Dielectic function calculations

11 dec



Used formulas

recap of last time

$$S_{tot}(E) = S_b(E)$$

$$S(E) = \frac{N_{ZLP}t}{\pi a_0 m_0 v^2} \operatorname{Im} \left[\frac{-1}{\varepsilon(E)} \right] \ln \left[1 + \left(\frac{\beta}{\theta_E} \right)^2 \right]$$

$$\operatorname{Re}\left[\frac{1}{\varepsilon(E)}\right] = \mathcal{C}\left\{\operatorname{sgn}\left[\mathcal{S}^{-1}\left\{\operatorname{Im}\left[\frac{-1}{\varepsilon(E)}\right]\right\}\right]\right\}$$



$$\theta_E = \frac{E}{\gamma m_0 v^2}$$

$$\frac{\int_0^\infty \frac{S(E)}{\ln\left[1 + \left(\frac{\beta}{\theta_E}\right)^2\right]} \frac{dE}{E}}{\frac{\pi}{2}(1 - \operatorname{Re}\left[\frac{1}{\varepsilon(0)}\right])} = \frac{N_{ZLP}t}{\pi a_0 m_0 v^2} \equiv K,$$



$$S_{s}(E) = \frac{2I_{0}k_{0}^{-1} \left[\operatorname{Im} \left(\frac{-4}{1+\varepsilon} \right) - \operatorname{Im} \left(\frac{-1}{\varepsilon} \right) \right]}{\pi^{2}a_{0}m_{0}v^{2}} \left[\frac{\tan^{-1}(\beta/\theta_{E})}{\theta_{E}} - \frac{\beta}{\beta^{2} + \theta_{E}^{2}} \right]$$

$$\hbar \mathbf{k}_{0} = \gamma m_{0}\mathbf{v}$$

$$\theta_{E} = \frac{E}{\gamma m_{0}v^{2}}$$



Plan of attack

Assume:

$$S_{tot}(E) = S_b(E)$$

- Calculate ε' with KK-analysis
- Calculate

$$S_s(E) = C_s(E) \left(\operatorname{Im} \left[\frac{-4}{1 + \varepsilon(E)} \right] - \operatorname{Im} \left[\frac{-1}{\varepsilon(E)} \right] \right)$$

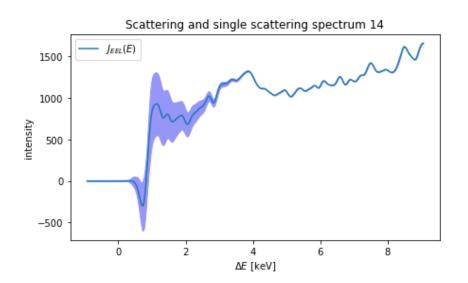
Better approximation:

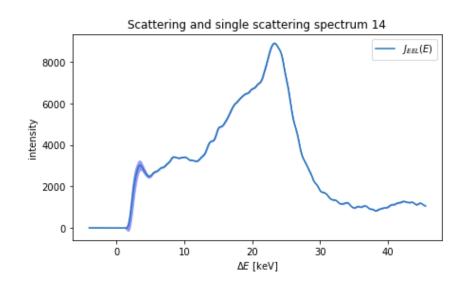
$$S_b(E) = S_{tot}(E) - S_s(E)$$

- Calculate ε " with KK-analysis
- Calculate S_s"
- Approximate S_b"
 - Calculate ε " with KK-analysis
 - Calculate S_s"
 - Approximate S_b""

Repeat until convergence

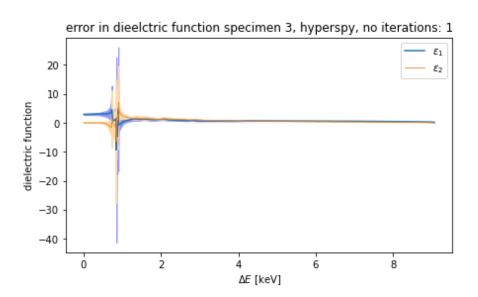
EELS

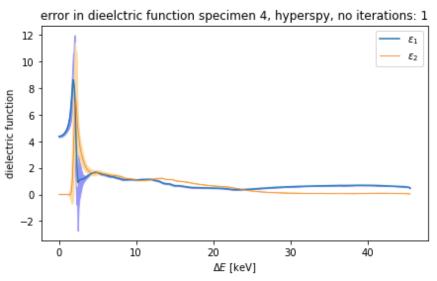




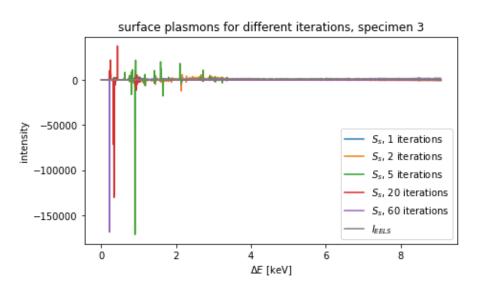


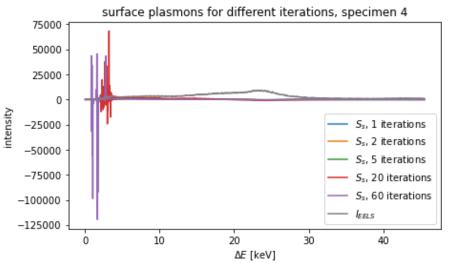
First iteration





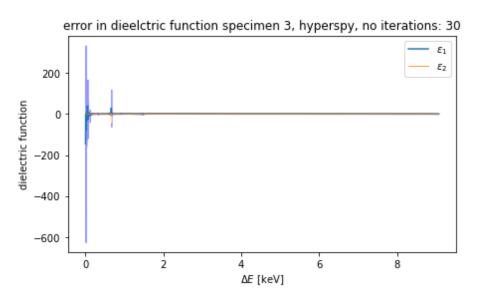


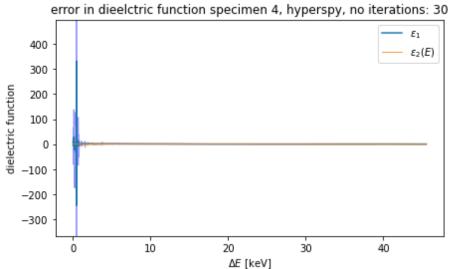






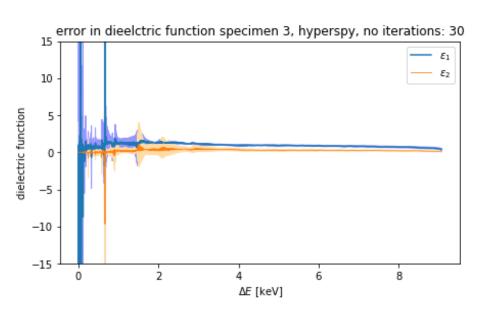
Next iterations

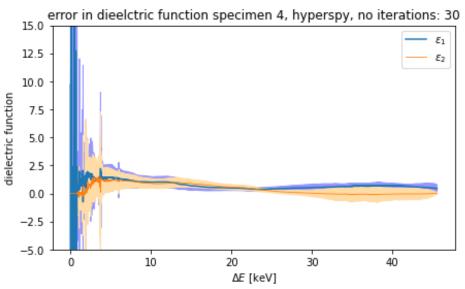






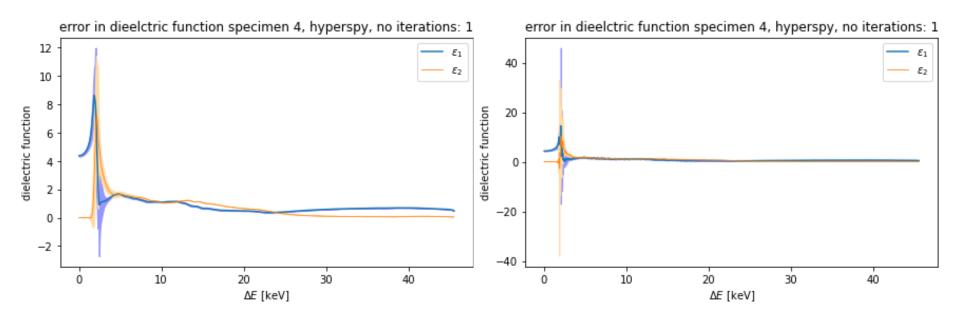
Equal axis over iterations





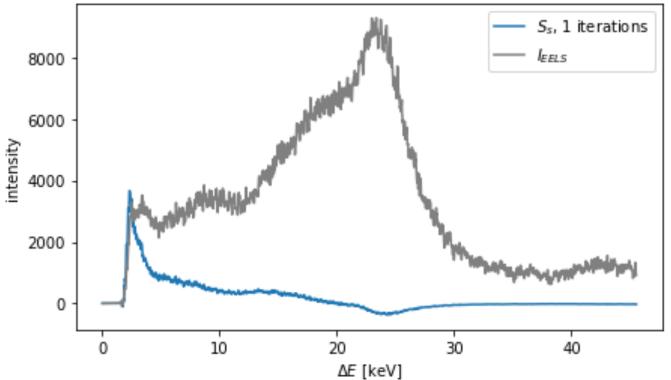


No smoothing





surface plasmons for different iterations, specimen 4





surface plasmons for different iterations, specimen 4

