

# Dark Matter Working Group recommendation for Two Higgs Doublet Model (draft title)

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**Abstract.** Draft abstract.

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## Contents

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### 1 Introduction

#### Reasoning behind this effort

- Simplified models only one signature at a time, sometimes not gauge invariant
- One step beyond this: less-simplified models
- Compare and confront different search sensitivity
- Combinations among different signatures
- Find new kinematic regimes / improve searches by exploring different signatures
- Still keeping the choice of model generic enough that this is reusable for theorists

#### Reasoning behind this effort

- Reasoning behind the choice of model
- Highlights more than one signature at a time, depending on parameters
- Leaves room for new unexplored kinematic signatures within existing searches (left for future work)
- Complete enough, still simplified so that one can choose grid planes
- Existing theory effort (HXS WG)

### 2 The model

#### Description of the model

- Citations: [? ? ? ? ? ]
- Particles, masses, couplings, mixing angles

**Comparison with existing models** How does the model compare with other 2HDMs/scalar models (with and without DM).

- Scalar to SSM to 2HDM evolution
- Other models:
  - S. Ipek, D. McKeen, A. Nelson, [? ]
  - Bell, Busoni, Sanderson, [? ]
  - No, Goncalves, Machado, [? ? ]
  - Higgs Cross-section Working Group

### 3 Model parameters

- Motivate the choice of parameters in [?] ]
- Vacuum stability study: fix lambda parameters to 3

For extension of the Higgs sector (and in general for scalar extensions of the Standard Model) one needs to worry about boundedness from below of the scalar potential, as well as absolute stability of the electroweak minimum<sup>1</sup>.

Regarding boundedness from below of the scalar potential in the present 2HDM + S model, we stress that provided that  $\lambda_{P1}, \lambda_{P2} > 0$  in

$$V_P = \frac{1}{2}m_P^2 P^2 + \kappa (i P H_1^\dagger H_2 + \text{h.c.}) + \lambda_{P1} P^2 |H_1|^2 + \lambda_{P2} P^2 |H_2|^2 ,$$

the study of boundedness from below at tree-level reduces to the corresponding study in the 2HDM. The boundedness from below conditions in this case are well-known [? ]:

$$\lambda_1 > 0, \lambda_2 > 0, \lambda_3 > -\sqrt{\lambda_1 \lambda_2}, \lambda_3 + \lambda_4 - |\lambda_5| > -\sqrt{\lambda_1 \lambda_2} \quad (3.1)$$

and can be inferred from analyzing the scalar potential at large field values  $H_1, H_2 \gg v$ . For  $m_{H^\pm} = m_{H_0}$ , the first two conditions in (??) may be simply written as

$$\frac{m_h^2}{v^2} (1 - t_\beta^2) + \lambda_3 t_\beta^2 > 0, \quad \frac{m_h^2}{v^2} (1 - t_\beta^{-2}) + \lambda_3 t_\beta^{-2} > 0 \quad (3.2)$$

which result in the requirement  $\lambda_3 > m_h^2/v^2 = 0.258$ . In figure ?? we show the regions of parameter space in the  $(m_a, m_{H_0})$  (left) and  $(s_\theta, m_a)$  (right) planes for which the tree-level boundedness from below conditions ?? are satisfied, assuming  $m_{H^\pm} = m_{H_0} = m_{A_0}$ .

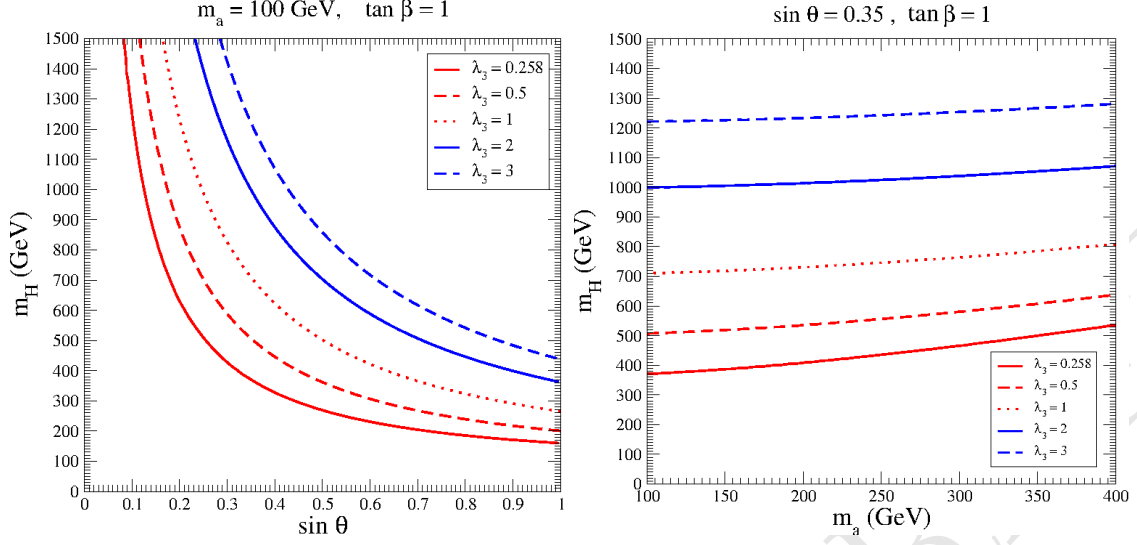
Figure ?? shows that the region satisfying the tree-level boundedness from below conditions increases as  $\lambda_3$  increases. At the same time, the choice  $\lambda_3 = \lambda_{P1} = \lambda_{P2}$  which we adopt in the present analysis allows the increase in  $\lambda_3$  not to affect the mono-Higgs sensitivity via a change in the coupling  $g_{aAh}$

$$\begin{aligned} g_{aAh} &= \frac{c_\theta s_\theta}{m_H v} [m_h^2 + m_H^2 - m_a^2 - 2(\lambda_3 - \lambda_{P1} c_\beta^2 - \lambda_{P2} s_\beta^2) v^2] \\ &= \frac{c_\theta s_\theta}{m_H v} [m_h^2 + m_H^2 - m_a^2] \end{aligned} \quad (3.3)$$

We then fix the value  $\lambda_3 = 3$  as benchmark for the rest of our analysis.

A few comments are in order.

<sup>1</sup>We remark here that implications from all indirect constraints - be it flavour, electroweak precision constraints or stability requirements - should be treated as preferred parameter space in a simplified model framework. It would contradict the idea of simplified models were these constraints taken at face value.



**Figure 1:** Regions of parameter space in the  $(m_a, m_{H_0})$  (left) and  $(s_\theta, m_a)$  (right) planes for which the tree-level boundedness from below conditions ?? are satisfied, assuming  $m_{H^\pm} = m_{H_0} = m_{A_0}$ .

- The choice of  $\lambda_3$ , motivated by boundedness from below conditions, while not affecting the mono-Higgs sensitivity if  $\lambda_3 = \lambda_{P1} = \lambda_{P2}$ , has an impact on the mono- $Z$  sensitivity since the coupling

$$\begin{aligned}
 g_{Haa} &= \frac{1}{m_H v} \left[ 2 t_{2\beta}^{-1} s_\theta^2 (m_h^2 - \lambda_3 v^2) + s_{2\beta} c_\theta^2 v^2 (\lambda_{P1} - \lambda_{P2}) \right] \\
 &= \frac{1}{m_H v} \left[ 2 t_{2\beta}^{-1} s_\theta^2 (m_h^2 - \lambda_3 v^2) \right]
 \end{aligned} \tag{3.4}$$

does depend on  $\lambda_3$  and influences the balance between  $\Gamma(H_0 \rightarrow aa)$  and  $\Gamma(H_0 \rightarrow Za)$  which ultimately determines the  $H_0 \rightarrow Za$  branching fraction. In short, the choice of  $\lambda_3$ ,  $\lambda_{P1}$ ,  $\lambda_{P2}$  affects either mono-Higgs or mono- $Z$  sensitivities (or both).

- Together with boundedness from below, other potential constraints are usually considered in the context of the 2HDM and apply in general, among them unitarity (see e.g. [? ? ]) and absolute stability of the electroweak vacuum (see e.g. [? ]). In the present context we find these constraints are generically weaker than the boundedness from below condition and therefore disregard them in the following.
- The boundedness from below conditions are here evaluated at tree-level, but in a fully consistent treatment they should be evaluated including the effect of radiative corrections. This is however a much more involved process than what has been discussed above for the tree-level case (see e.g. [? ]). In addition, the boundedness from below constraints discussed here are potentially sensitive to the existence of UV physics which our 2HDM+S simplified does not capture, and which could modify the above picture through the presence

of higher-dimensional operators. Still, it is worth pointing out that for the 2HDM+S simplified model to be a good description of LHC phenomenology we require the new physics scale suppressing these effective operators to be above the TeV scale (since in our scans we are considering scalar masses up to  $\sim 1$  TeV), and thus the presence of these high-energy operators is not expected to be of much help in case a runaway field direction exist at tree level in the 2HDM scalar potential.

## 4 Parameter grid

### 4.1 Parameter scans on masses, couplings and mixing angles

#### Logic of how we proceeded

- Starting from benchmark 3 of [?] ]
- Mapping the kinematics and sensitivity of the model by scanning some of the various parameters
- Checking whether other existing models can be rescaled

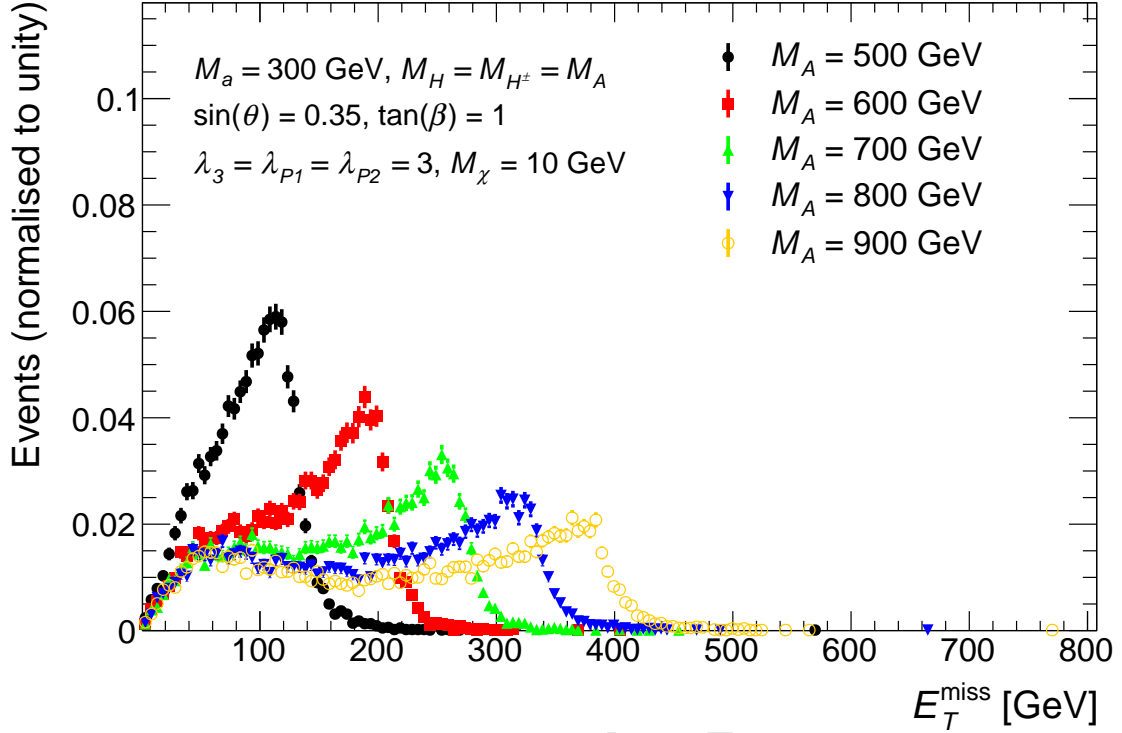
#### 4.1.1 Results of studies

Each of the signatures should have the following plots in the planes of the final recommendation:

- efficiency at parton level with simplified, published cuts
- total and fiducial cross-section at parton level
- 2 - 3 kinematic plots of what has been scanned that are most representative for the analysis (here the analysers decide, then we harmonize at the end)

Signatures:

- Mono-Z (lep/had)
- MonoH $\rightarrow$ bb
- Monojet
- ttbar+MET, with specific discussion about rescaling
- other signatures who have not yet presented at public meetings, in ATLAS and CMS



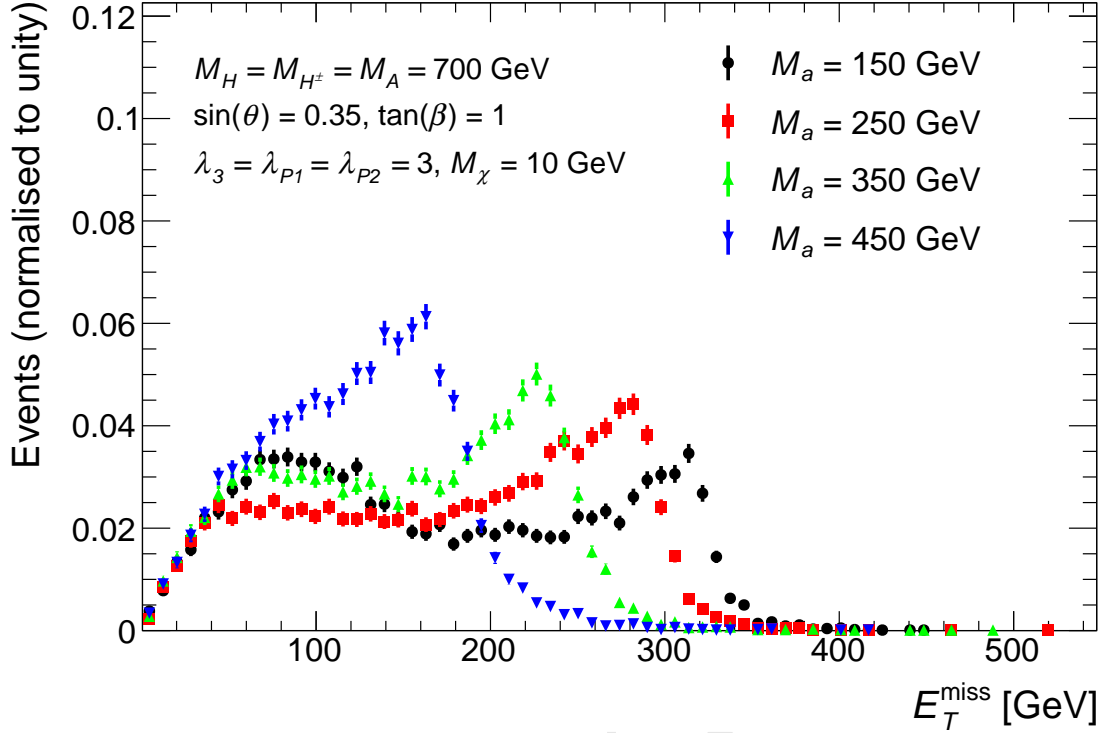
**Figure 2:** Missing transverse momentum distribution  $h \rightarrow bb + E_T^{\text{miss}}$  signal events at parton level for five representative models with different  $M_A (= M_H = M_{H^\pm})$  and fixed  $M_a = 300$  GeV,  $\sin \theta = 0.35$ ,  $\tan \beta = 1$ ,  $M_\chi = 10$  GeV and  $\lambda_{P1} = \lambda_{P2} = \lambda_3 = 3$ . Models with a larger  $M_A - M_a$  splitting have harder  $E_T^{\text{miss}}$  (s.a. ??).

#### 4.1.2 Studies of the $h(bb) + E_T^{\text{miss}}$ signature

The studies of the  $h(bb) + E_T^{\text{miss}}$  channel presented here are based on Monte Carlo simulations with version 2.4.3 of MadGraph 5 [?] using a Universal FeynRules Output [?] implementation of the 2HDM with Dark Matter mediator with a Yukawa sector of type II provided by the authors of [?]. The PDF set used for these simulations is the NNPDF collaboration's NNPDF30\_lo\_as\_0130 PDF set, a leading order five-flavor (assuming massless  $b$ -quarks) PDF set with  $\alpha_S(m_Z) = 0.130$  [?]. For the matrix element calculation in MG5, the five-flavor scheme is chosen, and the  $b$ -quark mass set to zero.

The matrix element generated for the parton-level studies is  $gg \rightarrow h\chi\bar{\chi}$ . For the  $M_a - \tan \beta$  scan (??, ??), the matrix element  $b\bar{b} \rightarrow h\chi\bar{\chi}$  is also generated. The additional matrix element is generated because at high  $\tan \beta$  and for a Yukawa sector of type II, the  $b\bar{b}$  initiated process can have an amplitude as large as, or even larger than, the gluon fusion initiated process [?]. However, gluon fusion dominates the remaining parameter space, so for all other scans the  $b\bar{b}$  initiated process is neglected.

**Signal kinematics** The masses  $M_A$  and  $M_a$  of the pseudoscalars  $A$  and  $a$  affect the  $h(bb) + E_T^{\text{miss}}$  signal in two ways:



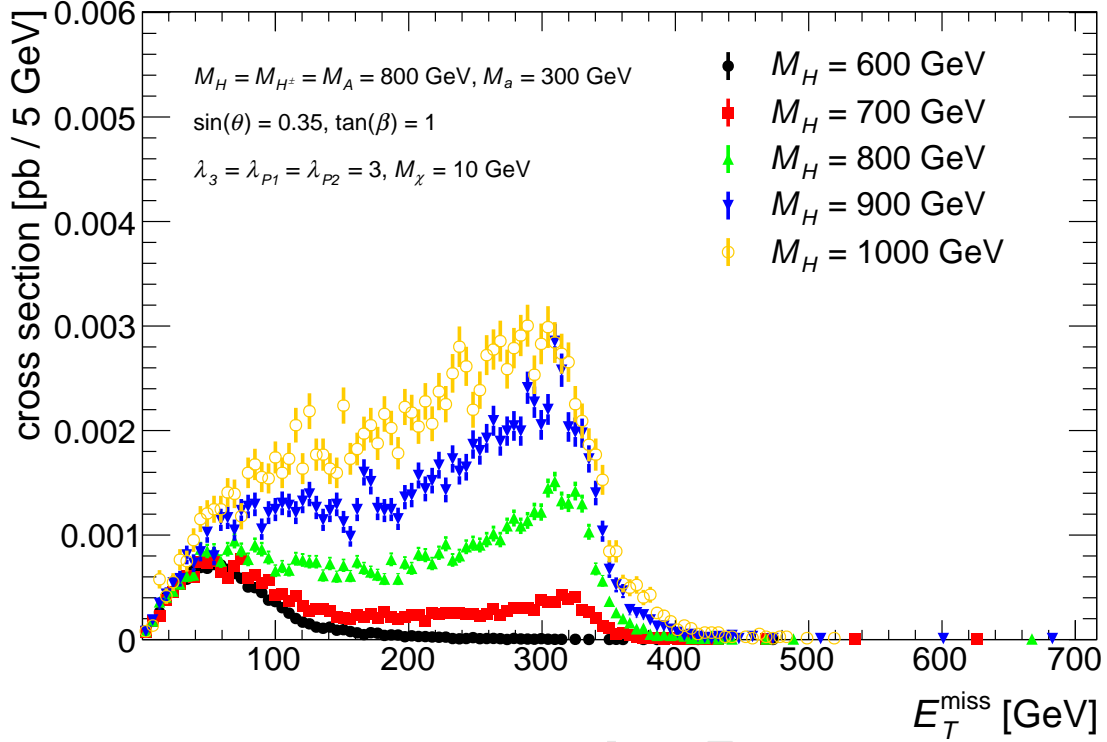
**Figure 3:** Missing transverse momentum distribution in  $h \rightarrow bb + E_T^{\text{miss}}$  signal events at parton level for four representative models with different  $M_a$  and fixed  $M_A = M_H = M_{H^\pm} = 700$  GeV,  $\sin \theta = 0.35$ ,  $\tan \beta = 1$ ,  $M_\chi = 10$  GeV and  $\lambda_{P1} = \lambda_{P2} = \lambda_3 = 3$ . Models with higher  $M_a$  have softer  $E_T^{\text{miss}}$  (s.a. ??).

- by changing the location of the Jacobian peak in the  $E_T^{\text{miss}}$  distribution
- by changing the overall signal cross-section

The latter effect can be seen in ???. The former is crucial to searches for  $h(bb) + E_T^{\text{miss}}$  such as [?], since the  $E_T^{\text{miss}}$  observable can be used to reduce many standard model backgrounds. Standard model backgrounds are often characterized by low  $E_T^{\text{miss}}$ , unlike Dark Matter signal processes with potentially very high  $E_T^{\text{miss}}$ .

The Jacobian peak is the result of a resonantly produced pseudoscalar  $A$  decaying in the  $1 \rightarrow 2$  decay  $A \rightarrow ah$ , where the  $h$  proceeds to decay into a mostly visible final state ( $h \rightarrow b\bar{b} \rightarrow \text{hadrons}$ ), and the  $a$  into an invisible one ( $a \rightarrow \chi\bar{\chi}$ ). The kinematics of  $1 \rightarrow 2$  processes are fixed by the masses of the involved particles. Thus the resonant  $A \rightarrow ah$  process has a sharply peaked resonance<sup>2</sup> in the invariant mass distribution of the final state system. This results in a peak in the momentum distribution of the Dark Matter system, and the transverse component of the Dark Matter momentum is reconstructed as the missing transverse momentum ( $E_T^{\text{miss}}$ ). This peak in the  $E_T^{\text{miss}}$  distribution resulting from the resonant signal process is called the Jacobian peak.

<sup>2</sup>with a finite width due to the widths of  $a$ ,  $A$  and  $h$



**Figure 4:** The  $E_T^{\text{miss}}$  distribution of the production cross section of  $h \rightarrow bb + E_T^{\text{miss}}$  signal events for five representative models with different  $M_H = M_{H^\pm}$  and fixed  $M_A = 800$  GeV,  $M_a = 300$  GeV,  $\sin \theta = 0.35$ ,  $\tan \beta = 1$ ,  $M_\chi = 10$  GeV and  $\lambda_{P1} = \lambda_{P2} = \lambda_3 = 3$ .

Since it is determined by the masses of the particle involved in the signal process, the location of the Jacobian peak can be calculated analytically [? ]:

$$E_T^{\text{miss}, \text{max}} \approx \frac{\sqrt{(M_A^2 - M_a^2 - M_h^2)^2 - 4M_a^2 M_h^2}}{2M_A} \quad (4.1)$$

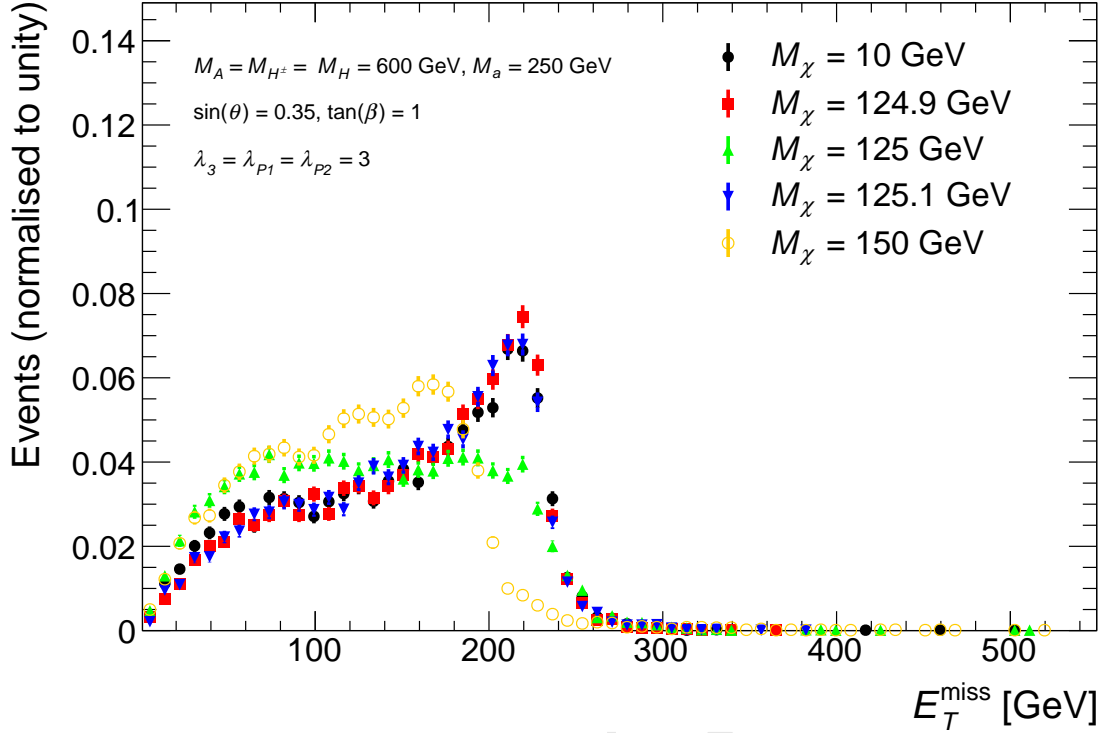
Thus increasing  $M_A$  leads to a Jacobian peak at higher  $E_T^{\text{miss}}$ , and vice versa (??). Conversely, models with higher  $M_a$  have a Jacobian peak at lower  $E_T^{\text{miss}}$ , and vice versa (??). Because they determine the location of the Jacobian peak,  $M_A$  and  $M_a$  strongly affect the sensitivity of a search for  $h(bb) + E_T^{\text{miss}}$  to a given model. For this reason, one of the proposed parameter scans for the 2HDM with pseudoscalar Dark Matter mediator is a scan in the  $(M_a, M_A)$  plane.

Some fraction of signal events is due to non-resonant  $2 \rightarrow 3$  processes  $gg \rightarrow h\chi\bar{\chi}$ . Due to the larger number of kinematic degrees of freedom, these processes have a broadly distributed invariant mass of the final state system. This in turn generates a broad distribution dominated by soft  $E_T^{\text{miss}}$ , distinct from the Jacobian peak discussed above. All the models in ?? and ?? also have low- $E_T^{\text{miss}}$  non-resonant contributions.

The mass of the heavy neutral<sup>3</sup> scalar  $H$  has an indirect effect on the rate and kine-

<sup>3</sup>For simplicity, we only consider the case of the neutral scalar  $H^\pm$  being mass-degenerate to  $H$ .

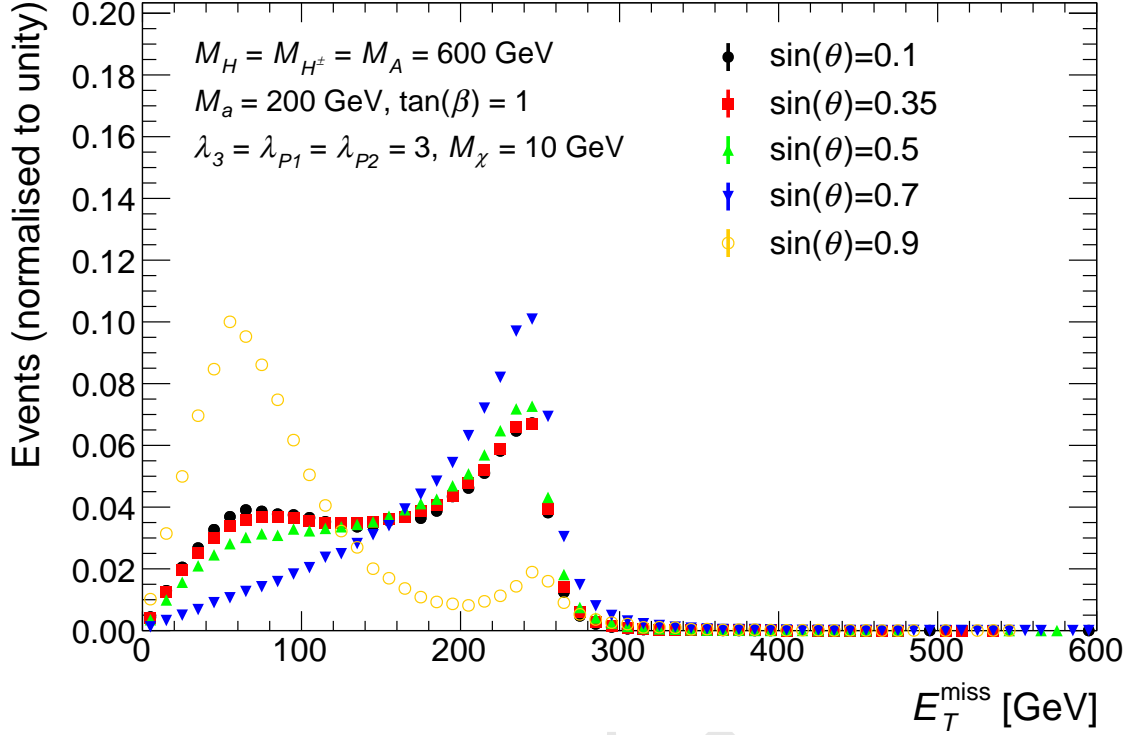




**Figure 5:** Missing transverse momentum distribution of  $h \rightarrow bb + E_T^{\text{miss}}$  signal events at parton level for five representative models with different  $M_\chi$  and fixed  $M_A = M_H = M_{H^\pm} = 600$  GeV,  $M_a = 250$  GeV,  $\sin \theta = 0.35$ ,  $\tan \beta = 1$  and  $\lambda_{P1} = \lambda_{P2} = \lambda_3 = 3$ . The shape of the  $E_T^{\text{miss}}$  distribution does not change for  $M_\chi < M_a/2$ , then changes significantly for  $M_\chi \geq M_a/2$ .

matics of the signal. This is caused by  $M_H$  changing the widths and couplings of the pseudoscalars  $A$  and  $a$ . Changing  $M_H$  can scale the signal cross-section up or down, and change the fraction of resonant vs. non-resonant signal events (??). The choice  $M_H (= M_{H^\pm}) = M_A$  gives a measurable cross-section for many signal points as well as a significant fraction of resonant signal events.

The mass  $M_H$  of the Dark Matter fermion  $M_\chi$  can change the cross-section and shape of the  $E_T^{\text{miss}}$  distribution, depending on the place of  $M_\chi$  in the mass hierarchy (??). If the Dark Matter is above the production threshold ( $M_\chi < M_a/2$ ), changing it has no effect on either kinematics or cross-section. The only exception is the case  $M_a/2 > M_\chi > M_a/2 - M_h$  (given a sufficiently heavy scalar  $a$ ). With such values of  $M_\chi$  non-resonantly producing an  $h$  simultaneously with an on-shell  $a (\rightarrow \chi\bar{\chi})$  becomes kinematically forbidden. However, this contribution is negligible for most of the parameter points in the scans presented here. If the Dark Matter is on threshold ( $M_\chi = M_a/2$ ), the signal cross section is significantly enhanced. This enhancement on threshold drops off rapidly towards both higher and lower  $M_\chi$ . Furthermore, the shape of the  $E_T^{\text{miss}}$  distribution at threshold differs significantly from the one below threshold, since amplitudes involving decays  $a \rightarrow \chi\bar{\chi}$  make up a larger

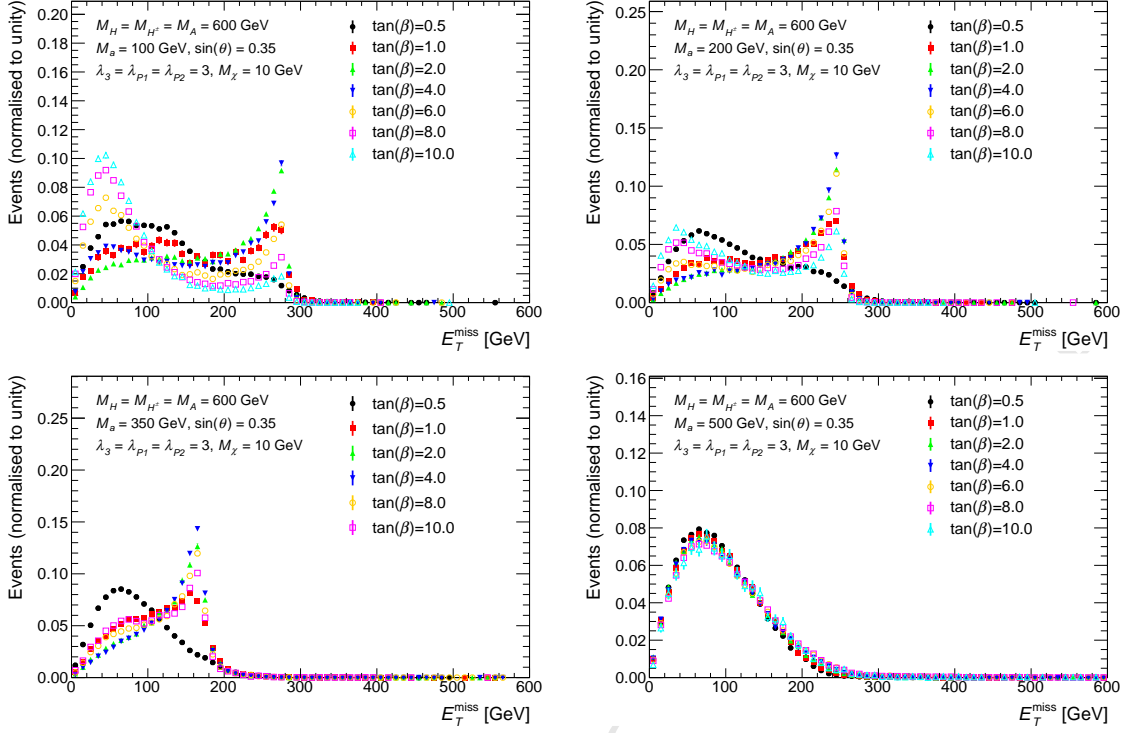


**Figure 6:** Missing transverse momentum distribution of  $h \rightarrow bb + E_T^{\text{miss}}$  signal events at parton level for five representative models with different  $\sin \theta$  and fixed  $M_A = M_H = M_{H^\pm} = 600 \text{ GeV}$ ,  $M_a = 200 \text{ GeV}$ ,  $M_\chi = 10 \text{ GeV}$ ,  $\tan \beta = 1$ , and  $\lambda_{P1} = \lambda_{P2} = \lambda_3 = 3$ . The shape of the  $E_T^{\text{miss}}$  distribution does not change much for  $\sin \theta < 0.7$ , then changes significantly for  $\sin \theta \geq 0.7$ . When  $\sin \theta = 0.9$ , the diagram  $gg \rightarrow a \rightarrow A^*h \rightarrow \chi\bar{\chi}h$ , producing a  $E_T^{\text{miss}}$  peak at around 60 GeV, starts to dominate.

fraction of all signal events. Below threshold ( $M_\chi > M_a/2$ ), the signal cross-section quickly drops by several orders of magnitude. In this regime, the shape of the  $E_T^{\text{miss}}$  distribution changes with  $M_\chi$  continuously.

The sine of the mixing angle between the two pseudoscalars  $A$  and  $a$ ,  $\sin \theta$ , affects not only the cross section, but also the shape of the  $E_T^{\text{miss}}$  distribution (??). For the resonant diagram  $gg \rightarrow A \rightarrow ah \rightarrow \chi\bar{\chi}h$ , the product of cross section times branching ratios  $\mathcal{B}(A \rightarrow ah)\mathcal{B}(a \rightarrow \chi\bar{\chi})$  scales with  $\sin^2 \theta \cos^6 \theta$ , while for the diagram  $gg \rightarrow a \rightarrow A^*h \rightarrow \chi\bar{\chi}h$ , the product of cross section times branching ratios  $\mathcal{B}(a \rightarrow Ah)\mathcal{B}(A \rightarrow \chi\bar{\chi})$  scales with  $\sin^6 \theta \cos^2 \theta$ . Therefore, at small  $\sin \theta$ , the resonant diagram  $A \rightarrow ah$  is the dominant production mode and the  $E_T^{\text{miss}}$  distribution has a Jacobian peak following ??; while at large  $\sin \theta$ , the  $a \rightarrow A^*h$  diagram starts to dominate and produces a second peak at a lower  $E_T^{\text{miss}}$  value.

The shape of  $E_T^{\text{miss}}$  distribution also has a non-trivial dependence on  $\tan \beta$  (??). As discussed in the sensitivity study later, at small  $\tan \beta$ , the Yukawa coupling to top quark is large and the signal production mode is dominated by the non-resonant 3-body

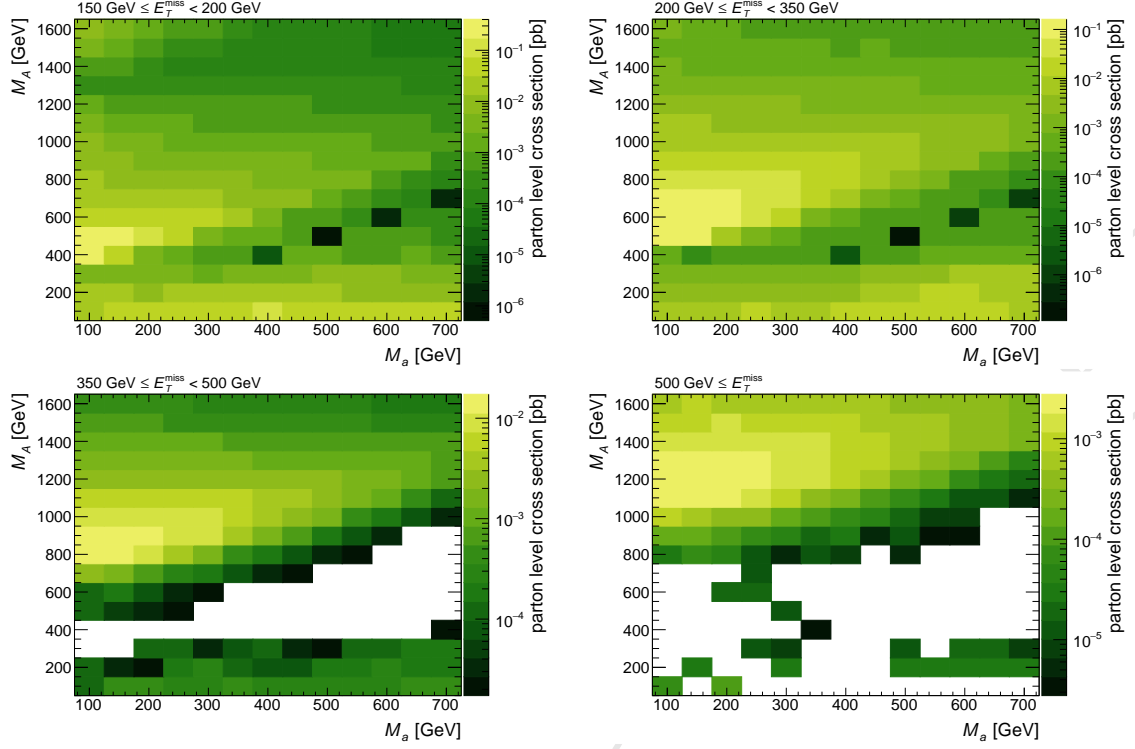


**Figure 7:** Missing transverse momentum distribution of  $h \rightarrow bb + E_T^{\text{miss}}$  signal events at parton level with different  $\tan\beta$  and fixed  $M_A = M_H = M_{H^\pm} = 600$  GeV,  $M_\chi = 10$  GeV,  $\sin\theta = 0.35$ , and  $\lambda_{P1} = \lambda_{P2} = \lambda_3 = 3$ . The values of  $M_a$  are set to 100, 200, 350, and 500 GeV, respectively. The shapes of the  $E_T^{\text{miss}}$  distributions for different  $\tan\beta$  are similar when  $M_A < M_h + M_a$ . Note, in these figures, both the contributions of  $gg$  and  $b\bar{b}$  initiated processes are included and a combined histogram is produced according to their corresponding cross sections.

processes  $gg \rightarrow h\chi\bar{\chi}$ , which gives a broad and soft  $E_T^{\text{miss}}$  spectrum. As  $\tan\beta$  increases, the contribution of resonant production increases as well and the Jacobian peak also appears. When the pseudoscalar  $A$  is produced off-shell, i.e. when  $M_A < M_a + M_h$ , the shapes of  $E_T^{\text{miss}}$  distributions become similar and the dependence on  $\tan\beta$  disappears.

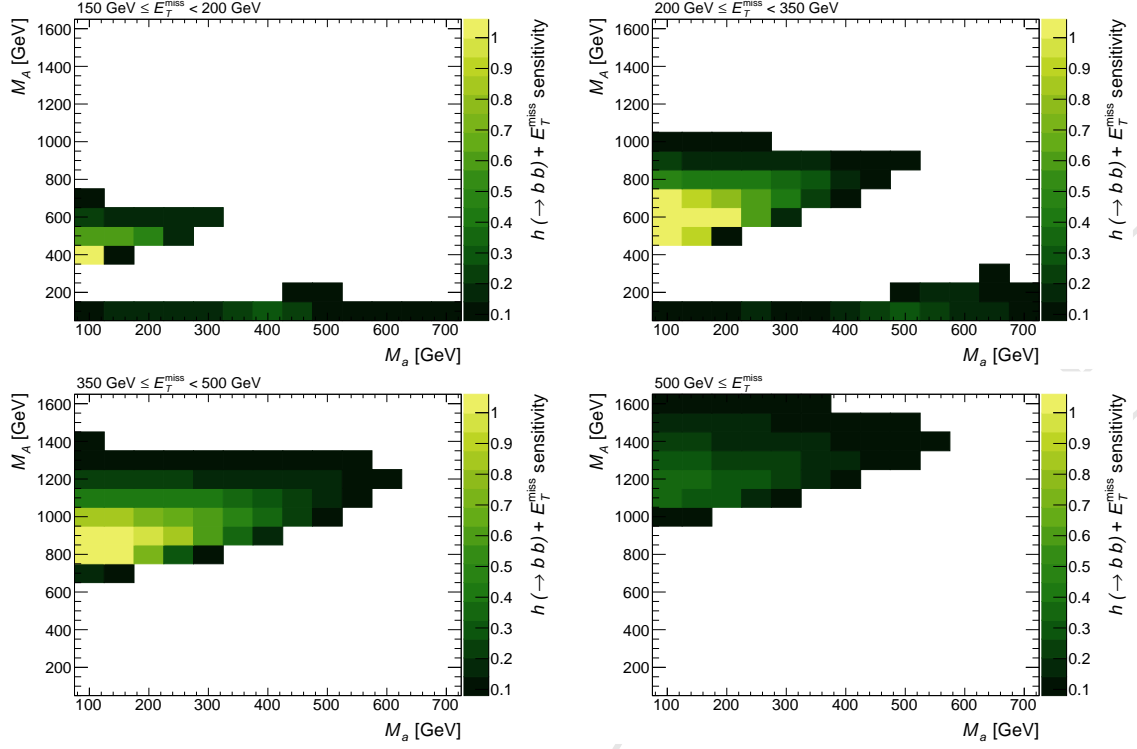
**Sensitivity estimate** The sensitivity of the search for  $h(bb) + E_T^{\text{miss}}$  described in [?] to the 2HDM with pseudoscalar Dark Matter mediator is estimated based on the limits with minimal model dependence from [?]. This allows one to directly use parton-level simulations of the 2HDM with pseudoscalar Dark Matter mediator as inputs for the estimate. Since there is no need to simulate the detector response, which is very costly in terms of CPU-time, the sensitivity can be estimated quickly. In this way, more iterations on different versions of the signal grid can be performed.

The limits with minimal model dependence are given in [?] in terms of the visible cross-section of  $h(bb) + E_T^{\text{miss}}$  events. To compare these values to the parton level simulation results, an estimate of the detector efficiency as well as the acceptance of the event



**Figure 8:** The production cross-section of  $h \rightarrow bb + E_T^{\text{miss}}$  signal events at parton level as a function of  $(M_A, M_a)$  in each of the four  $E_T^{\text{miss}}$  bins. The remaining parameters take the values  $M_H = M_{H^\pm} = M_A$ ,  $\sin \theta = 0.35$ ,  $\tan \beta = 1$ ,  $M_\chi = 10$  GeV and  $\lambda_{P1} = \lambda_{P2} = \lambda_3 = 3$ .

selections of the analysis is needed. This estimate is provided in [?] in terms of a single acceptance times efficiency ( $\mathcal{A} \times \epsilon$ ) value per  $E_T^{\text{miss}}$  bin. The value of  $\mathcal{A} \times \epsilon$  corresponds to the probability that an event generated at parton level in a given  $E_T^{\text{miss}}$  bin is reconstructed in that same  $E_T^{\text{miss}}$  bin and passes all selections. The limits with minimal model dependence are provided separately for each of the four  $E_T^{\text{miss}}$  bins used in [?]. Thus, the simulated events are binned into those bins (??). Then the simulated cross-section in one  $E_T^{\text{miss}}$  bin is compared to the limit with minimal model dependence in that  $E_T^{\text{miss}}$  bin (??). In this way, one gets four separate sensitivity estimates. To obtain a single number estimating the sensitivity of a search that uses all four  $E_T^{\text{miss}}$  bins, the individual contributions are



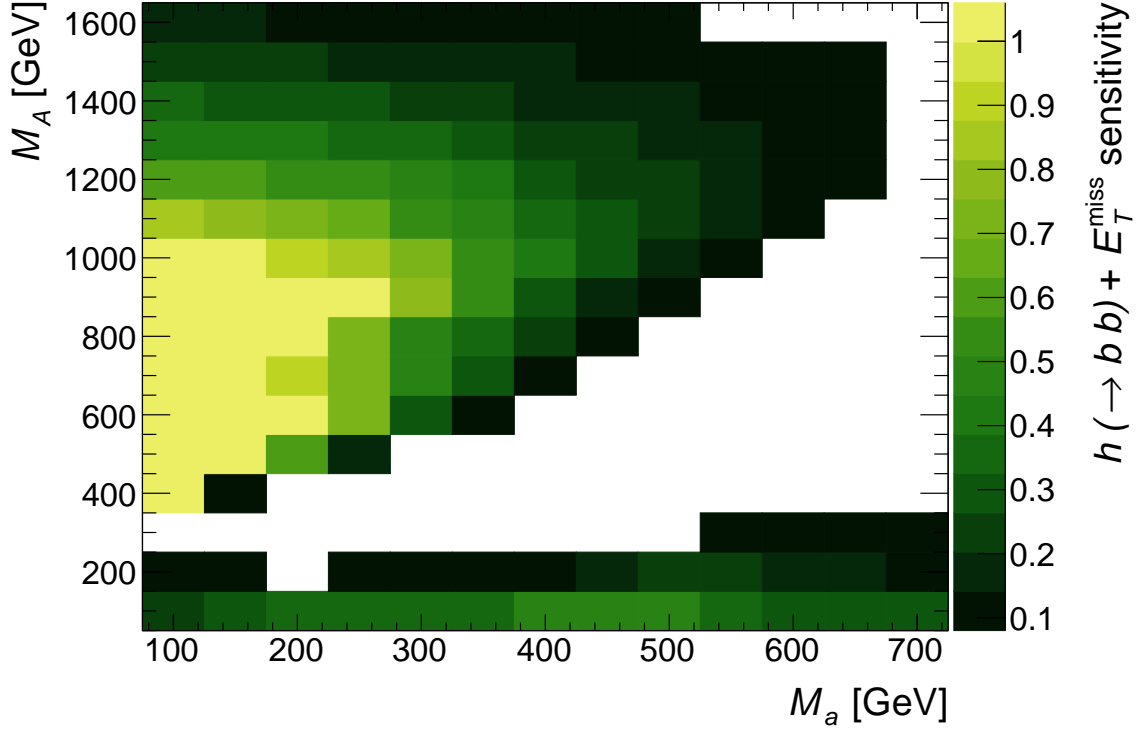
**Figure 9:** Estimated sensitivity to  $h \rightarrow bb + E_T^{\text{miss}}$  events as a function of  $(M_A, M_a)$  in each of the four  $E_T^{\text{miss}}$  bins. The sensitivity, defined in Eq. ??, is based on the limits with reduced model dependence from Ref. [? ]. The remaining parameters take the values  $M_H = M_{H^\pm} = M_A$ ,  $\sin \theta = 0.35$ ,  $\tan \beta = 1$ ,  $M_\chi = 10$  GeV and  $\lambda_{P1} = \lambda_{P2} = \lambda_3 = 3$ .

summed<sup>4</sup> (??). Thus the sensitivity is estimated as

$$\begin{aligned}
 S^m &= \sum_i^{E_T^{\text{miss}}\text{-bins}} S_i^m \\
 &= \sum_i^{E_T^{\text{miss}}\text{-bins}} \frac{\sigma_i^{m,\text{parton}}(h\chi\bar{\chi}) \times \mathcal{BR}_{\text{SM}}(h \rightarrow b\bar{b}) \times [\mathcal{A} \times \epsilon]_i}{\sigma_i^{\text{observed}}(h(bb) + E_T^{\text{miss}})},
 \end{aligned} \tag{4.2}$$

where  $m$  is a particular model,  $i$  is a particular  $E_T^{\text{miss}}$  bin,  $S_i^m$  the sensitivity to model  $m$  based on  $E_T^{\text{miss}}$ -bin  $i$  (??),  $\sigma_i^{m,\text{parton}}(h\chi\bar{\chi})$  the parton level  $h\chi\bar{\chi}$  production cross-section in bin  $i$  predicted by model  $m$  (??),  $\mathcal{BR}_{\text{SM}}(h \rightarrow b\bar{b})$  the  $h \rightarrow b\bar{b}$  branching ratio predicted by the standard model for  $M_h = 125$  GeV,  $[\mathcal{A} \times \epsilon]_i$  the acceptance times efficiency in bin  $i$  as given in [? ], and  $\sigma_i^{\text{observed}}(h(bb) + E_T^{\text{miss}})$  the limit on the  $h(bb) + E_T^{\text{miss}}$  cross-section observed in [? ] in  $E_T^{\text{miss}}$  bin  $i$ .

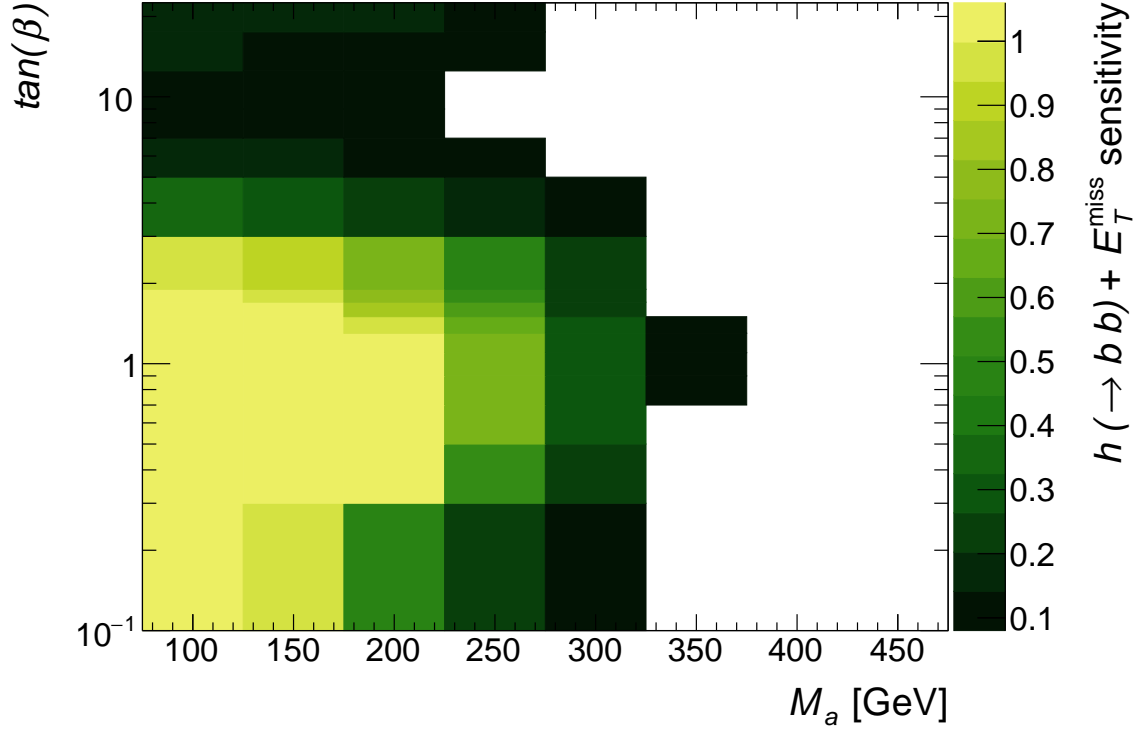
<sup>4</sup>This implies that there could be models where the sensitivity in every bin is  $< 1$ , yet the sum is  $> 1$ . This is desired for the purpose of estimating sensitivity when designing the grid to be used in a dedicated search, since one expects that the full search will be able to exclude those models. But for actually excluding models based on the limits with minimal model dependence, the sum is not appropriate. A better choice for the purpose of exclusion is e.g. the sensitivity of the most sensitive bin.



**Figure 10:** Sum over all  $E_T^{\text{miss}}$ -bins of the estimated sensitivity to  $h \rightarrow bb + E_T^{\text{miss}}$  events as a function of  $(M_A, M_a)$ . The sensitivity, defined in Eq. ??, is based on the limits with reduced model dependence from Ref. [? ]. The remaining parameters take the values  $M_H = M_{H^\pm} = M_A$ ,  $\sin \theta = 0.35$ ,  $\tan \beta = 1$ ,  $M_\chi = 10$  GeV and  $\lambda_{P1} = \lambda_{P2} = \lambda_3 = 3$ .

The  $h(bb) + E_T^{\text{miss}}$  sensitivity in the sense of eq. ?? to a scan in the  $(M_a, M_A)$  plane is shown in ??. The sensitivity drops with increasing  $M_A = M_H = M_{H^\pm}$  for  $M_A \geq 1$  TeV because the fraction of resonant signal events drops. The drop in the fraction of resonant signal events is caused by increasingly large  $\Gamma_A$ , which allows an increasing fraction of non-resonant signal events, driven by events with very off-shell  $A$ . Non-resonant signal events have soft  $E_T^{\text{miss}}$  and thus the search is less sensitive to them, since the minimum accepted  $E_T^{\text{miss}}$  is  $E_T^{\text{miss}} \geq 150$  GeV. Near the mass diagonal  $M_a = M_A$ , there is little to no sensitivity. This is because the Jacobian peak is at soft  $E_T^{\text{miss}}$  for a low mass-splitting  $M_A - M_a$  (??, ??, and ??). Furthermore the coupling  $g_{Aah}$  is small when all Higgs bosons are nearly mass degenerate [? ], giving a small total cross-section, and lowering the sensitivity even further. The sensitivity above the mass diagonal ( $M_A > M_a$ ) is larger than the sensitivity below the mass diagonal ( $M_A < M_a$ ). Two parameter choices cause this asymmetry:

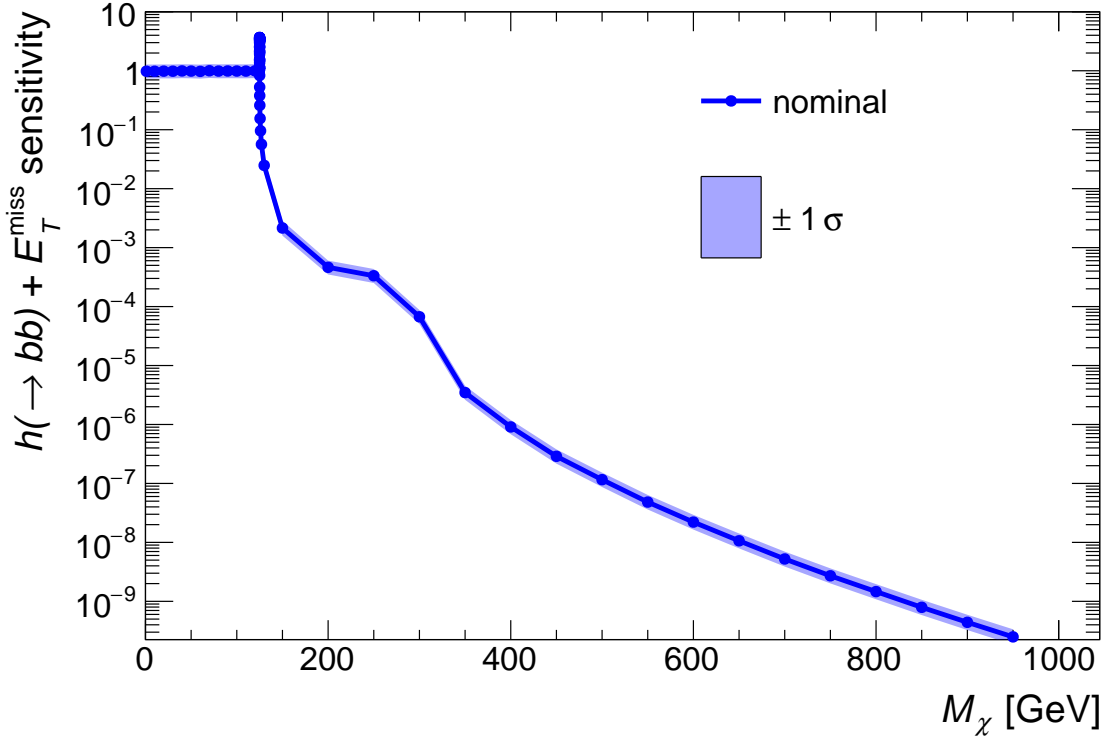
1.  $M_A = M_H = M_{H^\pm}$ , i.e. the neutral and charged CP-even scalars have low masses below the diagonal, but high masses above it, introducing asymmetry. In ?? one can see that values of  $M_H = M_{H^\pm}$  below the mass of the higher-mass pseudoscalar give a reduced overall cross-section and a lower fraction of resonant signal events. Both effects reduce sensitivity.



**Figure 11:** Sum over all  $E_T^{\text{miss}}$ -bins of the estimated signal sensitivity to  $h \rightarrow bb + E_T^{\text{miss}}$  events as a function of  $(M_a, \tan \beta)$ . The sensitivity, defined in Eq. ??, is based on the limits with reduced model dependence from Ref. [? ]. The remaining parameters take the values  $M_H = M_{H^\pm} = M_A = 600$  GeV,  $\sin \theta = 0.35$ ,  $M_\chi = 10$  GeV and  $\lambda_{P1} = \lambda_{P2} = \lambda_3 = 3$ .

2.  $\sin \theta = 0.35 \neq 1/\sqrt{2}$ , i.e. the pseudoscalar mixing is asymmetric.  $A$  couples comparatively more strongly to SM particles than  $a$ , and vice versa for the couplings to the Dark Matter fermion  $\chi$ . So the situation below the diagonal corresponds to the case of  $\sin \theta = \sqrt{1 - 0.35^2} \approx 0.938$  and  $M_A > M_a$ . As can be seen in ?? and ?? this configuration has a larger fraction of soft, nonresonant signal events, and correspondingly lower sensitivity (?? and ??).

For a scan in  $(M_a, \tan \beta)$  the sensitivity is shown in ??. At very low  $\tan \beta$ , the yukawa coupling to top quarks is large, and most of the signal events come from non-resonant processes. The non-resonant processes give soft  $E_T^{\text{miss}}$ , which lowers the signal acceptance and reduces the sensitivity of the search. For higher  $\tan \beta$  the fraction of resonant events increases, due to the reduced top Yukawa coupling, increasing the sensitivity. However reducing the top yukawa coupling also reduces the overall production cross-section. This effect is sub-dominant below  $\tan \beta \approx 1.2$ , and the sensitivity increases with  $\tan \beta$ . But above  $\tan \beta \approx 1.2$ , the sensitivity loss due to reduced cross-section outpaces the sensitivity gain due to a more resonant signal. Therefore, above  $\tan \beta \approx 1.2$ , the search gets less sensitive with higher  $\tan \beta$ . At very high  $\tan \beta (\geq 10)$ , this trend is reversed again, as the



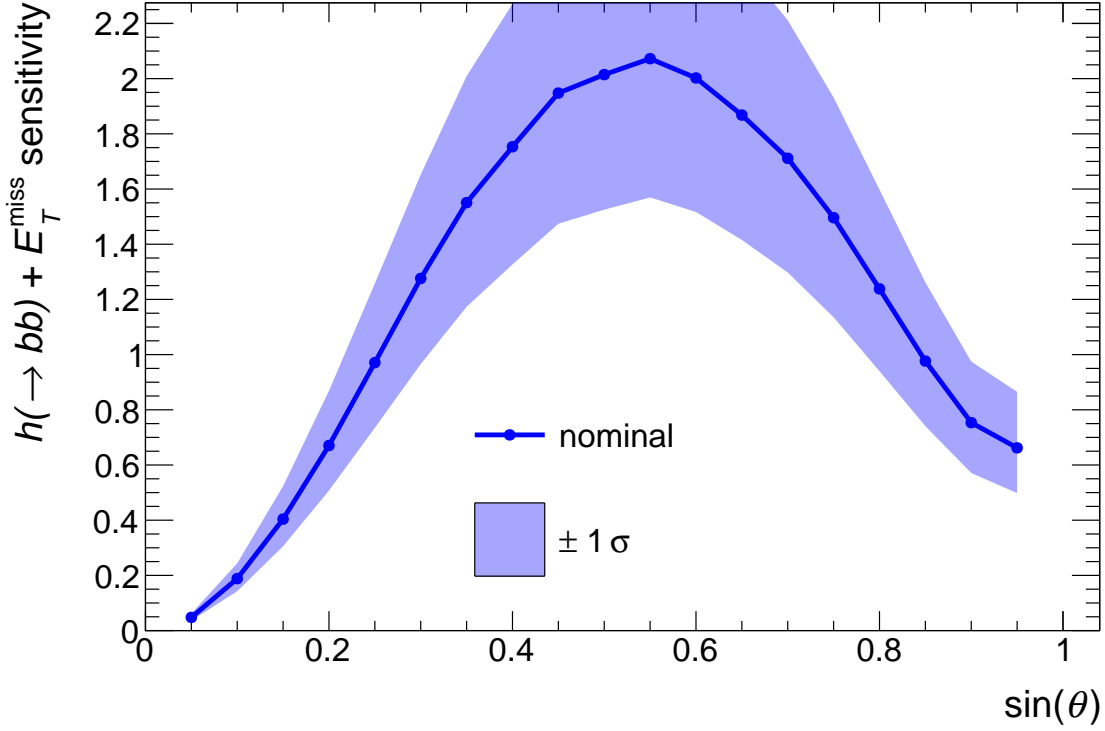
**Figure 12:** Sum over all  $E_T^{\text{miss}}$ -bins of the estimated signal sensitivity to  $h \rightarrow bb + E_T^{\text{miss}}$  events as a function of the Dark Matter mass  $M_\chi$ . The sensitivity, defined in Eq. ??, as well as the uncertainty on the sensitivity (shaded blue) are based on the limits with reduced model dependence from Ref. [?] and the uncertainties described therein. The remaining parameters take the values  $M_a = 250$  GeV,  $M_H = M_{H^\pm} = M_A = 600$  GeV,  $\sin \theta = 0.35$ ,  $\tan \beta = 1$ , and  $\lambda_{P1} = \lambda_{P2} = \lambda_3 = 3$ . The sensitivity is constant below  $M_\chi < M_a/2$ , and rapidly drops for  $M_\chi > M_a/2$ . The sensitivity is enhanced for  $M_\chi = M_a/2$ .

$\tan \beta$  enhancement<sup>5</sup> of the coupling to b-quarks relative to top quarks becomes so large that it compensates for the lower b quark Yukawa coupling corresponding to the lower b-quark mass. At this point  $b\bar{b}$  initiated processes start to dominate the production cross-section and drive the increase in sensitivity.

The sensitivity to models with varying  $\sin \theta$  is shown in Figs. ?? and ??. The sensitivity is 0 at  $\sin \theta = 0$  and  $\sin \theta = 1$ , since those values correspond to no mixing, and thus no coupling. So the sensitivity is in general not monotonous in  $\sin \theta$  (?). For intermediate values,  $\sin \theta$  influences the couplings of the pseudoscalars to Dark Matter, as well as to standard model fermions, and also the coupling strength of trilinear scalar vertices such as  $g_{Aah}$  [?]. Increasing the couplings increases the cross-section and thereby the sensitivity. However, increasing some couplings can also increase  $\Gamma_A$  and thereby decrease the resonant fraction of signal events. This means that there can be more than one local maximum in the sensitivity curve (?). The number and location of maxima and

<sup>5</sup>we are considering a Yukawa sector of type II

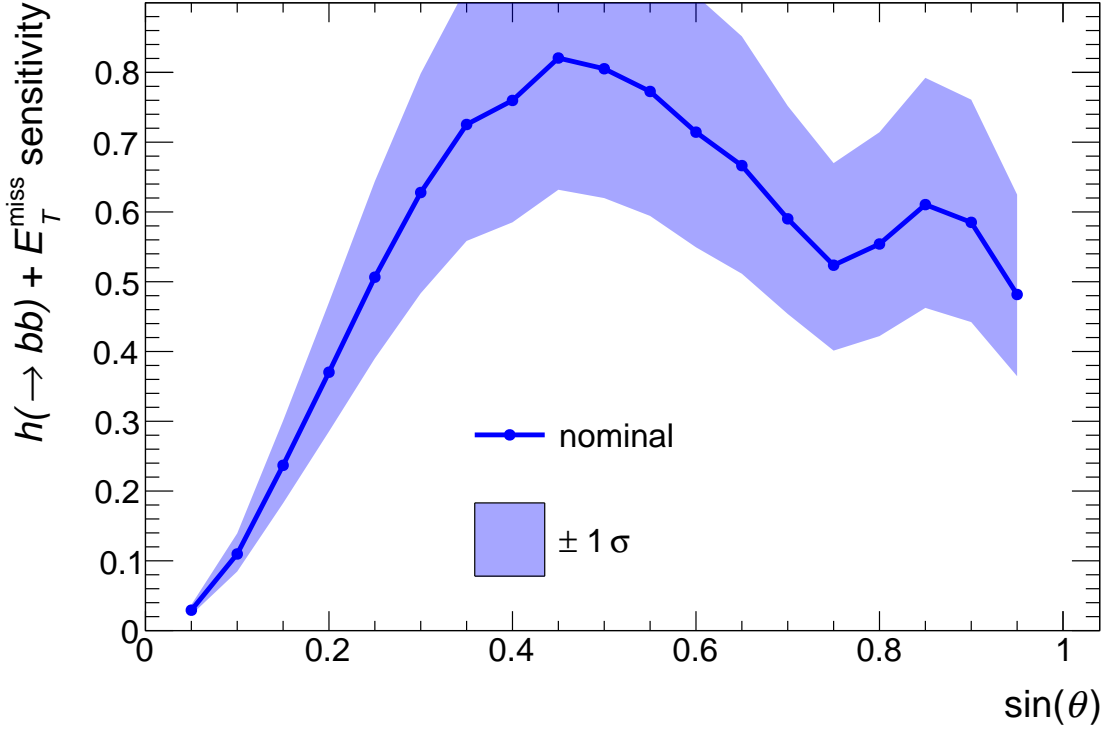




**Figure 13:** Sum over all  $E_T^{\text{miss}}$ -bins of the estimated signal sensitivity to  $h \rightarrow bb + E_T^{\text{miss}}$  events as a function of the pseudoscalar mixing parameter  $\sin \theta$ . The sensitivity, defined in Eq. ??, as well as the uncertainty on the sensitivity (shaded blue) are based on the limits with reduced model dependence from Ref. [?] and the uncertainties described therein. The remaining parameters take the values  $M_a = 200$  GeV,  $M_H = M_{H^\pm} = M_A = 600$  GeV,  $M_\chi = 10$  GeV,  $\tan \beta = 1$ , and  $\lambda_{P1} = \lambda_{P2} = \lambda_3 = 3$ .

turning points in the sensitivity depends on the precise interplay of the couplings. The couplings depend on all other model parameters including all the Higgs masses, so tuning the  $\sin \theta$  of a parameter scan to the sensitivity in a single point can lead to sub-optimal sensitivity in other points.

The sensitivity to models with varying  $M_\chi$  is shown in ?. Above threshold ( $M_\chi < M_a/2$ ), the sensitivity stays constant. This constant sensitivity results from the constant signal  $E_T^{\text{miss}}$  shape (?), and the constant signal cross-section. At threshold ( $M_\chi = M_a$ ) the sensitivity is enhanced because the partial width for  $a \rightarrow \chi\bar{\chi}$  is enhanced, increasing the signal cross-section. Below threshold ( $M_\chi > M_a/2$ ), the sensitivity drops rapidly. The reason for the rapid drop in sensitivity is that  $M_\chi > M_a/2$  requires a virtual  $a^* \rightarrow \chi\bar{\chi}$  decay in the signal event. The rate of this virtual  $a$  decay is strongly suppressed by the typically narrow width of  $a$ . The width of  $a$  is substantially reduced once  $a \rightarrow \chi\bar{\chi}$  is kinematically inaccessible, as  $\Gamma_{a \rightarrow \chi\bar{\chi}}$  is a large contribution to the total width of  $a$  for  $M_\chi \leq M_a/2$  [?]. There is a slight bump in sensitivity for  $M_\chi \approx M_A/2$ , when the  $A \rightarrow \chi\bar{\chi}$  hits it's threshold, but the absolute sensitivity remains negligible.



**Figure 14:** Sum over all  $E_T^{\text{miss}}$ -bins of the estimated signal sensitivity to  $h \rightarrow bb + E_T^{\text{miss}}$  events as a function of the pseudoscalar mixing parameter  $\sin \theta$ . The sensitivity, defined in Eq. ??, as well as the uncertainty on the sensitivity (shaded blue) are based on the limits with reduced model dependence from Ref. [?] and the uncertainties described therein. The remaining parameters take the values  $M_a = 350$  GeV,  $M_H = M_{H^\pm} = M_A = 1000$  GeV,  $M_\chi = 10$  GeV,  $\tan \beta = 1$ , and  $\lambda_{P1} = \lambda_{P2} = \lambda_3 = 3$ .

#### 4.1.3 Studies of the mono-Z (leptonic) signature

Mono-Z analyses use events with a reconstructed Z boson recoiling symmetrically against  $E_T^{\text{miss}}$  to detect the production of invisible particles. In previous LHC analyses [? ?], the DM interpretations of the analysis results have focused on either invisible decays of the SM-like Higgs bosons or topologies where the Z boson is produced as initial-state radiation (ISR) off a quark. The ISR-based topologies generically favor radiation of a gluon or photon rather than a massive gauge boson, thus limiting the discovery sensitive of a Z-based approach compared to monojet and mono-photon searches. In contrast, the model studies in this document generates the mono-Z signature dominantly via the all-bosonic H-a-Z vertex, which can lead to enhancements of the mono-Z sensitivity compared to jet and photon signature. In this section, the behavior and experimental accessibility of the model in  $Z + E_T^{\text{miss}}$  events is studied.

**Technical setup** Simulated event samples for the mono-Z signature are produced with Madgraph5\_aMC@NLO version 2.4.3, interfaced with Pythia version 8.2.2.6 for parton

**Table 1:** Event selection requirements for the analysis of the Mono-Z signature with leptonic Z decays. The requirements are inspired to follow those used in typical experimental analyses.

Selection stage	Quantity	Requirement
Inclusive	lepton $ \eta $	$< 2.5$
	leading (trailing) lepton $p_T$	$> 25(20) \text{ GeV}$
Preselection	$ m_{ll} - m_{Z,\text{nominal}} $	$< 15 \text{ GeV}$
	$E_T^{\text{miss}}$	$> 40 \text{ GeV}$
Final selection	$\Delta\Phi(ll, E_T^{\text{miss}})$	$> 2.7$
	$ p_{T,u} - E_T^{\text{miss}} /p_{T,u}$	$< 0.4$
	$\Delta R(ll)$	$< 1.8$

showering. The NNPDF3.0 PDF set is used at LO precision with the value of the strong coupling constant set to  $\alpha_S(M_Z) = 0.130$  (NNPDF30\_lo\_as\_0130). Only contributions from gluon-gluon initial states and  $l^+ l^- \chi\bar{\chi}$  final states are considered, where  $l = e$  or  $\mu$ . No additional matrix element partons are considered and diagrams with an intermediate s-channel SM Higgs boson are explicitly rejected to increase the calculation efficiency (generate  $g g \rightarrow \chi\bar{\chi} l^+ l^- / h1$ ).

**Event selection** Three consecutive stages of event selection are considered:

- Inclusive: Lepton  $p_T$  and  $\eta$  requirements corresponding to the typical experimental trigger acceptance are applied.
- Preselection: A dilepton candidate with an invariant mass in a window around the Z mass is required, and a minimum transverse momentum of the  $\chi\bar{\chi}$  system is required.
- Final selection: Requirements on the main variables used in the relevant analyses are added: The angular separation in the transverse plane between the  $\chi\bar{\chi}$  and  $l^+ l^-$  systems  $\Delta\Phi(ll, E_T^{\text{miss}})$ , the relative transverse momentum difference between them  $|p_{T,u} - E_T^{\text{miss}}|/p_{T,u}$  and the angular separation between the leptons  $\Delta R(ll)$ . Additionally, the  $E_T^{\text{miss}}$  requirement is tightened.

The exact event selection criteria are listed in Tab. ??.

**Cross-sections, kinematic distributions and acceptance** The overall cross-sections in the  $\tan\beta$  and mass scans are shown in Fig. ?. In the mass scan, maximal cross-sections are observed for the region of  $M_a < M_A$  for values of  $M_a \gtrsim 100 \text{ GeV}$ . Towards higher values of both  $M_a$  and  $M_A$ , the cross-sections fall off, reaching values smaller than 1 fb at  $M_a \approx 450 \text{ GeV}$  or  $M_A \approx 1.1 \text{ TeV}$ . In the  $M_a \approx M_A$ -region, the cross-section is suppressed by destructive interference. For the region with inverted mass hierarchy  $M_a > M_A$ , cross-sections of the order of multiple fb are observed, as long as  $|M_a - M_A|$  remains sufficiently large. In the  $\tan\beta$  scan, cross-sections smoothly fall with increasing  $M_a$  as well as  $\tan\beta$ . Cross-sections are typically larger than 1 fb up to  $\tan\beta \approx 5$ . The dependence on  $M_a$

is modulated by the value of  $\tan\beta$ : Crossing the  $M_a$  range from 100 to 400 GeV, cross-sections are reduced by a factor  $\approx 7$  for small  $\tan\beta \approx 1$ , but only a factor  $\approx 2$  for higher values of  $\tan\beta \approx 5$ .

Acceptances for the mass and  $\tan\beta$  scans are shown in Figures ?? and ?. In the mass scan, from  $M_a = 100$ ,  $M_A = 250$  to  $M_a = 350$ ,  $M_A = 450$ , we can see that for mass points where the Jacobian Peak is below the  $E_T^{\text{miss}}$  cut of the analysis, acceptances drop sharply approaching zero. Above this region, the acceptance curves are grouped into bands for fixed values of  $M_A - M_a$ . For large values of  $M_A$ , the acceptance changes more gradually and reaches a maximum value of 50%. In the inverted mass region, the acceptance is generally lower than in the rest of the mass scan, but can reach values as large as 30% for light values of  $M_A$ . In the  $\tan\beta$  scan, the acceptance is largely independent of  $\tan\beta$  and is constant for equal values of  $M_a$ .

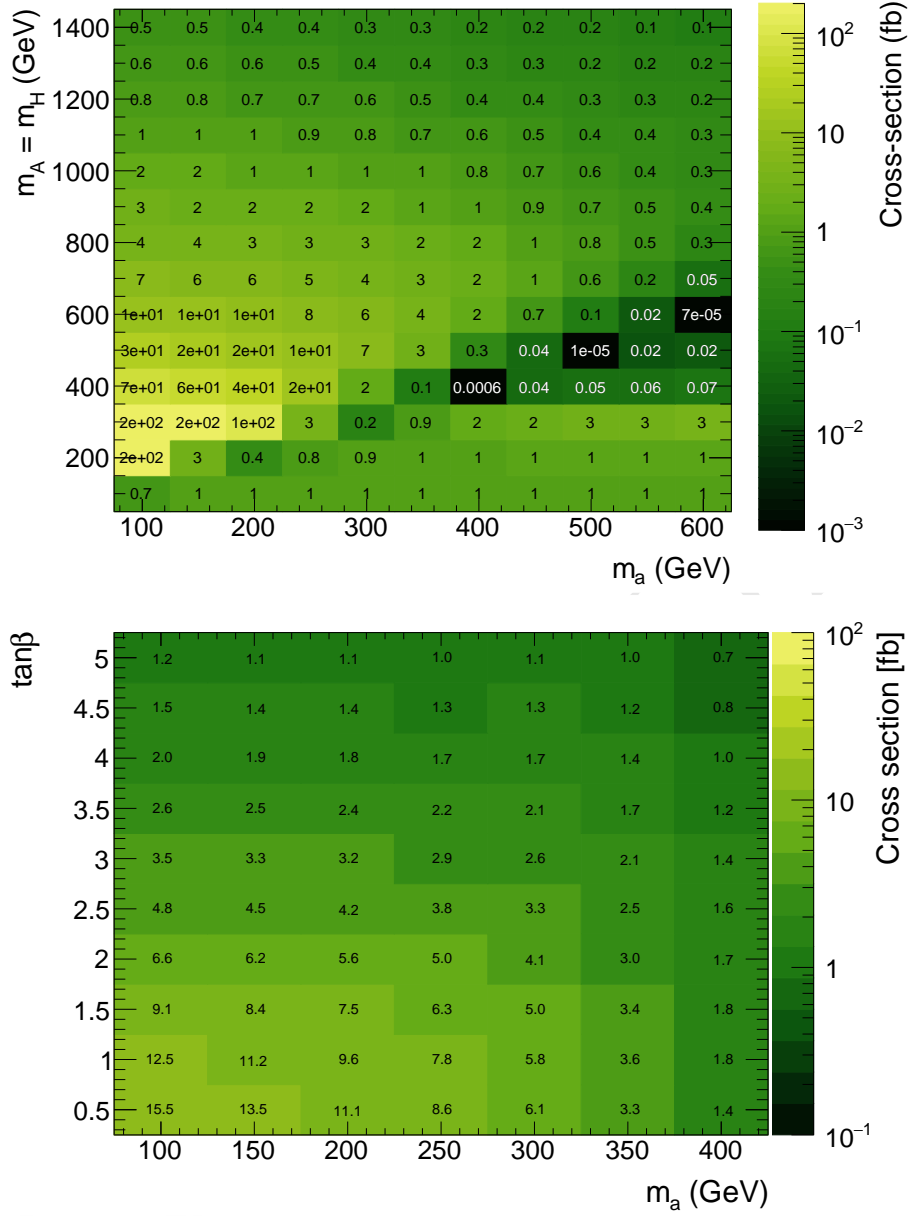
To assess the kinematic behavior of the signal, the distributions of the kinematic variables that are most relevant to the Mono-Z signature are studied as a function of the model parameters.

The distribution of the invariant masses of the dilepton and  $\chi\chi$  systems are shown in Fig. ?. Independent of the parameters, the dilepton mass spectrum is centered at the Z peak, without any nonresonant contribution. The  $M_{\chi\chi}$  distribution illustrates the signal contributions from different diagrams. For  $M_A > M_a$ , DM is dominantly produced from on-shell  $a$  boson production. In the inverted mass region  $M_A < M_a$ , the situation is reversed, and  $H$  diagrams dominate.

After applying the preselection requirements, the distributions of kinematic variables are shown in Fig. ?. In the region of  $M_A > M_a$ , distinct Jacobian peaks are visible in the distributions of the mediator  $p_T$ , the width of which generally increases with values of  $M_a$  and  $M_A$ . Significant portions of the spectrum are situated at relatively high boosts ( $E_T^{\text{miss}} > 200$  GeV), which is more easily accessible experimentally. This behavior is contrasted by the distributions in the inverted mass regions, which show nearly no distinct features and are mainly located at low mediator  $p_T$ . For  $M_A \approx M_a + m_Z$ , both the  $a$  and Z bosons are produced approximately at rest, leading to an event population with overall low boost. These qualitative trends are consistent between the observables studied here. Finally, the distributions of the  $E_T^{\text{miss}}$  and  $M_T$  variables after final selection are shown in Fig. ?. Traditionally, the Mono-Z search has relied on the  $E_T^{\text{miss}}$  distribution for signal extraction. While the presence of the Jacobian peak structure in the distribution facilitates signal-background separation, it may be beneficial to also consider the  $M_T$  distribution. Although only transverse information is available, the resonant structure of the signal is significantly enhanced in the  $M_T$  variable, which may enhance the sensitivity of a specialized search strategy.

The  $\tan\beta$  and  $\sin(\theta)$  variables have minimal effect on the distributions of kinematic variables (Fig. ?).

**Conclusions** The Mono-Z(l) provides experimental coverage of the pseudoscalar 2HDM model for a broad part of the parameter space. The light pseudoscalar can be probed up to mass values of  $\approx 350$  GeV, depending on the choice of other parameters. The Mono-Z is



**Figure 15:** Inclusive cross-sections for  $pp \rightarrow l^+l^-\chi\bar{\chi}$  in the  $M_a$ - $M_A$  (top) and  $M_a$ - $\tan \beta$  scans (bottom).

sensitive mostly in the region of low values of  $\tan \beta < 4$ .

**Expected significance** Expected significances for 2HDMa models are calculated using generator level signal samples and background estimates from recent  $Z(\ell\ell) + E_T^{\text{miss}}$  searches analyzing  $36.1 \text{ fb}^{-1}$  of data [? ].

Following the Asimov approximation, the expected significance for the ratio of likelihoods is given by equation ?? and is valid even for  $s$  not  $\ll b$  [? ]. This equation is modified to account for systematic uncertainties on the background (??) [? ], and the total

significance is taken as the per bin significances summed in quadrature.

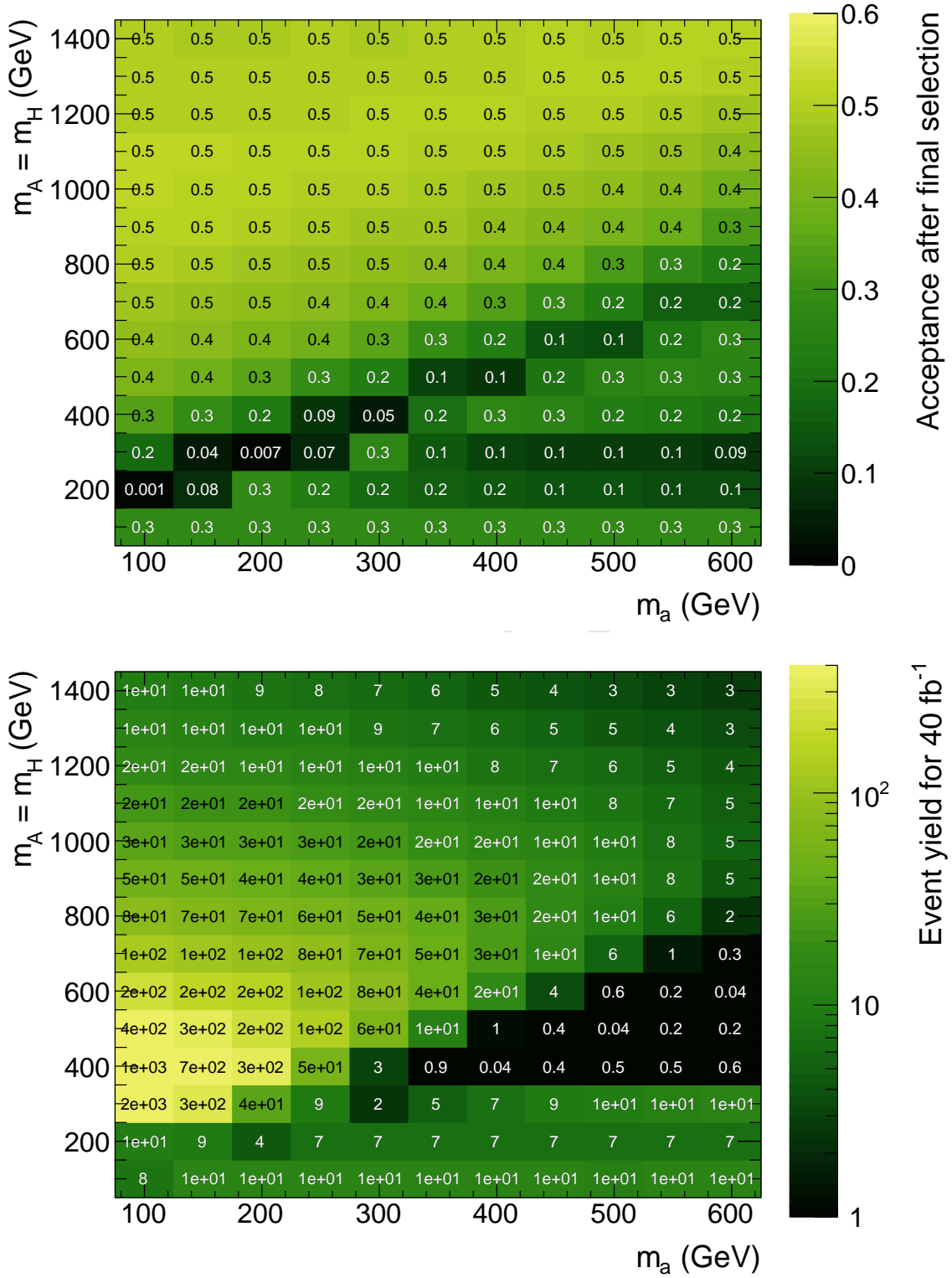
For the signal events a reconstruction efficiency of 75% is assumed. To be consistent with the background estimates, the ATLAS selection cuts are used. The significances are calculated for bins of  $E_T^{\text{miss}}$ . A conservative 20% systematic is assumed for  $E_T^{\text{miss}}$  and 10% for MET.

The expected significances are shown in Figure ??, the LHC should be sensitive to models with a significance greater than 2.

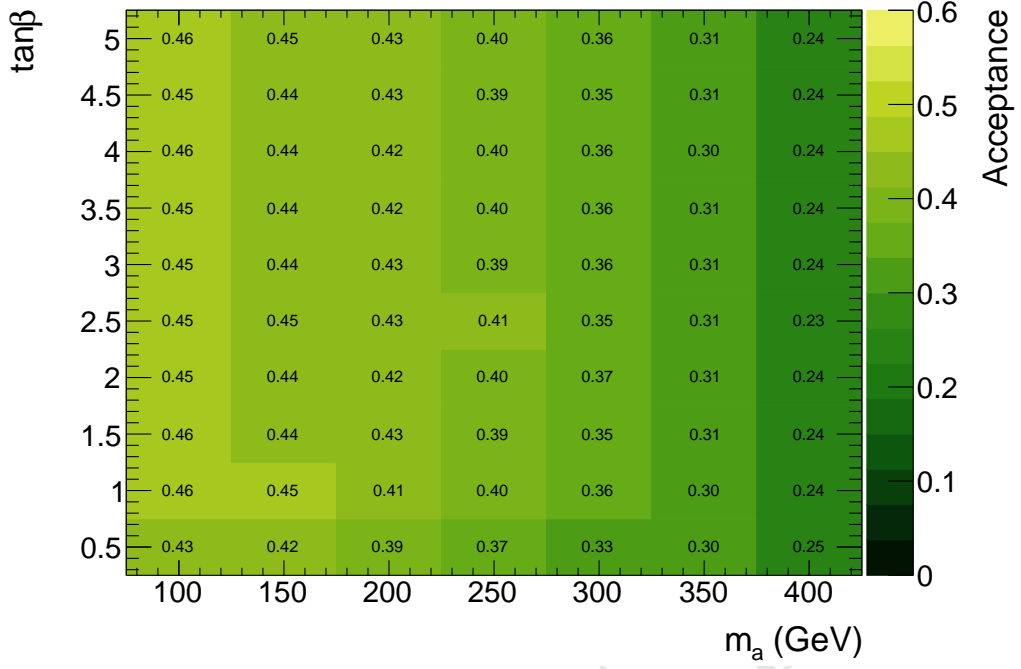
$$Z = \sqrt{2 \left( (s+b) \ln 1 + \frac{s}{b} - S \right)} \quad (4.3)$$

$$Z'_{bin} = \sqrt{2 \cdot \left( (s+b) \ln \left[ \frac{(s+b)(b+\sigma_b^2)}{b^2 + (s+b)\sigma_b^2} \right] - \frac{b^2}{\sigma_b^2} \ln \left[ 1 + \frac{\sigma_b^2 s}{b(b+\sigma_b^2)} \right] \right)} \quad (4.4)$$

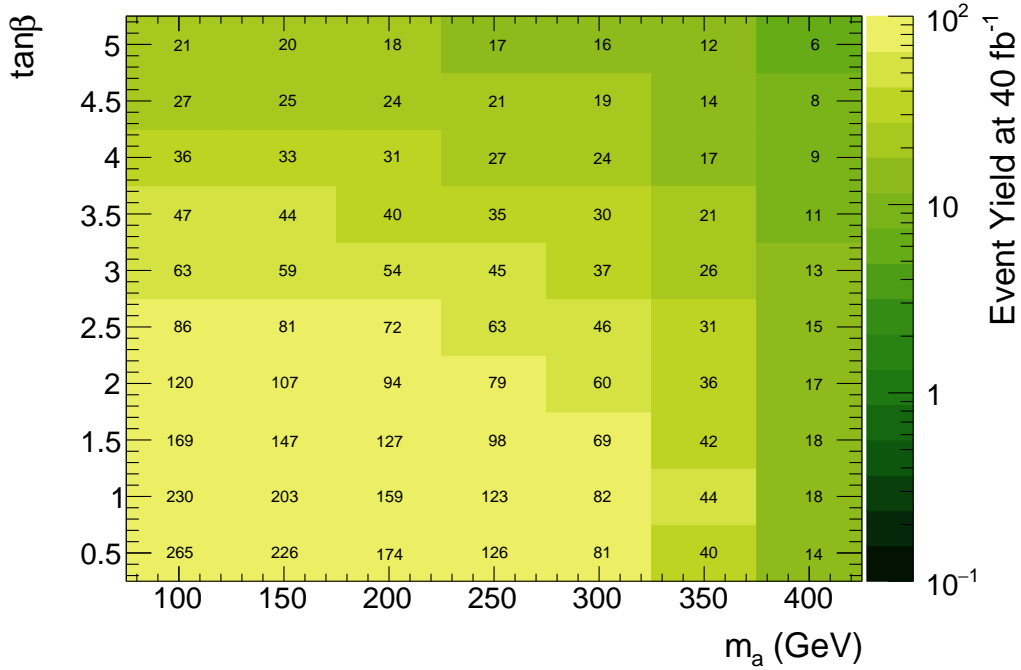
$$S = \sqrt{\sum_{bin} (Z'_{bin})^2} \quad (4.5)$$



**Figure 16:** Acceptance and event yields in the  $M_a$ - $M_A$  plane after applying the final selection. Event yields assume an integrated luminosity of 40 fb<sup>-1</sup>. The acceptance is maximal for  $M_A > M_a$ , where it reaches 50 %. In the inverted mass region  $M_A < M_a$ , lower values of 10-30% are observed. In the intermediate region around  $M_A \approx M_a + M_Z$ , the acceptance is strongly suppressed as the  $a$  and  $Z$  bosons are produced approximately at rest.

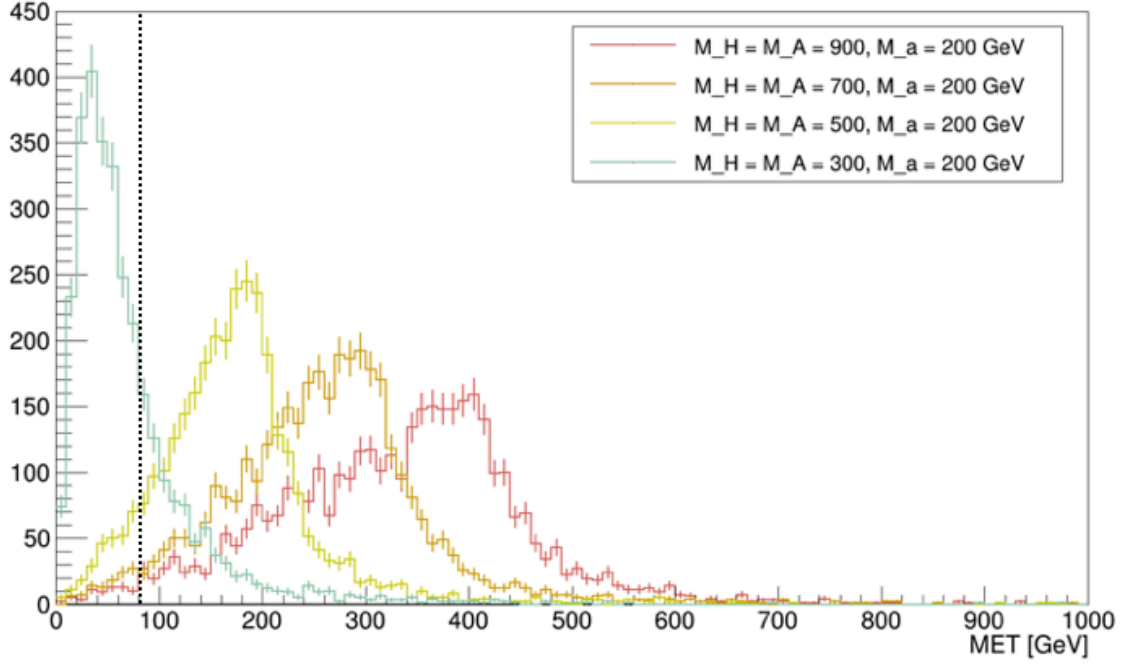


**Figure 17:** Acceptances across the  $M_a$ - $\tan\beta$  scan. Acceptance is flat over  $\tan\beta$  for constant values of  $M_a$ .

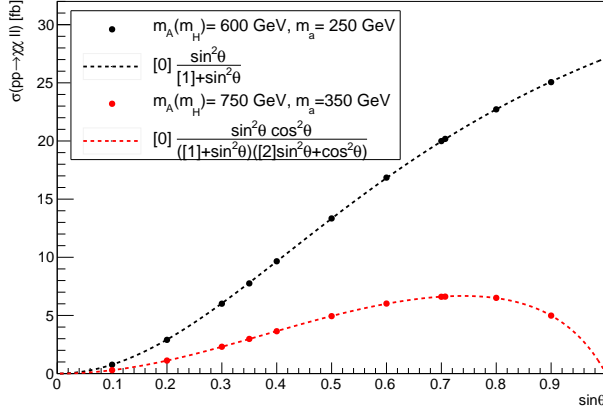


**Figure 18:** Event yield in the  $M_a$ - $\tan\beta$  grid, for an integrated luminosity of  $40 \text{ fb}^{-1}$ . The number of expected events diminishes with increasing  $\tan\beta$  and  $M_a$ .  $M_A$  fixed to 600 GeV and  $\sin\Theta$  to 0.35

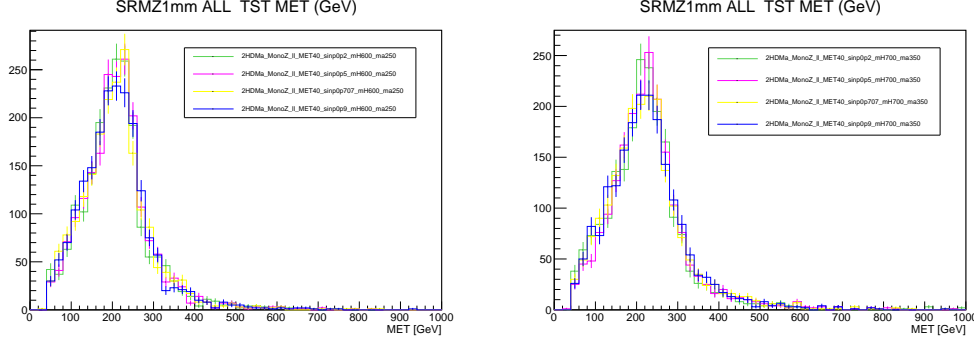




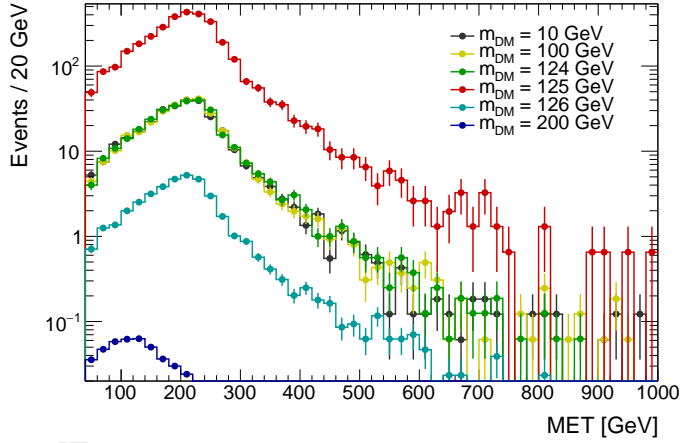
**Figure 19:** The position of the Jacobian peak in the  $E_T^{\text{miss}}$  distribution depends on the difference between  $M_H$  and  $M_a$ . For fixed values of  $M_a$  and  $M_A = M_H$ , increasing  $M_A$  shifts the peak towards higher energies, and decreasing  $M_A$  shifts it lower. For small mass splittings between  $M_H$  and  $M_a$ , most events will fail to pass the  $E_T^{\text{miss}}$  selection criteria.



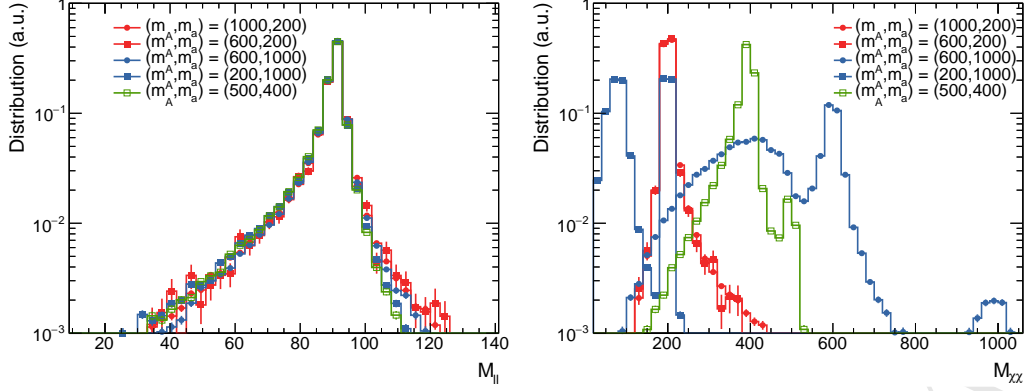
**Figure 20:** For two different mass points, this figure shows the cross section  $pp \rightarrow \chi\chi\ell\ell$  as a function of  $\sin\theta$ . For  $M_a < 350$  GeV,  $a$  decays solely to dark matter particles. As a consequence, the mixing angle only impacts the heavy scalar's branching fraction to  $aZ$  and cross section strictly increases with  $\sin\theta$ . For  $M_a$  above 350 GeV,  $\bar{t}t$  decays become accessible, introducing additional  $\sin\theta$  and  $\cos\theta$  dependences for the branching fraction of  $a \rightarrow \chi\chi$ . Above 350 GeV for large values of  $\sin\theta$ , there is a turnover point where the reduced  $a \rightarrow \chi\chi$  branching fraction outweighs the increased  $H \rightarrow aZ$  branching and the net cross section decreases.



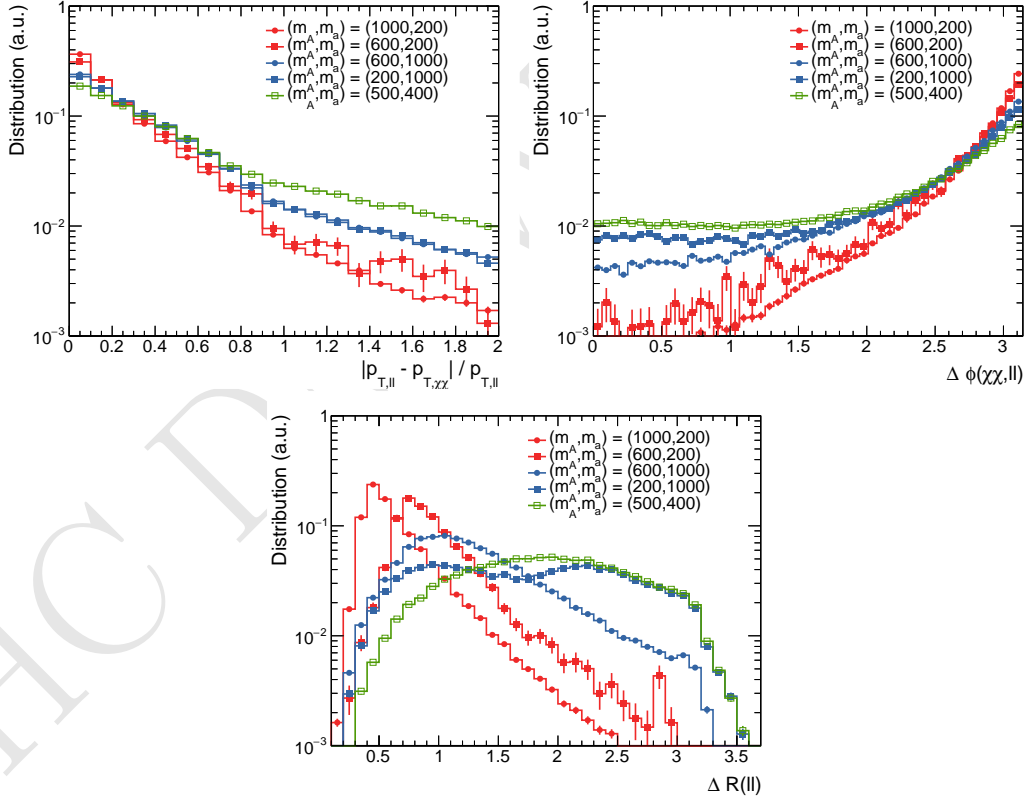
**Figure 21:** Performing one dimensional scans of  $\sin\Theta$  shows that it has little impact on the events' kinematic distributions. The first scan is performed at  $M_A = 600$  GeV and  $M_a = 250$  GeV, the second at  $M_A = 700$  GeV  $M_a = 350$  GeV. In both cases  $\tan\beta = 1.0$ .



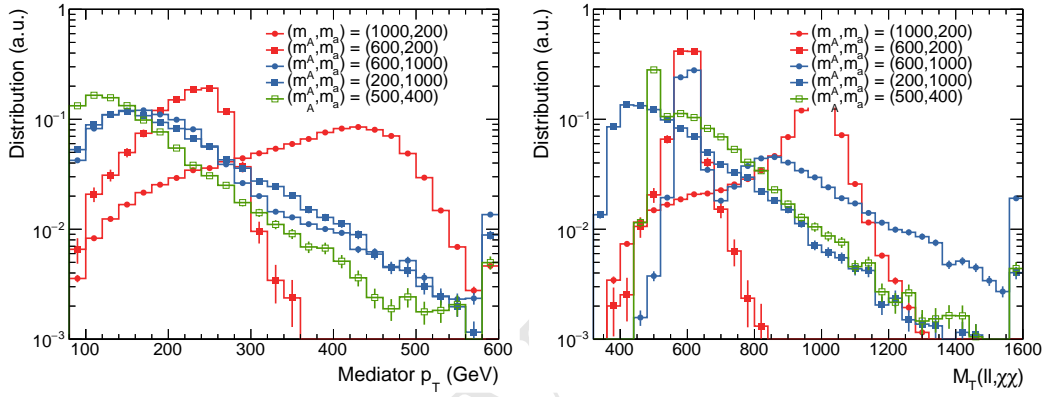
**Figure 22:** In the DM mass scan, for  $M_\chi < \frac{M_H}{2}$ , the DM mass has no effect on cross section or kinematic distributions, at  $M_\chi = \frac{M_H}{2}$  a resonant enhancement to the cross section occurs, and in the off-shell region where  $M_\chi > \frac{M_H}{2}$  cross section steeply drops and the  $E_T^{\text{miss}}$  distribution becomes more disperse.



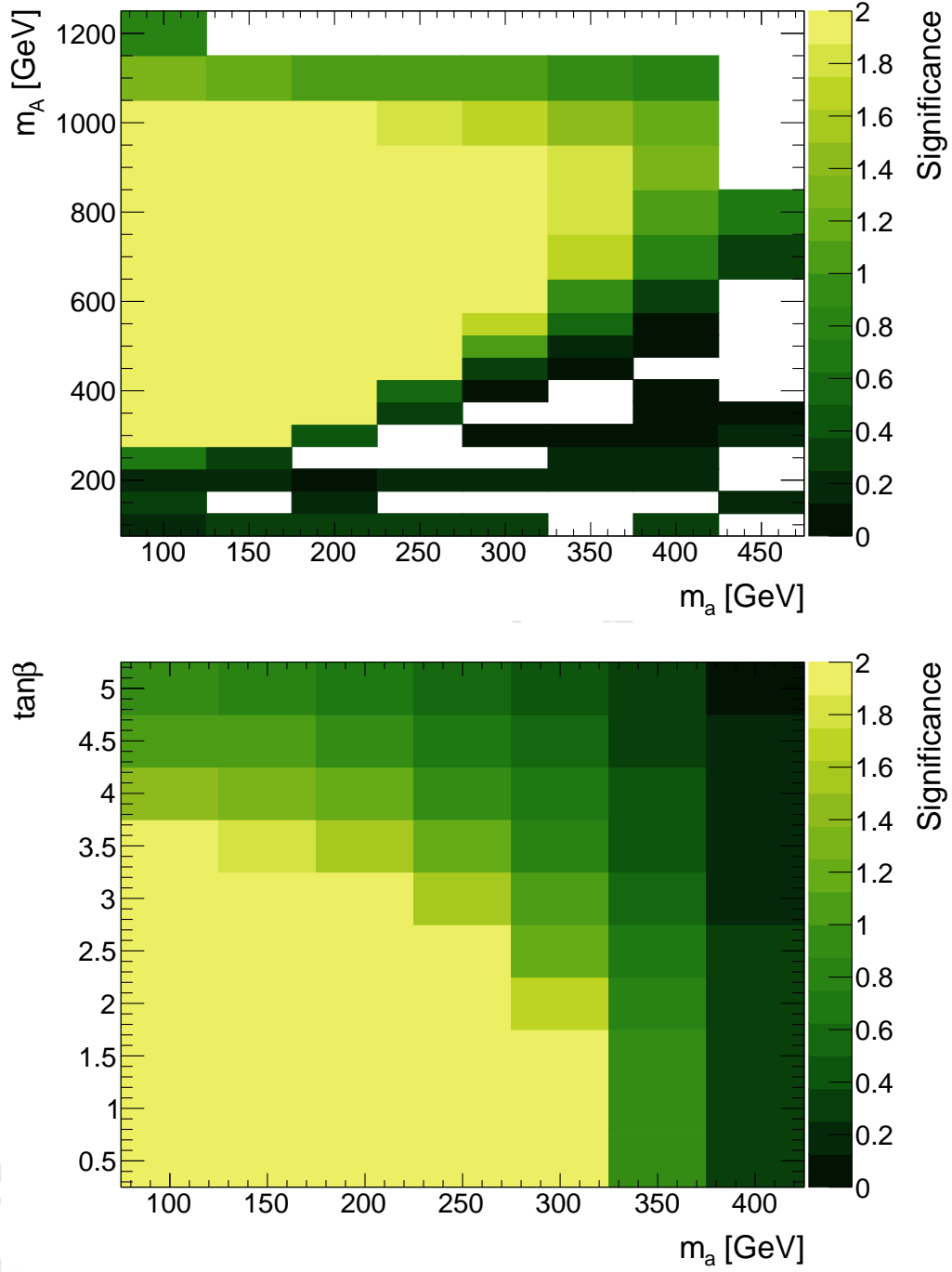
**Figure 23:** Distributions of the invariant mass of the dilepton (left) and  $\chi\bar{\chi}$  systems (right) with no selection applied in addition to the generation cuts. The  $M_{ll}$  distribution is centered around the Z boson mass independent of the chosen parameter point, indicating that there is no contribution from  $\gamma^*$  exchange. The  $M_{\chi\bar{\chi}}$  distribution



**Figure 24:** Distributions of the main selection variables after preselection:  $p_T$  balance (top panel),  $\Delta\Phi$  (middle) and  $\Delta R$  (bottom). The shown parameter points illustrate the different qualitative behavior in the three different mass regions.



**Figure 25:**  $E_T^{\text{miss}}$  and MT distributions in the signal region. The  $E_T^{\text{miss}}$  distribution shows a Jacobian structure in the  $M_A > M_a$  regime, the location of which strongly depends on  $M_A$ . In the region of inverted mass hierarchy  $M_A < M_a$ , the spectrum is less structured and does not fall off as steeply towards higher values. For a small mass splitting of  $M_a - M_A \approx M_Z$ , the spectrum is shifted to much lower values of  $E_T^{\text{miss}}$ . The MT distribution allows to access the resonant nature of the process. Clear mass peaks are present for the normal mass hierarchy. In the inverted region, the MT distribution is more sensitive to the mass difference  $M_a - M_A$  than the  $E_T^{\text{miss}}$  distribution, allowing to differentiate between signal hypotheses that give near-identical  $E_T^{\text{miss}}$  distributions.



**Figure 26:** Expected significances are calculated using published background estimates and assuming a reconstruction efficiency of 75%. The LHC is expected to be sensitive to regions with significances greater than 2.

#### 4.1.4 Studies of DM+heavy flavor signature

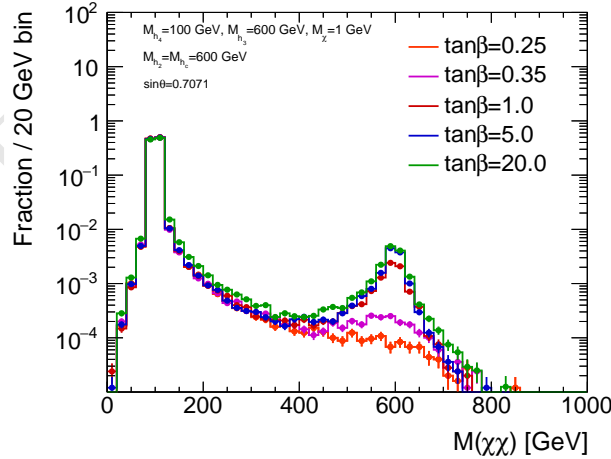
Heavy flavour final state have sizeable contributions to the production of the CP-even and CP-odd scalar mass eigenstates, due to the Yukawa structure of the couplings in the matter sector. In the following sections, the most important signatures involving either visible or invisible decays of the heavy Higgses are reviewed.

#### 4.1.5 Scanning the parameter space

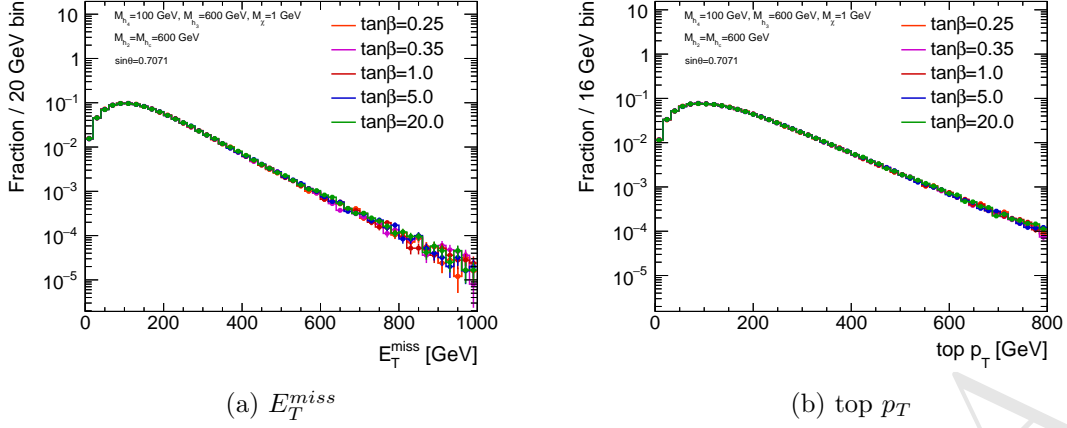
**Scan of  $\tan \beta$  and  $\sin \theta$ :** In the limit of small  $\tan \beta$  values, the couplings of  $h_3$  (A) and  $h_4$  (a) to down-type quarks are heavily suppressed irrespectively of the Yukawa assignment. At LO,  $t\bar{t} + \chi\bar{\chi}$  associated production is mediated through either CP-odd weak eigenstate, A or a, though it is shown in Fig. ?? that  $a \rightarrow \chi\bar{\chi}$  is the dominant production mode. Although the relative mediator contribution is dependent on  $\tan \beta$ , observables such as  $E_T^{miss}$  and top quark  $p_T$  do not have a kinematic dependence on  $\tan \beta$  as demonstrated in Fig. ??.

Mixing of the CP-odd weak eigenstates is achieved through the mixing angle,  $\theta$ . As shown in Fig. ??, the A and a mass peaks are quite narrow for values where  $\sin \theta$  approaches 1, and  $a \rightarrow \chi\bar{\chi}$  is the dominant  $\chi\bar{\chi}$  production mode. However, no kinematic dependence on  $\sin \theta$  is observed in the  $E_T^{miss}$  and top quark  $p_T$  as shown in Fig. ??.

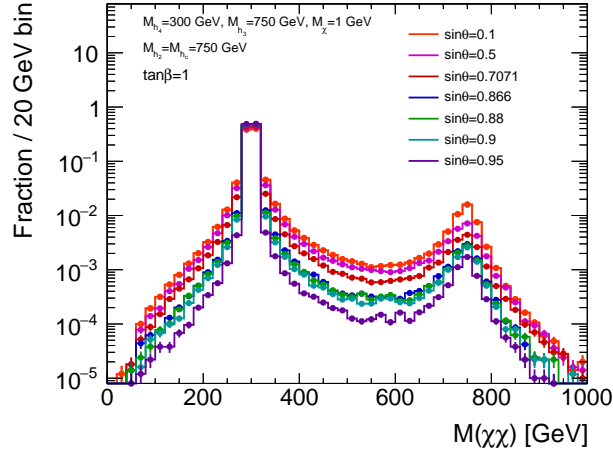
**Scan of  $M_a$  and  $M_A$ :** While the relevant kinematic distributions display no dependence on the aforementioned mixing angles, the same does not hold true for the masses,  $M_a$  and  $M_A$ . As shown in Fig. ??, the  $E_T^{miss}$ , and leading and trailing top quark  $p_T$  distributions broaden with increasing  $M_a$ . Similarly, for values of  $M_A < M_a$ , as  $M_A$  increases, the kinematic distributions mentioned above also broaden, as shown in Fig. ??.



**Figure 27:** The mass distribution of the  $\chi\bar{\chi}$  system for various values of  $\tan \beta$ , with  $M_a = 100$  GeV,  $M_A = 600$  GeV,  $M_H = M_{H^\pm} = 600$  GeV, and  $\sin \theta = 0.7071$ .



**Figure 28:** The  $E_T^{miss}$  and top  $p_T$  distribution for inclusive  $t\bar{t} + \chi\bar{\chi}$  production for various values of  $\tan\beta$ , with  $M_a = 100$  GeV,  $M_A = 600$  GeV,  $M_H = M_{H^\pm} = 600$  GeV, and  $\sin\theta = 0.7071$ .

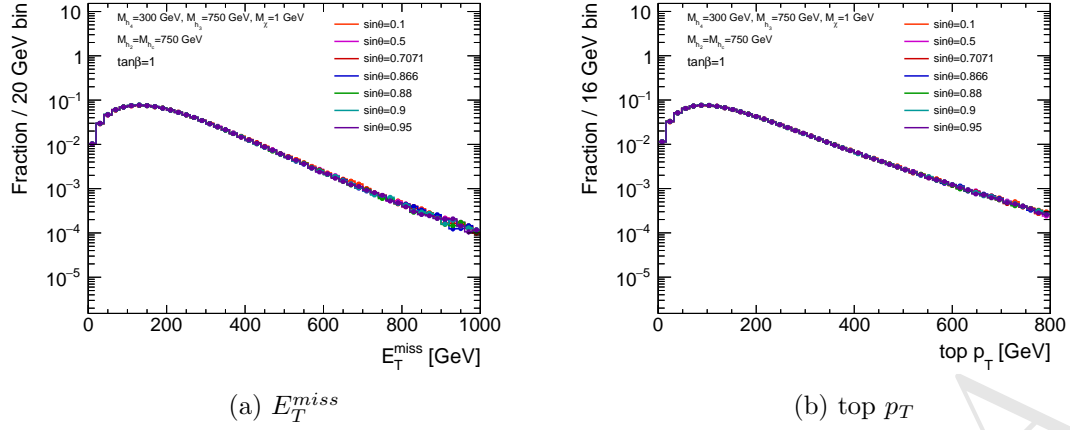


**Figure 29:** The mass distribution of the  $\chi\bar{\chi}$  system for various values of  $\sin\theta$ , with  $M_a = 300$  GeV,  $M_A = 750$  GeV,  $M_H = M_{H^\pm} = 750$  GeV, and  $\tan\beta = 1$ .

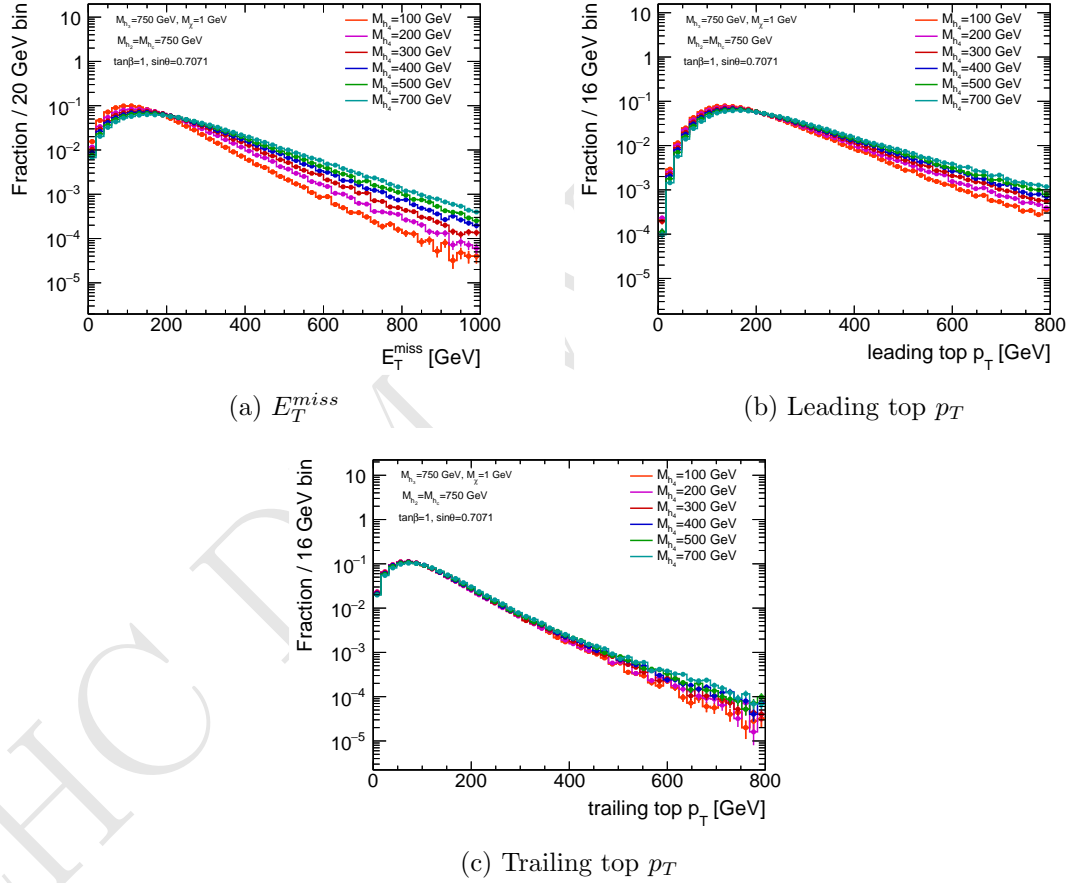
#### 4.1.6 Comparison with DMSimp Pseudoscalar Model

To date, simplified models of DM (DMSimp) are used to interpret Run II CMS and ATLAS HF+DM searches. A comparison of the pertinent kinematic distributions between the pseudoscalar simplified model and the 2HDM+a model for the same value of  $M_a$  are shown in Fig. ???. The kinematics of the pseudoscalar DMSimp model with  $M_a = 100$  GeV map directly onto those of the 2HDM+a model with  $M_a = 100$  GeV,  $M_A = 600$  GeV,  $M_H = M_{H^\pm} = 600$  GeV,  $\sin\theta = 0.7071$ , and  $\tan\beta = 1$ . From the mass distribution of the  $\chi\bar{\chi}$  shown in Fig. ??, it is evident that the 2HDM+a model contains contributions from both the light and heavy pseudoscalar mediator as in the DMSimp model.

In Fig. ??, relevant kinematic distributions, commonly employed in HF+DM searches,

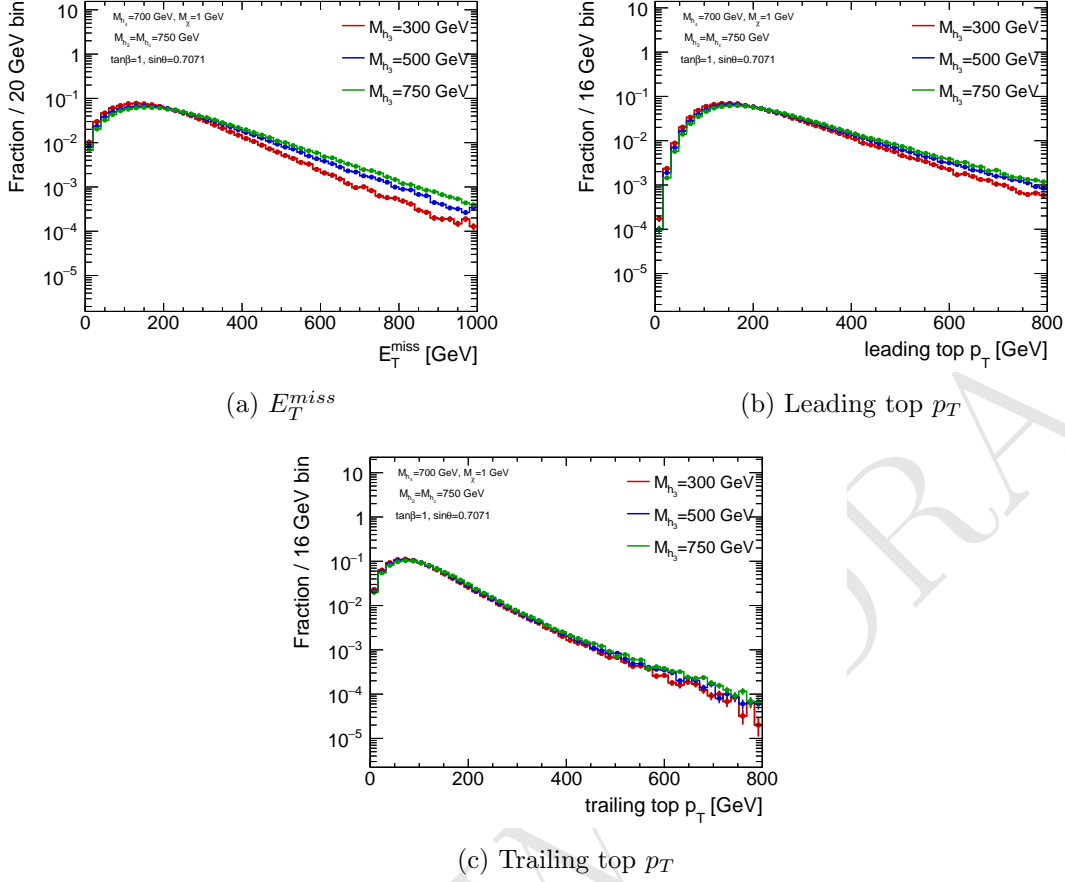


**Figure 30:** The  $E_T^{miss}$  and top  $p_T$  distribution for inclusive  $t\bar{t} + \chi\bar{\chi}$  production for various values of  $\sin \theta$ , with  $M_a = 300$  GeV,  $M_A = 750$  GeV,  $M_H = M_{H^\pm} = 750$  GeV, and  $\tan \beta = 1$ .



**Figure 31:** The  $E_T^{miss}$ , leading and trailing top  $p_T$  distributions for inclusive  $t\bar{t} + \chi\bar{\chi}$  production for various values of  $M_a$ , with  $M_A = 750$  GeV,  $M_H = M_{H^\pm} = 750$  GeV,  $\tan \beta = 1$ , and  $\sin \theta = 0.7071$ .





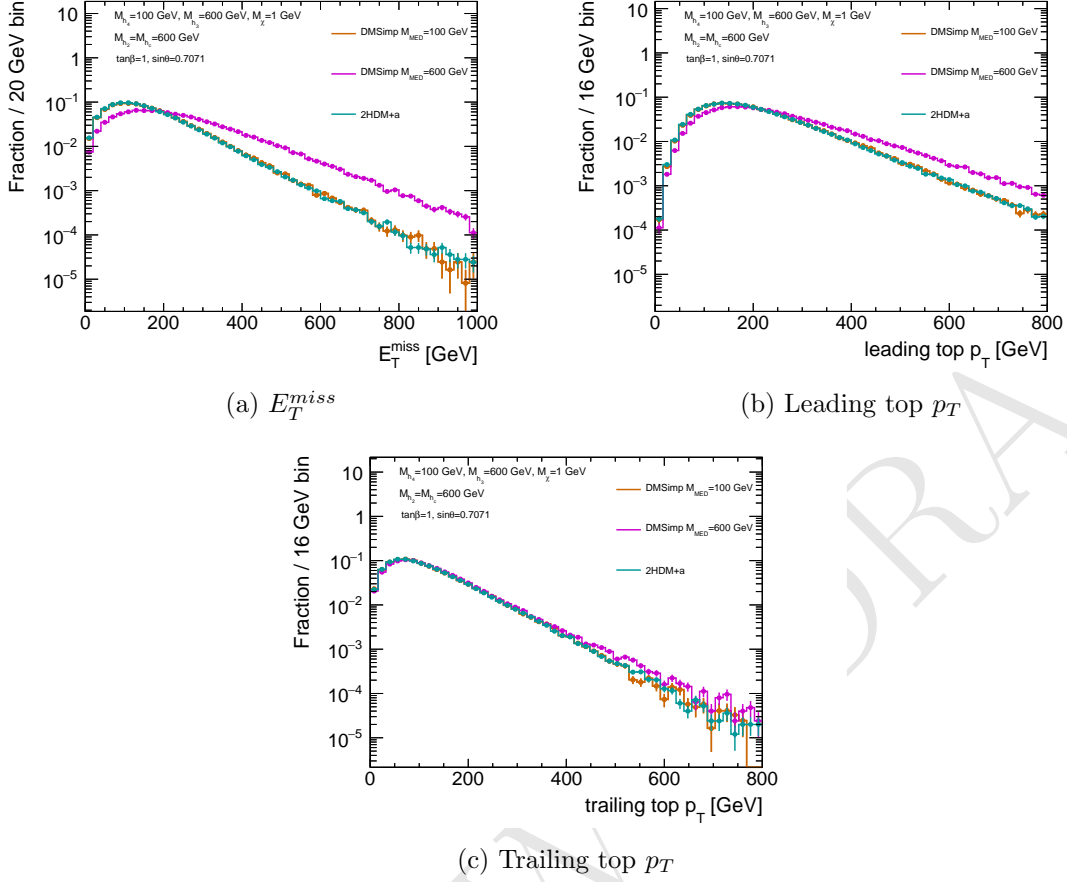
**Figure 32:** The  $E_T^{miss}$ , leading and trailing top  $p_T$  distributions for inclusive  $t\bar{t} + \chi\bar{\chi}$  production for various values of  $M_A$ , with  $M_a = 700$  GeV,  $M_H = M_{H^\pm} = 750$  GeV,  $\tan\beta = 1$ , and  $\sin\theta = 0.7071$ .

are mapped from the **DMsimp** pseudoscalar models to the 2HDM+a model, with the mediator masses corresponding to the additional light pseudoscalar in the latter model. The dashed distributions represent the **DMsimp** model, while the solid are the 2HDM+a model distributions. The  $t\bar{t} + \chi\bar{\chi}$  process was generated at LO precision using both models. As can be seen, the kinematics do not change appreciably between the models generated at the same value of  $M_a$ . A discussion on cross-section rescaling procedures can be found in the following section.

#### 4.1.7 Recasting existing $t\bar{t} + E_T^{miss}$ and $b\bar{b} + E_T^{miss}$ signatures

These two signatures are dominantly produced in diagrams involving the invisible decays of the two CP-odd scalars. Their relevance is therefore determined by the two pseudoscalar masses,  $m(A)$  and  $m(a)$  and it is a function of  $\sin\theta$  and  $\tan\beta$ . For both  $b\bar{b}$  and  $t\bar{t}$  associated productions, we find that the highest sensitivity of this signatures is obtained for high values of  $\sin\theta$ .

The 2HDM+a model is equivalent to a single pseudoscalar simplified model (DMF)

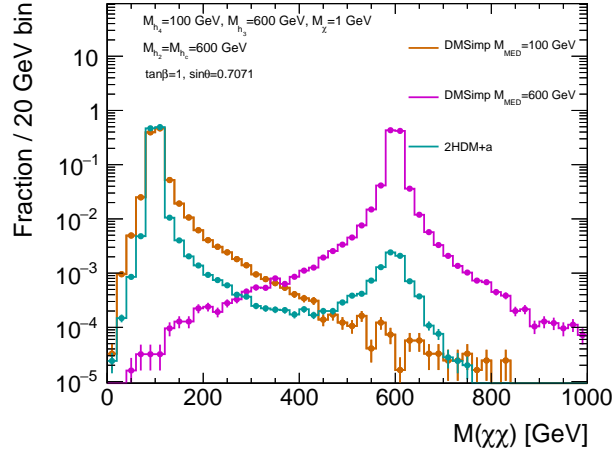


**Figure 33:** The  $E_T^{miss}$ , leading and trailing top  $p_T$  distributions for inclusive  $t\bar{t} + \chi\bar{\chi}$  production for various values of  $M_A$ , with  $M_a = 700$  GeV,  $M_H = M_{H^\pm} = 750$  GeV,  $\tan\beta = 1$ , and  $\sin\theta = 0.7071$ .

when  $A$  is much heavier than  $a$ , and therefore the former does not contribute to the considered final state. However, when the two mediators are closer in mass, the  $pp \rightarrow t\bar{t}A$  contribution becomes more relevant as it is possible to observe in Figure ??, where the two models are compared assuming  $m(A) = 750$  GeV and two different values for  $m(a)$ . An excellent agreement was observed between *DMSIMP* and *2HDMp* on parton-level variables sensitive to the helicity structure of the interaction between top and the mediator[?], if the invariant mass of the two DM particles in the 2HDM is required to be smaller than 200(300) GeV for  $m(a) = 150(300)$  GeV respectively, giving confidence that, once the contribution from  $A$  production is separated, it is possible to fully map the *2HDM* +  $a$  kinematics into the DMF simplified model.

This remapping is achieved by taking for each set of the parameters the average of the selection acceptances for  $m(A)$  and  $M(A)$  as calculated with *DMSIMP* weighted by the respective cross-section for  $A$  ( $\sigma_A$ ) and  $a$  ( $\sigma_a$ ) production, in formulas

$$Acc_{2HDM}(m(A), M(a)) = \frac{\sigma_a \times Acc_{DMSIMP}(m(a)) + \sigma_A \times Acc_{DMSIMP}(m(A))}{\sigma_a + \sigma_A} \quad (4.6)$$



**Figure 34:** The mass distribution of the  $\chi\bar{\chi}$  system for DMSimp pseudoscalar models with  $M_a = 100$  GeV and  $M_a = 600$  GeV, compared with 2HDM+a with  $M_a = 100$  GeV,  $M_A = 600$  GeV,  $M_H = M_{H^\pm} = 600$  GeV,  $\sin\theta = 0.7071$  and  $\tan\beta = 1$ .

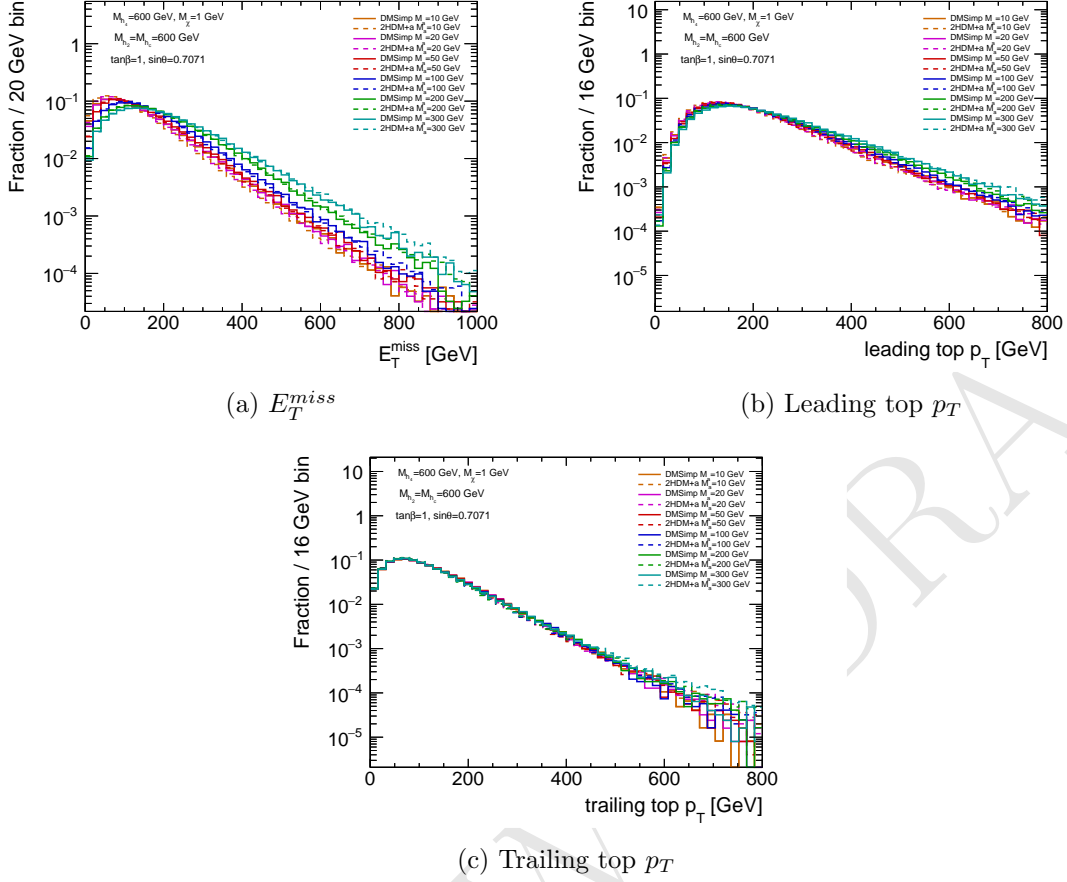
The acceptance in this case is a parton level implementation of the two-lepton analysis described in [arXiv:1710.11412]. The acceptance estimated in this way is shown as red triangles in Figure ??, and an excellent agreement can be seen with the acceptances evaluated directly on the 2HDM samples. The acceptance estimated in this way is shown as red triangles in Figure ??, and an excellent agreement can be seen with the acceptances evaluated directly on the 2HDM samples. Further validation were performed also on the acceptances calculated for zero and one lepton final states [1710.11412,1711.11520], both as a function of  $\sin\theta$  and  $\tan\beta$  and can be observed in Fig ??. Finally, the formula was successfully tested also the situation in which  $|m(A) - m(a)| \sim 50$  GeV, implying the possibility of a large interference between the production of the two bosons.

#### 4.1.8 Flavour scheme recommendations and studies

The relevant kinematic distributions for  $t\bar{t} + \chi\bar{\chi}$  associated production in the context of this model are shown to be independent from the choice of PDF flavour scheme. In Figures ??–??, the  $E_T^{\text{miss}}$ , which is taken to be the  $p_T$  of the  $\chi\bar{\chi}$  system, and the  $p_T$  distribution of the top quarks is presented using the 4 and 5-flavour scheme. The 4-flavour LHAPDF ID is 263400 and corresponds to NNPDF30\_lo\_as\_0130\_nf\_4, and the 5-flavour LHAPDF ID is 263000 and corresponds to NNPDF30\_lo\_as\_0130. As demonstrated for various configurations of the 2HDM+a model parameters, the kinematics are not affected by the flavour scheme choice of PDF. Furthermore, the difference in cross-section between the 4-flavour and 5-flavour generated LO  $t\bar{t} + \chi\bar{\chi}$  process is at the 2 – 3% level, as noted in Tab. ??.

Despite the lack of kinematic dependence on flavour scheme, it is recommended to use the 5-flavour PDF. [Add support/discussion and references](#)

**Motivations for an high  $\tan\beta$  scan for  $bb + E_T^{\text{miss}}$**  The projection of sensitivity in  $\tan\beta$  for benchmark #2, based on the CMS results for  $bb + \text{MET}$  [arXiv:1706.02581] are



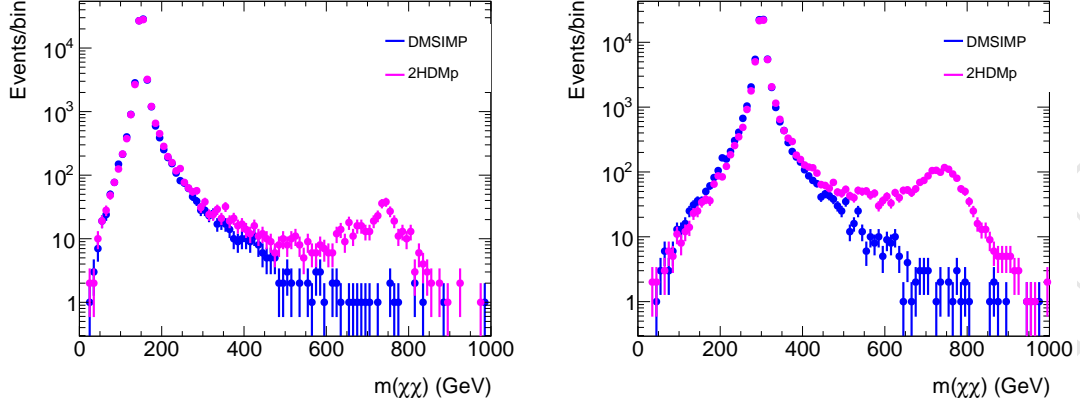
**Figure 35:** The  $E_T^{miss}$ , leading and trailing top  $p_T$  distributions for inclusive  $t\bar{t} + \chi\bar{\chi}$  production generated from the **DMSimp** (solid) and the **2HDM+a** (dashed) models with various values of  $M_a$ . The **2HDM+a** models are generated with the following model parameters:  $M_A = 600$  GeV,  $M_H = M_{H^\pm} = 600$  GeV,  $\tan\beta = 1$ , and  $\sin\theta = 0.7071$ .

$M_{h_2}, M_{h_c}$ [GeV]	$M_{h_3}$ [GeV]	$M_{h_4}$ [GeV]	$\sin\theta$	$\tan\beta$	4F $\sigma$ (pb)	5F $\sigma$ (pb)
750	500	100	0.7071	1	0.0988596	0.0964933
750	750	200	0.7071	1	0.0445115	0.043149
750	300	200	0.25	1	0.0310152	0.0300196

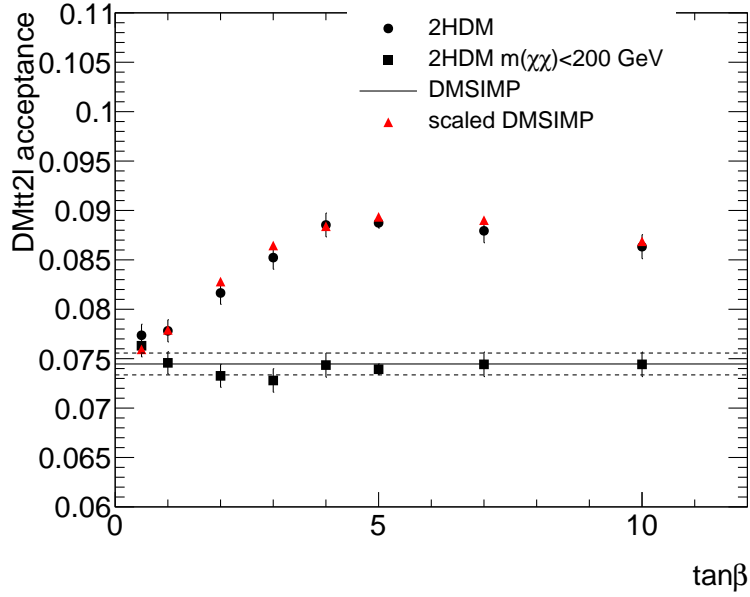
**Table 2:** Configurations of the **2HDM+a** model used to generate the  $t\bar{t} + \chi\bar{\chi}$  process at LO and the corresponding cross-sections from the 4-flavour (4F) and 5-flavour (5F) PDF.

shown in Figure ???. The reach for an upper bound on  $\tan(\beta)$  with  $bb + \text{MET}$  shows good potential, for  $\tan\beta$  values above 10.

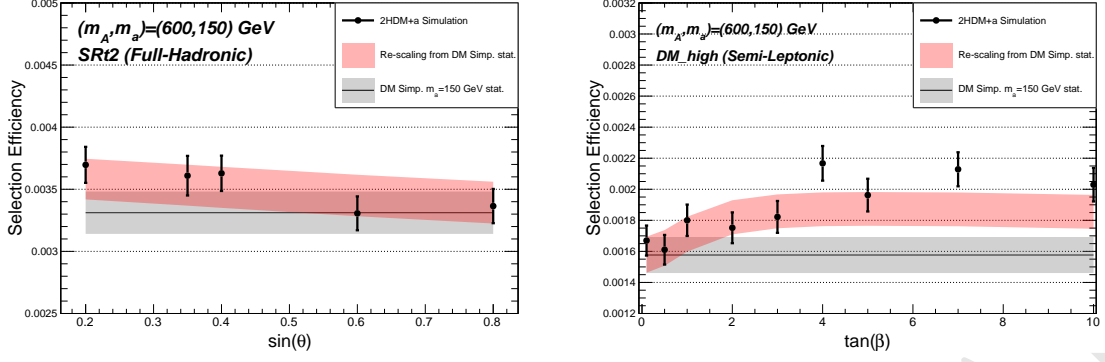
**Say something about high width for H?**



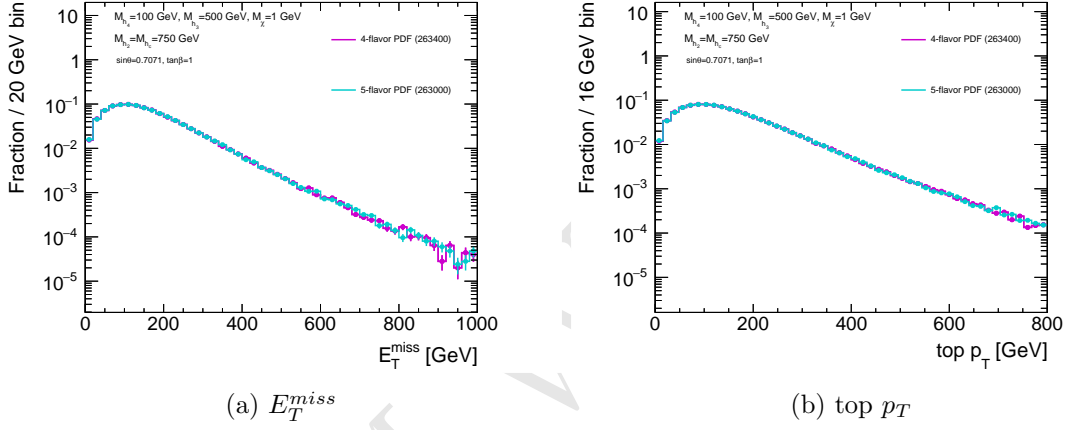
**Figure 36:** Comparison of  $m(\chi\chi)$ , the invariant mass of the two DM particles for the *DMSIMP* (blue) and the *2HDMp* model (magenta). The plot on the left (right) shows the comparison for  $m(a) = 150(300)$  GeV respectively.



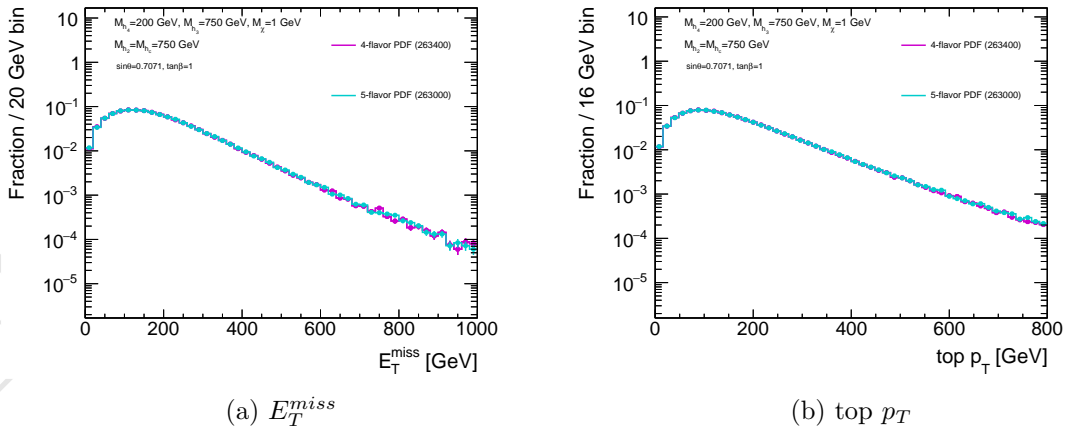
**Figure 37:** Acceptance of the two-lepton analysis as a function of  $\tan\beta$  for the *2HDMp* model (round markers), for the *2HDMp* model considering only events with  $m(\chi\chi) < 200$  GeV (square markers), and for the *DMSIMP* model (full line) for a mediator mass of 150 GeV. The two dashed lines indicate the statistical error of the *DMSIMP*. The value of  $m(A)$  is fixed at 600 GeV, and  $\sin\theta = 0.35$ . The acceptance calculated from the *DMSIMP* acceptance rescaled following the prescription ?? (red triangles) is also shown.



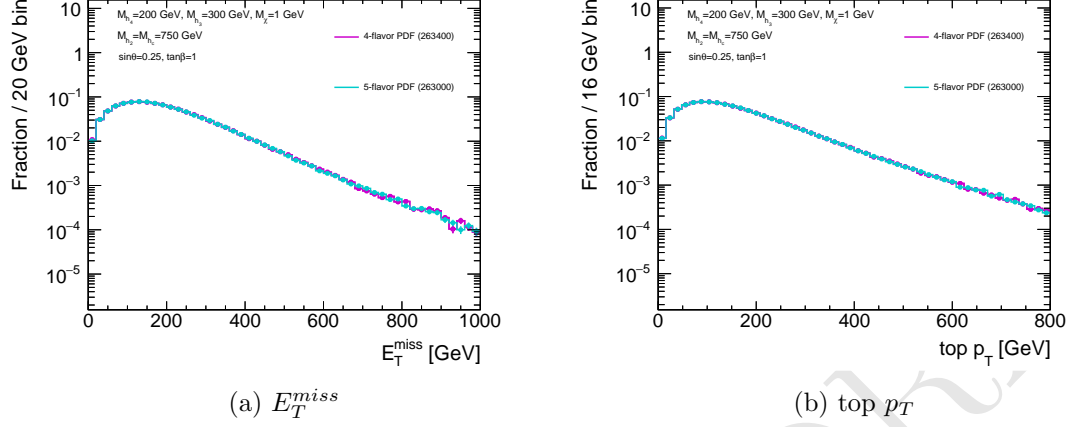
**Figure 38:** Validation of the re-scaling formula on zero and one lepton final states as a function of  $\tan\beta$  and  $\sin\theta$  parameters



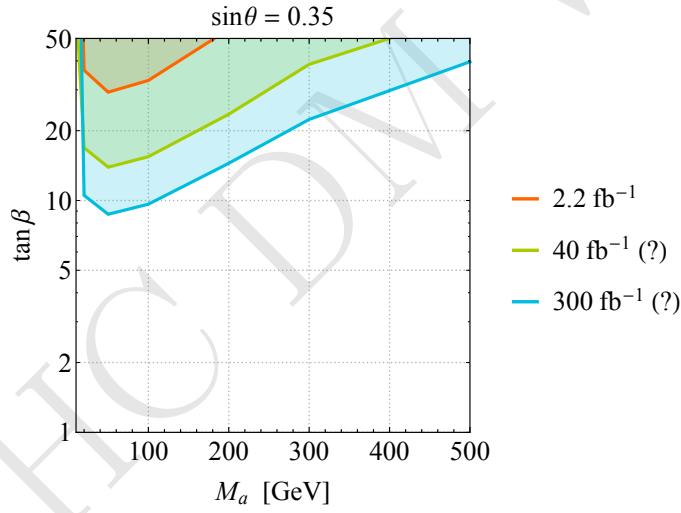
**Figure 39:**  $E_T^{miss}$  and top  $p_T$  distributions for  $M_{h_4} = 100$  GeV,  $M_{h_3} = 500$  GeV,  $M_{DM} = 1$  GeV,  $\sin\theta = 0.7071$ , and  $\tan\beta = 1$ .



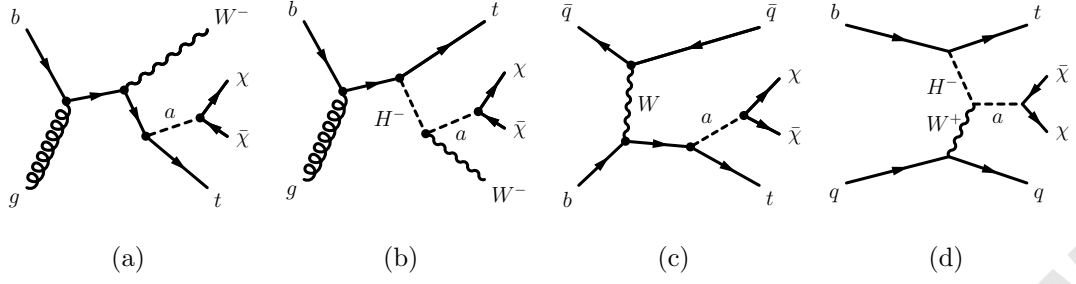
**Figure 40:**  $E_T^{miss}$  and top  $p_T$  distributions for  $M_{h_4} = 200$  GeV,  $M_{h_3} = 750$  GeV,  $M_{DM} = 1$  GeV,  $\sin\theta = 0.7071$ , and  $\tan\beta = 1$ .



**Figure 41:**  $E_T^{miss}$  and top  $p_T$  distributions for  $M_{h_4} = 200$  GeV,  $M_{h_3} = 300$  GeV,  $M_{D^*} = 1$  GeV,  $\sin\theta = 0.25$ , and  $\tan\beta = 1$ .



**Figure 42:** Sensitivity projection for benchmark #2 based on the CMS results for  $bb+MET$  [arXiv:1706.02581].



**Figure 43:** Representative diagrams for  $tW$  and  $t$ -channel production of DM in association with a single top quark.

#### 4.1.9 Motivation for a dedicated $tW + E_T^{\text{miss}}$ search

The sensitivity of the LHC experiments to the associated production of dark matter with a single top has been recently studied [?] in the framework of an extension of the standard model featuring two Higgs doublets and an additional pseudoscalar mediator. This study extends the work of previous literature [?], which demonstrated using a simplified model that the consideration of final states involving a single top quark and DM ( $DMt$ ) increases the coverage of existing analyses targeting the  $DMt\bar{t}$  process.

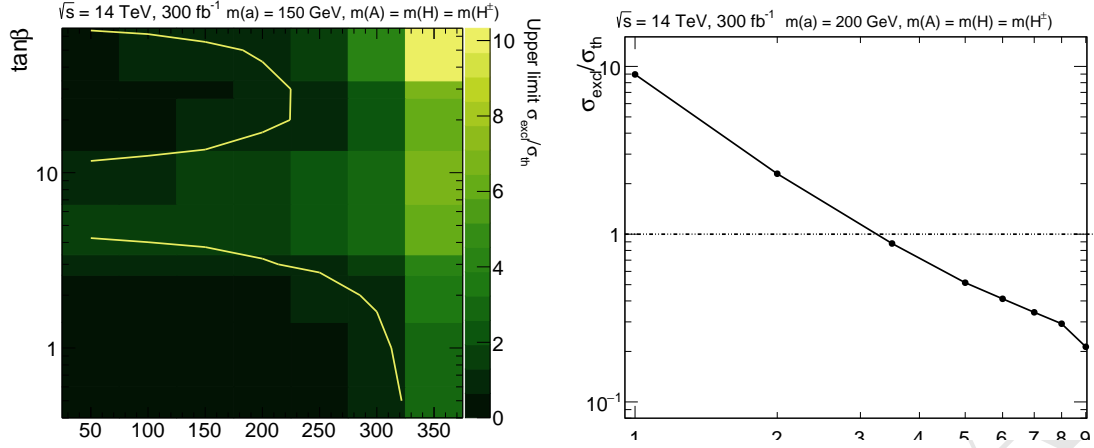
Like single top production within the SM, the  $DMt$  signature in the model receives three different types of contributions at leading order (LO) in QCD. These are  $t$ -channel production,  $s$ -channel production and associated production together with a  $W$  boson ( $tW$ ) (Fig. ??). When the decay  $H^\pm \rightarrow W^\pm a$  is possible, the  $H^\pm$  is produced on-shell, and the cross-section of  $pp \rightarrow tW\chi\chi$ , assuming  $H^\pm$  masses of a few hundred GeV, is around one order of magnitude larger than the one for the same process in the simplified model. Moreover the production and cascade decay of a resonance yields kinematic signatures which can be exploited to separate the signal from the SM background.

Dedicated selections considering one and two lepton final states are developed to assess the coverage in parameter space for this signature at a centre-of-mass energy of 14 TeV assuming an integrated luminosity of  $300 \text{ fb}^{-1}$  in Ref. [?]. Background and signal Monte Carlo simulated samples are employed for the estimate of the results. The effect of the detector on the kinematic quantities utilised in the analysis is simulated by applying a Gaussian smearing to the momenta of the different reconstructed objects and reconstruction and tagging efficiency factors. Figure ?? shows the sensitivity reach for two of the parameter scans proposed in this whitepaper. On the top panel the exclusion reach for the  $m(a), \tan\beta$  plane is presented, assuming  $\sin\theta = 0.35$  and  $m(A) = m(H^\pm) = m(H) = 500 \text{ GeV}$ . It is possible to observe that for this scenario the sensitivity reach is comparable to the one from the mono-h signature as presented in Ref. [?]. On the bottom panel of Figure ?? the signature's sensitivity to benchmark #4 is evaluated for the first time.

#### 4.1.10 Uncovered signatures with $tth + E_T^{\text{miss}}$

As discussed in Section ??, the production of the heavy mediator  $A$  gives a sizeable contribution to the  $t\bar{t} + E_T^{\text{miss}}$  production cross section in the  $2HDM + a$  model. This is also





**Figure 44:** Exclusion reach for benchmark #2 (top) and benchmark #4 (bottom), assuming  $\sin\theta = 0.35$  and  $m(A) = m(H^\pm) = m(H) = 500$  GeV.

true for the heavy  $H$ . When the decay of these mediators into the lightest pseudoscalar  $a$  is allowed, this decay process dominates over the direct decay into  $\chi\chi$ . In symmetry with what happens for the mono-h signature discussed in [?], for certain region of parameter space the signatures  $pp \rightarrow t\bar{t}A \rightarrow t\bar{t}ah$  and  $pp \rightarrow t\bar{t}H \rightarrow t\bar{t}aZ$  become sizeable. For the former case, it can be estimated from Fig. 12(b) of Ref. [?] that for relatively small  $m(A)$  the  $pp \rightarrow t\bar{t}ah$  cross section can be up to 30% that of the  $pp \rightarrow t\bar{t}\chi\chi$  process. The interplay between the parameters of the model, and especially between the heavy higgs masses for these types of final state render the phenomenology interesting and variegated, as can be seen for example in the branching ratio study of Fig. ??, although further studies are needed to fully understand the interplay and the complementarity between these  $t\bar{t}h + E_T^{\text{miss}}$  channels and the traditional heavy flavour dark matter searches.

#### 4.1.11 Top pair resonant searches

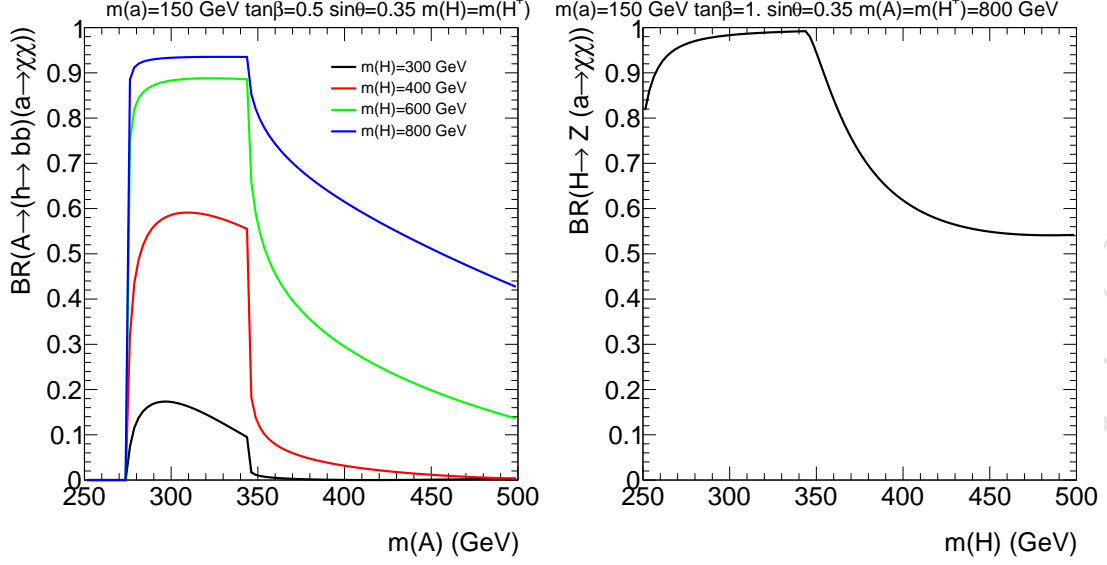
Heavy scalar and pseudoscalar bosons decaying dominantly into top-quark pairs can be searched for by studying the resulting  $t\bar{t}$  invariant mass spectra. However, interference effects between the signal processes and the SM  $t\bar{t}$  production distort the signal shape from a single peak to a peak-dip structure [appropriate REFs?]. Interference between a loop-induced and a tree-level process cannot currently be simulated in MadGraph. To amend this problem, the "Higgs\_Effective\_Couplings\_FormFactor" approach [?] is implemented in the UFO, replacing the loop production by an effective vertex. **Are we interested to insert one of the validation plots from atlas?**

#### 4.1.12 Four tops final states

Work in progress

#### 4.1.13 Final proposal for parameter scan

- a two-dimensional scan in the light pseudoscalar mass ( $m_a$ ) - heavy pseudoscalar mass ( $m_A$ ) plane where  $m_a = m_A$ , fixing  $\tan\beta$  to 1.0,  $\sin\theta$  to 0.35 and the



**Figure 45:** Example of the dependence of the  $A$  and  $H$  branching ratio into  $ah$  as a function of some parameters of the 2HDM model.

Dark Matter mass ( $m_{DM}$ ) to 10 GeV.

- a one-dimensional scan in DM mass from 1 GeV to 500 GeV for a point in the middle of the sensitivity range for the mono- $V$  analyses at  $m_A=600$ ,  $m_a=250$  GeV, so the connection between this model and cosmology is clear as the measured relic density starts being satisfied at values of DM mass around 100 GeV

In order to explore changes in complementarity with different analyses and kinematics, this should be complemented by:

- a two-dimensional scan in the  $m_a$  -  $\tan\beta$  plane, for comparison with the  $t\bar{t} + \text{MET}$  /  $b\bar{b} + \text{MET}$  analyses. In this case, the charged Higgs mass ( $m_{H^\pm}$ ), the heavy pseudoscalar mass ( $m_A$ ) and the heavy Higgs mass ( $m_H$ ) should be fixed to 600 GeV. This scan includes points: 50, 45, 40, 35, 30, 25, 20, 15, 10, 5 for  $M(a)$  masses between 10 and 350 GeV. The high- $\tan\beta$  points would be of primary interest to the HF + DM searches. Uli's studies have shown that one can simply reweight the existing  $t\bar{t} + \text{DM}/b\bar{b} + \text{DM}$  models from DMF to the new 2HDM+PS cross sections; full simulation of the newly proposed 2HDM+PS points is not required.
- two one-dimensional scans in  $\sin\theta$  for the comparison of mono-Higgs and  $b\bar{b} + \text{MET}$  analysis (it is expected that the  $b\bar{b} + \text{MET}$  analysis will only have to rescale previous models/cross-sections) [2]: -  $m_H = m_A = m_{H^\pm} = 600\text{GeV}$ ,  $m_a = 200\text{GeV}$ ,  $\tan\beta=1$   
-  $m_H = m_A = m_{H^\pm} = 1000\text{GeV}$ ,  $m_a = 350\text{GeV}$ ,  $\tan\beta=1$

The PDF recommended is five-flavor. ATLAS will use the NNPDF3.0 PDF set. Some text by Fabio Maltoni and Ulrich Haisch can be found in the `texinputs_app` folder.

## 5 Connection with cosmology

An important requirement for models of dark matter is their consistency with existing astrophysical observations, namely the observed dark matter relic density. The relic density is driven by the annihilation cross-section of dark matter into SM particles. For a given model of dark matter-SM interactions, the annihilation cross-section is fully defined and a calculation of the resulting relic density can be performed.

### 5.1 Technical setup

The MADDM [?] plugin for MG5\_aMC@NLO is used to calculate the present-day relic density for this model. By modeling the thermal evolution of the cross-section during the expansion of the early universe, the time of freeze-out is determined. All tree-level annihilation processes are taken into account, and the Yukawa couplings of all fermions are taken to be non-zero. The Feynman diagrams of annihilation processes taken into account in this calculation are shown in Fig. ???. Generally, the annihilation proceeds via single or double s-channel exchange of the pseudoscalars  $a$  and  $A$ , with subsequent decays. Since MADDM uses only tree-level diagrams, contributions from off-shell pseudoscalars can only be taken into account for the case of single s-channel mediation with direct decay of the pseudoscalar to SM fermions. If the pseudoscalar instead decays to other bosons or if the annihilation proceeds through double s-channel diagrams, the outgoing bosons are taken to be on-shell and their decays are not simulated.

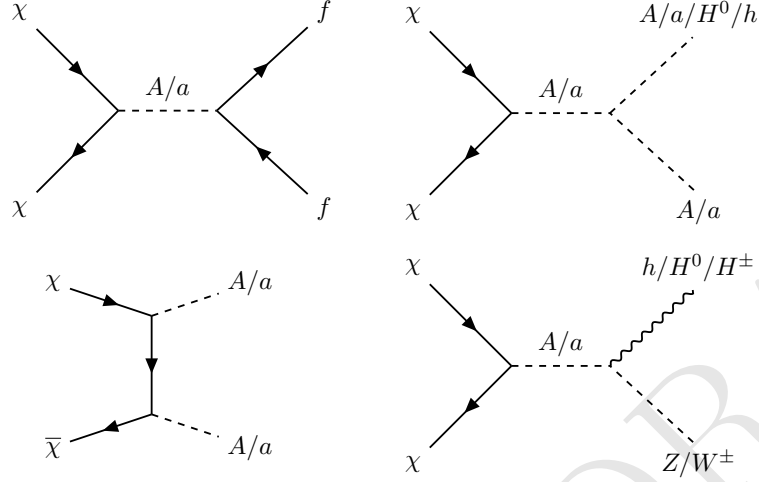
In all scans presented here, the common parameter choices  $\sin(\theta) = 0.35$ ,  $m_h = 125\text{GeV}$ ,  $g_\chi = 1$ ,  $\lambda_i = 3$  are used.

### 5.2 Results

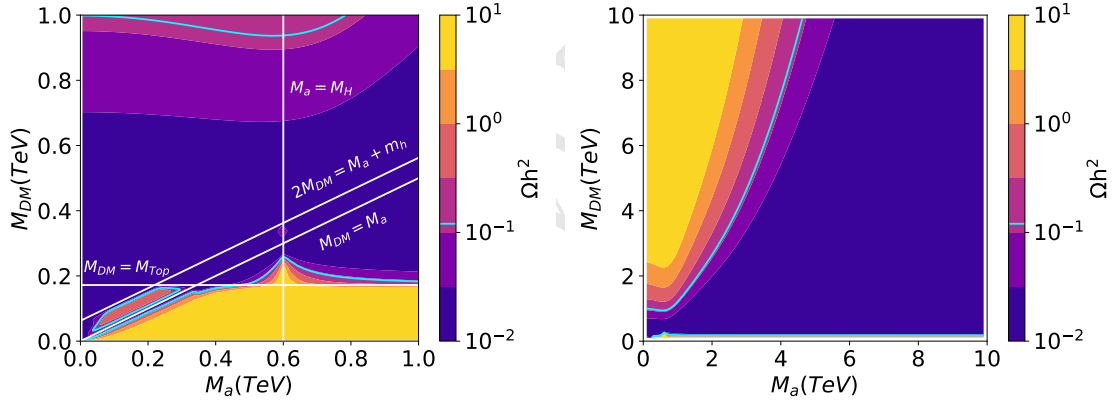
The relic density is shown for a scan in the  $M_a$ - $M_\chi$  plane in Fig. ???. For small values of  $M_\chi$  below the mass of the top quark, DM is mostly overabundant. In this regime, annihilation to quarks is suppressed by the small Yukawa couplings of the light fermions. The observed relic density can only be achieved for  $M_\chi \approx M_a/2$ , where annihilation is resonantly enhanced, or for  $M_\chi \approx (M_a + M_h)/2$ , close to the threshold for the  $\chi\chi \rightarrow ha$  process. Above the top threshold, annihilation into fermions becomes very efficient and DM is underabundant. As  $M_\chi$  increases further, annihilation via single s-channel diagrams is increasingly suppressed and the relic density rises again. The observed density is reproduced again for  $M_\chi \approx 1\text{TeV}$  at low  $M_a$ . For values of  $M_a$  beyond the LHC reach of a few TeV, the allowed parameter region at the top threshold  $M_\chi \approx m_{\text{top}}$  stays independent of the value of  $M_a$ , indicating that a DM candidate that is mass degenerate with the top quark cannot be excluded by LHC searches alone.

The dependence of the relic density on the choice of  $M_\chi$  is further explored by performing a one-dimensional scan, as shown in Fig. ???. The relic density shows clear structures corresponding to the previously discussed regions of resonant enhancement, as well as kinematic boundaries. Overall, the behavior is dominated by the low- $M_\chi$  suppression of the annihilation cross-section, the resonant enhancement at  $M_\chi = M_a/2$  and the kinematic

top thresholds. Other effects, such as resonant enhancement of  $\chi\chi \rightarrow A$  annihilation are present, but only have small effects.

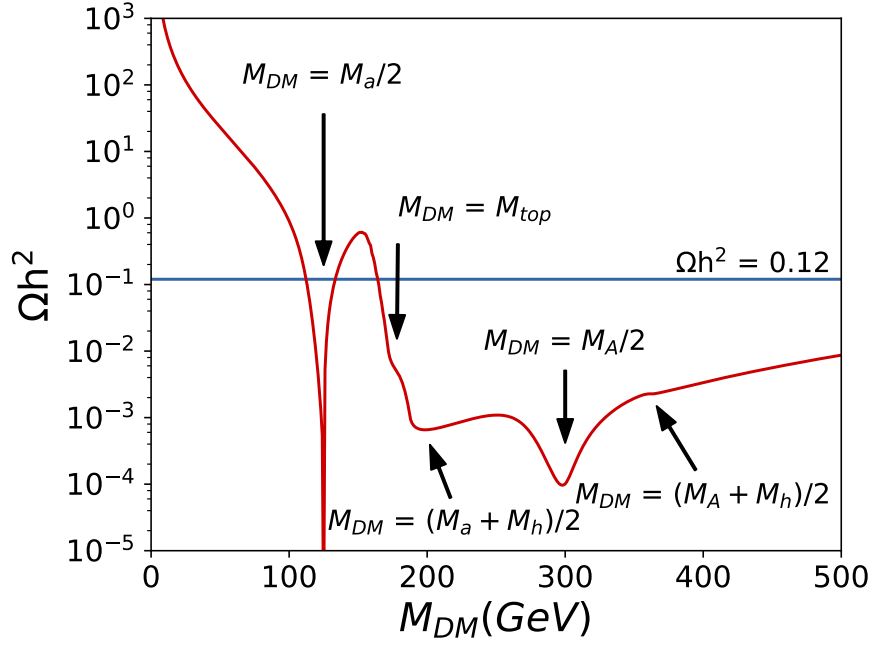


**Figure 46:** Annihilation diagrams taken into account in the relic density calculation.



**Figure 47:** Predicted relic density for a two-dimensional scan of  $M_\chi$  and  $M_a$ . The other parameters of the model remain fixed with  $m_H = m_A = m_{H^\pm} = 600$  GeV and  $\tan\beta = 1$ , as well as the default choices described in the text. The color scale indicates the relic density, the cyan solid line shows the observed value of  $\Omega h^2 = 0.12$ . The color scale is truncated at its ends, i.e. values larger than the maximum or smaller than the minimum are shown in the same color as the maximum/minimum. While the left focuses on the mass region relevant to collider searches, the right panel shows the development of the relic density for a larger mass region.

## 6 Conclusions



**Figure 48:** Relic density for a one-dimensional scan of  $M_\chi$ . The other parameters of the model remain fixed with  $m_H = m_A = m_{H^\pm} = 600$  GeV,  $M_a = 250$  GeV and  $\tan \beta = 1$ , as well as the default choices described in the text. Various kinematic thresholds and regions of resonant enhancement are visible. Consistency with the observed value of  $\Omega h^2 = 0.12$  is mainly controlled by the resonant enhancement of  $\chi\chi \rightarrow a$ , as well as the onset of  $\chi\chi \rightarrow t\bar{t}$ .