Version o.1 DRAFT
ATLAS+CMS DARK MATTER FORUM RECOMMENDA- TIONS
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# , Introduction

 $_{8}$  This is a citation test [HK11].

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# Overall choices for simplified models

- General topics:
- choice of Dark Matter type: Dirac (unless specified otherwise) and what we might be missing
- MFV and what we might be missing

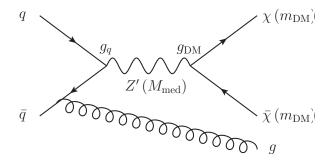


Figure 3.1: The diagram shows the pair production of dark matter particles in association with a parton from the initial state via an s-channel vector or axial-vector mediator. The process if specified by  $(M_{\rm med}, m_{\rm DM}, g_{\rm DM}, g_{\rm q})$ , the mediator and dark matter masses, and the mediator couplings to dark matter and quarks respectively.

### Recommended models for all MET+X analyses

#### 3.1 Vector and axial vector mediator, s-channel exchange

- 8 There are several matrix element implementations of the s-channel
- vector mediated DM production. This is available in POWHEG,
- 20 MADGRAPH and also MCFM. The implementation in POWHEG
- generates DM pair production with 1 parton at next-to-leading or-
- der (NLO), whilst MADGRAPH and MCFM are at leading order
- <sup>23</sup> (LO). As shown in POWHEG Ref. [HKR13], including NLO correc-
- tions result in an enhancement in the cross section as compared to
- LO and though this is not significant, it does lead to a substantial
- reduction in the dependence on the choice of the renormalization
- and factorization scale and hence the theoretical uncertainty on the
- signal prediction. Since NLO calculations are available for the pro-
- 29 cess in POWHEG, we recommend to proceed with POWHEG as the
- 30 generator of choice.

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- We consider the case of a dark matter particle that is a Dirac
- fermion and where the production proceeds via the exchange of a
- spin-1 s-channel mediator. We consider the following interactions
- between the DM and SM fields including a vector mediator with:
  - (a) vector couplings to DM and SM,
- (b) axial-vector couplings to DM and SM.

The corresponding Lagrangians are

$$\mathcal{L}_{\text{vector}} = \sum_{q} g_{q} Z'_{\mu} \bar{q} \gamma^{\mu} q + g_{\text{DM}} Z'_{\mu} \bar{\chi} \gamma^{\mu} \chi \tag{3.1}$$

$$\mathcal{L}_{\text{axial-vector}} = \sum_{q} g_{q} Z'_{\mu} \bar{q} \gamma^{\mu} \gamma^{5} q + g_{\text{DM}} Z'_{\mu} \bar{\chi} \gamma^{\mu} \gamma^{5} \chi \tag{3.2}$$

where the coupling extends over all the quarks and universal cou-

- plings are assumed for all the quarks. It is also possible to consider
- another model in which mixed vector and axial-vector couplings
- are considered, for instance the couplings to the quarks are vector
- whereas those to DM are axial-vector. As a starting point, we con-
- sider only the models with the vector couplings only and axial vector
- couplings only.

We assume that no additional visible or invisible decays contribute

- to the width of the mediator, this is referred to as the minimal width
- and it is defined as follows for the vector and axial-vector models.

$$\Gamma_{\min} = \Gamma_{\bar{\chi}\chi} + \sum_{q} \Gamma_{\bar{q}q} \tag{3.3}$$

47 where the individual contributions to this from the partial width are

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$$\Gamma_{\bar{\chi}\chi}^{V} = \frac{g_{\rm DM}^{2} M_{\rm med}}{12\pi} \left( 1 + \frac{2m_{\rm DM}^{2}}{M_{\rm med}^{2}} \right) \sqrt{1 - \frac{4m_{\rm DM}^{2}}{M_{\rm med}^{2}}} \theta(M_{\rm med} - 2m_{\rm DM}) \quad (3.4)$$

$$\Gamma_{\bar{q}q}^{V} = \frac{3g_{q}^{2}M_{\text{med}}}{12\pi} \left(1 + \frac{2m_{q}^{2}}{M_{\text{med}}^{2}}\right) \sqrt{1 - \frac{4m_{q}^{2}}{M_{\text{med}}^{2}}} \theta(M_{\text{med}} - 2m_{q})$$
(3.5)

$$\Gamma_{\bar{\chi}\chi}^{A} = \frac{g_{\rm DM}^{2} M_{\rm med}}{12\pi} \left( 1 - \frac{4m_{\rm DM}^{2}}{M_{\rm med}^{2}} \right)^{3/2} \theta (M_{\rm med} - 2m_{\rm DM})$$
(3.6)

$$\Gamma_{\bar{q}q}^{A} = \frac{3g_{q}^{2}M_{\text{med}}}{12\pi} \left(1 - \frac{4m_{q}^{2}}{M_{\text{med}}^{2}}\right)^{3/2} \theta(M_{\text{med}} - 2m_{q}), \qquad (3.7)$$

where  $\theta(x)$  denotes the Heaviside step function. Note the color fac-

tor 3 in the quark terms. Figure 3.2 shows the minimal width as a

function of mediator mass for both vector and axial-vector mediators

assuming couplings of 1. With this choice of the couplings, the dom-

inant contribution to the minimal width comes from the quarks due

to the color factor enhancement.

The simplified models described here have four free parameters:

mediator mass  $M_{\text{med}}$ , Dark Matter mass  $m_{\text{DM}}$ , coupling of the medi-

ator to quarks  $g_q$  and coupling of the mediator to Dark Matter  $g_{DM}$ .

In order to determine an optimal choice of the parameter grid for

presentation of the early Run-2 results, dependencies of the kinematic

quantities and cross sections on the individual parameters need to be

Figure 3.2: Minimal width as a func-

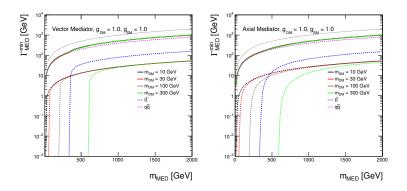
tion of mediator mass for vector and

axial-vector mediator assuming couplings of 1. The total width is shown as solid lines for Dark Matter masses

of 10 GeV, 30 GeV, 100 GeV and 300 GeV in black, red, brown and green, respectively. The individual contributions from Dark Matter are indicated by dotted lines with the same colors. The contribution from all quarks but top is shown as magenta dotted line and the

contribution from top quarks only is illustrated by the dotted blue line. The dotted black line shows the extreme

case  $\Gamma_{\min} = M_{\text{med}}$ .



- studied. The following paragraphs list the main observations from
- the scans over the parameters that support the final proposal for the
- 63 parameter grid.

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- 64 Scan over the couplings Figure 3.3 reveals there are no differences in
- the shape of the  $E_T$  distribution among the samples where the pair of
- 10 GeV Dark Matter particles are produced on-shell from the media-
- tor of 1 TeV, generated with different choice of the coupling strength.
- The considered coupling values range from 0.1 to 1.45, where the
- 69 latter value approximates the maximum allowed coupling value,
- holding  $g_q = g_{\rm DM}$ , such that  $\Gamma_{\rm min} < M_{\rm med}$ . Based on similar plots for
- different choices of mediator and Dark Matter masses, it is concluded
- that the shapes of kinematic distributions are not altered neither for
- the on-shell Dark Matter production where  $M_{
  m med} > 2 m_{
  m DM}$ , nor for
- the off-shell Dark Matter production where  $M_{\rm med} < 2m_{
  m DM}$ . Only
- the cross sections change. Differences in kinematic distributions are
- expected only close to the transition region where both on-shell and off-shell regimes mix.

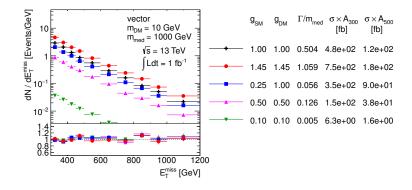


Figure 3.3: Scan over couplings. The  $E_T$  distribution is compared for the vector mediator models using the parameters as indicated. Ratios of the normalized distributions with respect to the first one are shown.  $A_{300}$  and  $A_{500}$  in the table denote the acceptance of the  $E_T > 300 \,\text{GeV}$  and  $E_T > 500 \,\text{GeV}$  cut, respectively.

- The only place where special care needs to be taken are extremely heavy and narrow mediators, in other words with low couplings.
- Figure 3.4 suggests a change in the shape of the  $E_T$  distribution for

5 TeV mediator once  $\Gamma_{\min}/M_{\mathrm{med}}$  gets down to the order of percent or below. This, however, does not come from physics as it is a feature of 82 the generator implementation, where a cutoff for the regions far away from the mediator mass is often used. This is illustrated in Fig. 3.5 showing the invariant mass of the Dark Matter pair in the samples 85 generated for 7 TeV mediator with different coupling strength. In all cases, it is expected to observe a peak around the mediator mass with a tail extending to  $m_{\bar{\chi}\chi} \to 0$ , significantly enhanced by parton distribution functions at low Bjorken x. For coupling strength 1 and 3, the massive enhancement at  $m_{\tilde{\chi}\chi} 
ightarrow 0$  implies the resonant production at  $m_{\bar{\chi}\chi} = 7 \text{ TeV}$  is statistically suppressed such that barely 91 any events are generated there. However, for narrower mediators 92 with couplings below 1, the peak around 7 TeV is clearly visible in the generated sample and the dominant tail at  $m_{\bar{\chi}\chi} \to 0$  is artificially 94 cut off, leading to unphysical cross section predictions and kinematic 95 shapes. This explains why the sample with the narrowest mediator in Fig. 3.4 is heavily suppressed in terms of production cross section and 97 also gives different  $E_T$  shape. In general, for such extreme parameter choices the EFT model should give the correct answer. [TODO: add 99 results of ongoing study.]

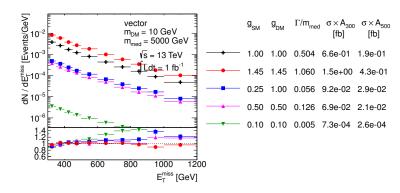


Figure 3.4: Scan over couplings. The  $E_T$  distribution is compared for the vector mediator models using the parameters as indicated. Ratios of the normalized distributions with respect to the first one are shown.  $A_{300}$  and  $A_{500}$  in the table denote the acceptance of the  $E_T > 300\,\text{GeV}$  and  $E_T > 500\,\text{GeV}$  cut, respectively.

Scan over the Dark Matter mass For the fixed mediator mass and couplings, both the cross section and the kinematic distributions remain 102 similar for different Dark Matter masses as long as  $M_{\text{med}} > 2m_{\text{DM}}$ . 103 This is illustrated in Fig. 3.6 on an example of 1 TeV mediator and Dark Matter masses ranging from 10 GeV to 300 GeV. It is observed 105 that the cross section decreases as the Dark Matter mass reaches 106 closer to  $M_{\text{med}}/2$ . Once the Dark Matter pair is produced off-shell, 107 the cross section of such simplified model is suppressed and the  $E_T$ spectrum hardens, as demonstrated with the choice of 1 TeV Dark 109 Matter in the same plot. Figure 3.7 reveals the  $E_T$  spectrum hardens 110 further with increasing Dark Matter mass, accompanied by the gradual decrease of the cross section. From these observations one can 112

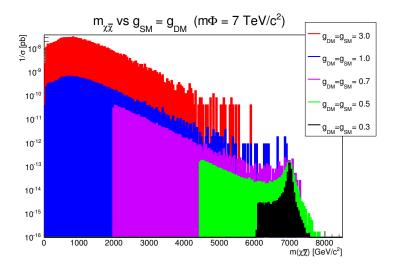


Figure 3.5: Invariant mass of the Dark Matter pair in the samples with  $M_{\rm med} = 7 \, \text{TeV}$  and different coupling strengths.

#### conclude: 113

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- A coarse binning along  $m_{\rm DM}$  is sufficient at  $M_{\rm med} \gg 2m_{\rm DM}$ .
- Finer binning is needed in order to capture the changes in the cross section and kinematic quantities close to the production threshold on both sides around  $M_{\text{med}} = 2m_{\text{DM}}$ .
- Due to the significant cross section suppression of the off-shell Dark Matter pair production, it is not necessary to populate the parameter space  $M_{\rm med} \ll 2m_{\rm DM}$  since the LHC is not going to be able to probe the models there.

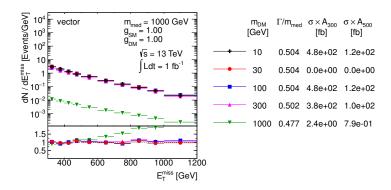


Figure 3.6: Scan over Dark Matter mass. The  $E_T$  distribution is compared for the vector mediator models using the parameters as indicated. Ratios of the normalized distributions with respect to the first one are shown.  $A_{300}$  and  $A_{500}$ in the table denote the acceptance of the  $E_T > 300 \,\text{GeV}$  and  $E_T > 500 \,\text{GeV}$  cut, respectively.

Scan over the mediator mass Changing the mediator mass for fixed Dark Matter mass and couplings leads to significant differences in 123 cross section and shapes of the kinematic variables for  $M_{\rm med} > 2m_{\rm DM}$ 124 as shown in Fig. 3.8. As expected, higher mediator masses lead to 125 harder  $E_T$  spectra. On the other hand, the  $E_T$  shapes are similar 126

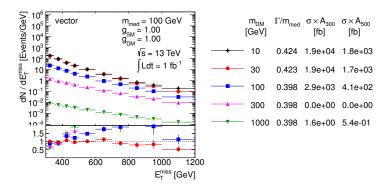


Figure 3.7: Scan over Dark Matter mass. The  $E_T$  distribution is compared for the vector mediator models using the parameters as indicated. Ratios of the normalized distributions with respect to the first one are shown.  $A_{300}$  and  $A_{500}$  in the table denote the acceptance of the  $E_T > 300 \, \text{GeV}$  and  $E_T > 500 \, \text{GeV}$  cut, respectively.

in the off-shell Dark Matter production regime as well as no dramatic differences in cross sections are observed, which is illustrated in Fig. 3.9. Therefore, a coarse binning along  $m_{\rm DM}$  is sufficient at  $M_{\rm med} \ll 2m_{\rm DM}$ .

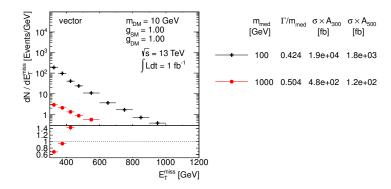


Figure 3.8: Scan over mediator mass. The  $E_T$  distribution is compared for the vector mediator models using the parameters as indicated. Ratios of the normalized distributions with respect to the first one are shown.  $A_{300}$  and  $A_{500}$  in the table denote the acceptance of the  $E_T > 300\,\text{GeV}$  and  $E_T > 500\,\text{GeV}$  cut, respectively.

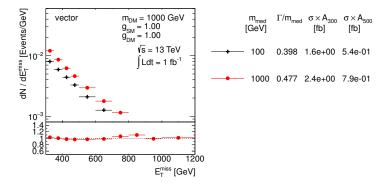


Figure 3.9: Scan over mediator mass. The  $E_T$  distribution is compared for the vector mediator models using the parameters as indicated. Ratios of the normalized distributions with respect to the first one are shown.  $A_{300}$  and  $A_{500}$  in the table denote the acceptance of the  $E_T > 300 \,\text{GeV}$  and  $E_T > 500 \,\text{GeV}$  cut, respectively.

Proposed parameter grid Based on the observations above, the following proposal is made for the presentation of the early Run-2 results from the LHC:

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(a) Give results in the  $M_{\text{med}}$ – $m_{\text{DM}}$  plane for a particular choice of the couplings.

(b) Give results in the  $g_q$ – $g_{DM}$  plane for a particular choice of the masses.

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We choose to display the results in the  $M_{\text{med}}$ - $m_{\text{DM}}$  plane for the choice of the couplings  $g_q = g_{DM} = 1$ . In order to motivate the high-139 est mediator mass grid point, the expected sensitivity of Run-2 LHC 140 data needs to be taken into account. The expected upper limit at 95% confidence level on the product of cross section, acceptance and efficiency,  $\sigma \times A \times \epsilon$ , in the final Run-1 ATLAS mono-jet analysis [A<sup>+</sup>15] 143 is 51 fb and 7.2 fb for  $E_T > 300 \,\text{GeV}$  and  $E_T > 500 \,\text{GeV}$ , respectively. 144 The ATLAS 14 TeV prospects [ATL14] predict twice better sensitivity with the first 5 fb<sup>-1</sup> of data already. Given the cross section for V+jets processes increases by roughly a factor 2 when going from 147  $\sqrt{s}=8\,\text{TeV}$  to 13 TeV, similar fiducial cross section limits can be expected with the first Run-2 data as from the final Run-1 analysis. The generator level cross section times the acceptance at  $E_T > 500 \,\text{GeV}$  for 150 the model with couplings  $g_q = g_{DM} = 1$ , light Dark Matter of 10 GeV 151 and 1 TeV vector mediator is at the order of 100 fb, i.e. the early Run-2 mono-jet analysis is going to be sensitive to heavier mediators than 153 this. The value of  $\sigma \times A$  at  $\not E_T > 500 \,\text{GeV}$  for 5 TeV vector mediator 154 is at the order of 0.1 fb, therefore this model probably lies beyond the 155 reach of the LHC. Based on these arguments, the following  $M_{\text{med}}$ grid points are chosen, roughly equidistant in the logarithmic scale: 157 10 GeV, 20 GeV, 50 GeV, 100 GeV, 200 GeV, 300 GeV, 500 GeV, 1000 GeV 158 and 2000 GeV. Given the fact that significant changes in cross section happen around the  $M_{\text{med}} = 2m_{\text{DM}}$  threshold, the  $m_{\text{DM}}$  grid points 160 are taken at approximately  $M_{\rm med}/2$ , namely: 10 GeV, 50 GeV, 150 GeV, 161 500 GeV and 1000 GeV. Points on the on-shell diagonal are always 162 chosen to be 5 GeV away from the threshold, to avoid numerical instabilities in the event generation. The detailed studies of the impact 164 of the parameter changes on the cross section and kinematic distri-165 butions presented earlier in this section support removing some of the grid points and rely on interpolation. The optimised grids pro-167 posed for the vector and axial-vector mediators are given in Table. 3.1, 168 containing 29 mass points each. One point at very high mediator mass (5 TeV) is added for each of the DM masses scanned, to aid the reinterpretation of results in terms of contact interaction operators 171 (EFTs). 172 173

The presentation of the results in the  $g_q$ – $g_{DM}$  plane for fixed masses benefits from cross section scaling and is discussed in Sec-174 tion 3.3. 175

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$m_{\mathrm{DM}}$ (GeV)					$m_{\rm r}$	ned (G	eV)			
1	10	20	50	100	200	300	500	1000	2000	5000
10	10	15	50	100						5000
50	10		50	95	200	300				5000
150	10				200	295	500			5000
500	10						500	995	2000	5000
1000	10							1000	1995	5000

Table 3.1: Simplified model benchmarks for s-channel simplified models (spin-1 mediators decaying to Dirac DM fermions in the V and A case, taking the minimum width for  $g_q = g_{DM} = 1$ )

#### Scalar and pseudoscalar mediator, s-channel exchange

One of the most simple UV complete extensions of the effective field theory approach is the addition of a scalar/pseudoscalar mediator between DM and SM. A gauge singlet mediator can have tree-level interactions with a singlet DM particle that is either a Dirac or Majorana fermion, or DM that is a scalar itself. The spin-0 mediator can either be a real or complex scalar; a complex scalar contains both scalar and pseudoscalar particles, whereas the real field only contains the scalar particle. In this document we consider only two of the possible choices for this simplified model: one where the interac-185 tion with the SM is mediated by a real scalar, and the second where we consider only a light pseudoscalar, assuming that the associated scalar is decoupled from the low-energy spectrum. The kinematics of the two cases is sufficiently different to suggest that further in-189 vestigation of the complex scalar case is needed but left for future studies.

Couplings to the SM fermions can be arranged by mixing with the SM Higgs. Such models have interesting connections with Higgs physics, and can be viewed as generalizations of the Higgs portal to DM. The most general scalar mediator models will have renormalizable interactions between the SM Higgs and the new scalar  $\phi$  or pseudoscalar a, as well as  $\phi/a$  interactions with electroweak gauge bosons. Such interactions are model dependent, often subject to constraints from electroweak precision tests, and would suggest specialized searches which cannot be generalized to a broad class of models (unlike, for instance, the  $E_T$  + jets searches). As a result, for this class of minimal simplified models with spin-0 mediators, we will focus primarily on couplings to fermions and loop-induced couplings to gluons.

Minimal Flavor Violation (MFV) implies that scalar couplings to fermions will be proportional to the fermion mass. However, they can differ for up- and down-type quarks and for charged leptons.

Following the assumption that DM is a fermion  $\chi$ , which couples to the SM only through a scalar  $\phi$  or pseudoscalar a, the most general tree-level Lagrangians compatible with the MFV assumption are [CRTW14, ADR<sup>+</sup>14, BFG15]:

$$\mathcal{L}_{\text{fermion},\phi} = \mathcal{L}_{\text{SM}} + i\bar{\chi}\partial\!\!/\chi + m_{\chi}\bar{\chi}\chi + \left|\partial_{\mu}\phi\right|^{2} + \frac{1}{2}m_{\phi}^{2}\phi^{2} + g_{\chi}\phi\bar{\chi}\chi + \frac{\phi}{\sqrt{2}}\sum_{i}\left(g_{u}y_{i}^{u}\bar{u}_{i}u_{i} + g_{d}y_{i}^{d}\bar{d}_{i}d_{i} + g_{\ell}y_{i}^{\ell}\bar{\ell}_{i}\ell_{i}\right), \quad (3.8)$$

$$\mathcal{L}_{\text{fermion},a} = \mathcal{L}_{\text{SM}} + i\bar{\chi}\partial\!\!/\chi + m_{\chi}\bar{\chi}\chi + \left|\partial_{\mu}a\right|^{2} + \frac{1}{2}m_{a}^{2}a^{2} + ig_{\chi}a\bar{\chi}\gamma_{5}\chi + \frac{ia}{\sqrt{2}}\sum_{i}\left(g_{u}y_{i}^{u}\bar{u}_{i}\gamma_{5}u_{i} + g_{d}y_{i}^{d}\bar{d}_{i}\gamma_{5}d_{i} + g_{\ell}y_{i}^{\ell}\bar{\ell}_{i}\gamma_{5}\ell_{3}\right)$$

Here the sums run over the all SM generations; the Yukawa couplings  $y_i^f$  are normalized to  $y_i^f = \sqrt{2} m_i^f/v$  where  $v \simeq 246\,\mathrm{GeV}$  represents the Higgs vacuum expectation value (VEV). We parametrise the DM-mediator coupling as  $g_\chi$ , without any additional Yukawa structure between the mediator and the dark sector.

As already stated we only choose a minimal set of interactions that do not include interactions with the Higgs field. For simplicity, we also assume universal SM-mediator couplings  $g_v = g_u = g_d = g_\ell$ 

Given these simplifications, the minimal set of parameters under consideration is

$$\left\{m_{\chi}, m_{\phi/a}, g_{\chi}, g_{q}\right\}. \tag{3.10}$$

The matrix element implementation of the s-channel spin-o mediated DM production is available in POWHEG with the full top-loop calculation at LO [HR15].

We choose to consider minimal mediator width given by

$$\Gamma_{\min} = \Gamma_{\bar{\chi}\chi} + \sum_{q} \Gamma_{\bar{q}q} + \Gamma_{gg}, \tag{3.11}$$

where the individual contributions follow from

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$$\Gamma_{\bar{\chi}\chi}^{S} = \frac{g_{\rm DM}^{2} M_{\rm med}}{8\pi} \left( 1 - \frac{4m_{\rm DM}^{2}}{M_{\rm med}^{2}} \right)^{3/2} \theta(M_{\rm med} - 2m_{\rm DM})$$
(3.12)

$$\Gamma_{\bar{q}q}^{S} = \frac{3g_{q}^{2}M_{\text{med}}}{8\pi} \frac{m_{q}^{2}}{v^{2}} \left(1 - \frac{4m_{q}^{2}}{M_{\text{med}}^{2}}\right)^{3/2} \theta(M_{\text{med}} - 2m_{q})$$
(3.13)

$$\Gamma_{gg}^{S} = \frac{g_{q}^{2} \alpha_{s}^{2}}{2\pi^{3} v^{2} M_{\text{med}}} \left| \sum_{q} m_{q}^{2} F_{S} \left( \frac{4m_{q}^{2}}{M_{\text{med}}^{2}} \right) \right|^{2}$$
(3.14)

$$\Gamma_{\bar{\chi}\chi}^{P} = \frac{g_{\rm DM}^{2} M_{\rm med}}{8\pi} \sqrt{1 - \frac{4m_{\rm DM}^{2}}{M_{\rm med}^{2}}} \theta(M_{\rm med} - 2m_{\rm DM})$$
(3.15)

$$\Gamma_{\bar{q}q}^{P} = \frac{3g_{q}^{2}M_{\text{med}}}{8\pi} \frac{m_{q}^{2}}{v^{2}} \sqrt{1 - \frac{4m_{q}^{2}}{M_{\text{med}}^{2}}} \theta(M_{\text{med}} - 2m_{q})$$
(3.16)

$$\Gamma_{gg}^{P} = \frac{g_{q}^{2} \alpha_{s}^{2}}{2\pi^{3} v^{2} M_{\text{med}}} \left| \sum_{q} m_{q}^{2} F_{P} \left( \frac{4m_{q}^{2}}{M_{\text{med}}^{2}} \right) \right|^{2} , \qquad (3.17)$$

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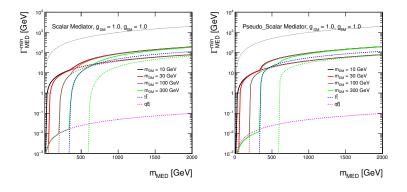
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with the form factors defined as

$$F_{\rm S}(x) = 1 + (1 - x) \arctan^2 \left(\frac{1}{\sqrt{x - 1}}\right)$$
 (3.18)

$$F_{\rm P}(x) = \arctan^2\left(\frac{1}{\sqrt{x-1}}\right) \ . \tag{3.19}$$

The minimal width for scalar and pseudo-scalar mediators with  $g_q = g_{\rm DM} = 1$  are shown in Fig. 3.10, illustrating the effect of the Higgs-like Yukawa couplings. For the mediator masses above twice the top quark mass  $m_t$ , the minimal width receives the dominant contribution from the top quark. For lighter mediator masses, Dark Matter dominates as the couplings to lighter quarks are Yukawa suppressed. Note that we decide to ignore the partial width coming from gluons through loops as it can be safely neglected [HR15].



Similarly as in the case of the vector and axial-vector mediators, scans in the parameter space are performed also for the scalar and pseudo-scalar mediators in order to decide on the optimised parameter grid for the presentation of Run-2 results. Figures 3.11- 3.15 show the scans over the couplings, Dark Matter mass and mediator mass and the same conclusions apply as in Section 3.1.

Since the top quark gives the dominant contribution to the mediator width due to Higgs-like Yukawa couplings, the effect of the top channel opening in the mediator production was studied in addition. Scan over the mediator mass is shown in Fig. 3.15 where the mediator masses 300 GeV and 500 GeV are chosen to be below and above  $2m_t$ . The off-shell Dark Matter production regime is assumed by taking  $m_{\rm DM}=1$  TeV in order to allow studying solely the effects of the couplings to quarks. No differences in the kinematic distributions are observed and also the cross sections remain similar in this case. Therefore, it is concluded that no significant changes appear for mediator masses around the  $2m_t$  threshold.

The optimized parameter grid in the  $M_{\rm med}$ – $m_{\rm DM}$  plane for scalar and pseudo-scalar mediators is motivated by similar arguments as

Figure 3.10: Minimal width as a function of mediator mass for scalar and pseudo-scalar mediator assuming couplings of 1. The total width is shown as solid lines for Dark Matter masses of 10 GeV, 30 GeV, 100 GeV and 300 GeV in black, red, brown and green, respectively. The individual contributions from Dark Matter are indicated by dotted lines with the same colors. The contribution from all quarks but top is shown as magenta dotted line and the contribution from top quarks only is illustrated by the dotted blue line. The dotted black line shows the extreme case  $\Gamma_{\min} = M_{\text{med}}$ .

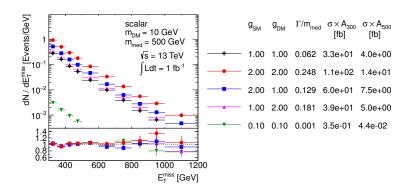


Figure 3.11: Scan over couplings. The  $E_T$  distribution is compared for the scalar mediator models using the parameters as indicated. Ratios of the normalized distributions with respect to the first one are shown.  $A_{300}$  and  $A_{500}$ in the table denote the acceptance of the  $\not\!E_T > 300 \,\text{GeV}$  and  $\not\!E_T > 500 \,\text{GeV}$  cut, respectively.

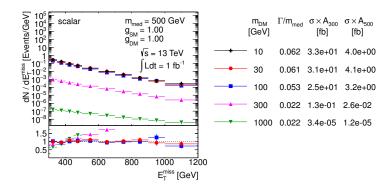


Figure 3.12: Scan over Dark Matter mass. The  $\not \! E_T$  distribution is compared for the scalar mediator models using the parameters as indicated. Ratios of the normalized distributions with respect to the first one are shown.  $A_{300}$  and  $A_{500}$  in the table denote the acceptance of the  $E_T > 300 \,\text{GeV}$  and  $E_T > 500 \,\text{GeV}$  cut, respectively.

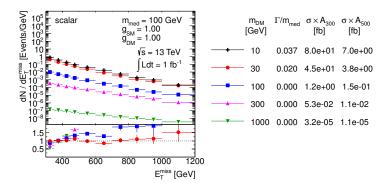


Figure 3.13: Scan over Dark Matter mass. The  $E_T$  distribution is compared for the scalar mediator models using the parameters as indicated. Ratios of the normalized distributions with respect to the first one are shown.  $A_{300}$  and  $A_{500}$  in the table denote the acceptance of the  $E_T > 300\,\text{GeV}$  and  $E_T > 500 \,\text{GeV}$  cut, respectively.

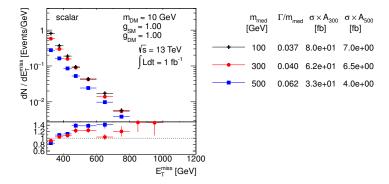


Figure 3.14: Scan over mediator mass. The  $E_T$  distribution is compared for the scalar mediator models using the parameters as indicated. Ratios of the normalized distributions with respect to the first one are shown.  $A_{300}$  and  $A_{500}$ in the table denote the acceptance of the  $E_T > 300\,\mathrm{GeV}$  and  $E_T > 500\,\mathrm{GeV}$  cut, respectively.

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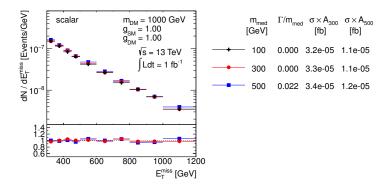


Figure 3.15: Scan over mediator mass. The  $E_T$  distribution is compared for the scalar mediator models using the parameters as indicated. Ratios of the normalized distributions with respect to the first one are shown.  $A_{300}$  and  $A_{500}$  in the table denote the acceptance of the  $E_T > 300\,\text{GeV}$  and  $E_T > 500\,\text{GeV}$  cut, respectively.

in the previous section. Therefore, a similar pattern is followed here, taking again  $g_q = g_{DM} = 1$ . Only the sensitivity to the highest mediator masses has to be revisited. The generator level cross section times the acceptance at  $E_T > 500\,\text{GeV}$  for the model with couplings  $g_q = g_{DM} = 1$ , light Dark Matter of 10 GeV and 500 GeV scalar mediator is at the order of 10 fb, i.e. just at the edge of the early Run-2 sensitivity. Increasing the mediator mass to 1 TeV pushes the product  $\sigma \times A$  down to approximately 0.1 fb, beyond the LHC sensitivity. Therefore, we choose to remove the 2 TeV mediator mass from the grid and present the final grid with 26 mass points only in Fig. 3.2. One point at very high mediator mass (5 TeV) is added for each of the DM masses scanned, to aid the reinterpretation of results in terms of contact interaction operators (EFTs).

$m_{\rm DM}$ (GeV)		$m_{\mathrm{med}}$ (GeV)							
1	10	20	50	100	200	300	500	1000	5000
10	10	15	50	100					5000
50	10		50	95	200	300			5000
150	10				200	295	500		5000
500	10						500	995	5000
1000	10							1000	5000

Table 3.2: Simplified model benchmarks for s—channel simplified models (spino mediators decaying to Dirac DM fermions in the scalar and pseudoscalar case, taking the minimum width for  $g_q = g_{DM} = 1$ )

The proposal for the scan in the  $g_q$ – $g_{\rm DM}$  plane is described in the following section.

#### 3.3 Cross section scaling

The aim of the parameter grid optimization is to find out whether certain parts of the parameter space can be omitted and one can rely on the neighboring grid points in order to populate the missing parts.

There are two ways of doing this:

• Interpolation is used in-between the grid points that are close

enough such that finer granularity is not needed for the presentation purposes, or between the points where smooth or no changes of the results are expected. The latter argument is exactly the one that motivates the reduction of the grid points in the  $M_{\rm med}$ – $m_{\rm DM}$  plane.

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 Recalculation of the results can be used when the dependencies with respect to the neighboring grid points are known.

The results of the scan over the couplings presented in the previous sections indicate there are no changes in kinematic distributions for different choices of the coupling strengths. This means that the acceptance remains the same in the whole  $g_q$ – $g_{DM}$  plane and it is sufficient to perform the detector simulation only for one single grid point. The resulting truth-level selection acceptance and the detector reconstruction efficiency can then be applied to all remaining grid points in the  $g_q$ – $g_{DM}$  plane where only the generator-level cross section needs to be known. This significantly reduces the computing time as the detector response is by far the most expensive part of the Monte Carlo sample production. However, a further step can be taken if a parameterization of the cross section dependence from one grid point to another exists, in which case the number of generated samples can be reduced even further.

Let us now elaborate on a cross section scaling procedure. The propagator on the s-channel exchange is written in a Breit-Wigner form as  $\frac{1}{q^2-M_{\rm med}^2+iM_{\rm med}\Gamma}$ , where q is the momentum transfer calculated from the two partons entering the hard process after the initial state radiation, which is equivalent to the invariant mass of the Dark Matter pair. The size of the momenum transfer with respect to the mediator mass allows to classify the production in the following way:

- off-shell production when  $q^2\gg M_{\rm med}$  leading to suppressed cross sections,
- on-shell production when  $q^2 \sim M_{
  m med}$  leading to enhanced cross sections,
- effective field theory (EFT) limit when  $q^2 \ll M_{\rm med}$ .

All three categories can be distinguished in Fig. 3.16 showing the upper limit on the interaction scale  $M^* \equiv M_{\rm med}/\sqrt{g_{\rm q}g_{\rm DM}}$  for vector mediator. In the case of the off-shell production and the EFT limit, the first term in the propagator dominates which reduces the dependence on the mediator width. Therefore, in these cases one can approximate the cross section as

$$\sigma \propto g_q^2 g_{\rm DM}^2. \tag{3.20}$$

The on-shell production regime is the most interesting one as it gives the best chances for a discovery at the LHC given the cross section enhancement. The propagator term with the width cannot be neglected in this case and, in the narrow width approximation which requires  $\Gamma \ll M_{\rm med}$ , one can integrate

$$\int \frac{ds}{(s - M_{\text{med}}^2)^2 + M_{\text{med}}^2 \Gamma^2} = \frac{\pi}{M_{\text{med}} \Gamma}$$
(3.21)

which further implies the cross section scaling

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$$\sigma \propto \frac{g_q^2 g_{\rm DM}^2}{\Gamma}.$$
 (3.22)

The narrow with approximation is important here as it ensures an integration over parton distribution functions (PDFs) can be neglected. In other words, it is assumed the integrant in Eq. 3.21 is non-zero only for a small region of s, such that the PDFs can be taken to be constant in this range. Since  $\Gamma \sim g_{\rm q}^2 + g_{\rm DM}^2$ , one can simplify this rule in the extreme cases as follows

$$\sigma \propto \frac{g_{\rm q}^2 g_{\rm DM}^2}{g_{\rm q}^2 + g_{\rm DM}^2} \xrightarrow{g_{\rm q} \ll g_{\rm DM}} g_{\rm q}^2$$
 (3.23)

$$\sigma \propto \frac{g_q^2 g_{\rm DM}^2}{g_q^2 + g_{\rm DM}^2} \xrightarrow{g_q \gg g_{\rm DM}} g_{\rm DM}^2.$$
 (3.24)

ing rule for how the cross section changes with the Dark Matter mass and the mediator mass, or for mediators with a large width, because PDFs matter in such cases as well. Therefore, the scaling procedure outlined above is expected to work only for fixed masses and fixed mediator width, assuming the narrow widht approximation applies. Figures 3.17 and 3.18 show the minimal width in the  $g_q$ – $g_{DM}$  plane for all vector, axial-vector, scalar and pseudo-scalar mediators for  $M_{\rm med} = 100 \,\text{GeV}$  and 1000 GeV, respectively, taking  $m_{\rm DM} = 10 \,\text{GeV}$ . The individual colors indicate the lines of constant width along which the cross section scaling works. For vector and axial-vector mediators, the minimal width is predominantly defined by  $g_q$  due to the number of quark flavors and the color factor. On the contrary, both the Standard Model and Dark Matter partial width have comparable contributions in case of scalar and pseudo-scalar mediators if the top quark channel is open  $(M_{\text{med}} > 2m_t)$ . However, mostly  $g_{\rm DM}$  defines the minimal width for  $M_{\rm med} < 2m_t$  due to the Yukawa-

However, it is important to keep in mind that there is no simple scal-

The performance of the cross section scaling is demonstrated in Fig. 3.19 where two mass points  $M_{\rm med} = 100\,{\rm GeV}$  and 1 TeV with  $m_{\rm DM} = 10\,{\rm GeV}$  are chosen and rescaled from the starting point

suppressed light quark couplings.

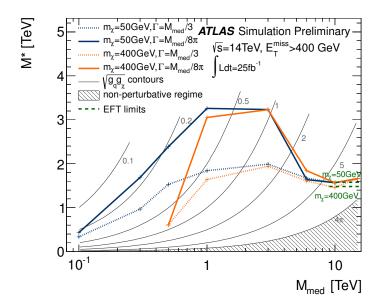


Figure 3.16: Comparison of the 95% CL lower limits on the scale of the interaction of a Z'-like simplified model at 14 TeV, in terms of the mediator mass. Corresponding limits from EFT models are shown on the same plot as green dashed lines to show equivalence between the two models for high mediator masses. Taken from Ref. [ATL14].

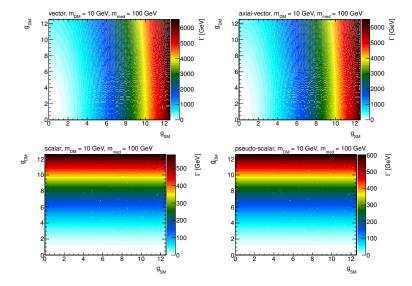


Figure 3.17: Minimal width for vector, axial-vector, scalar and pseudo-scalar mediators as a function of the individual couplings  $g_q$  and  $g_{\rm DM}$ , assuming  $M_{\rm med} = 100 \, \text{GeV}$  and  $m_{\rm DM} = 10 \, \text{GeV}$ .

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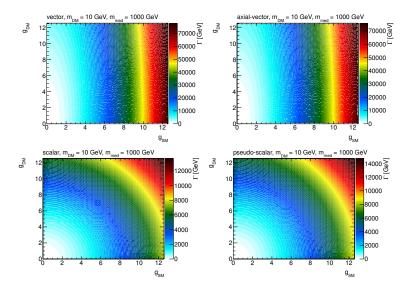


Figure 3.18: Minimal width for vector, axial-vector, scalar and pseudo-scalar mediators as a function of the individual couplings  $g_q$  and  $g_{DM}$ , assuming  $M_{\rm med}=1\,{\rm TeV}$  and  $m_{\rm DM}=10\,{\rm GeV}$ .

 $g_{
m q}=g_{
m DM}=1$  according to Eq. 3.22 to populate the whole  $g_{
m q}-g_{
m DM}$  plane. This means the width is not kept constant in this test and this is done in purpose in order to point out deviations from the scaling when the width is altered. For each mass point, the rescaled cross section is compared to the generator cross section and the ratio of the two is plotted. For the given choice of the mass points, the scaling seems to work approximately with the precision of  $\sim 20\%$  in the region where  $\Gamma_{
m min} < M_{
m med}$ . Constant colors indicate the lines along which the cross section scaling works precisely and there is a remarkable resemblance of the patterns shown in the plots of the mediator width. To prove the scaling along the lines of constant width works, one such line is chosen in Fig. 3.20 for a scalar mediator, defined by  $M_{
m med}=300\,{\rm GeV}$ ,  $m_{
m DM}=100\,{\rm GeV}$ ,  $g_{
m q}=g_{
m DM}=1$ , and the rescaled and generated cross sections are found to agree within 3%.

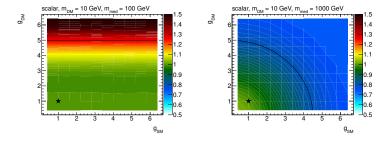
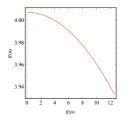


Figure 3.19: Ratio of the rescaled and generated cross sections in the  $g_q$ – $g_{\rm DM}$  plane. The point at  $g_q=g_{\rm DM}=1$ , taken as a reference for the rescaling, is denoted by a star symbol. Scalar model with  $M_{\rm med}=100\,{\rm GeV}$  (left) and 1 TeV (right) is plotted for  $m_{\rm DM}=10\,{\rm GeV}$ . The limiting case  $\Gamma_{\rm min}=M_{\rm med}$  is shown as a black line.

Proposed parameter grid We propose to present the results in the  $g_q$ – $g_{\rm DM}$  plane using the following prescription:

• Since the shapes of kinematic quantities do not change for different couplings, use the acceptance and efficiency for the available



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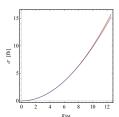
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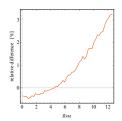


Figure 3.20: Scaling along the lines of constant width. The line of constant width for  $M_{\rm med}=300\,{\rm GeV}$  and  $m_{\rm DM}=100\,{\rm GeV}$ , intercepting  $g_{\rm q}=g_{\rm DM}=4$  is shown on left. The generated and rescaled cross sections are compared in the middle, the corresponding ratio is shown on right.

 $m_{\rm DM}=50\,{\rm GeV},\, M_{\rm med}=300\,{\rm GeV},\, g_{\rm q}=g_{\rm DM}=1$  grid point from the  $M_{\rm med}$ – $m_{\rm DM}$  plane for the scalar and pseudo-scalar mediator. In case of the vector and axial-vector mediator, use the grid point  $m_{\rm DM}=50\,{\rm GeV},\, M_{\rm med}=1\,{\rm TeV},\, g_{\rm q}=g_{\rm DM}=1.$ 

- Generate additional samples in order to get generator cross sections only. For scalar and pseudo-scalar mediator, choose  $m_{\rm DM} = 50\,{\rm GeV},\,M_{\rm med} = 300\,{\rm GeV}$  with the following values for  $g_{\rm q} = g_{\rm DM}$ : 0.1, 2, 3, 4, 5, 6. For vector and axial vector mediator, choose  $m_{\rm DM} = 50\,{\rm GeV},\,M_{\rm med} = 1\,{\rm TeV}$  with the following values for  $g_{\rm q} = g_{\rm DM}$ : 0.1, 0.25, 0.5, 0.75, 1.25, 1.5. The upper values are defined by the minimal width reaching the mediator mass.
- Rescale the generator cross sections along the lines of constant width in order to populate the whole  $g_q$ – $g_{\rm DM}$  plane.

Rescaling to different mediator width In general there may be an interest to consider larger mediator masses than  $\Gamma_{\min}$  in order to accommodate further couplings of the mediator. The cross section scaling method described above can be used to reinterpret the results presented for the minimal width, since multiplying the width by factor n is equivalent to changing the coupling strength by factor  $\sqrt{n}$ , i.e.

$$\sigma(g_{\rm q},g_{\rm DM},n\Gamma_{\rm min}(g_{\rm q},g_{\rm DM})) \propto \frac{g_{\rm q}^2g_{\rm DM}^2}{\Gamma_{\rm min}(\sqrt{n}g_{\rm q},\sqrt{n}g_{\rm DM})} \ . \eqno(3.25)$$

The cross section for the sample with couplings  $g_q$  and  $g_{DM}$  and modified mediator width  $\Gamma = n\Gamma_{\min}$  can therefore be rescaled from a sample generated with the minimal width corresponding to the couplings scaled by  $\sqrt{n}$  as described in the following formula.

$$\sigma(g_{q}, g_{DM}, n\Gamma_{\min}(g_{q}, g_{DM})) = \frac{1}{n^2} \sigma(\sqrt{n}g_{q}, \sqrt{n}g_{DM}, \Gamma_{\min}(\sqrt{n}g_{q}, \sqrt{n}g_{DM}))$$
(3.26)

Here, it is again assumed the narrow width approximation applies.
The advantage of doing this is in the fact that no event selection and detector response needs to be simulated since the changes in couplings do not have an effect on the shapes of kinematic distributions.

#### 68 3.3.1 POWHEG settings

- This section describes specific settings for the Dark Matter models needed to run the POWHEG generation.
  - The POWHEG implementation allows to generate a single sample that provides sufficient statistics in all mono-jet analysis signal regions. POWHEG generates weighted events and the bornsuppfact parameter is used to set the event suppression factor according to

$$F(k_{\mathrm{T}}) = \frac{k_{\mathrm{T}}^2}{k_{\mathrm{T}}^2 + \mathsf{bornsuppfact}^2} \,. \tag{3.27}$$

- In this way, the events at low  $E_T$  are suppressed and receive higher event weights which ensures higher statistics at high  $E_T$ . We recommend to set bornsuppfact to 1000.
- The bornktmin parameter allows to suppress the low  $E_T$  region even further by starting the generation at a certain value of  $k_T$ . It is recommended to set this parameter to half the lower analysis  $E_T$  cut, therefore the proposed value for bornktmin is 150.
- Set runningwidth to o.
- Set mass\_low and mass\_high to -1.
- The minimal values for ncall1, itmx1, ncall2, itmx2 are 250000, 5, 1000000, 5 for the DMV model, respectively. In order to increase speed, set foldsci and foldy to 2 and keep foldphi at 1.
- The minimal values for ncall1, itmx1, ncall2, itmx2 are 100000, 5, 100000, 5 for the DMS\_tloop model, respectively.
- Allow negative weights for the DMV model by setting withnegweights to 1.
- Since the DMS\_tloop model is a leading order process, set L0events and bornonly are set to 1 internally.

#### 3.4 Colored scalar mediator, t-channel exchange

An alternative set of simplified models exist where the mediator is exchanged in the t-channel, thereby coupling the quark and dark matter particle directly. Under the assumption that  $\chi$  is a Standard Model (SM) singlet, the mediating particle, labeled  $\phi$ , is necessarily charged and coloured. This model is parallel to, and partially motivated by, the squark of the MSSM, but in this case the  $\chi$  is chosen

to be Dirac. Following the example of Ref. [PVZ14], the interaction Lagrangian is written as

$$\mathcal{L}_{\text{int}} = g \sum_{i=1,2,3} (\phi_L^i \bar{Q}_L^i + \phi_{uR}^i \bar{u}_R^i + \phi_{dR}^i \bar{d}_R^i) \chi$$
 (3.28)

(Note: [PVZ14] uses only i = 1,2, but I think it's fine to extend this to 3 here.) where  $Q_L^i$ ,  $u_R^i$  and  $d_R^i$  are the SM quarks and  $\phi_L^i$ ,  $\phi_{uR}^i$  and  $\phi_{dR}^i$  are the corresponding mediators, which (unlike the s-channel mediators) must be heavier than  $\chi$ . These mediators have SM gauge representations under  $(SU(3),SU(2))_Y$  of  $(3,2)_{-1/6}$ ,  $(3,1)_{2/3}$  and  $(3,1)_{-1/3}$  respectively. Variations of the model previously studied include coupling to the left-handed quarks only [CEHL14, BDSJ+14], to the  $\phi_{uR}^i$  [DNRT13] or  $\phi_{dR}^i$  [PVZ14, A+14b], or some combination [BB13, AWZ14].

Minimal Flavour Violation (MFV) requires that the mediator masses for each flavour be equal; the same logic also applies to the couplings *g*. The available parameters are then

$$\{m_{\chi}, M_{\phi}, g\}. \tag{3.29}$$

In practice, the third mediator mass and coupling could be separated from the other two, if higher order corrections to the MFV prediction arise due to the large top Yukawa coupling – a common variation is then to define this split between the first two generations and the third, so the parameters are extended to

$$\{m_{\chi}, M_{\phi_{1,2}}, M_{\phi_3}, g_{1,2}, g_3\}.$$
 (3.30)

The width of each mediator is expressed, using the example of decay to an up quark, as

$$\Gamma(\phi_i \to \bar{u}_i \chi) = \frac{g_i^2}{16\pi M_{\phi_i}^3} (M_{\phi_i}^2 - m_{u_i}^2 - m_{\chi}^2) \times \sqrt{M_{\phi_i}^4 + m_{u_i}^4 + m_{\chi}^4 - 2M_{\phi_i}^2 m_{u_i}^2 - 2M_{\phi_i}^2 m_{\chi}^2 - 2m_{u_i}^2 m_{\chi}^2},$$
(3.31)

this reduces to

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$$\frac{g_i^2 M_{\phi_i}}{16\pi} \left( 1 - \frac{m_{\chi}^2}{M_{\phi_i}^2} \right)^2 \tag{3.32}$$

in the limit  $M_{\phi_i}$ ,  $m_\chi\gg m_{u_i}$ .

An interesting point of difference with the s-channel simplified models is that the mediator can radiate a SM object, such as a jet or gauge boson, thus providing three separate mono-X diagrams which must be considered together in calculations. This model can also give a signal in the di-jet + MET channel when, for example, the  $\chi$  is exchanged in the t-channel and the resulting  $\phi$  pair each decay to a jet +  $\chi$ .

## Specific models for signatures with EW bosons

- In this Section, we consider models with a photon, a W boson, a
- <sup>429</sup> Z boson or a Higgs boson in the final state, accompanied by Dark
- 430 Matter particles that either couple directly to the boson or are medi-
- ated by a new particle. The experimental signature is identified as
- 432 V+MET.
- These models are interesting both as some are demanded by gauge
- coupling relations in models where the gluon provides the experi-
- mentally detectable signature, and also as stand-alone models with
- final states that cannot be generated by the models in Section 3.

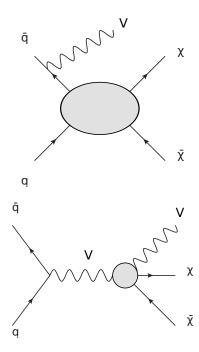


Figure 4.1: Sketch of benchmark models including a contact interaction for V+MET searches, adapted from [NCC<sup>+</sup>14].

- The models considered can be divided in four categories:
- Models including a contact operator, where the boson is radiated from the initial state
- As depicted in the top diagram of Figure 4.1, these models follow
- the nomenclature and theory for the EFT benchmarks commonly

used by MET+X searches [GIR<sup>+</sup>10]. These models have been used in past experimental searches [Kha14, Aad14b, K<sup>+</sup>14, Aad14b, A<sup>+</sup>14a, Aad14a], and they will not be described here.

Models including a contact operator, where the boson is directly coupled to DM
 Shown in the bottom of Figure 4.1, these models allow for a contact interaction vertex that directly couples the boson to Dark
 Matter.

Simplified models where the boson is radiated from the initial state These models follow those already described in Section 3, replacing the initial state gluon with a boson.

V-specific simplified models These models postulate direct couplings of new mediators to bosons, e.g. they couple the Higgs boson to a new scalar [CDM<sup>+</sup>14].

The following Sections describe the models within these categories, the parameters for each of the benchmark models chosen, the studies towards the choices of the parameters to be scanned, and finally point to the location of their Matrix Element implementation.

#### 458 SIMPLIFIED MODELS WITH ISR BOSON RADIATION

Searches in the jet+MET final state are generally more sensitive with respect to final states including bosons, due to the much larger rates of signal events featuring quark or gluon radiation with respect 461 to radiation of bosons [ZBW13], in combination with the low branch-462 ing ratios if leptons from boson decays are required in the final state. The rates for the Higgs boson radiation is too low for these models 464 to be considered a viable benchmark [CDM<sup>+</sup>14]. However, the pres-465 ence of photons leptons from W and Z decays and W or Z bosons decaying hadronically allows to reject the background more effectively, making Z/gamma/W+MET searches still worth comparing 468 with searches in the jet+MET final state.

Vector mediator exchanged in the s-channel The case for searches with W bosons in the final state has so far been strenghtened by the presence of particular choices of couplings between the WIMP and the up and down quarks which enhance W radiation [BT13], in the case of the exchange of a vector mediator in the s-channel. Run-1 searches have considered three sample cases for the product of up and down quark couplings to the mediator  $\xi$ :

- No couplings between mediator and either up or down quarks ( $\xi$  = 0);
- Same coupling between mediator and each of the quark types ( $\xi$  = 1);

• Coupling of opposite sign between mediator and each of the quark types ( $\xi = -1$ ).

The  $\xi = -1$  case leads to a large increase in the cross-section of the 483 process, and modifies the spectrum of missing transverse energy or transverse mass used for the searches. The sensitivity of the W+MET search for this benchmark in this case surpasses that of the jet+MET 486 search. However, as shown in Ref. [BCD<sup>+</sup>15], the cross-section in-487 crease is due to the production of longitudinally polarized W bosons, as a consequence of a violation of electroweak gauge symmetries. 489 Unless further particles are introduced (in a fashion similar to the Higgs boson in the Standard Model), choosing a value of  $\xi = -1$ for this simplified model will lead to a manifest violation of unitar-492 ity at LHC energies. The simplified model with a vector mediator 493 exchanged in the s-channel model can still be considered as a benchmark for searches with a W boson if  $\xi = 1$ . We leave the study of further models with cross-section enhancements due to different couplings to up and down quarks for studies beyond the early LHC 497 searches covered in this document. An example of such model is the case of both DM and SM Higgs charged under a new U(1)', with a a small mass mixing between SM Z-boson and the new Zprime. This 500 leads to different effective DM couplings to  $u_L$  and  $d_L$ , proportional to their coupling to the Z boson, detailed in Appendix B.

The scan in the parameters that characterize this simplified model for EW boson + MET searches follow what already detailed in Section 3.

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As in the case of the jet+MET models, the width does not have a significant impact on the kinematic distributions relevant for those searches. An example of the particle-level analysis acceptance using the generator-level cuts from Ref. [Aad15] for the photon+MET analysis, but raising the photon  $p_T$  cut to 150 GeV is shown in Figure 4.2, comparing a width that is set to  $\Gamma = M_{med}/3$  to the minimal width (the ratio between the two widths ranges from 1.05 to 1.5 with increasing mediator masses).

Examples of relevant kinematic distributions for selected benchmark points are shown in Fig. 4.7; leading-order cross-sections for the chosen benchmark points are shown in Table ?? [TODO: Insert table of cross-sections].

Colored scalar mediator exchanged in the s-channel t-channel colored scalar, to be completed...

Model implementation These models are generated at leading order with MadGraph 2.2.2, and parameter cards can be found on SVN [TODO: Add SVN location]. The parton shower is done using

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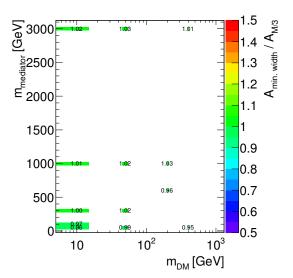


Figure 4.2: Analysis acceptance for the photon+MET analysis when varying the mediator width, in the case of a vector mediator exchanged in the *s*-channel

Pythia 8, with a matching scale of... [TODO: To be completed.]

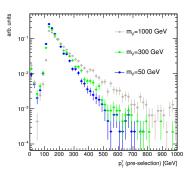
EFT MODELS WITH DIRECT DM-BOSON COUPLINGS

A complete list of effective operators with direct DM/boson couplings for Dirac DM, up to dimension 7, can be found in [CHLR13].

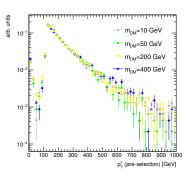
The lowest dimension benchmark operators we may consider are effective dimension 5. Following the notation of [CNS<sup>+</sup>13], models from this category have a Lagrangian that includes terms such as:

$$\frac{m_W^2}{\Lambda_5^3} \bar{\chi} \chi W^{+\mu} W_{\mu}^- + \frac{m_Z^2}{2\Lambda_5^3} \bar{\chi} \chi Z^{\mu} Z_{\mu} . \tag{4.1}$$

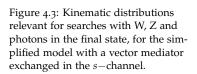
where  $m_Z$  and  $m_W$  are the masses of the Z and W boson,  $W^{\mu}$  and  $Z^{\mu}$  are the fields of the gauge bosons,  $\chi$  denote the Dark Matter fields and  $\Lambda_5$  is the effective field theory scale. Note that these operators are of true dimension 7, but reduce to effective dimension 5 once Higgs vevs, contained in the W and Z mass terms, are inserted. As such, one expects these that operators would naturally arise in UV complete models where Dark Matter interacts via a Higgs portal where heavy mediators would couple to the Higgs or other fields in an extended Higgs sector. In such models the full theory may be expected to contain additional operators with Higgs-Dark Matter couplings. Concentrating for the moment on mono-gauge boson signals, the above operator induces signatures with MET in conjunction with Z and W bosons at tree level, while at loop level it induces couplings to photon pairs and  $Z\gamma$  through W loops. In these models, a clear relation exists between final states with photons, EW bosons and Higgs boson. [TODO: see if mono-Higgs studies exist for these



(a) Missing transverse momentum distribution for the photon+MET final state, for different mediator mass choices, for a DM mass of 10 GeV.



(b) Leading photon transverse momentum distribution for the photon+MET final state, for different DM mass choices, with a mediator mass of 1 TeV.

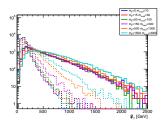




(c) Missing transverse momentum distribution for the leptonic Z+MET final state.



(d) Transverse mass  $(m_T)$  for the leptonic W+MET final state.



(e) Missing transverse momentum distribution for the hadronic W+MET final state.

#### operators, include them here].

The dimension-7 benchmark models contain the  $SU(2)_L \times U(1)_Y$ gauge-invariant couplings between DM fields and the kinetic terms of the EW bosons. The CP-conserving scalar couplings of this type can be written as

$$\frac{c_1}{\Lambda_S^3} \, \bar{\chi} \chi \, B_{\mu\nu} B^{\mu\nu} + \frac{c_2}{\Lambda_S^3} \, \bar{\chi} \chi \, W^i_{\mu\nu} W^{i,\mu\nu} \,. \tag{4.2}$$

Here  $B_{\mu\nu}=\partial_{\mu}B_{\nu}-\partial_{\nu}B_{\mu}$  and  $W^i_{\mu\nu}=\partial_{\mu}W^i_{\nu}-\partial_{\nu}W^i_{\mu}+g_2\epsilon^{ijk}W^j_{\mu}W^k_{\mu}$ are the  $U(1)_Y$  and  $SU(2)_L$  field strength tensor, respectively, and  $g_2$ 

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denotes the weak coupling constant. In the case of the pseudoscalar couplings, one has instead

$$\frac{c_1}{\Lambda_P^3} \bar{\chi} \gamma_5 \chi \, B_{\mu\nu} \tilde{B}^{\mu\nu} + \frac{c_2}{\Lambda_P^3} \bar{\chi} \gamma_5 \chi \, W^i_{\mu\nu} \tilde{W}^{i,\mu\nu} \,, \tag{4.3}$$

where  $\tilde{B}_{\mu\nu}=1/2\,\epsilon_{\mu\nu\lambda\rho}\,B^{\lambda\rho}$  and  $\tilde{W}^i_{\mu\nu}=1/2\,\epsilon_{\mu\nu\lambda\rho}\,W^{i,\lambda\rho}$  are the dual field strength tensors. In addition to the CP-conserving interactions (4.2) and (4.3), there are also four CP-violating couplings that are obtained from the above operators by the replacement  $\bar{\chi}\chi\leftrightarrow\bar{\chi}\gamma_5\chi$ .

The effective interactions introduced in (4.2) and (4.3) appear in models of Rayleigh DM [?]. Ultraviolet completions where the operators are generated through loops of states charged under  $U(1)_Y$  and/or  $SU(2)_L$  have been proposed in [?] and their LHC signatures have been studied in [?]. If these new charged particles are light, the high- $p_T$  gauge bosons that participate in the MET processes considered here are able to resolve the substructure of the loops. This generically suppresses the cross sections compared to the EFT predictions [?], and thus will weaken the bounds on the interaction strengths of DM and the EW gauge bosons to some extent. Furthermore, the light charged mediators may be produced on-shell in pp collisions, rendering direct LHC searches potentially more restrictive than MET searches. Making the above statements precise would require further studies beyond the timescale of this forum.

Since for  $\Lambda_S = \Lambda_P$  the effective interactions (4.2) and (4.3) predict essentially the same value of the mono-photon, mono-Z and mono-W cross section [CNS+13, CHH15], we consider below only the former couplings. We emphasise however that measurements of the jet-jet azimuthal angle difference in MET+2j events may be used to disentangle whether DM couples more strongly to the combination  $B_{\mu\nu}B^{\mu\nu}$  ( $W^i_{\mu\nu}W^{i,\mu\nu}$ ) or the product  $B_{\mu\nu}\tilde{B}^{\mu\nu}$  ( $W^i_{\mu\nu}\tilde{W}^{i,\mu\nu}$ ) of field strength tensors [CHLR13, CHH15].

After EW symmetry breaking the interactions (4.2) induce direct couplings between pairs of DM particles and gauge bosons. The corresponding Feynman rule reads

$$\frac{4i}{\Lambda_S^3} g_{V_1 V_2} \left( p_1^{\mu_2} p_2^{\mu_1} - g^{\mu_1 \mu_2} p_1 \cdot p_2 \right), \tag{4.4}$$

where  $p_i$  ( $\mu_i$ ) denotes the momentum (Lorentz index) of the vector field  $V_i$  and for simplicity the spinors associated with the DM fields have been dropped. The couplings  $g_{V_iV_i}$  take the form

$$g_{\gamma\gamma} = c_w^2 c_1 + s_w^2 c_2,$$

$$g_{\gamma Z} = -s_w c_w (c_1 - c_2),$$

$$g_{ZZ} = s_w^2 c_1 + c_w^2 c_2,$$

$$g_{WW} = c_2,$$
(4.5)

with  $s_w$  ( $c_w$ ) the sine (cosine) of the weak mixing angle. Note that our coefficients  $c_1$  and  $c_2$  are identical to the coefficients  $C_B$  and  $C_W$  used in [CHH15], while they are related via  $k_1 = \frac{1}{c_w^2}c_1$  and  $k_2 = \frac{1}{s_w^2}c_2$  to the coefficients  $k_1$  and  $k_2$  introduced in [CNS<sup>+</sup>13].

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The coefficients  $c_1$  and  $c_2$  appearing in (4.5) determine the relative importance of each of the MET channels and their correlations. For example, one observes that:

- Only  $c_2$  enters the coupling between DM and W bosons, meaning that only models with  $c_2 \neq 0$  predict a mono-W signal;
- If  $c_1 = c_2$  the mono-photon (mono-Z) signal does not receive contributions from diagrams involving Z (photon) exchange;
- Since numerically  $c_w^2/s_w^2 \simeq 3.3$  the mono-photon channel is particularly sensitive to  $c_1$ .

As shown in Fig. 4.4 kinematics of this model can be approximated by that of a simplified model including a high-mass scalar mediator exchanged in the s-channel. For this reason, the list of benchmark models with direct boson-DM couplings only includes dimension 7 operators. [TODO: then we need to recommend the scalar mediator, but then the sensitivity is very poor wrt monojets - however, I still prefer to generate a few (high-mass) simplified model points wrt an EFT if given the choice.]



Figure 4.4: Comparison of the missing transverse momentum for the simplified model where a scalar mediator is exchanged in the s-channel and the model including a dimension-5 scalar contact operator, in the leptonic Z+MET final state

The kinematic distributions for dimension-7 scalar and pseudoscalar operators only shows small differences, as shown in Fig. 4.5.

Similarly, the differences in kinematics for the various signatures are negligible when changing the coefficients  $k_1$  and  $k_2$ , as shown in Figure ??. Only the case  $k_1 = k_2 = 1$  is generated as benchmark; other cases are left for reinterpretation as they will only need a rescaling of the cross-sections shown in Table ?? [TODO: add tables with cross sections] for the various Dark Matter mass points considered.

Examples of relevant kinematic distributions for selected benchmark points are shown in Fig. 4.7.



Figure 4.5: Comparison of the missing transverse momentum for the scalar and pseudoscalar operators with direct interaction between DM and photon, in the photon+MET final state



(a) Missing transverse momentum distribution for the photon+MET final

Figure 4.6: Kinematic distributions relevant for searches with W, Z and photons in the final state, for for the scalar and pseudoscalar operators representing direct interactions between DM and bosons.



(b) Missing transverse momentum distribution for the leptonic Z+MET final state.



(c) Transverse mass  $(m_T)$  for the leptonic W+MET final state.

Specific simplified models Mono-Higgs, to be completed...

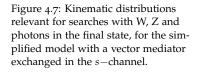
Higgs portals with scalar mediators are among the most concise versions of simplified models that produce couplings of Dark Matter to pairs of gauge-bosons. Scalar fields may couple directly to pairs of electroweak gauge bosons, but must carry part of the electroweak vev. One may thus consider a simple model where Dark Matter couples to a a scalar singlet mediator, which mixes with the fields in the Higgs sector.

$$L \subset m_s S^2 + \lambda S^2 H^2 + \lambda' S H^2 + y S \chi \overline{\chi}$$
 (4.6)

- Where H is a field in the Higgs sector that contains part of the elec-605
- troweak vev, S is a heavy scalar singlet and  $\chi$  is a Dark Matter field. 606
- There is then an S channel diagram where DM pairs couple to the 607
- singlet field S, which then mixes with a Higgs-sector field, and cou-



(a) Missing transverse momentum distribution for the photon+MET final





(b) Missing transverse momentum distribution for the leptonic Z+MET final state.



(c) Transverse mass  $(m_T)$  for the leptonic W+MET final state.



(d) Fat [Insert algorithm] jet mass  $(m_T)$ for the the hadronic W+MET final state.

- ples to W and Z bosons. This diagram contains 2 insertions of EW
- symmetry breaking fields. This diagram corresponds in form to the 610
- effective dimension-5 operator in the previous section.

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## Specific models for signatures with heavy flavor quarks

- 614 5.1 bb+MET models
- 5.2 Models with a single b—quark + MET
- $_{616}$  5.3  $t\bar{t}$ +MET models

As described in Section 3.2, a model with a scalar/pseudoscalar particle mediating the DM-SM interactions is one of the simplest UV completions of our EFT models.

The expected signal of DM pair production depends on the production rate defined by the dark matter mass  $m_\chi$ , mediator  $m_{\phi/a}$ , on the couplings  $g_i$  and on the branching ratio defined by the total decay width of the mediator  $\phi/a$ . We calculate the minimum possible width (assuming only decays into the dark matter and the Standard Model fermions) that is consistent with a given value of  $g_\chi g_q$ , and assuming all couplings to SM particles equal  $g_q = g_u = g_d = g_\ell$ . These are given by Eq. (5.1) [BFG15].

$$\Gamma_{\phi,a} = \sum_{f} N_{c} \frac{y_{f}^{2} g_{q}^{2} m_{\phi,a}}{16\pi} \left( 1 - \frac{4m_{f}^{2}}{m_{\phi,a}^{2}} \right)^{3/2} + \frac{g_{\chi}^{2} m_{\phi,a}}{8\pi} \left( 1 - \frac{4m_{\chi}^{2}}{m_{\phi,a}^{2}} \right)^{3/2} + \frac{\alpha_{s}^{2} y_{t}^{2} g_{q}^{2} m_{\phi,a}^{3}}{32\pi^{3} v^{2}} \left| f_{\phi,a} \left( \frac{4m_{t}^{2}}{m_{\phi,a}^{2}} \right) \right|^{2}$$
(5.1)

where

$$f_{\phi}(\tau) = \tau \left[ 1 + (1 - \tau) \operatorname{arctan}^2 \left( \frac{1}{\sqrt{\tau - 1}} \right) \right], \qquad f_a(\tau) = \tau \operatorname{arctan}^2 \left( \frac{1}{\sqrt{\tau - 1}} \right). (5.2)$$

The first term in each width corresponds to the decay into SM fermions, and the sum runs over all kinematically available fermions,  $N_c = 3$  for quarks and  $N_c = 1$  for leptons. The second term is the decay into DM, assuming that is kinematically allowed. The factor

of two between the decay into SM fermions and into DM is a result 633 of our choice of normalization of the Yukawa couplings due to spin 634 dependencies. The last two terms correspond to decay into gluons. Since we have assumed that  $g_q = g_u = g_d = g_\ell$ , we have included in 636 the partial decay widths  $\Gamma(\phi/a \to gg)$  only the contributions stem-637 ming from top loops, which provide the by far largest corrections given that  $y_t \gg y_b$  etc. At the loop level the mediators can decay not only to gluons but also to pairs of photons and other final states if 640 kinematical accessible. However the decay rates  $\Gamma(\phi/a \rightarrow gg)$  are always larger than the other loop-induced partial widths, and in consequence the total decay widths  $\Gamma_{\phi/a}$  are well approximated by the 643 corresponding sum of the individual partial decay widths involving DM, fermion or gluon pairs. It should be noted that if  $m_{\phi/a} > 2m_t$ the total widths of  $\phi/a$  will typically be dominated by the partial widths to top quarks. 647

### <sub>548</sub> 5.3.1 Parameter scan

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As discussed in Sec. 3.2, the MFV assumption for spin-0 mediators leads to quark mass dependent Yukawa couplings, and therefore dominant couplings to top quarks. This motivates dedicated DM+*tĒ* searches. The benchmark chosen for these searches follows the assumptions mentioned in the previous Section: we consider a Dirac fermion DM particle, universal couplings to quarks, and minimum mediator width.

The benchmark points scanning the model parameters have been selected to ensure that the kinematic features of the parameter space are sufficiently represented. Detailed studies were performed to identify points in the  $m_{\rm DM}$ ,  $m_{\phi,a}$ ,  $g_{\rm DM}$ ,  $g_{\rm q}$  (and  $\Gamma_{\phi,a}$ ) parameter space that differ significantly from each other in terms of expected detector acceptance. Because missing transverse momentum is the key observable for searches, the mediator  $p_T$  spectra is taken to represent the main kinematics of a model. Another consideration in determining the set of benchmarks is to focus on the phase space where we expect the searches to be sensitive during the 2015 LHC run. Based on a projected integrated luminosity of 30 fb<sup>-1</sup> expected for 2015, we disregard model points with a cross section times branching ratio smaller than 0.1 fb.

### 5.3.2 Parameter scan

The kinematics is most dependent on the masses  $m_{\rm DM}$  and  $m_{\phi,a}$ .

Figure 5.1 and 5.2 show typical dependencies for scalar and pseudoscalar couplings respectively. Typically, the mediator  $p_T$  spectra broadens with larger  $m_{\phi,a}$ . The kinematics are also quite different

between on-shell and off-shell production. Furthermore, the kinematic differences between scalar and pseudoscalar are large with light mediator masses and are reduced for larger masses. It is therefore important to benchmark points covering on-shell and off-shell production with sufficient granularity.

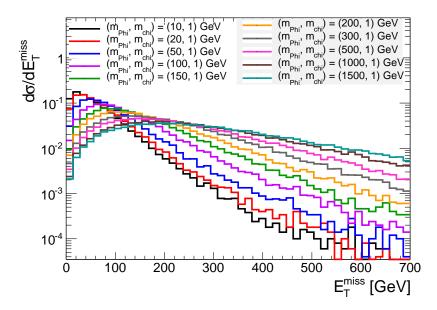


Figure 5.1: Example of the dependence of the kinematics on the scalar mediator mass. The Dark Matter mass is fixed to be 1GeV.

Typically only weak dependencies on width or equivalently couplings are observed (see Fig 5.4), except for large mediator masses of  $\sim 1.5$  TeV or for very small couplings of  $\sim 10^{-2}$ . These regimes where width effects are significant have production cross sections that are too small to be relevant for  $30\,\mathrm{fb}^{-1}$  and are not considered here. However, with the full Run-2 dataset, such models may be within reach. The weak dependence on the typical width values can be understood as the parton distribution function are the dominant effect on mediator production. In other words, for couplings  $\sim O(1)$  the width is large enough that the  $p_T$  of the mediator is determined mainly by the PDF.

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Another case where the width can impact the kinematics is when  $m_{\phi,a}$  is slightly larger than  $2m_{\chi}$ . Here, the width determines the relative contribution between on-shell and off-shell production. An example is given in Fig. 5.5. In our recommendations we propose to use for simplicity the minimal width, as this is represents the most conservative choice to interpret the LHC results. [TODO: mention larger widths too]

Given that the kinematics are similar for all couplings  $\sim O(1)$ ,

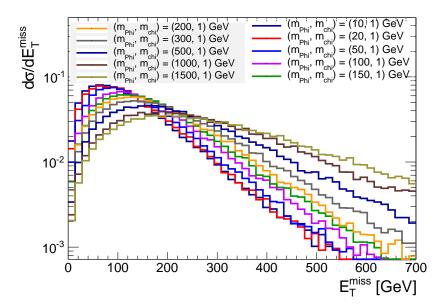


Figure 5.2: Example of the dependence of the kinematics on the pseudoscalar mediator mass. The Dark Matter mass is fixed to be 1GeV.

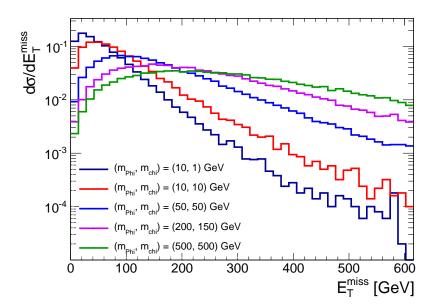


Figure 5.3: Example of the dependence of the kinematic for points of the grid proposed in Tab. 3.2 close to the  $m_{\phi,a}\sim 2m_\chi$  limit.3

we recommend to generate only samples with  $g_{\rm DM}=g_{\rm q}=1$ . It follows from this that these benchmark points should be a good approximation for non-unity couplings and for  $g_{\rm DM}\neq g_{\rm q}$ , provided that the sample is rescaled to the appropriate cross section times

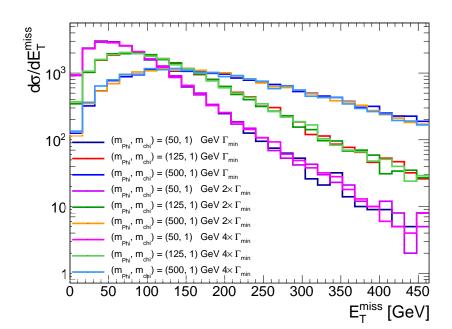


Figure 5.4: Study of the dependence of kinematics on the width of a scalar mediator. The width is increased up to four times the minimal width for each mediator and dark matter mass combination.

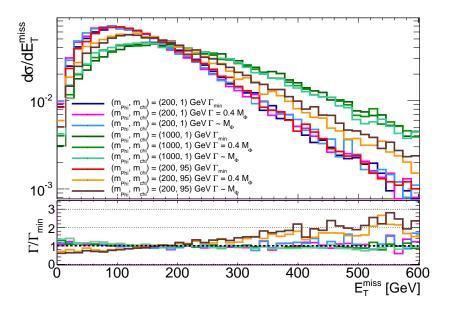


Figure 5.5: Dependence of the kinematics on the width of a scalar mediator. The width is increased up to the mediator mass. Choices of mediator and dark matter masses such that  $m_{\phi,a}$  is slightly larger than  $2m_\chi$  is the only case that shows a sizeable variation of the kinematics as a function of the width.

branching ratio. While the simple scaling function  $\sigma' * BR' = [\sigma *$ BR] \*  $(g_{\rm q}'/g_{\rm q})^2*(g_{\rm DM}'/g_{\rm DM})^2*(\Gamma/\Gamma')$  is sufficient for a limited range of coupling values (see Fig. 5.6 for example), we also choose to provide instead a table of cross section times branching ratio values over a large range of couplings to support interpretation of search results (see the Appendix C). The table lists couplings from g=0.1 to g=3.5, where the upper limit is chosen to close to the perturbative limit.

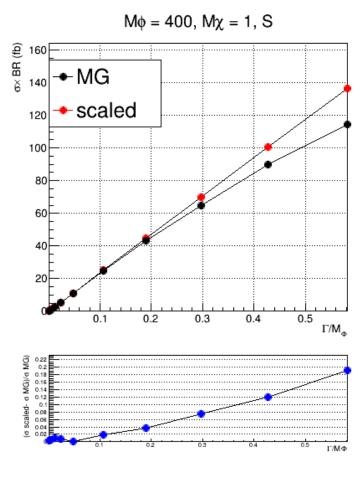


Figure 5.6: An example comparing a simple cross section scaling versus the computation from the generator, for a scalar model with  $m_{\phi}=400\,\mathrm{GeV}$ ,  $m_{\mathrm{DM}}=1\,\mathrm{GeV}$  and all couplings set to unity. In this example, the scaling relationship holds for  $\Gamma_{\phi}/m_{\phi}$  below 0.2, beyond which finite width effects become important and the simple scaling breaks down.

The points for the parameter scan chosen for this model are listed in Table 3.2, chosen to be harmonized with those for other analyses employing the same scalar model as benchmark. Based on the sensitivity considerations above, DM masses are only simulated up to 500 GeV, leading to a total of 24 benchmark points.

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In addition to the considerations discussed in the preceding subsections, very light DM fermions are included ( $m_{\rm DM}=10\,{\rm GeV}$ ) as this is a region where colliders have a complementary sensitivity to

current direct detection experiments.

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### 5.4 *Models with a single top—quark + MET*

Many different theories predict final states with a single top and associated missing transverse momentum (monotop), some of them including dark matter candidates. A simplified model encompassing the processes leading to this phenomenology is described in Refs. [AFM11, AAB+14, BCDF15], and is adopted as one of the benchmarks for Run 2 LHC searches.

A dark matter candidate  $\chi$  and a new particle M (vector or scalar) are added to the SM, in a theory that respects the SU(2)<sub>L</sub> × U(1)<sub>Y</sub> symmetry and produces a single top quark in association with either the DM particle or a new particle decaying invisibly.

Within this model, two distinct processes can lead to monotop production:

- resonant production, as shown in the diagram of Fig. 5.7 (a), where a scalar (S in the figure,  $\varphi$  in the following) or vector (X) field are exchanged in the s-channel, and decay into the a spin 1/2 invisible DM candidate (called  $f_{met}$  in the figure) and a top quark;
- non-resonant production, as shown in the diagrams of Fig. 5.7 (b) and (c), where a flavor-changing interaction produces a top quark in association with a new colored scalar ( $\Phi$ ) or vector (V). The new colored particles, called  $v_{met}$  in the figure, decay invisibly, e.g. to a pair of DM particles.  $v_{met}$  can also decay into a top quark and an up quark, leading to a same-sign top quark final state; a detailed study of the complementarity of this signature is beyond the scope of this Forum report.

In the following, resonant and non-resonant production are treated independently as separate benchmarks. Only the case of a scalar resonance is considered for the resonant model, while the case of vector resonances is left for future studies.

### 8 RESONANT PRODUCTION

In this case, a colored 2/3-charged scalar ( $\varphi^{\pm}$ ) is produced resonantly and decays into a top quark and a spin-1/2 invisible particle,  $\chi$ . The dynamics of the new sector is described by the following Lagrangian:

$$\mathcal{L} = \left[ \varphi \bar{d}^{c} \left[ a_{SR}^{q} + b_{SR}^{q} \gamma_{5} \right] d + \varphi \bar{u} \left[ a_{SR}^{1/2} + b_{SR}^{1/2} \gamma_{5} \right] \chi \right. \\
+ \left. X_{\mu} \bar{d}^{c} \gamma^{\mu} \left[ a_{VR}^{q} + b_{VR}^{q} \gamma_{5} \right] d + X_{\mu} \bar{u} \gamma^{\mu} \left[ a_{VR}^{1/2} + b_{VR}^{1/2} \gamma_{5} \right] \chi + \text{h.c.} \right] .$$
(5.3)



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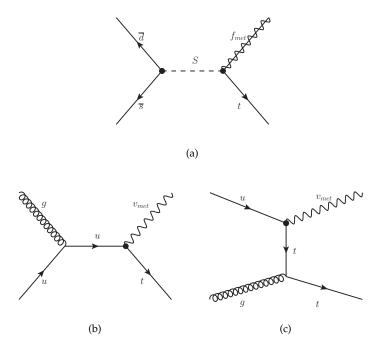


Figure 5.7: Feynman diagram of leading order processes leading to monotop events: production of a coloured scalar resonance S decaying into a top quark and a spin-1/2 fermion  $f_{met}$  (top), s- and t-channel non resonant production of a top quark in association with a spin-1 boson  $v_{met}$  (bottom).

where u (d) stands for any up-quark (down-quark), the index S (V) stands for scalar (vector) field, and the index q runs over the three quark generations.

In the notation of [AAB<sup>+</sup>14], the couplings of the new colored fields to down-type quarks are embedded into the 3 × 3 matrices  $a_{\{S,V\}R}^q$  (scalar/vector couplings) and  $b_{\{S,V\}R}^q$  (pseudoscalar/axial vector couplings) while those to the DM candidate  $\chi$  and one single up-type quarks are given by the three-component vectors  $a_{\{S,V\}R}^{1/2}$  and  $b_{\{S,V\}R}^{1/2}$  in flavor space.

In the following, we only consider the model with a new colored scalar, as the requirement of invariance under  $SU(2)_L XU(1)_Y$  would require the introduction of further particles in the case of a new colored vector [BCDF15].

### Non-Resonant production

For the non-resonant production, the top quark is produced in association with the new particle: either a new scalar ( $\phi$ ) or a new vector (V). For simplicity, we only consider the case of a vector new particle, as the scalar case would involve a mixing with the SM Higgs boson and therefore a larger parameter space. The Lagrangian describing the dynamics of the non-resonant case is:

$$\mathcal{L} = \left[ \phi \bar{u} \left[ a_{FC}^0 + b_{FC}^0 \gamma_5 \right] u + V_{\mu} \bar{u} \gamma^{\mu} \left[ a_{FC}^1 + b_{FC}^1 \gamma_5 \right] u + \text{h.c.} \right].$$
 (5.4)

The strength of the interactions among these two states and a pair of up-type quarks is modeled via two  $3 \times 3$  matrices in flavor

space  $a_{FC}^{\{0,1\}}$  for the scalar/vector couplings and  $b_{FC}^{\{0,1\}}$  for the pseudoscalar/axial vector couplings.

#### Model parameters and assumptions

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The models considered as benchmarks for the first LHC searches contain further assumptions in terms of the flavour and chiral structure of the model with respect to the full Lagrangians of equations (5.3) and (5.4). These assumptions are qualitatively discussed below.

Assumptions in the flavour and chiral structure of the models We only consider right-handed quark components, in order to simplify the model phenomenology. The representation of the left-handed com-779 ponents under the  $SU(2)_L$  symmetry would lead to a coupling to 780 down-type quarks, since the effective theory is invariant under  $SU(2)_L \times U(1)_Y$  gauge symmetry. Having a coupling between the 782 new particle and *down*-type quarks would complicate the collider 783 phenomenology, adding the  $V \rightarrow b\bar{d} + \bar{b}d$  decay mode in addition 784 to the invisible decay mode. This in turn sets the scalar (vector) and pseudoscalar (axial vector) matrices to have elements of equal values. Furthermore, in order to be visible at the LHC in the monotop 787 final state, these models must include a strong coupling between the new particle  $\phi$  and  $t\chi$ . The same kind of assumption exists for the non-resonant production. This means that only the couplings 790 between the new scalar resonance and light quarks ( $a_{VR}$ ,  $a_{SR}$ ), and

$$(a_{VR}^q)_{11} = (a_{VR}^{1/2})_3 = a (5.5)$$

#### IMPLEMENTATION

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 $(a_{FC})$ , are set to non-zero values

This Section describes the notations used in the MadGraph model convention, in term of the ones introduced in the previous Section.

the couplings between the new vector, the top quark and light quarks

The Madgraph model [Fuk] used for these benchmarks corresponds to the Lagrangian from [AFM11]. Each coupling constant of this dynamics can be set via the parameter card and the blocks which are relevant for the two models used for the experimental searches are described below. The relevant parameters in the Mad-Graph parameter cards, also expressed in the notation introduced in the previous Section, are as follows for the two models considered.

- 1. Resonant scalar model described by the Lagrangian (5.3)
  - AQS and BQS:  $3 \times 3$  matrices (flavour space) fixing the coupling

- of the scalar  $\phi$  (S stands for scalar) and down-type quarks (Q stands for quarks), previously called  $a/b_{SR}$ .
  - A12S and B12S:  $3 \times 1$  matrices (flavour space) fixing the coupling of the DM candidate  $\chi$  (where 12 stands for spin-1/2 fermion) and up-type quarks, previously called  $a_{VR}^{1/2}$ .
- particle names: the scalar  $\phi^\pm$  is labeled S and the fermion  $\chi$  is  $f_{met}$
- 2. Non-resonant vectorial model described by the Lagrangian (5.4)
- A1FC and B1FC:  $3 \times 3$  matrices (flavour space) fixing the coupling of the vector V (1 stands for vector) and up-type quarks, previously called  $a_{FC}^0$ .
- particle name: the vector V is labelled  $v_{met}$ , while the dark matter candidate  $\chi$  is not implemented (as this model assumes  $BR(V \to \chi \chi) = 100\%$ )

The width of the scalar resonance and of the new vector are set to only the allowed decays in the models, namely a DM candidate and a top quark for the resonant model.

#### 823 PARAMETER SCAN

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The relevant parameters for the resonant model are:

- The mass of the new scalar  $\phi$ ;
- The mass of the DM candidate  $\chi$ ;
- The coupling of the new scalar to the DM candidate and top quark *a*, related to the width of the scalar in the minimal width assumption;
- The relevant parameters for the non-resonant model are:
- The mass of the new vector *V*;
- The mass of the DM candidate  $\chi$ ;
- The coupling of the new vector to the up and top quark *a*, related to the width of the scalar in the minimal width assumption;
- The coupling of the new vector to the DM candidate  $\chi$ , related to the branching fraction of the vector into invisible and visible particle, and as a consequence to the width of the vector.
- It has been checked for the non-resonant model that the relevant kinematics does not change when changing the width of the resonance. Figures 5.9 and 5.10 show the V mass distribution, the transverse momentum for V and for the top quark from the  $V \to t\bar{u}$  decay,

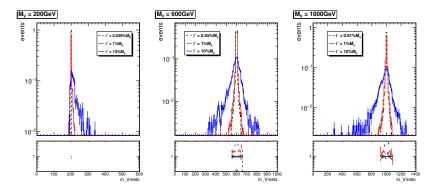


Figure 5.8: Distribution of *V* invariant mass for the  $gu \to tV (\to t\bar{u})$  (on-shell V) for  $m_V = 200$ , 600, 1000 GeV (from left to right) and for three different visible decay width (computed from Madgraph directly, 1% and 10%).

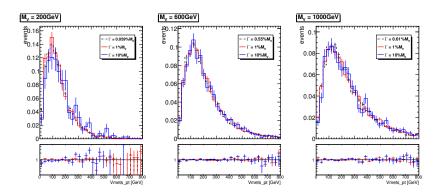


Figure 5.9: Distribution of the V  $p_T$  for the  $gu \to tV (\to t\bar{u})$  (on-shell V) for  $m_V$ = 200, 600, 1000 GeV (from left to right) and for three different visible decay width (computed from Madgraph directly, 1% and 10%).

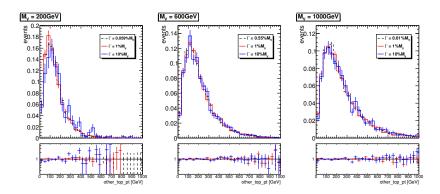


Figure 5.10: Distribution of the top quark  $p_T$  produced in association with V in  $gu \rightarrow tV$  for  $m_V = 200, 600,$ 1000 GeV (from left to right) and for three different visible decay width (computed from Madgraph directly, 1% and 10%).

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for different *V* masses and widths. These figures are relevant independently of the *V* decay mode (be it visible or invisible).

The limited timescale allowed to reach a consensus for the recommendations contained in this document has not allowed further studies on the parameter scan of these models. The two Collaborations are however encouraged to continue the path started for those studies and agree on a common parameter scan, following the same path as for other models described in this document.

### Validity of EFT approach

Effective Field Theories (EFTs) are an extremely useful tool for DM searches at the LHC. Given the current lack of indications about the nature of the DM particle and its interactions, a model independent interpretation of the collider bounds appears mandatory, especially in complementarity with the reinterpretation of the exclusion limits within a choice of simplified models, which cannot exhaust the set of possible completions of an effective Lagrangian. However EFTs must be used with caution at LHC energies, where the energy scale of the interaction is at a scale where the EFT approximation can no longer be assumed to be valid. Here we summarise some methods that can be used to ensure the validity of the EFT approximation.

These methods are described in detail in Refs. [BDSMR14?, BDSJ+14, A+15, RWZ15].

### 6.1 Outline of the procedure described in Refs. [? $A^+$ 15]

For a tree-level interaction between DM and the Standard Model (SM) via some mediator with mass M, the EFT approximation corresponds to expanding the propagator in powers of  $Q_{\rm tr}^2/M^2$ , truncating at lowest order, and combining the remaining parameters into a single parameter  $M_*$  (also called  $\Lambda$ ). For an example scenario with a Z'-type mediator (leading to some combination of operators D5 to D8 in the EFT limit) this corresponds to setting

$$\frac{g_{\text{DM}}g_q}{Q_{\text{tr}}^2 - M^2} = -\frac{g_{\text{DM}}g_q}{M^2} \left( 1 + \frac{Q_{\text{tr}}^2}{M^2} + \mathcal{O}\left(\frac{Q_{\text{tr}}^4}{M^4}\right) \right) \simeq -\frac{1}{M_*^2}, \tag{6.1}$$

where  $Q_{\rm tr}$  is the momentum carried by the mediator, and  $g_{\rm DM}$ ,  $g_q$  are the DM-mediator and quark-mediator couplings respectively. Similar expressions exist for other operators. Clearly the condition that must be satisfied for this approximation to be valid is that  $Q_{\rm tr}^2 < M^2 = g_{\rm DM} g_q M_*^2$ .

We can use this condition to enforce the validity of the EFT approximation by restricting the signal (after the imposition of the cuts

of the analysis) to events for which  $Q_{\rm tr}^2 < M^2$ . This truncated signal can then be used to derive the new, truncated limit on  $M_*$  as a function of  $(m_{\rm DM}, g_{\rm DM} g_g)$ .

For the example D5-like operator,  $\sigma \propto {M_*}^{-4}$ , and so there is a simple rule for converting a rescaled cross section into a rescaled constraint on  $M_*$  if the original limit is based on a simple cut-and-count procedure. Defining  $\sigma_{\rm EFT}^{\rm cut}$  as the cross section truncated such that all events pass the condition  $\sqrt{g_{\rm DM}g_q}M_*^{\rm rescaled} > Q_{\rm tr}$ , we have

$$M_*^{\text{rescaled}} = \left(\frac{\sigma_{\text{EFT}}}{\sigma_{\text{EFT}}^{\text{cut}}}\right)^{1/4} M_*^{\text{original}},$$
 (6.2)

which can be solved for  $M_*^{\rm rescaled}$  via either iteration or a scan (note that  $M_*^{\rm rescaled}$  appears on both the LHS and RHS of the equation). Similar relations exist for a given UV completion of each operator. The details and application of this procedure to ATLAS results can be found in Ref. [A $^+$ 15] for a range of operators. Since this method uses the physical couplings and energy scale  $Q_{\rm tr}$ , it gives the strongest possible constraints in the EFT limit while remaining robust by ensuring the validity of the EFT approximation.

### 6.2 Outline of the procedure described in Ref. [RWZ15]

In [RWZ15] a procedure to extract model independent and consistent bounds within the EFT is described. This procedure can be applied to any effective Lagrangian describing the interactions between the DM and the SM, and provides limits that can be directly reinterpreted in any completion of the EFT.

The range of applicability of the EFT is defined by a mass scale  $M_{\rm cut}$ , a parameter which marks the upper limit of the range of energy scales at which the EFT can be used reliably, independently of the particular completion of the model. Regardless of the details of the full theory, the energy scale probing the validity of the EFT is less than or equal to the centre-of-mass energy  $E_{\rm cm}$ , the total invariant mass of the hard final states of the reaction. Therefore, the condition ensuring the validity of the EFT is, by definition of  $M_{\rm cut}$ ,

$$E_{\rm cm} < M_{\rm cut} \,. \tag{6.3}$$

For example, in the specific case of a tree level mediation with a single mediator,  $M_{\text{cut}}$  can be interpreted as the mass of that mediator.

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There are then at least three free parameters describing an EFT: the DM mass  $m_{\rm DM}$ , the scale  $M_*$  of the interaction, and the cutoff scale  $M_{\rm cut}$ .

We can use the same technique as above to restrict the signal to the events for which  $E_{\rm cm} < M_{\rm cut}$ , using only these events to derive the exclusion limits on  $M_*$  as a function of  $(m_{\rm DM}, M_{\rm cut})$ . We can also define an *effective coupling strength*  $M_{\rm cut} = g_* M_*$ , where  $g_*$  is a free parameter that substitutes the parameter  $M_{\rm cut}$ , and therefore derive exclusions on  $M_*$  as a function of  $(m_{\rm DM}, g_*)$ . This allows us to see how much of the theoretically allowed parameter space has been actually tested and how much is still unexplored; For example, in the Z'-type model considered above,  $g_*$  is equal to  $\sqrt{g_{\rm DM}g_q}$ . The resulting plots are shown in [RWZ15] for a particular effective operator.

The advantage of this procedure is that the obtained bounds can be directly and easily recast in any completion of the EFT, by computing the parameters  $M_*$ ,  $M_{\rm cut}$  in the full model as functions of the parameters of the complete theory. On the other hand, the resulting limits will be weaker than those obtained using  $Q_{\rm tr}$  and a specific UV completion.

- 6.3 EFT validity recommendations
- 6.4 Recommendation for contact interaction theories with simplified models available
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Recommendation for truncation of theories with no simplified models available

 $M_{\rm cut}$  is related to physical couplings and masses only in a UV complete theory, and so is effectively a free parameter. It makes sense to choose  $M_{\rm cut}$ such that we identify the transition region where the EFT stops being a good description of UV complete theories. This can be done using R, which is defined as the fraction of events for which  $\hat{s} > M_{\rm cut}^2$ .

For large values of  $M_{\rm cut}$ , no events are thrown away in the truncation procedure, and R=1. As  $M_{\rm cut}$  becomes smaller, eventually all events are thrown away in the truncation procedure, i.e. R=0, and the EFT gives no exclusion limits for the chosen acceptance.

We propose a rough scan over  $M_{\rm cut}$ , such that we find the values of  $M_{\rm cut}$  for which R ranges from, say, 0.1 to 1. We can then perform a scan over (several, your choice) values of  $M_{\rm cut}$ , showing the truncated limit for each one.

When R=0, there is no limit. When R reaches 1, the truncated limit is identical to the original limit.

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## Appendix: Detailed studies on mono-jet signatures

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CKKW parton matching implementation
   A.1
   The parton matching techniques are implemented in the mono-jet
   like MC generation in order to avoid double counting the partons
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   from matrix elements and parton showering. The CKKW matching
   is better developed and preferred in this study. As the illustration
   sample, the EFT D5 samples are generated with MadGraph5_aMC@NLO
   version 2.2.2. The technical implementations are shown as below.
      On the generator side, i.e., MadGraph5_aMC@NLO:
   • ickkw = 0
     ktdurham = matching scale
     dparameter = 0.4
     dokt = T
     ptj=20
   • drjj=0
   • mmjj=0
     ptj1min=0
   On the parton showering side, i.e., Pythia 8:
   • Merging:ktType = 1
   • Merging: TMS = matching scale
   • 1000022:all = chi chi 2 0 0 30.0 0.0 0.0 0.0 0.0
     1000022:isVisible = false
   • Merging:doKTMerging = on
   • Merging:Process = pp>chi,1000022chi ,-1000022
```

### Merging:nJetMax = 2

The matching scales should be the same for the generation and parton showering. In MadGraph5\_aMC@NL0, the particle data group ID
1000022 is used for weakly interacting dark matter candidates, which should be informed to Pythia 8.

In this test we are generating the process with up to two parton emissions, so the command Merging:nJetMax = 2 is applied to Pythia 8. The different parton emission cases are generated separately:

p p > chi chi
 p p > chi chi j
 p p > chi chi j j
 p p > chi chi j j

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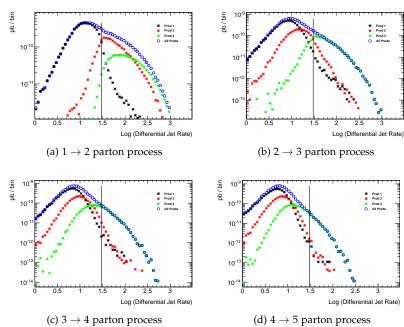
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Two matching scales are tested at 30 and 80 GeV. The differential jet rates are shown in Fig. A.1 for matching scale 30 GeV and Fig. A.2 for 80 GeV. The 80 GeV matching scale gives smoother distribution, which is desired to avoid artifical effect due to parton matching.

There will be a small tink around the matching scale for both cases.



To compare the effect in a finer step, the matching scales at 30, 50, 70, 80 and 90 GeV are plotted in FigA.3. Globally good agreement is seen among different matching scales, with some difference observed around the matching scale. A closer look in this range shows that the 80 and 90 GeV matching scales produce very close distributions, so it is safe to use 80 GeV as the baseline matching scale.

Figure A.1: Jet differential rates distributions for EFT D5 sample with CKKW matching scale at 30 GeV. o-, 1- and 2-parton emission cases are generated separatedly. A vertical line is drawn at the matching scale.

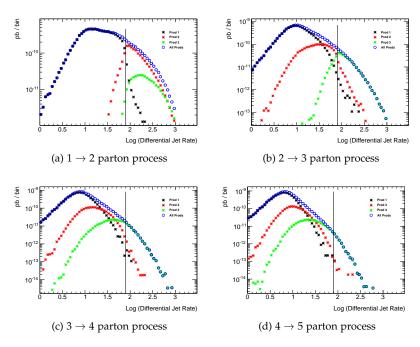


Figure A.2: Jet differential rates distributions for EFT D5 sample with CKKW matching scale at 80 GeV. o-, 1- and 2-parton emission cases are generated separatedly. A vertical line is drawn at the matching scale.

The MC distributions for the missing transverse energy and transverse momenta for the leading and subleading jets are plotted in Fig.. For the mono-jet analysis, usually a missing transverse energy cut larger than 300 GeV is applied for offline selection, which makes the contribution of the o-parton emission case negligible in the mono-jet analysis.

### Parton emission generation

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In order to describe the signal kinematics correctly and save time in MC generation, the parton emissions will only be generated up to a certain numbers of parton and ignore the cases with more partons. The later ones usually have cross sections small enough and limited contribution in the interested kinematic regions.

It is found that the 3- or more-parton emission cases are negligible in our intersted regions, but the 2-parton emission case has significant contributions. The o- and 1-parton emissions are out of discussion since they give the baseline signature in this analysis. The impacts of 2- and 3-parton emissions are quantified in this section.

Here the o-, 1-, 2- and 3-parton emissions are generated separately and requested in matching step with Merging:nJetMax=3 and scale at 80 GeV in Pythia8for 0+1+2+3 parton emission case, while Merging:nJetMax=2 requested for o+1+2 case and Merging:nJetMax=1 requested for 0+1 case. The kinematic distributions for MET, leading and subleading jet transverse momenta are plotted in Fig.A.5, while

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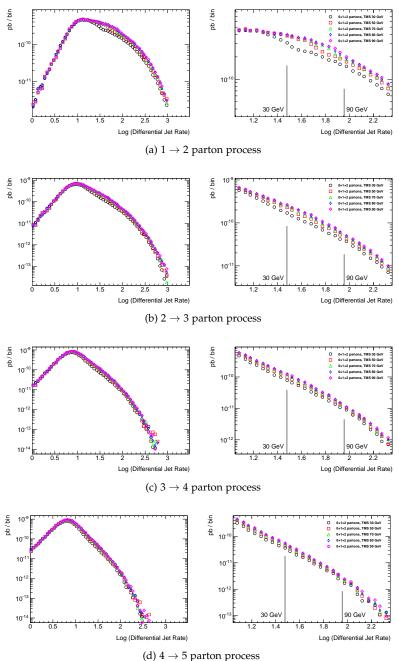
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is shown in Fig.A.6.



the jet multiplicity at different leading jet transverse momentum cuts

With the ATLAS run-I baseline cut (MET and leading jet  $p_T$  larger than 250 GeV, less than 4 jets), the 0+1 parton emission has 17.4% yield less compared to 0+1+2+3 parton emission, while the 0+1+2 has 2.2% less. With MET>400 GeV, 0+1 parton emission has 16.8% yield less and 0+1+2 parton emission has 2.4% less compared to 0+1+2+3 parton emission. With MET>600 GeV, 0+1 parton emission has 16.5%

Figure A.3: Jet differential rates distributions for EFT D5 sample with CKKW matching scale at 30, 50, 70, 80 and 90 GeV. 0-, 1- and 2-parton emission cases are generated separatedly and the total merged contribution is shown. A closer look is shown around the matching scale.

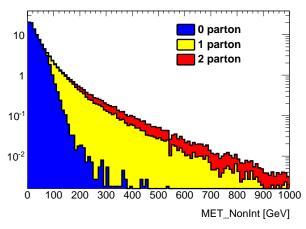
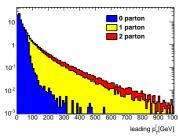
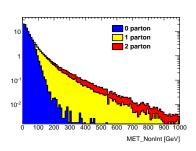


Figure A.4: Kinematics distributions for EFT D5 sample with CKKW matching scale at 80 GeV. o-, 1- and 2-parton emission cases are generated separatedly and added together by cross sections. The o-parton emission case has very limited contribution for missing transverse energy larger than 300 GeV region.

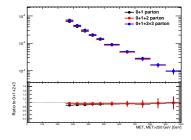
(a) Missing transverse momentum

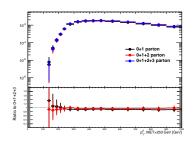




(b) Transverse momentum of leading jet

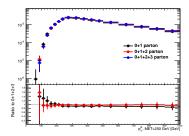
(c) Transverse momentum of subleading





(a) Missing transverse momentum

(b) Transverse momentum of leading jet



(c) Transverse momentum of subleading

Figure A.5: Kinematics distributions for EFT D<sub>5</sub> sample with CKKW matching scale at 80 GeV. o-, 1-, 2- and 3-parton emission cases are generated separatedly and added together by cross sections.

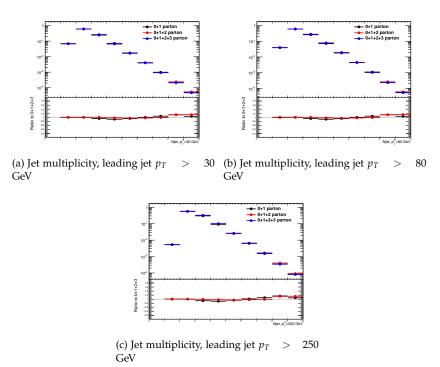


Figure A.6: Jet multiplicity distributions for EFT D5 sample with CKKW matching scale at 80 GeV. o-, 1-, 2- and 3-parton emission cases are generated separatedly and added together by cross sections.

yield less and 0+1+2 parton emission has 2.9% less compared to
 0+1+2+3 parton emission. The same numbers hold if a sysmetric cut
 is added on leading jet transverse momentum.

## Appendix: Detailed studies for EW models

B.1 Further W+MET models with possible cross-section enhance-

As pointed out in Ref. [BCD<sup>+</sup>15], the mono-W signature can probe the iso-spin violating interactions of dark matter with quarks. The relevant operators after the electroweak symmetry breaking is

$$\frac{1}{\Lambda^2} \overline{\chi} \gamma_{\mu} \chi \left( \overline{u}_L \gamma^{\mu} u_L + \xi \overline{d}_L \gamma^{\mu} d_L \right) . \tag{B.1}$$

Here, we only keep the left-handed quarks because the right-handed quarks do not radiate a *W*-gauge boson from the weak interaction. As the LHC constraints the cutoff to higher values, it is also important to know the corresponding operators before the electroweak symmetry. At the dimension-six level, the following operator

$$\frac{c_6}{\Lambda^2} \overline{\chi} \gamma_\mu \chi \, \overline{Q}_L \gamma^\mu Q_L \tag{B.2}$$

conserves iso-spin and provides us  $\xi=1$  [?]. At the dimension-eight level, new operators appear to induce iso-spin violation and can be

$$\frac{c_8^d}{\Lambda^4} \overline{\chi} \gamma_\mu \chi \left( H \overline{Q}_L \right) \gamma^\mu (Q_L H^\dagger) + \frac{c_8^u}{\Lambda^4} \overline{\chi} \gamma_\mu \chi \left( \tilde{H} \overline{Q}_L \right) \gamma^\mu (Q_L \tilde{H}^\dagger) \,. \tag{B.3}$$

After inputting the vacuum expectation value of the Higgs field, we have

$$\xi = \frac{c_6 + c_8^d \, v_{\text{EW}}^2 / 2\Lambda^2}{c_6 + c_8^d \, v_{\text{FW}}^2 / 2\Lambda^2}.$$
 (B.4)

For a nonzero  $c_6$  and  $v_{\rm EW} \ll \Lambda$ , the iso-spin violation effects are suppressed. On the other hand, the values of  $c_6$ ,  $c_8^d$  and  $c_8^u$  depend on the UV-models.

There is one possible UV-model to obtain a zero value for  $c_6$  and non-zero values for  $c_8^d$  and  $c_8^u$ . One can have the dark matter and the SM Higgs field charged under a new U(1)'. There is a small mass mixing between SM Z-boson and the new Z' with a mixing angle

of  $\mathcal{O}(v_{\rm EW}^2/M_{Z'}^2)$ . After integrating out Z', one has different effective dark matter couplings to  $u_L$  and  $d_L$  fields, which are proportional to their couplings to the Z boson. For this model, we have  $c_6=0$  and

$$\xi = \frac{-\frac{1}{2} + \frac{1}{3}\sin^2\theta_W}{\frac{1}{2} - \frac{2}{3}\sin^2\theta_W} \approx -2.7$$
 (B.5)

and order of unity.

# Appendix: Table of cross sections for $t\bar{t}$ +MET searches

All tables need to be adjusted with right number of significant digits

Coupling (g)	$m_{Phi}$ [GeV]	$m_{\chi}$ [GeV]	$\Gamma_{min}$ [GeV]	$\sigma$
0.1	10	1	0.00374318	$0.207 \pm 0.0006846$
0.1	20	1	0.00784569	$0.1121 \pm 0.0003285$
0.1	50	1	0.01987	$0.03211 \pm 0.0001005$
0.1	100	1	0.0398141	$0.007325 \pm 2.416e-05$
0.1	150	1	0.0597437	$0.002396 \pm 7.419e-06$
0.1	200	1	0.0796724	$0.001018 \pm 3.398 \text{e-}06$
0.1	300	1	0.119549	0.0003394 $\pm$ 1.234e-06
0.1	500	1	0.310863	$6.802\text{e-}05 \pm 2.343\text{e-}07$
0.1	1000	1	0.881329	$5.817e\text{-}06 \pm 2.356e\text{-}08$
0.1	1500	1	1.40417	$8.942e ext{-07} \pm 3.832e ext{-09}$
0.1	10	10	0.000100	$1.007e-05 \pm 3.761e-08$
0.1	20	10	0.000100	$3.491e$ -05 $\pm$ 1.012e-07
0.1	50	10	0.0153395	$0.03212 \pm 0.0001037$
0.1	100	10	0.0374747	$0.007343 \pm 2.011e-05$
0.1	150	10	0.0581752	$0.002389 \pm 7.654$ e-06
0.1	200	10	0.0784937	$0.001018 \pm 6.258 \text{e-}06$
0.1	300	10	0.118762	$0.0003373 \pm 1.448e-06$
0.1	500	10	0.310391	$6.773 \text{e-o}5 \pm 2.326 \text{e-o}7$
0.1	1000	10	0.881093	$5.81\text{e-}06 \pm 2.245\text{e-}08$
0.1	1500	10	1.40401	$8.937\text{e-o}7 \pm 4.013\text{e-o}9$
0.1	50	50	0.0000233555	$2.581 \text{e-o}7 \pm 1.214 \text{e-o}9$
0.1	100	50	0.0000492402	$1.526e-06 \pm 7.038e-09$
0.1	150	50	0.0247905	$0.002387 \pm 8.272e$ -06
0.1	200	50	0.051794	$0.00102 \pm 3.216$ e-06
0.1	300	50	0.100226	$0.0003366 \pm 1.393e-06$
0.1	500	50	0.299052	$6.679 \text{e-o}5 \pm 2.406 \text{e-o}7$
0.1	1000	50	0.875378	$5.764e-06 \pm 2.472e-08$
0.1	1500	50	1.4002	$8.866$ e-07 $\pm$ 3.257e-09

Table C.1 – continued from previous page

Coupling (g)	$m_{Phi}$ [GeV]	$m_{\chi}$ [GeV]	$\Gamma_{min}$ [GeV]	$\sigma$
0.1	100	150	0.0000492402	$1.246\text{e-}08 \pm 5.121\text{e-}11$
0.1	150	150	0.0000765167	$1.393 \text{e-} 08 \pm 6.653 \text{e-} 11$
0.1	200	150	0.000106902	$1.693 \text{e-}08 \pm 8.493 \text{e-}11$
0.1	300	150	0.000190543	$7.557\text{e-}08 \pm 2.171\text{e-}10$
0.1	500	150	0.213784	$5.063$ e-05 $\pm$ 1.724e-07
0.1	1000	150	0.828844	$5.365 \text{e-}06 \pm 2.028 \text{e-}08$
0.1	1500	150	1.36872	$8.603\text{e-o}7 \pm 3.769\text{e-o}9$
0.1	200	300	0.000106902	$1.415 ext{e-o9} \pm 5.97 ext{e-12}$
0.1	300	300	0.000190543	$1.64e-09 \pm 7.878e-12$
0.1	500	300	0.111924	$3.078e-09 \pm 1.482e-11$
0.1	1000	300	0.687162	$3.828e-06 \pm 1.416e-08$
0.1	1500	300	1.26683	$7.579e-07 \pm 3.041e-09$
0.1	500	500	0.111924	$1.784e$ -10 $\pm$ 1.105e-12
0.1	1000	500	0.483444	$1.98 ext{e-}09 \pm 9.199 ext{e-}12$
0.1	1500	500	1.05448	$4.92e$ -07 $\pm$ 2.14e-09
0.3	10	1	0.0336886	$1.876 \pm 0.006611$
0.3	20	1	0.0706112	$1.006 \pm 0.003894$
0.3	50	1	0.17883	$0.2886 \pm 0.0009285$
0.3	100	1	0.358327	$0.06598 \pm 0.000182$
0.3	150	1	0.537693	0.0214 $\pm$ 6.701e-05
0.3	200	1	0.717052	$0.009216 \pm 3.533e-05$
0.3	300	1	1.07594	$0.003044 \pm 1.194e-05$
0.3	500	1	2.79777	$0.0006105 \pm 2.187e-06$
0.3	1000	1	7.93196	$5.256e-05 \pm 2.165e-07$
0.3	1500	1	12.6376	$8.048e-06 \pm 3.473e-08$
0.3	10	10	5.69808	$0.0008143 \pm 3.272e-06$
0.3	20	10	0.0000630938	$0.002836 \pm 9.724e-06$
0.3	50	10	0.138055	$0.2869 \pm 0.0008971$
0.3	100	10	0.337272	$0.06606 \pm 0.0002407$
0.3	150	10	0.523576	0.02145 $\pm$ 8.01e-05
0.3	200	10	0.706443	$0.009222 \pm 2.807e-05$
0.3	300	10	1.06886	$0.003051 \pm 1.001e-05$
0.3	500	10	2.79352	$0.0006115 \pm 2.268e-06$
0.3	1000	10	7.92983	$5.24e-05 \pm 1.964e-07$
0.3	1500	10	12.6361	$8.053e-06 \pm 3.203e-08$
0.3	10	50	5.69808	$1.704e-05 \pm 7.077e-08$
0.3	20	50	0.0000630938	$1.746e-05 \pm 7.383e-08$
0.3	50	50	0.000210199	$2.071e-05 \pm 8.162e-08$
0.3	100	50	0.000443162	$0.0001245 \pm 3.888 \text{e-o7}$
0.3	150	50	0.223114	o.o2138 ± 6.22e-o5

Table C.1 – continued from previous page

Coupling (g)	$m_{Phi}$ [GeV]	$m_{\chi}$ [GeV]	$\Gamma_{min}$ [GeV]	$\sigma$
0.3	200	50	0.466146	$0.009186 \pm 3.168 e - 05$
0.3	300	50	0.902031	$0.003039 \pm 1.09e-05$
0.3	500	50	2.69146	$0.0005971 \pm 2.181e-06$
0.3	1000	50	7.8784	$5.222e-05 \pm 1.907e-07$
0.3	1500	50	12.6018	$7.947e-06 \pm 2.996e-08$
0.3	100	150	0.000443162	$1.004e-06 \pm 4.682e-09$
0.3	150	150	0.00068865	$1.132e-06 \pm 4.644e-09$
0.3	200	150	0.000962116	$1.349e-06 \pm 6.834e-09$
0.3	300	150	0.00171489	$6.08\text{e-}06 \pm 2.289\text{e-}08$
0.3	500	150	1.92405	$0.000456 \pm 2.064e-06$
0.3	1000	150	7.45959	$4.818e-05 \pm 1.84e-07$
0.3	1500	150	12.3185	$7.796e-06 \pm 2.802e-08$
0.3	200	300	0.000962116	$1.144e-07 \pm 4.635e-10$
0.3	300	300	0.00171489	$1.324e-07 \pm 6.534e-10$
0.3	500	300	1.00732	$2.5e-07 \pm 1.113e-09$
0.3	1000	300	6.18446	$3.439e-05 \pm 1.376e-07$
0.3	1500	300	11.4014	$6.834e\text{-}06 \pm 2.623e\text{-}08$
0.3	500	500	1.00732	$1.449e-08 \pm 5.536e-11$
0.3	1000	500	4.35099	$1.487e-07 \pm 6.617e-10$
0.3	1500	500	9.49035	$4.374e-06 \pm 1.739e-08$
0.7	10	1	0.183416	$10.2 \pm 0.03649$
0.7	20	1	0.384439	$5.462 \pm 0.02022$
0.7	50	1	0.97363	$1.558 \pm 0.004491$
0.7	100	1	1.95089	$0.3568 \pm 0.001143$
0.7	150	1	2.92744	$0.1161 \pm 0.0003685$
0.7	200	1	3.90395	$0.04995 \pm 0.0001494$
0.7	300	1	5.85789	$0.01649 \pm 5.579 \text{e-}05$
0.7	500	1	15.2323	$0.003313 \pm 1.464e-05$
0.7	1000	1	43.1851	$0.0002823 \pm 1.233e-06$
0.7	1500	1	68.8045	$4.481e-05 \pm 1.885e-07$
0.7	10	10	0.0000310229	$0.02403 \pm 0.0001038$
0.7	20	10	0.000343511	$0.08347 \pm 0.0004742$
0.7	50	10	0.751635	$1.553 \pm 0.004764$
0.7	100	10	1.83626	$0.3569 \pm 0.0009501$
0.7	150	10	2.85058	$0.1165 \pm 0.0004139$
0.7	200	10	3.84619	$0.04984 \pm 0.0001855$
0.7	300	10	5.81933	$0.01649 \pm 6.843e-05$
0.7	500	10	15.2092	$0.003301 \pm 1.289e-05$
0.7	1000	10	43.1735	$0.0002815 \pm 1.129e-06$
0.7	1500	10	68.7967	4.491e-05 ± 2.108e-07

Table C.1 – continued from previous page

Coupling (g)	$m_{Phi}$ [GeV]		$\Gamma_{min}$ [GeV]	$\sigma$
0.7	10	50	0.0000310229	0.000511 ± 1.977e-06
0.7	20	50	0.000343511	$0.0005184 \pm 2.146e-06$
0.7	50	50	0.00114442	$0.0006176 \pm 3.053e-06$
0.7	100	50	0.00241277	$0.003681 \pm 1.333e-05$
0.7	150	50	1.21473	$0.1156 \pm 0.0003755$
0.7	200	50	2.53791	$0.04988 \pm 0.0001824$
0.7	300	50	4.91106	$0.01651 \pm 6.317 e$ -05
0.7	500	50	14.6535	$0.003218 \pm 1.523e-05$
0.7	1000	50	42.8935	$0.0002794 \pm 1.049e-06$
0.7	1500	50	68.6098	$4.46\text{e-}05 \pm 1.989\text{e-}07$
0.7	100	150	0.00241277	$2.968e-05 \pm 1.364e-07$
0.7	150	150	0.00374932	$3.327e-05 \pm 1.594e-07$
0.7	200	150	0.00523819	$4.04e-05 \pm 1.861e-07$
0.7	300	150	0.00933663	$0.0001787 \pm 7.694e$ -07
0.7	500	150	10.4754	0.00243 $\pm$ 1.128e-05
0.7	1000	150	40.6133	$0.0002573 \pm 1.014e-06$
0.7	1500	150	67.0675	$4.239e-05 \pm 1.707e-07$
0.7	100	300	0.00241277	$3.132e-06 \pm 1.547e-08$
0.7	150	300	0.00374932	$3.227e-06 \pm 1.433e-08$
0.7	200	300	0.00523819	$3.393e-06 \pm 1.437e-08$
0.7	300	300	0.00933663	$3.918e-06 \pm 1.628e-08$
0.7	500	300	5.4843	$7.383e-06 \pm 2.87e-08$
0.7	1000	300	33.6709	$0.0001801 \pm 7.992e-07$
0.7	1500	300	62.0745	$3.644e-05 \pm 1.473e-07$
0.7	500	500	5.4843	$4.301e-07 \pm 1.836e-09$
0.7	1000	500	23.6887	$3.684e-06 \pm 2.358e-08$
0.7	1500	500	51.6697	$2.291e-05 \pm 9.843e-08$
1.	10	1	0.374318	$20.79 \pm 0.08102$
1.	20	1	0.784569	$11.08 \pm 0.0396$
1.	50	1	1.987	$3.146 \pm 0.01331$
1.	100	1	3.98141	$0.7199 \pm 0.002775$
1.	150	1	5.97437	$0.2354 \pm 0.0008189$
1.	200	1	7.96724	$0.1009 \pm 0.0003854$
1.	300	1	11.9549	$0.03369 \pm 0.0001155$
1.	500	1	31.0863	$0.006652 \pm 2.898e-05$
1.	1000	1	88.1329	$0.0005705 \pm 2.817e-06$
1.	1500	1	140.417	$9.244e-05 \pm 4.273e-07$
1.	10	10	0.000063312	$0.1009 \pm 0.00035$
1.	20	10	0.000701043	$0.3475 \pm 0.002265$
1.	50	10	1.53395	$3.139 \pm 0.01028$

Table C.1 – continued from previous page

Coupling (g)	$m_{Phi}$ [GeV]	$m_{\chi}$ [GeV]	$\Gamma_{min}$ [GeV]	$\sigma$
1.	100	10	3.74747	$0.7158 \pm 0.002486$
1.	150	10	5.81752	$0.236 \pm 0.0007591$
1.	200	10	7.84937	$0.1013 \pm 0.0003668$
1.	300	10	11.8762	$0.03374 \pm 0.0001403$
1.	500	10	31.0391	$0.006631 \pm 2.585 e{-}05$
1.	1000	10	88.1093	$0.0005663 \pm 2.515e-06$
1.	1500	10	140.401	9.408e-05 ± 4.698e-07
1.	10	50	0.000063312	$0.00212 \pm 8.815 e\text{-}06$
1.	20	50	0.000701043	$0.002149 \pm 9.604 e$ -06
1.	50	50	0.00233555	$0.002568 \pm 1.017e-05$
1.	100	50	0.00492402	$0.01523 \pm 5.043 e$ -05
1.	150	50	2.47905	$0.2351 \pm 0.0008404$
1.	200	50	5.1794	$0.09993 \pm 0.0003164$
1.	300	50	10.0226	$0.03349 \pm 0.0001351$
1.	500	50	29.9052	$0.006402 \pm 2.604e-05$
1.	1000	50	87.5378	$0.0005634 \pm 2.601e-06$
1.	1500	50	140.02	$9.211e-05 \pm 4.909e-07$
1.	100	150	0.00492402	$0.0001247 \pm 5.899e$ -07
1.	150	150	0.00765167	$0.0001387 \pm 5.889$ e-07
1.	200	150	0.0106902	$0.000168 \pm 7.656$ e-07
1.	300	150	0.0190543	$0.0007464 \pm 2.977e-06$
1.	500	150	21.3784	$0.004856 \pm 1.95e-05$
1.	1000	150	82.8844	$0.0005122 \pm 1.98e-06$
1.	1500	150	136.872	$8.662e-05 \pm 3.821e-07$
1.	200	300	0.0106902	$1.422e-05 \pm 6.147e-08$
1.	300	300	0.0190543	$1.626e-05 \pm 6.865e-08$
1.	500	300	11.1924	$3.081e-05 \pm 1.244e-07$
1.	1000	300	68.7162	$0.0003534 \pm 1.392e-06$
1.	1500	300	126.683	$7.258e-05 \pm 3.651e-07$
1.	500	500	11.1924	$1.777e-06 \pm 9.67e-09$
1.	1000	500	48.3444	$1.331e-05 \pm 6.551e-08$
1.	1500	500	105.448	$4.443e-05 \pm 1.988e-07$
1.5	10	1	0.842215	$46.59 \pm 0.1797$
1.5	20	1	1.76528	$24.52 \pm 0.08387$
1.5	50	1	4.47075	$6.903 \pm 0.02244$
1.5	100	1	8.95817	$1.577 \pm 0.005493$
1.5	150	1	13.4423	$0.5224 \pm 0.002309$
1.5	200	1	17.9263	$0.2259 \pm 0.0008625$
1.5	300	1	26.8985	$0.07529 \pm 0.0003407$
1.5	500	1	69.9442	0.01445 ± 6.469e-05

Table C.1 – continued from previous page

1.5         1000         1         198.299 $0.001234 \pm 5.694e-06$ 1.5         1500         1         315.939 $0.002179 \pm 1.024e-06$ 1.5         10         10 $0.000157735$ $1.763 \pm 0.01031$ 1.5         20         10 $0.00157735$ $1.763 \pm 0.01031$ 1.5         50         10 $3.45138$ $6.906 \pm 0.02283$ 1.5         100         10 $8.4318$ $1.568 \pm 0.006489$ 1.5         150         10 $13.0894$ $0.5162 \pm 0.001934$ 1.5         200         10 $17.6611$ $0.2249 \pm 0.0008153$ 1.5         300         10 $26.7214$ $0.07541 \pm 0.0002941$ 1.5         300         10 $26.7214$ $0.07541 \pm 0.0002841$ 1.5         300         10 $198.246$ $0.00147 \pm 6.923e-05$ 1.5         1500         10 $315.903$ $0.002157 \pm 8.805e-07$ 1.5         1500         10 $315.903$ $0.002157 \pm 8.805e-07$ 1.5         150         10 $30.503$ $0.00157735$ $0.016$	Coupling (g)			$\Gamma_{min}$ [GeV]	$\sigma$
1.5         10         10 $0.000142452$ $0.5117 \pm 0.002037$ 1.5         20         10 $0.00157735$ $1.763 \pm 0.01031$ 1.5         50         10 $3.45138$ $6.906 \pm 0.02283$ 1.5         100         10 $8.4318$ $1.568 \pm 0.006489$ 1.5         150         10 $13.0894$ $0.5162 \pm 0.001934$ 1.5         200         10 $17.6611$ $0.2249 \pm 0.0008153$ 1.5         300         10 $26.7214$ $0.07541 \pm 0.0002941$ 1.5         500         10 $69.8379$ $0.01447 \pm 6.923e-05$ 1.5         1000         10 $198.246$ $0.001242 \pm 6.739e-06$ 1.5         1500         10 $315.903$ $0.0002157 \pm 8.805e-07$ 1.5         100         50 $0.00157735$ $0.01068 \pm 4.527e-05$ 1.5         10         50 $0.00157735$ $0.01093 \pm 6.079e-05$ 1.5         10         50 $0.011079$ $0.07677 \pm 0.0002445$ 1.5         15         50         50 $0.011079$ $0.07$	1.5	1000	1	198.299	$0.001234 \pm 5.694$ e-06
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	1.5	1500	1	315.939	$0.0002179 \pm 1.024e$ -06
1.5         50         10 $3.45138$ $6.906 \pm 0.02283$ 1.5         100         10 $8.4318$ $1.568 \pm 0.006489$ 1.5         150         10 $13.0894$ $0.5162 \pm 0.001934$ 1.5         200         10 $17.6611$ $0.2249 \pm 0.0008153$ 1.5         300         10 $26.7214$ $0.07541 \pm 0.002941$ 1.5         500         10 $69.8379$ $0.01447 \pm 6.923e-05$ 1.5         1000         10 $198.246$ $0.001242 \pm 6.739e-06$ 1.5         1500         10 $198.246$ $0.001242 \pm 6.739e-06$ 1.5         1500         10 $315.903$ $0.0002157 \pm 8.805e-07$ 1.5         150         10         50 $0.00142452$ $0.01083 \pm 6.092e-05$ 1.5         150         50 $0.00157735$ $0.01093 \pm 6.092e-05$ 1.5         10         50 $0.0011079$ $0.07677 \pm 0.0002445$ 1.5         10         50 $0.011079$ $0.07677 \pm 0.0002445$ 1.5         150         50 $5.57786$	1.5	10	10	0.000142452	$0.5117 \pm 0.002037$
1.5         100         10         8.4318 $1.568 \pm 0.006489$ 1.5         150         10 $13.0894$ $0.5162 \pm 0.001934$ 1.5         200         10 $17.6611$ $0.2249 \pm 0.0008153$ 1.5         300         10 $26.7214$ $0.07541 \pm 0.0002941$ 1.5         500         10 $69.8379$ $0.01447 \pm 6.923e-05$ 1.5         1000         10 $198.246$ $0.001242 \pm 6.739e-06$ 1.5         1500         10 $315.903$ $0.0002157 \pm 8.805e-07$ 1.5         10         50 $0.000142452$ $0.01083 \pm 6.79e-05$ 1.5         10         50 $0.00157735$ $0.0193 \pm 6.079e-05$ 1.5         10         50 $0.0011079$ $0.07677 \pm 0.0002445$ 1.5         10         50 $0.011079$ $0.07677 \pm 0.0002445$ 1.5         150         50 $5.57786$ $0.5195 \pm 0.000511$ 1.5         150         50 $5.57786$ $0.5195 \pm 0.0006711$ 1.5         150         50 $5.25786$ $0.07353 \pm 0.0003291$ <td>1.5</td> <td>20</td> <td>10</td> <td>0.00157735</td> <td><math>1.763 \pm 0.01031</math></td>	1.5	20	10	0.00157735	$1.763 \pm 0.01031$
1.5       150       10       13.0894 $0.5162 \pm 0.001934$ 1.5       200       10       17.6611 $0.2249 \pm 0.0008153$ 1.5       300       10       26.7214 $0.07541 \pm 0.0002941$ 1.5       500       10       69.8379 $0.01447 \pm 6.923e-05$ 1.5       1000       10       198.246 $0.001242 \pm 6.73ge-06$ 1.5       1500       10       315.903 $0.0002157 \pm 8.805e-07$ 1.5       10       50 $0.0012452$ $0.01083 \pm 6.527e-05$ 1.5       10       50 $0.00157735$ $0.01093 \pm 6.079e-05$ 1.5       10       50 $0.00157735$ $0.01093 \pm 6.079e-05$ 1.5       10       50 $0.0011279$ $0.07677 \pm 0.0002445$ 1.5       10       50 $0.011079$ $0.07677 \pm 0.0002445$ 1.5       150       50 $0.011079$ $0.07677 \pm 0.0002445$ 1.5       150       50 $0.011079$ $0.07677 \pm 0.0002445$ 1.5       150       50 $0.011079$ $0.07677 \pm 0.00024$ 1.5       150       50 $0.024866$ $0.0139 \pm 0.0002$	1.5	50	10	3.45138	$6.906 \pm 0.02283$
1.5       200       10 $17.6611$ $0.2249 \pm 0.0008153$ 1.5       300       10 $26.7214$ $0.07541 \pm 0.0002941$ 1.5       500       10 $69.8379$ $0.01447 \pm 6.923e-05$ 1.5       1000       10 $198.246$ $0.001242 \pm 6.739e-06$ 1.5       1500       10 $315.903$ $0.0002157 \pm 8.805e-07$ 1.5       10       50 $0.00015775$ $0.01068 \pm 4.527e-05$ 1.5       10       50 $0.0015775$ $0.01093 \pm 6.079e-05$ 1.5       20       50 $0.0015775$ $0.01093 \pm 6.079e-05$ 1.5       100       50 $0.011079$ $0.07677 \pm 0.0002445$ 1.5       150       50 $0.72866$ $0.0139 \pm 0.00057$ 1.5       150       50 $0.72866$ $0.01$	1.5	100	10	8.4318	$1.568 \pm 0.006489$
1.5       300       10 $26.7214$ $0.07541 \pm 0.0002941$ 1.5       500       10 $69.8379$ $0.01447 \pm 6.923e-05$ 1.5       1000       10 $198.246$ $0.001242 \pm 6.739e-06$ 1.5       1500       10 $315.903$ $0.0002157 \pm 8.805e-07$ 1.5       10       50 $0.000157735$ $0.01068 \pm 4.527e-05$ 1.5       20       50 $0.00157735$ $0.01093 \pm 6.079e-05$ 1.5       50       50 $0.00525498$ $0.01302 \pm 6.649e-05$ 1.5       100       50 $0.011079$ $0.07677 \pm 0.0002445$ 1.5       150       50 $5.57786$ $0.5195 \pm 0.001577$ 1.5       150       50 $5.57786$ $0.5195 \pm 0.001577$ 1.5       150       50 $11.6536$ $0.2195 \pm 0.000571$ 1.5       150       50 $16.966$ $0.0159 \pm 0.000671$ 1.5       150       50 $50.25508$ $0.07353 \pm 0.000329$ 1.5       1500       50 $67.2866$ $0.01299 \pm 7.038e-06$ 1.5       1500       50 $315.045$ $0.000219$	1.5	150	10	13.0894	$0.5162 \pm 0.001934$
1.5       500       10 $69.8379$ $0.01447 \pm 6.923e-05$ 1.5       1000       10 $198.246$ $0.001242 \pm 6.739e-06$ 1.5       1500       10 $315.903$ $0.0002157 \pm 8.805e-07$ 1.5       10       50 $0.000157735$ $0.01068 \pm 4.527e-05$ 1.5       20       50 $0.00157735$ $0.01093 \pm 6.079e-05$ 1.5       50       50 $0.00525498$ $0.01302 \pm 6.649e-05$ 1.5       100       50 $0.011079$ $0.07677 \pm 0.0002445$ 1.5       150       50 $5.57786$ $0.5195 \pm 0.001577$ 1.5       150       50 $5.57786$ $0.5195 \pm 0.0001577$ 1.5       150       50 $5.57786$ $0.5195 \pm 0.0001577$ 1.5       150       50 $5.57786$ $0.5195 \pm 0.0006711$ 1.5       150       50 $67.2866$ $0.0139 \pm 6.13e-05$ 1.5       150       50 $67.2866$ $0.0139 \pm 6.13e-05$ 1.5       1500       50 $315.045$ $0.0002199 \pm 7.038e-06$ 1.5       1500       50 $315.045$ $0.0002$	1.5	200	10	17.6611	$0.2249 \pm 0.0008153$
1.5       1000       10       198.246 $0.001242 \pm 6.739e-06$ 1.5       1500       10       315.903 $0.0002157 \pm 8.805e-07$ 1.5       10       50 $0.000142452$ $0.01068 \pm 4.527e-05$ 1.5       20       50 $0.00157735$ $0.01093 \pm 6.079e-05$ 1.5       50       50 $0.00525498$ $0.01302 \pm 6.649e-05$ 1.5       100       50 $0.011079$ $0.07677 \pm 0.0002445$ 1.5       150       50 $5.57786$ $0.5195 \pm 0.000577$ 1.5       200       50 $11.6536$ $0.2195 \pm 0.0006711$ 1.5       300       50 $22.5508$ $0.07353 \pm 0.0003291$ 1.5       500       50 $67.2866$ $0.0139 \pm 6.13e-05$ 1.5       1000       50 $196.96$ $0.001209 \pm 7.038e-06$ 1.5       1500       50 $315.045$ $0.002109 \pm 8.631e-07$ 1.5       1500       50 $315.045$ $0.002109 \pm 7.038e-06$ 1.5       150       50 $0.011079$ $0.006295 \pm 3.608e-06$ 1.5       150       150 $0.011079$ $0$	1.5	300	10	26.7214	$0.07541 \pm 0.0002941$
1.5       1500       10       315.903 $0.0002157 \pm 8.805e-07$ 1.5       10       50 $0.000142452$ $0.01068 \pm 4.527e-05$ 1.5       20       50 $0.00157735$ $0.01093 \pm 6.079e-05$ 1.5       50       50 $0.00525498$ $0.01302 \pm 6.649e-05$ 1.5       100       50 $0.011079$ $0.07677 \pm 0.0002445$ 1.5       150       50 $5.57786$ $0.5195 \pm 0.000577$ 1.5       200       50 $11.6536$ $0.2195 \pm 0.0006711$ 1.5       300       50 $22.5508$ $0.07353 \pm 0.0003291$ 1.5       500       50 $67.2866$ $0.0139 \pm 6.13e-05$ 1.5       1000       50 $196.96$ $0.001209 \pm 7.038e-06$ 1.5       1500       50 $315.045$ $0.002109 \pm 8.631e-07$ 1.5       1500       50 $315.045$ $0.002109 \pm 8.631e-07$ 1.5       150       50 $0.011079$ $0.006295 \pm 3.008e-06$ 1.5       150       150 $0.011079$ $0.006295 \pm 3.608e-06$ 1.5       150       150 $0.0240529$ <t< td=""><td>1.5</td><td>500</td><td>10</td><td>69.8379</td><td><math>0.01447 \pm 6.923 \text{e-}05</math></td></t<>	1.5	500	10	69.8379	$0.01447 \pm 6.923 \text{e-}05$
1.5       10       50 $0.000142452$ $0.01068 \pm 4.527e-05$ 1.5       20       50 $0.00157735$ $0.0193 \pm 6.079e-05$ 1.5       50       50 $0.00525498$ $0.01302 \pm 6.649e-05$ 1.5       100       50 $0.011079$ $0.07677 \pm 0.0002445$ 1.5       150       50 $5.57786$ $0.5195 \pm 0.000577$ 1.5       200       50 $11.6536$ $0.2195 \pm 0.0006711$ 1.5       300       50 $22.5508$ $0.07353 \pm 0.0003291$ 1.5       500       50 $67.2866$ $0.0139 \pm 6.13e-05$ 1.5       1000       50 $196.96$ $0.001209 \pm 7.038e-06$ 1.5       1500       50 $315.045$ $0.002109 \pm 8.631e-05$ 1.5       1500       50 $315.045$ $0.002109 \pm 8.631e-05$ 1.5       150       150 $0.011079$ $0.006295 \pm 3.008e-06$ 1.5       150       150 $0.0172162$ $0.000706 \pm 3.661e-06$ 1.5       150       150 $0.0240529$ $0.00086 \pm 3.608e-06$ 1.5       300       150 $48.1013$ <	1.5	1000	10	198.246	$0.001242 \pm 6.739e-06$
1.5       20       50 $0.00157735$ $0.0193 \pm 6.079e-05$ 1.5       50       50 $0.00525498$ $0.01302 \pm 6.649e-05$ 1.5       100       50 $0.011079$ $0.07677 \pm 0.0002445$ 1.5       150       50 $5.57786$ $0.5195 \pm 0.000577$ 1.5       200       50 $11.6536$ $0.2195 \pm 0.0006711$ 1.5       300       50 $22.5508$ $0.07353 \pm 0.0003291$ 1.5       500       50 $67.2866$ $0.0139 \pm 6.13e-05$ 1.5       1000       50       196.96 $0.001209 \pm 7.038e-06$ 1.5       1500       50       315.045 $0.002109 \pm 8.631e-05$ 1.5       150       50       315.045 $0.002109 \pm 8.631e-05$ 1.5       150       150 $0.0172162$ $0.0002109 \pm 8.631e-06$ 1.5       150       150 $0.0172162$ $0.000706 \pm 3.661e-06$ 1.5       150       150 $0.0240529$ $0.0086 \pm 3.608e-06$ 1.5       300       150 $0.0428723$ $0.003751 \pm 1.304e-05$ 1.5       1500       150       307.963 $0.$	1.5	1500	10	315.903	$0.0002157 \pm 8.805$ e-07
1.55050 $0.00525498$ $0.01302 \pm 6.649e-05$ 1.5 $100$ $50$ $0.011079$ $0.07677 \pm 0.0002445$ 1.5 $150$ $50$ $5.57786$ $0.5195 \pm 0.001577$ 1.5 $200$ $50$ $11.6536$ $0.2195 \pm 0.0006711$ 1.5 $300$ $50$ $22.5508$ $0.07353 \pm 0.0003291$ 1.5 $500$ $50$ $67.2866$ $0.0139 \pm 6.13e-05$ 1.5 $1000$ $50$ $196.96$ $0.001209 \pm 7.038e-06$ 1.5 $1500$ $50$ $315.045$ $0.0002109 \pm 8.631e-07$ 1.5 $150$ $150$ $0.011079$ $0.0006295 \pm 3.008e-06$ 1.5 $150$ $150$ $0.0172162$ $0.000706 \pm 3.661e-06$ 1.5 $150$ $150$ $0.0240529$ $0.00086 \pm 3.608e-06$ 1.5 $300$ $150$ $0.0240529$ $0.00086 \pm 3.608e-06$ 1.5 $300$ $150$ $0.0428723$ $0.003751 \pm 1.304e-05$ 1.5 $1500$ $150$ $48.1013$ $0.01046 \pm 4.013e-05$ 1.5 $1500$ $150$ $307.963$ $0.001072 \pm 4.469e-06$ 1.5 $1500$ $150$ $307.963$ $0.0001931 \pm 1.022e-06$ 1.5 $1500$ $300$ $0.0240529$ $7.176e-05 \pm 3.641e-07$ 1.5 $300$ $300$ $0.0240529$ $7.176e-05 \pm 3.641e-07$ 1.5 $500$ $300$ $25.183$ $0.000155 \pm 6.658e-07$ 1.5 $1500$ $300$ $285.036$ $0.0001529 \pm 7.694e-07$ 1.5 $1500$ $500$ $285.036$ $0.000152$	1.5	10	50	0.000142452	$0.01068 \pm 4.527 e$ -05
1.510050 $0.011079$ $0.07677 \pm 0.0002445$ 1.515050 $5.57786$ $0.5195 \pm 0.001577$ 1.520050 $11.6536$ $0.2195 \pm 0.0006711$ 1.530050 $22.5508$ $0.07353 \pm 0.0003291$ 1.550050 $67.2866$ $0.0139 \pm 6.13e-05$ 1.5100050 $196.96$ $0.001209 \pm 7.038e-06$ 1.5150050 $315.045$ $0.0002109 \pm 8.631e-07$ 1.5100150 $0.011079$ $0.0006295 \pm 3.008e-06$ 1.5150150 $0.0172162$ $0.000706 \pm 3.661e-06$ 1.5200150 $0.0240529$ $0.00086 \pm 3.608e-06$ 1.5300150 $0.0428723$ $0.003751 \pm 1.304e-05$ 1.5500150 $48.1013$ $0.01046 \pm 4.013e-05$ 1.51000150 $186.49$ $0.001072 \pm 4.469e-06$ 1.51500150 $307.963$ $0.0001931 \pm 1.022e-06$ 1.5200300 $0.0240529$ $7.176e-05 \pm 3.641e-07$ 1.5300300 $0.0428723$ $8.3e-05 \pm 3.627e-07$ 1.5500300 $25.183$ $0.000155 \pm 6.658e-07$ 1.51500300 $285.036$ $0.0001529 \pm 7.694e-07$ 1.51500300 $285.036$ $0.0001529 \pm 7.694e-07$ 1.51500500 $237.259$ $8.736e-05 \pm 4.269e-07$ 1.51500500 $237.259$ $8.736e-05 \pm 4.268e-07$ 2.101 $1.49727$	1.5	20	50	0.00157735	$0.01093 \pm 6.079 e - 05$
1.515050 $5.57786$ $0.5195 \pm 0.001577$ 1.520050 $11.6536$ $0.2195 \pm 0.0006711$ 1.530050 $22.5508$ $0.07353 \pm 0.0003291$ 1.550050 $67.2866$ $0.0139 \pm 6.13e-05$ 1.5100050 $196.96$ $0.001209 \pm 7.038e-06$ 1.5150050 $315.045$ $0.0002109 \pm 8.631e-07$ 1.5100150 $0.011079$ $0.0006295 \pm 3.008e-06$ 1.5150150 $0.0172162$ $0.000706 \pm 3.661e-06$ 1.5200150 $0.0240529$ $0.00086 \pm 3.608e-06$ 1.5300150 $0.0428723$ $0.003751 \pm 1.304e-05$ 1.51000150 $48.1013$ $0.01046 \pm 4.013e-05$ 1.51000150 $186.49$ $0.001072 \pm 4.469e-06$ 1.51500150 $307.963$ $0.0001931 \pm 1.022e-06$ 1.5200300 $0.0240529$ $7.176e-05 \pm 3.641e-07$ 1.5300300 $0.0428723$ $8.3e-05 \pm 3.627e-07$ 1.5500300 $25.183$ $0.000155 \pm 6.658e-07$ 1.51000300 $154.611$ $0.0007234 \pm 2.773e-06$ 1.51500300 $285.036$ $0.0001529 \pm 7.694e-07$ 1.5500500 $25.183$ $9.099e-06 \pm 4.301e-08$ 1.51500500 $25.183$ $9.099e-06 \pm 4.301e-08$ 1.51500500 $237.259$ $8.736e-05 \pm 4.268e-07$ 2.101 $1.49727$ <td< td=""><td>1.5</td><td>50</td><td>50</td><td>0.00525498</td><td><math>0.01302 \pm 6.649e-05</math></td></td<>	1.5	50	50	0.00525498	$0.01302 \pm 6.649e-05$
1.520050 $11.6536$ $0.2195 \pm 0.0006711$ 1.530050 $22.5508$ $0.07353 \pm 0.0003291$ 1.550050 $67.2866$ $0.0139 \pm 6.13e-05$ 1.5100050 $196.96$ $0.001209 \pm 7.038e-06$ 1.5150050 $315.045$ $0.0002109 \pm 8.631e-07$ 1.5100150 $0.011079$ $0.0006295 \pm 3.008e-06$ 1.5150150 $0.0172162$ $0.000706 \pm 3.661e-06$ 1.5200150 $0.0240529$ $0.00086 \pm 3.608e-06$ 1.5300150 $0.0428723$ $0.003751 \pm 1.304e-05$ 1.5500150 $48.1013$ $0.01046 \pm 4.013e-05$ 1.51000150 $186.49$ $0.001072 \pm 4.469e-06$ 1.51500150 $307.963$ $0.0001931 \pm 1.022e-06$ 1.5200300 $0.0240529$ $7.176e-05 \pm 3.641e-07$ 1.5300300 $0.0428723$ $8.3e-05 \pm 3.627e-07$ 1.5500300 $25.183$ $0.000155 \pm 6.658e-07$ 1.51500300 $25.183$ $0.0001529 \pm 7.694e-07$ 1.5500500 $25.183$ $9.099e-06 \pm 4.301e-08$ 1.51500500 $25.183$ $9.099e-06 \pm 4.301e-08$ 1.51500500 $237.259$ $8.736e-05 \pm 2.699e-07$ 1.51500500 $237.259$ $8.736e-05 \pm 4.268e-07$ 2.101 $1.49727$ $82.65 \pm 0.3408$ 2.201 $3.13828$ $43.1 \pm$	1.5	100	50	0.011079	$0.07677 \pm 0.0002445$
1.53005022.5508 $0.07353 \pm 0.0003291$ 1.550050 $67.2866$ $0.0139 \pm 6.13e-05$ 1.5100050 $196.96$ $0.001209 \pm 7.038e-06$ 1.5150050 $315.045$ $0.0002109 \pm 8.631e-07$ 1.5100 $150$ $0.011079$ $0.0006295 \pm 3.008e-06$ 1.5150 $150$ $0.0172162$ $0.000706 \pm 3.661e-06$ 1.5200 $150$ $0.0240529$ $0.00086 \pm 3.608e-06$ 1.5300 $150$ $0.0428723$ $0.003751 \pm 1.304e-05$ 1.5500 $150$ $48.1013$ $0.01046 \pm 4.013e-05$ 1.51000 $150$ $186.49$ $0.001072 \pm 4.469e-06$ 1.51500 $150$ $307.963$ $0.0001931 \pm 1.022e-06$ 1.5200300 $0.0240529$ $7.176e-05 \pm 3.641e-07$ 1.5300300 $0.0428723$ $8.3e-05 \pm 3.627e-07$ 1.5500300 $25.183$ $0.000155 \pm 6.658e-07$ 1.51500300 $25.183$ $0.000155 \pm 6.658e-07$ 1.51500300 $25.183$ $0.0001529 \pm 7.694e-07$ 1.51500300 $285.036$ $0.0001529 \pm 7.694e-07$ 1.51500500 $25.183$ $9.099e-06 \pm 4.301e-08$ 1.51500500 $25.183$ $9.099e-06 \pm 4.301e-08$ 1.51500500 $237.259$ $8.736e-05 \pm 2.699e-07$ 1.51500500 $237.259$ $8.736e-05 \pm 4.268e-07$ 2.101<	1.5	150	50	5.57786	$0.5195 \pm 0.001577$
1.550050 $67.2866$ $0.0139 \pm 6.13e-05$ 1.5 $1000$ 50 $196.96$ $0.001209 \pm 7.038e-06$ 1.5 $1500$ 50 $315.045$ $0.0002109 \pm 8.631e-07$ 1.5 $100$ $150$ $0.011079$ $0.0006295 \pm 3.008e-06$ 1.5 $150$ $150$ $0.0172162$ $0.000706 \pm 3.661e-06$ 1.5 $200$ $150$ $0.0240529$ $0.00086 \pm 3.608e-06$ 1.5 $300$ $150$ $0.0428723$ $0.003751 \pm 1.304e-05$ 1.5 $500$ $150$ $48.1013$ $0.01046 \pm 4.013e-05$ 1.5 $1000$ $150$ $186.49$ $0.001072 \pm 4.469e-06$ 1.5 $1500$ $150$ $307.963$ $0.0001931 \pm 1.022e-06$ 1.5 $200$ $300$ $0.0240529$ $7.176e-05 \pm 3.641e-07$ 1.5 $300$ $300$ $0.0428723$ $8.3e-05 \pm 3.627e-07$ 1.5 $500$ $300$ $25.183$ $0.000155 \pm 6.658e-07$ 1.5 $1500$ $300$ $25.183$ $0.000155 \pm 6.658e-07$ 1.5 $1500$ $300$ $285.036$ $0.0001529 \pm 7.694e-07$ 1.5 $500$ $500$ $25.183$ $9.099e-06 \pm 4.301e-08$ 1.5 $1500$ $500$ $25.183$ $9.099e-06 \pm 4.301e-08$ 1.5 $1500$ $500$ $237.259$ $8.736e-05 \pm 2.699e-07$ 1.5 $1500$ $500$ $237.259$ $8.736e-05 \pm 4.268e-07$ 2. $10$ $1$ $1.49727$ $82.65 \pm 0.3408$ 2. $20$ $1$ $3.13828$ $43.1 \pm 0.1487$ <td>1.5</td> <td>200</td> <td>50</td> <td>11.6536</td> <td><math>0.2195 \pm 0.0006711</math></td>	1.5	200	50	11.6536	$0.2195 \pm 0.0006711$
1.5100050196.96 $0.001209 \pm 7.038e-06$ 1.5150050 $315.045$ $0.0002109 \pm 8.631e-07$ 1.5100150 $0.011079$ $0.0006295 \pm 3.008e-06$ 1.5150150 $0.0172162$ $0.000706 \pm 3.661e-06$ 1.5200150 $0.0240529$ $0.00086 \pm 3.608e-06$ 1.5300150 $0.0428723$ $0.003751 \pm 1.304e-05$ 1.5500150 $48.1013$ $0.01046 \pm 4.013e-05$ 1.51000150 $186.49$ $0.001072 \pm 4.469e-06$ 1.51500150 $307.963$ $0.0001931 \pm 1.022e-06$ 1.5200300 $0.0240529$ $7.176e-05 \pm 3.641e-07$ 1.5300300 $0.0428723$ $8.3e-05 \pm 3.627e-07$ 1.5500300 $25.183$ $0.000155 \pm 6.658e-07$ 1.51500300 $285.036$ $0.0001529 \pm 7.694e-07$ 1.51500300 $285.036$ $0.0001529 \pm 7.694e-07$ 1.51500500 $25.183$ $9.099e-06 \pm 4.301e-08$ 1.51500500 $25.183$ $9.099e-06 \pm 4.301e-08$ 1.51500500 $237.259$ $8.736e-05 \pm 4.268e-07$ 2.101 $1.49727$ $82.65 \pm 0.3408$ 2.201 $3.13828$ $43.1 \pm 0.1487$	1.5	300	50	22.5508	$0.07353 \pm 0.0003291$
1.5150050315.045 $0.0002109 \pm 8.631e-07$ 1.5100150 $0.011079$ $0.0006295 \pm 3.008e-06$ 1.5150150 $0.0172162$ $0.000706 \pm 3.661e-06$ 1.5200150 $0.0240529$ $0.00086 \pm 3.608e-06$ 1.5300150 $0.0428723$ $0.003751 \pm 1.304e-05$ 1.5500150 $48.1013$ $0.01046 \pm 4.013e-05$ 1.51000150 $186.49$ $0.001072 \pm 4.469e-06$ 1.51500150 $307.963$ $0.0001931 \pm 1.022e-06$ 1.5200300 $0.0240529$ $7.176e-05 \pm 3.641e-07$ 1.5300300 $0.0428723$ $8.3e-05 \pm 3.627e-07$ 1.5500300 $25.183$ $0.000155 \pm 6.658e-07$ 1.51500300 $25.183$ $0.000155 \pm 6.658e-07$ 1.51500300 $285.036$ $0.0001529 \pm 7.694e-07$ 1.5500500 $25.183$ $9.099e-06 \pm 4.301e-08$ 1.51000500 $108.775$ $5.335e-05 \pm 2.699e-07$ 1.51500500 $237.259$ $8.736e-05 \pm 4.268e-07$ 2.101 $1.49727$ $82.65 \pm 0.3408$ 2.201 $3.13828$ $43.1 \pm 0.1487$	1.5	500	50	67.2866	$0.0139 \pm 6.13e-05$
1.51001500.0110790.0006295 $\pm$ 3.008e-061.51501500.01721620.000706 $\pm$ 3.661e-061.52001500.02405290.00086 $\pm$ 3.608e-061.53001500.04287230.003751 $\pm$ 1.304e-051.550015048.10130.01046 $\pm$ 4.013e-051.51000150186.490.001072 $\pm$ 4.469e-061.51500150307.9630.0001931 $\pm$ 1.022e-061.52003000.02405297.176e-05 $\pm$ 3.641e-071.53003000.04287238.3e-05 $\pm$ 3.627e-071.550030025.1830.000155 $\pm$ 6.658e-071.51000300154.6110.0007234 $\pm$ 2.773e-061.51500300285.0360.0001529 $\pm$ 7.694e-071.550050025.1839.099e-06 $\pm$ 4.301e-081.51000500108.7755.335e-05 $\pm$ 2.699e-071.51500500237.2598.736e-05 $\pm$ 4.268e-072.1011.4972782.65 $\pm$ 0.34082.2013.1382843.1 $\pm$ 0.1487	1.5	1000	50	196.96	$0.001209 \pm 7.038e-06$
1.51501500.01721620.000706 $\pm$ 3.661e-061.52001500.02405290.00086 $\pm$ 3.608e-061.53001500.04287230.003751 $\pm$ 1.304e-051.550015048.10130.01046 $\pm$ 4.013e-051.51000150186.490.001072 $\pm$ 4.469e-061.51500150307.9630.0001931 $\pm$ 1.022e-061.52003000.02405297.176e-05 $\pm$ 3.641e-071.53003000.04287238.3e-05 $\pm$ 3.627e-071.550030025.1830.000155 $\pm$ 6.658e-071.51000300154.6110.0007234 $\pm$ 2.773e-061.51500300285.0360.0001529 $\pm$ 7.694e-071.550050025.1839.099e-06 $\pm$ 4.301e-081.51000500108.7755.335e-05 $\pm$ 2.699e-071.51500500237.2598.736e-05 $\pm$ 4.268e-072.1011.4972782.65 $\pm$ 0.34082.2013.1382843.1 $\pm$ 0.1487	1.5	1500	50	315.045	$0.0002109 \pm 8.631e-07$
1.52001500.02405290.00086 $\pm$ 3.608e-061.53001500.04287230.003751 $\pm$ 1.304e-051.550015048.10130.01046 $\pm$ 4.013e-051.51000150186.490.001072 $\pm$ 4.469e-061.51500150307.9630.0001931 $\pm$ 1.022e-061.52003000.02405297.176e-05 $\pm$ 3.641e-071.53003000.04287238.3e-05 $\pm$ 3.627e-071.550030025.1830.000155 $\pm$ 6.658e-071.51000300154.6110.0007234 $\pm$ 2.773e-061.51500300285.0360.0001529 $\pm$ 7.694e-071.550050025.1839.099e-06 $\pm$ 4.301e-081.51000500108.7755.335e-05 $\pm$ 2.699e-071.51500500237.2598.736e-05 $\pm$ 4.268e-072.1011.4972782.65 $\pm$ 0.34082.2013.1382843.1 $\pm$ 0.1487	1.5	100	150	0.011079	$0.0006295 \pm 3.008e-06$
1.53001500.04287230.003751 $\pm$ 1.304e-051.550015048.10130.01046 $\pm$ 4.013e-051.51000150186.490.001072 $\pm$ 4.469e-061.51500150307.9630.0001931 $\pm$ 1.022e-061.52003000.02405297.176e-05 $\pm$ 3.641e-071.53003000.04287238.3e-05 $\pm$ 3.627e-071.550030025.1830.000155 $\pm$ 6.658e-071.51000300154.6110.0007234 $\pm$ 2.773e-061.51500300285.0360.0001529 $\pm$ 7.694e-071.550050025.1839.099e-06 $\pm$ 4.301e-081.51000500108.7755.335e-05 $\pm$ 2.699e-071.51500500237.2598.736e-05 $\pm$ 4.268e-072.1011.4972782.65 $\pm$ 0.34082.2013.1382843.1 $\pm$ 0.1487	1.5	150	150	0.0172162	$0.000706 \pm 3.661e-06$
1.5500150 $48.1013$ $0.01046 \pm 4.013e-05$ 1.51000150 $186.49$ $0.001072 \pm 4.469e-06$ 1.51500150 $307.963$ $0.0001931 \pm 1.022e-06$ 1.5200300 $0.0240529$ $7.176e-05 \pm 3.641e-07$ 1.5300300 $0.0428723$ $8.3e-05 \pm 3.627e-07$ 1.5500300 $25.183$ $0.000155 \pm 6.658e-07$ 1.51000300 $154.611$ $0.0007234 \pm 2.773e-06$ 1.51500300 $285.036$ $0.0001529 \pm 7.694e-07$ 1.5500500 $25.183$ $9.099e-06 \pm 4.301e-08$ 1.51000500 $108.775$ $5.335e-05 \pm 2.699e-07$ 1.51500500 $237.259$ $8.736e-05 \pm 4.268e-07$ 2.101 $1.49727$ $82.65 \pm 0.3408$ 2.201 $3.13828$ $43.1 \pm 0.1487$	1.5	200	150	0.0240529	$0.00086 \pm 3.608 e\text{-}06$
1.51000150186.49 $0.001072 \pm 4.469e-06$ 1.51500150 $307.963$ $0.0001931 \pm 1.022e-06$ 1.5200300 $0.0240529$ $7.176e-05 \pm 3.641e-07$ 1.5300300 $0.0428723$ $0.000155 \pm 6.658e-07$ 1.5500300 $25.183$ $0.000155 \pm 6.658e-07$ 1.51000300 $154.611$ $0.0007234 \pm 2.773e-06$ 1.51500300 $285.036$ $0.0001529 \pm 7.694e-07$ 1.5500500 $25.183$ $9.099e-06 \pm 4.301e-08$ 1.51000500 $108.775$ $5.335e-05 \pm 2.699e-07$ 1.51500500 $237.259$ $8.736e-05 \pm 4.268e-07$ 2.101 $1.49727$ $82.65 \pm 0.3408$ 2.201 $3.13828$ $43.1 \pm 0.1487$	1.5	300	150	0.0428723	$0.003751 \pm 1.304e-05$
1.51500150307.9630.0001931 $\pm$ 1.022e-061.52003000.0240529 $7.176e-05 \pm 3.641e-07$ 1.53003000.0428723 $8.3e-05 \pm 3.627e-07$ 1.550030025.1830.000155 $\pm$ 6.658e-071.51000300154.6110.0007234 $\pm$ 2.773e-061.51500300285.0360.0001529 $\pm$ 7.694e-071.550050025.1839.099e-06 $\pm$ 4.301e-081.51000500108.7755.335e-05 $\pm$ 2.699e-071.51500500237.2598.736e-05 $\pm$ 4.268e-072.1011.4972782.65 $\pm$ 0.34082.2013.1382843.1 $\pm$ 0.1487	1.5	500	150	48.1013	$0.01046 \pm 4.013e-05$
1.52003000.0240529 $7.176e-05 \pm 3.641e-07$ 1.53003000.0428723 $8.3e-05 \pm 3.627e-07$ 1.5500300 $25.183$ 0.000155 $\pm 6.658e-07$ 1.51000300 $154.611$ 0.0007234 $\pm 2.773e-06$ 1.51500300 $285.036$ 0.0001529 $\pm 7.694e-07$ 1.5500500 $25.183$ 9.099e-06 $\pm 4.301e-08$ 1.51000500 $108.775$ $5.335e-05 \pm 2.699e-07$ 1.51500500 $237.259$ $8.736e-05 \pm 4.268e-07$ 2.101 $1.49727$ $82.65 \pm 0.3408$ 2.201 $3.13828$ $43.1 \pm 0.1487$	1.5	1000	150	186.49	$0.001072 \pm 4.469e-06$
1.53003000.04287238.3e-05 $\pm$ 3.627e-071.550030025.1830.000155 $\pm$ 6.658e-071.51000300154.6110.0007234 $\pm$ 2.773e-061.51500300285.0360.0001529 $\pm$ 7.694e-071.550050025.1839.099e-06 $\pm$ 4.301e-081.51000500108.7755.335e-05 $\pm$ 2.699e-071.51500500237.2598.736e-05 $\pm$ 4.268e-072.1011.4972782.65 $\pm$ 0.34082.2013.1382843.1 $\pm$ 0.1487	1.5	1500	150	307.963	$0.0001931 \pm 1.022e-06$
1.550030025.1830.000155 $\pm$ 6.658e-071.51000300154.6110.0007234 $\pm$ 2.773e-061.51500300285.0360.0001529 $\pm$ 7.694e-071.550050025.1839.099e-06 $\pm$ 4.301e-081.51000500108.7755.335e-05 $\pm$ 2.699e-071.51500500237.2598.736e-05 $\pm$ 4.268e-072.1011.4972782.65 $\pm$ 0.34082.2013.1382843.1 $\pm$ 0.1487	1.5	200	300		$7.176e-05 \pm 3.641e-07$
1.51000300154.6110.0007234 $\pm$ 2.773e-061.51500300285.0360.0001529 $\pm$ 7.694e-071.550050025.1839.099e-06 $\pm$ 4.301e-081.51000500108.7755.335e-05 $\pm$ 2.699e-071.51500500237.2598.736e-05 $\pm$ 4.268e-072.1011.4972782.65 $\pm$ 0.34082.2013.1382843.1 $\pm$ 0.1487	1.5	300	300	0.0428723	$8.3e-05 \pm 3.627e-07$
1.51500300285.0360.0001529 $\pm$ 7.694e-071.550050025.1839.099e-06 $\pm$ 4.301e-081.51000500 $108.775$ 5.335e-05 $\pm$ 2.699e-071.51500500 $237.259$ $8.736e$ -05 $\pm$ 4.268e-072.101 $1.49727$ $82.65 \pm 0.3408$ 2.201 $3.13828$ $43.1 \pm 0.1487$	1.5	500	300	25.183	$0.000155 \pm 6.658e-07$
1.550050025.1839.099e-06 $\pm$ 4.301e-081.51000500 $108.775$ 5.335e-05 $\pm$ 2.699e-071.51500500 $237.259$ $8.736e-05 \pm 4.268e-07$ 2.101 $1.49727$ $82.65 \pm 0.3408$ 2.201 $3.13828$ $43.1 \pm 0.1487$	1.5	1000	300	154.611	$0.0007234 \pm 2.773e-06$
1.51000500 $108.775$ $5.335e-05 \pm 2.699e-07$ 1.51500500 $237.259$ $8.736e-05 \pm 4.268e-07$ 2.101 $1.49727$ $82.65 \pm 0.3408$ 2.201 $3.13828$ $43.1 \pm 0.1487$	1.5	1500	300	285.036	$0.0001529 \pm 7.694e$ -07
1.51500500237.2598.736e-05 $\pm$ 4.268e-072.1011.4972782.65 $\pm$ 0.34082.2013.1382843.1 $\pm$ 0.1487	1.5	500	500	25.183	$9.099e-06 \pm 4.301e-08$
2. 10 1 1.49727 82.65 $\pm$ 0.3408 2. 20 1 3.13828 43.1 $\pm$ 0.1487	1.5	1000	500	108.775	$5.335e-05 \pm 2.699e-07$
2. 20 1 $3.13828$ $43.1 \pm 0.1487$	1.5	1500	500	237.259	$8.736\text{e-}05 \pm 4.268\text{e-}07$
	2.	10	1	1.49727	$82.65 \pm 0.3408$
2. 50 1 7.948 11.84 $\pm$ 0.04278	2.	20	1	3.13828	$43.1 \pm 0.1487$
<u> </u>	2.	50	1	7.948	$11.84 \pm 0.04278$

Table C.1 – continued from previous page

Coupling (g)	$m_{Phi}$ [GeV]	$m_{\chi}$ [GeV]	$\Gamma_{min}$ [GeV]	$\sigma$
2.	100	1	15.9256	$2.712 \pm 0.01209$
2.	150	1	23.8975	$0.9056 \pm 0.004237$
2.	200	1	31.869	$0.3952 \pm 0.001653$
2.	300	1	47.8195	$0.132 \pm 0.0004713$
2.	500	1	124.345	$0.02461 \pm 0.0001101$
2.	1000	1	352.532	$0.002071 \pm 1.061e-05$
2.	1500	1	561.669	$0.0003815 \pm 1.4e-06$
2.	10	10	0.000253248	$1.627 \pm 0.005672$
2.	20	10	0.00280417	$5.528 \pm 0.03152$
2.	50	10	6.13579	$11.98 \pm 0.04005$
2.	100	10	14.9899	$2.696 \pm 0.01091$
2.	150	10	23.2701	$0.8981 \pm 0.004067$
2.	200	10	31.3975	$0.3921 \pm 0.001675$
2.	300	10	47.5047	$0.1312 \pm 0.0005524$
2.	500	10	124.156	$0.02454 \pm 0.0001302$
2.	1000	10	352.437	$0.002051 \pm 9.73e-06$
2.	1500	10	561.606	$0.0003797 \pm 1.522e-06$
2.	10	50	0.000253248	$0.03397 \pm 0.0001354$
2.	20	50	0.00280417	$0.03452 \pm 0.0001623$
2.	50	50	0.00934219	$0.04088 \pm 0.0001623$
2.	100	50	0.0196961	$0.24 \pm 0.0008579$
2.	150	50	9.9162	$0.8991 \pm 0.002903$
2.	200	50	20.7176	$0.382 \pm 0.001411$
2.	300	50	40.0903	$0.1287 \pm 0.0005596$
2.	500	50	119.621	$0.02328 \pm 0.0001255$
2.	1000	50	350.151	$0.001995 \pm 1.184e-05$
2.	1500	50	560.08	$0.0003671 \pm 1.741e-06$
2.	10	150	0.000253248	$0.001822 \pm 7.946e-06$
2.	20	150	0.00280417	$0.001842 \pm 8.453e-06$
2.	50	150	0.00934219	$0.00187 \pm 8.818 \text{e-}06$
2.	100	150	0.0196961	$0.001985 \pm 8.101$ e-06
2.	150	150	0.0306067	$0.002231 \pm 1.131e-05$
2.	200	150	0.0427607	$0.002694 \pm 1.215 e\text{-}05$
2.	300	150	0.0762174	$0.01186 \pm 4.862e-05$
2.	500	150	85.5134	$0.01769 \pm 8.02e-05$
2.	1000	150	331.538	$0.001716 \pm 7.617e-06$
2.	1500	150	547.49	$0.0003242 \pm 1.537e-06$
2.	100	300	0.0196961	$0.0002092 \pm 8.197e-07$
2.	150	300	0.0306067	$0.0002152 \pm 8.37e-07$
2.	200	300	0.0427607	0.0002275 ± 8.607e-07

Table C.1 – continued from previous page

$\begin{array}{cccccccccccccccccccccccccccccccccccc$	Coupling (g)	$m_{Phi}$ [GeV]		$\Gamma_{min}$ [GeV]	$\sigma$
2.	2.	300	300	0.0762174	0.0002609 ± 1.05e-06
2.	2.	500	300	44.7698	$0.0004931 \pm 2.01e-06$
2.	2.	1000	300		$0.001119 \pm 5.167e-06$
2.         500         500         44.7698 $2.871e-05 \pm 1.09e-07$ 2.         1000         500         193.378 $0.000131 \pm 5.569e-07$ 2.         1500         500         421.793 $0.0001323 \pm 5.222e-07$ 2.5         10         1 $2.33949$ $128.4 \pm 0.4393$ 2.5         20         1 $4.90356$ $65.92 \pm 0.2248$ 2.5         50         1 $12.4187$ $17.77 \pm 0.0663$ 2.5         100         1 $24.8838$ $4.051 \pm 0.01562$ 2.5         150         1 $37.3398$ $1.364 \pm 0.004927$ 2.5         200         1 $49.7953$ $0.6008 \pm 0.002928$ 2.5         300         1 $74.718$ $0.2036 \pm 0.000894$ 2.5         500         1 $194.29$ $0.03629 \pm 0.0001865$ 2.5         1000         1 $550.831$ $0.00218 \pm 1.235e-05$ 2.5         1000         1 $877.608$ $0.0005639 \pm 2.327e-06$ 2.5         10         10 $0.0003957$ $3.918 \pm 0.0159$ 2.5 </td <td>2.</td> <td>1500</td> <td>300</td> <td></td> <td><math>0.0002432 \pm 1.053e-06</math></td>	2.	1500	300		$0.0002432 \pm 1.053e-06$
2.         1000         500         193.378 $0.000131 \pm 5.569e-07$ 2.         1500         500 $421.793$ $0.0001323 \pm 5.222e-07$ 2.5         10         1 $2.33949$ $128.4 \pm 0.4393$ 2.5         20         1 $4.90356$ $65.92 \pm 0.2248$ 2.5         50         1 $12.4187$ $17.77 \pm 0.0663$ 2.5         100         1 $24.8838$ $4.051 \pm 0.01562$ 2.5         150         1 $37.3398$ $1.364 \pm 0.004927$ 2.5         200         1 $49.7953$ $0.6008 \pm 0.002928$ 2.5         300         1 $74.718$ $0.2036 \pm 0.000894$ 2.5         300         1 $74.718$ $0.2036 \pm 0.000894$ 2.5         500         1 $194.29$ $0.03629 \pm 0.0001865$ 2.5         1500         1 $877.608$ $0.000539 \pm 0.0001865$ 2.5         1500         1 $877.608$ $0.000539 \pm 2.327e-06$ 2.5         10         10 $0.00438152$ $13.54 \pm 0.05349$ 2.5<	2.	300	500	0.0762174	2.367e-05 ± 1.206e-07
2.         1000         500         193.378 $0.000131 \pm 5.569e-07$ 2.         1500         500 $421.793$ $0.0001323 \pm 5.222e-07$ 2.5         10         1 $2.33949$ $128.4 \pm 0.4393$ 2.5         20         1 $4.90356$ $65.92 \pm 0.2248$ 2.5         50         1 $12.4187$ $17.77 \pm 0.0663$ 2.5         100         1 $24.8838$ $4.051 \pm 0.01562$ 2.5         150         1 $37.3398$ $1.364 \pm 0.004927$ 2.5         200         1 $49.7953$ $0.6008 \pm 0.002928$ 2.5         300         1 $74.718$ $0.2036 \pm 0.0008994$ 2.5         500         1 $194.29$ $0.03629 \pm 0.0001865$ 2.5         500         1 $194.29$ $0.03629 \pm 0.0001865$ 2.5         1500         1 $877.608$ $0.000539 \pm 2.327e-05$ 2.5         1500         1 $877.608$ $0.000539 \pm 2.327e-05$ 2.5         10         10 $0.00438152$ $13.54 \pm 0.05349$ 2	2.	500	500	44.7698	$2.871e-05 \pm 1.09e-07$
2. $1500$ $500$ $421.793$ $0.0001323 \pm 5.222e-07$ 2.5 $10$ $1$ $2.33949$ $128.4 \pm 0.4393$ 2.5 $20$ $1$ $4.90356$ $65.92 \pm 0.2248$ 2.5 $50$ $1$ $12.4187$ $17.77 \pm 0.0663$ 2.5 $100$ $1$ $24.8838$ $4.051 \pm 0.01562$ 2.5 $150$ $1$ $37.3398$ $1.364 \pm 0.004927$ 2.5 $200$ $1$ $49.7953$ $0.6008 \pm 0.002928$ 2.5 $300$ $1$ $74.718$ $0.2036 \pm 0.0008994$ 2.5 $500$ $1$ $194.29$ $0.03629 \pm 0.0001865$ 2.5 $500$ $1$ $194.29$ $0.03629 \pm 0.0001865$ 2.5 $1500$ $1$ $877.608$ $0.002918 \pm 1.2350-05$ 2.5 $1500$ $1$ $877.608$ $0.0025639 \pm 2.3270-06$ 2.5 $150$ $1$ $0.002357$ $3.918 \pm 0.0159$ 2.5 $1$ $0.002357$ $0.01458$	2.	1000	500		$0.000131 \pm 5.569e-07$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	2.	1500	500	421.793	$0.0001323 \pm 5.222e-07$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	2.5	10	1	2.33949	$128.4 \pm 0.4393$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	2.5	20	1	4.90356	$65.92 \pm 0.2248$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	2.5	50	1	12.4187	$17.77 \pm 0.0663$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	2.5	100	1	24.8838	$4.051 \pm 0.01562$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	2.5	150	1	37.3398	$1.364 \pm 0.004927$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	2.5	200	1	49.7953	$0.6008 \pm 0.002928$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	2.5	300	1	74.718	$0.2036 \pm 0.0008994$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	2.5	500	1	194.29	$0.03629 \pm 0.0001865$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	2.5	1000	1	550.831	$0.002918 \pm 1.235 e$ -05
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	2.5	1500	1	877.608	$0.0005639 \pm 2.327e-06$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	2.5	10	10	0.0003957	$3.918 \pm 0.0159$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	2.5	20	10	0.00438152	$13.54 \pm 0.05349$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	2.5	50	10	9.58718	$18.03 \pm 0.06068$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	2.5	100	10	23.4217	$4.025 \pm 0.01458$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	2.5	150	10	36.3595	$1.36 \pm 0.00698$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	2.5	200	10	49.0586	$0.5979 \pm 0.002445$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	2.5	300	10	74.2262	$0.2016 \pm 0.0006995$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	2.5	500	10	193.994	$0.03579 \pm 0.0001738$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	2.5	1000	10	550.683	$0.002902 \pm 1.515 e\text{-}05$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	2.5	1500	10	877.509	$0.0005651 \pm 2.275e-06$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	2.5	10	50	0.0003957	$0.08298 \pm 0.000365$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	2.5	20	50	0.00438152	$0.08474 \pm 0.0003631$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	2.5	50	50	0.0145972	$0.09986 \pm 0.000455$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	2.5	100	50	0.0307751	$0.5855 \pm 0.001667$
2.530050 $62.6411$ $0.1938 \pm 0.0008665$ 2.550050 $186.907$ $0.03384 \pm 0.0001589$ 2.5100050 $547.111$ $0.002773 \pm 1.645e-05$ 2.5150050 $875.125$ $0.0005349 \pm 3.534e-06$ 2.510150 $0.0003957$ $0.004461 \pm 1.951e-05$	2.5	150	50	15.4941	$1.359 \pm 0.005802$
2.550050 $186.907$ $0.03384 \pm 0.0001589$ 2.5100050 $547.111$ $0.002773 \pm 1.645e-05$ 2.5150050 $875.125$ $0.0005349 \pm 3.534e-06$ 2.510150 $0.0003957$ $0.004461 \pm 1.951e-05$	2.5	200	50	32.3712	$0.5728 \pm 0.002188$
2.5100050547.111 $0.002773 \pm 1.645e\text{-}05$ 2.5150050875.125 $0.0005349 \pm 3.534e\text{-}06$ 2.510150 $0.0003957$ $0.004461 \pm 1.951e\text{-}05$	2.5	300	50		$0.1938 \pm 0.0008665$
2.5 1500 50 875.125 0.0005349 $\pm$ 3.534e-06 2.5 10 150 0.0003957 0.004461 $\pm$ 1.951e-05	2.5	500	50		$0.03384 \pm 0.0001589$
2.5 10 150 0.0003957 0.004461 $\pm$ 1.951e-05	2.5	1000	50	547.111	$0.002773 \pm 1.645 e - 05$
	2.5	1500	50	875.125	$0.0005349 \pm 3.534e\text{-}06$
2.5 20 150 0.00438152 0.004473 $\pm$ 2.159e-05	2.5	10	150	0.0003957	$0.004461 \pm 1.951e-05$
	2.5	20	150	0.00438152	$0.004473 \pm 2.159e-05$

Table C.1 – continued from previous page

Coupling (g)	$m_{Phi}$ [GeV]	$m_{\chi}$ [GeV]	$\Gamma_{min}$ [GeV]	$\sigma$
2.5	50	150	0.0145972	$0.00451 \pm 1.808 e - 05$
2.5	100	150	0.0307751	$0.00486 \pm 1.984 e\text{-}05$
2.5	150	150	0.0478229	$0.00548 \pm 2.35 \text{e-}05$
2.5	200	150	0.0668136	$0.006545 \pm 2.81\text{e-}05$
2.5	300	150	0.11909	$0.02878 \pm 0.0001168$
2.5	500	150	133.615	$0.02572 \pm 0.00011$
2.5	1000	150	518.027	$0.002339 \pm 1.101e\text{-}05$
2.5	1500	150	855.453	$0.0004622 \pm 2.297e-06$
2.5	100	300	0.0307751	$0.0005104 \pm 2.62e-06$
2.5	150	300	0.0478229	$0.000526 \pm 2.091e$ -06
2.5	200	300	0.0668136	$0.0005503 \pm 2.402e-06$
2.5	300	300	0.11909	$0.0006368 \pm 2.911e\text{-}06$
2.5	500	300	69.9528	$0.001197 \pm 4.697 e$ -06
2.5	1000	300	429.476	$0.001499 \pm 6.445 e$ -06
2.5	1500	300	791.767	$0.0003277 \pm 1.439e-06$
2.5	300	500	0.11909	$5.773$ e-05 $\pm$ 2.645e-07
2.5	500	500	69.9528	$6.973e-05 \pm 3.037e-07$
2.5	1000	500	302.152	$0.0002498 \pm 1.042e$ -06
2.5	1500	500	659.052	$0.000172 \pm 8.531e-07$
3.	10	1	3.36886	$185.9 \pm 0.8608$
3.	20	1	7.06112	$92.49 \pm 0.3581$
3.	50	1	17.883	$24.38 \pm 0.08507$
3.	100	1	35.8327	$5.551 \pm 0.02275$
3.	150	1	53.7693	$1.878 \pm 0.008801$
3.	200	1	71.7052	$0.8398 \pm 0.004651$
3.	300	1	107.594	$0.2856 \pm 0.001301$
3.	500	1	279.777	$0.04861 \pm 0.0002143$
3.	1000	1	793.196	$0.003716 \pm 1.874e-05$
3.	1500	1	1263.76	$0.0007294 \pm 3.217e-06$
3.	10	10	0.000569808	$8.181 \pm 0.03184$
3.	20	10	0.00630938	$28.05 \pm 0.09412$
3.	50	10	13.8055	$24.97 \pm 0.07128$
3.	100	10	33.7272	$5.485 \pm 0.01916$
3.	150	10	52.3576	$1.858 \pm 0.007406$
3.	200	10	70.6443	$0.8336 \pm 0.003435$
3.	300	10	106.886	$0.2832 \pm 0.001293$
3.	500	10	279.352	$0.04802 \pm 0.0003129$
3.	1000	10	792.983	$0.003669 \pm 1.542e-05$
3.	1500	10	1263.61	$0.0007221 \pm 3.036e-06$
3.	10	50	0.000569808	$0.1714 \pm 0.0007653$

Table C.1 – continued from previous page

Coupling (g)	$m_{Phi}$ [GeV]		$\Gamma_{min}$ [GeV]	$\sigma$
3.	20	50	0.00630938	$0.1751 \pm 0.000689$
3.	50	50	0.0210199	$0.2073 \pm 0.001019$
3.	100	50	0.0443162	$1.21 \pm 0.003153$
3.	150	50	22.3114	$1.896 \pm 0.007571$
3.	200	50	46.6146	$0.787 \pm 0.002939$
3.	300	50	90.2031	$0.2685 \pm 0.001344$
3.	500	50	269.146	$0.04468 \pm 0.0002221$
3.	1000	50	787.84	$0.003505 \pm 1.861e-05$
3.	1500	50	1260.18	$0.0006823 \pm 3.857 e\text{-}06$
3.	10	150	0.000569808	$0.009285 \pm 4.234e-05$
3.	20	150	0.00630938	$0.00924 \pm 4.234e-05$
3.	50	150	0.0210199	$0.009462 \pm 3.85 \text{e-}05$
3.	100	150	0.0443162	$0.01017 \pm 4.443e-05$
3.	150	150	0.068865	$0.01124 \pm 5.221e$ -05
3.	200	150	0.0962116	$0.01366 \pm 6.834 \text{e-}05$
3.	300	150	0.171489	$0.05937 \pm 0.0002495$
3.	500	150	192.405	$0.03448 \pm 0.0001467$
3.	1000	150	745.959	$0.00288 \pm 1.359 \mathrm{e}\text{-}05$
3.	1500	150	1231.85	$0.0005735 \pm 3.925 e\text{-}06$
3.	50	300	0.0210199	$0.001039 \pm 3.982e-06$
3.	100	300	0.0443162	$0.001056 \pm 4.834e-06$
3.	150	300	0.068865	$0.001096 \pm 4.922e$ -06
3.	200	300	0.0962116	$0.001147 \pm 5.869 e$ -06
3.	300	300	0.171489	$0.001327 \pm 6.728 \text{e-}06$
3.	500	300	100.732	$0.00245 \pm 9.636$ e-06
3.	1000	300	618.446	$0.001853 \pm 7.863$ e-06
3.	1500	300	1140.14	$0.0003934 \pm 2.083e-06$
3.	150	500	0.068865	$0.0001123 \pm 4.327e-07$
3.	200	500	0.0962116	$0.000114 \pm 5.127e-07$
3.	300	500	0.171489	$0.0001206 \pm 5.124$ e-07
3.	500	500	100.732	$0.0001447 \pm 6.102e$ -07
3.	1000	500	435.099	$0.0004016 \pm 1.656$ e-06
3.	1500	500	949.035	$0.0002061 \pm 8.548 e$ -07
3.5	10	1	4.58539	$257.5 \pm 0.9241$
3.5	20	1	9.61097	$123.8 \pm 0.4645$
3.5	50	1	24.3407	$31.59 \pm 0.09614$
3.5	100	1	48.7723	$7.04 \pm 0.02954$
3.5	150	1	73.186	$2.417 \pm 0.01038$
3.5	200	1	97.5987	$1.089 \pm 0.004308$
3.5	300	1	146.447	$0.3709 \pm 0.001616$
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Table C.1 – continued from previous page

Coupling (g)	$m_{Phi}$ [GeV]		$\Gamma_{min}$ [GeV]	$\sigma$
3.5	500	1	380.808	$0.06035 \pm 0.0003762$
3.5	1000	1	1079.63	0.004345 $\pm$ 2.711e-05
3.5	1500	1	1720.11	$0.0008581 \pm 3.653e-06$
3.5	10	10	0.000775572	$15.08 \pm 0.0569$
3.5	20	10	0.00858777	$51.42 \pm 0.1478$
3.5	50	10	18.7909	$32.56 \pm 0.1113$
3.5	100	10	45.9065	$6.963 \pm 0.03199$
3.5	150	10	71.2646	$2.38 \pm 0.009493$
3.5	200	10	96.1548	$1.079 \pm 0.004244$
3.5	300	10	145.483	$0.369 \pm 0.001602$
3.5	500	10	380.229	$0.05978 \pm 0.0003017$
3.5	1000	10	1079.34	$0.004302 \pm 2.412e-05$
3.5	1500	10	1719.92	$0.0008525 \pm 3.878e-06$
3.5	10	50	0.000775572	$0.3176 \pm 0.001314$
3.5	20	50	0.00858777	$0.3229 \pm 0.001215$
3.5	50	50	0.0286105	$0.3857 \pm 0.001618$
3.5	100	50	0.0603192	$2.228 \pm 0.00751$
3.5	150	50	30.3684	$2.477 \pm 0.008787$
3.5	200	50	63.4476	$1.025 \pm 0.003864$
3.5	300	50	122.776	$0.3483 \pm 0.001614$
3.5	500	50	366.338	$0.05534 \pm 0.0003035$
3.5	1000	50	1072.34	$0.004076 \pm 2.371e-05$
3.5	1500	50	1715.24	$0.0008077 \pm 4.889e-06$
3.5	10	150	0.000775572	$0.01719 \pm 9.115 e$ -05
3.5	20	150	0.00858777	$0.01719 \pm 8.334e-05$
3.5	50	150	0.0286105	$0.01754 \pm 8.239e-05$
3.5	100	150	0.0603192	$0.01855 \pm 8.371e-05$
3.5	150	150	0.0937329	$0.02099 \pm 0.0001038$
3.5	200	150	0.130955	$0.0252 \pm 0.0001138$
3.5	300	150	0.233416	$0.1096 \pm 0.0006465$
3.5	500	150	261.885	$0.04374 \pm 0.0002091$
3.5	1000	150	1015.33	$0.00334 \pm 1.751e-05$
3.5	1500	150	1676.69	$0.0006583 \pm 3.614e-06$
3.5	10	300	0.000775572	$0.001925 \pm 9.279 \text{e-}06$
3.5	20	300	0.00858777	$0.001916 \pm 1.026$ e-05
3.5	50	300	0.0286105	$0.001918 \pm 8.166$ e-06
3.5	100	300	0.0603192	$0.001958 \pm 7.426$ e-06
3.5	150	300	0.0937329	$0.002036 \pm 8.81 \text{e-}06$
3.5	200	300	0.130955	$0.002123 \pm 8.379e-06$
3.5	300	300	0.233416	0.002448 ± 9.259e-06

Table C.1 – continued from previous page

Coupling (g)	$m_{Phi}$ [GeV]	$m_{\chi}$ [GeV]	$\Gamma_{min}$ [GeV]	σ
3.5	500	300	137.107	0.004413 ± 2.588e-05
3.5	1000	300	841.774	$0.002184 \pm 1.014e-05$
3.5	1500	300	1551.86	$0.0004471 \pm 2.349e-06$
3.5	10	500	0.000775572	$0.0002016 \pm 7.906$ e-07
3.5	20	500	0.00858777	$0.0002011 \pm 9.138e-07$
3.5	50	500	0.0286105	$0.0002018 \pm 9.929 e$ -07
3.5	100	500	0.0603192	$0.0002033 \pm 8.104 e$ -07
3.5	150	500	0.0937329	$0.0002067 \pm 8.026$ e-07
3.5	200	500	0.130955	$0.0002106 \pm 8.439e-07$
3.5	300	500	0.233416	$0.0002225 \pm 9.256$ e-07
3.5	500	500	137.107	$0.0002686 \pm 1.162e\text{-}06$
3.5	1000	500	592.219	$0.0005877 \pm 2.823e-06$
3.5	1500	500	1291.74	0.0002318 ± 1.11e-06

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