator.

The advantage of this procedure is that the obtained bounds can be directly and easily recast in any completion of the EFT, by computing the parameters M_* , $M_{\rm cut}$ in the full model as functions of the parameters of the complete theory. On the other hand, the resulting limits will be weaker than those obtained using $Q_{\rm tr}$ and a specific UV completion.

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Appendix: Detailed studies on mono-jet signatures

```
CKKW parton matching implementation
   A.1
   The parton matching techniques are implemented in the mono-jet
   like MC generation in order to avoid double counting the partons
   from matrix elements and parton showering. The CKKW matching
   is better developed and preferred in this study. As the illustration
   sample, the EFT D5 samples are generated with MadGraph5_aMC@NLO
   version 2.2.2. The technical implementations are shown as below.
      On the generator side, i.e., MadGraph5_aMC@NLO:
   • ickkw = 0
   • ktdurham = matching scale
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   • dparameter = 0.4
   • dokt = T
     ptj=20
   • drjj=0
   • mmjj=0
   • ptj1min=0
   On the parton showering side, i.e., Pythia 8:
   • Merging:ktType = 1
   • Merging: TMS = matching scale
   • 1000022:all = chi chi 2 0 0 30.0 0.0 0.0 0.0 0.0
     1000022:isVisible = false
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   • Merging:doKTMerging = on
   • Merging:Process = pp>chi,1000022chi ,-1000022
```

• Merging:nJetMax = 2

The matching scales should be the same for the generation and parton showering. In MadGraph5_aMC@NLO, the particle data group ID
1000022 is used for weakly interacting dark matter candidates, which should be informed to Pythia 8.

In this test we are generating the process with up to two parton emissions, so the command Merging:nJetMax = 2 is applied to Pythia 8. The different parton emission cases are generated separately:

```
    p p > chi chi
    p p > chi chi j
    p p > chi chi j j
    p p > chi chi j j
```

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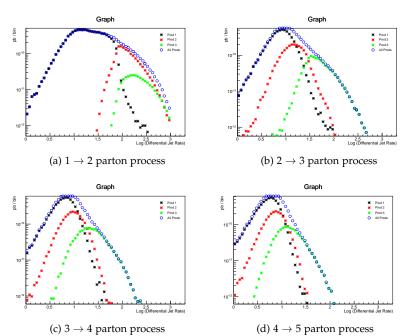
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Two matching scales are tested at 30 and 80 GeV. The differential jet rates are shown in Fig. A.1 for matching scale 30 GeV and Fig. A.2 for 80 GeV. The 80 GeV matching scale gives smoother distribution, which is desired to avoid artifical effect due to parton matching.

There will be a small tink around the matching scale for both cases.



The MC distributions for the missing transverse energy and transverse momenta for the leading and subleading jets are plotted in Fig.. For the mono-jet analysis, usually a missing transverse energy cut larger than 300 GeV is applied for offline selection, which makes the contribution of the o-parton emission case negligible in the mono-jet analysis.

Figure A.1: Jet differential rates distributions for EFT D5 sample with CKKW matching scale at 30 GeV. 0-, 1- and 2-parton emission cases are generated separatedly.

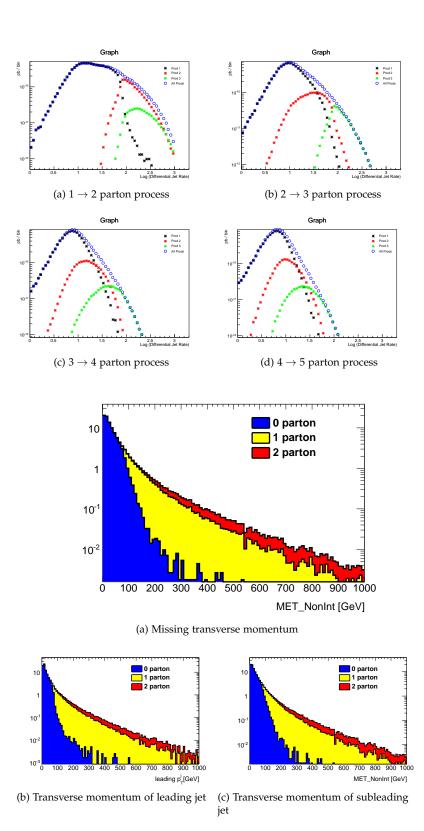


Figure A.2: Jet differential rates distributions for EFT D5 sample with CKKW matching scale at 80 GeV. o-, 1- and 2-parton emission cases are generated separatedly.

Figure A.3: Kinematics distributions for EFT D5 sample with CKKW matching emission cases are generated sepa-

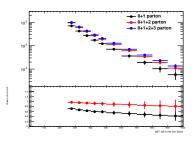
scale at 80 GeV. o-, 1- and 2-parton ratedly and added together by cross sections. The o-parton emission case has very limited contribution for missing transverse energy larger than 300 GeV region.

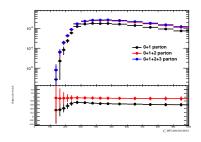
A.2 Parton emission generation

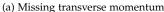
In order to describe the signal kinematics correctly and save time in MC generation, the parton emissions will only be generated up to a certain numbers of parton and ignore the cases with more partons. The later ones usually have cross sections small enough and limited contribution in the interested kinematic regions.

It is found that the 3- or more-parton emission cases are negligible in our intersted regions, but the 2-parton emission case has significant contributions. The o- and 1-parton emissions are out of discussion since they give the baseline signature in this analysis. The impacts of 2- and 3-parton emissions are quantified in this section.

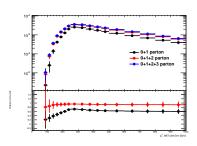
Here the o-, 1-, 2- and 3-parton emissions are generated separately and requested in matching step with Merging:nJetMax=3 and scale at 80 GeV in Pythia8. The kinematic distributions for MET, leading and subleading jet transverse momenta are plotted in Fig, while the jet multiplicity at different leading jet transverse momentum cuts is shown in Fig.







(b) Transverse momentum of leading jet



(c) Transverse momentum of subleading jet

With the ATLAS run-I baseline cut (MET and leading jet p_T larger than 250 GeV, less than 4 jets), the 0+1 parton emission has 11.4% yield less compared to 0+1+2+3 parton emission, while the 0+1+2 has only 0.4% less. With MET>400 GeV, 0+1 parton emission has 16.8% yield less and 0+1+2 parton emission has 0.8% less compared to 0+1+2+3 parton emission. With MET>600 GeV, 0+1 parton emission

Figure A.4: Kinematics distributions for EFT D5 sample with CKKW matching scale at 80 GeV. o-, 1-, 2- and 3-parton emission cases are generated separatedly and added together by cross sections.

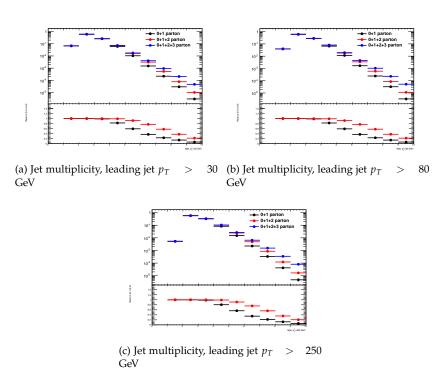


Figure A.5: Jet multiplicity distributions for EFT D5 sample with CKKW matching scale at 80 GeV. o-, 1-, 2- and 3-parton emission cases are generated separatedly and added together by cross sections.

sion has 22.1% yield less and 0+1+2 parton emission has 1.6% less

compared to 0+1+2+3 parton emission.

** Appendix: Detailed studies for EW models

B.1 Further W+MET models with possible cross-section enhance-

As pointed out in Ref. [BCD⁺15], the mono-W signature can probe the iso-spin violating interactions of dark matter with quarks. The relevant operators after the electroweak symmetry breaking is

$$\frac{1}{\Lambda^2} \overline{\chi} \gamma_{\mu} \chi \left(\overline{u}_L \gamma^{\mu} u_L + \xi \overline{d}_L \gamma^{\mu} d_L \right) . \tag{B.1}$$

Here, we only keep the left-handed quarks because the right-handed quarks do not radiate a *W*-gauge boson from the weak interaction. As the LHC constraints the cutoff to higher values, it is also important to know the corresponding operators before the electroweak symmetry. At the dimension-six level, the following operator

$$\frac{c_6}{\Lambda^2} \overline{\chi} \gamma_\mu \chi \, \overline{Q}_L \gamma^\mu Q_L \tag{B.2}$$

conserves iso-spin and provides us $\xi=1$ [?]. At the dimension-eight level, new operators appear to induce iso-spin violation and can be

$$\frac{c_8^d}{\Lambda^4} \overline{\chi} \gamma_\mu \chi (H \overline{Q}_L) \gamma^\mu (Q_L H^\dagger) + \frac{c_8^u}{\Lambda^4} \overline{\chi} \gamma_\mu \chi (\tilde{H} \overline{Q}_L) \gamma^\mu (Q_L \tilde{H}^\dagger). \tag{B.3}$$

After inputting the vacuum expectation value of the Higgs field, we have

$$\xi = \frac{c_6 + c_8^d \, v_{\rm EW}^2 / 2\Lambda^2}{c_6 + c_8^u \, v_{\rm EW}^2 / 2\Lambda^2}.$$
 (B.4)

- For a nonzero c_6 and $v_{\rm EW} \ll \Lambda$, the iso-spin violation effects are suppressed. On the other hand, the values of c_6 , c_8^d and c_8^u depend on the UV-models.
 - There is one possible UV-model to obtain a zero value for c_6 and non-zero values for c_8^d and c_8^u . One can have the dark matter and the SM Higgs field charged under a new U(1)'. There is a small mass mixing between SM *Z*-boson and the new Z' with a mixing angle

of $\mathcal{O}(v_{\rm EW}^2/M_{Z'}^2)$. After integrating out Z', one has different effective dark matter couplings to u_L and d_L fields, which are proportional to their couplings to the Z boson. For this model, we have $c_6=0$ and

$$\xi = \frac{-\frac{1}{2} + \frac{1}{3}\sin^2\theta_W}{\frac{1}{2} - \frac{2}{3}\sin^2\theta_W} \approx -2.7$$
 (B.5)

842 and order of unity.

Appendix: Table of cross sections for $t\bar{t}$ +MET searches

 $_{845}$ All tables need to be adjusted with right number of significant digits

Coupling (g)	m_{Phi} [GeV]	m_{χ} [GeV]	Γ_{min} [GeV]	σ
0.1	10	1	0.00374318	0.207 ± 0.0006846
0.1	20	1	0.00784569	0.1121 ± 0.0003285
0.1	50	1	0.01987	0.03211 ± 0.0001005
0.1	100	1	0.0398141	$0.007325 \pm 2.416e-05$
0.1	150	1	0.0597437	$0.002396 \pm 7.419e-06$
0.1	200	1	0.0796724	$0.001018 \pm 3.398 \text{e-}06$
0.1	300	1	0.119549	0.0003394 \pm 1.234e-06
0.1	500	1	0.310863	$6.802\text{e-}05 \pm 2.343\text{e-}07$
0.1	1000	1	0.881329	$5.817e\text{-}06 \pm 2.356e\text{-}08$
0.1	1500	1	1.40417	$8.942e ext{-07} \pm 3.832e ext{-09}$
0.1	10	10	0.000100	$1.007e-05 \pm 3.761e-08$
0.1	20	10	0.000100	$3.491e$ -05 \pm 1.012e-07
0.1	50	10	0.0153395	0.03212 ± 0.0001037
0.1	100	10	0.0374747	$0.007343 \pm 2.011e-05$
0.1	150	10	0.0581752	0.002389 ± 7.654 e-06
0.1	200	10	0.0784937	$0.001018 \pm 6.258 \text{e-}06$
0.1	300	10	0.118762	$0.0003373 \pm 1.448e-06$
0.1	500	10	0.310391	$6.773 \text{e-o}5 \pm 2.326 \text{e-o}7$
0.1	1000	10	0.881093	$5.81\text{e-}06 \pm 2.245\text{e-}08$
0.1	1500	10	1.40401	$8.937 \text{e-o}7 \pm 4.013 \text{e-o}9$
0.1	50	50	0.0000233555	$2.581 \text{e-o}7 \pm 1.214 \text{e-o}9$
0.1	100	50	0.0000492402	$1.526e-06 \pm 7.038e-09$
0.1	150	50	0.0247905	$0.002387 \pm 8.272e$ -06
0.1	200	50	0.051794	0.00102 ± 3.216 e-06
0.1	300	50	0.100226	$0.0003366 \pm 1.393e-06$
0.1	500	50	0.299052	$6.679 \text{e-o}5 \pm 2.406 \text{e-o}7$
0.1	1000	50	0.875378	$5.764e-06 \pm 2.472e-08$
0.1	1500	50	1.4002	8.866 e-07 \pm 3.257e-09

Table C.1 – continued from previous page

Coupling (g)	m_{Phi} [GeV]	m_{χ} [GeV]	Γ_{min} [GeV]	σ
0.1	100	150	0.0000492402	$1.246\text{e-}08 \pm 5.121\text{e-}11$
0.1	150	150	0.0000765167	$1.393e-08 \pm 6.653e-11$
0.1	200	150	0.000106902	$1.693e-08 \pm 8.493e-11$
0.1	300	150	0.000190543	$7.557\text{e-}08 \pm 2.171\text{e-}10$
0.1	500	150	0.213784	5.063e-05 ± 1.724e-07
0.1	1000	150	0.828844	$5.365e-06 \pm 2.028e-08$
0.1	1500	150	1.36872	$8.603e-07 \pm 3.769e-09$
0.1	200	300	0.000106902	$1.415 \text{e-}09 \pm 5.97 \text{e-}12$
0.1	300	300	0.000190543	$1.64 ext{e-09} \pm 7.878 ext{e-12}$
0.1	500	300	0.111924	$3.078\text{e-}09 \pm 1.482\text{e-}11$
0.1	1000	300	0.687162	$3.828e-06 \pm 1.416e-08$
0.1	1500	300	1.26683	$7.579e-07 \pm 3.041e-09$
0.1	500	500	0.111924	$1.784e$ -10 \pm 1.105e-12
0.1	1000	500	0.483444	1.98e-09 \pm 9.199e-12
0.1	1500	500	1.05448	$4.92\text{e-}07 \pm 2.14\text{e-}09$
0.3	10	1	0.0336886	1.876 ± 0.006611
0.3	20	1	0.0706112	1.006 ± 0.003894
0.3	50	1	0.17883	0.2886 ± 0.0009285
0.3	100	1	0.358327	0.06598 ± 0.000182
0.3	150	1	0.537693	$0.0214 \pm 6.701 e$ -05
0.3	200	1	0.717052	$0.009216 \pm 3.533e-05$
0.3	300	1	1.07594	$0.003044 \pm 1.194e-05$
0.3	500	1	2.79777	$0.0006105 \pm 2.187e-06$
0.3	1000	1	7.93196	$5.256e-05 \pm 2.165e-07$
0.3	1500	1	12.6376	$8.048e-06 \pm 3.473e-08$
0.3	10	10	5.69808	$0.0008143 \pm 3.272e-06$
0.3	20	10	0.0000630938	$0.002836 \pm 9.724e-06$
0.3	50	10	0.138055	0.2869 ± 0.0008971
0.3	100	10	0.337272	0.06606 ± 0.0002407
0.3	150	10	0.523576	$0.02145 \pm 8.01e-05$
0.3	200	10	0.706443	$0.009222 \pm 2.807 \text{e-}05$
0.3	300	10	1.06886	$0.003051 \pm 1.001e-05$
0.3	500	10	2.79352	$0.0006115 \pm 2.268e-06$
0.3	1000	10	7.92983	$5.24e-05 \pm 1.964e-07$
0.3	1500	10	12.6361	$8.053e-06 \pm 3.203e-08$
0.3	10	50	5.69808	$1.704e-05 \pm 7.077e-08$
0.3	20	50	0.0000630938	$1.746e-05 \pm 7.383e-08$
0.3	50	50	0.000210199	$2.071e-05 \pm 8.162e-08$
0.3	100	50	0.000443162	$0.0001245 \pm 3.888 e$ -07
0.3	150	50	0.223114	$0.02138 \pm 6.22e-05$

Table C.1 – continued from previous page

0.3	Coupling (g)	m_{Phi} [GeV]		Γ_{min} [GeV]	σ
0.3 500 50 2.69146 0.0005971 ± 2.181e-06 0.3 1000 50 7.8784 5.222e-05 ± 1.907e-07 0.3 1500 50 12.6018 7.947e-06 ± 2.996e-08 0.3 150 150 0.000443162 1.004e-06 ± 4.682e-09 0.3 150 150 0.00068865 1.132e-06 ± 4.644e-09 0.3 200 150 0.000962116 1.349e-06 ± 6.834e-06 0.3 300 150 0.00171489 6.08e-06 ± 2.289e-08 0.3 500 150 1.92405 0.000456 ± 2.064e-06 0.3 1000 150 7.45959 4.818e-05 ± 1.84e-07 0.3 1500 150 12.3185 7.796e-06 ± 2.802e-08 0.3 200 300 0.000962116 1.144e-07 ± 4.635e-10 0.3 300 300 0.00171489 1.324e-07 ± 6.634e-10 0.3 300 300 0.00171489 1.324e-07 ± 6.634e-10 0.3 500 300 1.00732 2.5e-07 ± 1.113e-09 0.3 1500 300 11.4014 6.834e-06 ± 2.623e-08 0.3 500 300 11.4014 6.834e-06 ± 2.623e-08 0.3 500 500 1.00732 1.449e-08 ± 5.536e-11 0.3 1500 500 4.35099 1.487e-07 ± 6.617e-10 0.3 1500 500 9.49035 4.374e-06 ± 1.739e-08 0.7 10 1 0.183416 10.2 ± 0.03649 0.7 20 1 0.384439 5.462 ± 0.02022 0.7 50 1 0.97363 1.558 ± 0.004491 0.7 100 1 1.95089 0.3568 ± 0.001143 0.7 150 1 2.92744 0.1161 ± 0.003685 0.7 200 1 3.90395 0.04995 ± 0.0001494 0.7 300 1 5.85789 0.01649 ± 5.579e-05 0.7 500 1 15.2323 0.003313 ± 1.464e-05 0.7 100 1 0.000310229 0.02403 ± 0.0001038 0.7 20 10 0.000343511 0.08347 ± 0.0004764 0.7 1500 10 1.83626 0.3569 ± 0.0009501 0.7 150 10 2.85058 0.1165 ± 0.0004139 0.7 200 10 3.84619 0.04984 ± 0.0001855 0.7 500 10 15.2092 0.03301 ± 1.289e-05 0.7 500 10 15.2092 0.003301 ± 1.289e-05 0.7 1000 10	0.3	200	50	0.466146	0.009186 ± 3.168e-05
0.3	0.3	300	50	0.902031	0.003039 ± 1.09e-05
0.3	0.3	500	50	2.69146	0.0005971 \pm 2.181e-06
0.3	0.3	1000	50	7.8784	5.222e-05 ± 1.907e-07
0.3	0.3	1500	50	12.6018	$7.947e-06 \pm 2.996e-08$
0.3 200 150 0.000962116 1.349e-06 ± 6.834e-09 0.3 300 150 0.00171489 6.08e-06 ± 2.289e-08 0.3 500 150 1.92405 0.000456 ± 2.064e-06 0.3 1000 150 7.45959 4.818e-05 ± 1.84e-07 0.3 1500 150 12.3185 7.796e-06 ± 2.802e-08 0.3 200 300 0.000962116 1.144e-07 ± 4.635e-10 0.3 300 300 0.00171489 1.324e-07 ± 6.534e-10 0.3 500 300 1.00732 2.5e-07 ± 1.113e-09 0.3 1500 300 11.4014 6.834e-06 ± 2.623e-08 0.3 500 300 11.4014 6.834e-06 ± 2.623e-08 0.3 500 300 11.4014 6.834e-06 ± 2.623e-08 0.3 500 500 1.00732 1.449e-08 ± 5.536e-11 0.3 1500 500 4.35099 1.487e-07 ± 6.617e-10 0.3 1500 500 9.49035 4.374e-06 ± 1.739e-08 0.7 10 1 0.183416 10.2 ± 0.03649 0.7 20 1 0.384439 5.462 ± 0.02022 0.7 50 1 0.97363 1.558 ± 0.004491 0.7 150 1 1.95089 0.3568 ± 0.001143 0.7 150 1 2.92744 0.1161 ± 0.0003685 0.7 200 1 3.90395 0.04995 ± 0.0001494 0.7 300 1 5.85789 0.01649 ± 5.579e-05 0.7 500 1 15.2323 0.003313 ± 1.464e-05 0.7 1500 1 43.1851 0.0002823 ± 1.233e-06 0.7 1500 1 43.1851 0.0002823 ± 1.233e-06 0.7 1500 1 68.8045 4.481e-05 ± 1.885e-07 0.7 150 1 0.000343511 0.08347 ± 0.0001738 0.7 20 10 0.000343511 0.08347 ± 0.0001738 0.7 20 10 0.000343511 0.08347 ± 0.0001742 0.7 50 10 0.751635 1.553 ± 0.004764 0.7 150 10 2.85058 0.1165 ± 0.0004732 0.7 500 10 1.83626 0.3569 ± 0.0001738 0.7 200 10 3.84619 0.04984 ± 0.0001855 0.7 200 10 3.84619 0.04984 ± 0.0001855 0.7 500 10 15.2092 0.003301 ± 1.289e-05	0.3	100	150	0.000443162	$1.004\text{e-}06 \pm 4.682\text{e-}09$
0.3 300 150 0.00171489 6.08e-06 ± 2.289e-08 0.3 500 150 1.92405 0.000456 ± 2.064e-06 0.3 1000 150 7.45959 4.818e-05 ± 1.84e-07 0.3 1500 150 12.3185 7.796e-06 ± 2.802e-08 0.3 200 300 0.000962116 1.144e-07 ± 4.635e-10 0.3 300 300 0.00171489 1.324e-07 ± 6.534e-10 0.3 500 300 1.00732 2.5e-07 ± 1.113e-09 0.3 1000 300 6.18446 3.439e-05 ± 1.376e-07 0.3 1500 300 11.4014 6.834e-06 ± 2.622e-08 0.3 500 500 1.00732 1.449e-08 ± 5.536e-11 0.3 1500 300 11.4014 6.834e-06 ± 2.622e-08 0.3 500 500 1.00732 1.449e-08 ± 5.536e-11 0.3 1500 500 4.35099 1.487e-07 ± 6.617e-10 0.3 1500 500 9.49035 4.374e-06 ± 1.739e-08 0.7 10 1 0.183416 10.2 ± 0.03649 0.7 20 1 0.384439 5.462 ± 0.02022 0.7 50 1 0.97363 1.558 ± 0.004491 0.7 150 1 2.92744 0.1161 ± 0.0003685 0.7 200 1 3.90395 0.04995 ± 0.0001494 0.7 300 1 5.85789 0.01649 ± 5.579e-05 0.7 500 1 15.2323 0.003313 ± 1.464e-05 0.7 1500 1 43.1851 0.0002823 ± 1.233e-06 0.7 1500 1 68.8045 4.481e-05 ± 1.885e-07 0.7 150 1 0.000343511 0.08347 ± 0.0004742 0.7 50 10 0.751635 1.553 ± 0.004764 0.7 150 10 1.83626 0.3569 ± 0.0001439 0.7 150 10 1.83626 0.3569 ± 0.0001439 0.7 200 10 3.84619 0.04984 ± 0.0001855 0.7 200 10 3.84619 0.04984 ± 0.0001855 0.7 500 10 15.2092 0.003301 ± 1.289e-05	0.3	150	150	0.00068865	$1.132e ext{-}06 \pm 4.644e ext{-}09$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.3	200	150	0.000962116	$1.349e-06 \pm 6.834e-09$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.3	300	150	0.00171489	$6.08\text{e-}06 \pm 2.289\text{e-}08$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.3	500	150	1.92405	$0.000456 \pm 2.064e-06$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.3	1000	150	7.45959	$4.818e-05 \pm 1.84e-07$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.3	1500	150	12.3185	$7.796\text{e-}06 \pm 2.802\text{e-}08$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.3	200	300	0.000962116	$1.144e ext{-07} \pm 4.635e ext{-10}$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.3	300	300	0.00171489	$1.324e ext{-07} \pm 6.534e ext{-10}$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.3	500	300	1.00732	$2.5e-07 \pm 1.113e-09$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.3	1000	300	6.18446	$3.439e-05 \pm 1.376e-07$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.3	1500	300	11.4014	$6.834\text{e-}06 \pm 2.623\text{e-}08$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.3	500	500	1.00732	$1.449 \text{e-} 08 \pm 5.536 \text{e-} 11$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.3	1000	500	4.35099	$1.487 e$ -07 \pm 6.617e-10
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.3	1500	500	9.49035	$4.374e-06 \pm 1.739e-08$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.7	10	1	0.183416	10.2 ± 0.03649
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.7	20	1	0.384439	5.462 ± 0.02022
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.7	50	1	0.97363	1.558 ± 0.004491
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.7	100	1	1.95089	0.3568 ± 0.001143
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.7	150	1	2.92744	0.1161 ± 0.0003685
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.7	200	1	3.90395	0.04995 ± 0.0001494
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.7	300	1	5.85789	$0.01649 \pm 5.579 \mathrm{e} ext{-}05$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.7	500	1	15.2323	$0.003313 \pm 1.464e-05$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.7	1000	1	43.1851	$0.0002823 \pm 1.233e-06$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.7	1500	1	68.8045	$4.481e ext{-05} \pm 1.885e ext{-07}$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.7	10	10	0.0000310229	0.02403 ± 0.0001038
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.7	20	10	0.000343511	0.08347 ± 0.0004742
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.7	50	10	0.751635	1.553 ± 0.004764
0.7 200 10 3.84619 0.04984 ± 0.0001855 0.7 300 10 5.81933 $0.01649 \pm 6.843e-05$ 0.7 500 10 15.2092 $0.003301 \pm 1.289e-05$ 0.7 1000 10 43.1735 $0.0002815 \pm 1.129e-06$	0.7	100	10	1.83626	0.3569 ± 0.0009501
0.730010 5.81933 $0.01649 \pm 6.843e$ -050.750010 15.2092 $0.003301 \pm 1.289e$ -050.7100010 43.1735 $0.0002815 \pm 1.129e$ -06	0.7	150	10	2.85058	0.1165 ± 0.0004139
0.7 500 10 15.2092 0.003301 \pm 1.289e-05 0.7 1000 10 43.1735 0.0002815 \pm 1.129e-06	0.7	200	10	3.84619	0.04984 ± 0.0001855
0.7 1000 10 43.1735 0.0002815 \pm 1.129e-06	0.7	300	10	5.81933	$0.01649 \pm 6.843 \text{e-}05$
	0.7	500	10	15.2092	$0.003301 \pm 1.289 e\text{-}05$
0.7 1500 10 68.7967 4.491e-05 \pm 2.108e-07	0.7	1000	10	43.1735	$0.0002815 \pm 1.129e\text{-}06$
	0.7	1500	10	68.7967	$4.491e-05 \pm 2.108e-07$

Table C.1 – continued from previous page

0.7 10 50 0.000310229 0.000511 ± 1.977e-06 0.7 20 50 0.000343511 0.0005184 ± 2.146e-06 0.7 50 50 0.00114442 0.0006176 ± 3.053e-06 0.7 100 50 0.00241277 0.003681 ± 1.333e-05 0.7 150 50 1.21473 0.1156 ± 0.0003755 0.7 200 50 2.53791 0.04988 ± 0.0001824 0.7 300 50 4.91106 0.01651 ± 6.317e-05 0.7 1000 50 42.8935 0.0002794 ± 1.049e-06 0.7 1500 50 42.8935 0.0002794 ± 1.049e-06 0.7 1500 50 68.6098 4.46e-05 ± 1.989e-07 0.7 150 150 0.00374932 3.327e-05 ± 1.861e-07 0.7 150 150 0.0033663 0.0001787 ± 7.694e-07 0.7 200 150 0.00333663 0.0001787 ± 7.694e-07 0.7 300 150 0.00333663 0.0001787 ± 7.694e-07 0.7 1500 150 40.6133 0.0002573 ± 1.014e-06 0.7 1500 150 40.6133 0.0002573 ± 1.014e-06 0.7 1500 150 67.0675 4.239e-05 ± 1.547e-08 0.7 150 300 0.00374932 3.227e-06 ± 1.433e-08 0.7 200 300 0.00523819 3.393e-06 ± 1.437e-08 0.7 150 300 0.00333663 3.918e-06 ± 1.437e-08 0.7 200 300 0.00523819 3.393e-06 ± 1.437e-08 0.7 150 300 0.00374932 3.227e-06 ± 1.437e-08 0.7 150 300 300 0.00374932 3.227e-06 ± 1.437e-08 0.7 1500 300 5.4843 7.383e-06 ± 2.87e-08 0.7 1500 300 5.4843 7.383e-06 ± 2.87e-08 0.7 1500 300 5.4843 4.301e-07 ± 1.836e-09 0.7 1500 300 5.4843 4.301e-07 ± 1.836e-09 0.7 1500 500 5.4843 4.301e-07 ± 1.836e-09 0.7 1500 500 5.4843 4.301e-07 ± 1.836e-09 0.7 1500 500 5.4843 4.301e-07 ± 1.836e-09 1. 10 1 0.374318 20.79 ± 0.08102 1. 20 1 0.784569 11.08 ± 0.0396 1. 10 1 1.987 3.146 ± 0.01331 1. 10 1 1 0.374318 20.79 ± 0.08102 1. 20 1 0.784569 11.08 ± 0.0396 1. 100 1 1.987 3.146 ± 0.01331 1. 150 1 1.987 3.146 ± 0.01331 1. 150 1 1.987 0.2354 ± 0.0008189 1. 200 1 1.796724 0.1009 ± 0.0003854 1. 300 1 11.984 0.03369 ± 0.0001155 1. 500 1 1.40417 9.244e-05 ± 4.273e-07 1. 100 0 0.000063312 0.0005705 ± 2.817e-06 1. 100 0 0.000063312 0.0005705 ± 2.817e-06 1. 100 0 0.000063312 0.0005705 ± 2.817e-06 1. 100 0 0.00006312 0.1009 ± 0.00035 1. 20 10 0.000071043 0.3475 ± 0.000265	Coupling (g)	m_{Phi} [GeV]		Γ_{min} [GeV]	σ
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.7	10	50	0.0000310229	0.000511 ± 1.977e-06
0.7 100 50 0.00241277 0.003681 ± 1.333e-05 0.7 150 50 1.21473 0.1156 ± 0.0003755 0.7 200 50 2.53791 0.04988 ± 0.0001824 0.7 300 50 4.91106 0.01651 ± 6.317e-05 0.7 500 50 4.91106 0.01651 ± 6.317e-05 0.7 1000 50 42.8935 0.002794 ± 1.049e-06 0.7 1500 50 68.6098 4.46e-05 ± 1.989e-07 0.7 150 150 0.00241277 2.968e-05 ± 1.364e-07 0.7 150 150 0.00374932 3.327e-05 ± 1.594e-07 0.7 200 150 0.00523819 4.04e-05 ± 1.861e-07 0.7 200 150 0.00523819 4.04e-05 ± 1.861e-07 0.7 200 150 0.00523819 4.04e-05 ± 1.861e-07 0.7 1000 150 40.6133 0.00223 ± 1.014e-06 0.7 1000 300 0.00241277 3.132e-06 ± 1.54re-08 <td>0.7</td> <td>20</td> <td>50</td> <td>0.000343511</td> <td>$0.0005184 \pm 2.146e-06$</td>	0.7	20	50	0.000343511	$0.0005184 \pm 2.146e-06$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.7	50	50	0.00114442	$0.0006176 \pm 3.053e-06$
0.7 200 50 2.53791 0.04988 ± 0.0001824 0.7 300 50 4.91106 0.01651 ± 6.317e-05 0.7 500 50 14.6535 0.003218 ± 1.523e-05 0.7 1000 50 42.8935 0.0002794 ± 1.049e-06 0.7 1500 50 68.6098 4.46e-05 ± 1.989e-07 0.7 100 150 0.00241277 2.968e-05 ± 1.364e-07 0.7 150 150 0.00374932 3.327e-05 ± 1.594e-07 0.7 200 150 0.00523819 4.04e-05 ± 1.861e-07 0.7 300 150 0.00933663 0.0001787 ± 7.694e-07 0.7 300 150 0.00933663 0.0001787 ± 7.694e-07 0.7 1000 150 40.6133 0.000253 ± 1.014e-06 0.7 1500 150 40.6133 0.0002573 ± 1.014e-06 0.7 150 150 67.0675 4.239e-05 ± 1.707e-07 0.7 150 300 0.00374932 3.227e-06 ± 1.433e-08	0.7	100	50	0.00241277	$0.003681 \pm 1.333e-05$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.7	150	50	1.21473	0.1156 ± 0.0003755
0.7 500 50 14.6535 0.003218 ± 1.523e-05 0.7 1000 50 42.8935 0.0002794 ± 1.049e-06 0.7 1500 50 68.6098 4.46e-05 ± 1.989e-07 0.7 100 150 0.00241277 2.968e-05 ± 1.364e-07 0.7 150 150 0.00374932 3.327e-05 ± 1.594e-07 0.7 200 150 0.00523819 4.04e-05 ± 1.861e-07 0.7 300 150 0.00933663 0.0001787 ± 7.694e-07 0.7 500 150 10.4754 0.00243 ± 1.128e-05 0.7 1000 150 40.6133 0.0002573 ± 1.014e-06 0.7 1500 150 67.0675 4.239e-05 ± 1.707e-07 0.7 100 300 0.00241277 3.132e-06 ± 1.547e-08 0.7 150 300 0.00374932 3.227e-06 ± 1.433e-08 0.7 150 300 0.00523819 3.393e-06 ± 1.437e-08 0.7 150 300 5.4843 7.383e-06 ± 2.87e-08	0.7	200	50	2.53791	0.04988 ± 0.0001824
0.7 1000 50 42.8935 0.0002794 ± 1.049e-06 0.7 1500 50 68.6098 4.46e-05 ± 1.989e-07 0.7 100 150 0.00241277 2.968e-05 ± 1.364e-07 0.7 150 150 0.00374932 3.327e-05 ± 1.594e-07 0.7 200 150 0.00523819 4.04e-05 ± 1.861e-07 0.7 300 150 0.00933663 0.0001787 ± 7.694e-07 0.7 500 150 10.4754 0.00243 ± 1.128e-05 0.7 1000 150 40.6133 0.0002573 ± 1.014e-06 0.7 1500 150 67.0675 4.239e-05 ± 1.707e-07 0.7 100 300 0.00241277 3.132e-06 ± 1.547e-08 0.7 150 300 0.00374932 3.227e-06 ± 1.433e-08 0.7 150 300 0.00374932 3.227e-06 ± 1.433e-08 0.7 200 300 0.00374932 3.227e-06 ± 1.437e-08 0.7 300 300 0.0033663 3.918e-06 ± 1	0.7	300	50	4.91106	$0.01651 \pm 6.317 e$ -05
0.7 1500 50 68.6098 4.46e-05 ± 1.989e-07 0.7 100 150 0.00241277 2.968e-05 ± 1.364e-07 0.7 150 150 0.00374932 3.327e-05 ± 1.594e-07 0.7 200 150 0.00523819 4.04e-05 ± 1.861e-07 0.7 300 150 0.00933663 0.0001787 ± 7.694e-07 0.7 500 150 10.4754 0.00243 ± 1.128e-05 0.7 1000 150 40.6133 0.0002573 ± 1.014e-06 0.7 1500 150 67.0675 4.239e-05 ± 1.707e-07 0.7 100 300 0.00241277 3.132e-06 ± 1.547e-08 0.7 150 300 0.00274932 3.227e-06 ± 1.433e-08 0.7 150 300 0.00523819 3.393e-06 ± 1.437e-08 0.7 200 300 0.00933663 3.918e-06 ± 1.628e-08 0.7 500 300 5.4843 7.383e-06 ± 2.87e-08 0.7 1500 300 62.0745 3.644e-05 ± 1.47	0.7	500	50	14.6535	$0.003218 \pm 1.523e-05$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.7	1000	50	42.8935	$0.0002794 \pm 1.049e$ -06
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.7	1500	50	68.6098	$4.46 ext{e-}05 \pm 1.989 ext{e-}07$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.7	100	150	0.00241277	$2.968 ext{e-o5} \pm 1.364 ext{e-o7}$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.7	150	150	0.00374932	$3.327e-05 \pm 1.594e-07$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.7	200	150	0.00523819	$4.04\text{e-}05 \pm 1.861\text{e-}07$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.7	300	150	0.00933663	$0.0001787 \pm 7.694 e$ -07
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.7	500	150	10.4754	0.00243 \pm 1.128e-05
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.7	1000	150	40.6133	$0.0002573 \pm 1.014e-06$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.7	1500	150	67.0675	$4.239 ext{e-o5} \pm 1.707 ext{e-o7}$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.7	100	300	0.00241277	$3.132e\text{-}06 \pm 1.547e\text{-}08$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.7	150	300	0.00374932	$3.227e-06 \pm 1.433e-08$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.7	200	300	0.00523819	$3.393\text{e-}06 \pm 1.437\text{e-}08$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.7	300	300	0.00933663	$3.918\text{e-}06 \pm 1.628\text{e-}08$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.7	500	300	5.4843	7.383 e-06 \pm 2.87e-08
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.7	1000	300	33.6709	$0.0001801 \pm 7.992e$ -07
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.7	1500	300	62.0745	$3.644e-05 \pm 1.473e-07$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.7	500	500	5.4843	$4.301 ext{e-o7} \pm 1.836 ext{e-o9}$
1.101 0.374318 20.79 ± 0.08102 1.201 0.784569 11.08 ± 0.0396 1.501 1.987 3.146 ± 0.01331 1.1001 3.98141 0.7199 ± 0.002775 1.1501 5.97437 0.2354 ± 0.0008189 1.2001 7.96724 0.1009 ± 0.0003854 1.3001 11.9549 0.03369 ± 0.0001155 1.5001 31.0863 $0.006652 \pm 2.898e-05$ 1.10001 88.1329 $0.0005705 \pm 2.817e-06$ 1.15001 140.417 $9.244e-05 \pm 4.273e-07$ 1.1010 0.000063312 0.1009 ± 0.00035 1.2010 0.000063312 0.1009 ± 0.000265	0.7	1000	500	23.6887	$3.684 \text{e-}06 \pm 2.358 \text{e-}08$
1.201 0.784569 11.08 ± 0.0396 1.501 1.987 3.146 ± 0.01331 1. 100 1 3.98141 0.7199 ± 0.002775 1. 150 1 5.97437 0.2354 ± 0.0008189 1. 200 1 7.96724 0.1009 ± 0.0003854 1. 300 1 11.9549 0.03369 ± 0.0001155 1. 500 1 31.0863 $0.006652 \pm 2.898e-05$ 1. 1000 1 88.1329 $0.0005705 \pm 2.817e-06$ 1. 1500 1 140.417 $9.244e-05 \pm 4.273e-07$ 1. 10 10 0.000063312 0.1009 ± 0.00035 1. 20 10 0.000701043 0.3475 ± 0.002265	0.7	1500	500	51.6697	$2.291e-05 \pm 9.843e-08$
1.501 1.987 3.146 ± 0.01331 1.1001 3.98141 0.7199 ± 0.002775 1.1501 5.97437 0.2354 ± 0.0008189 1.2001 7.96724 0.1009 ± 0.0003854 1.3001 11.9549 0.03369 ± 0.0001155 1.5001 31.0863 $0.006652 \pm 2.898e-05$ 1.10001 88.1329 $0.0005705 \pm 2.817e-06$ 1.15001 140.417 $9.244e-05 \pm 4.273e-07$ 1.1010 0.000063312 0.1009 ± 0.00035 1.2010 0.000701043 0.3475 ± 0.002265	1.	10	1	0.374318	20.79 ± 0.08102
1.1001 3.98141 0.7199 ± 0.002775 1.1501 5.97437 0.2354 ± 0.0008189 1.2001 7.96724 0.1009 ± 0.0003854 1.3001 11.9549 0.03369 ± 0.0001155 1.5001 31.0863 $0.006652 \pm 2.898e-05$ 1.10001 88.1329 $0.0005705 \pm 2.817e-06$ 1.15001 140.417 $9.244e-05 \pm 4.273e-07$ 1.1010 0.000063312 0.1009 ± 0.00035 1.2010 0.000701043 0.3475 ± 0.002265	1.	20	1	0.784569	11.08 ± 0.0396
1.1501 5.97437 0.2354 ± 0.0008189 1.2001 7.96724 0.1009 ± 0.0003854 1.3001 11.9549 0.03369 ± 0.0001155 1.5001 31.0863 $0.006652 \pm 2.898e-05$ 1.10001 88.1329 $0.0005705 \pm 2.817e-06$ 1.15001 140.417 $9.244e-05 \pm 4.273e-07$ 1.1010 0.000063312 0.1009 ± 0.00035 1.2010 0.000701043 0.3475 ± 0.002265	1.	50	1	1.987	3.146 ± 0.01331
1. 200 1 7.96724 0.1009 ± 0.0003854 1. 300 1 11.9549 0.03369 ± 0.0001155 1. 500 1 31.0863 $0.006652 \pm 2.898e-05$ 1. 1000 1 88.1329 $0.0005705 \pm 2.817e-06$ 1. 1500 1 140.417 $9.244e-05 \pm 4.273e-07$ 1. 10 10 0.000063312 0.1009 ± 0.00035 1. 20 10 0.000701043 0.3475 ± 0.002265	1.	100	1	3.98141	0.7199 ± 0.002775
1.3001 11.9549 0.03369 ± 0.0001155 1.5001 31.0863 $0.006652 \pm 2.898e-05$ 1. 1000 1 88.1329 $0.0005705 \pm 2.817e-06$ 1. 1500 1 140.417 $9.244e-05 \pm 4.273e-07$ 1.1010 0.000063312 0.1009 ± 0.00035 1.2010 0.000701043 0.3475 ± 0.002265	1.	150	1	5.97437	0.2354 ± 0.0008189
1.500131.0863 $0.006652 \pm 2.898e-05$ 1.1000188.1329 $0.0005705 \pm 2.817e-06$ 1.15001140.417 $9.244e-05 \pm 4.273e-07$ 1.1010 0.000063312 0.1009 ± 0.00035 1.2010 0.000701043 0.3475 ± 0.002265	1.	200	1	7.96724	0.1009 ± 0.0003854
1.1000188.1329 $0.0005705 \pm 2.817e-06$ 1.15001 140.417 $9.244e-05 \pm 4.273e-07$ 1.1010 0.000063312 0.1009 ± 0.00035 1.2010 0.000701043 0.3475 ± 0.002265	1.	300	1	11.9549	0.03369 ± 0.0001155
1.15001140.4179.244e-05 \pm 4.273e-071.10100.0000633120.1009 \pm 0.000351.20100.0007010430.3475 \pm 0.002265	1.	500	1	31.0863	$0.006652 \pm 2.898 \text{e-}05$
1. 10 10 0.000063312 0.1009 \pm 0.00035 1. 20 10 0.000701043 0.3475 \pm 0.002265	1.	1000	1	88.1329	$0.0005705 \pm 2.817e-06$
1. 20 10 0.000701043 0.3475 ± 0.002265	1.	1500	1	140.417	9.244 e-05 \pm 4.273e-07
	1.	10	10	0.000063312	0.1009 ± 0.00035
1. 50 10 1.53395 3.139 ± 0.01028	1.	20	10	0.000701043	0.3475 ± 0.002265
	1.	50	10	1.53395	3.139 ± 0.01028

Table C.1 – continued from previous page

Coupling (g)	m_{Phi} [GeV]		Γ_{min} [GeV]	σ
1.	100	10	3.74747	0.7158 ± 0.002486
1.	150	10	5.81752	0.236 ± 0.0007591
1.	200	10	7.84937	0.1013 ± 0.0003668
1.	300	10	11.8762	0.03374 ± 0.0001403
1.	500	10	31.0391	$0.006631 \pm 2.585e-05$
1.	1000	10	88.1093	$0.0005663 \pm 2.515e-06$
1.	1500	10	140.401	$9.408 ext{e-o5} \pm 4.698 ext{e-o7}$
1.	10	50	0.000063312	$0.00212 \pm 8.815 e\text{-}06$
1.	20	50	0.000701043	$0.002149 \pm 9.604 e$ -06
1.	50	50	0.00233555	$0.002568 \pm 1.017e-05$
1.	100	50	0.00492402	0.01523 ± 5.043 e-05
1.	150	50	2.47905	0.2351 ± 0.0008404
1.	200	50	5.1794	0.09993 ± 0.0003164
1.	300	50	10.0226	0.03349 ± 0.0001351
1.	500	50	29.9052	$0.006402 \pm 2.604e-05$
1.	1000	50	87.5378	$0.0005634 \pm 2.601e-06$
1.	1500	50	140.02	$9.211e-05 \pm 4.909e-07$
1.	100	150	0.00492402	$0.0001247 \pm 5.899 e - 07$
1.	150	150	0.00765167	0.0001387 ± 5.889 e-07
1.	200	150	0.0106902	0.000168 ± 7.656 e-07
1.	300	150	0.0190543	$0.0007464 \pm 2.977e-06$
1.	500	150	21.3784	$0.004856 \pm 1.95 e - 05$
1.	1000	150	82.8844	$0.0005122 \pm 1.98e-06$
1.	1500	150	136.872	$8.662e-05 \pm 3.821e-07$
1.	200	300	0.0106902	$1.422e-05 \pm 6.147e-08$
1.	300	300	0.0190543	$1.626e-05 \pm 6.865e-08$
1.	500	300	11.1924	$3.081e-05 \pm 1.244e-07$
1.	1000	300	68.7162	$0.0003534 \pm 1.392e-06$
1.	1500	300	126.683	$7.258e-05 \pm 3.651e-07$
1.	500	500	11.1924	$1.777e-06 \pm 9.67e-09$
1.	1000	500	48.3444	$1.331e-05 \pm 6.551e-08$
1.	1500	500	105.448	$4.443e-05 \pm 1.988e-07$
1.5	10	1	0.842215	46.59 ± 0.1797
1.5	20	1	1.76528	24.52 ± 0.08387
1.5	50	1	4.47075	6.903 ± 0.02244
1.5	100	1	8.95817	1.577 ± 0.005493
1.5	150	1	13.4423	0.5224 ± 0.002309
1.5	200	1	17.9263	0.2259 ± 0.0008625
1.5	300	1	26.8985	0.07529 ± 0.0003407
1.5	500	1	69.9442	$0.01445 \pm 6.469e-05$
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Table C.1 – continued from previous page

Coupling (g)			Γ_{min} [GeV]	σ
1.5	1000	1	198.299	0.001234 ± 5.694e-06
1.5	1500	1	315.939	$0.0002179 \pm 1.024e-06$
1.5	10	10	0.000142452	0.5117 ± 0.002037
1.5	20	10	0.00157735	1.763 ± 0.01031
1.5	50	10	3.45138	6.906 ± 0.02283
1.5	100	10	8.4318	1.568 ± 0.006489
1.5	150	10	13.0894	0.5162 ± 0.001934
1.5	200	10	17.6611	0.2249 ± 0.0008153
1.5	300	10	26.7214	0.07541 ± 0.0002941
1.5	500	10	69.8379	$0.01447 \pm 6.923 \text{e-}05$
1.5	1000	10	198.246	$0.001242 \pm 6.739e-06$
1.5	1500	10	315.903	0.0002157 ± 8.805 e-07
1.5	10	50	0.000142452	$0.01068 \pm 4.527 e$ -05
1.5	20	50	0.00157735	$0.01093 \pm 6.079 \text{e-}05$
1.5	50	50	0.00525498	$0.01302 \pm 6.649 \text{e-}05$
1.5	100	50	0.011079	0.07677 ± 0.0002445
1.5	150	50	5.57786	0.5195 ± 0.001577
1.5	200	50	11.6536	0.2195 ± 0.0006711
1.5	300	50	22.5508	0.07353 ± 0.0003291
1.5	500	50	67.2866	$0.0139 \pm 6.13e-05$
1.5	1000	50	196.96	$0.001209 \pm 7.038e-06$
1.5	1500	50	315.045	$0.0002109 \pm 8.631e-07$
1.5	100	150	0.011079	$0.0006295 \pm 3.008e-06$
1.5	150	150	0.0172162	$0.000706 \pm 3.661e-06$
1.5	200	150	0.0240529	$0.00086 \pm 3.608 e\text{-}06$
1.5	300	150	0.0428723	$0.003751 \pm 1.304e-05$
1.5	500	150	48.1013	$0.01046 \pm 4.013e-05$
1.5	1000	150	186.49	$0.001072 \pm 4.469e-06$
1.5	1500	150	307.963	$0.0001931 \pm 1.022e-06$
1.5	200	300	0.0240529	$7.176e-05 \pm 3.641e-07$
1.5	300	300	0.0428723	$8.3e-05 \pm 3.627e-07$
1.5	500	300	25.183	$0.000155 \pm 6.658 e$ -07
1.5	1000	300	154.611	$0.0007234 \pm 2.773e-06$
1.5	1500	300	285.036	$0.0001529 \pm 7.694e$ -07
1.5	500	500	25.183	$9.099e-06 \pm 4.301e-08$
1.5	1000	500	108.775	$5.335e-05 \pm 2.699e-07$
1.5	1500	500	237.259	$8.736\text{e-}05 \pm 4.268\text{e-}07$
2.	10	1	1.49727	82.65 ± 0.3408
2.	20	1	3.13828	43.1 ± 0.1487
2.	50	1	7.948	11.84 ± 0.04278

Table C.1 – continued from previous page

Coupling (g)	m_{Phi} [GeV]	m_{χ} [GeV]	Γ_{min} [GeV]	σ
2.	100	1	15.9256	2.712 ± 0.01209
2.	150	1	23.8975	0.9056 ± 0.004237
2.	200	1	31.869	0.3952 ± 0.001653
2.	300	1	47.8195	0.132 ± 0.0004713
2.	500	1	124.345	0.02461 ± 0.0001101
2.	1000	1	352.532	$0.002071 \pm 1.061e-05$
2.	1500	1	561.669	$0.0003815 \pm 1.4e-06$
2.	10	10	0.000253248	1.627 ± 0.005672
2.	20	10	0.00280417	5.528 ± 0.03152
2.	50	10	6.13579	11.98 ± 0.04005
2.	100	10	14.9899	2.696 ± 0.01091
2.	150	10	23.2701	0.8981 ± 0.004067
2.	200	10	31.3975	0.3921 ± 0.001675
2.	300	10	47.5047	0.1312 ± 0.0005524
2.	500	10	124.156	0.02454 ± 0.0001302
2.	1000	10	352.437	$0.002051 \pm 9.73e-06$
2.	1500	10	561.606	$0.0003797 \pm 1.522e-06$
2.	10	50	0.000253248	0.03397 ± 0.0001354
2.	20	50	0.00280417	0.03452 ± 0.0001623
2.	50	50	0.00934219	0.04088 ± 0.0001623
2.	100	50	0.0196961	0.24 ± 0.0008579
2.	150	50	9.9162	0.8991 ± 0.002903
2.	200	50	20.7176	0.382 ± 0.001411
2.	300	50	40.0903	0.1287 ± 0.0005596
2.	500	50	119.621	0.02328 ± 0.0001255
2.	1000	50	350.151	$0.001995 \pm 1.184e-05$
2.	1500	50	560.08	$0.0003671 \pm 1.741e-06$
2.	10	150	0.000253248	$0.001822 \pm 7.946e-06$
2.	20	150	0.00280417	$0.001842 \pm 8.453e-06$
2.	50	150	0.00934219	$0.00187 \pm 8.818 \text{e-}06$
2.	100	150	0.0196961	0.001985 ± 8.101 e-06
2.	150	150	0.0306067	$0.002231 \pm 1.131e-05$
2.	200	150	0.0427607	$0.002694 \pm 1.215 e\text{-}05$
2.	300	150	0.0762174	$0.01186 \pm 4.862e-05$
2.	500	150	85.5134	$0.01769 \pm 8.02e-05$
2.	1000	150	331.538	$0.001716 \pm 7.617e-06$
2.	1500	150	547.49	$0.0003242 \pm 1.537e-06$
2.	100	300	0.0196961	$0.0002092 \pm 8.197e-07$
2.	150	300	0.0306067	$0.0002152 \pm 8.37e-07$
2.	200	300	0.0427607	0.0002275 ± 8.607e-07

Table C.1 – continued from previous page

Coupling (g)	m_{Phi} [GeV]		Γ_{min} [GeV]	σ
2.	300	300	0.0762174	0.0002609 ± 1.05e-06
2.	500	300	44.7698	0.0004931 \pm 2.01e-06
2.	1000	300	274.865	$0.001119 \pm 5.167e-06$
2.	1500	300	506.731	$0.0002432 \pm 1.053e-06$
2.	300	500	0.0762174	2.367e-05 ± 1.206e-07
2.	500	500	44.7698	$2.871e-05 \pm 1.09e-07$
2.	1000	500	193.378	$0.000131 \pm 5.569 e$ -07
2.	1500	500	421.793	$0.0001323 \pm 5.222e$ -07
2.5	10	1	2.33949	128.4 ± 0.4393
2.5	20	1	4.90356	65.92 ± 0.2248
2.5	50	1	12.4187	17.77 ± 0.0663
2.5	100	1	24.8838	4.051 ± 0.01562
2.5	150	1	37.3398	1.364 ± 0.004927
2.5	200	1	49.7953	0.6008 ± 0.002928
2.5	300	1	74.718	0.2036 ± 0.0008994
2.5	500	1	194.29	0.03629 ± 0.0001865
2.5	1000	1	550.831	$0.002918 \pm 1.235e-05$
2.5	1500	1	877.608	$0.0005639 \pm 2.327e-06$
2.5	10	10	0.0003957	3.918 ± 0.0159
2.5	20	10	0.00438152	13.54 ± 0.05349
2.5	50	10	9.58718	18.03 ± 0.06068
2.5	100	10	23.4217	4.025 ± 0.01458
2.5	150	10	36.3595	1.36 ± 0.00698
2.5	200	10	49.0586	0.5979 ± 0.002445
2.5	300	10	74.2262	0.2016 ± 0.0006995
2.5	500	10	193.994	0.03579 ± 0.0001738
2.5	1000	10	550.683	$0.002902 \pm 1.515e-05$
2.5	1500	10	877.509	$0.0005651 \pm 2.275e-06$
2.5	10	50	0.0003957	0.08298 ± 0.000365
2.5	20	50	0.00438152	0.08474 ± 0.0003631
2.5	50	50	0.0145972	0.09986 ± 0.000455
2.5	100	50	0.0307751	0.5855 ± 0.001667
2.5	150	50	15.4941	1.359 ± 0.005802
2.5	200	50	32.3712	0.5728 ± 0.002188
2.5	300	50	62.6411	0.1938 ± 0.0008665
2.5	500	50	186.907	0.03384 ± 0.0001589
2.5	1000	50	547.111	$0.002773 \pm 1.645e-05$
2.5	1500	50	875.125	$0.0005349 \pm 3.534e-06$
2.5	10	150	0.0003957	$0.004461 \pm 1.951e-05$
2.5	20	150	0.00438152	0.004473 ± 2.159e-05

Table C.1 – continued from previous page

Coupling (g)	m_{Phi} [GeV]	m_{χ} [GeV]	Γ_{min} [GeV]	σ
2.5	50	150	0.0145972	$0.00451 \pm 1.808 e - 05$
2.5	100	150	0.0307751	$0.00486 \pm 1.984 e\text{-}05$
2.5	150	150	0.0478229	$0.00548 \pm 2.35 \text{e-}05$
2.5	200	150	0.0668136	$0.006545 \pm 2.81\text{e-}05$
2.5	300	150	0.11909	0.02878 ± 0.0001168
2.5	500	150	133.615	0.02572 ± 0.00011
2.5	1000	150	518.027	$0.002339 \pm 1.101e\text{-}05$
2.5	1500	150	855.453	$0.0004622 \pm 2.297e-06$
2.5	100	300	0.0307751	$0.0005104 \pm 2.62e-06$
2.5	150	300	0.0478229	$0.000526 \pm 2.091e$ -06
2.5	200	300	0.0668136	$0.0005503 \pm 2.402e-06$
2.5	300	300	0.11909	$0.0006368 \pm 2.911e\text{-}06$
2.5	500	300	69.9528	$0.001197 \pm 4.697 e$ -06
2.5	1000	300	429.476	$0.001499 \pm 6.445 e$ -06
2.5	1500	300	791.767	$0.0003277 \pm 1.439e-06$
2.5	300	500	0.11909	5.773 e-05 \pm 2.645e-07
2.5	500	500	69.9528	$6.973e-05 \pm 3.037e-07$
2.5	1000	500	302.152	$0.0002498 \pm 1.042e$ -06
2.5	1500	500	659.052	$0.000172 \pm 8.531e-07$
3.	10	1	3.36886	185.9 ± 0.8608
3.	20	1	7.06112	92.49 ± 0.3581
3.	50	1	17.883	24.38 ± 0.08507
3.	100	1	35.8327	5.551 ± 0.02275
3.	150	1	53.7693	1.878 ± 0.008801
3.	200	1	71.7052	0.8398 ± 0.004651
3.	300	1	107.594	0.2856 ± 0.001301
3.	500	1	279.777	0.04861 ± 0.0002143
3.	1000	1	793.196	$0.003716 \pm 1.874e-05$
3.	1500	1	1263.76	$0.0007294 \pm 3.217e-06$
3.	10	10	0.000569808	8.181 ± 0.03184
3.	20	10	0.00630938	28.05 ± 0.09412
3.	50	10	13.8055	24.97 ± 0.07128
3.	100	10	33.7272	5.485 ± 0.01916
3.	150	10	52.3576	1.858 ± 0.007406
3.	200	10	70.6443	0.8336 ± 0.003435
3.	300	10	106.886	0.2832 ± 0.001293
3.	500	10	279.352	0.04802 ± 0.0003129
3.	1000	10	792.983	$0.003669 \pm 1.542e-05$
3.	1500	10	1263.61	$0.0007221 \pm 3.036e-06$
3.	10	50	0.000569808	0.1714 ± 0.0007653

Table C.1 – continued from previous page

3. 20 50 0.00630938 0.1751 ± 0.000689 3. 50 50 0.0210199 0.2073 ± 0.001019 3. 100 50 0.0443162 1.21 ± 0.003153 3. 150 50 22.3114 1.896 ± 0.007571 3. 200 50 46.6146 0.787 ± 0.002939 3. 300 50 90.2031 0.2685 ± 0.001344 3. 500 50 269.146 0.04468 ± 0.0002221 3. 1000 50 787.84 0.003505 ± 1.861e-05 3. 1500 50 1260.18 0.0005823 ± 3.857e-06 3. 1500 50 10.000569808 0.0092285 ± 4.234e-05 3. 20 150 0.00630938 0.0092285 ± 4.234e-05 3. 100 150 0.00630938 0.009245 ± 4.234e-05 3. 150 0.0010199 0.009462 ± 3.85e-05 3. 100 150 0.0443162 0.01017 ± 4.443e-05 3. 150 150 0.068865 0.01124 ± 5.221e-05 3. 200 150 0.0062116 0.01366 ± 6.834e-05 3. 300 150 0.171489 0.05937 ± 0.0002495 3. 500 150 192.405 0.03448 ± 0.0001467 3. 1000 150 745.999 0.00288 ± 1.359e-05 3. 1500 150 1231.85 0.0005735 ± 3.925e-06 3. 1500 300 0.0210199 0.00139 ± 3.982e-06 3. 1500 300 0.0443162 0.01016 ± 4.834e-06 3. 1500 300 0.0443162 0.01056 ± 4.834e-06 3. 1500 300 0.068865 0.001096 ± 4.92e-06 3. 1500 300 0.068865 0.001147 ± 5.869e-06 3. 1500 300 0.068865 0.001147 ± 5.869e-06 3. 1500 300 0.068865 0.001147 ± 5.809e-06 3. 1500 300 0.068865 0.0001447 ± 5.7809e-06 3. 1500 300 0.071489 0.001327 ± 6.728e-06 3. 1500 300 100.732 0.00245 ± 9.636e-06 3. 1500 300 100.732 0.00245 ± 9.636e-06 3. 1500 300 100.732 0.00246 ± 5.124e-07 3. 300 500 0.0962116 0.001147 ± 5.27e-07 3. 300 500 0.0962116 0.001147 ± 5.29e-06 3. 1500 300 100.732 0.000246 ± 5.124e-07 3. 1500 500 0.0962116 0.001147 ± 5.29e-06 3. 1500 300 100.732 0.0001447 ± 6.102e-07 3. 1500 500 0.0962116 0.001147 ± 6.102e-07 3. 1500 500 100.732 0.0001447 ± 6.102e-07 3. 1500 500 10	Coupling (g)	m_{Phi} [GeV]		From previous Γ_{min} [GeV]	σ
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3.51001 48.7723 7.04 ± 0.02954 3.51501 73.186 2.417 ± 0.01038 3.52001 97.5987 1.089 ± 0.004308	3.5	20	1	9.61097	123.8 ± 0.4645
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	3.5	50	1	24.3407	31.59 ± 0.09614
3.5 200 1 97.5987 1.089 ± 0.004308	3.5	100	1	48.7723	7.04 ± 0.02954
	3.5	150	1	73.186	2.417 ± 0.01038
3.5 300 1 146.447 0.3709 ± 0.001616	3.5	200	1	97.5987	1.089 ± 0.004308
	3.5	300	1	146.447	0.3709 ± 0.001616

Table C.1 – continued from previous page

Coupling (g)	m_{Phi} [GeV]	m_{χ} [GeV]	Γ_{min} [GeV]	σ
3.5	500	1	380.808	0.06035 ± 0.0003762
3.5	1000	1	1079.63	$0.004345 \pm 2.711e-05$
3.5	1500	1	1720.11	$0.0008581 \pm 3.653e-06$
3.5	10	10	0.000775572	15.08 ± 0.0569
3.5	20	10	0.00858777	51.42 ± 0.1478
3.5	50	10	18.7909	32.56 ± 0.1113
3.5	100	10	45.9065	6.963 ± 0.03199
3.5	150	10	71.2646	2.38 ± 0.009493
3.5	200	10	96.1548	1.079 ± 0.004244
3.5	300	10	145.483	0.369 ± 0.001602
3.5	500	10	380.229	0.05978 ± 0.0003017
3.5	1000	10	1079.34	$0.004302 \pm 2.412e-05$
3.5	1500	10	1719.92	$0.0008525 \pm 3.878e-06$
3.5	10	50	0.000775572	0.3176 ± 0.001314
3.5	20	50	0.00858777	0.3229 ± 0.001215
3.5	50	50	0.0286105	0.3857 ± 0.001618
3.5	100	50	0.0603192	2.228 ± 0.00751
3.5	150	50	30.3684	2.477 ± 0.008787
3.5	200	50	63.4476	1.025 ± 0.003864
3.5	300	50	122.776	0.3483 ± 0.001614
3.5	500	50	366.338	0.05534 ± 0.0003035
3.5	1000	50	1072.34	$0.004076 \pm 2.371e-05$
3.5	1500	50	1715.24	$0.0008077 \pm 4.889e-06$
3.5	10	150	0.000775572	$0.01719 \pm 9.115 \text{e-}05$
3.5	20	150	0.00858777	$0.01719 \pm 8.334e-05$
3.5	50	150	0.0286105	$0.01754 \pm 8.239e-05$
3.5	100	150	0.0603192	$0.01855 \pm 8.371e-05$
3.5	150	150	0.0937329	0.02099 ± 0.0001038
3.5	200	150	0.130955	0.0252 ± 0.0001138
3.5	300	150	0.233416	0.1096 ± 0.0006465
3.5	500	150	261.885	0.04374 \pm 0.0002091
3.5	1000	150	1015.33	0.00334 \pm 1.751e-05
3.5	1500	150	1676.69	$0.0006583 \pm 3.614e-06$
3.5	10	300	0.000775572	$0.001925 \pm 9.279e-06$
3.5	20	300	0.00858777	$0.001916 \pm 1.026e-05$
3.5	50	300	0.0286105	0.001918 ± 8.166 e-06
3.5	100	300	0.0603192	$0.001958 \pm 7.426e-06$
3.5	150	300	0.0937329	$0.002036 \pm 8.81e-06$
3.5	200	300	0.130955	$0.002123 \pm 8.379e-06$
3.5	300	300	0.233416	0.002448 ± 9.259e-06

Table C.1 – continued from previous page

Coupling (g)	m_{Phi} [GeV]	m_{χ} [GeV]	Γ_{min} [GeV]	σ
3.5	500	300	137.107	0.004413 ± 2.588e-05
3.5	1000	300	841.774	$0.002184 \pm 1.014e-05$
3.5	1500	300	1551.86	$0.0004471 \pm 2.349e-06$
3.5	10	500	0.000775572	0.0002016 ± 7.906 e-07
3.5	20	500	0.00858777	$0.0002011 \pm 9.138e-07$
3.5	50	500	0.0286105	$0.0002018 \pm 9.929 e$ -07
3.5	100	500	0.0603192	$0.0002033 \pm 8.104 e$ -07
3.5	150	500	0.0937329	0.0002067 ± 8.026 e-07
3.5	200	500	0.130955	$0.0002106 \pm 8.439e-07$
3.5	300	500	0.233416	$0.0002225 \pm 9.256 e$ -07
3.5	500	500	137.107	$0.0002686 \pm 1.162e\text{-}06$
3.5	1000	500	592.219	$0.0005877 \pm 2.823e-06$
3.5	1500	500	1291.74	0.0002318 \pm 1.11e-06

846 Bibliography

875

[A⁺14a] Georges Aad et al. Search for new particles in events 847 with one lepton and missing transverse momentum in pp collisions at $\sqrt{s} = 8$ TeV with the ATLAS detector. JHEP, 1409:037, 2014. 850 [A+14b] Jalal Abdallah et al. Simplified Models for Dark 851 Matter and Missing Energy Searches at the LHC. 852 arXiv:1409.2893, 2014. [A⁺15] Georges Aad et al. Search for new phenomena in final 854 states with an energetic jet and large missing transverse momentum in pp collisions at $\sqrt{s} = 8$ TeV with the 856 ATLAS detector. 2015. 857 [Aad14a] Search for dark matter in events with a hadronically de-858 caying W or Z boson and missing transverse momentum in pp collisions at $\sqrt{s} = 8$ TeV with the ATLAS detector. Phys.Rev.Lett., 112(4):041802, 2014. 861 [Aad14b] Search for dark matter in events with a Z boson and 862 missing transverse momentum in pp collisions at \sqrt{s} =8 863 TeV with the ATLAS detector. Phys.Rev., D90(1):012004, 2014. 865 [Aad15] Search for new phenomena in events with a photon and missing transverse momentum in pp collisions at $\sqrt{s} = 8$ 867 TeV with the ATLAS detector. *Phys.Rev.*, D91(1):012008, 2015. [ADR⁺14] Mohammad Abdullah, Anthony DiFranzo, Arvind 870 Rajaraman, Tim M.P. Tait, Philip Tanedo, et al. Hidden on-shell mediators for the Galactic Center γ -ray excess. 872 Phys. Rev., D90(3):035004, 2014. 873 [ATL14] Sensitivity to WIMP Dark Matter in the Final States 874

Containing Jets and Missing Transverse Momentum

with the ATLAS Detector at 14 TeV LHC. Technical

882

- Report ATL-PHYS-PUB-2014-007, CERN, Geneva, Jun 2014.
- [AWZ14] Haipeng An, Lian-Tao Wang, and Hao Zhang. Dark matter with *t*-channel mediator: a simple step beyond contact interaction. *Phys. Rev. D*, 89:115014, 2014.
 - [BB13] Yang Bai and Joshua Berger. Fermion Portal Dark Matter. *JHEP*, 11:171, 2013.
- [BCD⁺15] Nicole F. Bell, Yi Cai, James B. Dent, Rebecca K. Leane, and Thomas J. Weiler. Dark matter at the LHC: EFTs and gauge invariance. 2015.
- [BDSJ⁺14] Giorgio Busoni, Andrea De Simone, Thomas Jacques,
 Enrico Morgante, and Antonio Riotto. On the Validity
 of the Effective Field Theory for Dark Matter Searches
 at the LHC Part III: Analysis for the *t*-channel. *JCAP*,
 1409:022, 2014.
- [BDSMR14] Giorgio Busoni, Andrea De Simone, Enrico Morgante,
 and Antonio Riotto. On the Validity of the Effective
 Field Theory for Dark Matter Searches at the LHC.
 Phys.Lett., B728:412-421, 2014.
- [BFG15] Matthew R. Buckley, David Feld, and Dorival Goncalves.

 Scalar Simplified Models for Dark Matter. *Phys.Rev.*,
 D91(1):015017, 2015.
- [BT13] Yang Bai and Tim M.P. Tait. Searches with Mono-Leptons. *Phys.Lett.*, B723:384–387, 2013.
- [CDM⁺14] Linda Carpenter, Anthony DiFranzo, Michael Mulhearn, Chase Shimmin, Sean Tulin, et al. Mono-Higgsboson: A new collider probe of dark matter. *Phys.Rev.*, D89(7):075017, 2014.
- [CEHL14] Spencer Chang, Ralph Edezhath, Jeffrey Hutchinson,
 and Markus Luty. Effective WIMPs. *Phys. Rev. D*,
 89:015011, 2014.
- [CHH15] Andreas Crivellin, Ulrich Haisch, and Anthony Hibbs. LHC constraints on gauge boson couplings to dark matter. 2015.
- [CHLR13] R.C. Cotta, J.L. Hewett, M.P. Le, and T.G. Rizzo. Bounds
 on Dark Matter Interactions with Electroweak Gauge
 Bosons. *Phys.Rev.*, D88:116009, 2013.

- [CNS+13] Linda M. Carpenter, Andrew Nelson, Chase Shimmin, 914 Tim M.P. Tait, and Daniel Whiteson. Collider searches for dark matter in events with a Z boson and missing 916 energy. *Phys.Rev.*, D87(7):074005, 2013. 917
- [CRTW14] Randel C. Cotta, Arvind Rajaraman, Tim M. P. Tait, and Alexander M. Wijangco. Particle Physics Implications 919 and Constraints on Dark Matter Interpretations of the 920 CDMS Signal. *Phys.Rev.*, D90(1):013020, 2014.
- [DNRT13] Anthony DiFranzo, Keiko I. Nagao, Arvind Rajaraman, 922 and Tim M. P. Tait. Simplified Models for Dark Matter 923 Interacting With Quarks. *JHEP*, 1311, 2013. 924

926

927

929

930

935

936

937

939

940

- [GIR⁺10] Jessica Goodman, Masahiro Ibe, Arvind Rajaraman, William Shepherd, Tim M.P. Tait, et al. Constraints on Dark Matter from Colliders. Phys. Rev., D82:116010, 2010.
- [HK11] Robert M. Harris and Konstantinos Kousouris. Searches for dijet resonances at hadron colliders. Int. J. Modern Phys., 26(30n31):5005-5055, 2011.
- [HKR13] Ulrich Haisch, Felix Kahlhoefer, and Emanuele Re. QCD effects in mono-jet searches for dark matter. JHEP, 932 1312:007, 2013. 933
 - [HR15] Ulrich Haisch and Emanuele Re. Simplified dark matter top-quark interactions at the LHC. 2015.
 - [K⁺14] Vardan Khachatryan et al. Search for physics beyond the standard model in final states with a lepton and missing transverse energy in proton-proton collisions at $\sqrt{s} = 8$ TeV. 2014.
 - [Kha14] Search for new phenomena in monophoton final states in proton-proton collisions at \sqrt{s} = 8 TeV. 2014.
- [NCC⁺14] Andy Nelson, Linda M. Carpenter, Randel Cotta, Adam 942 Johnstone, and Daniel Whiteson. Confronting the Fermi 943 Line with LHC data: an Effective Theory of Dark Matter Interaction with Photons. Phys. Rev., D89(5):056011, 2014.
- [PVZ14] Michele Papucci, Alessandro Vichi, and Kathryn M. 946 Zurek. Monojet versus the rest of the world I: t-channel models. JHEP, 2014.
- [RWZ15] Davide Racco, Andrea Wulzer, and Fabio Zwirner. Ro-949 bust collider limits on heavy-mediator Dark Matter. 2015. 951

70 ATLAS+CMS DARK MATTER FORUM

[ZBW13] Ning Zhou, David Berge, and Daniel Whiteson. Mono-everything: combined limits on dark matter production at colliders from multiple final states. *Phys.Rev.*, D87(9):095013, 2013.