1	ATLAS+CMS DARK MATTER FORUM RECOMMENDATIONS
2	Author/contributor list to be added as document is finalized.
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# 17 Introduction

Dark matter has not yet been seen in particle physics experiments, and there is not yet any evidence for non-gravitational interactions between dark matter and Standard Model particles. If such interactions exist, pairs of dark matter particles could be produced at the LHC, leading to signatures including one or more hard objects  $^{1}$  in association with missing transverse energy ( $\cancel{E}_{T} + X$ ).

Early Run 1 searches for  $E_T+X$  signatures at ATLAS and CMS employed a set of effective field theories (EFTs) [GIR+10] to model the possible signals. If a contact interaction is the correct description of dark matter pair production at colliders, the missing energy distribution of the signal depends only on the mass of the dark matter particles and the spin structure of the interaction; only the overall rate is a free parameter. Both experiments studied a variety EFTs with different spin structures. Provided the contact interaction approximation holds, these EFTs also provide a straightforward way to translate results amongst LHC results and the different types of non-collider searches for dark matter.

From the Run 1 results, however, it has become clear [BDSMR14] that a contact interaction is often not the correct description for the signals to which the LHC is truly sensitive. The LHC is exploring a regime where the mediating process may play a significant role, leading to signals that can be kinematically distinct from those predicted by the EFT, as well as qualitatively different signatures requiring new search strategies. While the EFT integrates out the degrees of freedom of the (heavy) intermediate particle, "simplified models" [A $^+$ 12] with directly-accessible mediators describe this richer phenomenology. Such models can be used both to interpret  $E_T$ +X searches and to guide the design of complementary searches for additional signatures.

Many proposals for such models began to emerge, for example Refs. [AJW12, AHW13, DNRT13, BDM14, BB13a, BB14, AWZ14a, A+14b, MMA+14, HKSW15, BFG15] and, at the end of 2014, AT-LAS and CMS organized a forum, the ATLAS-CMS Dark Matter Forum, to form a consensus with the participation of experts on theories of dark matter. This is the final report of that forum. One of the guiding principles of this report is to channel the

One of the guiding principles of this report is to channel the efforts of the ATLAS and CMS Collaboration towards a minimal set

<sup>1</sup> In the case of a single hard object, these signatures are commonly called 'mono-X'.

of dark matter models that should influence the design of the early Run-2 searches, rather than providing exhaustive and elaborate interpretations and re-interpretations of the results. At the same time, a thorough survey of realistic collider signals of dark matter is 58 a crucial input to the overall design of the search program. The goal of this report is such a survey, though confined within 60 some broad assumptions and focused on benchmarks for kinematicallydistinct signals which are most urgently needed. As far as time and 62 resources have allowed, the assumptions have been carefully motivated by theoretical consensus and comparisons of simulation. But 64 to achieve a true consensus with only a few months before Run 2 would begin, it was important to narrow the scope and timescale to the following:

- A prioritized, small set of benchmark simplified models should
   be agreed upon by both collaborations for Run-2 searches.
- The matrix element implementation of the simplified models should be standardized, and other common technical details (order of the calculation, showering) harmonized as much as practical. The forum should outline a common choice of LO/NLO, ME-parton shower matching and merging, factorization and renormalization scales for each of the simplified models. This leads to a single set of theory uncertainties, which will be easier to deal with when comparing results from the two collaborations.
- The forum should also discuss the conditions under which the
   EFT interpretation may still be desirable.
- the forum should prepare a report summarizing these items, suitable both as a reference for the internal ATLAS and CMS audiences and as an explanation for theory and non-collider readers. This report represents the views of the participants of the forum.

### 86 1.1 Grounding Assumptions

The first choice made for the Run-2 benchmarks is on the nature of the Dark Matter itself: it is assumed to be a particle, stable on collider timescales and non-interacting with the detector, and a Dirac fermion. The latter is a practical choice, given that the Forum relied upon a large body of theoretical work which made this assumption. Many of the conclusions in this report also apply to  $E_T$  signals of Majorana fermion DM or scalar DM with some minor modification to account for their different angular distributions, especially when considering cut-and-count analyses. Thus the choice of Dirac fermion dark matter is deemed sufficient for the benchmarks aiding the design of the upcoming Run-2 searches. Nevertheless, a more complete set of models will certainly be required upon a discovery,

as physics observables may be used to distinguish the spin of the DM particle [CHH15].

We also assume that Minimal Flavor Violation (MFV) applies to the recommended models. This means that the flavor structure of the couplings between dark matter and ordinary particles follows the structure as the Standard Model. This choice is both natural, as there is no required additional theory of flavor beyond what is already present in the SM, and and it ensures that the models do not violate flavor constraints. As a consequence, spin-o resonances exchanged in the *s*-channel must have Yukawa couplings to SM fermions. Flavor-safe models can still be constructed beyond the MFV assumption [ABG14], but their phenomenology is left for future studies.

In the parameter scan for the recommended models, we make the assumption of minimal width for the particles mediating the interaction between SM and DM. This means that only the decays that are strictly necessary for the self-consistency of the model (e.g. to DM and to quarks) are accounted for in the definition of the mediator width. In turn, this forbids any further decays of the mediator to other invisible particles of the Dark Sector that may increase its width. However, studies within the Forum show that, for many models in the cut and count analyses, the kinematic distributions and therefore the sensitivity of the search do not depend significantly on the mediator width up to extreme values where the particle nature of the mediator comes into question.

The particle content of the models chosen as benchmarks is limited to one single kind of DM whose self-interactions are not relevant for LHC phenomenology, and to one type of SM/DM interaction at a time. These assumptions only add a limited number of new particles to the SM. These simplified models, independently sought by different experimental analyses, can be used as starting points to build more complete theories. Even though this factorized picture does not always lead to full theories and leaves out details that are necessary for the self-consistency of single models (e.g. the mass generation for mediator particles), it is a starting point to prepare a set of distinct but yet complementary collider searches for Dark Matter, as it leads to benchmarks that are easily comparable across channels.

Contact interaction operators (EFTs) are also suggested wherever neither a simplified model completion nor simplified model operators yielding similar kinematic distributions are available. This is the case for dimension 5-7 operators with direct Dark Matter-electroweak boson couplings. Model-independent results should be emphasized in the signal regions that are unique to these models, and results should be considered with the necessary caution due to EFT validity issues covered in the last chapter in this report.

# 1.2 Structure of this document

The first chapter of the report is dedicated to simplified models with radiation of a hard object either from the initial state or from 147 the mediator. These models produce primarily monojet signatures, 148 but are recommended for all  $E_T+X$  searches. Details of the imple-149 mentation of these models in Monte Carlo generators are provided in Appendix A. Chapter 3 describes the specific details of the gen-151 eral models for final states including heavy flavor quarks, leaving 152 the implementation details to appendix B. Chapter 4 contains the 153 benchmark model recommendations and choices for final states containing an electroweak boson (W/Z/gamma/H). Simplified 155 models from chapter 2 are considered, together with contact inter-156 action operators wherever simplified models are not available and 157 specific simplified models leading to mono-boson signatures. The 158 technical implementation and further models that can be studied 159 beyond early searches are in appendix C. The final chapter is de-160 voted to the treatment of the validity of benchmark models from 161 contact interaction operators. Appendix D contains the necessary 162 elements that should be included in the results of experimental 163 searches to allow for further reinterpretation.

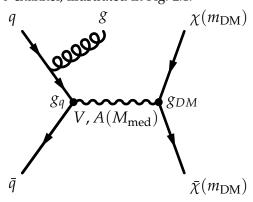
# Recommended models for all $\not \! E_T$ +X analyses

In this chapter we review recommendations for final states of  $E_T$  recoiling against a particle extracted from initial state radiation. While the recommendations are general, the discussions in this chapter are made based on the monojet final state. Further details on the mono- $\gamma/W/Z$  final states from boson radiation are discussed in Sec. 4.1.

## 2.1 Vector and axial vector mediator, s-channel exchange

A simple extension of the Standard Model (SM) is an additional U(1) gauge symmetry, where a dark matter (DM) candidate particle has charges only under this new group. Assuming that some SM particles are also charged under this group, then a new gauge boson can mediate interactions between the SM and DM.

We consider the case of a DM particle that is a Dirac fermion and where the production proceeds via the exchange of a spin-1 mediator in the *s*-channel, illustrated in Fig. 2.1.



We consider two models with vector and axial-vector couplings between the spin-1 mediator and SM and DM fields, with the corresponding interaction Lagrangians:

$$\mathcal{L}_{\text{vector}} = g_{\text{q}} \sum_{q=udscbt} Z'_{\mu} \bar{q} \gamma^{\mu} q + g_{\text{DM}} Z'_{\mu} \bar{\chi} \gamma^{\mu} \chi \tag{2.1}$$

$$\mathcal{L}_{\text{axial-vector}} = g_{\text{q}} \sum_{q=udscbt} Z'_{\mu} \bar{q} \gamma^{\mu} \gamma^{5} q + g_{\text{DM}} Z'_{\mu} \bar{\chi} \gamma^{\mu} \gamma^{5} \chi. \tag{2.2}$$

The coupling  $g_q$  is assumed to be universal to all quarks. It is also possible to consider other models in which mixed vector and axial-vector couplings are considered, for instance the couplings to the

Figure 2.1: Representative Feynman diagram showing the pair production of dark matter particles in association with a parton from the initial state via a vector or axial-vector mediator. The cross section and kinematics depend upon the mediator and dark matter masses, and the mediator couplings to dark matter and quarks respectively:  $(M_{\rm med}, m_{\rm DM}, g_{\rm DM}, g_{\rm q})$ .

quarks are vector whereas those to DM are axial-vector. We recommend the models with pure vector couplings or pure axial vector couplings. As mentioned in the introduction, when no additional visible or invisible decays contribute to the width of the mediator, the minimal width is fixed by the choices of couplings  $g_q$  and  $g_{DM}$ . The effect of larger widths is discussed on page 26. For the vector and axial-vector models, the minimal width is

$$\Gamma_{\min}^{V/A} = \Gamma_{\bar{\chi}\bar{\chi}}^{V/A} + \sum_{q} \Gamma_{\bar{q}q}^{V/A}.$$
 (2.3)

The leading order expressions for the partial widths are:

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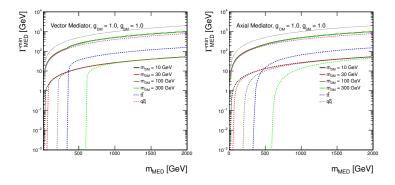
$$\Gamma_{\bar{\chi}\chi}^{V} = \frac{g_{\rm DM}^{2} M_{\rm med}}{12\pi} \left( 1 + \frac{2m_{\rm DM}^{2}}{M_{\rm med}^{2}} \right) \beta_{DM} \theta (M_{\rm med} - 2m_{\rm DM})$$
(2.4)

$$\Gamma_{\bar{q}q}^{V} = \frac{3g_{q}^{2}M_{\text{med}}}{12\pi} \left(1 + \frac{2m_{q}^{2}}{M_{\text{med}}^{2}}\right) \beta_{q}\theta(M_{\text{med}} - 2m_{q})$$
(2.5)

$$\Gamma_{\bar{\chi}\chi}^{A} = \frac{g_{\rm DM}^{2} M_{\rm med}}{12\pi} \beta_{\rm DM}^{3/2} \theta(M_{\rm med} - 2m_{\rm DM})$$
(2.6)

$$\Gamma_{\bar{q}q}^{A} = \frac{3g_{q}^{2}M_{\text{med}}}{12\pi}\beta_{q}^{3/2}\theta(M_{\text{med}} - 2m_{q}),$$
(2.7)

 $\theta(x)$  denotes the Heaviside step function, and  $\beta_f = \sqrt{1 - \frac{4m_f^2}{M_{\rm med}^2}}$  is the velocity of the fermion f in the mediator rest frame. Note the color factor 3 in the quark terms. Figure 2.2 shows the minimal width as a function of mediator mass for both vector and axial-vector mediators assuming  $g_q = g_{\rm DM} = 1$ . With this choice of the couplings, the dominant contribution to the minimal width comes from the quarks due to the color factor enhancement and the large number of them.



The simplified models described here have four free parameters: mediator mass  $M_{\rm med}$ , Dark Matter mass  $m_{\rm DM}$ , coupling of the mediator to quarks  $g_{\rm q}$  and coupling of the mediator to Dark Matter  $g_{\rm DM}$ . See [BDMM15] for a thorough discussion. In order to determine an optimal choice of the parameter grid for presentation of the early Run-2 results, dependencies of the kinematic quantities and cross sections on the individual parameters need to be studied. The following paragraphs list the main observations from the

To do Studies have been performed to see if the case of a mixed coupling can be simply extracted from the other models by some reweighting procedure to take account of the difference in cross section. This would assume that the difference between the pure and mixed couplings case does not affect the kinematics of the event. Note, though, that in the mediator rest frame, the angular distribution of the DM relative to the mediator direction of motion has the form:  $1 + z^2 + 2 * C * z (z = \cos \theta)$ , with the second term only present in the mixed case. This may lead to acceptance differences. (??)

Figure 2.2: Minimal width as a function of mediator mass for vector and axial-vector mediator assuming couplings of 1. The total width is shown as solid lines for Dark Matter masses of 10 GeV, 30 GeV, 100 GeV and 300 GeV in black, red, brown and green, respectively. The individual contributions from Dark Matter are indicated by dotted lines with the same colors. The contribution from all quarks but top is shown as magenta dotted line and the contribution from top quarks only is illustrated by the dotted blue line. The dotted black line shows the extreme case  $\Gamma_{\min} = M_{\text{med}}$ .

scans over the parameters that support the final proposal for the parameter grid.

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Scan over the couplings Figure 2.3 reveals there are no differences in the shape of the  $E_T$  distribution among the samples where the pair of  $m_{\rm DM}$  =10 GeV Dark Matter particles are produced on-shell from the mediator of  $M_{\text{med}}$  =1 TeV, generated with different choices of the coupling strength. This a generator-level prediction with no kinematic selections or detector simulation. Coupling values in the range 0.1–1.45, holding  $g_q = g_{DM}$ , correspond to a rough estimate of the lower sensitivity of mono-jet analyses and a maximum coupling value such that  $\Gamma_{\min} < M_{\text{med}}$ . Based on similar plots for different choices of  $M_{\text{med}}$  and  $m_{\text{DM}}$ , we conclude that the shapes of kinematic distributions are not altered either for the on-shell Dark Matter production where  $M_{\rm med} > 2m_{\rm DM}$ , or for the off-shell Dark Matter production where  $M_{\rm med} < 2m_{\rm DM}$ . Only the cross sections change. Differences in kinematic distributions are expected only close to the transition region where both on-shell and off-shell decays occur.

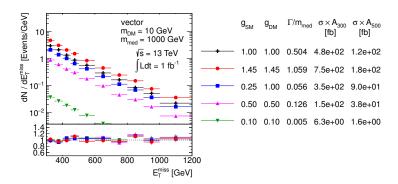
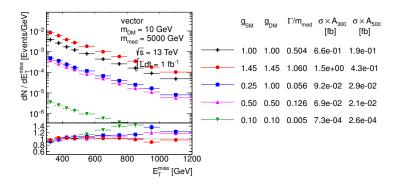
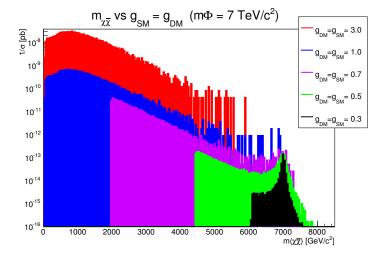


Figure 2.3: Scan over couplings. The  $E_T$  distribution is compared for the vector mediator models using the parameters as indicated. Ratios of the normalized distributions with respect to the first one are shown.  $A_{300}$  and  $A_{500}$  in the table denote the acceptance of the  $E_T > 300$  GeV and  $E_T > 500$  GeV cut, respectively.

One situation requiring a careful consideration is the case of extremely heavy and narrow mediators, which can arise for small coupling strengths. Upon close examination, it was determined that this case is not peculiar. However, the complete story is a cautionary tale about understanding the details of the generator tools. Figure 2.4 suggests a change in the shape of the  $E_T$  distribution for a  $M_{\text{med}}$  =5 TeV mediator once  $\Gamma_{\text{min}}/M_{\text{med}}$  is of the order of a percent or lower. This, however, does not come from physics, but is an artifact of the generator implementation, where a cutoff for the regions far away from the mediator mass is generally used. This is illustrated in Fig. 2.5 showing the invariant mass of the Dark Matter pair in the samples generated for a  $M_{\text{med}}$  =7 TeV mediator with different coupling strengths. In all cases, it is expected to observe a peak around the mediator mass with a tail extending to  $m_{\bar{\chi}\chi} \to 0$ , significantly enhanced by parton distribution functions at low Bjorken x. For coupling strength 1 and 3, the massive enhancement at  $m_{\bar{\chi}\chi} \to 0$  implies that resonant production at  $m_{\bar{\chi}\chi} = 7$  TeV is statistically suppressed such that barely any events are generated there. However, for narrower mediators with couplings below 1,

the peak around 7 TeV is clearly visible in the generated sample and the dominant tail at  $m_{\bar{\chi}\chi} \to 0$  is artificially cut off, leading to unphysical cross section predictions and kinematic shapes. This explains why the sample with the narrowest mediator in Fig. 2.4 is heavily suppressed in terms of production cross section and also gives different  $E_T$  shape. In general, for such extreme parameter choices the EFT model should give the correct answer.





# To do Refer to results of ongoing study in Section 6. (??)

Figure 2.4: Scan over couplings. The  $E_T$  distribution is compared for the vector mediator models using the parameters as indicated. Ratios of the normalized distributions with respect to the first one are shown.  $A_{300}$  and  $A_{500}$  in the table denote the acceptance of the  $E_T > 300$  GeV and  $E_T > 500$  GeV cut, respectively.

Figure 2.5: Invariant mass of the Dark Matter pair in the samples with  $M_{\text{med}} = 7$  TeV and different coupling strengths.

Since kinematic distributions are robust to changes in the specific values of coupling, the choice of  $g_q = g_{\rm DM}$  is reasonable to reduce the parameter space to be scanned. There are no complications associated with small couplings, but, also, the early part of Run-1 will not be sensitive to them. We recommend a range of couplings that limit the calculated width of the mediator to be near or below  $M_{\rm med}$ .

For direct mediator searches, asymmetric couplings ( $g_q \neq g_{DM}$ ) might also be considered. For example, one might fix the mediator mass and produce a scan in  $g_{DM}$  vs  $g_q$ . Such searches, such as those for dijet and ttbar resonances, may restrict  $g_q$  to a greater degree than  $g_{DM}$ .

Scan over the Dark Matter mass For a fixed mediator mass  $M_{\text{med}}$  and couplings, both the cross section and the kinematic distributions remain similar for different Dark Matter masses as long as

 $M_{\rm med} > 2m_{\rm DM}$ . This simply reflects the fact that most mediators 268 are produced on-shell, and the details of the invisible decay are 269 unimportant. This is illustrated in Fig. 2.6 for an example of  $M_{\text{med}}$ 270 =1 TeV 10 GeV  $< m_{\rm DM} <$  300 GeV. It is observed that the cross 271 section decreases as the  $m_{\rm DM}$  approaches  $M_{\rm med}/2$ . Once the Dark 272 Matter pair is produced off-shell, the cross section of the simplified 273 model is suppressed and the  $E_T$  spectrum hardens, as demon-274 strated with the choice of  $m_{\rm DM}$  =1 TeV in the same plot. Figure 2.7 275 reveals the  $E_T$  spectrum hardens further with increasing  $m_{DM}$ , ac-276 companied by the gradual decrease of the cross section. From these 277 observations one can conclude: 278

• A coarse binning along  $m_{\rm DM}$  is sufficient at  $M_{\rm med}\gg 2m_{\rm DM}$ .

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- Finer binning is needed in order to capture the changes in the cross section and kinematic quantities close to the production threshold on both sides around  $M_{\text{med}} = 2m_{\text{DM}}$ .
- Due to the significant cross section suppression of the off-shell Dark Matter pair production, it is not necessary to populate the parameter space  $M_{\rm med} \ll 2m_{\rm DM}$  since imminent LHC searches are not expected to be sensitive to these signals.

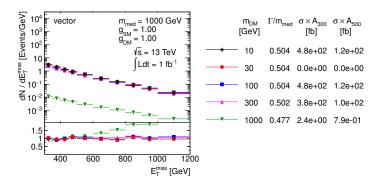


Figure 2.6: Scan over Dark Matter mass. The  $\not\! E_T$  distribution is compared for the vector mediator models using the parameters as indicated. Ratios of the normalized distributions with respect to the first one are shown.  $A_{300}$  and  $A_{500}$  in the table denote the acceptance of the  $\not\! E_T > 300\,$  GeV and  $\not\! E_T > 500\,$  GeV cut, respectively.

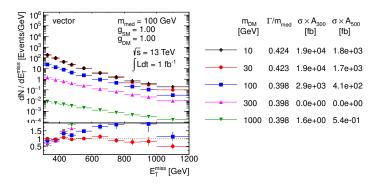


Figure 2.7: Scan over Dark Matter mass. The  $E_T$  distribution is compared for the vector mediator models using the parameters as indicated. Ratios of the normalized distributions with respect to the first one are shown.  $A_{300}$  and  $A_{500}$  in the table denote the acceptance of the  $E_T > 300$  GeV and  $E_T > 500$  GeV cut, respectively.

Scan over the mediator mass Changing the mediator mass for fixed Dark Matter mass and couplings leads to significant differences in cross section and shapes of the kinematic variables for  $M_{\rm med} > 2m_{\rm DM}$  as shown in Fig. 2.8. As expected, higher mediator masses lead to harder  $E_T$  spectra. On the other hand, the  $E_T$ 

shapes are similar in the off-shell Dark Matter production regime. 292 This is illustrated in Fig. 2.9. Therefore, a coarse binning in  $m_{DM}$  is sufficient at  $M_{\rm med} \ll 2m_{\rm DM}$ .

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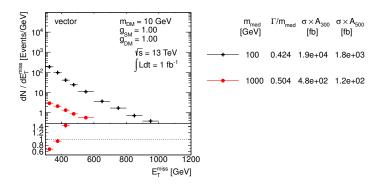


Figure 2.8: Scan over mediator mass. The  $E_T$  distribution is compared for the vector mediator models using the parameters as indicated. Ratios of the normalized distributions with respect to the first one are shown.  $A_{300}$  and  $A_{500}$  in the table denote the acceptance of the  $E_T > 300$  GeV and  $E_T > 500$  GeV cut, respectively.

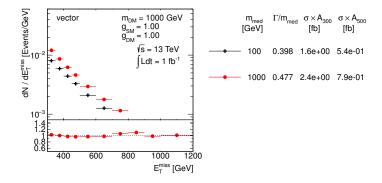


Figure 2.9: Scan over mediator mass. The  $\not\!E_T$  distribution is compared for the vector mediator models using the parameters as indicated. Ratios of the normalized distributions with respect to the first one are shown.  $A_{300}$  and  $A_{500}$  in the table denote the acceptance of the  $E_T > 300$  GeV and  $E_T > 500$  GeV cut, respectively.

Proposed parameter grid The final step in proposing a parameter grid is to evaluate the sensitivity of Run-2 LHC data with respect to rate and/or kinematics. Projected sensitivities for a 14 TeV mono-jet analysis are available from ATLAS [ATL14]. The expected upper limit at 95% confidence level on the product of cross section, acceptance and efficiency,  $\sigma \times A \times \epsilon$ , in the final Run-1 ATLAS mono-jet analysis [A<sup>+</sup>15] is 51 fb and 7.2 fb for  $E_T > 300$  GeV and  $E_T > 500$  GeV, respectively. ATLAS estimates a factor of two increase in sensitivity with the 2015 data. Given that cross section for V+jets processes increases by roughly a factor 2 when going from  $\sqrt{s} = 8$  TeV to 13 TeV, similar fiducial cross section limits can be expected with the first Run-2 data as from the final Run-1 analysis. The generator level cross section times the acceptance at  $E_T > 500$  GeV for the model with couplings  $g_q = g_{DM} = 1$ , light Dark Matter of  $m_{\rm DM}$  =10 GeV and a  $M_{\rm med}$  =1 TeV vector mediator is at the order of 100 fb, i.e. the early Run-2 mono-jet analysis is going to be sensitive to heavier mediators than this. The value of  $\sigma \times A$  at  $\not\!E_T > 500$  GeV for 5 TeV vector mediator is at the order of 0.1 fb, therefore this model probably lies beyond the reach of the LHC in the early Run 2.

Based on these arguments, the following  $M_{\text{med}}$  grid points are chosen, roughly equidistant in the logarithmic scale: 10 GeV, 20 GeV, 50 GeV, 100 GeV, 200 GeV, 300 GeV, 500 GeV, 1000 GeV and 2000 GeV. Given the fact that significant changes in cross section happen around the  $M_{\text{med}} = 2m_{\text{DM}}$  threshold, the  $m_{\text{DM}}$ grid points are taken at approximately  $M_{\text{med}}/2$ , namely: 10 GeV, 50 GeV, 150 GeV, 500 GeV and 1000 GeV. Points on the on-shell diagonal are always chosen to be 5 GeV away from the threshold, to avoid numerical instabilities in the event generation. The detailed studies of the impact of the parameter changes on the cross section and kinematic distributions presented earlier in this section support removing some of the grid points and relying on interpolation. The optimized grids proposed for the vector and axial-vector mediators are given in Table. 2.1, containing 35 mass points each. One point at very high mediator mass (5 TeV) is added for each of the DM masses scanned, to aid the reinterpretation of results in terms of contact interaction operators (EFTs) as discussed in Section 5.4.

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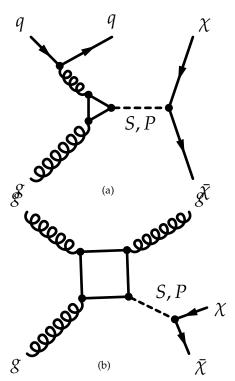
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$m_{\mathrm{DM}}/\mathrm{GeV}$	$M_{ m med}$ / GeV									
1	10	20	50	100	200	300	500	1000	2000	5000
10	10	15	50	100						5000
50	10		50	95	200	300				5000
150	10				200	295	500		1000	5000
500	10						500	995	2000	5000
1000	10							1000	1995	5000

Table 2.1: Simplified model benchmarks for s-channel simplified models (spin-1 mediators decaying to Dirac DM fermions in the V and A case, taking the minimum width for gq  $=g_{\mathrm{DM}}=1$ 

The presentation of the results in the  $g_q$ – $g_{DM}$  plane for fixed 332 masses benefits from cross section scaling and is discussed in Sec-333 tion 2.3.

# Scalar and pseudoscalar mediator, s-channel exchange



One of the simplest UV complete extensions of the effective field

Figure 2.10: One-loop diagrams of processes exchanging a scalar (S) or pseudoscalar (P) mediator, leading to a mono-jet signature.

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theory approach is the addition of a scalar/pseudoscalar mediator between DM and SM. A gauge singlet mediator can have tree-level interactions with a singlet DM particle that is either a Dirac or Majorana fermion, or DM that is a scalar itself. The spin-0 mediator can either be a real or complex scalar; a complex scalar contains both scalar and pseudoscalar particles, whereas the real field only contains the scalar particle. Refs. [BFG15, HKSW15] contain a thorough discussion of these models. One-loop diagrams leading to a  $\not\!\!E_T$  +X signature are shown in Fig. 2.10. In this document we consider only two of the possible choices for this simplified model: one where the interaction with the SM is mediated by a real scalar, and the second where we consider only a pseudoscalar for which the associated scalar is assumed to be decoupled at higher energies. Note that this assumption does not hold in a UV complete model where the two components of the complex scalar mediator would be approximately degenerate. As stated in the Introduction of this document, these models are deemed sufficient as a starting point for early Run-2 searches, but the complex scalar case could be studied separately in the case of heavy flavor final states given the sufficiently different kinematics.

Couplings to the SM fermions can be arranged by mixing with the SM Higgs. Such models have interesting connections with Higgs physics, and can be viewed as generalizations of the Higgs portal to DM. The most general scalar mediator models will have renormalizable interactions between the SM Higgs and the new scalar  $\phi$  or pseudoscalar a, as well as  $\phi/a$  interactions with electroweak gauge bosons. Such interactions are model dependent, often subject to constraints from electroweak precision tests, and would suggest specialized searches which cannot be generalized to a broad class of models (unlike, for instance, the  $E_T$  + jets searches). As a result, for this class of minimal simplified models with spin-0 mediators, we will focus primarily on couplings to fermions and loop-induced couplings to gluons.

Working under the assumption of Minimal Flavor Violation (MFV) implies scalar couplings to fermions are proportional to the fermion mass. However, the overall normalization constant of this coupling can differ for up- and down-type quarks and charged leptons. Assuming that DM is a fermion  $\chi$  that couples to the SM only through a scalar  $\phi$  or pseudoscalar a, the most general tree-level Lagrangians<sup>1</sup> compatible with the MFV assumption are [CRTW14, ADR<sup>+</sup>14]:

$$\mathcal{L}_{\phi} = g_{\chi}\phi\bar{\chi}\chi + \frac{\phi}{\sqrt{2}}\sum_{i}\left(g_{u}y_{i}^{u}\bar{u}_{i}u_{i} + g_{d}y_{i}^{d}\bar{d}_{i}d_{i} + g_{\ell}y_{i}^{\ell}\bar{\ell}_{i}\ell_{i}\right), (2.8)$$

$$\mathcal{L}_{a} = ig_{\chi}a\bar{\chi}\gamma_{5}\chi + \frac{ia}{\sqrt{2}}\sum_{i}\left(g_{u}y_{i}^{u}\bar{u}_{i}\gamma_{5}u_{i} + g_{d}y_{i}^{d}\bar{d}_{i}\gamma_{5}d_{i} + g_{\ell}y_{i}^{\ell}\bar{\ell}_{i}\gamma_{5}\ell_{i}\right). (2.9)$$

Here, the sums run over the all SM generations; the Yukawa cou-

Note that these includes couplings to leptons, while in the vector/axialvector case discussed earlier this was resctricted to quarks only for historical reasons

plings  $y_i^f$  are normalized to  $y_i^f = \sqrt{2}m_i^f/v$  where  $v \simeq 246$  GeV represents the Higgs vacuum expectation value (VEV). While the couplings  $g_u$ ,  $g_d$ ,  $g_\ell$  to SM fermions are factors multiplying the SM Yukawa structure, we parametrise the DM-mediator coupling as  $g_\chi$ , without any additional Yukawa structure between the mediator and the dark sector.

As already stated we only choose a minimal set of interactions that do not include interactions with the SM Higgs field. For simplicity and ease of comparison, we assume universal SM-mediator couplings  $g_v \equiv g_u = g_d = g_\ell$  in the remainder of this work. This allows the relative discovery and exclusion power of each search to be directly compared, though again we emphasize the importance of multiple search channels, not an exclusive focus on the single, most powerful channel under the assumption of universal couplings.

Given these simplifications, the minimal set of parameters under consideration is

$$\left\{m_{\chi}, m_{\phi/a}, g_{\chi}, g_{v}\right\}. \tag{2.10}$$

Despite our simplifying assumption, one should keep the more general possibility in mind, as even simple extensions of the mediating sector can result in  $g_u \neq g_d \neq g_\ell$ . A well-known realization of this would be the coupling of the pseudoscalar to up-type quarks (proportional to  $m_u \cot \beta$ ) and down-type quarks and charged leptons (proportional to  $m_{d/\ell} \tan \beta$ ) in two-Higgs doublet extensions of the SM. Here  $\tan \beta$  denoting the ratio of VEVs of the two Higgs doublets. This possibility of non-equal couplings motivates searches in complementary channels which probe couplings to different flavors of quarks and leptons.

We choose the minimal mediator width given by

$$\Gamma_{\phi,a} = \sum_{f} N_{c} \frac{y_{f}^{2} g_{v}^{2} m_{\phi,a}}{16\pi} \left( 1 - \frac{4m_{f}^{2}}{m_{\phi,a}^{2}} \right)^{x/2} + \frac{g_{\chi}^{2} m_{\phi,a}}{8\pi} \left( 1 - \frac{4m_{\chi}^{2}}{m_{\phi,a}^{2}} \right)^{x/2} + \frac{\alpha_{s}^{2} y_{t}^{2} g_{v}^{2} m_{\phi,a}^{3}}{32\pi^{3} v^{2}} \left| f_{\phi,a} \left( \frac{4m_{t}^{2}}{m_{\phi,a}^{2}} \right) \right|^{2}$$
(2.11)

where x=3 for scalars and x=1 for pseudoscalars, and the loop integrals are

$$f_{\phi}(\tau) = \tau \left[ 1 + (1 - \tau) \operatorname{arctan}^2 \left( \frac{1}{\sqrt{\tau - 1}} \right) \right], \qquad f_a(\tau) = \tau \operatorname{arctan}^2 \left( \frac{1}{\sqrt{\tau - 1}} \right)$$
(2.12)

for  $\tau < 1$  and

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$$f_{\phi}(\tau) = \tau \left[ 1 + (1 - \tau) \left( -\frac{1}{4} \left( \log \frac{1 + \sqrt{1 - \tau}}{1 - \sqrt{1 - \tau}} + i\pi \right)^{2} \right) \right] , f_{a}(\tau) = \tau \left( -\frac{1}{4} \left( \log \frac{1 + \sqrt{1 - \tau}}{1 - \sqrt{1 - \tau}} + i\pi \right)^{2} \right) (2.13)$$

for au>1, where  $au=4m_t^2/m_{\phi,a}^2$ .

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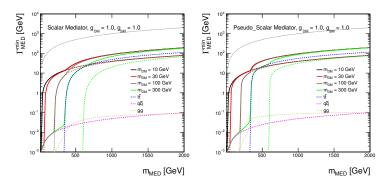
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The first term in the width corresponds to the decay into SM fermions, and the sum runs over all kinematically available fermions,  $N_c = 3$  for quarks. The second term is the decay into DM, assuming that is kinematically allowed. The factor of two between the decay into SM fermions and into DM is a result of our choice of normalization of the Yukawa couplings due to spin dependencies. The last term corresponds to decay into gluons. Since we have assumed that  $g_q = g_u = g_d = g_\ell$ , we have included in the partial decay widths  $\Gamma(\phi/a \to gg)$  only the contributions stemming from top loops, which provide the by far largest corrections given that  $y_t \gg y_h$  etc. At the loop level the mediators can decay not only to gluons but also to pairs of photons and other final states if kinematical accessible. However the decay rates  $\Gamma(\phi/a \to gg)$  are always larger than the other loop-induced partial widths, and in consequence the total decay widths  $\Gamma_{\phi/a}$  are well approximated by the corresponding sum of the individual partial decay widths involving DM, fermion or gluon pairs. It should be noted that if  $m_{\phi/a} > 2m_t$  the total widths of  $\phi/a$  will typically be dominated by the partial widths to top quarks.

The minimal width for scalar and pseudo-scalar mediators with  $g_q = g_{\rm DM} = 1$  are shown in Fig. 2.11, illustrating the effect of choosing the SM Higgs-like Yukawa couplings for the SM fermions. For the mediator mass above twice the top quark mass  $m_t$ , the minimal width receives the dominant contribution from the top quark. For lighter mediator masses, Dark Matter dominates as the couplings to lighter quarks are Yukawa suppressed.



It can be seen in Fig. 2.12 that the kinematics for the scalar and pseudoscalar models coincides. For this reason, we recommend to only generate only one of the two models, and report the cross-sections on HEPData for the other one. No preference is given between the two models as they have the same kinematics, although it is worth pointing out that the pseudo-scalar model has been used for a Dark Matter interpretation of the DAMA signal and of the galactic center excess [ADNP15].

Similarly as in the case of the vector and axial-vector couplings of spin-1 mediators, scans in the parameter space are performed also for the scalar and pseudo-scalar couplings of the spin-0 mediators in order to decide on the optimized parameter grid for the

Figure 2.11: Minimal width as a function of mediator mass for scalar and pseudo-scalar mediator assuming couplings of 1. The total width is shown as solid lines for Dark Matter masses of  $m_{\rm DM}$  =10 GeV, 30 GeV, 100 GeV and 300 GeV in black, red, brown and green, respectively. The individual contributions from Dark Matter are indicated by dotted lines with the same colors. The contribution from all quarks but top is shown as magenta dotted line and the contribution from top quarks only is illustrated by the dotted blue line. The dotted beige line shows the contribution fron the coupling to gluons. The dotted black line shows the extreme case  $\Gamma_{\min} = M_{\text{med}}$ 

To do Clarify shape of model repository (??)

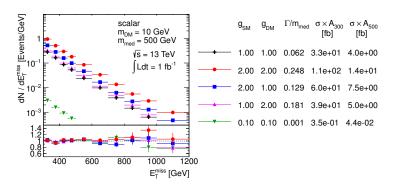


Figure 2.12: PLACEHOLDER: Comparison of the  $\mathcal{E}_T$  distributions for the scalar and pseudoscalar models for different DM and mediator masses. Ratios of the normalized distributions with respect to the first one are shown.  $A_{300}$  and  $A_{500}$  in the table denote the acceptance of the  $\mathcal{E}_T > 300$  GeV and  $\mathcal{E}_T > 500$  GeV cut, respectively.

presentation of Run-2 results. Figures 2.13- 2.17 show the scans over the couplings, Dark Matter mass and mediator mass and the same conclusions apply as in Section 2.1.

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Since the top quark gives the dominant contribution to the mediator width due to SM Higgs-like Yukawa couplings, the effect of the kinematic threshold at  $M_{\rm med}=2m_t$  was studied in detail. A scan over the mediator mass is shown in Fig. 2.17 where  $M_{\rm med}=300$  GeV and 500 GeV are chosen to be below and above  $2m_t$ . The off-shell Dark Matter production regime is assumed by taking  $m_{\rm DM}=1$  TeV in order to study solely the effects of the couplings to quarks. No differences in the kinematic distributions are observed and also the cross sections remain similar in this case. Therefore, it is concluded that no significant changes appear for mediator masses around the  $2m_t$  threshold.

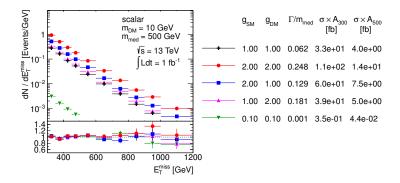


Figure 2.13: Scan over couplings. The  $\mathcal{E}_T$  distribution is compared for the scalar mediator models using the parameters as indicated. Ratios of the normalized distributions with respect to the first one are shown.  $A_{300}$  and  $A_{500}$  in the table denote the acceptance of the  $\mathcal{E}_T > 300$  GeV and  $\mathcal{E}_T > 500$  GeV cut, respectively.

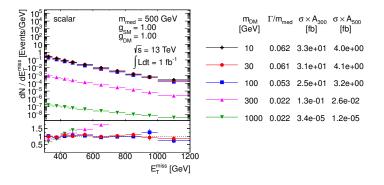


Figure 2.14: Scan over Dark Matter mass. The  $E_T$  distribution is compared for the scalar mediator models using the parameters as indicated. Ratios of the normalized distributions with respect to the first one are shown.  $A_{300}$  and  $A_{500}$  in the table denote the acceptance of the  $E_T > 300\,$  GeV and  $E_T > 500\,$  GeV cut, respectively.

The optimized parameter grid in the  $M_{\text{med}}$ – $m_{\text{DM}}$  plane for scalar and pseudo-scalar mediators is motivated by similar arguments

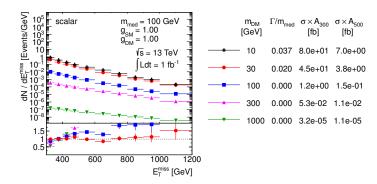


Figure 2.15: Scan over Dark Matter mass. The  $\not\! E_T$  distribution is compared for the scalar mediator models using the parameters as indicated. Ratios of the normalized distributions with respect to the first one are shown.  $A_{300}$  and  $A_{500}$  in the table denote the acceptance of the  $\not\! E_T > 300$  GeV and  $\not\! E_T > 500$  GeV cut, respectively.

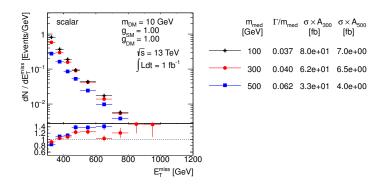


Figure 2.16: Scan over mediator mass. The  $E_T$  distribution is compared for the scalar mediator models using the parameters as indicated. Ratios of the normalized distributions with respect to the first one are shown.  $A_{300}$  and  $A_{500}$  in the table denote the acceptance of the  $E_T > 300$  GeV and  $E_T > 500$  GeV cut, respectively.

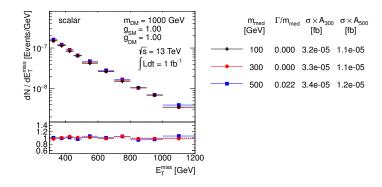


Figure 2.17: Scan over mediator mass. The  $E_T$  distribution is compared for the scalar mediator models using the parameters as indicated. Ratios of the normalized distributions with respect to the first one are shown.  $A_{300}$  and  $A_{500}$  in the table denote the acceptance of the  $E_T > 300\,$  GeV and  $E_T > 500\,$  GeV cut, respectively.

as in the previous section. Therefore, a similar pattern is followed 464 here, taking again  $g_q = g_{DM} = 1$ . Only the sensitivity to the high-465 est mediator masses has to be revisited. The generator level cross 466 section times the acceptance at  $E_T > 500$  GeV for the model with 467 couplings  $g_q = g_{DM} = 1$ , light Dark Matter of  $m_{DM}$  =10 GeV and 468 a  $M_{\rm med}$  =500 GeV scalar mediator is at the order of 10 fb, i.e. just 469 at the edge of the early Run-2 sensitivity. Increasing the mediator 470 mass to 1 TeV pushes the product  $\sigma \times A$  down to approximately 471 0.1 fb, below the LHC sensitivity. Therefore, we choose to remove 472 the 2 TeV mediator mass from the grid and present the final grid 473 with 32 mass points only, as shown in Tab. 2.2. One point at very 474 high mediator mass (5 TeV) is added for each of the DM masses 475 scanned, to aid the reinterpretation of results in terms of contact interaction operators (EFTs).

$m_{\mathrm{DM}}$ (GeV)	M <sub>med</sub> (GeV)								
1	10	20	50	100	200	300	500	1000	5000
10	10	15	50	100					5000
50	10		50	95	200	300			5000
150	10				200	295	500		5000
500	10						500	995	5000
1000	10							1000	5000

Table 2.2: Simplified model benchmarks for s—channel simplified models (spin-o mediators decaying to Dirac DM fermions in the scalar and pseudoscalar case, taking the minimum width for  $g_q = g_{DM} = 1$ )

The proposal for the scan in the  $g_q$ – $g_{\rm DM}$  plane is described in the following section.

### 2.3 Presentation of results for reinterpretation

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The aim of the parameter grid optimization is to reduce the parameter space for simulation using neighboring grid points to populate the missing parts. Two ways of doing this are:

- Interpolation is used in-between the grid points that are close enough such that finer granularity is not needed for the presentation purposes, or between the points where smooth or no changes of the results are expected. The latter argument is exactly the one that motivates the reduction of the grid points in the M<sub>med</sub>-m<sub>DM</sub> plane.
- Recalculation of the results can be used when the dependencies with respect to the neighboring grid points are known.

The results of the scan over the couplings presented in the previous sections indicate there are no changes in kinematic distributions for different choices of the coupling strengths. This means that the acceptance remains the same in the whole  $g_q$ – $g_{DM}$  plane and it is sufficient to perform the detector simulation only for one single choice of  $g_q$ ,  $g_{DM}$ . The resulting truth-level selection acceptance and the detector reconstruction efficiency can then be applied to all remaining grid points in the  $g_q$ – $g_{DM}$  plane where only the

generator-level cross section needs to be known. This significantly reduces the computing time as the detector response is by far the most expensive part of the Monte Carlo sample production. However, the number of generated samples can be reduced even further if a parameterization of the cross section dependence from one grid point to another exists.

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Let us now elaborate on a cross section scaling procedure. The propagator on the s-channel exchange is written in a Breit-Wigner form as  $\frac{1}{q^2-M_{\rm med}^2+iM_{\rm med}\Gamma}$ , where q is the momentum transfer calculated from the two partons entering the hard process after the initial state radiation, which is equivalent to the invariant mass of the Dark Matter pair. The size of the momentum transfer with respect to the mediator mass allows to classify the production in the following way:

- off-shell production when  $q^2 \gg M_{\rm med}$  leading to suppressed cross sections,
- on-shell production when  $q^2 \sim M_{\rm med}$  leading to enhanced cross sections,
- effective field theory (EFT) limit when  $q^2 \ll M_{\rm med}$ .

All three categories can be distinguished in Fig. 2.18 showing the upper limit on the interaction scale  $M^* \equiv M_{\rm med}/\sqrt{g_{\rm q}g_{\rm DM}}$  for vector mediator. In the case of the off-shell production and the EFT limit, the first and second term in the propagator dominate, respectively, which reduces the dependence on the mediator width. Therefore, in these cases one can approximate the cross section as

$$\sigma \propto g_q^2 g_{\rm DM}^2. \tag{2.14}$$

The on-shell production regime is the most interesting one as it gives the best chances for a discovery at the LHC given the cross section enhancement. The propagator term with the width cannot be neglected in this case and, in the narrow width approximation which requires  $\Gamma \ll M_{\rm med}$  (this is not necessarily the case in the benchmarks considered in the scans), one can integrate

$$\int \frac{ds}{(s - M_{\text{med}}^2)^2 + M_{\text{med}}^2 \Gamma^2} = \frac{\pi}{M_{\text{med}} \Gamma}$$
 (2.15)

which further implies the cross section scaling

$$\sigma \propto \frac{g_q^2 g_{\rm DM}^2}{\Gamma}.$$
 (2.16)

The narrow with approximation is important here as it ensures an integration over parton distribution functions (PDFs) can be neglected. In other words, it is assumed the integrand in Eq. 2.15 is non-zero only for a small region of s, such that the PDFs can be taken to be constant in this range. Since  $\Gamma \sim g_{\rm q}^2 + g_{\rm DM}^2$ , one can

To do This procedure needs a clarification: this can work only for fixed masses (??)

simplify this rule in the extreme cases as follows

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$$\sigma \propto \frac{g_{\rm q}^2 g_{\rm DM}^2}{g_{\rm q}^2 + g_{\rm DM}^2} \xrightarrow{g_{\rm q} \ll g_{\rm DM}} g_{\rm q}^2$$
 (2.17)

$$\sigma \propto \frac{g_{q}^{2}g_{DM}^{2}}{g_{q}^{2} + g_{DM}^{2}} \xrightarrow{g_{q} \ll g_{DM}} g_{q}^{2} \qquad (2.17)$$

$$\sigma \propto \frac{g_{q}^{2}g_{DM}^{2}}{g_{q}^{2} + g_{DM}^{2}} \xrightarrow{g_{q} \gg g_{DM}} g_{DM}^{2}. \qquad (2.18)$$

However, it is important to keep in mind that there is no simple scaling rule for how the cross section changes with the Dark Matter mass and the mediator mass, or for mediators with a large width, because PDFs matter in such cases as well. Therefore, the scaling procedure outlined above is expected to work only for fixed masses and fixed mediator width, assuming the narrow width approximation applies.

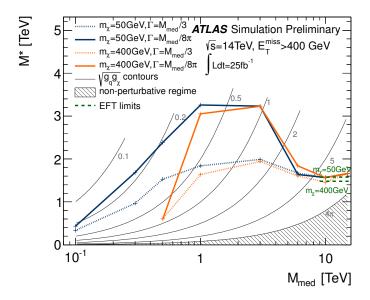


Figure 2.18: Comparison of the 95% CL lower limits on the scale of the interaction of a Z'-like simplified model at 14 TeV, in terms of the mediator mass. Corresponding limits from EFT models are shown on the same plot as green dashed lines to show equivalence between the two models for high mediator masses. Taken from Ref. [ATL14].

Figures 2.19 and 2.20 show the minimal width in the  $g_q$ – $g_{DM}$ plane for all vector, axial-vector, scalar and pseudo-scalar mediators for  $M_{\rm med} = 100$  GeV and 1000 GeV, respectively, taking  $m_{\rm DM} =$ 10 GeV. The individual colors indicate the lines of constant width along which the cross section scaling works. For vector and axialvector mediators, the minimal width is predominantly defined by  $g_q$  due to the number of quark flavors and the color factor. On the contrary, both the Standard Model and Dark Matter partial width have comparable contributions in case of scalar and pseudo-scalar mediators if the top quark channel is open ( $M_{\text{med}} > 2m_t$ ). However, mostly  $g_{\rm DM}$  defines the minimal width for  $M_{\rm med} < 2m_t$  due to the Yukawa-suppressed light quark couplings.

The performance of the cross section scaling is demonstrated in Fig. 2.21 where two mass points  $M_{\rm med} = 100$  GeV and 1 TeV with  $m_{\rm DM}=10$  GeV are chosen and rescaled from the starting point  $g_q = g_{DM} = 1$  according to Eq. 2.16 to populate the whole  $g_q$ – $g_{DM}$ plane. This means the width is not kept constant in this test and this is done in purpose in order to point out deviations from the

To do Indicate mMed=GammaMin in the plots (gDM = 6, gSM = 1.5 for Vand gSM = gDM = 5 for S) (??)

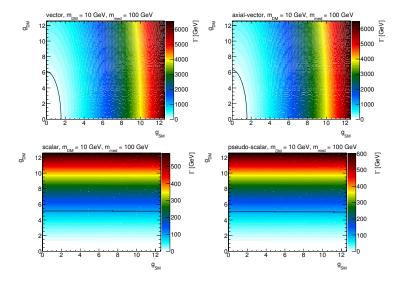


Figure 2.19: Minimal width for vector, axial-vector, scalar and pseudo-scalar mediators as a function of the individual couplings  $g_{\rm q}$  and  $g_{\rm DM}$ , assuming  $M_{\rm med}=100$  GeV and  $m_{\rm DM}=10$  GeV. The limiting case  $\Gamma_{\rm min}=M_{\rm med}$  is indicated by the black line.

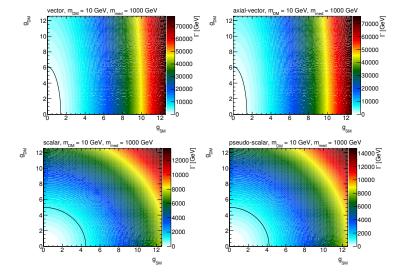


Figure 2.20: Minimal width for vector, axial-vector, scalar and pseudo-scalar mediators as a function of the individual couplings  $g_{\rm q}$  and  $g_{\rm DM}$ , assuming  $M_{\rm med}=1$  TeV and  $m_{\rm DM}=10$  GeV. The limiting case  $\Gamma_{\rm min}=M_{\rm med}$  is indicated by the black line.

scaling when the width is altered. For each mass point, the rescaled cross section is compared to the generator cross section and the ratio of the two is plotted. For the given choice of the mass points, the scaling seems to work approximately with the precision of  $\sim 20\%$  in the region where  $\Gamma_{\rm min} < M_{\rm med}$ . Constant colors indicate the lines along which the cross section scaling works precisely and there is a remarkable resemblance of the patterns shown in the plots of the mediator width. To prove the scaling along the lines of constant width works, one such line is chosen in Fig. 2.22 for a scalar mediator, defined by  $M_{\rm med} = 300$  GeV,  $m_{\rm DM} = 100$  GeV,  $g_{\rm q} = g_{\rm DM} = 1$ , and the rescaled and generated cross sections are found to agree within 3%.

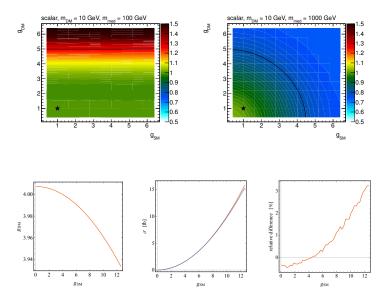


Figure 2.21: Ratio of the rescaled and generated cross sections in the  $g_q$ – $g_{DM}$  plane. The point at  $g_q$  =  $g_{DM}$  = 1, taken as a reference for the rescaling, is denoted by a star symbol. Scalar model with  $M_{\rm med}$  = 100 GeV (left) and 1 TeV (right) is plotted for  $m_{\rm DM}$  = 10 GeV. The limiting case  $\Gamma_{\rm min}$  =  $M_{\rm med}$  is shown as a black line.

Figure 2.22: Scaling along the lines of constant width. The line of constant width for  $M_{\rm med} = 300$  GeV and  $m_{\rm DM} = 100$  GeV, intercepting  $g_{\rm q} = g_{\rm DM} = 4$  is shown on left. The generated and rescaled cross sections are compared in the middle, the corresponding ratio is shown on right.

Proposed parameter grid for cross-section scaling We propose to present the results in the  $g_q$ – $g_{DM}$  plane using the following prescription:

- Since the shapes of kinematic quantities do not change for different couplings, use the acceptance and efficiency for the available  $m_{\rm DM}=50$  GeV,  $M_{\rm med}=300$  GeV,  $g_{\rm q}=g_{\rm DM}=1$  grid point from the  $M_{\rm med}$ - $m_{\rm DM}$  plane for the scalar and pseudo-scalar mediator. In case of the vector and axial-vector mediator, use the grid point  $m_{\rm DM}=50$  GeV,  $M_{\rm med}=1$  TeV,  $g_{\rm q}=g_{\rm DM}=1$ .
- Generate additional samples in order to get generator cross sections only. For scalar and pseudo-scalar mediator, choose  $m_{\rm DM}=50$  GeV,  $M_{\rm med}=300$  GeV with the following values for  $g_{\rm q}=g_{\rm DM}$ : 0.1, 1, 2, 3. For vector and axial vector mediator, choose  $m_{\rm DM}=50$  GeV,  $M_{\rm med}=1$  TeV with the following values for  $g_{\rm q}=g_{\rm DM}$ : 0.1, 0.25, 0.5, 0.75, 1.25, 1.5. The upper values are defined by the minimal width reaching the mediator mass.
- Rescale the generator cross sections for on-shell resonance production along the lines of constant width in order to populate

To do Waiting for scalar mediator calculation of perturbativity limit from J. Alcaraz.). (??)

the whole  $g_q$ – $g_{DM}$  plane.

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Rescaling to different mediator width In general it is also important to consider a larger mediator width than  $\Gamma_{\min}$  in order to accommodate additional interactions of the mediator with the visible and hidden sector particles [BFG15, HKSW15]. The cross section scaling method described above can be used to reinterpret the results presented for the minimal width, since multiplying the width by factor n is equivalent to changing the coupling strength by factor  $\sqrt{n}$ , i.e.

$$\sigma(g_{\rm q},g_{\rm DM},n\Gamma_{\rm min}(g_{\rm q},g_{\rm DM})) \propto \frac{g_{\rm q}^2g_{\rm DM}^2}{\Gamma_{\rm min}(\sqrt{n}g_{\rm q},\sqrt{n}g_{\rm DM})} \ . \eqno(2.19)$$

The cross section for the sample with couplings  $g_q$  and  $g_{DM}$  and modified mediator width  $\Gamma = n\Gamma_{\min}$  can therefore be rescaled from a sample generated with the minimal width corresponding to the couplings scaled by  $\sqrt{n}$  as described in the following formula.

$$\sigma(g_{q}, g_{\text{DM}}, n\Gamma_{\min}(g_{q}, g_{\text{DM}})) = \frac{1}{n^2} \sigma(\sqrt{n}g_{q}, \sqrt{n}g_{\text{DM}}, \Gamma_{\min}(\sqrt{n}g_{q}, \sqrt{n}g_{\text{DM}}))$$
(2.20)

Here, it is again assumed the narrow width approximation applies.

The advantage of doing this is in the fact that no event selection and detector response needs to be simulated since the changes in couplings do not have an effect on the shapes of kinematic distributions.

## <sup>586</sup> 2.4 Colored scalar mediator, t-channel exchange

The preceding sections address models with a Dirac fermion coupled to the SM through exchange of a neutral spin-o or spin-1 in an s-channel process. A t-channel process may couple the SM and DM directly, leading to a different phenomenology. Here, we examine a model where  $\chi$  is a Standard Model (SM) singlet, a Dirac fermion; the mediating particle, labeled  $\phi$ , is charged and coloured; and the SM particle is a quark. Such models have been studied in Refs. [AWZ14b, PVZ14].

Following the example of Ref. [PVZ14], the interaction Lagrangian is written as

$$\mathcal{L}_{\text{int}} = g \sum_{i=1,2,3} (\phi_L^i \bar{Q}_L^i + \phi_{uR}^i \bar{u}_R^i + \phi_{dR}^i \bar{d}_R^i) \chi$$
 (2.21)

where  $Q_L^i$ ,  $u_R^i$  and  $d_R^i$  are the SM quarks and  $\phi_L^i$ ,  $\phi_{uR}^i$  and  $\phi_{dR}^i$  are the corresponding mediators, which (unlike the *s*-channel mediators) must be heavier than  $\chi$ . These mediators have SM gauge representations under  $(SU(3),SU(2))_Y$  of  $(3,2)_{-1/6}$ ,  $(3,1)_{2/3}$  and  $(3,1)_{-1/3}$  respectively. Variations of the model previously studied include coupling to the left-handed quarks only [CEHL14, BDSJ+14], to the  $\phi_{uR}^i$  [DNRT13] or  $\phi_{dR}^i$  [PVZ14, A+14b], or some combination [BB13b, AWZ14a].

To do Note: [PVZ14] uses only i = 1,2, but I think it's fine to extend this to 3 here. (??)

As for the *s*-channel models, we assume Minimal Flavour Violation (MFV), setting the mediator masses for each flavour equal; the same logic also applies to the couplings *g*. The available parameters are then

$$\{m_{\rm DM}, M_{\phi}, g\}.$$
 (2.22)

In practice, the third mediator mass and coupling could be separated from the other two, if higher order corrections to the MFV prediction arise due to the large top Yukawa coupling — a common variation is then to define this split between the first two generations and the third, so the parameters are extended to

$$\{m_{\rm DM}, M_{\phi_{1,2}}, M_{\phi_{3}}, g_{1,2}, g_{3}\}.$$
 (2.23)

For the purposes of the rest of this section, we will assume the universal variant  $M_{\phi_{1,2}}=M_{\phi_3}$ ,  $g_{1,2}=g_3$ .

The minimal width of each mediator is expressed, using the example of decay to an up quark, as

$$\Gamma(\phi_i \to \bar{u}_i \chi) = \frac{g_i^2}{16\pi M_{\phi_i}^3} (M_{\phi_i}^2 - m_{u_i}^2 - m_{\rm DM}^2) \times \sqrt{(M_{\phi_i}^2 - (m_{u_i} + m_{\rm DM})^2)(M_{\phi_i}^2 - (m_{u_i} - m_{\rm DM})^2)},$$
(2.24)

which reduces to

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$$\frac{g_i^2 M_{\phi_i}}{16\pi} \left( 1 - \frac{m_{\rm DM}^2}{M_{\phi_i}^2} \right)^2 \tag{2.25}$$

in the limit  $M_{\phi_i}$ ,  $m_{\rm DM}\gg m_{u_i}$ .

We note that in SUSY models, the width is generally fixed by the couplings assumed in the model, while it could be wider in case of large  $m_{\rm DM}$ , leading to different kinematic distributions between the two kinds of benchmarks.

The leading-order processes involved in MET+jet production are shown in Fig. 2.23. Note that the generation index for  $\phi$  is linked to the incoming fermion(s). Thus, mono-jet production via  $\phi_u^3$  is not possible at this order, while production through  $\phi_d^3$  is suppressed by the b parton PDF. This model can also give a signal in the di-jet + MET channel when, for example, the  $\chi$  is exchanged in the t-channel and the resulting  $\phi$  pair each decay to a jet +  $\chi$ . Fig. 2.24 shows the leading order diagrams. Except for the gg induced process, di-jet production through  $\phi_u^3$  is not possible, and production through  $\phi_d^3$  is again suppressed. The diagram involving the t-channel exchange of  $\chi$  is strongly dependent upon the Dirac fermion assumption. For a Majorana fermion,  $q\bar{q}$ ,  $\bar{q}\bar{q}$ , and qq

production would be possible with the latter having a pronounced enhancement at the LHC.

This model is similar to the MSSM with only light squarks and a neutralino, except for two distinct points: the  $\chi$  is a Dirac fermion and the coupling g is not limited to be weak scale. In the MSSM, most of these processes are sub-dominant, even if resonantly enhanced, because the production is proportional to weak couplings. In the more general theories considered here, g is free to take on large values of order 1 or more, and thus diagrams neglected in MSSM simulation can occur at a much higher rate here. While constraints from SUSY jets+MET analyses on MSSM models can be recast to apply to the specific model in this report, DM searches should also directly test their sensitivity to the MSSM benchmark models.

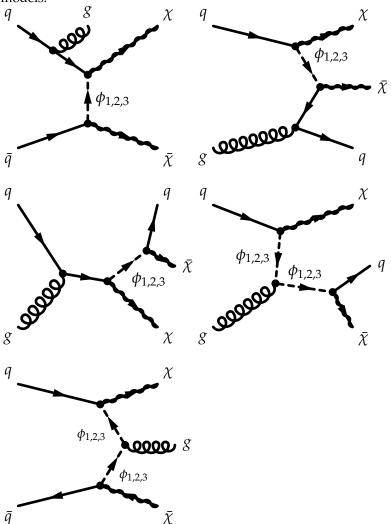


Figure 2.23: Leading order mono-jet *t*-channel processes, adapted from [PVZ<sub>14</sub>].

#### PARAMETER SCANS

Ref. [PVZ14] studies the parameter space and obtains bounds on this model from LHC Run 1 mono-jet and dijets+MET data.

As in the *s*-channel models, scans should be performed over  $m_{\rm DM}$  and  $M_{\phi}$ . The viable ranges of both parameters nearly coincide with the scan proposed for the *s*-channel; for simplicity we

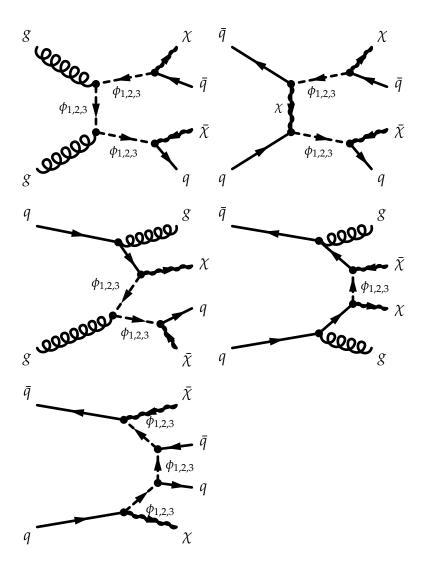


Figure 2.24: Leading order two-jet t-channel processes, adapted from [PVZ14].

recommend adopting the s-channel mono-jet grid.

The rates of the first three diagrams of Fig. 2.23 scale as one with the coupling g. In the heavy mediator limit, then, the kinematic distributions depend only indirectly on the coupling through the effect 659 on the minimal mediator width. In contrast with the s-channel case, 660 however, the bounds one obtains from X+MET searches depends 661 strongly on the width of the mediator, as is visible in Figs. 5 and 6 of Ref. [PVZ14], except in the heavy mediator limit ( $M_{\phi} \approx 2 \,\text{TeV}$ ). 663 A scan over the width was not available for this report; thus we 664 recommend scanning a range of possible widths as discussed in a 665 more-limited way for the s-channel mono-jet, spanning from the 666 minimal width to a value approaching the particle limit (for exam-667 ple,  $\Gamma \approx M_{\phi}/3$  in Ref. [PVZ14]). 668

#### 669 IMPLEMENTATION

The MadGraph implementation of the Ref. [PVZ14] is available from the Forum repository [For15g], following the matching and merging prescription described in its Section II and Appendix A.

# 2.5 Spin-2 mediator

In models with extra dimensions, the Kaluza-Klein excitations of the graviton could also serve as a mediator between the Standard Model and dark sector physics. Below a few TeV in mediator mass, production of a graviton with universal couplings is dominantly gluon-initiated, leading to forward-peaked angular distributions [AOP+02] distinct from the other models considered above. This kind of model was not studied in the forum and is not included in the recommendations, but it and models such as Ref. [LPS14] may warrant further study on a longer timescale.

# Specific models for signatures with heavy flavor quarks

The first part of this Chapter describes details of the models from in Section 2.2, with emphasis on heavy flavour final states that arise due to the Yukawa couplings of SM quarks to the mediator. In addition, simplified models yielding signatures of a single top of bottom quark in the final state are outlined in Sections ??. These models are not as generally applicable as those in the rest of this report, as they make a number of assumptions to enhance the production of these specific final states, but they are included as they still provide a unique search signature. Presentation of model-independent results is strongly encouraged to allow for further reinterpretation that relaxes some of the assumptions in these models.

# 3.1 tt and bb+MET models

As described in Section 2.2, a model with a scalar/pseudoscalar particle mediating the DM-SM interactions is one of the simplest UV completions of our EFT models. With the MFV assumption, the top quark plays a primary role in the phenomenology: The model predicts not only the monojet process described earlier, but also production of dark matter in association with top pairs, as illustrated in Fig. 3.1. Dedicated searches including jets from heavy flavor quarks in the final state can be designed for this production mechanism.

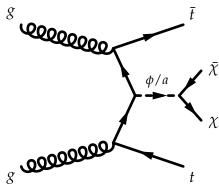


Figure 3.1: Representative Feynman diagram showing the pair production of dark matter particles in association with  $t\bar{t}$ .

### 3.1.1 Parameter scan

As discussed in Sec. 2, the MFV and universal coupling assumptions for spin-0 mediators leads to quark mass dependent Yukawa

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couplings and therefore dominant couplings to top quarks.

The parameter scan for the dedicated  $t\bar{t}+E_T$  searches has been studied in detail to target the production mechanism of DM associated to heavy flavor quarks, still sharing many details of the scan for the scalar model with a gluon radiation The benchmark points scanning the model parameters have been selected to ensure that the kinematic features of the parameter space are sufficiently represented. Detailed studies were performed to identify points in the  $m_{\rm DM}$ ,  $m_{\phi,a}$ ,  $g_{\rm DM}$ ,  $g_{\rm q}$  (and  $\Gamma_{\phi,a}$ ) parameter space that differ significantly from each other in terms of expected detector acceptance. Because missing transverse momentum is the key observable for searches, the mediator  $p_T$  spectra is taken to represent the main kinematics of a model. Another consideration in determining the set of benchmarks is to focus on the phase space where we expect the searches to be sensitive during the 2015 LHC run. Based on a projected integrated luminosity of 30 fb<sup>-1</sup> expected for 2015, we disregard model points with a cross section times branching ratio smaller than 0.1 fb, corresponding to a minimum of one expected event assuming a conservative 0.1% signal efficiency.

The kinematics is most dependent on the masses  $m_{\rm DM}$  and  $m_{\phi,a}$ . Figure 3.2 and 3.3 show typical dependencies for scalar and pseudoscalar couplings respectively. Typically, the mediator  $p_T$  spectra broadens with larger  $m_{\phi,a}$ . The kinematics are also different between on-shell ( $M_{\rm med} > 2m_{\rm DM}$ ) and off-shell ( $M_{\rm med} < 2m_{\rm DM}$ ) mediators as in Section 2.2. Furthermore, the kinematic differences in  $E_T$  spectrum between scalar and pseudoscalar are larger for light mediator masses with respect to heavier mediators. It is therefore important to benchmark points covering on-shell and off-shell mediators with sufficient granularity, including the transition region between on-shell and off-shell mediators.

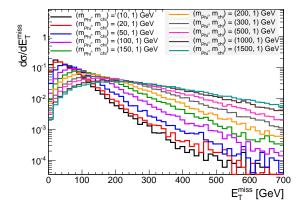


Figure 3.2: Example of the dependence of the kinematics on the scalar mediator mass. The Dark Matter mass is fixed to be  $m_{\text{DM}}$  =1GeV.

Typically only weak dependencies on width or equivalently couplings are observed (see Fig 3.4), except for large mediator masses of  $\sim 1.5\,\text{TeV}$  or for very small couplings of  $\sim 10^{-2}$ . These regimes where width effects are significant have production cross sections that are too small to be relevant for 30 fb $^{-1}$  and are not considered here. However, with the full Run-2 dataset, such models may be

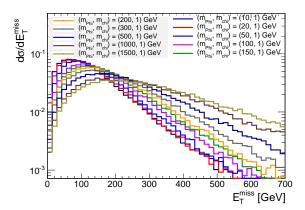


Figure 3.3: Example of the dependence of the kinematics on the pseudoscalar mediator mass. The Dark Matter mass is fixed to be  $m_{\rm DM}$  =1GeV.

within reach. The weak dependence on the typical width values can be understood as the parton distribution function are the dominant effect on mediator production. As shown in Section 2.3, for couplings  $\sim O(1)$  the width is large enough that the  $p_T$  of the mediator is determined mainly by the PDF.

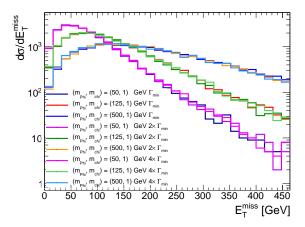


Figure 3.4: Study of the dependence of kinematics on the width of a scalar mediator. The width is increased up to four times the minimal width for each mediator and dark matter mass combination.

Another case where the width can impact the kinematics is when  $m_{\phi,a}$  is slightly larger than  $2m_\chi$ . Here, the width determines the relative contribution between on-shell and off-shell mediators. An example is given in Fig. 3.5. As the minimal width choice pursued in this document is the most conservative one, this effect can be neglected in order to reduce the number of benchmark points to be generated.

The points for the parameter scan chosen for this model are listed in Table 2.2, chosen to be harmonized with those for other analyses employing the same scalar model as benchmark. Based on the sensitivity considerations above, DM masses are only simulated up to 500 GeV (but the 5 TeV mediator point is retained) leading to a total of 24 benchmark points. However for these searches we recommend to generate scalar and pseudoscalar models separately, as the kinematics differs due to the different coupling of the mediator to the final state top quarks in the two cases, as shown in Figs. 3.2 and 3.3.

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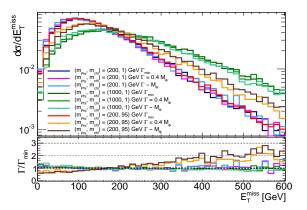


Figure 3.5: Dependence of the kinematics on the width of a scalar mediator. The width is increased up to the mediator mass. Choices of mediator and dark matter masses such that  $m_{\phi,a}$  is slightly larger than  $2m_\chi$  is the only case that shows a sizeable variation of the kinematics as a function of the width.

# 3.2 Presentation of results for reinterpretation

The cross-section scaling considerations shown in 2.3 still apply for this model. Here we detail the specific studies done for this model.

Given that the kinematics are similar for all couplings  $g=\sim 1$ , we recommend to generate only samples with  $g_{\rm DM}=g_{\rm q}=1$ . It follows from this that these benchmark points should be a good approximation for non-unity couplings and for  $g_{\rm DM}\neq g_{\rm q}$ , provided that the sample is rescaled to the appropriate cross section times branching ratio.

While the simple scaling function

$$\sigma' \times BR' = [\sigma \times BR] \times \frac{g_{\rm q}'^2}{g_{\rm q}} \times \frac{g_{\rm DM}'}{g_{\rm DM}}^2 \times \frac{\Gamma}{\Gamma'}$$
 (3.1)

is sufficient for a limited range of coupling values (see Fig. 3.6 for example). This scaling is only approximate (up to 20%) and relies on the narrow width approximation, ignoring PDFs effects. We also choose to provide instead a table of cross section times branching ratio values over a large range of couplings to support interpretation of search results (see the Appendix B). The table lists couplings from g = 0.1 to g = 3.5, where the upper limit is chosen to be close to but lower than the perturbative limit.

## 3.2.1 Specific models involving b— quarks in the final state

In some theoretically motivated scenario (e.g. for high  $tan\beta$  in 2HDM in the pMSSM), spin-o mediators might couple more strongly to down generation quarks. This assumption motivates the study of final states involving b-quarks as a complementary search to the  $t\bar{t}$ +DM models presented in the previous section, to directly probe the b- quark coupling. An example of such a model can be found in Ref. [BFG15]

As in the  $t\bar{t}$  case, detailed studies were performed, analyzing these models and their key features. It was found that they show the same weak dependence of the kinematics of the event on width variation, except in few corner cases. In addition, it was found that

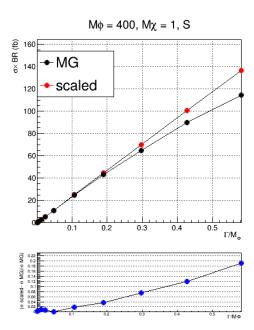


Figure 3.6: An example comparing a simple cross section scaling versus the computation from the generator, for a scalar model with  $m_{\phi}=400\,\mathrm{GeV}$ ,  $m_{\mathrm{DM}}=1\,\mathrm{GeV}$  and all couplings set to unity. In this example, the scaling relationship holds for  $\Gamma_{\phi}/m_{\phi}$  below 0.2, beyond which finite width effects become important and the simple scaling breaks down.

the same benchmark parameters of the  $t\bar{t}$  case could be chosen.

IMPLEMENTATION There are some subtleties to the Monte Carlo simulation relevant for this case that are discussed in Appendix A.

## 3.3 *Models with a single top—quark + MET*

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Many different theories predict final states with a single top and associated missing transverse momentum (monotop), some of them including dark matter candidates. A simplified model encompassing the processes leading to this phenomenology is described in Refs. [AFM11, AAB<sup>+</sup>14, BCDF15], and is adopted as one of the benchmarks for Run 2 LHC searches.

The simplified model is constructed by imposing that the model Lagrangian respects the electroweak  $SU(2)_L \times U(1)_Y$  gauge symmetry and by requiring minimality in terms of new states to supplement to the Standard Model fields. As a result, two monotop production mechanisms are possible. In the first case, the monotop system is constituted by an invisible (or long-lived with respect to detector distances) fermion  $\chi$  and a top quark. It is produced, as shown in the diagram of 3.7 (a) where a colored resonance  $\varphi$  lying in the triplet representation of  $SU(3)_C$  decays into a top quark and a  $\chi$  particle. In the second production mode, the monotop state is made of a top quark and a vector state V connected to a hidden sector so that it could decay invisibly into, e.g., a pair of dark matter particles as studied in [BCDF15]. The production proceeds via flavor-changing neutral interactions of the top quark with a quark of the first or second generation and the invisible V boson (see the diagrams of 3.7 (b) and (c)).

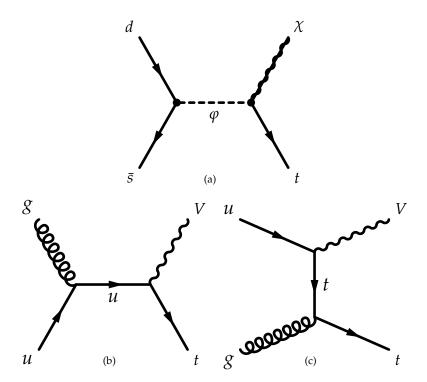


Figure 3.7: Feynman diagram of leading order processes leading to monotop events: production of a coloured scalar resonance  $\varphi$  decaying into a top quark and a spin-1/2 fermion  $\chi$  (a), s- (b) and t-channel (c) non resonant production of a top quark in association with a spin-1 boson V decaying invisibly.

#### RESONANT PRODUCTION

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In this case, a colored 2/3-charged scalar ( $\varphi$ ) is produced and decays into a top quark and a spin-1/2 invisible particle,  $\chi$ . The dynamics of the new sector is described by the following Lagrangian:

$$\mathcal{L} = \left[ \varphi \bar{d}^c \left[ a_{SR}^q + b_{SR}^q \gamma_5 \right] d + \varphi \bar{u} \left[ a_{SR}^{1/2} + b_{SR}^{1/2} \gamma_5 \right] \chi + \text{h.c.} \right]$$
 (3.2)

where u (d) stands for any up-type (down-type) quark, the notation SR refers to the monotop production mechanism via a scalar resonance and all flavor and color indices are understood for clarity.

In the notation of [AAB<sup>+</sup>14], the couplings of the new colored fields to down-type quarks are embedded into the  $3\times 3$  antisymmetric matrices  $a_{SR}^q$  (scalar couplings) and  $b_{SR}^q$  (pseudoscalar couplings) while those to the new fermion  $\chi$  and one single up-type quark are given by the three-component vectors  $a_{\{S\}R}^{1/2}$  and  $b_{\{S\}R}^{1/2}$  in flavor space.

Under the form of Eq. (3.2), the Lagrangian corresponds to the one introduced in the original monotop search proposal [AFM11] and has been used by the CMS for Run I analyses after neglecting the pseudoscalar component of the coupling and adding the vector resonance case for which minimality requirements are difficult to accomodate [CMS14]. In contrast, the study of Ref. [BCDF15] has imposed electroweak gauge invariance and requires minimality, which enforces all new couplings to be right-handed,

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accomodate [CMS14]. In contrast, the study of Ref. [BCDF15] has imposed electroweak gauge invariance and required minimality. This enforces all new couplings to be right-handed so that

$$a_{SR}^{1/2} = b_{SR}^{1/2} = \frac{1}{2} y_s^*$$
 and  $a_{SR}^q = b_{SR}^q = \frac{1}{2} \lambda_s$ , (3.3)

where the objects  $\lambda_s$  and  $y_s$  are a tridimensional vector and a  $3 \times 3$  matrix in flavor space respectively. This class of scenarios is the one that has been adopted by the ATLAS collaboration for its Run I monotop searches [ATL15] and will be considered by both collaborations for Run II analyses.

The resulting model can be likened to the MSSM with an *R*-parity violating of a top squark to the Standard Model down-type quarks and an *R*-parity conserving interaction of a top quark and a top-squark to a neutralino.

#### Non-Resonant production

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For non-resonant monotop production, the monotop state is produced via flavor-changing neutral interactions of the top quark, a lighter up-type quark and a new invisible vector particle V. This is the only case considered, as having a new scalar would involve a mixing with the SM Higgs boson and therefore a larger number of free parameters. The Lagrangian describing the dynamics of this non-resonant monotop production case is:

$$\mathcal{L} = \left[ V_{\mu} \bar{u} \gamma^{\mu} \left[ a_{FC}^1 + b_{FC}^1 \gamma_5 \right] u + \text{h.c.} \right]$$
 (3.4)

where the flavor and color indices are again understood for clarity.

The strength of the interactions among these two states and a pair of up-type quarks is modeled via two  $3 \times 3$  matrices in flavor space  $a_{FC}^{\{1\}}$  for the vector couplings and  $b_{FC}^{\{1\}}$  for the axial vector couplings.

As for the resonant case, the Lagrangian of Eq. (3.4) is the one that has been used by CMS after reintroducing the scalar option for the invisible state and neglecting all pseudoscalar interactions [CMS14]. as already mentioned, a simplified setup motivated by gauge invariance and minimality has been prefered so that, as shown in Ref. [BCDF15], we impose all interactions to involve right-handed quarks only in order to simplify the model phenomenology,

$$a_{FC}^1 = b_{FC}^1 = \frac{1}{2} a_R \tag{3.5}$$

where  $a_R$  denotes a 3 × 3 matrix in flavor space.

#### Model parameters and assumptions

The models considered as benchmarks for the first LHC searches contain further assumptions in terms of the flavour and chiral structure of the model with respect to the full Lagrangians of equations (3.2) and (3.4).

This implies the vector to be an SU(2)L singlet, hence in turn setting the vector and axial vector matrices to have elements of equal values.

In order to have an observable monotop signature at the LHC, the Lagrangians introduced above must include not too small couplings of the new particles to first and second generation quarks. For simplicity, we assumed that only channels enhanced by parton density effects will be considered, so that we fix

$$(a_R)_{13} = (a_R)_{31} = a$$
,  
 $(\lambda_s)_{12} = -(\lambda_s)_{21} = \lambda$  and  $(y_s)_3 = y$ ,

all other elements of the matrices and vectors above being set to zero.

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- IMPLEMENTATION The Monte Carlo simulation relevant for this
   case is discussed in Appendix A.
- 872 3.3.1 Parameter scan
- <sup>873</sup> The relevant parameters for the resonant model are:
- The mass of the new scalar  $\phi$ ;
- The mass of the new fermion  $\chi$ ;
- The coupling of the new scalar to the new fermion and top quark a, related to the width of the scalar in the minimal width assumption;
- The relevant parameters for the non-resonant model are:
- The mass of the new vector V;

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- The coupling of the new vector to the up and top quark *a*, related to the width of the scalar in the minimal width assumption;
  - The coupling of the new vector to the new fermion  $\chi$ , related to the branching fraction of the vector into invisible and visible particle, and as a consequence to the width of the vector.

In the case of the non-resonant model, the invisible vector is connected to a hidden sector that could be, in its simplest form, parameterized by a new fermion. This has effects on the width of the invisible V state.

It has been checked for the non-resonant model that the relevant kinematics does not change when changing the width of the resonance, for widths up to 10% of the V mass. Figures 3.8 and 3.9 show the V mass distribution, the transverse momentum for V in the case of the  $V \to t\bar{u}$  decay, for different V masses and widths. Since they only show kinematic quantities related to V, these figures are relevant independently of the V decay mode (be it visible or invisible).

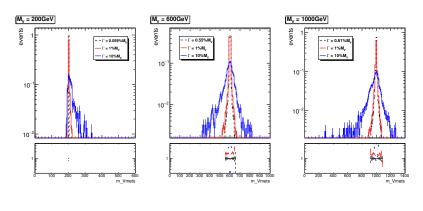


Figure 3.8: Distribution of V invariant mass for the  $gu \to tV (\to t\bar{u})$  (on-shell V) for  $m_V =$  200, 600, 1000 GeV (from left to right) and for three different visible decay width (computed from Madgraph directly according to the allowed decays and their couplings, 1% and 10%).

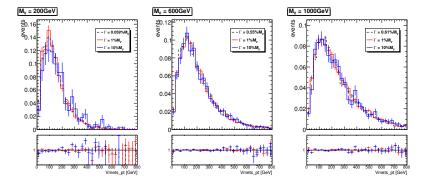


Figure 3.9: Distribution of the V  $p_T$  for the  $gu \to tV(\to t\bar{u})$  (on-shell V) for  $m_V$  = 200, 600, 1000 GeV (from left to right) and for three different visible decay width (computed from Madgraph directly, 1% and 10%).

The limited timescale allowed to reach a consensus for the recommendations contained in this document has not allowed further studies on the parameter scan of these models. The two Collaborations have however agreed to continue studying these models and agree on a common parameter scan, following the same path as for other models described in this document.

#### 3.4 Models with a single b—quark + MET

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Models of bottom-flavored Dark Matter have been proposed in Refs. [LKW13, ABHL14]. We focus on the b-FDM model of Ref. [ABHL14], created to explain the Galactic Center (GC) gamma-ray excess observed in data collected by the Fermi-LAT collaboration [DFH $^+$ 14]. This model is closely related to the t-channel mediated model from Section 2.4, with DM preferentially coupling to bottom quarks, with a decoupled third generation.

The interest in this model lies in producing an annihilation cross section consistent with the gamma-ray excess can be achieved for perturbative values of the couplings, while being consistent with LHC constraints on the colored mediator. For parameters capable of explaining the anomalous gamma-ray signal in terms of Dark Matter coupling preferentially to b- quarks, the model predicts a direct detection cross section that is consistent with current constraints, but within the near future reach of Direct Detection experiments. The model will be decisively tested with data from the upcoming

To do Spell out implications on MFV assumption. (??)

high-energy run at the LHC.

The model contains a Dirac fermion transforming as a flavor triplet. The third component of the triplet  $\chi_b$  comprises the cosmological DM. A flavor singlet, color triplet scalar field  $\Phi$  mediates the interactions between the DM and the Standard Model quarks. The model is similar to the MSSM with a light bottom squark and neutralino, and is thus a flavor-specific example of a t-channel model.

The Lagrangian considered is given by

$$-\mathcal{L} \supset g\Phi^*\chi_b b_R + \text{h.c.}$$
 (3.7)

Within the framework of minimal flavor violation, the other fermions in the flavor triplet can be made sufficiently heavy and weakly-coupled that they can be neglected in the analysis.

#### 3.4.1 Parameter scan

The nature of the model doesn't allow to derive a simple scaling behaviour which would allow us reduce the number of points to be simulated. This is because of the interference of diagrams with QCD production of the mediator (which scale as  $g_s^2$ ) with diagrams that are proportional to the coupling g in the  $b+\not\!\!\!E_T$  and  $b\bar b+\not\!\!\!E_T$  final states. Fixing the couplings also fixes the mediator width, when adopting the minimal width assumption. Therefore, the coupling scan is chosen as a discrete set of values g=0.5,1,2,3 for each mass point. A sizable, O(1) coupling benchmark such as g=1 should be considered for each mass point since this would be a distinctive feature of this benchmark from SUSY models with sbottom squarks (see Section 2.4 for further discussion). The coupling could also be chosen to fullfill constraints from the relic density (see Appendix B.1, with corresponding cross sections in Tables B.2 onwards).

To do Are we sure the models in SVN have minimal width? What is the max coupling so that the width is still lower than the mass? (??)

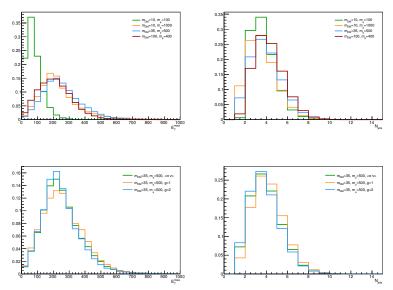


Figure 3.10: MET (left) and jet multiplicity (right) for various DM and mediator masses and couplings normalised to the relic density observed in the early universe.

In light of these considerations, we recommend to produce the following benchmark points in the parameter space for this model:

Figure 3.11: MET (left) and jet multiplicity (right) for  $m_{\rm DM}=35~{\rm GeV}$  and  $MPhi=500~{\rm GeV}$  for couplings corresponding to relic density weights and also g=1,2

- $m_{\rm DM}=10-500$  GeV with a binning of 50 GeV for  $m_{\rm DM}<100$  and 100 GeV otherwise;
- MPhi = 10 1300 with a binning of 100 GeV;
- $MPhi > m_{\rm DM} + m_b$ , since the cross-sections in the off-shell region are too small to be sensitive with early LHC data;
- Cross-sections for unit couplings can be found in Appendix B.2.
- 955 3.4.2 Model implementation
- $^{956}$  We simulate the model using the MG5\_aMC v2.2.3. The corresponding
- card files can be found on the Forum SVN repository [For15e].

## Specific models for signatures with EW bosons

In this Section, we consider models with a photon, a W boson, a Z boson or a Higgs boson in the final state, accompanied by Dark Matter particles that either couple directly to the boson or are mediated by a new particle. The experimental signature is identified as V+MET.

These models are interesting both as some are demanded by gauge coupling relations in models where the gluon provides the experimentally detectable signature, and also as stand-alone models with final states that cannot be generated by the models in Section 2.

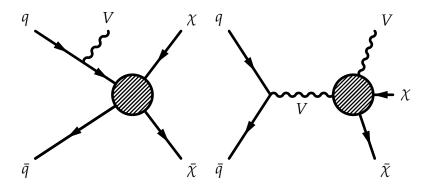


Figure 4.1: Sketch of benchmark models including a contact interaction for V+MET searches, adapted from [NCC<sup>+</sup>14].

The models considered can be divided into four categories:

Models including a contact operator, where the boson is radiated from the initial state

As depicted in the left diagram of Figure 4.1, these models

follow the nomenclature and theory for the EFT benchmarks

commonly used by MET+X searches [GIR<sup>+</sup>10]. These models

have been used in past experimental searches [Kha14, Aad14b,

 $K^{+}$ 14, Aad14b,  $A^{+}$ 14a, Aad14a], and they will not be described

here [CHLR13, CNS<sup>+</sup>13, CHH15, BLW14].

Simplified models with a boson radiated either from the initial state or from the mediator

These models follow those already described in Section 2, replac-

ing the gluon with a boson.

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Models including a contact operator, where the boson is directly coupled to DM

Shown on the right-hand side of Figure 4.1, these models allow

for a contact interaction vertex that directly couples the boson to

Dark Matter. These models are included in this report devoted to

simplified models since UV completions for most of these operators proceed through loops and are not available to date. These models provide a benchmark to motivate signal regions that are unique to searches with EW final states and would otherwise not be studied. However, we recommend to use these models as placeholders and emphasize model-independent results especially in signal regions tailored to these models. Wherever results are interpreted in terms of these operators, a truncation procedure to ensure the validity of the EFT should be employed, as detailed in Section 5.

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V-specific simplified models These models postulate direct couplings 995 of new mediators to bosons, e.g. they couple the Higgs boson to a new vector or to a new scalar [CDM<sup>+</sup>14, BLW14].

The following Sections describe the models within these categories, the parameters for each of the benchmark models chosen, the studies towards the choices of the parameters to be scanned, and finally point to the location of their Matrix Element implementation.

#### Simplified models with boson radiation

Monojet searches are generally more sensitive with respect to final states including bosons, due to the much larger rates of signal 1005 events featuring quark or gluon radiation with respect to radiation 1006 of bosons [ZBW13], in combination with the low branching ratios 1007 if leptons from boson decays are required in the final state. The 1008 rates for the Higgs boson radiation is too low for these models 1009 to be considered a viable benchmark [CDM<sup>+</sup>14]. However, the 1010 presence of photons, leptons from W and Z decays, and W or Z 1011 bosons decaying hadronically allow backgrounds to be rejected 1012 more effectively, making Z/gamma/W+ $E_T$  searches still worth 1013 comparing with searches in the jet+ $\not\!E_T$  final state. 1014

#### *Vector mediator exchanged in the s-channel*

An example Feynman diagram for these processes can be con-1016 structed by taking Fig. 2.1 and replacing the gluon with  $\gamma$ , W or Z. 1017 The interest for searches with W bosons in the final state has been 1018 elevated by the increased cross section for certain choices of cou-1019 plings for a spin-1 mediator [BT13]. Run-1 searches have considered 1020 three sample cases for the product of up and down quark couplings to the mediator, denoted as  $\xi$ :

- No couplings between mediator and either up or down quarks ( $\xi$  = 1023 0);1024
- Same coupling between mediator and each of the quark types ( $\xi$  = 1025 1); 1026

To do Additional motivations exist for this final state from SUSY searches. (??)

• Coupling of opposite sign between mediator and each of the quark types ( $\xi = -1$ ).

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The  $\xi = -1$  case leads to a large increase in the cross-section of the process, and modifies the spectrum of missing transverse energy or transverse mass used for the searches. The sensitivity of the W+ $E_T$ search for this benchmark in this case surpasses that of the jet+ $E_T$ search. However, as shown in Ref. [BCD<sup>+</sup>15], the cross-section increase is due to the production of longitudinally polarized W bosons, as a consequence of a violation of electroweak gauge symmetries. Unless further particles are introduced (in a fashion similar to the Higgs boson in the Standard Model), choosing a value of  $\xi = -1$  for this simplified model will lead to a manifest violation of unitarity at LHC energies. The simplified model with a vector mediator exchanged in the s-channel model can still be considered as a benchmark for searches with a W boson if  $\xi = 1$ . We leave the study of further models with cross-section enhancements due to different couplings to up and down quarks for studies beyond the early LHC searches covered in this document. An example of such model is the case of both DM and SM Higgs charged under a new U(1)', with a a small mass mixing between SM Z-boson and the new Z'. This leads to different effective DM couplings to  $u_L$ and  $d_L$ , proportional to their coupling to the Z boson, detailed in Appendix C.

The scan in the parameters that characterize this simplified model for EW boson +  $E_T$  searches follow what is already detailed in Section 2.

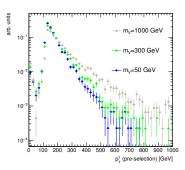
As in the case of the jet+ $\not\!E_T$  models, the width does not have a significant impact on the kinematic distributions relevant for those searches. An example of the particle-level analysis acceptance using the generator-level cuts from Ref. [Aad15] for the photon+ $\not\!E_T$  analysis, but raising the photon  $p_T$  cut to 150 GeV is shown in Figure 4.1, comparing a width that is set to  $\Gamma = M_{med}/3$  to the minimal width (the ratio between the two widths ranges from 1.05 to 1.5 with increasing mediator masses).

Acceptance ratio for $\Gamma = \Gamma_{\min}$ vs $\Gamma = M_{\text{med}}/3$				
	m <sub>DM</sub> /GeV			
$M_{\rm med}/{\rm GeV}$	10	50	200	400
50	0.96	0.99		0.95
100	0.97			
300	1.00	1.02		
600			0.96	
1000	1.01	1.02	1.03	
3000	1.02	1.03		1.01

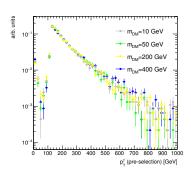
Examples of relevant kinematic distributions for selected benchmark points are shown in Fig. 4.2. leading-order cross-sections for the chosen benchmark points are shown in Appendix C.

Table 4.1: Analysis acceptance for the photon+ $\not$ E $_T$  analysis when varying the mediator width, in the case of a vector mediator exchanged in the s-channel

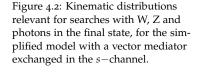


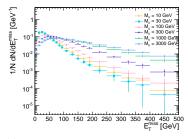


(a) Missing transverse momentum distribution for the photon+ $\not\!E_T$  final state, for different mediator mass choices, for  $m_{\rm DM}$  =10 GeV.



(b) Leading photon transverse momentum distribution for the photon+ $E_T$ final state, for different DM mass choices, with  $M_{\text{med}} = 1$  TeV.





(c) Missing transverse momentum distribution for the leptonic  $Z+E_T$ final state, for different mediator mass choices, for  $m_{\rm DM}$  =15 GeV

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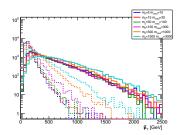
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(d) Missing transverse momentum distribution for the hadronic  $W+E_T$  final state.

#### Scalar mediator exchanged in the s-channel

The parameters for the model with a scalar mediator exchanged in the s- channel follow those in Section 2.

Even though the sensitivity of mono-boson searches to this model is low and it may not be in reach of early LHC searches, we recommend to generate this model for W, Z and photon searches in order to reproduce the kinematics of contact interaction operators described in Section 4.2.1, for later reinterpretation.

#### Colored scalar mediator exchanged in the t-channel

The model parameters with emission of an EW boson generally follow those in Section 2, even though fewer diagrams are involved. A representative Feynman diagram can be constructed by replacing a gluon in Fig. 2.23 with a  $\gamma$ , W, Z boson. See Ref. [BDG<sup>+</sup>12] for a theoretical overview of this model with specific examples for the  $Z+E_T$  final state.

Figure 4.3 shows the  $E_T$  distribution for the hadronic  $Z+E_T$  final state, with varying dark matter and mediator mass, before any selection. The acceptance for a series of simplified analysis cuts ( $E_T$ >350 GeV, leading jet  $p_T >$  40 GeV, minimum azimuthal angle between jet and  $E_T > 0.4$ ) applied at the generator level is shown in Figure 4.4.

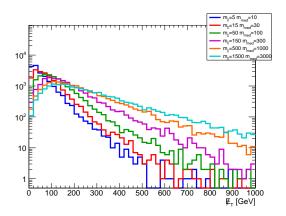


Figure 4.3: Missing transverse momentum distribution for the hadronic  $Z+E_T$  final state, for the simplified model with a colored scalar mediator exchanged in the t-channel.

#### t-scalar model acceptance

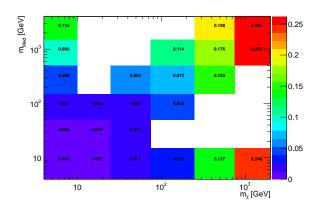


Figure 4.4: Acceptance table for the hadronic  $Z+E_T$  final state, for the simplified model with a colored scalar mediator exchanged in the t-channel.

The parameter scan for the t- channel model is still under discussion.

#### Model implementation discussed in the appendix

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#### 4.2 EFT models with direct DM-boson couplings

The EFT operators considered in this section do not have a simplified model completion for Dirac fermion Dark Matter available to date. They provide kinematic distributions that are unique to mono-boson signatures, and that in most cases are not reproduced by an equivalent simplified model <sup>1</sup>.

A complete list of effective operators with direct DM/boson couplings for Dirac DM, up to dimension 7, can be found in [CHLR13, CNS $^+$ 13, CHH15]. Higher dimensional operators, up to dimension 8, leading to Higgs+ $\rlap/E_T$  signatures, are mentioned in [CNS $^+$ 13, BLW14]. The first part of this Section outlines the main characteristics for a limited number of these models that could be considered in Run-2 searches. In the spirit of the Forum consensus to privilege simplified models, model-independent results as in Appendix D should be privileged over considering these operators as realistic

To do The parameter scan, and the conclusions that can be drawn from the plots below, need to be cross-checked with those in the monojet channel. (??)

<sup>&</sup>lt;sup>1</sup> Wherever this is the case, we recommend only generation of simplified model result as that can be reinterpreted.

#### 4.2.1 Dimension 5 operators

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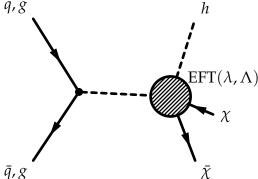
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The lowest dimension benchmark operators we consider are effective dimension 5, such as the one depicted in Figure 4.5.



Following the notation of [CNS<sup>+</sup>13], models from this category have a Lagrangian that includes terms such as:

 $\frac{m_W^2}{\Lambda_5^3} \bar{\chi} \chi W^{+\mu} W_{\mu}^- + \frac{m_Z^2}{2\Lambda_5^3} \bar{\chi} \chi Z^{\mu} Z_{\mu} , \qquad (4.1)$ 

where  $m_Z$  and  $m_W$  are the masses of the Z and W boson,  $W^\mu$  and  $Z^\mu$  are the fields of the gauge bosons,  $\chi$  denote the Dark Matter fields and  $\Lambda_5$  is the effective field theory scale . Note that these operators are of true dimension 7, but reduce to effective dimension 5 once the Higgs vacuum expectation values, contained in the W and Z mass terms, are inserted. As such, one expects these that operators would naturally arise in UV complete models where Dark Matter interacts via a Higgs portal where heavy mediators would couple to the Higgs or other fields in an extended Higgs sector. In such models the full theory may be expected to contain additional operators with Higgs-Dark Matter couplings ??.

Concentrating for the moment on mono-gauge boson signals, the above operator induces signatures with  $E_T$  in conjunction with Z and W bosons at tree level, while at loop level it induces couplings to photon pairs and  $Z\gamma$  through W loops. In these models, a clear relation exists between final states with photons, EW bosons and Higgs boson.

As shown in Fig. 4.6 kinematics of this model can be approximated by that of a simplified model including a high-mass scalar mediator exchanged in the *s*-channel described in Section 4.1.2. For this reason, the list of benchmark models with direct boson-DM

Figure 4.5: Diagram for EFT operators giving rise to a Higgs+ $\cancel{E}_T$  signature.

To do The nomenclature in different models differs from literature:  $\Lambda_5$  vs  $\lambda$  (??)

couplings for photon, Z and W only includes dimension 7 operators: the scalar model with initial state radiation of an EW boson is already recommended and its results can be rescaled.

The Higgs+ $\mathcal{E}_T$  analysis, however, will not consider the scalar simplified model as benchmark, due to the very low sensitivity in early LHC analyses, and will instead use this dimension 5 operator.

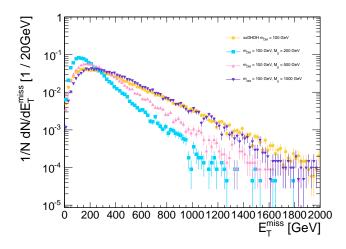


Figure 4.6: Comparison of the missing transverse momentum for the simplified model where a scalar mediator is exchanged in the s-channel and the model including a dimension-5 scalar contact operator, in the leptonic  $Z+E_T$  final state

4.2.1.1 Parameter scan

The two parameters of this model are the scale of new physics  $\lambda$  and the DM particle mass. SM-DM coupling and new physics scale are related by  $g_{\rm DM}=(246~{\rm GeV})/\lambda$ .

The initial value of the new physics scale  $\lambda$  chosen for the sample generation is 3 TeV; this is a convention and does not affect the signal kinematics; the cross-section of the samples can be rescaled according to the  $\lambda^3$  dependence when deriving the constraints on this scale. However, more care should be given when rescaling Higgs+ $E_T$  operators of higher dimensions, as different diagrams have a different  $\lambda$  dependence.

The DM mass values for the benchmark points to be simulated are chosen to span a sufficient Dark Matter range leading to different kinematics, that is within the LHC sensitivity for early searches and that is consistent across the various signatures and EFT operators. We therefore start the mass scan at  $m_{\rm DM}$  =1 GeV, where collider experiments are complementary to direct and indirect detection and choose the last point corresponding to a DM mass of 1 TeV. We recommend a scan in seven mass points, namely:

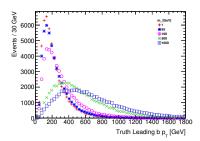
 $m_{\rm DM} = 1, 10, 50, 100, 200, 400, 800, 1300 \,\text{GeV}.$ 

A set of kinematic distributions from the Higgs+ $E_T$  signature where the Higgs decays into two b-quarks is shown in Fig. 4.7, for points similar to those of the grid scan proposed.

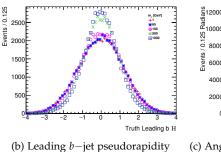
To do Clarify the reason why this happens in Madgraph through explicit Lagrangian terms? (??)

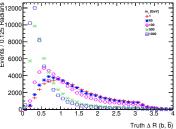
To do Waiting for plot by Bhawna Gomber showing this (??)

To do Include unpublished study of rescaling for dimension-8 operators by N. Whallon in dimension-8 section. (??)



(a) Leading b-jet transverse momentum





ing b-jet pseudorapidity (c) Angular distance between the two leading b-jets

#### 4.2.2 Dimension 7 operators

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The dimension-7 benchmark models contain the  $SU(2)_L \times U(1)_Y$  gauge-invariant couplings between DM fields and the kinetic terms of the EW bosons. The CP-conserving scalar couplings of this type can be written as

$$\frac{c_1}{\Lambda_S^3} \, \bar{\chi} \chi \, B_{\mu\nu} B^{\mu\nu} + \frac{c_2}{\Lambda_S^3} \, \bar{\chi} \chi \, W^i_{\mu\nu} W^{i,\mu\nu} \,. \tag{4.2}$$

Here  $B_{\mu\nu}=\partial_{\mu}B_{\nu}-\partial_{\nu}B_{\mu}$  and  $W^{i}_{\mu\nu}=\partial_{\mu}W^{i}_{\nu}-\partial_{\nu}W^{i}_{\mu}+g_{2}\epsilon^{ijk}W^{j}_{\mu}W^{k}_{\mu}$  are the  $U(1)_{Y}$  and  $SU(2)_{L}$  field strength tensor, respectively, and  $g_{2}$  denotes the weak coupling constant. In the case of the pseudoscalar couplings, one has instead

$$\frac{c_1}{\Lambda_P^3} \bar{\chi} \gamma_5 \chi B_{\mu\nu} \tilde{B}^{\mu\nu} + \frac{c_2}{\Lambda_P^3} \bar{\chi} \gamma_5 \chi W_{\mu\nu}^i \tilde{W}^{i,\mu\nu} , \qquad (4.3)$$

where  $\tilde{B}_{\mu\nu}=1/2\,\epsilon_{\mu\nu\lambda\rho}\,B^{\lambda\rho}$  and  $\tilde{W}^i_{\mu\nu}=1/2\,\epsilon_{\mu\nu\lambda\rho}\,W^{i,\lambda\rho}$  are the dual field strength tensors. In addition to the CP-conserving interactions (4.2) and (4.3), there are also four CP-violating couplings that are obtained from the above operators by the replacement  $\bar{\chi}\chi\leftrightarrow\bar{\chi}\gamma_5\chi$ .

The effective interactions introduced in (4.2) and (4.3) appear in models of Rayleigh DM [WY12]. Ultraviolet completions where the operators are generated through loops of states charged under  $U(1)_Y$  and/or  $SU(2)_L$  have been proposed in [WY13] and their LHC signatures have been studied in [LSWY13]. If these new charged particles are light, the high- $p_T$  gauge bosons that participate in the  $E_T$  processes considered here are able to resolve the substructure of the loops. This generically suppresses the cross sections compared to the EFT predictions [HKU13], and thus will weaken the bounds on the interaction strengths of DM and the EW gauge bosons to some extent. Furthermore, the light charged mediators may be produced on-shell in  $p_T$  collisions, rendering direct

Figure 4.7: Comparison of the kinematic distributions for the two leading b— jets (from the Higgs decay) in the model with direct interactions between the Higgs boson and the DM particle, when varying the DM mass.

LHC searches potentially more restrictive than  $E_T$  searches. Making the above statements precise would require further studies beyond the timescale of this forum.

Since for  $\Lambda_S = \Lambda_P$  the effective interactions (4.2) and (4.3) predict essentially the same value of the mono-photon, mono-Z and mono-W cross section [CNS<sup>+</sup>13, CHH15], we consider below only the former couplings. We emphasize however that measurements of the jet-jet azimuthal angle difference in  $E_T + 2j$  events may be used to disentangle whether DM couples more strongly to the combination  $B_{\mu\nu}B^{\mu\nu}$  ( $W^i_{\mu\nu}W^{i,\mu\nu}$ ) or the product  $B_{\mu\nu}\tilde{B}^{\mu\nu}$  ( $W^i_{\mu\nu}\tilde{W}^{i,\mu\nu}$ ) of field strength tensors [CHLR13, CHH15].

After EW symmetry breaking the interactions (4.2) induce direct couplings between pairs of DM particles and gauge bosons. The corresponding Feynman rule reads

$$\frac{4i}{\Lambda_S^3} g_{V_1 V_2} \left( p_1^{\mu_2} p_2^{\mu_1} - g^{\mu_1 \mu_2} p_1 \cdot p_2 \right), \tag{4.4}$$

where  $p_i$  ( $\mu_i$ ) denotes the momentum (Lorentz index) of the vector field  $V_i$  and for simplicity the spinors associated with the DM fields have been dropped. The couplings  $g_{V_iV_i}$  take the form

$$g_{\gamma\gamma} = c_w^2 c_1 + s_w^2 c_2,$$

$$g_{\gamma Z} = -s_w c_w (c_1 - c_2),$$

$$g_{ZZ} = s_w^2 c_1 + c_w^2 c_2,$$

$$g_{WW} = c_2,$$
(4.5)

with  $s_w$  ( $c_w$ ) the sine (cosine) of the weak mixing angle. Note that our coefficients  $c_1$  and  $c_2$  are identical to the coefficients  $C_B$  and  $C_W$  used in [CHH15], while they are related via  $k_1 = c_w^2 c_1$  and  $k_2 = s_w^2 c_2$  to the coefficients  $k_1$  and  $k_2$  introduced in [CNS<sup>+</sup>13]. The coefficients  $c_1$  and  $c_2$  appearing in (4.5) determine the relative importance of each of the  $E_T$  channels and their correlations. For example, one observes that:

- Only  $c_2$  enters the coupling between DM and W bosons, meaning that only models with  $c_2 \neq 0$  predict a mono-W signal;
- If  $c_1 = c_2$  the mono-photon (mono-Z) signal does not receive contributions from diagrams involving Z (photon) exchange;
- Since numerically  $c_w^2/s_w^2 \simeq 3.3$  the mono-photon channel is particularly sensitive to  $c_1$ .

#### 4.2.2.1 Parameter scan

As stated above and shown in Ref. [NCC<sup>+</sup>14], the kinematic distributions for dimension-7 scalar and pseudoscalar operators only shows small differences. This has been verified from a generator-level study: the signal acceptance after a simplified analysis selection ( $\not\!E_T$  >350 GeV, leading jet  $p_T$  > 40 GeV, minimum azimuthal difference between either of the two jets and the  $\not\!E_T$  direction > 0.4)

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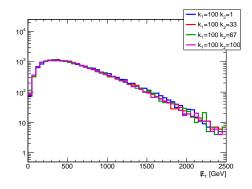
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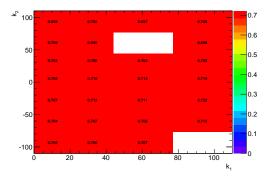
is roughly 70% for both. We therefore only suggest to generate one of the two models. TodoWhen we have the cross-sections for both, we can recommend the one with the highest cross-section.

The differences in kinematics for the various signatures are negligible when changing the coefficients  $c_1$  and  $c_2$ , as shown in Figure 4.8. Only the case  $c_1 = c_2 = 1$  is generated as benchmark; other cases are left for reinterpretation as they will only need a rescaling of the cross-sections shown in Appendix C for the various DM mass points considered.



(a) Missing transverse momentum distribution.

#### Scalar acceptance



(b) Acceptance.

#### 4.2.3 Higher dimensional operators

Many higher dimensional operators can induce signals of photons or W/Z/H bosons in the final state. A complete list can be found in Refs. [CDM $^+$ 14, BLW14, PS14] and references therein.

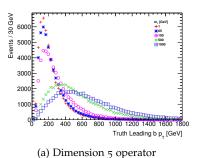
Although with lower priority with respect to the operators above, a representative dimension-8 operators can be chosen as benchmark, with the form:

$$\frac{1}{\Lambda^4}\bar{\chi}\gamma^\mu\chi B_{\mu\nu}H^\dagger D^\nu H$$

In this case, the new physics scale is  $\Lambda$  is connected with the coupling of the DM as  $y_{\chi}=\frac{1}{\Lambda^4}$ . TodoIs more detail needed here? An advantage of this operator is that it includes all signatures with

Figure 4.8:  $\mathcal{E}_T$  distribution and acceptance for the dimension-7 model with a hadronically decaying Z in the final state, for the scalar and pseudoscalar operators representing direct interactions between DM and bosons.

EW bosons, allowing to assess the relative sensitivity of the various channels with the same model. The kinematics for this operator is different with respect to other operators, leading to a harder  $E_T$  spectrum, as illustrated by comparing the leading b—jet distribution for the dimension 5 operator to the dimension 8 operator.



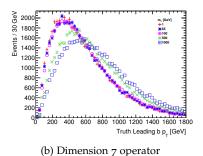


Figure 4.9: Comparison of the transverse momentum for the leading b— jet from the Higgs decay for a dimension 5 and dimension 7 operator with direct boson-DM couplings.

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4.2.4 Validity of EW contact operators and possible completions

It is important to remember that the operators described in this section may present problems in terms of the validity of the contact interaction approach for the energy scales reached at the LHC.

As outlined in [BLW14], designing very high  $\mathcal{E}_T$  search signal regions that are exclusively motivated by the hard  $\mathcal{E}_T$  spectra of the dimension 7 and 8 operators will mean that the momentum transfer in the selected events is larger. This in turn means that processes at that energy scale (mediators, particles exchanged in loops) are accessible, and a simple contact interaction will not be able to correctly describe the kinematics of these signals.

Contact interaction operators like the ones in this section remain useful tools for comparison of the sensitivity of different search channels, and for reinterpretation of other models under the correct assumptions. To date, there are no UV-complete models available for most of those operators: dimension-7 operators are particularly challenging since their completion involves loops <sup>2</sup>.

However, this may be the focus of future theoretical exploration, as discussed in Ref. [CHH15]. An example of a complete model for scalar DM corresponding to the dimension-5 operator is provided in the Appendix C. Providing results for the pure EFT limit of these models will prove useful to cross-check the implementation of future.

Given these considerations, the recommendations on the presentation of the results for these models are:

- Deliver fiducial limits on the cross section of any new physics events, without any model assumption, according to the guidelines in Appendix D.
- Assess the percentage of events that pass the EFT validity condition, and present results using a truncation of the invalid events using the procedure in Section 5 alongside pure EFT results;

To do (??)

<sup>&</sup>lt;sup>2</sup> An example case for the need of loop completions is a simplified model with an additional scalar exchanged at tree level. The scalar couples to WW and ZZ in a gauge-invariant way, Integrating out the mediator does not lead to the Lorentz structure of a dimension-7 operator, so it is not possible to generate dimension-7 operators that satisfy gauge and Lorentz invariance at the same time. A model with a spin-1 mediator cannot be considered as an candidate for completion either, since dimension-7 operators only have scalar or pseudoscalar couplings.

#### Model implementation discussed in the appendix

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4.3 Specific simplified models including EW bosons, tailored to Higgs+MET searches

Three benchmark simplified models [CDM<sup>+</sup>14, BLW14] are recommended for Higgs+ $\not$ E $_T$  searches:

- A model where a leptophobic vector mediator (Z'<sub>B</sub>) is exchanged in the s-channel, radiates a Higgs boson and decays into two DM particles (Fig. 4.10 (a));
- A model where a scalar mediator *S* couples to the SM only through the SM Higgs and decays to two DM particles (Fig. 4.11);
  - A model where a vector Z' is produced resonantly and decays into a Higgs boson plus an intermediate heavy pseudoscalar particle  $A^0$ , in turn decaying into two DM particles (Fig. 4.10 (b)).

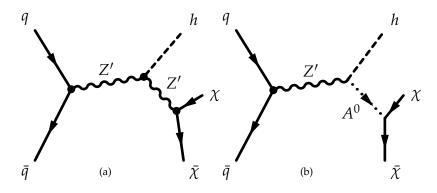


Figure 4.10: Feynman diagrams of leading order processes leading to Higgs+ $\mathcal{E}_T$  events: (a) a model with a vector mediator (Z') coupling with DM and with the Higgs boson h, and (b) a 2HDM model with a new invisibly decaying pseudoscalar  $A^0$  from the decay of an on-shell resonance Z' giving rise to a Higgs+ $\mathcal{E}_T$  signature .

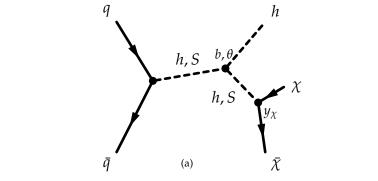
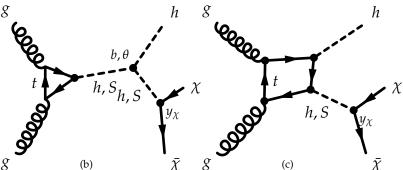


Figure 4.11: Feynman diagrams of leading order processes leading to Higgs+ $E_T$  events for a model with a scalar mediator (S) coupling with DM and with the Higgs boson h.



These models are kinematically distinct from one another, as shown in the comparison of the  $E_T$  spectra in Fig. 4.12 for high and low masses of the pseudoscalar mediator. Figure 4.12 (a) shows the  $E_T$  distribution for models with high mediator masses ( $m_S=1$  TeV,  $m_{Z'}=1$  TeV,  $m_{A^0}=1$  TeV) and DM mass of either 50 ( $Z'_B$  and  $A^0$  models) or 65 GeV (scalar mediator model). Figure 4.12 (b) shows the  $E_T$  distribution for models with low pseudoscalar mediator masses ( $m_{Z'_B}=100$  GeV,  $m_{Z'}=1$  TeV,  $m_{A^0}=100$  GeV) and DM mass of 1 TeV for all models.

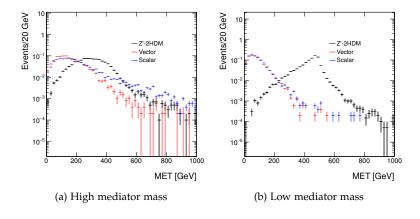


Figure 4.12: Comparison of the missing transverse momentum distributions at generator level in different simplified models leading to a Higgs+ $E_T$  signature. The model parameter settings are detailed in the

#### 4.3.1 $\not\!\!E_T$ +Higgs from a baryonic Z'

The model shown in Fig. 4.10 (a) postulates a new gauge boson Z' corresponding to a new  $U(1)_B$  baryon number symmetry. The stable baryonic states included in this model are the DM candidate particles. The mass of the Z' boson is acquired through a baryonic Higgs  $h_B$ , which mixes with the SM Higgs boson. The interactions between the Z', the quarks and the DM are described by the following Lagrangian:

$$L = g_{\mathbf{q}}\bar{q}\gamma^{\mu}qZ'_{\mu} + g_{\mathrm{DM}}\bar{\chi}\gamma^{\mu}\chi Z'_{\mu}. \tag{4.6}$$

The quark couplings  $g_q$  are fixed to be equal to one third of the gauge coupling  $g_B$ , while the DM coupling to the Z' are proportional to the baryon number and to the gauge coupling ( $g_\chi = Bg_B$ ). No leptonic couplings of the Z' are allowed, thus evading dilepton constraints. After incorporating the mixing of the baryonic and SM Higgs bosons, this model is is described by the following Lagrangian term at energies below  $m_{Z'}$ :

$$L_{\text{eff}} = -\frac{g_{\text{q}}g_{\text{DM}}}{m_{Z'}^2} \bar{q} \gamma^{\mu} q \bar{\chi} \gamma_{\mu} \chi \left( 1 + \frac{g_{hZ'Z'}}{m_{Z'}^2} h \right), \tag{4.7}$$

The first term of this equation gives rise to a term that is equivalent to the radiation of a jet (or another EW gauge boson) in the initial state. The second term describes the interaction between the Z' and the SM Higgs boson, via the coupling  $g_{hZ'Z'} = \frac{m_{Z'}2\sin\theta}{v_B}$ , where  $\sin\theta$  is the mixing angle between the SM Higgs and the baryonic Higgs  $h_B$ , and  $v_B$  is the Baryonic Higgs vev.

1297 **4.3.1.1** Parameter scan

1298 The model is described by six parameters:

- <sub>299</sub> 1. the mediator mass  $M_{\rm med}$ , (also referred to as  $m_{Z'}$ )
- $_{1300}$  2. mass of dark matter,  $m_{\rm DM}$
- 3. coupling of Z' mediator to dark matter,  $g_{DM}$
- 4. coupling of the mediator to quarks,  $g_q$
- 5. mixing angle between baryonic Higgs  $h_B$  and the SM-like Higgs boson,  $\sin \theta$
- 6. coupling of the mediator to SM-like Higgs boson,  $g_{hZ'Z'}$

The width of the Z' mediator is calculated using all possible decays to SM particles (quarks) and to pairs of DM particles if kinematically allowed.

The dependence of the missing transverse momentum ( $\not\!E_T$ ) on the model parameters is studied by varying the parameters one at a time. The variation of parameters other than  $M_{\rm med}$  and  $m_{\rm DM}$  does not result in significant variations of the  $\not\!E_T$  spectrum, as shown in Figures 4.13. Figure 4.14 shows that for an on-shell mediator, varying  $m_{\rm DM}$  with the other parameters fixed does not affect the  $\not\!E_T$  distribution, while the distribution broadens significantly in the case of an off-shell mediator. For this reason, the same grid in  $M_{\rm med}$ ,  $m_{\rm DM}$  as for the vector mediator of the jet+ $\not\!E_T$  search (Table 2.1) is chosen as a starting point. The coupling  $g_{hZ'Z'}$ , along with  $g_q$  and  $g_{\rm DM}$ , are subject to perturbativity bounds:

$$g_q, g_{\mathrm{DM}} < 4\pi$$

and

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$$g_{hZ'Z'} < \sqrt{4\pi}m_{Z'}\sin\theta$$

The value  $g_{hZ'Z'}/m_{Z'}=1.0$  is chosen as a benchmark value for the generation of Monte Carlo samples since it maximizes the cross section (as shown in the following paragraph) without violating the bounds. The mediator-DM coupling  $g_{\rm DM}$  is fixed to 1, and the mediator-quark  $g_q$  coupling is fixed to 1/3. The kinematic distributions do not change as a function of these parameters, so results for other values of  $g_{hZ'Z'}/m_{Z'}$ ,  $g_{\rm DM}$  and  $g_q$  can be obtained through rescaling by the appropriate cross sections.

Figs 4.15 and 4.16 show the kinematic distributions for the two leading jets in the  $H \to \bar{b}b$  decay channel, for two values of the mediator mass and varying the DM mass.

Analyses should perform further studies, beyond those studies performed for the forum, to estimate the reach of the analysis with respect to all points in the grid and therefore decide on a smaller set of grid points to be generated.

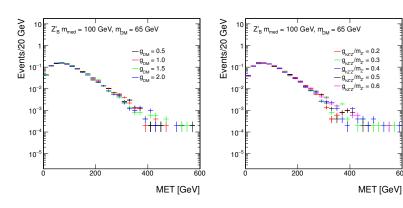


Figure 4.13: Missing transverse momentum distributions at generator level in the vector mediator scenario for different values of: the mediator-dark matter coupling  $g_{\rm DM}$  (left), and the coupling between the mediator and the SM-like Higgs boson, scaled by the mediator mass,  $g_{hZ'Z'}/m_{Z'}$  (right).

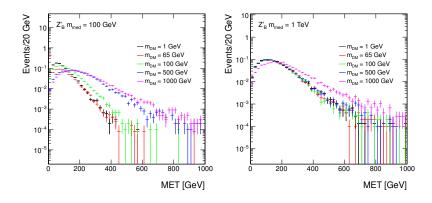
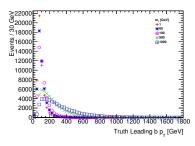
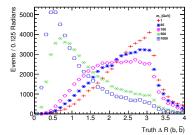


Figure 4.14: Missing transverse momentum distributions at generator level in the vector mediator scenario: for different values of the dark matter mass  $m_{\rm DM}$  and a mediator mass of  $M_{\rm med}$  = 100 GeV (left) and  $M_{\rm med}$  = 1 TeV (right).



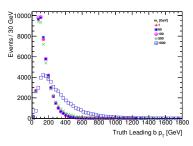
(a) Leading  $b-{\rm jet}$  transverse momentum

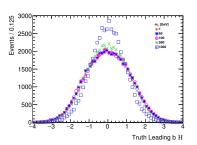
(b) Leading b-jet pseudorapidity



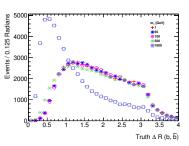
(c) Angular distance between the two leading b—jets

Figure 4.15: Comparison of the kinematic distributions for the two leading b—jets (from the Higgs decay) in the vector Z' simplified model, when fixing the Z' mass to 100 GeV and varying the DM mass.





- (a) Leading b—jet transverse momentum
- (b) Leading b-jet pseudorapidity



(c) Angular separation of the two leading b-jets

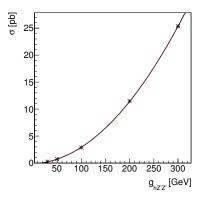
#### 4.3.1.2 Cross-section scaling

The dependence of the cross section of the  $pp \to H\chi\bar{\chi} + X$  process on  $g_{hZ'Z'}$  is shown in Figure 4.17. The curves have been fit to second-order polynomials. For  $m_{med} = 100$  GeV, the fit function is

$$y = -0.12 - 3.4 \times 10^{-3} x + 2.7 \times 10^{-4} x^2$$

. For  $m_{med} = 1$  TeV, the fit function is is

$$y = 0.0012 - 2.4 \times 10^{-7} x + 1.5 \times 10^{-7} x^2$$



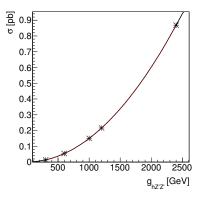


Figure 4.16: Comparison of the kinematic distributions for the two leading jets from the Higgs decay in the vector Z' simplified model, when fixing the Z' mass to 1000 GeV and varying the DM mass.

Figure 4.17: Cross section of the  $pp \to H\chi\bar{\chi}$  process as a function of  $g_{hZ'Z'}$  for  $m_{Z'} = 100$  GeV (left) and  $m_{Z'} = 1$  TeV (right). The fit functions are shown in the text.

#### 4.3.2 $\not\!\!E_T$ +Higgs from a scalar mediator

A real scalar singlet S coupling to DM can be introduced as a portal between SM and the dark sector through the Higgs field. The new scalar mixes with the SM Higgs boson, and couples to DM through a Yukawa term  $y_{\chi}$ . The relevant terms in the scalar potential are

$$V \supset a|H|^2 S + b|H|^2 S^2 + \lambda_h |H|^4$$

$$\longrightarrow \frac{1}{2} a(h+v)^2 S + \frac{1}{2} b(h+v)^2 S^2 + \frac{\lambda_h}{4} (h+v)^4, \tag{4.8}$$

where a,b are new physics couplings and  $\lambda_h$  is the Higgs quartic. The additional Lagrangian terms for this model are:

$$L \supset -y_{\chi}\bar{\chi}\chi(\cos\theta S - \sin\theta h) - \frac{m_q}{v}\bar{q}q(\cos\theta h + \sin\theta S)$$
 (4.9)

where  $\theta$  is the mixing angle between the Higgs boson and the new scalar.

Mono-Higgs signals in this second model arise through processes shown in Fig. 4.11 (a,b), or through the radiation of a Higgs boson from the t quark in the production loop, in Fig. 4.11 (c). The first two processes depend on the  $h^2S$  and  $hS^2$  cubic terms in Eq. (4.8). At leading order in  $\sin\theta$ , these terms are

$$V_{\text{cubic}} \approx \frac{\sin \theta}{v} (2m_h^2 + m_S^2) h^2 S + b v h S^2 + \dots$$
 (4.10)

with a and  $\lambda_h$  expressed in terms of  $\sin\theta$  and  $m_h^2$ , respectively. At leading order of  $\sin\theta$ , the  $h^2S$  term is fixed once the mass eigenvalues  $m_h, m_S$  and mixing angle are specified. The h  $S^2$  term is not fixed and remains a free parameter of the model, depending on the new physics coupling b.

1334 4.3.2.1 Parameter scan

<sup>1335</sup> The model is described by five parameters:

- 1. the Yukawa coupling of heavy scalar to dark matter,  $g_{\rm DM}$  (also referred to as  $y_\chi$ )
- the mixing angle between heavy scalar and SM-like Higgs boson,  $\sin \theta$ ;
- 3. the new physics coupling, b;
- 4. mass of heavy scalar,  $m_S$ , also termed  $M_{\text{med}}$ ;
- <sub>1342</sub> 5. mass of dark matter,  $m_{DM}$ ;

The mixing angle is constrained from current Higgs data to satisfy  $\cos\theta=1$  within 10% and therefore  $\sin\theta\lesssim0.4$ . This provides a starting point for the parameter scan in this model: we recommend to set  $\sin\theta=0.3$ . Figure 4.19 shows that there is no dependence of the kinematics from the value of this angle, and different values

can be obtained via rescaling the results for this mixing angle according to the relevant cross-section. It can also be observed from Figures 4.20 and 4.18 that the kinematics of this model follows that of the equivalent jet+ $\mathcal{E}_T$  model: only small changes are observed in the on-shell region, while the relevant distributions diverge when the mediator is off-shell. For this reason, the same grid in  $M_{\text{med}}$ ,  $m_{\text{DM}}$  as for the scalar mediator of the jet+ $\mathcal{E}_T$  search (Table 2.2) is chosen as a starting point. The Yukawa coupling to DM  $y_{DM}$  is set to 1, the new physics coupling between scalar and SM Higgs b = 3. Results for other values can be obtained via a rescaling of the results for these parameters.

To do Estimate the sensitivity and possibly prune parameter scan. (??)

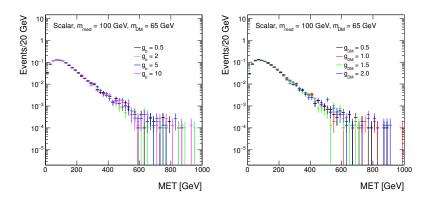


Figure 4.18: Missing transverse momentum distributions at generator level in the scalar mediator scenario, for different values of: the new physics coupling  $g_b$  (left), and the mediator-dark matter coupling  $g_{DM}$  (right).

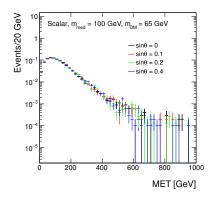


Figure 4.19: Missing transverse momentum distributions at generator level in the scalar mediator scenario: for different values of the mixing angle  $\sin \theta$ .

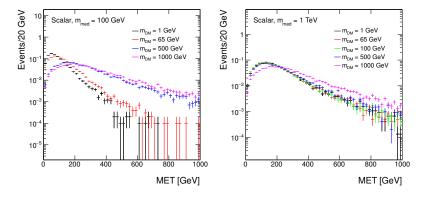


Figure 4.20: Missing transverse momentum distributions at generator level in the scalar mediator scenario: for different values of the dark matter mass  $m_{\rm DM}$  and a mediator mass of  $M_{\rm med}=100$  GeV (left) and  $M_{\rm med}=1$  TeV (right).

Figs. 4.21 and 4.22 show the kinematic distributions for the two leading jets in the  $H \to \bar{b}b$  decay channel, for two values of the mediator mass and varying the DM mass.

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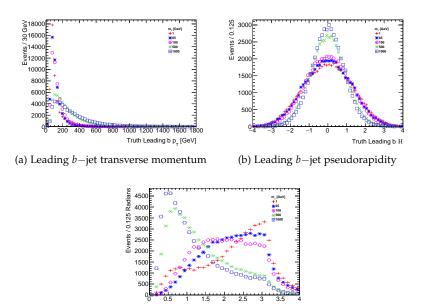
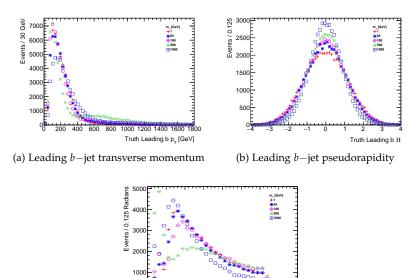


Figure 4.21: Comparison of the kinematic distributions for the two leading jets from the Higgs decay in the scalar simplified model, when fixing the new scalar mass to 100 GeV and varying the DM mass.



(c) Angular distance between the two

leading b-jets

Figure 4.22: Comparison of the kinematic distributions for the two leading jets from the Higgs decay in the scalar simplified model, when fixing the new scalar mass to 1000 GeV and varying the DM mass.

4.3.3 Higgs+ $\not$ E<sub>T</sub> signal from 2HDM model with a Z' and a new pseudoscalar

In this simplified model [BLW14], a new Z' resonance decays to a Higgs boson h plus a heavy pseudoscalar state  $A^0$  in the 2HDM

(c) Angular distance between the two

leading *b*-jets

framework, which in turn decays to a DM pair. This model is represented in the diagram in Fig. 4.10 (b).

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The motivation for coupling the dark matter to the pseudoscalar is that dark matter coupling to a Higgs or Z' boson is generically constrained by other signal channels and direct detection. An advantage of including this model is that it has different kinematics due to the on-shell Z' production, where for heavy Z' masses the  $\mathcal{E}_T$  and pT spectra are much harder. This model can satisfy electroweak precision tests and constraints from dijet resonance searches, and still give a potentially observable Higgs+ $\mathcal{E}_T$  signal.

This model comprises two doublets, where  $\Phi_u$  couples to uptype quarks and  $\Phi_d$  couples to down-type quarks and leptons:

$$-\mathcal{L} \supset y_u Q \tilde{\Phi}_u \bar{u} + y_d Q \Phi_d \bar{d} + y_e L \Phi_d \bar{e} + \text{h.c.}$$
 (4.11)

After electroweak symmetry breaking, the Higgs doublets attain vevs  $v_u$  and  $v_d$ , and in unitary gauge the doublets are parametrized as

$$\Phi_{d} = \frac{1}{\sqrt{2}} \begin{pmatrix} -\sin\beta H^{+} \\ v_{d} - \sin\alpha h + \cos\alpha H - i\sin\beta A^{0} \end{pmatrix} ,$$

$$\Phi_{u} = \frac{1}{\sqrt{2}} \begin{pmatrix} \cos\beta H^{+} \\ v_{u} + \cos\alpha h + \sin\alpha H + i\cos\beta A^{0} \end{pmatrix}$$
(4.12)

where h,H are neutral CP-even scalars and  $A^0$  is a neutral CP-odd scalar. In this framework,  $\tan\beta \equiv v_u/v_d$ , and  $\alpha$  is the mixing angle that diagonalizes the h-H mass squared matrix. We take  $\alpha=\beta-\pi/2$ , in the limit where h has SM-like couplings to fermions and gauge bosons as per Ref. [CGT13], and  $\tan\beta \geq 0.3$  as implied from the perturbativity of the top Yukawa coupling. The Higgs vevs lead to Z-Z' mass mixing, with a mixing parameter given by

$$\epsilon \equiv \frac{1}{M_{Z'}^2 - M_Z^2} \frac{gg_z}{2\cos\theta_w} (z_d v_d^2 + z_u v_u^2) 
= \frac{(M_Z^0)^2}{M_{Z'}^2 - M_Z^2} \frac{2g_z \cos\theta_w}{g} z_u \sin^2 \beta.$$
(4.13)

The production cross section for this model scales as  $(g_z)^2$ , as the decay width for this process to leading order in  $\epsilon$  (Eq. 4.13) is

$$\Gamma_{Z' \to hA^0} = (g_z \cos \alpha \cos \beta)^2 \frac{|p|}{24\pi} \frac{|p|^2}{M_{Z'}^2}.$$
 (4.14)

where the center of mass momentum for the decay products  $|p|=\frac{1}{2M_{Z'}}\lambda^{1/2}(M_{Z'}^2,m_h^2,m_{A^0}^2)$ , and  $\lambda$  is the Källen triangle function<sup>3</sup>.

$$^{3} \lambda(c_{1}, c_{2}, c_{3}) \equiv c_{1}^{2} + c_{2}^{2} + c_{3}^{2}$$
$$-2(c_{1}c_{2} + c_{2}c_{3} + c_{3}c_{1})$$

1378 4.3.3.1 Parameter scan

The model is described by five parameters:

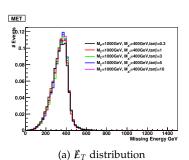
- the pseudoscalar mass  $M_{A^0}$ ,
- the DM mass  $m_{\rm DM}$

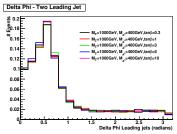
- the Z' mass,  $M_{Z'}$ ,
- $\tan \beta (\equiv v_u/v_d)$ ,

• the Z' coupling strength  $g_z$ .

To study the signal production and kinematic dependencies on these parameters, we produced signal samples varying each of the five parameters through MadGraph for the matrix element, PYTHIA for the parton shower, and DELPHES[dF<sup>+</sup>14] for a parameterized detector-level simulation.

As seen in Fig. 4.23, variations of  $\tan \beta$  does not lead to any kinematic difference and the production cross section simply scales as a function of  $\tan \beta$ . Hence we recommend to fix  $\tan \beta$  to unity in the signal generation.

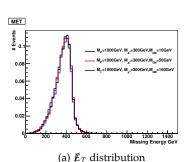


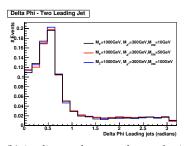


(b)  $\Delta \phi$  distance between the two b- jets

Similarly, variations of  $g_z$  do not lead to any kinematic changes. The value of  $g_z$  for a given  $M_{Z'}$  and  $\tan \beta$  can be set according to the maximum value allowed by electroweak global fits and dijet constraints, as described in [BLW14]. Since this parameter does not influence the kinematics, we leave it up to individual analyses on whether they generate benchmark points only according to these external constraints.

Since the DM pair are produced as a result of the decay of  $A^0$ , there are minimal kinematic changes when varying  $m_{\rm DM}$  as long as  $m_{\rm DM} < M_{A^0}/2$  so that  $A^0$  production is on-shell, as shown in Fig. 4.24 and 4.25 (before detector simulation).





(b)  $\Delta \phi$  distance between the two b- jets

We recommend to produce signal events for a fixed  $g_z=0.8$ ,  $\tan\beta=1$  and  $m_{\rm DM}=100$  GeV. For these values, we scan the 2-D parameter space of  $M_{Z'}, M_{A^0}$  with  $M_{Z'}=600,800,1000,1200,1400$  GeV, and  $M_{A^0}=300,400,500,600,700,800$  GeV with  $M_{A^0}< M_{Z'}-m_h$ , for a total of 24 points. The choice of scan is justified by the sensitivity study in [BLW14]: the expected LHC sensitivity for Run-2

Figure 4.23: Kinematic distributions of the signal process varying  $\tan \beta$ , in the case of a Higgs boson decaying into two b quarks, after parameterized detector simulation: no kinematic dependency is observed

Figure 4.24: Kinematic distributions of the signal process varying  $m_{\rm DM}$ : minimal kinematic dependency on  $m_{\rm DM}$  as expected when  $A^0$  is produced on-shell. Plots shown for  $M_{Z'}=1000$  GeV,  $M_{A^0}=300$  GeV.

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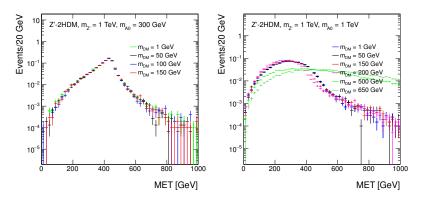


Figure 4.25: Missing transverse momentum distributions at generator level in the Z' +2HDM scenario for different values of the dark matter mass  $m_{\rm DM}$ , with  $m_{Z'}=1$  TeV and  $m_{A^0}=$ 300 GeV (left) and  $m_{A^0} = 1$  TeV (right).

is up to  $M_{Z'} \sim 1.5$  TeV. For the parameter scan, the DM mass is fixed to 100 GeV. For two  $M_{Z'}$ ,  $M_{A^0}$  value sets, we vary the DM mass to obtain sample cross section for rescaling results. All LO cross sections for the various parameter scan points are reported in Appendix C. The parameter scan excludes the off-shell region, as the cross-sections are suppressed and the LHC would not have any sensitivity to these benchmark points in early data.

The kinematic distributions with varying  $M_{Z'}$  for fixed  $M_{A^0}$ are shown in Fig. 4.26, while the dependency on  $M_{A^0}$  is shown in Fig. 4.27.

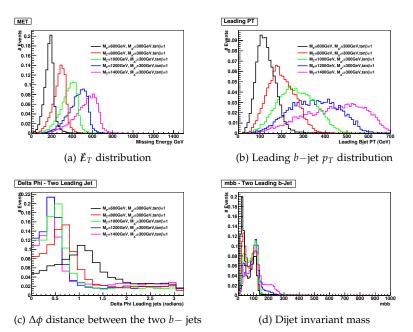


Figure 4.26: Kinematic distributions of the signal process varying  $M_{Z'}$ , for  $m_{\rm DM} = 100\,$  GeV,  $M_{A^0} = 300\,$  GeV.

This model also allows for an additional source of Higgs plus  $E_T$  signal with a similar kinematics (Fig. 4.28, shown with detector simulation samples) to the signal process from the decay of  $Z' \rightarrow$ hZ, where the Z decays invisibly. The partial decay width for the Z'is:

$$\Gamma_{Z'\to hZ} = (g_z \cos \alpha \sin \beta)^2 \frac{|p|}{24\pi} \left( \frac{|p|^2}{M_{Z'}^2} + 3 \frac{M_Z^2}{M_{Z'}^2} \right), \tag{4.15}$$

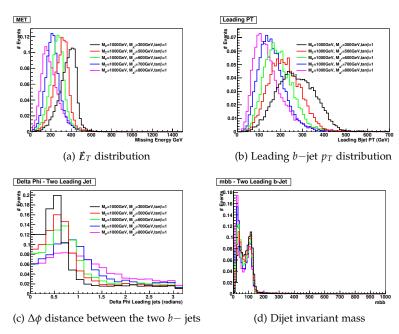


Figure 4.27: Kinematic distributions of the signal process varying  $M_{A^0}$ , for  $m_{\rm DM}=100\,$  GeV,  $M_{Z'}=1000\,$  GeV.

The values for the Z' masses scanned for those samples should follow those of the previous samples, namely values of  $M_{Z'} = 600,800,1000,1200,1400$  GeV. This signal process has no  $M_A$  dependence.

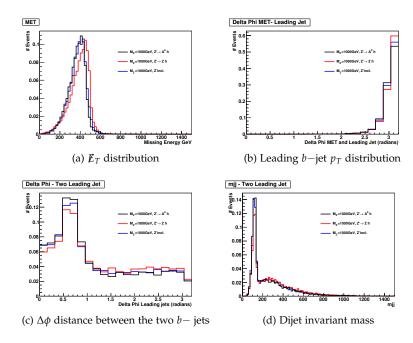


Figure 4.28: Kinematic distributions of  $Z' \to A^0 h$  exclusive production,  $Z' \to Zh$  exclusive production and Z' inclusive production for  $M_{Z'}=1000$  GeV and  $M_{A^0}=300$  GeV

IMPLEMENTATION DISCUSSED IN THE APPENDIX

# Validity of EFT approach

Effective Field Theories (EFTs) are an extremely useful framework for interpreting DM searches at the LHC. Given our current lack of knowledge about the nature of a DM particle and its interactions, a model independent interpretation of the collider bounds appears mandatory. This approach should be complemented with an interpretation within a choice of simplified models. However, these models cannot exhaust the set of possible completions of an effective Lagrangian. EFTs must be used with caution at colliders, where the energy scale of the interaction can be above the point where the EFT approximation is valid.

To illustrate the problem, consider an effective interaction

$$(\bar{\psi}\psi)(\bar{\chi}\chi)\frac{g}{\Lambda^2}$$

that couples SM and DM fields. The strength of this interaction can be parametrized by  $f=\frac{g}{\Lambda^2}$ . A monojet signature can be generated by applying perturbation theory in the QCD coupling (assuming  $\phi$  is a quark, for example). An experimental search will place a limit on f. For a fixed f, a small value of g will require a small value of  $\Lambda$ . The EFT approximation breaks down if  $Q>\Lambda$ , where Q is a typical hard scale of the process. One reasonable choice is  $Q_{\rm tr}^2=p(\bar\chi\chi)^2$ , i.e. the momentum flow through the s-channel. On the other hand, large  $\Lambda$  implies large g, raising the question if perturbation theory is even applicable.

Here we summarize some methods that can be used to ensure the validity of the EFT approximation. These methods are described in detail in Refs. [BDSMR14, BDSG<sup>+</sup>14, BDSJ<sup>+</sup>14, A<sup>+</sup>15, RWZ15]. We then propose a recommendation for the presentation of EFT results for Run-2 LHC benchmarks.

## 5.1 Outline of the procedure described in Refs. [BDSG $^+$ 14, $A^+$ 15]

A standard approach has been to consider a simplified model and work backwards to determine the validity of the EFT approximation. For a tree-level interaction between DM and the Standard Model (SM) via some mediator with mass  $M_{\rm med}$ , the EFT approximation corresponds to expanding the propagator for the mediator in powers of  $Q_{\rm tr}^2/M_{\rm med}^2$ , truncating at lowest order, and combining

To do right symbol? (??)

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the remaining parameters into a single parameter  $m_*$  (also called  $\Lambda$ in the literature). For an example scenario with a Z'-type mediator (leading to some combination of operators D<sub>5</sub> to D<sub>8</sub> in the EFT limit) this corresponds to setting

$$\frac{g_{\rm DM}g_{\rm q}}{Q_{\rm tr}^2 - M^2} = -\frac{g_{\rm DM}g_{\rm q}}{M^2} \left( 1 + \frac{Q_{\rm tr}^2}{M^2} + \mathcal{O}\left(\frac{Q_{\rm tr}^4}{M^4}\right) \right) \simeq -\frac{1}{m_*^2}, \quad (5.1)$$

where  $Q_{tr}$  is the momentum carried by the mediator, and  $g_{DM}$ ,  $g_q$ are the DM-mediator and quark-mediator couplings respectively. Similar expressions exist for other operators. Clearly the condition that must be satisfied for this approximation to be valid is that  $Q_{\rm tr}^2 < M^2 = g_{\rm DM} g_{\rm q} m_*^2$ . In this framework, there are clearly three regions to consider:

- $Q_{\rm tr}^2 \sim M^2$ , in which case the EFT misses a resonant enhancement, and it is conservative to ignore this enhancement;
- $Q_{\rm tr}^2 \ll M^2$ , in which case the EFT is valid; and
- $Q_{\rm tr}^2 \gg M^2$ , in which case the signal cross section should fall according to a power of  $Q_{\rm tr}^{-1}$  instead of  $M^{-1}$ . This is the problematic kinematic region.

We can use the condition  $Q_{\rm tr}^2 < M^2 = g_{\rm DM} g_{\rm q} m_*^2$  to restrict the kinematics of the signal and enforce the validity of the EFT approximation (after the imposition of the event selection of the analysis). This truncated signal can then be used to derive the new, truncated limit on  $m_*$  as a function of  $(m_{\rm DM}, g_{\rm DM}g_{\rm q})$ .

For the example D5-like operator,  $\sigma \propto m_*^{-4}$ , and so there is a simple rule for converting a rescaled cross section into a rescaled constraint on  $m_*$  if the original limit is based on a simple cut-andcount procedure. Defining  $\sigma_{\rm EFT}^{\rm cut}$  as the cross section truncated such that all events pass the condition  $\sqrt{g_{\rm DM}g_{\rm q}}m_*^{\rm rescaled}>Q_{\rm tr}$ , we have

$$m_*^{\text{rescaled}} = \left(\frac{\sigma_{\text{EFT}}}{\sigma_{\text{EFT}}^{\text{cut}}}\right)^{1/4} m_*^{\text{original}},$$
 (5.2)

which can be solved for  $m_*^{\text{rescaled}}$  via either iteration or a scan (note that  $m_*^{\text{rescaled}}$  appears on both the LHS and RHS of the equation). Similar relations exist for a given UV completion of each operator. The details and application of this procedure to ATLAS results can be found in Ref. [A<sup>+</sup>15] for a range of operators. Since this method uses the physical couplings and energy scale  $Q_{tr}$ , it gives the strongest possible constraints in the EFT limit while remaining robust by ensuring the validity of the EFT approximation.

If a search is not simply a counting experiment and exploits the shapes of kinematic distributions, the condition on the momentum transfer should be applied on the benchmarks using generator level information, by discarding events that are invalid. This provides the necessary rescaling of the cross section while keeping the information on the change in the kinematic distributions due to the removal of the invalid events

#### 5.2 Outline of the procedure described in Ref. [RWZ15]

In [RWZ15] a procedure to extract model independent and consistent bounds within the EFT is described. This procedure can be applied to any effective Lagrangian describing the interactions between the DM and the SM, and provides limits that can be directly reinterpreted in any completion of the EFT.

The range of applicability of the EFT is defined by a mass scale  $m_{\rm cut}$ , a parameter which marks the upper limit of the range of energy scales at which the EFT can be used reliably, independently of the particular completion of the model. Regardless of the details of the full theory, the energy scale probing the validity of the EFT is less than or equal to the center-of-mass energy  $E_{\rm cm}$ , the total invariant mass of the hard final states of the reaction. To be specific, consider the basic mono-jet process with kinematics  $p_1 + p_2 \rightarrow k + p_{\bar{\chi}\chi}$ : k is the momentum of the outgoing jet, whereas  $p_{\bar{\chi}\chi}$  is the momentum of the  $\bar{\chi}\chi$  pair and  $p_{\bar{\chi}\chi} = Q_{\rm tr}$ .  $E_{\rm cm}^2 = (p_1 + p_2)^2 > Q_{\rm tr}^2$ . The condition ensuring the validity of the EFT is, by definition of  $m_{\rm cut}$ ,

$$E_{\rm cm} < M_{\rm cut} \,. \tag{5.3}$$

For example, in the specific case of a tree level mediation with a single mediator,  $m_{\text{cut}}$  can be interpreted as the mass of that mediator.

There are then at least three free parameters describing an EFT: the DM mass  $m_{\rm DM}$ , the scale  $m_*$  of the interaction, and the cutoff scale  $m_{\rm cut}$ .

We can use the same technique as above to restrict the signal to the events for which  $E_{\rm cm} < M_{\rm cut}$ , using only these events to derive the exclusion limits on  $m_*$  as a function of  $(m_{\rm DM}, M_{\rm cut})$ . We can also define an *effective coupling strength*  $m_{\rm cut} = g_* m_*$ , where  $g_*$  is a free parameter that substitutes the parameter  $m_{\rm cut}$ , and therefore derive exclusions on  $m_*$  as a function of  $(m_{\rm DM}, g_*)$ . This allows us to see how much of the theoretically allowed parameter space has been actually tested and how much is still unexplored; For example, in the Z'-type model considered above,  $g_*$  is equal to  $\sqrt{g_{\rm DM}g_{\rm q}}$ . The resulting plots are shown in [RWZ15] for a particular effective operator.

The advantage of this procedure is that the obtained bounds can be directly and easily recast in any completion of the EFT, by computing the parameters  $m_*$ ,  $m_{\rm cut}$  in the full model as functions of the parameters of the complete theory. On the other hand, the resulting limits will be weaker than those obtained using  $Q_{\rm tr}$  and a specific UV completion.

#### 5.3 Comments on Unitarity Considerations

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#### 5.4 Recommendation for presentation of EFT results

A full discussion of the presentation of collider results is left to work beyond this Forum, where ATLAS, CMS, the theory community and the Direct and Indirect Detection communities are involved. In this report we recommend two strategies for the presentation of results in terms of Effective Field Theories. We divide the EFT operators in two categories: those which can be mapped to one or more UV-complete simplified models, such as those commonly used in LHC searches so far and detailed in [GIR+10], and those for which no UV completion is available, such as those outlined in Section 4.2. Results for the first class of operators can be recast using simplified models with high mediator masses, therefore removing the need to explicitly simulate EFT events and provide experimental limits for those operators. For the second class of models, a truncation procedure should be applied and the truncated results should be presented alongside the naive EFT results.

Three proposals for the treatment of EFT have been stated so far: (1) truncate using  $Q_{\rm tr}$ , (2) truncate and iterate using  $Q_{\rm tr}$ , and (3) truncate using  $E_{\rm cm}$ . Another possibility is to present the raw EFT results, but qualify that they might not be valid. Finally, one can quantify the validity of the EFT result by presenting the sensitivity to R, the fraction of events that satisfy  $\hat{s} > m_{\rm cut}^2$ , for example.

### 5.5 Recommendation for contact interaction theories with simplified models available

If a simplified model can be mapped to a given EFT, then the model's high-mediator-mass limit will converge to the EFT. This can be seen in Fig. 2.18, where the limits on the scale of the interaction of a Z'-like simplified model are presented in terms of the mediator mass. The limits at high mediator mass for this model are equivalent to those of the corresponding EFT benchmark. For this reason, experimental collaboration should deliver results for high-mass mediators instead of pure EFT results, and leave further reinterpretation to theorists.

We therefore recommend the addition of one point at very high mediator mass (5 TeV) to the scan, for each of the DM masses for the simplified models described in Section 2. The truncation procedure in Section 5.2 can be used to fine-tune the mediator mass to be simulated for this purpose. Studies are ongoing for s—channel vector mediators.

# 5.6 Recommendation for truncation of theories with no simplified models available

Whenever a UV completion is not available, EFT results can still be a source of useful information as described in Section 4.2.4. However, we can only naively control the validity of the EFT operator.

To do The extrapolation to other couplings and mediator masses can be done using the  $Q_{tr}$  prescription for that model. (??)

To do Is this sufficient information for reinterpretation, or should we have instructions? (??)

Despite the fact that a propagator was introduced to motivate the truncation procedure for s-channel models, the prescription is only dependent upon the simplified model to derive the energy scaling. The simple fact remains that the effective coupling of the operator –  $g/\Lambda^n$  – should not allow momentum flow  $Q>\Lambda$  or  $g>4\pi$ . Given our ignorance of the actual kinematics, the truncation procedure suggested for this purpose is the one described in Section 5.2, as it is independent from any UV completion details.

Because there is no UV completion, the parameter  $m_{\rm cut}$  can be treated more freely than an explicit function of g and  $\Lambda$ . It makes sense to choose  $m_{\rm cut}$  such that we identify the transition region where the EFT stops being a good description of UV complete theories. This can be done using the ratio R, which is defined as the fraction of events for which  $s_{hat} > m_{\rm cut}^2$ . For large values of  $m_{\rm cut}$ , no events are thrown away in the truncation procedure, and R=1. As  $m_{\rm cut}$  becomes smaller, eventually all events are thrown away in the truncation procedure, i.e. R=0, and the EFT gives no exclusion limits for the chosen acceptance.

We propose a rough scan over  $m_{\rm cut}$ , such that we find the values of  $m_{\rm cut}$  for which R ranges from 0.1 to 1. The analysis can then perform a scan over several values of  $m_{\rm cut}$ , and show the truncated limit for each one of them alongside the naive limit corresponding to R=1.

To do agree on how many? (??)

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# Recommendations for evaluation of signal theoretical uncertainties

[Comment on proper PDF sets to use, concerns about sea quark PDF in b-initiated diagrams (perhaps the latter belongs in the b-flavored DM section]

To do This section describes the technical details of how to vary input parameters, but it does not describe the overall strategy of what parameters to vary or by how much. (??)

#### 6.1 powheg

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A comprehensive and careful assessment of theoretical uncertainties plays a much more important role for the background estimations (especially when their evaluation is non-entirely datadriven) than it does for signal simulations. Nevertheless, when using POWHEG it is possible to study scale and PDF errors for the dark matter signals. A fast reweighting machinery is available in POWHEG-BOX that allows one to add, after each event, new weights according to different scale or PDF choices, without the need to regenerate all the events from scratch.

To enable this possibilty, the variable storeinfo\_rwgt should be set to 1 in the POWHEG input file when the events are generated for the first time<sup>1</sup>. After each event, a line starting with

#### #rwgt

is appended, containing the necessary information to generate extra weights. In order to obtain new weights, corresponding to different PDFs or scale choice, after an event file has been generated, a line

#### compute\_rwgt 1

should be added in the input file along with the change in parameters that is desired. For instance, renscfact and facscfact allow one to study scale variations on the renormalisation and factorisation scales around a central value. By running the program again, a new event file will be generated, named <OriginalName>-rwgt.lhe, with one more line at the end of each event of the form

#new weight,renfact,facfact,pdf1,pdf2

<sup>1</sup> Notice that even if the variable is not present, by default it is set to 1.

followed by five numbers and a character string. The first of these numbers is the weight of that event with the new parameters chosen. By running in sequence the program in the reweighting mode, several weights can be added on the same file. Two remarks are in order.

• The file with new weights is always named

```
<OriginalName>-rwgt.lhe
```

hence care has to be taken to save it as

```
1624 <OriginalName>.lhe
```

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before each iteration of the reweighting procedure.

 Due to the complexity of the environment where the program is likely to be run, it is strongly suggested as a self-consistency check that the first reweighting is done keeping the initial parameters. If the new weights are not exactly the same as the original ones, then some inconsistency must have happened, or some file was probably corrupted.

It is possible to also have weights written in the version 3 Les
Houches format. To do so, in the original run, at least the token

```
1634 lhrwgt_id 'ID'
```

must be present. The reweighting procedure is the same as described above, but now each new run can be tagged by using a different value for the lhrwgt\_id keyword. After each event, the following lines will appear:

```
1639 <rwgt>
1640 <wgt id='ID'>
1641 <wgt id='ID1'>
1642 </rwqt>
```

A more detailed explanation of what went into the computation of every single weight can be included in the <header> section of the event file by adding/changing the line

in the input card, before each "reweighting" run is performed.

Other useful keywords to group together different weights are

lhrwgt\_group\_name and lhrwgt\_group\_combine.

More detailed information can be obtained by inspecting the document in /Docs/V2-paper.pdf under the common POWHEG-BOX-V2 directory.

#### 6.2 madgraph

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# Acknowledgements

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## Α

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# Appendix: Implementation of Models

#### A.1 Mono-jet model implementation

There are several matrix element implementations of the DM production through spin-o and spin-1 mediators.

For a spin-1 mediator, the implementation in Powheg generates DM pair production with 1 parton at next-to-leading order (NLO), whilst MADGRAPH and MCFM are at leading order (LO) <sup>1</sup>. As shown in Powheg Ref. [HKR13], including NLO corrections result in an enhancement in the cross section as compared to LO and though this is not significant, it does lead to a substantial reduction in the dependence on the choice of the renormalization and factorization scale and hence the theoretical uncertainty on the signal prediction. Since NLO calculations are available for the process in Powheg, we recommend to proceed with Powheg as the generator of choice.

For a spin-o mediator, the top-quark loop is the most important consideration. The matrix element implementation of the *s*-channel spin-o mediated DM production is available in MCFM [FW13, HKSW15] and POWHEG [HR15] with the full top-loop calculation at LO. The POWHEG and MCFM implementations include the finite top quark mass dependence for DM pair production with 1 parton at LO. For consistency with the spin-1 generation, we recommend using POWHEG for this case as well.

Here, we document some specific settings needed to run the POWHEG generation for the Dark Matter models.

- POWHEG can handle the generation of events (be it at LO or NLO)
  in two different modes explained in the following. The second
  one is the recommended one. The relevant keywords in the input
  card are bornsuppfact and bornktmin.
  - 1. unweighted events:

bornsuppfact: negative or absent bornktmin <PT>

This runs the program in the most straightforward way, but most likely it is not the more convenient choice, as will be explained below. POWHEG will generate unweighted events using a sharp lower cut (with value PT) on the leading-jet  $p_{\rm T}$ . Since this is a generation cut, the user should make sure

<sup>1</sup> Spin-o and spin-1 mediator models will also be provided in the near future to the same precision in Mad-Graph5\_aMC@NLO [A+14c].

that the value used for bornktmin is lower than the actual analysis cut to be eventually used. It is good practice to use as a value in the input card a transverse momentum 10-20% smaller than the final analysis cut, and check that the final result is independent, by exploring an even smaller value of bornktmin. The drawback of this running mode is that it's difficult to populate well and in a single run both the low- $p_{\rm T}$  region as well as the high-pt tail.

#### 2. weighted events:

bornsuppfact <PTS>

bornktmin <PT>

POWHEG will now produce weighted events, thereby allowing to generate a single sample that provides sufficient statistics in all signal regions. Events are still generated with a sharp lower cut set by bornktmin, but the bornsuppfact parameter is used to set the event suppression factor according to

$$F(k_{\mathrm{T}}) = \frac{k_{\mathrm{T}}^2}{k_{\mathrm{T}}^2 + \mathrm{bornsuppfact}^2} \ . \tag{A.1}$$

In this way, the events at, for instance, low  $\mathcal{E}_T$ , are suppressed but receive an higher weight, which ensures at the same time higher statistics at high  $\mathcal{E}_T$ . We recommend to set bornsuppfact to 1000.

The bornktmin parameter allows to suppress the low  $E_T$  region even further by starting the generation at a certain value of  $k_T$  also in this runnning mode. It is recommended to set this parameter to half the lower analysis  $E_T$  cut. For instance for the event selection used in the CMS/ATLAS monojet analyses, assuming the lowest  $E_T$  region being defined above 300 GeV, the proposed value for bornktmin is 150. However, this parameter should be set keeping in mind the event selection of all the analyses that will use these signal samples and hence a threshold lower than 150 may be required.

Remove the runningwidth keyword, or set it to o, which is the
default value. Running with fixed widths is the recommended
option. Although there are limitations, this is the more straightforward, simple and transparent option, and it was used for
Forum studies.

While not recommended, the alternative, a running width for the propagator of the s-channel mediator, can be selected by setting runningwidth to 1. In this case the denominator of the mediator's propagator

$$O^2 - M^2 + i M \Gamma$$

is replaced by

$$Q^2 - M^2 + i Q^2 \frac{\Gamma}{M}$$

To do Emanuele:"On the usage of fixed or running width. It is my opinion that one should use fixed widths. Although clearly there are limitations, I think this goes into the direction of making all as simple and transparent as possible. Moreover, all the discussions in the last months aw well as the large majority of runs were done with fixed widths. Since there was some interest over the last couple of weeks, here is my suggestion for the powheg section."

- where Q is the virtuality of the mediator, and M and  $\Gamma$  are its mass and width respectively.
- Set the parameters defining the bounds on the invariant mass of the Dark Matter pair, mass\_low and mass\_high, to -1. In this way, POWHEG will assign values internally.
- The minimal values for ncall1, itmx1, ncall2, itmx2 are 250000, 5, 1000000, 5 for the DMV model, respectively.
- The minimal values for ncall1, itmx1, ncall2, itmx2 are 100000, 5, 100000, 5 for the DMS\_tloop model, respectively.
- When NLO corrections are included (as for instance in the DMV model), negative-weighted events could happen and should be kept in the event sample, hence withnegweights should be set to
   If needed, their fraction can be decreased by setting foldsci and foldy to bigger value (2 for instance). foldphi can be kept to
   1.
- Since the DMS\_tloop model is a leading order process, set L0events and bornonly are set to 1 internally.
- One can benefit from the automatic calculation of systematic uncertainties associated with the choice of hard scale and PDFs as described in Section 6.

#### 1754 A.2 Parton matching

The parton matching techniques are implemented in the mono-jet like MC generation in MADGRAPH in order to avoid double counting the partons from matrix elements and parton showering in PYTHIA 8. Based on the comparative study in Ref. [A+08], we recommend using the CKKW-L matching scheme.

#### 1760 A.2.1 Implementation of the CKKW-L matching

To illustrate the settings related to parton matching, the EFT D5 samples are generated with MadGraph5\_aMC@NL0 version 2.2.2 and showerd in PYTHIA 8.201. The technical implementation of the CKKW-L  $k_t$ -merging scheme is shown below.

• On the generator side:

ickkw = 0

ktdurham = matching scale

dparameter = 0.4

dokt = T

ptj=20

drjj=0

mmjj=0

ptj1min=0

```
On the parton showering side in PYTHIA 8.2: Merging:ktType = 1
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       Merging: TMS = matching scale
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       1000022:all = chi chi~ 2 0 0 30.0 0.0 0.0 0.0 0.0, where 2
1776
       stands for the DM particle spin and 30 stands for its mass in GeV
1777
       1000022:isVisible = false
1778
       Merging:doKTMerging = on
1779
       Merging:Process = pp>{chi,1000022}{chi~,-1000022}
1780
       Merging:nJetMax = 2
1781
```

The matching scales should be the same for the generation and par-1782 ton showering. In MADGRAPH 5aMCNLO, the particle data group ID 1783 1000022 is used for weakly interacting dark matter candidates. The 1784 dark matter particle is defined in PYTHIA 8 accordingly using the 1785 commands above that specify an invisible spin ½ particle of 30 GeV 1786 mass. The Mergin: Process command specifies the lowest parton 1787 emission process generated in MADGRAPH and Merging: nJetMax 1788 = 2 gives the maximum number of additional parton emissions 1789 with respect to the lowest parton emission process. Therefore, the following three processes need to be generated in this case:

```
p p > chi chi<sup>~</sup>

j

p p > chi chi<sup>~</sup>

j
```

Note that the MADGRAPH cards and PYTHIA 8 commands are identical for all three samples.

#### A.2.2 Matching scale

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In general, it is desired to take the hard parton emissions from the matrix element generation in MADGRAPH and allow PYTHIA 8 to take care of soft emissions only. The transition between these two regimes is defined by the matching scale and its optimal value can be determined by studying the cross-section as a function of the number of jets (differential jet rates). The differential rates  $\frac{dN_{i\rightarrow j}}{d\log_{10}(k_{\rm cut})}$  give the number of events which pass from i jets to j jets as the  $k_t$  value increases beyond  $k_{\rm cut}$ . An optimal matching scale should lead to smooth differential jet rates.

Two examples of differential jet rates, using matching scale 30 GeV and 80 GeV, from the EFT D5 sample generated as described in the previous section are given in Fig. A.1 and A.2, respectively. Although a kink is visible around the matching scale value in both cases, the 80 GeV scale leads to smoother distributions. In order to find the optimal matching scale, additional samples with matching scale 50, 70, and 90 GeV are generated as well and a detailed comparison of the differential jet rates close to the transition region is shown in Fig. A.3. The largest differences among the samples are visible for the  $1 \rightarrow 2$  jets transition where the 30 GeV and 50 GeV scale lead to a drop of the rates around the matching scale values. On the contrary, there is a hint of an increased rate around the matching scale value in the sample generated with the 90 GeV scale. Therefore, we recommend to use 80 GeV as the base-

#### line matching scale.

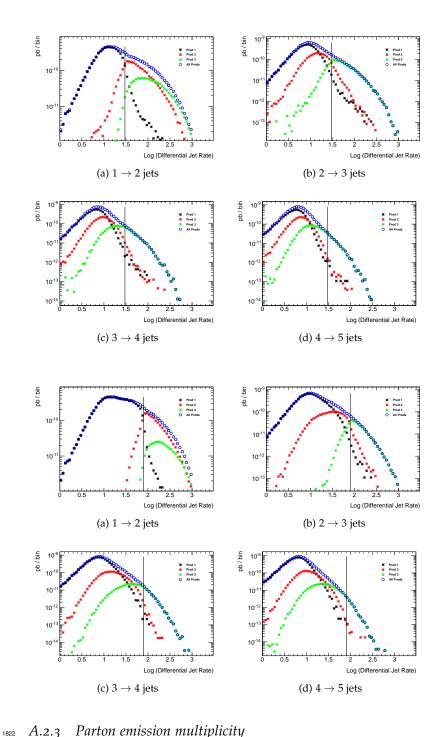


Figure A.1: Distributions of differential jet rates  $\frac{dN_{i\rightarrow j}}{d\log_{10}(k_{\text{cut}})}$  for EFT D<sub>5</sub> sample with CKKW-L matching scale at 30 GeV. The o-, 1- and 2-parton emission samples are generated separately and indicated in the plots as Prod 1, Prod 2 and Prod 3, respectively. A vertical line is drawn at the matching scale.

Figure A.2: Distributions of differential jet rates  $\frac{dN_{i\rightarrow j}}{d\log_{10}(k_{\text{cut}})}$  for EFT D5 sample with CKKW-L matching scale at 80 GeV. The o-, 1- and 2-parton emission samples are generated separately and indicated in the plots as Prod 1, Prod 2 and Prod 3, respectively. A vertical line is drawn at the matching

Parton emission multiplicity

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The prescription for the event generation given in Section A.2.1 starts with the emission of o partons and ends with maxim 2 partons in addition. Producing the samples separately allows to investigate the relative composition of the individual samples in various parts of the phase space. Figure A.4 shows the  $E_T$  distribution of the EFT D5 sample with the matching scale at 80 GeV. The plot reveals that the o-parton sample gives the dominant contribution in the region below the matching scale value that rapidly decreases

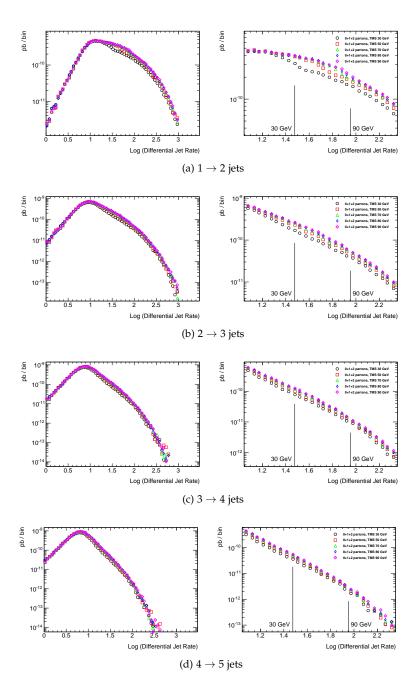


Figure A.3: Distributions of differential jet rates  $\frac{dN_{i\rightarrow j}}{d\log_{10}(k_{\rm cut})}$  for EFT D5 sample with CKKW-L matching scale at 30, 50, 70, 80 and 90 GeV. A zoom of the region around the matching scale values is shown on right.

at higher  $E_T$ . Assuming the lowest analysis  $E_T$  cut in Run-2 monojet analyses at 300 GeV, the generation of the o-parton emission sample can be safely omitted as it only gives < 1% contribution at  $E_T > 300$  GeV. For the 1- and 2-parton emission samples, one can use a generator cut on the leading parton  $p_T$ , ptj1min, in order to avoid generating low  $E_T$  events that are irrelevant for the analysis.

In order to describe the signal kinematics correctly and save time during MC production, the parton emissions will only be generated up to a certain multiplicity. The higher multiplicity samples usually have small enough cross sections and the corresponding parts of the phase space can be sufficiently approximated by parton showering in PYTHIA 8. A dedicated study comparing samples generated with up to 1-, 2-, or 3-parton multiplicities was performed, using

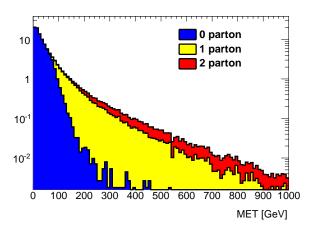


Figure A.4: Missing transverse momentum distributions for EFT D5 sample with CKKW-L matching scale at 80 GeV. Individual contributions from the o-, 1- and 2-parton emission samples are shown.

again the settings for the CKKW-L  $k_t$ -merging with the 80 GeV matching scale and the Merging:nJetMax parameter adjusted accordingly. Figure A.5 shows the  $\not\!E_T$  distribution of the samples at  $\not\!E_T > 250$  GeV.

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With an event selection requiring  $\not E_T$  and the leading jet  $p_T$  being larger than 250 GeV and allowing for up to 4 jets with  $p_T > 30$  GeV, the sample generated with up to 1 parton has 17.4% smaller yield compared to the sample with up to 3 partons, while the yield of the sample with up to 2 partons is only 2.2% smaller. This justifies it is sufficient to produce samples with up to 2 parton emissions only at the generator level and ignore generating higher parton emissions.

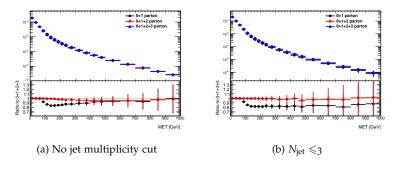


Figure A.5: Missing transverse momentum distributions for EFT D5 sample with CKKW-L matching scale at 80 GeV produced with maximum 1 (black), 2 (red) and 3 (blue) partons emitted at the generator level. The ratios are shown with respect to the latter sample.

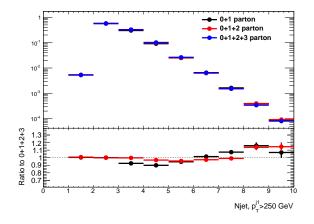


Figure A.6: Multiplicity of jets with  $p_T > 30$  GeV and  $|\eta < 2.8$  for EFT D5 sample with CKKW-L matching scale at 80 GeV produced with maximum 1 (black), 2 (red) and 3 (blue) partons emitted at the generator level. The ratios are shown with respect to the latter sample. The leading jet  $p_T$  is required to be larger than 250 GeV.

#### $_{5}$ A.3 Simplified models for EW final states.

These models are generated at leading order with MadGraph 2.2.2, using Pythia8 for the parton shower. Parameter cards can be found on the Forum SVN repository [For15a].

To do Add models and instructions for other final states (??)

#### A.4 Model implementation for mono-Higgs models

All three Higgs+ $E_T$  models are generated at leading order with MADGRAPH 2.2.2, using PYTHIA 8 for the parton shower. The MAD-GRAPH implementations of the scalar and vector models can be found on the Forum SVN repository [For15f], while the 2HDM model can be found at this link [For15b].

In all cases, it is recommended not to handle the h decay through MADGRAPH as it does not include the proper h branching ratios, or, if using MADGRAPH, then the resulting cross section should be rescaled to match onto the correct branching ratio.

Madgraph details for scalar mediator Higgs+MET model In this model, the contribution from the gghS box is included through an effective Lagrangian evaluated in the large  $m_t$  limit. This may overestimate the rates of the  $h + \not\!\!E_T$  signal [HKU13], but a

#### MADGRAPH DETAILS FOR 2HDM HIGGS+MET MODEL

The two couplings that can be changed in the Madgraph model follow the nomenclature below:

• Tb -  $\tan \beta$ 

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• gz -  $g_z$ , gauge coupling of Z' to quarks

full evaluation is left to future studies.

The other couplings are not changed, including gx (the  $A\bar{\chi}\chi$  coupling) which has little impact on the signal.  $\sin\alpha$  is fixed internally such that  $\cos(\beta-\alpha)=0$ . The width of the Z' and A can be computed automatically within Madgraph. The couplings here don't affect the signal kinematics, so they can be fixed to default values and then the signal rates can be scaled appropriately.

The nomenclature for the masses in the Madgraph model is:

- MZp PDG ID 32 Z'
- MAO PDG ID 28 A
- MX PDG ID 1000022 dark matter particle

The other masses are unchanged and do not affect the result. Both  $Z' \to hZ(\bar{\nu}\nu)$  and  $Z' \to hA(\bar{\chi}\chi)$  contribute to the final state, scaling different with model parameters. We recommend to generate them separately, and then add the two signal processes together weighted by cross sections.

#### A.5 Heavy Flavor Models

In this particular model we recommend an additional care when choosing the flavor scheme generation. It is found that the best modeling of two *b*-quarks final states is achieved using a 4-flavor scheme and a massive treatment of the *b*-quarks . In addition, we recommend to calculate the cross sections of these models in the 5-flavor scheme, and as in the *tbart* case we provide values for the suggested coupling scan in the appendix. The PDF used to calculate these cross section is NNPDF3.0 (lhaid 263000).

To do [TODO: Add reference] (??)

To do [TODO: The following figures are placeholders for now and will be added later] (??)

Figure A.7: Comparison of the subleading jet  $p_T$  and b-jet multiplicity for bb+DM scalar model generated in the 4-flavor (left) and 5-flavor (right) schemes, respectively

### A.6 Single Top Models

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Card files for MADGRAPH are provided on the Forum SVN repos-1905 itory [For15d], corresponding to the Lagrangian from [AFM11]. 1906 Each coupling constant of this model can be set via the parameter 1907 card and the blocks which are relevant for the two models used for 1908 the experimental searches are described below. The relevant pa-1909 rameters in the MADGRAPH parameter cards, also expressed in the 1910 notation introduced in the previous Section, are as follows for the 1911 two models considered. 1912

- 1913 1. Resonant scalar model described by the Lagrangian (3.2)
  - AQS and BQS:  $3 \times 3$  matrices (flavour space) fixing the coupling of the scalar  $\phi$  (S stands for scalar) and *down*-type quarks (Q stands for quarks), previously called  $a^q/b_{SR}^q$ .
    - A12S and B12S:  $3 \times 1$  matrices (flavor space) fixing the coupling of the new fermion  $\chi$  (where 12 stands for spin-1/2 fermion) and up-type quarks, previously called  $a_{VR}^{1/2}$ .
- 2. Non-resonant vectorial model described by the Lagrangian (3.4)
  - A1FC and B1FC:  $3 \times 3$  matrices (flavor space) fixing the coupling of the vector V (1 stands for vector) and up-type quarks, previously called  $a_{FC}^1$ .
    - particle name: the dark matter candidate  $\chi$  is not implemented

The width of the scalar resonance and of the new vector are set to all allowed decays in the ATLAS implementation, while the only allowed decay in the CMS implementation to the new fermion and a top quark for the resonant model.

To do Continue discussion between ATLAS and CMS to reach an agreement, or include instructions to compare results. (??)

# • A.7 EFT Mono-Higgs implementation

These models are generated at leading order with Madgraph 2.2.2, using Pythia 8 for the parton shower. No matching is performed. Parameter cards can be found on the Forum SVN repository: [For15f] for operators with Higgs+MET final states and [For15c] for  $W/Z/\gamma$  final states.

# 1936 A.8 Simplified Models of Mono-Higgs

These models are generated at leading order with MADGRAPH
2.2.2, using PYTHIA 8 for the parton shower. No matching is performed. Parameter cards can be found on the Forum SVN repository [For15b, For15f].

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# Appendix: Table of cross sections for $t\bar{t}+\not\!\!E_T$ searches

### <sup>943</sup> B.1 Relic density constraints for b—flavored Dark Matter

For Dirac fermion DM the relic density is governed primarily by the *s*-wave annihilation cross section, which is given approximately given by:

$$\langle \sigma v \rangle = \frac{3g^4}{32\pi} \frac{m_{\chi}^2 \sqrt{1 - (m_b/m_{\chi})^2}}{\left(m_{\Phi}^2 + m_{\chi}^2 - m_b^2\right)} \approx \frac{3g^4 m_{\chi}^2}{32\pi (m_{\Phi}^2 + m_{\chi}^2)}$$
 (B.1)

We assume  $\langle \sigma v \rangle = 1.5$  pb.

Figure B.1 shows the couplings for various dark matter and mediator massed required to obtain the correct relic density observed in the early universe.

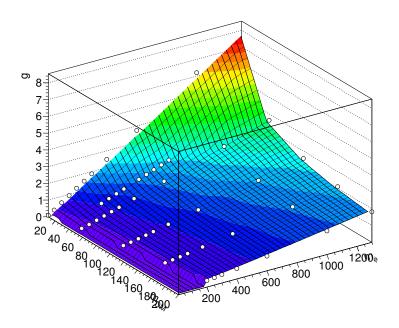


Figure B.1: Coupling constants required to obtain correct relic density in the early universe.

 $m_{\underline{\chi}}$  $\sigma$  [pb]  $m_{\underline{\chi}}$  $m_{\Phi}$  $\sigma$  [pb]  $m_{\Phi}$ 5.48E-03 1.23E-01 1.91E-02 4.94E-03 8.90E-04 7.82E-04 6.66E+oo 2.66E-03 9.86E+00 6.48E-01 1.69E+00 7.67E+00 4.12E+00 9.41E-01 1.11E+00 1.16E-01 1.30E-01 9.75E+00 4.56E+00 5.8oE-03 7.84E+01 2.22E+00 4.09E-01 1.19E+00 3.76E-01 9.53E-04 3.95E+01 2.24E-01 2.12E+01 1.37E-01 9.92E+00 8.62E-02 4.57E+00 5.54E-02 1.20E+00 5.72E-03 1.59E+02 3.25E+01 1.38E-01 9.34E-04 5.22E-03 2.84E+01 1.84E+o1 8.37E-04 6.64E-03 9.52E+00 1.87E+00 4.49E+00 1.17E+00 3.86E+00 3.35E+00 7.06E-02 1.03E+00 1.36E-01

Table B.1: Dark matter masses  $m_\chi$  and mediator masses  $m_\Phi$  generated for g=1 for 13 TeV. The resulting production cross sections are given in pb.

#### $^{948}$ B.2 Cross sections for b-flavored Dark Matter

### $^{1949}$ B.3 Cross sections for the $t\bar{t}+DM$ scalar simplified model

Table B.3: Cross section calculation for each coupling choice and minimal width assumption for the  $t\bar{t}$ +DM scalar simplified model grid

Coupling (g)	$m_{Phi}$ [GeV]	$m_{\chi}$ [GeV]	$\Gamma_{min}$ [GeV]	$\sigma$ [pb]
0.1	10	1	0.00374	$0.1955 \pm 0.00066$
0.1	20	1	0.00785	$0.1054 \pm 0.00031$
0.1	50	1	0.0199	$0.03011 \pm 9.1e-05$
0.1	100	1	0.0398	0.006867 $\pm$ 2.5e-05
0.1	200	1	0.0797	$0.0009397 \pm 2.6e-06$
0.1	300	1	0.120	$0.0002942 \pm 1e-06$
0.1	500	1	0.311	$5.289 ext{e-}05 \pm 1.9 ext{e-}07$
0.1	1000	1	0.881	$3.717e-06 \pm 1.5e-08$

Table B.3 – continued from previous page

Coupling (g)	$m_{Phi}$ [GeV]	$m_{\chi}$ [GeV]	rom previous $\Gamma_{min}$ [GeV]	$\sigma$ [pb]
0.1	2000	1	1.91	$7.81$ e-08 $\pm$ 3.2e-10
0.1	5000	1	4.89	1.111e-11 ± 5.5e-14
0.1	10	10	6.33	$9.418e-06 \pm 3.6e-08$
0.1	50	10	0.0153	$0.03016 \pm 8.1\text{e-}05$
0.1	100	10	0.0375	$0.00686 \pm 2.2e-05$
0.1	5000	10	4.89	1.095e-11 ± 5.8e-14
0.1	15	10	3.84	$1.2e-05 \pm 4.8e-08$
0.1	10	50	6.33	$1.914e-07 \pm 7.2e-10$
0.1	50	50	2.34e-05	$2.323e-07 \pm 8.8e-10$
0.1	200	50	0.0518	0.0009421 $\pm$ 2.8e-06
0.1	300	50	0.100	0.0002954 $\pm$ 9.8e-07
0.1	5000	50	4.88	1.059e-11 $\pm$ 5.3e-14
0.1	95	50	4.66e-05	$6.548 ext{e-o7} \pm 2.3 ext{e-o9}$
0.1	10	150	6.33	$8.684\text{e-09} \pm 4.1\text{e-11}$
0.1	200	150	0.000107	$1.296 ext{e-}08 \pm 5.3 ext{e-}11$
0.1	500	150	0.214	$3.92e ext{-}05 \pm 1.6e ext{-}07$
0.1	5000	150	4.87	9.079e-12 ± 5.9e-14
0.1	295	150	0.000185	$3.969e-08 \pm 2e-10$
0.1	10	500	6.33	$7.367e$ -11 $\pm$ 3.2e-13
0.1	500	500	0.112	$9.86e$ -11 $\pm$ $3.9e$ -13
0.1	2000	500	1.63	$5.953\text{e-}08 \pm 2.3\text{e-}10$
0.1	5000	500	4.77	$5.768$ e-12 $\pm$ 2.6e-14
0.1	995	500	0.480	$8.67e$ -10 $\pm$ 3.6e-12
0.1	10	1000	6.33	$6.576e$ -13 $\pm$ 2.8e-15
0.1	1000	1000	0.483	$9.426e-13 \pm 4.2e-15$
0.1	5000	1000	4.43	$4.314e$ -12 $\pm$ 2e-14
0.1	1995	1000	1.11	$1.589e$ -11 $\pm$ 9.2e-14
0.3	10	1	0.0337	$1.766 \pm 0.006$
0.3	20	1	0.0706	$0.9493 \pm 0.0029$
0.3	50	1	0.179	$0.2695 \pm 0.00082$
0.3	100	1	0.358	$0.06159 \pm 0.00021$
0.3	200	1	0.717	$0.008466 \pm 2.4e-05$
0.3	300	1	1.08	$0.002649 \pm 8.5 e-06$
0.3	500	1	2.80	$0.0004741 \pm 1.6e-06$
0.3	1000	1	7.93	$3.349e-05 \pm 1.3e-07$
0.3	2000	1	17.2	$7.227e-07 \pm 3.2e-09$
0.3	5000	1	44.0	$5.42e-10 \pm 3.5e-12$
0.3	10	10	5.70	$0.0007633 \pm 2.5e-06$
0.3	50	10	0.138	$0.2706 \pm 0.00082$
0.3	100	10	0.337	$0.06182 \pm 0.00022$
0.3	5000	10	44.0	$5.386e-10 \pm 2.7e-12$
0.3	15	10	3.45e-05	$0.0009761 \pm 3.6e-06$
0.3	10	50	5.70	$1.561e-05 \pm 6.1e-08$
0.3	50	50	0.000210	$1.892e-05 \pm 7.3e-08$
0.3	200	50	0.466	$0.008444 \pm 2.2e-05$

Table B.3 – continued from previous page

Coupling (g)	$m_{Phi}$ [GeV]	$m_{\chi}$ [GeV]	from previous $\Gamma_{min}$ [GeV]	$\sigma$ [pb]
0.3	300	50	0.902	o.oo2677 ± 7.7e-o6
0.3	5000	50	44.0	$5.012e-10 \pm 3.1e-12$
0.3	95	50	0.000420	5.306e-05 ± 2.3e-07
0.3	10	150	5.70	$7.02e-07 \pm 3.3e-09$
0.3	200	150	0.000962	$1.051e-06 \pm 4.1e-09$
0.3	500	150	1.92	0.000351 ± 1.3e-06
0.3	5000	150	43.9	$3.805$ e-10 $\pm$ 2.4e-12
0.3	295	150	0.00166	$3.211e-06 \pm 1.5e-08$
0.3	10	500	5.70	$5.945 ext{e-09} \pm 2.7 ext{e-11}$
0.3	500	500	1.01	$7.991 ext{e-}09 \pm 4.9 ext{e-}11$
0.3	2000	500	14.7	$5.347 \text{e-o}7 \pm 2.3 \text{e-o}9$
0.3	5000	500	42.9	$1.264e$ -10 $\pm$ 6.9e-13
0.3	995	500	4.32	$7.039e-08 \pm 3e-10$
0.3	10	1000	5.70	$5.302e$ -11 $\pm$ 2.4e-13
0.3	1000	1000	4.35	$7.606e$ -11 $\pm$ $3.4e$ -13
0.3	5000	1000	39.8	$4.887e$ -11 $\pm$ 2.1e-13
0.3	1995	1000	10.0	$1.279  ext{e-09} \pm 6.4  ext{e-12}$
0.7	10	1	0.183	$9.624 \pm 0.034$
0.7	20	1	0.384	$5.129 \pm 0.015$
0.7	50	1	0.974	$1.461 \pm 0.0048$
0.7	100	1	1.95	$0.3324 \pm 0.0014$
0.7	200	1	3.90	$0.04588 \pm 0.00013$
0.7	300	1	5.86	$0.01442 \pm 5e-05$
0.7	500	1	15.2	$0.002548 \pm 9.6e-06$
0.7	1000	1	43.2	$0.0001813 \pm 8.9e-07$
0.7	2000	1	93.7	$4.478e-06 \pm 1.9e-08$
0.7	5000	1	239	$1.504e-08 \pm 6.7e-11$
0.7	10	10	3.10e-05	$0.02264 \pm 8.3 \text{e-}05$
0.7	50	10	0.752	$1.462 \pm 0.0041$
0.7	100	10	1.84	$0.3347 \pm 0.0011$
0.7	5000	10	239	$1.494e-08 \pm 6.7e-11$
0.7	15	10	0.000188	$0.02881 \pm 0.00011$
0.7	10	50	3.10e-05	$0.0004597 \pm 1.8e-06$
0.7	50	50	0.00114	$0.0005588 \pm 2.3e-06$
0.7	200	50	2.54	$0.0458 \pm 0.00013$
0.7	300	50	4.91	$0.01433 \pm 4.9e-05$
0.7	5000	50	239	$1.363e-08 \pm 6.9e-11$
0.7	95	50	0.00228	$0.00157 \pm 7.3e-06$
0.7	10	150	3.10e-05	$2.097e-05 \pm 8.5e-08$
0.7	200	150	0.00524	$3.123e-05 \pm 1.6e-07$
0.7	500	150	10.5	$0.001889 \pm 6.8e-06$
0.7	5000	150	239	$1.018e-08 \pm 5.2e-11$
0.7	295	150	0.00906	$9.511e-05 \pm 4e-07$
0.7	10	500	3.10e-05	$1.78e-07 \pm 6.8e-10$
0.7	500	500	5.48	2.373e-07 ± 9.8e-10

Table B.3 – continued from previous page

Coupling (g)	$m_{Phi}$ [GeV]		$\Gamma_{min}$ [GeV]	$\sigma$ [pb]
0.7	2000	500	80.0	2.877e-06 ± 1.2e-08
0.7	5000	500	234	2.682e-09 ± 1.7e-11
0.7	995	500	23.5	1.939e-06 ± 7.3e-09
0.7	10	1000	3.10e-05	1.584e-09 ± 7.6e-12
0.7	1000	1000	23.7	2.26e-09 ± 1.1e-11
0.7	5000	1000	217	$5.244e$ -10 $\pm$ 2.4e-12
0.7	1995	1000	54.52	$3.227e-08 \pm 1.4e-10$
1.	10	1	0.374	$19.59 \pm 0.062$
1.	20	1	0.785	$10.48 \pm 0.03$
1.	50	1	1.99	$2.941 \pm 0.0091$
1.	100	1	3.98	$0.6723 \pm 0.0024$
1.	200	1	7.97	$0.09327 \pm 0.00029$
1.	300	1	12.0	$0.0295 \pm 0.00011$
1.	500	1	31.1	$0.00518 \pm 2.2e-05$
1.	1000	1	88.1	$0.0003687 \pm 1.7e-06$
1.	2000	1	191	$1.034e-05 \pm 4.6e-08$
1.	5000	1	489	$6.17e-08 \pm 2.4e-10$
1.	10	10	6.33e-05	$0.09487 \pm 0.00036$
1.	50	10	1.53	$2.942 \pm 0.0083$
1.	100	10	3.75	$0.6732 \pm 0.0023$
1.	5000	10	489	$6.138\text{e-}08 \pm 2.3\text{e-}10$
1.	15	10	0.000384	$0.1202 \pm 0.0005$
1.	10	50	6.33e-05	$0.001906 \pm 8.4e-06$
1.	50	50	0.00234	$0.002329 \pm 1e-05$
1.	200	50	5.18	$0.09224 \pm 0.00025$
1.	300	50	10.0	$0.02901 \pm 0.0001$
1.	5000	50	488	$5.616e-08 \pm 2.2e-10$
1.	95	50	0.00466	$0.006558 \pm 2.7e-05$
1.	10	150	6.33e-05	$8.634e-05 \pm 4e-07$
1.	200	150	0.0107	$0.00013 \pm 5.7e-07$
1.	500	150	21.4	$0.003754 \pm 1.9e-05$
1.	5000	150	487	$4.162e-08 \pm 1.8e-10$
1.	295	150	0.0185	0.000394 ± 1.6e-06
1.	10	500	6.33e-05	$7.356e-07 \pm 3.3e-09$
1.	500	500	11.2	$9.894e-07 \pm 5e-09$
1.	2000	500	163	$5.808e-06 \pm 2.4e-08$
1.	5000	500	477	$1.048e-08 \pm 5.7e-11$
1.	995	500	48.0	$7.3e-06 \pm 3.2e-08$
1.	10	1000	6.33e-05	$6.607e-09 \pm 2.7e-11$
1.	1000	1000	48.3	$9.433e-09 \pm 4e-11$
1.	5000	1000	443	1.7e-09 ± 1e-11
1.	1995	1000	111	1.108e-07 ± 5.7e-10
1.5	10	1	0.842	$44.1 \pm 0.16$
1.5	20	1	1.77	$23.19 \pm 0.078$
1.5	50	1	4.47	$6.471 \pm 0.02$

Table B.3 – continued from previous page

Coupling (g)	$m_{Phi}$ [GeV]	$m_{\chi}$ [GeV]	from previous $\Gamma_{min}$ [GeV]	$\sigma$ [pb]
1.5	100	1	8.96	1.478 ± 0.0061
1.5	200	1	17.9	$0.2074 \pm 0.00068$
1.5	300	1	26.9	$0.0657 \pm 0.00024$
1.5	500	1	69.9	$0.01123 \pm 5.6$ e-05
1.5	1000	1	198	$0.0008135 \pm 3.5e-06$
1.5	2000	1	430	2.873e-05 ± 1.2e-07
1.5	5000	1	1099	2.964e-07 ± 1.2e-09
1.5	10	10	0.000143	$0.4772 \pm 0.0019$
1.5	50	10	3.45	$6.499 \pm 0.022$
1.5	100	10	8.43	$1.469 \pm 0.0056$
1.5	5000	10	1099	$2.932e-07 \pm 1.3e-09$
1.5	15	10	0.000863	$0.613 \pm 0.0022$
1.5	10	50	0.000143	$0.009661 \pm 3.4 e-05$
1.5	50	50	0.00526	$0.0118 \pm 4.2e-05$
1.5	200	50	11.7	$0.2032 \pm 0.00064$
1.5	300	50	22.6	$0.06446 \pm 0.00024$
1.5	5000	50	1099	$2.687e-07 \pm 1.2e-09$
1.5	95	50	0.0105	$0.03298 \pm 0.00013$
1.5	10	150	0.000143	$0.0004384 \pm 1.8e-06$
1.5	200	150	0.0241	$0.0006557 \pm 2.7e-06$
1.5	500	150	48.1	$0.008036 \pm 3.9e-05$
1.5	5000	150	1097	$2.008e-07 \pm 1.4e-09$
1.5	295	150	0.0416	$0.002022 \pm 8.3e-06$
1.5	10	500	0.000143	$3.712e-06 \pm 1.5e-08$
1.5	500	500	25.2	$5.001e-06 \pm 1.9e-08$
1.5	2000	500	367	$1.223e-05 \pm 6e-08$
1.5	5000	500	1072	$4.885$ e-08 $\pm$ 2.7e-10
1.5	995	500	108	$2.975e-05 \pm 1.5e-07$
1.5	10	1000	0.000143	$3.342e-08 \pm 1.5e-10$
1.5	1000	1000	109	$4.786$ e-08 $\pm$ 2.1e-10
1.5	5000	1000	996	$6.688e-09 \pm 3.1e-11$
1.5	1995	1000	250	$3.982e-07 \pm 2.2e-09$
2.	10	1	1.50	$78.28 \pm 0.3$
2.	20	1	3.14	$40.52 \pm 0.13$
2.	50	1	7.95	$11.12 \pm 0.038$
2.	100	1	15.9	$2.531 \pm 0.011$
2.	200	1	31.9	$0.3644 \pm 0.0012$
2.	300	1	47.8	$0.1157 \pm 0.00053$
2.	500	1	124	0.01917 ± 9e-05
2.	1000	1	353	$0.001382 \pm 6.1e-06$
2.	2000	1	765	5.899e-05 ± 2.7e-07
2.	5000	1	1954	$8.392e-07 \pm 3.4e-09$
2.	10	10	0.0002532	$1.509 \pm 0.0052$
2.	50	10	6.14	$11.19 \pm 0.037$
2.	100	10	15.0	$2.513 \pm 0.0091$

Table B.3 – continued from previous page

2. 5000 10 1954 8.317e-07 ± 3.6e-09 2. 15 10 0.00153 1.923 ± 0.0066 2. 10 50 0.000253 0.03065 ± 0.00011 2. 50 50 0.00934 0.03716 ± 0.00018 2. 200 50 20.7 0.3487 ± 0.0011 2. 300 50 40.1 0.1114 ± 0.0041 2. 5000 50 1953 7.612e-07 ± 4e-09 2. 95 50 0.0187 0.1045 ± 0.0005 2. 10 150 0.000253 0.001376 ± 6.3e-06 2. 200 150 0.00428 0.002081 ± 9.1e-06 2. 5000 150 1950 5.605e-07 ± 3e-09 2. 5000 150 1950 5.605e-07 ± 3e-09 2. 295 150 0.0740 0.006316 ± 2.8e-05 2. 205 500 44.8 1.586e-05 ± 8.6e-08 2. 200 50 653 1.953e-05 ± 9.5e-08 2. 200 500 653 1.953e-05 ± 9.5e-08 2. 200 500 653 1.953e-05 ± 9.5e-08 2. 200 500 1907 1.3339e-07 ± 6.5e-10 2. 995 500 192 7.427e-05 ± 3.9e-07 2. 10 1000 0.000253 1.056e-07 ± 5e-10 2. 100 1000 193 1.507e-07 ± 6.7e-10 2. 1995 1000 445 8.764e-07 ± 5.3e-09 2. 1995 1000 1771 1.624e-08 ± 6.7e-11 2. 1995 1000 445 8.764e-07 ± 5.3e-09 2.5 10 1 2.34 122.2 ± 0.44 2.5 20 1 4.99 61.98 ± 0.21 2.5 50 1 12.4 16.62 ± 0.057 2.5 50 1 12.4 16.62 ± 0.057 2.5 50 1 12.4 16.62 ± 0.007 2.5 500 1 194 0.02816 ± 0.00011 2.5 500 1 194 0.02816 ± 0.00011 2.5 500 1 194 0.02816 ± 0.00011 2.5 500 1 194 0.02816 ± 0.00011 2.5 500 1 194 0.02816 ± 0.00011 2.5 500 1 194 0.02816 ± 0.00011 2.5 500 1 194 0.02816 ± 0.00011 2.5 500 1 194 0.02816 ± 0.00011 2.5 500 1 194 0.02816 ± 0.00011 2.5 500 1 194 0.02816 ± 0.00011 2.5 500 1 194 0.02816 ± 0.00011 2.5 500 1 194 0.02816 ± 0.00011 2.5 500 1 194 0.02816 ± 0.00011 2.5 500 1 194 0.02816 ± 0.00011 2.5 500 1 194 0.02816 ± 0.00011 2.5 500 1 195 0.000396 0.07571 ± 0.00038 2.5 500 1 195 0.000396 0.07571 ± 0.00038 2.5 500 50 0.0146 0.09133 ± 0.00038 2.5 500 50 0.0291 0.2247 ± 0.0008 2.5 500 50 0.0291 0.2247 ± 0.0008 2.5 500 50 0.0291 0.2247 ± 0.0008 2.5 500 50 0.00096 0.00396 ± 1.7e-05 2.5 500 150 0.0068 0.00398	Coupling (g)	$m_{Phi}$ [GeV]	$m_{\chi}$ [GeV]	rom previous $\Gamma_{min}$ [GeV]	$\sigma$ [pb]
2.	2.	5000	10	1954	8.317e-07 ± 3.6e-09
2.	2.	15	10		
2.         50         50         0.00934         0.03716 $\pm$ 0.00018           2.         200         50         20.7         0.3487 $\pm$ 0.0011           2.         300         50         40.1         0.1114 $\pm$ 0.00041           2.         5000         50         1953         7.612e-07 $\pm$ 4e-09           2.         95         50         0.0187         0.1045 $\pm$ 0.0005           2.         10         150         0.00253         0.001376 $\pm$ 6.3e-06           2.         200         150         0.0428         0.002081 $\pm$ 9.1e-06           2.         200         150         0.0428         0.002081 $\pm$ 9.1e-06           2.         200         150         0.0740         0.006316 $\pm$ 2.8e-05           2.         2000         150         0.0740         0.006316 $\pm$ 2.8e-05           2.         205         150         0.000253         1.177e-05 $\pm$ 4.8e-08           2.         200         500         44.8         1.586e-05 $\pm$ 8.6e-08           2.         200         500         44.8         1.586e-05 $\pm$ 8.6e-08           2.         2000         500         1907         1.333e-07 $\pm$ 5-9-10           2.         1000 <t< td=""><td>2.</td><td></td><td>50</td><td></td><td></td></t<>	2.		50		
2. $300$ $50$ $40.1$ $0.1114 \pm 0.00041$ 2. $5000$ $50$ $1953$ $7.612e-07 \pm 4e-09$ 2. $95$ $50$ $0.0187$ $0.1045 \pm 0.0005$ 2. $10$ $150$ $0.000253$ $0.001376 \pm 6.3e-06$ 2. $200$ $150$ $0.0428$ $0.002081 \pm 9.1e-06$ 2. $500$ $150$ $0.5428$ $0.002081 \pm 9.1e-06$ 2. $500$ $150$ $0.5428$ $0.002081 \pm 9.1e-06$ 2. $500$ $150$ $1950$ $5.605e-07 \pm 3e-09$ 2. $295$ $150$ $0.0740$ $0.006316 \pm 2.8e-05$ 2. $295$ $150$ $0.0740$ $0.006316 \pm 2.8e-05$ 2. $500$ $500$ $500$ $0.000253$ $1.177e-05 \pm 4.8e-08$ 2. $500$ $500$ $653$ $1.953e-05 \pm 9.5e-08$ 2. $500$ $500$ $653$ $1.953e-05 \pm 9.5e-08$ 2. $500$ $500$ $1907$ $1.333e-07 \pm 6.5e-10$ 2. $995$ $500$ $1907$ $1.333e-07 \pm 6.5e-10$ 2. $995$ $500$ $192$ $7.427e-05 \pm 3.9e-07$ 2. $10$ $1000$ $0.000253$ $1.056e-07 \pm 5e-10$ 2. $1000$ $1000$ $193$ $1.507e-07 \pm 6.7e-10$ 2. $1000$ $1000$ $1771$ $1.624e-08 \pm 6.7e-11$ 2. $1995$ $1000$ $445$ $8.764e-07 \pm 5.3e-09$ 2.5 $10$ $1$ $2.34$ $122.2 \pm 0.44$ 2.5 $20$ $1$ $4.90$ $61.98 \pm 0.21$ 2.5 $20$ $1$ $4.90$ $61.98 \pm 0.21$ 2.5 $300$ $1$ $12.4$ $16.62 \pm 0.057$ 2.5 $300$ $1$ $194$ $0.02816 \pm 0.00021$ 2.5 $300$ $1$ $194$ $0.02816 \pm 0.00021$ 2.5 $300$ $1$ $194$ $0.02816 \pm 0.00014$ 2.5 $100$ $1$ $100$ $100$ $100$ $1194$ $100$ $100$ $100$ $100$ $1195$ $100$ $100$ $1195$ $100$	2.	50	50	0.00934	
2. $5000$ $50$ $1953$ $7.612e-07 \pm 4e-09$ 2. $95$ $50$ $0.0187$ $0.1045 \pm 0.0005$ 2. $10$ $150$ $0.000253$ $0.001376 \pm 6.3e-06$ 2. $200$ $150$ $0.0428$ $0.002081 \pm 9.1e-06$ 2. $500$ $150$ $0.955$ $0.01343 \pm 5.5e-05$ 2. $500$ $150$ $1950$ $5.605e-07 \pm 3e-09$ 2. $295$ $150$ $0.0740$ $0.00616 \pm 2.8e-05$ 2. $295$ $150$ $0.000253$ $1.177e-05 \pm 4.8e-08$ 2. $2000$ $500$ $44.8$ $1.586e-05 \pm 8.6e-08$ 2. $5000$ $500$ $44.8$ $1.586e-05 \pm 8.6e-08$ 2. $2000$ $500$ $653$ $1.953e-05 \pm 9.5e-08$ 2. $2000$ $500$ $1907$ $1.333e-07 \pm 6.5e-10$ 2. $2995$ $500$ $1907$ $1.333e-07 \pm 6.5e-10$ 2. $1000$ $1000$ $1.000253$ $1.056e-07 \pm 5e-10$ 2. $1000$ $10000$ $193$	2.				
2.       95       50 $0.0187$ $0.1045 \pm 0.0005$ 2.       10       150 $0.000253$ $0.001376 \pm 6.3e-06$ 2.       200       150 $0.0428$ $0.002081 \pm 9.1e-06$ 2.       500       150 $85.5$ $0.01343 \pm 5.5e-05$ 2.       5000       150 $1950$ $5.605e-07 \pm 3e-09$ 2.       295       150 $0.0740$ $0.06316 \pm 2.8e-05$ 2.       10       500 $0.000253$ $1.177e-05 \pm 4.8e-08$ 2.       500       500 $44.8$ $1.586e-05 \pm 8.6e-08$ 2.       2000       500 $653$ $1.953e-05 \pm 9.5e-08$ 2.       2000       500 $653$ $1.953e-05 \pm 9.5e-08$ 2.       2000       500 $1907$ $1.333e-07 \pm 6.5e-10$ 2.       2995       500 $192$ $7.427e-05 \pm 3.9e-07$ 2.       100 $1000$ $1.000253$ $1.056e-07 \pm 5e-10$ 2.       1995       500 $192$ $7.427e-0.5 \pm 3.9e-07$ 2.       100 $10000$ $193$ $1.507e-07 \pm 6.7e-10$	2.	300	50	40.1	$0.1114 \pm 0.00041$
2.         10         150 $0.002253$ $0.001376 \pm 6.3e-06$ 2.         200         150 $0.0428$ $0.002081 \pm 9.1e-06$ 2.         500         150 $85.5$ $0.01343 \pm 5.5e-05$ 2.         5000         150 $1950$ $5.605e-07 \pm 3e-09$ 2.         295         150 $0.0740$ $0.006316 \pm 2.8e-05$ 2.         295         150 $0.000253$ $1.177e-05 \pm 4.8e-08$ 2.         500         500 $44.8$ $1.586e-05 \pm 8.6e-08$ 2.         2000         500 $653$ $1.933e-05 \pm 9.5e-08$ 2.         2000         500 $1907$ $1.333e-07 \pm 6.5e-10$ 2.         2995         500 $192$ $7.427e-05 \pm 3.9e-07$ 2.         100         1000 $0.000253$ $1.056e-07 \pm 5e-10$ 2.         100         1000 $0.000253$ $1.056e-07 \pm 5e-10$ 2.         1000         1000 $193$ $1.507e-07 \pm 6.7e-10$ 2.         1000         1000 $1771$ $1.624e-08 \pm 6.7e-10$	2.	5000	50	1953	$7.612e-07 \pm 4e-09$
2.       200       150 $0.0428$ $0.002081 \pm 9.1e-06$ 2.       500       150 $85.5$ $0.01343 \pm 5.5e-05$ 2.       5000       150       1950 $5.605e-07 \pm 3e-09$ 2.       295       150 $0.0740$ $0.006316 \pm 2.8e-05$ 2.       10       500 $0.000253$ $1.177e-05 \pm 4.8e-08$ 2.       500       500       44.8 $1.586e-05 \pm 8.6e-08$ 2.       2000       500       653 $1.93e-05 \pm 9.5e-08$ 2.       2000       500       1907 $1.333e-07 \pm 6.5e-10$ 2.       2000       500       1907 $1.333e-07 \pm 6.5e-10$ 2.       100       1000 $0.000253$ $1.056e-07 \pm 5.9e-09$ 2.       10       1000 $0.000253$ $1.056e-07 \pm 5.9e-00$ 2.       10       1000 $0.000253$ $1.056e-07 \pm 5.9e-10$ 2.       10       1000 $0.000253$ $1.056e-07 \pm 6.7e-10$ 2.       10       1.000 $1.000$ $1.000$ $1.000$ 2.       10       1.000 $1.000$ $1.000$ $1.000$	2.	95	50	0.0187	$0.1045 \pm 0.0005$
2.       500       150       85.5 $0.01343 \pm 5.5e-05$ 2.       5000       150       1950 $5.605e-07 \pm 3e-09$ 2.       295       150 $0.0740$ $0.006316 \pm 2.8e-05$ 2.       10       500 $0.000253$ $1.177e-05 \pm 4.8e-08$ 2.       500       500       44.8 $1.586e-05 \pm 8.6e-08$ 2.       2000       500       653 $1.953e-05 \pm 9.5e-08$ 2.       2000       500       1907 $1.333e-07 \pm 6.5e-10$ 2.       3000       500       1907 $1.333e-07 \pm 6.5e-10$ 2.       100       1000 $0.000253$ $1.056e-07 \pm 9.5e-08$ 2.       100       1000 $0.000253$ $1.056e-07 \pm 9.5e-01$ 2.       100       1000 $0.000253$ $1.056e-07 \pm 5.9e-01$ 2.       100       1000 $1.000253$ $1.056e-07 \pm 5.9e-01$ 2.       100       1000 $1.000253$ $1.056e-07 \pm 6.7e-10$ 2.       100       1000 $1.000253$ $1.056e-07 \pm 6.7e-10$ 2.       1095       1000 $1.0000200000$ $1.0000000000000$ </td <td>2.</td> <td>10</td> <td>150</td> <td>0.000253</td> <td><math>0.001376 \pm 6.3e-06</math></td>	2.	10	150	0.000253	$0.001376 \pm 6.3e-06$
2. $5000$ $150$ $1950$ $5.605e-07 \pm 3e-09$ 2. $295$ $150$ $0.0740$ $0.006316 \pm 2.8e-05$ 2. $10$ $500$ $0.000253$ $1.177e-05 \pm 4.8e-08$ 2. $500$ $500$ $44.8$ $1.586e-05 \pm 8.6e-08$ 2. $2000$ $500$ $653$ $1.953e-05 \pm 9.5e-08$ 2. $5000$ $500$ $1907$ $1.333e-07 \pm 6.5e-10$ 2. $995$ $500$ $192$ $7.427e-05 \pm 3.9e-07$ 2. $100$ $1000$ $193$ $1.507e-07 \pm 6.7e-10$ 2. $1000$ $1000$ $193$ $1.507e-07 \pm 6.7e-10$ 2. $1000$ $1000$ $1771$ $1.624e-08 \pm 6.7e-11$ 2. $1995$ $1000$ $1471$ $1.624e-08 \pm 6.7e-11$ 2. $1995$ $1000$ $1771$ $1.624e-08 \pm 6.7e-10$ 2. $1995$ $1000$ $1771$ $1.624e-08 \pm 6.7e-11$ 2. $1995$ $1000$ $1771$ $1.624e-08 \pm 6.7e-11$ 2. $1000$ $11000$ $1000$	2.	200	150	0.0428	$0.002081 \pm 9.1e-06$
2.       295       150 $0.0740$ $0.06316 \pm 2.8e-05$ 2.       10       500 $0.000253$ $1.177e-05 \pm 4.8e-08$ 2.       500       500 $44.8$ $1.586e-05 \pm 8.6e-08$ 2.       2000       500 $653$ $1.953e-05 \pm 9.5e-08$ 2.       5000       500 $1907$ $1.333e-07 \pm 6.5e-10$ 2.       995       500 $192$ $7.427e-05 \pm 3.9e-07$ 2.       10 $1000$ $0.000253$ $1.056e-07 \pm 5.9e-07$ 2. $1000$ $1000$ $193$ $1.507e-07 \pm 6.7e-10$ 2. $5000$ $1000$ $1771$ $1.624e-08 \pm 6.7e-11$ 2. $1995$ $1000$ $145$ $8.764e-07 \pm 5.3e-09$ 2.5 $10$ $1$ $2.34$ $122.2 \pm 0.44$ 2.5 $10$ $1$ $2.34$ $122.2 \pm 0.44$ 2.5 $20$ $1$ $4.90$ $61.98 \pm 0.21$ 2.5 $10$ $1$ $24.9$ $3.788 \pm 0.016$ 2.5 $100$ $1$ $24.9$ $3.788 \pm 0.016$ 2	2.	500	150	85.5	$0.01343 \pm 5.5 \text{e-}05$
2. 10 500 0.000253 1.177e-05 ± 4.8e-08 2. 500 500 44.8 1.586e-05 ± 8.6e-08 2. 2000 500 653 1.953e-05 ± 9.5e-08 2. 5000 500 1907 1.333e-07 ± 6.5e-10 2. 995 500 192 7.427e-05 ± 3.9e-07 2. 10 1000 0.000253 1.056e-07 ± 5e-10 2. 1000 1000 1771 1.624e-08 ± 6.7e-10 2. 5000 1000 1771 1.624e-08 ± 6.7e-11 2. 1995 1000 445 8.764e-07 ± 5.3e-09 2.5 10 1 2.34 122.2 ± 0.44 2.5 20 1 4.90 61.98 ± 0.21 2.5 500 1 12.4 16.62 ± 0.057 2.5 100 1 24.9 3.788 ± 0.016 2.5 200 1 49.8 0.551 ± 0.0021 2.5 300 1 74.7 0.1762 ± 0.00073 2.5 500 1 194 0.02816 ± 0.00014 2.5 1000 1 551 0.001971 ± 8.5e-06 2.5 2000 1 1195 9.628e-05 ± 4.1e-07 2.5 5000 1 3053 1.685e-06 ± 6.9e-09 2.5 10 10 23.4 3.755 ± 0.014 2.5 500 10 3053 1.68e-06 ± 6.7e-09 2.5 10 10 23.4 3.755 ± 0.014 2.5 500 10 3053 1.68e-06 ± 6.7e-09 2.5 500 50 3024 0.07571 ± 0.00038 2.5 500 50 3052 1.519e-06 ± 8e-09 2.5 500 50 3052 1.519e-06 ± 8e-09 2.5 500 50 0.0291 0.2547 ± 0.00089 2.5 500 50 0.0291 0.2547 ± 0.00089 2.5 10 150 0.000396 0.003396 ± 1.7e-05	2.	5000	150	1950	$5.605$ e-07 $\pm$ 3e-09
2. $500$ $500$ $44.8$ $1.586e-05 \pm 8.6e-08$ 2. $2000$ $500$ $653$ $1.953e-05 \pm 9.5e-08$ 2. $5000$ $500$ $1907$ $1.333e-07 \pm 6.5e-10$ 2. $995$ $500$ $192$ $7.427e-05 \pm 3.9e-07$ 2. $1000$ $1000$ $1.056e-07 \pm 5e-10$ 2. $1000$ $1000$ $193$ $1.507e-07 \pm 6.7e-10$ 2. $1000$ $1000$ $1771$ $1.624e-08 \pm 6.7e-11$ 2. $1995$ $1000$ $445$ $8.764e-07 \pm 5.3e-09$ 2.5 $10$ $1$ $2.34$ $122.2 \pm 0.44$ 2.5 $20$ $1$ $4.90$ $61.98 \pm 0.21$ 2.5 $20$ $1$ $4.90$ $61.98 \pm 0.21$ 2.5 $20$ $1$ $4.90$ $61.98 \pm 0.21$ 2.5 $20$ $1$ $4.9.8$ $0.551 \pm 0.057$ 2.5 $100$ $1$ $24.9$ $3.788 \pm 0.016$ 2.5 $300$ $1$ $74.7$ $0.1762 \pm 0.00073$ 2.5       <	2.	295	150	0.0740	$0.006316 \pm 2.8 e-05$
2.       2000       500       653       1.953e-05 $\pm$ 9.5e-08         2.       5000       500       1907       1.333e-07 $\pm$ 6.5e-10         2.       995       500       192       7.427e-05 $\pm$ 3.9e-07         2.       10       1000       0.000253       1.056e-07 $\pm$ 5e-10         2.       1000       1000       193       1.507e-07 $\pm$ 6.7e-10         2.       5000       1000       1771       1.624e-08 $\pm$ 6.7e-11         2.       1995       1000       445       8.764e-07 $\pm$ 5.3e-09         2.5       10       1       2.34       122.2 $\pm$ 0.44         2.5       20       1       4.90       61.98 $\pm$ 0.21         2.5       50       1       12.4       16.62 $\pm$ 0.057         2.5       100       1       24.9       3.788 $\pm$ 0.016         2.5       200       1       49.8       0.551 $\pm$ 0.0021         2.5       300       1       74.7       0.1762 $\pm$ 0.00073         2.5       500       1       194       0.02816 $\pm$ 0.00014         2.5       1000       1       551       0.001971 $\pm$ 8.5e-06         2.5       2000       1       1195       9	2.	10	500	0.000253	$1.177e-05 \pm 4.8e-08$
2. $5000$ $500$ $1907$ $1.333e-07 \pm 6.5e-10$ 2. $995$ $500$ $192$ $7.427e-05 \pm 3.9e-07$ 2. $100$ $1000$ $193$ $1.507e-07 \pm 6.7e-10$ 2. $5000$ $1000$ $1771$ $1.624e-08 \pm 6.7e-11$ 2. $1995$ $1000$ $445$ $8.764e-07 \pm 5.3e-09$ 2.5 $10$ $1$ $2.34$ $122.2 \pm 0.44$ 2.5 $20$ $1$ $4.90$ $61.98 \pm 0.21$ 2.5 $50$ $1$ $12.4$ $16.62 \pm 0.057$ 2.5 $100$ $1$ $24.9$ $3.788 \pm 0.016$ 2.5 $200$ $1$ $49.8$ $0.551 \pm 0.0021$ 2.5 $300$ $1$ $74.7$ $0.1762 \pm 0.00073$ 2.5 $500$ $1$ $194$ $0.02816 \pm 0.00073$ 2.5 $500$ $1$ $194$ $0.02816 \pm 0.00074$ 2.5 $1000$ $1$ $195$ $9.628e-05 \pm 4.1e-07$ 2.5 $5000$ $1$ $3053$ $1.685e-06 \pm 6.9e-09$	2.	500	500	44.8	$1.586\text{e-}05 \pm 8.6\text{e-}08$
2.       995       500       192 $7.427e-05 \pm 3.9e-07$ 2.       10       1000 $0.000253$ $1.056e-07 \pm 5e-10$ 2.       1000       1000 $193$ $1.507e-07 \pm 6.7e-10$ 2.       5000       1000 $1771$ $1.624e-08 \pm 6.7e-11$ 2.       1995       1000       445 $8.764e-07 \pm 5.3e-09$ 2.5       10       1 $2.34$ $122.2 \pm 0.44$ 2.5       20       1 $4.90$ $61.98 \pm 0.21$ 2.5       50       1 $12.4$ $16.62 \pm 0.057$ 2.5       100       1 $24.9$ $3.788 \pm 0.016$ 2.5       200       1 $49.8$ $0.551 \pm 0.0021$ 2.5       300       1 $74.7$ $0.1762 \pm 0.00073$ 2.5       500       1 $194$ $0.02816 \pm 0.00014$ 2.5       500       1 $194$ $0.02816 \pm 0.00014$ 2.5       2000       1 $1195$ $9.628e-05 \pm 4.1e-07$ 2.5       5000       1 $3053$ $1.685e-06 \pm 6.9e-09$ 2.5       50       10 <td< td=""><td>2.</td><td>2000</td><td>500</td><td>653</td><td><math>1.953 \text{e-}05 \pm 9.5 \text{e-}08</math></td></td<>	2.	2000	500	653	$1.953 \text{e-}05 \pm 9.5 \text{e-}08$
2.       10       1000       0.000253       1.056e-07 $\pm$ 5e-10         2.       1000       1000       193       1.507e-07 $\pm$ 6.7e-10         2.       5000       1000       1771       1.624e-08 $\pm$ 6.7e-11         2.       1995       1000       445       8.764e-07 $\pm$ 5.3e-09         2.5       10       1       2.34       122.2 $\pm$ 0.44         2.5       20       1       4.90       61.98 $\pm$ 0.21         2.5       50       1       12.4       16.62 $\pm$ 0.057         2.5       100       1       24.9       3.788 $\pm$ 0.016         2.5       200       1       49.8       0.551 $\pm$ 0.0021         2.5       300       1       74.7       0.1762 $\pm$ 0.00073         2.5       500       1       194       0.02816 $\pm$ 0.00014         2.5       1000       1       551       0.001971 $\pm$ 8.5e-06         2.5       2000       1       1195       9.628e-05 $\pm$ 4.1e-07         2.5       5000       1       3053       1.685e-06 $\pm$ 6.9e-09         2.5       50       10       9.59       16.9 $\pm$ 0.016         2.5       50       10       3053       1.68e-06	2.	5000	500	1907	$1.333 \text{e-o7} \pm 6.5 \text{e-1o}$
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Table B.3 – continued from previous page

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3. $200$ 50 $46.61$ $0.7242 \pm 0.0023$
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3. 5000 50 4395 2.394e-06 $\pm$ 1.4e-08
3. 95 50 0.04196 0.5301 $\pm$ 0.0019
3. 10 150 0.0005698 0.007036 $\pm$ 3.3e-05
3. 200 150 0.09621 0.01053 $\pm$ 4.4e-05
3. 500 150 192.4 $0.02598 \pm 0.00012$
3. 5000 150 4387 1.767e-06 $\pm$ 1.2e-08
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3. 10 500 0.0005698 5.989e-05 $\pm$ 2.7e-07
3. 500 500 100.7 $7.985e-05 \pm 3.1e-07$
3. 2000 500 1469 3.073e-05 $\pm$ 1.6e-07
3. 5000 500 4290 3.921e-07 $\pm$ 1.8e-09
3. 995 500 432.1 0.0002263 $\pm$ 9.7e-07
3. 10 1000 0.0005698 5.337e-07 $\pm$ 2.3e-09
3. 1000 1000 435.1 $7.512e-07 \pm 4.1e-09$

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Table B.3	e – continued	trom	previous page	

Coupling (g)	$m_{Phi}$ [GeV]	$m_{\chi}$ [GeV]	$\Gamma_{min}$ [GeV]	$\sigma$ [pb]
3.	5000	1000	3984	4.011e-08 ± 1.7e-10
3.	1995	1000	1001	$2.15 \text{e-}06 \pm 1 \text{e-}08$
3.5	10	1	4.585	$242 \pm 0.94$
3.5	20	1	9.611	$116.6 \pm 0.36$
3.5	50	1	24.34	$29.39 \pm 0.093$
3.5	100	1	48.77	$6.585 \pm 0.027$
3.5	200	1	97.6	$0.993 \pm 0.0042$
3.5	300	1	146.4	$0.3235 \pm 0.0019$
3.5	500	1	380.8	$0.04713 \pm 0.00021$
3.5	1000	1	1080	$0.00299 \pm 1.5 e-05$
3.5	2000	1	2341	$0.0001649 \pm 6.2e$ -07
3.5	5000	1	5984	$3.53e-06 \pm 1.8e-08$
3.5	10	10	0.0007756	$14.23 \pm 0.052$
3.5	50	10	18.79	$30.44 \pm 0.11$
3.5	100	10	45.91	$6.51 \pm 0.024$
3.5	5000	10	5984	$3.514e-06 \pm 1.3e-08$
3.5	15	10	0.004699	$18.1 \pm 0.067$
3.5	10	50	0.0007756	$0.2893 \pm 0.0011$
3.5	50	50	0.02861	$0.3505 \pm 0.0017$
3.5	200	50	63.45	$0.9325 \pm 0.0035$
3.5	300	50	122.8	$0.2972 \pm 0.0014$
3.5	5000	50	5982	$3.185e-06 \pm 1.7e-08$
3.5	95	50	0.05711	$0.981 \pm 0.0043$
3.5	10	150	0.0007756	$0.01295 \pm 6.7e-05$
3.5	200	150	0.131	$0.01947 \pm 8.7e-05$
3.5	500	150	261.9	$0.03264 \pm 0.00016$
3.5	5000	150	5971	$2.316e-06 \pm 1.3e-08$
3.5	295	150	0.2265	$0.05947 \pm 0.00026$
3.5	10	500	0.0007756	0.0001104 $\pm$ 4.8e-07
3.5	500	500	137.1	0.0001486 $\pm$ 7.1e-07
3.5	2000	500	2000	$3.401e-05 \pm 1.5e-07$
3.5	5000	500	5839	$5.061$ e-07 $\pm$ 2.6e-09
3.5	995	500	588.1	$0.0003275 \pm 1.4e-06$
3.5	10	1000	0.0007756	$9.835e-07 \pm 4.7e-09$
3.5	1000	1000	592.2	$1.401e-06 \pm 7.5e-09$
3.5	5000	1000	5423	$4.878\text{e-}08 \pm 2.5\text{e-}10$
3.5	1995	1000	1363	2.809e-06 ± 1.2e-08

Table B.4: Cross section calculation for each coupling choice and minimal width assumption for the  $t\bar{t}$ +DM pseudoscalar simplified model grid

Coupling (g)	$m_{Phi}$ [GeV]	$m_{\chi}$ [GeV]	$\Gamma_{min}$ [GeV]	σ [pb]
0.1	10	1	0.004	0.004237 ± 1.8e-05

Table B.4 – continued from previous page

Coupling (g)	$m_{Phi}$ [GeV]	$m_{\chi}$ [GeV]	$\Gamma_{min}$ [GeV]	$\sigma$ [pb]
0.1	20	1	0.008	0.003931 ± 1.5e-05
0.1	50	1	0.02	0.003005 ± 1.4e-05
0.1	100	1	0.04	$0.001905 \pm 8.1e-06$
0.1	200	1	0.08	$0.0008608 \pm 3.3 e$ -06
0.1	300	1	0.12	$0.0004105 \pm 1.6e-06$
0.1	500	1	0.413	$5.591 ext{e-}05 \pm 2.2 ext{e-}07$
0.1	1000	1	0.949	$3.961e-06 \pm 1.7e-08$
0.1	2000	1	1.95	$7.961e-08 \pm 3.2e-10$
0.1	5000	1	4.9	1.19e-11 $\pm$ 7.1e-14
0.1	10	10	2.0	$1.489e-06 \pm 9.6e-09$
0.1	50	10	0.018	$0.003 \pm 1.5 e{-}05$
0.1	100	10	0.04	$0.001926 \pm 1e-05$
0.1	5000	10	4.9	$1.179e$ -11 $\pm$ 6.2e-14
0.1	15	10	5.9	1.798e-06 $\pm$ 1e-08
0.1	10	50	2.0	$2.42e ext{-07} \pm 1.1e ext{-09}$
0.1	50	50	2.5e-05	$2.97 ext{e-o7} \pm 1.2 ext{e-o9}$
0.1	200	50	0.069	$0.0008585 \pm 4.7e-06$
0.1	300	50	0.11	$0.0004108 \pm 1.7 e\text{-}06$
0.1	5000	50	4.9	$1.166e$ -11 $\pm$ 6.5e-14
0.1	95	50	5.4e-05	$1.065$ e-06 $\pm$ 5.7e-09
0.1	10	150	2.0	$2.359e-08 \pm 1.2e-10$
0.1	200	150	0.00019	$4.119$ e-08 $\pm$ 2e-10
0.1	500	150	0.37	4.953e-05 ± 1.9e-07
0.1	5000	150	4.9	$1.066e$ -11 $\pm$ $7.3e$ -14
0.1	295	150	0.00063	$3.366\text{e-o7} \pm 1.8\text{e-o9}$
0.1	10	500	2.0	$2.276e$ -10 $\pm$ 9.7e-13
0.1	500	500	0.21	$3.261e$ -10 $\pm$ 1.4e-12
0.1	2000	500	1.84	$7.296\text{e-}08 \pm 2.9\text{e-}10$
0.1	5000	500	4.86	$6.723e$ -12 $\pm$ 3.1e-14
0.1	995	500	0.55	$1.418\text{e-}08 \pm 9.2\text{e-}11$
0.1	10	1000	2.0	$2.593e$ -12 $\pm$ 1.2e-14
0.1	1000	1000	0.55	$3.939e$ -12 $\pm$ 1.5e-14
0.1	5000	1000	4.74	$4.964$ e-12 $\pm$ 2.1e-14
0.1	1995	1000	1.15	$4.176e$ -10 $\pm$ 2.2e-12
0.3	10	1	0.035	$0.03821 \pm 0.0002$
0.3	20	1	0.071	$0.03519 \pm 0.00017$
0.3	50	1	0.179	$0.02707 \pm 0.00012$
0.3	100	1	0.359	$0.01728 \pm 7e-05$
0.3	200	1	0.718	$0.007718 \pm 3e-05$
0.3	300	1	1.08	$0.003678 \pm 1.5 e\text{-}05$
0.3	500	1	3.72	0.0004992 ± 1.9e-06
0.3	1000	1	8.54	$3.541e-05 \pm 1.5e-07$
0.3	2000	1	17.5	$7.434\text{e-07} \pm 2.9\text{e-09}$
0.3	5000	1	44.1	$6.065$ e-10 $\pm$ 3.3e-12
0.3	10	10	1.8e-05	$0.0001216 \pm 7.6$ e-07

Table B.4 – continued from previous page

Coupling (g)	$m_{Phi}$ [GeV]	$m_{\chi}$ [GeV]	from previous $\Gamma_{min}$ [GeV]	$\sigma$ [pb]
0.3	50	10	0.164	0.0273 ± 0.00013
0.3	100	10	0.351	$0.01718 \pm 6.8$ e-05
0.3	5000	10	44.1	$6.164e-10 \pm 4.3e-12$
0.3	15	10	5.3e-05	0.0001503 ± 8.7e-07
0.3	10	50	1.8e-05	1.985e-05 ± 1e-07
0.3	50	50	0.000226	2.405e-05 ± 1.1e-07
0.3	200	50	0.622	$0.007692 \pm 2.8 \text{e-}05$
0.3	300	50	1.02	$0.003682 \pm 1.5 e\text{-}05$
0.3	5000	50	44.1	$6.003$ e-10 $\pm$ 3.4e-12
0.3	95	50	0.00049	$8.676\text{e-o5} \pm 5.3\text{e-o7}$
0.3	10	150	1.8e-05	$1.91e ext{-}06 \pm 8.5e ext{-}09$
0.3	200	150	0.00173	$3.362e-06 \pm 1.4e-08$
0.3	500	150	3.36	$0.0004437 \pm 1.9e-06$
0.3	5000	150	44.1	$5.071e$ -10 $\pm$ 2.9e-12
0.3	295	150	0.00568	$2.746e-05 \pm 1.9e-07$
0.3	10	500	1.8e-05	$1.837 \mathrm{e} ext{-}08 \pm 8.7 \mathrm{e} ext{-}11$
0.3	500	500	1.93	$2.647e-08 \pm 1.1e-10$
0.3	2000	500	16.6	$6.605 ext{e-o7}\pm ext{2.6e-o9}$
0.3	5000	500	43.8	1.956e-10 $\pm$ 1e-12
0.3	995	500	4.93	$1.111e-06 \pm 5.3e-09$
0.3	10	1000	1.8e-05	$2.107e-10 \pm 8.3e-13$
0.3	1000	1000	4.96	$3.169e-10 \pm 1.3e-12$
0.3	5000	1000	42.6	$6.77e$ -11 $\pm$ 3.4e-13
0.3	1995	1000	10.4	$3.021e-08 \pm 1.4e-10$
0.7	10	1	0.191	$0.213 \pm 0.0011$
0.7	20	1	0.389	$0.1942 \pm 0.00094$
0.7	50	1	0.975	$0.1483 \pm 0.00074$
0.7	100	1	1.95	$0.09367 \pm 0.00043$
0.7	200	1	3.91	$0.04172 \pm 0.00017$
0.7	300	1	5.89	$0.01991 \pm 7.9e-05$
0.7	500	1	20.3	$0.002681 \pm 1.3e-05$
0.7	1000	1	46.5	$0.0001949 \pm 8.2e-07$
0.7	2000	1	95.5	$4.648e-06 \pm 2.2e-08$
0.7	5000	1	240	$1.714e-08 \pm 7.6e-11$
0.7	10	10	9.78e-05	$0.00357 \pm 1.7e-05$
0.7	50	10	0.895	$0.1482 \pm 0.0007$
0.7	100	10	1.91	$0.09343 \pm 0.00038$
0.7	5000	10	240	$1.71e-08 \pm 8e-11$
0.7	15	10	0.000289	$0.004422 \pm 2.6e-05$
0.7	10	50	9.78e-05	$0.0005819 \pm 2.5e-06$
0.7	50	50	0.00123	$0.0007124 \pm 3.3e-06$
0.7	200	50	3.39	$0.04143 \pm 0.00018$
0.7	300	50	5.55	$0.01998 \pm 9.3\text{e-}05$
0.7	5000	50	240	$1.661e-08 \pm 1e-10$
0.7	95	50	0.00266	0.002575 ± 1.7e-05

Table B.4 – continued from previous page

0.7 10 150 9.78e-05 5.65e-05 ± 2.9e-07 0.7 200 150 0.0094 9.979e-05 ± 4.8e-07 0.7 500 150 18.3 0.002329 ± 1.3e-05 0.7 5000 150 240 1.393e-08 ± 6.7e-11 0.7 295 150 0.0399 0.0008152 ± 4e-06 0.7 10 500 9.78e-05 5.458e-07 ± 2.2e-09 0.7 500 500 10.5 7.888e-07 ± 2.2e-09 0.7 500 500 10.5 7.888e-07 ± 2.2e-09 0.7 2000 500 90.3 3.71e-06 ± 1.6e-08 0.7 5000 500 238 4.666e-09 ± 3e-11 0.7 995 500 26.9 2.182e-05 ± 9.7e-08 0.7 10 1000 9.78e-05 6.257e-09 ± 2.7e-11 0.7 1000 1000 27 9.46e-09 ± 3.7e-11 0.7 5000 500 232 9.89ye-10 ± 5.3e-12 0.7 1995 1000 56.4 4.386e-07 ± 2.2e-09 1. 10 1 0.39 0.4499 ± 0.0014 1. 20 1 0.793 0.3992 ± 0.0016 1. 50 1 1.99 0.3032 ± 0.0015 1. 100 1 3.98 0.1909 ± 0.0001 1. 200 1 7.98 0.8836 ± 0.00035 1. 200 1 1. 50 1. 1. 500 1	Coupling (g)	$m_{Phi}$ [GeV]	$m_{\chi}$ [GeV]	from previous $\Gamma_{min}$ [GeV]	$\sigma$ [pb]
0.7   200   150   0.0094   9.979e-05 ± 4.8e-07   0.7   500   150   18.3   0.002329 ± 1.3e-05   0.7   5000   150   240   1.393e-08 ± 6.7e-11   0.7   295   150   0.0309   0.0008152 ± 4e-06   0.7   10   500   9.78e-05   5.458e-07 ± 2.2e-09   0.7   500   500   10.5   7.888e-07 ± 3.2e-09   0.7   2000   500   90.3   3.71e-06 ± 1.6e-08   0.7   5000   500   238   4.666e-09 ± 3e-11   0.7   995   500   26.9   2.182e-05 ± 9.7e-08   0.7   1000   1000   27   9.46e-09 ± 3.7e-11   0.7   1000   1000   232   9.897e-10 ± 5.3e-12   0.7   1095   1000   56.4   4.386e-07 ± 2.2e-09   1.   10   1   0.39   0.3992 ± 0.0016   1.   500   1   1.99   0.3032 ± 0.0015   1.   100   1   3.98   0.1909 ± 0.0014   1.   200   1   7.98   0.0836 ± 0.00035   1.   300   1   12   0.03999 ± 0.00016   1.   500   1   41.3   0.005408 ± 2.2e-05   1.   100   1   94.9   0.0003973 ± 1.7e-06   1.   5000   1   490   7.022e-08 ± 2.8e-10   1.   100   1   3.9   0.3034 ± 0.0016   1.   5000   1   490   7.022e-08 ± 2.8e-10   1.   100   1   3.9   0.3034 ± 0.0016   1.   5000   1   490   7.022e-08 ± 2.8e-10   1.   100   10   3.9   0.1901 ± 0.00085   1.   100   10   3.9   0.1901 ± 0.00085   1.   5000   10   490   7.023e-08 ± 3e-10   1.   100   10   3.9   0.1901 ± 0.00085   1.   5000   50   490   6.831e-08 ± 4.1e-10   1.   5000   10   490   7.023e-08 ± 3e-10   1.   5000   50   490   6.831e-08 ± 4.1e-10   1.   5000   150   37.4   0.004611 ± 1.9e-05   1.   5000   500   486   5.698e-08 ± 2.5e-10   1.   5000   500   486   5.698e-08 ± 2.5e-10   1.   5000   500   486   5.698e-08 ± 2.5e-	0.7	10	150	9.78e-05	5.65e-05 ± 2.9e-07
0.7   500   150   18.3   0.002329 ± 1.3e-05   0.7   5000   150   240   1.393e-08 ± 6.7e-11   0.7   295   150   0.0309   0.0008152 ± 4e-06   0.7   10   500   9.78e-05   5.458e-07 ± 2.2e-09   0.7   500   500   10.5   7.888e-07 ± 2.2e-09   0.7   2000   500   90.3   3.71e-06 ± 1.6e-08   0.7   5000   500   238   4.666e-09 ± 3e-11   0.7   995   500   26.9   2.182e-05 ± 9.7e-08   0.7   100   1000   27   9.46e-09 ± 3.7e-11   0.7   5000   1000   232   9.897e-10 ± 5.3e-12   0.7   1995   1000   56.4   4.386e-07 ± 2.2e-09   1.   10   1   0.39   0.4409 ± 0.0014   1.   20   1   0.793   0.3992 ± 0.0016   1.   50   1   1.99   0.3032 ± 0.0015   1.   100   1   3.98   0.1909 ± 0.001   1.   200   1   7.98   0.0836 ± 0.00035   1.   300   1   12   0.03999 ± 0.00016   1.   500   1   41.3   0.005408 ± 2.2e-05   1.   1000   1   94.9   0.003973 ± 1.7e-06   1.   5000   1   490   7.022e-08 ± 2.8e-10   1.   500   1   490   7.022e-08 ± 2.8e-10   1.   100   10   3.9   0.1901 ± 0.0005   1.   5000   10   490   7.022e-08 ± 3.e-10   1.   5000   10   490   7.023e-08 ± 3e-10   1.   5000   10   490   7.023e-08 ± 3e-10   1.   5000   10   490   7.023e-08 ± 3e-10   1.   5000   50   490   6.831e-08 ± 1.2e-05   1.   5000   50   490   6.831e-08 ± 1.2e-05   1.   5000   50   490   6.831e-08 ± 4.1e-10   1.   5000   50   490   6.831e-08 ± 4.1e-10   1.   5000   50   490   0.00247 ± 1.7e-06   1.   5000   50   490   0.00247 ± 1.7e-06   1.   5000   50   490   0.00365 ± 1.7e-05   1.   5000   50   500   489   5.698e-08 ± 2.5e-10   1.   5000   500   500   21.4   3.275e-06 ± 1.4e-06   1.   5000   500   486   1.86r-08 ± 1.2e-10		200			
0.7 295 150 0.0309 0.008152 ± 4e-06 0.7 10 500 9.78e-05 5.458e-07 ± 2.2e-09 0.7 500 500 10.5 7.888e-07 ± 2.2e-09 0.7 2000 500 90.3 3.71e-06 ± 1.6e-08 0.7 5000 500 238 4.666e-09 ± 3e-11 0.7 995 500 26.9 2.182e-05 ± 9.7e-08 0.7 10 1000 9.78e-05 6.257e-09 ± 2.7e-11 0.7 1000 1000 27 9.46e-09 ± 3.7e-11 0.7 1000 1000 232 9.897e-10 ± 5.3e-12 0.7 1995 1000 56.4 4.386e-07 ± 2.2e-09 1. 10 1 0.39 0.4409 ± 0.0014 1. 20 1 0.793 0.3992 ± 0.0016 1. 50 1 1.99 0.3032 ± 0.0015 1. 100 1 3.98 0.1909 ± 0.001 1. 200 1 7.98 0.0836 ± 0.0035 1. 300 1 12 0.03999 ± 0.00016 1. 500 1 41.3 0.005408 ± 2.2e-05 1. 1000 1 94.9 0.003973 ± 1.7e-06 1. 2000 1 195 1.087e-05 ± 5.2e-08 1. 5000 1 490 7.022e-08 ± 2.8e-10 1. 10 10 10 0.0002 0.01499 ± 8.4e-05 1. 5000 10 490 7.022e-08 ± 2.8e-10 1. 100 10 3.9 0.1901 ± 0.0016 1. 500 1 1.83 0.3934 ± 0.0016 1. 500 1 1.99 0.003973 ± 1.7e-06 1. 5000 1 490 7.022e-08 ± 2.8e-10 1. 10 10 0.0002 0.01499 ± 8.4e-05 1. 5000 1 490 7.022e-08 ± 3e-10 1. 10 10 10 0.0002 0.01499 ± 8.4e-05 1. 5000 10 490 7.023e-08 ± 3e-10 1. 10 10 50 0.0002 0.002444 ± 1.2e-05 1. 500 50 0.00251 0.002979 ± 1.5e-05 1. 500 50 0.00251 0.002979 ± 1.5e-05 1. 5000 50 490 6.831e-08 ± 4.1e-10 1. 5000 150 499 0.000364 ± 1.1e-06 1. 5000 150 499 0.000365 ± 1.7e-05 1. 5000 150 37.4 0.004611 ± 1.9e-05 1. 5000 150 489 5.698e-08 ± 2.5e-10 1. 500 150 37.4 0.004611 ± 1.9e-05 1. 500 500 0.0002 2.279e-06 ± 8.7e-09 1. 5000 500 486 1.867e-08 ± 1.2e-10	0.7	500		18.3	
0.7 10 500 9.78e-05 5.458e-07 ± 2.2e-09 0.7 500 500 10.5 7.888e-07 ± 3.2e-09 0.7 500 500 90.3 3.71e-06 ± 1.6e-08 0.7 5000 500 90.3 3.71e-06 ± 1.6e-08 0.7 5000 500 238 4.666e-09 ± 3e-11 0.7 995 500 26.9 2.182e-05 ± 9.7e-08 0.7 10 1000 9.78e-05 6.257e-09 ± 2.7e-11 0.7 1000 1000 27 9.46e-09 ± 3.7e-11 0.7 5000 1000 232 9.897e-10 ± 5.3e-12 0.7 1995 1000 56.4 4.386e-07 ± 2.2e-09 1. 10 1 0.39 0.4409 ± 0.0014 1. 20 1 0.793 0.3992 ± 0.0016 1. 50 1 1.99 0.3032 ± 0.0015 1. 100 1 3.98 0.1909 ± 0.001 1. 200 1 7.98 0.0836 ± 0.00035 1. 200 1 1 2 0.03999 ± 0.00016 1. 500 1 41.3 0.005408 ± 2.2e-05 1. 1000 1 94.9 0.0003973 ± 1.7e-06 1. 2000 1 195 1.087e-05 ± 5.2e-08 1. 5000 1 490 7.022e-08 ± 2.8e-10 1. 100 10 3.9 0.1901 ± 0.00085 1. 5000 10 490 7.022e-08 ± 2.8e-10 1. 100 10 3.9 0.1901 ± 0.00085 1. 5000 10 490 7.023e-08 ± 3e-10 1. 15 10 10 50 0.0002 0.00240 ± 1.2e-05 1. 100 10 3.9 0.1901 ± 0.00085 1. 5000 10 490 7.023e-08 ± 3e-10 1. 15 10 0.000589 0.0163 ± 9.3e-05 1. 10 0.0002 0.00240 ± 1.2e-05 1. 10 0.0002 0.00240 ± 1.2e-05 1. 10 0.000589 0.0160 ± 3.9e-05 1. 10 0.000589 0.0160 ± 3.9e-05 1. 10 0.000589 0.00240 ± 1.2e-05 1. 200 50 6.91 0.08382 ± 0.00016 1. 5000 50 490 6.831e-08 ± 4.1e-10 1. 5000 150 499 6.831e-08 ± 4.1e-10 1. 5000 150 489 5.698e-08 ± 2.5e-10 1. 5000 150 489 5.698e-08 ± 2.5e-10 1. 5000 150 489 5.698e-08 ± 2.5e-10 1. 5000 150 37.4 0.004611 ± 1.9e-05 1. 5000 150 489 5.698e-08 ± 2.5e-10 1. 205 150 0.0192 0.000214 ± 1.8e-06 1. 205 150 0.0192 0.000412 ± 1.8e-06 1. 205 150 0.0002 0.00036 ± 1.7e-05 1. 200 150 0.0192 0.000412 ± 1.8e-06 1. 205 150 0.0002 0.00036 ± 1.7e-05 1. 200 150 0.0192 0.000412 ± 1.8e-06 1. 205 150 0.0002 0.00036 ± 1.7e-05 1. 200 150 0.0003 1. 2.299e-06 ± 8.7e-09 1. 20006 500 184 7.61	0.7	5000	150	240	1.393e-08 ± 6.7e-11
0.7 500 500 10.5 7.888e-07 ± 3.2e-09 0.7 2000 500 90.3 3.71e-06 ± 1.6e-08 0.7 5000 500 238 4.666e-09 ± 3e-11 0.7 995 500 26.9 2.182e-05 ± 9.7e-08 0.7 10 1000 9.78e-05 6.257e-09 ± 2.7e-11 0.7 1000 1000 27 9.46e-09 ± 3.7e-11 0.7 5000 1000 232 9.897e-10 ± 5.3e-12 0.7 1995 1000 56.4 4.386e-07 ± 2.2e-09 1. 10 1 0.39 0.4409 ± 0.0014 1. 20 1 0.793 0.3992 ± 0.0016 1. 50 1 1.99 0.3032 ± 0.0015 1. 100 1 3.98 0.1909 ± 0.001 1. 200 1 7.98 0.0836 ± 0.00035 1. 300 1 12 0.03999 ± 0.0016 1. 500 1 41.3 0.005408 ± 2.2e-05 1. 1000 1 94.9 0.0003973 ± 1.7e-06 1. 2000 1 195 1.087e-05 ± 5.2e-08 1. 5000 1 490 7.022e-08 ± 2.8e-10 1. 10 10 10 0.0002 0.01491 ± 0.00065 1. 500 10 1.83 0.3034 ± 0.0016 1. 500 10 490 7.022e-08 ± 3e-10 1. 15 10 10 3.9 0.1901 ± 0.00085 1. 500 10 490 7.022e-08 ± 3e-10 1. 15 10 10 3.9 0.1901 ± 0.00085 1. 500 50 0.0022 0.002444 ± 1.2e-05 1. 500 50 0.0025 1 0.002979 ± 1.5e-05 1. 500 50 0.0024 0.00244 ± 1.2e-05 1. 500 50 0.0024 0.00365 ± 1.7e-05 1. 500 150 489 5.698e-08 ± 2.5e-10 1. 500 150 489 5.698e-08 ± 2.5e-10 1. 500 500 150 0.0002 2.279e-06 ± 8.7e-09 1. 500 500 184 7.611e-06 ± 3.7e-08 1. 5000 500 184 7.611e-06 ± 3.7e-08	0.7	295			
0.7 2000 500 90.3 3.71e-06 ± 1.6e-08 0.7 5000 500 238 4.666e-09 ± 3e-11 0.7 995 500 26.9 2.182e-05 ± 9.7e-08 0.7 10 1000 9.78e-05 6.257e-09 ± 2.7e-11 0.7 1000 1000 27 9.46e-09 ± 3.7e-11 0.7 5000 1000 232 9.897e-10 ± 5.3e-12 0.7 1995 1000 56.4 4.386e-07 ± 2.2e-09 1. 10 1 0.39 0.4409 ± 0.0014 1. 20 1 0.793 0.3992 ± 0.0016 1. 50 1 1.99 0.3032 ± 0.0015 1. 100 1 3.98 0.1909 ± 0.001 1. 200 1 7.98 0.0836 ± 0.00035 1. 300 1 12 0.03999 ± 0.0016 1. 500 1 41.3 0.005408 ± 2.2e-05 1. 1000 1 94.9 0.003973 ± 1.7e-06 1. 1000 1 194.9 0.003973 ± 1.7e-06 1. 2000 1 195 1.087e-05 ± 5.2e-08 1. 5000 1 490 7.022e-08 ± 2.8e-10 1. 100 10 0.0002 0.01499 ± 8.4e-05 1. 500 10 1.83 0.3034 ± 0.0016 1. 500 10 490 7.022e-08 ± 3e-10 1. 15 10 10 3.9 0.1901 ± 0.00085 1. 500 10 490 7.023e-08 ± 3e-10 1. 15 10 0.000589 0.1863 ± 9.3e-05 1. 10 10 50 0.0002 0.002444 ± 1.2e-05 1. 200 50 6.91 0.08382 ± 0.00036 1. 300 50 11.3 0.03989 ± 0.00015 1. 5000 50 490 6.831e-08 ± 4.1e-10 1. 5000 15 490 0.00399 ± 1.5e-05 1. 5000 50 490 6.831e-08 ± 4.1e-10 1. 5000 150 0.0002 0.000244 ± 1.8e-06 1. 5000 150 0.0002 0.000261 ± 1.8e-05 1. 5000 50 490 6.831e-08 ± 4.1e-10 1. 5000 150 0.0002 0.000244 ± 1.8e-06 1. 5000 150 0.0002 0.000261 ± 1.8e-06 1. 5000 50 490 6.831e-08 ± 4.1e-10 1. 5000 150 0.0002 0.00026 ± 2.5e-10 1. 5000 150 0.0002 0.00026 ± 2.5e-10 1. 5000 150 0.0002 0.00026 ± 2.7e-05 1. 5000 150 0.0002 0.00026 ± 2.5e-10 1. 5000 500 486 1.8e-09 1. 5000 500 6.84 0.00365 ± 1.7e-05 1. 5000 500 2.279e-06 ± 1.4e-08 1. 5000 500 6.84 7.611e-06 ± 3.7e-08 1. 5000 500 184 7.611e-06 ± 3.7e-08 1. 5000 500 184 7.611e-06 ± 3.7e-08	0.7	10	500	9.78e-05	$5.458\text{e-o}7 \pm 2.2\text{e-o}9$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.7	500	500	10.5	$7.888e-07 \pm 3.2e-09$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.7	2000	500	90.3	$3.71e-06 \pm 1.6e-08$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.7	5000	500	238	$4.666e-09 \pm 3e-11$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.7	995	500	26.9	$2.182e-05 \pm 9.7e-08$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.7	10	1000	9.78e-05	$6.257 ext{e-09} \pm 2.7 ext{e-11}$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.7	1000	1000	27	9.46e-09 ± 3.7e-11
1.       10       1 $0.39$ $0.4409 \pm 0.0014$ 1.       20       1 $0.793$ $0.3992 \pm 0.0016$ 1.       50       1 $1.99$ $0.3032 \pm 0.0015$ 1.       100       1 $3.98$ $0.1909 \pm 0.001$ 1.       200       1 $7.98$ $0.0836 \pm 0.00035$ 1.       300       1       12 $0.03999 \pm 0.00016$ 1.       500       1       41.3 $0.005408 \pm 2.2e-05$ 1.       1000       1       94.9 $0.003973 \pm 1.7e-06$ 1.       2000       1       195 $1.087e-05 \pm 5.2e-08$ 1.       2000       1       490 $7.022e-08 \pm 2.8e-10$ 1.       10       10 $0.0002$ $0.01499 \pm 8.4e-05$ 1.       50       10 $1.83$ $0.3034 \pm 0.0016$ 1.       10       10 $3.9$ $0.1901 \pm 0.00085$ 1.       50       10 $4.90$ $7.022e-08 \pm 3e-10$ 1.       10       10 $3.9$ $0.1901 \pm 0.00085$ 1.       50       10 $3.9$ $0.1901 \pm $	0.7	5000	1000	232	$9.897e$ -10 $\pm$ 5.3e-12
1.       20       1       0.793       0.3992 $\pm$ 0.0016         1.       50       1       1.99       0.3032 $\pm$ 0.0015         1.       100       1       3.98       0.1909 $\pm$ 0.001         1.       200       1       7.98       0.0836 $\pm$ 0.00035         1.       300       1       12       0.03999 $\pm$ 0.00016         1.       500       1       41.3       0.005408 $\pm$ 2.2e-05         1.       1000       1       94.9       0.0003973 $\pm$ 1.7e-06         1.       2000       1       195       1.087e-05 $\pm$ 5.2e-08         1.       5000       1       490       7.022e-08 $\pm$ 2.8e-10         1.       10       10       0.0002       0.01499 $\pm$ 8.4e-05         1.       10       10       0.0002       0.01499 $\pm$ 8.4e-05         1.       10       10       3.9       0.1901 $\pm$ 0.00085         1.       100       10       3.9       0.1901 $\pm$ 0.00085         1.       15       10       0.000589       0.01863 $\pm$ 9.3e-05         1.       15       10       0.000599       0.01863 $\pm$ 9.3e-05         1.       200       50       0.0025       0.002979 $\pm$	0.7	1995	1000	56.4	$4.386$ e-07 $\pm$ 2.2e-09
1.       50       1       1.99 $0.3032 \pm 0.0015$ 1.       100       1 $3.98$ $0.1909 \pm 0.001$ 1.       200       1 $7.98$ $0.0836 \pm 0.00035$ 1.       300       1       12 $0.03999 \pm 0.00016$ 1.       500       1       41.3 $0.005408 \pm 2.2e-05$ 1.       1000       1       94.9 $0.0003973 \pm 1.7e-06$ 1.       2000       1       195 $1.087e-05 \pm 5.2e-08$ 1.       5000       1       490 $7.022e-08 \pm 2.8e-10$ 1.       10       10 $0.0002$ $0.01499 \pm 8.4e-05$ 1.       10       10 $0.0002$ $0.01863 \pm 9.3e-05$ 1.       10       10 $0.0002$ $0.00244 \pm 1.2e-05$ 1.       10       50 $0.0002$ <	1.	10	1	0.39	$0.4409 \pm 0.0014$
1. $100$ 1 $3.98$ $0.1909 \pm 0.001$ 1. $200$ 1 $7.98$ $0.0836 \pm 0.00035$ 1. $300$ 1 $12$ $0.03999 \pm 0.00016$ 1. $500$ 1 $41.3$ $0.005408 \pm 2.2e-05$ 1. $1000$ 1 $94.9$ $0.0003973 \pm 1.7e-06$ 1. $1000$ 1 $195$ $1.087e-05 \pm 5.2e-08$ 1. $5000$ 1 $490$ $7.022e-08 \pm 2.8e-10$ 1. $10$ $10$ $0.0002$ $0.01499 \pm 8.4e-05$ 1. $10$ $10$ $0.0002$ $0.0160$ $0.0016$ 1. $10$ $10$ $0.0002$ $0.01863 \pm 9.3e-05$ 1. $10$ $10$ $0.0002$ $0.002799 \pm 1.5e-05$ <	1.	20	1	0.793	$0.3992 \pm 0.0016$
1.       200       1 $7.98$ $0.0836 \pm 0.00035$ 1.       300       1 $12$ $0.03999 \pm 0.00016$ 1.       500       1 $41.3$ $0.005408 \pm 2.2e-05$ 1. $1000$ 1 $94.9$ $0.0003973 \pm 1.7e-06$ 1. $1000$ 1 $195$ $1.087e-05 \pm 5.2e-08$ 1. $5000$ 1 $490$ $7.022e-08 \pm 2.8e-10$ 1. $10$ $10$ $0.0002$ $0.01499 \pm 8.4e-05$ 1. $100$ $10$ $3.9$ $0.1901 \pm 0.00085$ 1. $100$ $10$ $3.9$ $0.1901 \pm 0.00085$ 1. $10$ $10$ $0.0002$ $0.002444 \pm 1.2e-05$ 1. $10$ $10$ $0.0002$ $0.00388 \pm 0.00036$ 1. </td <td>1.</td> <td>50</td> <td>1</td> <td>1.99</td> <td><math>0.3032 \pm 0.0015</math></td>	1.	50	1	1.99	$0.3032 \pm 0.0015$
1. $300$ 1 $12$ $0.03999 \pm 0.00016$ 1. $500$ 1 $41.3$ $0.005408 \pm 2.2e-05$ 1. $1000$ 1 $94.9$ $0.0003973 \pm 1.7e-06$ 1. $2000$ 1 $195$ $1.087e-05 \pm 5.2e-08$ 1. $5000$ 1 $490$ $7.022e-08 \pm 2.8e-10$ 1. $10$ $10$ $0.0002$ $0.01499 \pm 8.4e-05$ 1. $10$ $10$ $0.0002$ $0.01499 \pm 8.4e-05$ 1. $10$ $10$ $0.39$ $0.1901 \pm 0.00085$ 1. $100$ $10$ $3.9$ $0.1901 \pm 0.00085$ 1. $15$ $10$ $0.000589$ $0.01863 \pm 9.3e-05$ 1. $15$ $10$ $0.0002$ $0.002444 \pm 1.2e-05$ 1. $10$ $50$ $0.0002$ $0.002979 \pm 1.5e-05$ 1. $200$ $50$ $6.91$ $0.08382 \pm 0.00036$ 1. $300$ $50$ $11.3$ $0.03989 \pm 0.00015$ 1. $5000$ $50$ $490$ $6.831e-08 \pm 4.1e-10$	1.	100	1	3.98	$0.1909 \pm 0.001$
1. $500$ 1 $41.3$ $0.005408 \pm 2.2e-05$ 1. $1000$ 1 $94.9$ $0.0003973 \pm 1.7e-06$ 1. $2000$ 1 $195$ $1.087e-05 \pm 5.2e-08$ 1. $5000$ 1 $490$ $7.022e-08 \pm 2.8e-10$ 1. $10$ $10$ $0.0002$ $0.01499 \pm 8.4e-05$ 1. $10$ $10$ $1.83$ $0.3034 \pm 0.0016$ 1. $100$ $10$ $3.9$ $0.1901 \pm 0.00085$ 1. $100$ $10$ $3.9$ $0.1901 \pm 0.00085$ 1. $15$ $10$ $0.000589$ $0.01863 \pm 9.3e-05$ 1. $15$ $10$ $0.0002$ $0.002444 \pm 1.2e-05$ 1. $10$ $50$ $0.00251$ $0.002979 \pm 1.5e-05$ 1. $200$ $50$ $6.91$ $0.08382 \pm 0.00036$ 1. $300$ $50$ $11.3$ $0.03989 \pm 0.00015$ 1. $5000$ $50$ $490$ $6.831e-08 \pm 4.1e-10$ 1. $95$ $50$ $0.00544$ $0.0167 \pm 5.7e-05$ <tr< td=""><td>1.</td><td>200</td><td>1</td><td>7.98</td><td><math>0.0836 \pm 0.00035</math></td></tr<>	1.	200	1	7.98	$0.0836 \pm 0.00035$
1. $1000$ 1 $94.9$ $0.0003973 \pm 1.7e-06$ 1. $2000$ 1 $195$ $1.087e-05 \pm 5.2e-08$ 1. $5000$ 1 $490$ $7.022e-08 \pm 2.8e-10$ 1. $10$ $10$ $0.0002$ $0.01499 \pm 8.4e-05$ 1. $50$ $10$ $1.83$ $0.3034 \pm 0.0016$ 1. $100$ $10$ $3.9$ $0.1901 \pm 0.00085$ 1. $100$ $10$ $490$ $7.023e-08 \pm 3e-10$ 1. $15$ $10$ $0.000589$ $0.1863 \pm 9.3e-05$ 1. $15$ $10$ $0.0002$ $0.002444 \pm 1.2e-05$ 1. $10$ $50$ $0.00251$ $0.002979 \pm 1.5e-05$ 1. $200$ $50$ $6.91$ $0.08382 \pm 0.00036$ 1. $300$ $50$ $11.3$ $0.03389 \pm 0.00015$ 1. $200$ $50$ $490$ $6.831e-08 \pm 4.1e-10$ 1. $95$ $50$ $0.00544$ $0.01067 \pm 5.7e-05$ 1. $10$ $150$ $0.002$ $0.0002364 \pm 1.1e-06$	1.	300	1	12	$0.03999 \pm 0.00016$
1.       2000       1       195 $1.087e-05 \pm 5.2e-08$ 1.       5000       1       490 $7.022e-08 \pm 2.8e-10$ 1.       10       10 $0.0002$ $0.01499 \pm 8.4e-05$ 1.       50       10 $1.83$ $0.3034 \pm 0.0016$ 1.       100       10 $3.9$ $0.1901 \pm 0.00085$ 1.       100       10 $490$ $7.023e-08 \pm 3e-10$ 1.       15       10 $0.000589$ $0.01863 \pm 9.3e-05$ 1.       10       50 $0.0002$ $0.002444 \pm 1.2e-05$ 1.       10       50 $0.0002$ $0.002444 \pm 1.2e-05$ 1.       200       50 $6.91$ $0.08382 \pm 0.00036$ 1.       300       50 $11.3$ $0.03989 \pm 0.00015$ 1.       300       50 $11.3$ $0.03989 \pm 0.00015$ 1.       5000       50 $490$ $6.831e-08 \pm 4.1e-10$ 1.       95       50 $0.00544$ $0.01067 \pm 5.7e-05$ 1.       10       150 $0.0002$ $0.0002364 \pm 1.1e-06$ 1.       500       150<	1.	500	1	41.3	$0.005408 \pm 2.2e-05$
1. $5000$ 1 $490$ $7.022e-08 \pm 2.8e-10$ 1. $10$ $10$ $0.0002$ $0.01499 \pm 8.4e-05$ 1. $50$ $10$ $1.83$ $0.3034 \pm 0.0016$ 1. $100$ $10$ $3.9$ $0.1901 \pm 0.00085$ 1. $5000$ $10$ $490$ $7.023e-08 \pm 3e-10$ 1. $15$ $10$ $0.000589$ $0.01863 \pm 9.3e-05$ 1. $10$ $50$ $0.0002$ $0.002444 \pm 1.2e-05$ 1. $10$ $50$ $0.0002$ $0.002979 \pm 1.5e-05$ 1. $200$ $50$ $6.91$ $0.08382 \pm 0.00036$ 1. $300$ $50$ $11.3$ $0.03989 \pm 0.00015$ 1. $5000$ $50$ $490$ $6.831e-08 \pm 4.1e-10$ 1. $95$ $50$ $0.00544$ $0.01067 \pm 5.7e-05$ 1. $10$ $150$ $0.0002$ $0.0002364 \pm 1.1e-06$ 1. $200$ $150$ $37.4$ $0.004611 \pm 1.9e-05$ 1. $5000$ $150$ $489$ $5.698e-08 \pm 2.5e-10$	1.	1000	1	94.9	$0.0003973 \pm 1.7e-06$
1.       10       10 $0.0002$ $0.01499 \pm 8.4e-05$ 1.       50       10 $1.83$ $0.3034 \pm 0.0016$ 1.       100       10 $3.9$ $0.1901 \pm 0.00085$ 1.       5000       10 $490$ $7.023e-08 \pm 3e-10$ 1.       15       10 $0.000589$ $0.01863 \pm 9.3e-05$ 1.       10       50 $0.0002$ $0.002444 \pm 1.2e-05$ 1.       50       50 $0.00251$ $0.002979 \pm 1.5e-05$ 1.       200       50 $6.91$ $0.08382 \pm 0.00036$ 1.       300       50 $11.3$ $0.03882 \pm 0.00036$ 1.       300       50 $11.3$ $0.03882 \pm 0.00036$ 1.       5000       50       490 $6.831e-08 \pm 4.1e-10$ 1.       5000       50       490 $6.831e-08 \pm 4.1e-10$ 1.       95       50 $0.00544$ $0.01067 \pm 5.7e-05$ 1.       10       150 $0.002$ $0.0002364 \pm 1.1e-06$ 1.       200       150 $0.0192$ $0.0004124 \pm 1.8e-06$ 1.       500 <t< td=""><td>1.</td><td>2000</td><td>1</td><td>195</td><td><math>1.087e-05 \pm 5.2e-08</math></td></t<>	1.	2000	1	195	$1.087e-05 \pm 5.2e-08$
1.       50       10       1.83 $0.3034 \pm 0.0016$ 1.       100       10       3.9 $0.1901 \pm 0.00085$ 1.       5000       10       490 $7.023e-08 \pm 3e-10$ 1.       15       10 $0.000589$ $0.01863 \pm 9.3e-05$ 1.       10       50 $0.0002$ $0.002444 \pm 1.2e-05$ 1.       50       50 $0.00251$ $0.002979 \pm 1.5e-05$ 1.       200       50 $6.91$ $0.08382 \pm 0.00036$ 1.       300       50 $11.3$ $0.03989 \pm 0.00015$ 1.       300       50 $11.3$ $0.03989 \pm 0.00015$ 1.       5000       50       490 $6.831e-08 \pm 4.1e-10$ 1.       95       50 $0.00544$ $0.01067 \pm 5.7e-05$ 1.       10       150 $0.0002$ $0.0002364 \pm 1.1e-06$ 1.       200       150 $0.0192$ $0.0004124 \pm 1.8e-06$ 1.       500       150       37.4 $0.004611 \pm 1.9e-05$ 1.       5000       150       489 $5.698e-08 \pm 2.5e-10$ 1.       295       150	1.	5000	1	490	$7.022e-08 \pm 2.8e-10$
1.       100       10       3.9 $0.1901 \pm 0.00085$ 1.       5000       10       490 $7.023e-08 \pm 3e-10$ 1.       15       10 $0.000589$ $0.01863 \pm 9.3e-05$ 1.       10       50 $0.0002$ $0.002444 \pm 1.2e-05$ 1.       50       50 $0.00251$ $0.002979 \pm 1.5e-05$ 1.       200       50 $6.91$ $0.08382 \pm 0.00036$ 1.       300       50 $11.3$ $0.03989 \pm 0.00015$ 1.       5000       50       490 $6.831e-08 \pm 4.1e-10$ 1.       95       50 $0.00544$ $0.01067 \pm 5.7e-05$ 1.       10       150 $0.0002$ $0.0002364 \pm 1.1e-06$ 1.       200       150 $0.0192$ $0.0004124 \pm 1.8e-06$ 1.       500       150       37.4 $0.004611 \pm 1.9e-05$ 1.       5000       150       489 $5.698e-08 \pm 2.5e-10$ 1.       295       150 $0.0631$ $0.003365 \pm 1.7e-05$ 1.       500       500       21.4 $3.275e-06 \pm 8.7e-09$ 1.       500	1.	10	10	0.0002	
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				-	
1. 995 500 54.8 6.171e-05 $\pm$ 2.5e-07		_	_	-	
	1.	995	500	54.8	6.171e-05 ± 2.5e-07

Table B.4 – continued from previous page

Coupling (g)	$m_{Phi}$ [GeV]		$\Gamma_{min}$ [GeV]	$\sigma$ [pb]
1.	10	1000	0.0002	2.595e-08 ± 1e-10
1.	1000	1000	55.1	$3.933e-08 \pm 1.5e-10$
1.	5000	1000	474	$3.536\text{e-}09 \pm 1.8\text{e-}11$
1.	1995	1000	115	1.103e-06 ± 5e-09
1.5	10	1	0.878	$1.041 \pm 0.004$
1.5	20	1	1.78	$0.9304 \pm 0.0037$
1.5	50	1	4.48	$0.6793 \pm 0.003$
1.5	100	1	8.96	$0.4189 \pm 0.002$
1.5	200	1	17.9	$0.1836 \pm 0.00074$
1.5	300	1	27	$0.08863 \pm 0.00038$
1.5	500	1	93	$0.01129 \pm 5.5 \text{e-}05$
1.5	1000	1	214	$0.000878 \pm 4.1e-06$
1.5	2000	1	439	$3.1e-05 \pm 1.2e-07$
1.5	5000	1	1103	$3.408\text{e-o7} \pm 1.6\text{e-o9}$
1.5	10	10	0.000449	$0.0747 \pm 0.00036$
1.5	50	10	4.11	$0.6777 \pm 0.0032$
1.5	100	10	8.78	$0.424 \pm 0.002$
1.5	5000	10	1103	$3.418e-07 \pm 1.3e-09$
1.5	15	10	0.00133	$0.09382 \pm 0.00049$
1.5	10	50	0.000449	$0.01227 \pm 6.9 e-05$
1.5	50	50	0.00566	$0.01488 \pm 7.4e-05$
1.5	200	50	15.5	$0.1861 \pm 0.00087$
1.5	300	50	25.5	$0.08815 \pm 0.00041$
1.5	5000	50	1103	$3.334e-07 \pm 2e-09$
1.5	95	50	0.0122	$0.05397 \pm 0.00029$
1.5	10	150	0.000449	$0.0012 \pm 6.1e-06$
1.5	200	150	0.0432	$0.002092 \pm 9.1e-06$
1.5	500	150	84.1	$0.009493 \pm 4.2e-05$
1.5	5000	150	1102	$2.739e-07 \pm 1.5e-09$
1.5	295	150	0.142	$0.01722 \pm 0.00011$
1.5	10	500	0.000449	$1.147e-05 \pm 4.7e-08$
1.5	500	500	48.2	$1.659e-05 \pm 6.5e-08$
1.5	2000	500	415	$1.716e-05 \pm 9e-08$
1.5	5000	500	1094	$8.722e-08 \pm 3.9e-10$
1.5	995	500	123	$0.0001753 \pm 6.8e-07$
1.5	10	1000	0.000449	$1.32e-07 \pm 5.2e-10$
1.5	1000	1000	124	$1.975e-07 \pm 7.7e-10$
1.5	5000	1000	1065	$1.508e-08 \pm 6.2e-11$
1.5	1995	1000	259	$2.741e-06 \pm 1.3e-08$
2.	10	1	1.56	$1.962 \pm 0.0076$
2.	20	1	3.17	$1.718 \pm 0.0064$
2.	50	1	7.96	$1.217 \pm 0.0061$
2.	100	1	15.9	$0.7382 \pm 0.0029$
2.	200	1	31.9	$0.3179 \pm 0.0015$
2.	300	1	48	0.1503 ± 0.00067

Table B.4 – continued from previous page

Coupling (g)	$m_{Phi}$ [GeV]		$\Gamma_{min}$ [GeV]	$\sigma$ [pb]
2.	500	1	165	0.01871 ± 0.0001
2.	1000	1	380	$0.001487 \pm 9.1e-06$
2.	2000	1	<del>7</del> 80	$6.481e-05 \pm 3e-07$
2.	5000	1	1961	9.619e-07 ± 3.9e-09
2.	10	10	0.000799	$0.2395 \pm 0.0012$
2.	50	10	7.3	$1.217 \pm 0.0051$
2.	100	10	15.6	$0.7347 \pm 0.003$
2.	5000	10	1961	$9.544 \text{e-o}7 \pm 4.6 \text{e-o}9$
2.	15	10	0.00236	$0.2973 \pm 0.0015$
2.	10	50	0.000799	$0.03855 \pm 0.00018$
2.	50	50	0.0101	$0.04728 \pm 0.00022$
2.	200	50	27.6	$0.3166 \pm 0.0016$
2.	300	50	45.3	$0.149 \pm 0.00061$
2.	5000	50	1960	$9.34 ext{e-o7} \pm 4.6 ext{e-o9}$
2.	95	50	0.0217	$0.1717 \pm 0.00096$
2.	10	150	0.000799	$0.003778 \pm 1.8 e\text{-}05$
2.	200	150	0.0768	$0.006619 \pm 2.7 \text{e-}05$
2.	500	150	149	$0.01511 \pm 8.1e-05$
2.	5000	150	1959	$7.835e-07 \pm 3.9e-09$
2.	295	150	0.253	$0.05408 \pm 0.00031$
2.	10	500	0.000799	$3.638e-05 \pm 1.5e-07$
2.	500	500	85.8	$5.258\text{e-}05 \pm 2.4\text{e-}07$
2.	2000	500	736.9	$2.857e-05 \pm 1.7e-07$
2.	5000	500	1945	$2.44e ext{-07} \pm 1.1e ext{-09}$
2.	995	500	219.2	$0.0003371 \pm 1.4e-06$
2.	10	1000	0.0007987	4.139e-07 ± 1.7e-09
2.	1000	1000	220.5	$6.26\text{e-o}7 \pm 2.8\text{e-o}9$
2.	5000	1000	1894	$3.818e-08 \pm 1.5e-10$
2.	1995	1000	460.1	$4.794e-06 \pm 2.4e-08$
2.5	10	1	2.44	$3.313 \pm 0.016$
2.5	20	1	4.95	$2.805 \pm 0.013$
2.5	50	1	12.4	$1.92 \pm 0.01$
2.5	100	1	24.9	$1.131 \pm 0.0054$
2.5	200	1	49.9	$0.4734 \pm 0.0021$
2.5	300	1	75.0	$0.2216 \pm 0.0012$
2.5	500	1	258	$0.02611 \pm 0.00012$
2.5	1000	1	593	$0.002111 \pm 1e-05$
2.5	2000	1	1218	$0.0001072 \pm 4.2e-07$
2.5	5000	1	3064	$1.927e-06 \pm 9.9e-09$
2.5	10	10	0.00125	$0.5815 \pm 0.0026$
2.5	50	10	11.4	$1.928 \pm 0.011$
2.5	100	10	24.4	$1.131 \pm 0.006$
2.5	5000	10	3064	$1.937e-06 \pm 9.9e-09$
2.5	15	10	0.00368	$0.7216 \pm 0.0041$
2.5	10	50	0.00125	$0.09521 \pm 0.00048$

Table B.4 – continued from previous page

Coupling (g)	$m_{Phi}$ [GeV]	$m_{\chi}$ [GeV]	rom previous $\Gamma_{min}$ [GeV]	$\sigma$ [pb]
2.5	50	50	0.0157	o.1158 ± o.00055
2.5	200	50	43.2	$0.475 \pm 0.0018$
2.5	300	50	70.8	$0.2214 \pm 0.0012$
2.5	5000	50	3064	1.868e-06 ± 1e-08
2.5	95	50	0.034	$0.421 \pm 0.0022$
2.5	10	150	0.00125	0.009221 ± 4.6e-05
2.5	200	150	0.12	$0.01604 \pm 6.7e-05$
2.5	500	150	234	$0.0206 \pm 8.7 e$ -05
2.5	5000	150	3062	$1.55 \text{e-}06 \pm 7.6 \text{e-}09$
2.5	295	150	0.395	$0.1314 \pm 0.0007$
2.5	10	500	0.00125	$8.948e-05 \pm 3.4e-07$
2.5	500	500	134	$0.0001273 \pm 5 e ext{-}07$
2.5	2000	500	1151	$3.922e-05 \pm 1.8e-07$
2.5	5000	500	3039	$4.732e-07 \pm 2e-09$
2.5	995	500	343	$0.0005315 \pm 2.5e-06$
2.5	10	1000	0.00125	$1.014e-06 \pm 4.2e-09$
2.5	1000	1000	345	$1.522e-06 \pm 7e-09$
2.5	5000	1000	2960	$6.909e-08 \pm 3.6e-10$
2.5	1995	1000	719	$6.791e-06 \pm 3.3e-08$
3⋅	10	1	3.51	$5.17 \pm 0.021$
3⋅	20	1	7.13	$4.262 \pm 0.017$
3.	50	1	17.9	$2.814 \pm 0.014$
3⋅	100	1	35.9	$1.595 \pm 0.0073$
3.	200	1	71.8	$0.651 \pm 0.0028$
3.	300	1	108	$0.3028 \pm 0.0014$
3.	500	1	372	$0.03314 \pm 0.00019$
3.	1000	1	854	$0.002641 \pm 1.5e-05$
3.	2000	1	1754	$0.0001496 \pm 5.3e-07$
3.	5000	1	4412	$3.035e-06 \pm 1.4e-08$
3.	10	10	0.0018	$1.214 \pm 0.0059$
3.	50	10	16.4	$2.849 \pm 0.012$
3.	100	10	35.1	$1.611 \pm 0.0071$
3.	5000	10	4412	$3.031e-06 \pm 2.1e-08$
3.	15	10	0.00530	$1.509 \pm 0.0076$
3.	10	50	0.00178	$0.1967 \pm 0.00093$
3.	50	50	0.0226	$0.242 \pm 0.0012$
3.	200	50	62.2	$0.6533 \pm 0.0033$
3.	300	50	102	$0.3011 \pm 0.0013$
3.	5000	50	4412	$2.974e-06 \pm 1.6e-08$
3.	95	50	0.0489	$0.8669 \pm 0.0046$
3.	10	150	0.0018	$0.01918 \pm 8.3\text{e-}05$
3.	200	150	0.173	$0.03357 \pm 0.00015$
3.	500	150	336	$0.02601 \pm 0.00013$
3⋅	5000	150	4409	$2.417e-06 \pm 1.1e-08$
3.	295	150	0.568	0.2747 ± 0.0017

Table B.4 – continued from previous page

Coupling (g)	m <sub>Phi</sub> [GeV]	$m_{\chi}$ [GeV]	$\Gamma_{min}$ [GeV]	σ [pb]
3.	10	500	0.0018	$0.0001847 \pm 7.2e-07$
3.	500	500	193	$0.0002634 \pm 1.2e-06$
3.	2000	500	1658	$4.736\text{e-}05 \pm 2.1\text{e-}07$
3.	5000	500	4376	$7.254$ e-07 $\pm$ $3.1$ e-09
3.	995	500	493	$0.0007379 \pm 3e-06$
3.	10	1000	0.0018	$2.087e-06 \pm 9.5e-09$
3.	1000	1000	496	$3.142e-06 \pm 1.3e-08$
3.	5000	1000	4263	$9.753 \text{e-}08 \pm 4 \text{e-}10$
3.	1995	1000	1035	$8.775$ e-06 $\pm$ 3.8e-08
3.5	10	1	4.78	$7.684 \pm 0.025$
3.5	20	1	9.71	$6.209 \pm 0.026$
3.5	50	1	24.4	$3.911 \pm 0.024$
3.5	100	1	48.8	$2.138 \pm 0.011$
3.5	200	1	97.7	$0.8426 \pm 0.0034$
3.5	300	1	147	$0.3824 \pm 0.0018$
3.5	500	1	506	$0.03921 \pm 0.00026$
3.5	1000	1	1163	$0.003103 \pm 1.6e-05$
3.5	2000	1	2387	$0.0001824 \pm 8e-07$
3.5	5000	1	6005	$4.039e-06 \pm 2.6e-08$
3.5	10	10	0.00245	$2.231 \pm 0.011$
3.5	50	10	22.4	$3.911 \pm 0.021$
3.5	100	10	47.8	$2.133 \pm 0.0093$
3.5	5000	10	6005	$4.037e-06 \pm 1.9e-08$
3.5	15	10	0.00722	$2.777 \pm 0.013$
3.5	10	50	0.00245	$0.3644 \pm 0.0016$
3.5	50	50	0.0308	$0.4471 \pm 0.002$
3.5	200	50	84.7	$0.8484 \pm 0.0041$
3.5	300	50	139	$0.3844 \pm 0.002$
3.5	5000	50	6005	$3.938e-06 \pm 2.2e-08$
3.5	95	50	0.0666	$1.603 \pm 0.01$
3.5	10	150	0.00245	$0.03531 \pm 0.00018$
3.5	200	150	0.235	$0.0618 \pm 0.00027$
3.5	500	150	458	$0.03087 \pm 0.00015$
3.5	5000	150	6001	$3.227e-06 \pm 1.6e-08$
3.5	295	150	0.773	$0.5139 \pm 0.0026$
3.5	10	500	0.00245	$0.0003434 \pm 1.5e-06$
3.5	500	500	263	$0.0004874 \pm 2e-06$
3.5	2000	500	2257	$5.311e-05 \pm 2.5e-07$
3.5	5000	500	5956	$9.439e-07 \pm 4.7e-09$
3.5	995	500	672	$0.0009553 \pm 3.7e-06$
3.5	10	1000	0.00245	$3.857e-06 \pm 1.9e-08$
3.5	1000	1000	675	$5.748e-06 \pm 2.4e-08$
3.5	5000	1000	5802	$1.197e-07 \pm 6.2e-10$
3.5	1995	1000	1409	1.037e-05 ± 4.9e-08

$m_{\chi}$	$m_{\Phi}$	σ [pb]	$m_{\chi}$	$m_{\Phi}$	σ [pb]
100	1000	1.50E-02	150	600	1.22E-01
100	100	1.13E-04	200	1000	7.04E-03
100	1300	7.05E-03	200	1300	2.11E-03
100	150	6.12E+00	200	200	6.29E-05
100	200	9.6oE+oo	200	250	5.83E-01
100	250	7.57E+00	200	300	1.64E+00
100	300	4.01E+00	200	400	9.08E-01
100	400	1.06E+00	200	600	1.11E-01
100	600	1.45E-01	35	250	9.62E+00
10	1000	3.55E-01	35	300	4.56E+00
10	100	7.67E+01	35	350	2.35E+00
10	10	2.43E-05	35	400	1.33E+00
10	1300	2.35E-01	35	500	5.48E-01
10	150	3.92E+01	35	550	3.80E-01
10	200	2.13E+01	35	600	2.76E-01
10	250	1.05E+01	35	650	2.07E-01
10	300	5.57E+00	35	700	1.60E-01
10	400	2.35E+00	50	1000	3.69E-02
10	50	1.51E+02	50	100	3.07E+01
10	600	8.16E-01	50	1300	2.39E-02
150	1000	9.44E-03	50	150	2.76E+01
150	1300	3.44E-03	50	200	1.82E+01
150	150	8.84E-05	50	250	9.31E+00
150	200	1.69E+00	50	300	4.40E+00
150	250	3.76E+00	50	400	1.22E+00
150	300	3.29E+00	50	50	1.04E-04
150	400	9.83E-01	50	600	2.14E-01

Table B.2: Dark matter masses  $m_\chi$  and mediator masses  $m_\Phi$  generated such that relic density constraints are fullfilled for 13 TeV. The resulting production cross sections are given in pb.

 $^{_{1950}}$  B.4 Cross sections for the  $bar{b}+DM$  scalar simplified model

[TODO: add cross-sections, they will be available with plots]

1955

# Appendix: Detailed studies for EW models

# C.1 Further W+MET models with possible cross-section enhancements

As pointed out in Ref. [BCD<sup>+</sup>15], the mono-W signature can probe the iso-spin violating interactions of dark matter with quarks. The relevant operators after the electroweak symmetry breaking is

$$\frac{1}{\Lambda^2} \overline{\chi} \gamma_{\mu} \chi \left( \overline{u}_L \gamma^{\mu} u_L + \xi \overline{d}_L \gamma^{\mu} d_L \right) . \tag{C.1}$$

Here, we only keep the left-handed quarks because the right-handed quarks do not radiate a *W*-gauge boson from the weak interaction. As the LHC constraints the cutoff to higher values, it is also important to know the corresponding operators before the electroweak symmetry. At the dimension-six level, the following operator

$$\frac{c_6}{\Lambda^2} \overline{\chi} \gamma_\mu \chi \, \overline{Q}_L \gamma^\mu Q_L \tag{C.2}$$

conserves iso-spin and provides us  $\xi=1$  [BCD<sup>+</sup>15]. At the dimension-eight level, new operators appear to induce iso-spin violation and can be

$$\frac{c_8^d}{\Lambda^4} \overline{\chi} \gamma_\mu \chi (H \overline{Q}_L) \gamma^\mu (Q_L H^\dagger) + \frac{c_8^u}{\Lambda^4} \overline{\chi} \gamma_\mu \chi (\tilde{H} \overline{Q}_L) \gamma^\mu (Q_L \tilde{H}^\dagger). \tag{C.3}$$

After inputting the vacuum expectation value of the Higgs field, we have

$$\xi = \frac{c_6 + c_8^d v_{\rm EW}^2 / 2\Lambda^2}{c_6 + c_8^u v_{\rm EW}^2 / 2\Lambda^2}.$$
 (C.4)

For a nonzero  $c_6$  and  $v_{\rm EW} \ll \Lambda$ , the iso-spin violation effects are suppressed. On the other hand, the values of  $c_6$ ,  $c_8^d$  and  $c_8^u$  depend on the UV-models.

There is one possible UV-model to obtain a zero value for  $c_6$  and non-zero values for  $c_8^d$  and  $c_8^u$ . One can have the dark matter and the SM Higgs field charged under a new U(1)'. There is a small mass mixing between SM Z-boson and the new Z' with a mixing angle of  $\mathcal{O}(v_{\rm EW}^2/M_{Z'}^2)$ . After integrating out Z', one has different effective dark matter couplings to  $u_L$  and  $d_L$  fields, which are proportional to their couplings to the Z boson. For this model,

we have  $c_6 = 0$  and

$$\xi = \frac{-\frac{1}{2} + \frac{1}{3}\sin^2\theta_W}{\frac{1}{2} - \frac{2}{3}\sin^2\theta_W} \approx -2.7$$
 (C.5)

959 and order of unity.

C.2 Simplified model corresponding to dimension-5 EFT oper-

As an example of a simplified model corresponding to the dimension-5 EFT operator described in Section 4.2, we consider a Higgs portal with a scalar mediator. Models of this kind are among the most concise versions of simplified models that produce couplings of Dark Matter to pairs of gauge-bosons. Scalar fields may couple directly to pairs of electroweak gauge bosons, but must carry part of the electroweak vev. One may thus consider a simple model where Dark Matter couples to a a scalar singlet mediator, which mixes with the fields in the Higgs sector.

$$L \subset m_s S^2 + \lambda S^2 H^2 + \lambda' S H^2 + y S \chi \overline{\chi}$$
 (C.6)

Where H is a field in the Higgs sector that contains part of the electroweak vev, S is a heavy scalar singlet and  $\chi$  is a Dark Matter field. There is then an S channel diagram where DM pairs couple to the singlet field S, which then mixes with a Higgs-sector field, and couples to W and Z bosons. This diagram contains 2 insertions of EW symmetry breaking fields, corresponding in form to the effective dimension-5 operator in Section 4.2.1.

1969 C.3 Tabulated cross-sections

1980

970 C.3.1 photon+MET signal, s-channel vector mediator model

1971 C.3.2 Higgs+MET signal, vector mediator model

Figure C.1 shows the cross sections in this vector mediator model in the  $m_{med}$  vs  $m_{DM}$  plane. The tabulated values can be found in Table C.1

1975 C.3.3 Higgs+MET signal, scalar mediator model

Figure C.2 shows the cross sections of the  $pp \to H\chi\bar{\chi}$  process in this vector mediator model in the  $m_{med}$  vs  $m_{DM}$  plane. The tabulated values can be found in Table C.2

C.3.4 Higgs+MET signal from 2HDM model with a Z' and a new pseudoscalar

The leading order cross-sections from the Madgraph generator for the signal samples are listed in Tables C.3, C.4, C.5, for the various scan points recommended.

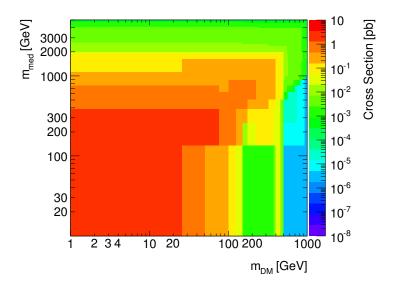


Figure C.1: Cross section of the  $pp \to H\chi\bar{\chi}$  process in units of pico-barn for the vector mediator model.

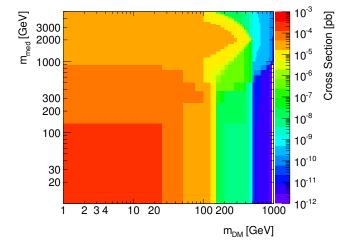


Figure C.2: Cross section of the  $pp \to H\chi\bar{\chi}$  process in units of picobarn for the scalar mediator model.

 $m_{DM}$  [GeV]  $m_{med}$  [GeV]  $\sigma_{pp\to h\chi\bar{\chi}}$  [pb] 0.0003835 0.0003177 0.0001467 0.0001065 6.867e-05 7.388e-05 7.858e-05 4.327e-05 4.018e-05 3.336e-05 3.603e-06 1.477e-05 0.0001547 0.0001104 4.5e-05 1.401e-07 2.099e-07 2.813e-05 4.82e-05 7.485e-05 3.384e-05 4.833e-09 3.65e-08 6.463e-07 2.407e-08 8.672e-12 1.157e-11 5.254e-10 7.138e-10 5.87e-10 5.946e-14 1.546e-13 8.316e-12 2.112e-11 

Table C.1: Cross section of the  $pp \to h\chi\bar{\chi}$  process in units of pico-barn for the vector mediator model.

$m_{DM}$ [GeV]	$m_{med}$ [GeV]	$\sigma_{pp  o h\chi\bar{\chi}}$ [pb]	
1	10	2.389	
1	20	2.483	
1	50	2.98	
1	100	2.881	
1	200	2.344	
1	300	2.041	
1	500	0.9328	
1	1000	0.1524	
1	2000	0.008919	
1	5000	1.39e-05	
10	10	0.01895	
10	15	0.7378	
10	50	2.929	
10	100	2.875	
10	5000	1.387e-05	
50	10	0.0003215	
50	50	0.01127	
50	95	0.2784	
50	200	1.868	
50	300	1.759	
50	5000	1.391e-05	
150	10	4.786e-06	
150	200	0.004841	
150	295	0.156	
150	500	0.575	
150	5000	1.391e-05	
500	10	6.296e-09	
500	500	2.855e-05	
500	995	0.008244	
500	2000	0.007899	
500	5000	1.355e-05	
1000	10	3.78e-11	
1000	1000	7.372e-07	
1000	1995	0.0004346	
1000	5000	1.245e-05	

Table C.2: Cross section of the  $pp \to h\chi\bar{\chi}$  process in units of pico-barn for the scalar mediator.

$M_{Z'}$ (GeV)	$M_{A^0}(GeV)$	σ [pb]
600	300	1.55E-01
600	400	2.18E-02
800	300	8.30E-02
800	400	2.72E-02
800	500	1.09E-02
800	600	2.98E-03
1000	300	3.74E-02
1000	400	1.53E-02
1000	500	8.91E-03
1000	600	4.89E-03
1000	700	2.21E-03
1000	800	7.05E-04
1200	300	1.70E-02
1200	400	7.65E-03
1200	500	5.14E-03
1200	600	3.52E-03
1200	700	2.25E-03
1200	800	1.27E-03
1400	300	8.00E-03
1400	400	3.79E-03
1400	500	2.75E-03
1400	600	2.09E-03
1400	700	1.58E-03
1400	800	1.06E-03

Table C.3: LO cross-sections for  $Z' \rightarrow$  $A^0h$  samples, varying  $M_{Z'}$  and  $M_{A^0}$ , keeping the DM mass fixed to 100 GeV. The columns from left to right describe  $M_{Z'}$ ,  $M_{A^0}$  and the sample cross section

$M_{Z'}$ (GeV)	$M_{A^0}(GeV)$	$M_{DM}(GeV)$	σ [pb]
1000	300	10	3.76E-02
1000	300	50	3.75E-02
1200	600	10	3.64E-03
1200	600	20	3.07E-03

Table C.4: LO cross-sections for  $Z' \rightarrow$  $A^0h$  samples, when varying  $M_{DM}$ . The columns from left to right describe  $M_{Z'}$ ,  $M_{A^0}$ ,  $M_{DM}$ , and the sample cross section in pb.

$M_{Z'}$ (GeV)	σ [pb]
600	1.15E-01
800	3.21E-02
1000	1.13E-02
1200	4.54E-03
1400	2.00E-03

Table C.5: LO cross-sections for  $Z' \rightarrow$ Zh exclusive samples, varying  $M_{Z'}$ . The columns from left to right describe  $M_{Z'}$  and the sample cross section in pb.

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# Appendix: Presentation of experimental results for reinterpretation

We suggest the following to collider searches, when presenting results from the recommended benchmarks:

- Provide limits in collider language, on fundamental parameters of interaction: couplings and masses of particles in simplified model.
- Translate limits to non-collider language, for a range of assumptions in order to convey a rough idea of the range of possibilities.

  The details of this point are left for work beyond the scope of this Forum.
- Provide all necessary material for theorists to reinterpret simplified model results as building blocks for more complete models
   (e.g. signal cutflows, acceptances, etc). This point is detailed
   further in this appendix.
  - As detailed in [KAM<sup>+</sup>12], model-independent results in terms of limits on cross-section times acceptance of new phenomena should be provided for all cases, but especially when EFTs are employed as benchmarks.

Along with the design of new searches to hunt for new physics at the LHC, it is important to consider information needed in order to reinterpret the searches outside of the collaborations. The following is a non-exhaustive list of recommendations in order to make reinterpretation easier and faster. This appendix details considerations for reimplementation of the analysis as well as for using the simplified model results directly given by the collaborations.

One of the important developments in recent years is an active development of the analyses recasting codes [DFK+15, CDFW14, KSTR15, CY11, KPSW]. The aim of these codes is to provide a public library of reimplemented and validated LHC analyses. Such libraries can then be used to analyze validity of a BSM scenario in a systematic and effective manner. The availability of public libraries further facilitates a unified framework and can lead to an organized and central structure to preserve LHC information in a long run.

In order to be able to develop such codes, it is important to get complete and systematic information from the collaborations.

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Data digitization: Availability of digitized data is one of the primary requirement. All information given by collaborations in the form of plots should be made available in a digitized format. Platforms such as HepData can be used in oder to maintain a centralised manner. In case when HepData can not be used, digitised data can be provided via analyses twiki pages. This information primarily includes expected and observed exclusion lines along with their  $\pm 1\sigma$  uncertainty, expected and observed upper limits in case of simplified models, efficiency maps and all kinematic distributions as reported in the analysis. Units should be clearly specified. If the digitised figures are made available as a C macro or a ROOT file, the names of the objects should be clearly identifiable e.g. expected upper limits of a particular topology/model given as a ROOT file can be labeled as KEY: TH2D ExpectedUpperLimit; 1. Furthermore, these digitised files can potentially contain more information (larger axes ranges) than displayed on the plot. This will help facilitate understand what happens beyond the limits displayed in the plot, e.g. a distribution for number of jets can be artificially limited to a point in the plot (for the purpose of clarity of figure), however, this artificial limit leads to a sharp cutoff in the plot. While validating the analysis it is often necessary to compare the distributions beyond such artificial limits, having this information digitised will be of a great help in such cases.

#### D.1 Reimplementing analyses

This section lists information necessary in order to reimplement an analysis. Analysis reimplementation usually consists of several stages. Usually, one starts with reading the analysis note carefully, following which the preselection and event selection cuts are identified. These are then mimicked using a code typically written in C++. The detector simulation is carried out by using public detector simulation softwares e.g. Delphes [dF<sup>+</sup>14]. The resulting ROOT file is then analysed using the C++ code written in the previous step.

• Analysis documentation: The collaborations should provide a cutflow table with every analysis, such a cutflow table will naturally define the order of cuts implemented in an analysis. There are several preselection criteria which can not be easily simulated in phenomenology, e.g. MET cleaning. Numbers should be provided after such cuts so that theorists can rescale their number of events in order to account for such cuts. Efficiencies of several reconstructed objects are given as an input to detector simulation software like Delphes. It is thus very useful to get parametrised efficiencies for reconstructed objects (as a function of the rapidity  $\eta$  and/or transverse momentum  $p_T$ ), along with the working

points at which they were evaluated (e.g. loose, tight selection). Object definitions should be clearly identifiable.

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- Validation: Validation corresponds to re-deriving the results as given by collaborations in order to verify that the implementation of the analysis is correct. Usually most of the bug catching takes place in the phase of validation. The following items are necessary in order to recreate the results.
  - Monte Carlo generators: Monte Carlo generators along with the exact versions used to produce the event files should be listed.
  - Production cross sections: The order of production cross sections (e.g. LO,NLO,NLL) as well as the codes which were used to compute them should be provided. A table of reference cross sections for several values of particle masses such as ones provided by SUSY cross section working group will be highly appreciated.
  - Process Generation: Details of the generated process, detailing number of additional partons generated.
  - Availability of the LHE files: selected LHE files (detailing at least a few events if not the entire file) corresponding to the benchmarks listed in the analysis should be made available in order to cross check process generation. Experimental collaborations may generate events on-the-fly without saving the intermediate LHE file; we advocate that the cross-check of process generation is straight-forward if this information is present, so we encourage the generation of a few selected benchmark points allowing for a LHE file to be saved. For models concerning SUSY, corresponding SLHA files of benchmark files should also be details. Special attention should be paid to list the parameters which change the production cross section or kinematics of the process e.g. mixing angles.
  - Process cards: Process cards includes PDF choices, details of matching algorithms and scales and details of process generation. If process cards are not available, above items should be clearly identified.
  - MadGraph model files: For models which are not already implemented in MadGraph, availability of the corresponding model files is highly desired. It details the exact notation used in the model and hence sets up a complete framework. In case MadGraph is not used, enough information should be provided in order to clearly identify the underlying model used for interpretations.
- Limit setting: Detailed description of the likelihood used in order to derive the limits should be given, this can contain statistical procedure within the analysis text itself, however direct availability of the limit setting code as a workspace in RooStats or HistFitter [BBC+15] is highly desirable.

- **Binned backgrounds**: For analyses using techniques such as sliding windows or an unbinned technique, the Standard Model backgrounds should be given in the form of bins. These backgrounds can then be interpolated.
  - Recast code: Finally, the collaborations can provide an analysis
    code directly implemented in one of the public recasting codes
    detailed above. Such codes can be published via INSPIRE in
    order to track the versioning and citations.

#### D.2 Simplified model interpretations

The analyses almost always provide at least one simplified model interpretation along with the search results. These interpretations are simple and can be used in order to take a quick survey of viability of parameter space. Codes such as [KKL<sup>+</sup>14b, KKL<sup>+</sup>14a, PSWZ14] can make use of the simplified model results given in the form of 95% Confidence Level (CLs) upper limit or efficiency maps in order to test Beyond the Standard Model parameter space. It will thus be extremely useful if the results are given in a form as easily usable by the theory community.

- Direct usability of the results: The results given should be as useful as possible. For example, for a simplified model containing dark matter mass  $m_{\rm DM}$ , mediator mass  $M_{\rm med}$  and couplings  $g_{\rm DM}$ ,  $g_{\rm q}$  it will be extremely useful to have 95% CLs upper limits on the product of couplings  $\sqrt{g_{\rm DM}g_{\rm q}}$  or cross section times branching ratio as a function of  $m_{\rm DM}$ ,  $M_{\rm med}$ . Limits on visible cross sections of the simplified models considered for interpretations should be made available.
- Smooth grids: The usage of simplified model results relies on interpolating between upper limit values. In order to facilitate the interpolation, regions where large variation of upper limits is observed should contain denser grid, if a uniform grid over the entire plane is not possible. For simplified model involving more than three parameters (two masses and product of couplings), slices of upper limits in the additional dimensions will be very useful e.g. for a simplified model involving one step cascade decay, upper limits can be provided for several values of intermediate mass in the plane of mother daughter masses. Results with only one slice often render invalid to be used in a general model testing.
- Availability of acceptance and efficiency maps: Finally, acceptance and efficiency maps for all the signal regions involved in the analysis should be made available. These results are not only useful for model testing using simplified models but also to validate implementation of the analysis. Information about the most sensitive signal region as a function of masses is also very useful in order to determine the validity of approximate limit setting

- $_{\mbox{\tiny 2157}}$   $\,\,\,\,\,\,\,\,\,$  procedures being used by theorists (in the absence of any other
- sophisticated limit setting technique).

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