Grid2Grid: HOS Wrapper Program

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23 March, 2017

Version 2.0





Ecole Centrale de Nantes

Release Notes

Version 2.0

New features

- The source code file structure is organized for the recognization of class header and its functionality.
- HOS results file generated by HDF5 library is added as an input file for Grid2Grid.
- Dictionary type input for Grid2Grid is introduced.
- Input file for postGrid2Grid is changed to follow dictionary format.
- Cmake is introduced.

Fixed

- HOS-NWT FFTW3 memory deallocation error (destructor of HOS-NWT class).
- z-directional surf2vol grid bug (when meshGrid with meshRatio= 1).
- 3D HOS-Ocean interpolation class initialization error (when n_x and n_y is different).
- ...

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1 Introduction

Wave generation solvers using Higher Order Spectral Method (HOS) have been validated and developed for several years (Ducrozet et al. (2016), Ducrozet et al. (2007), Bonnefoy et al. (2011) and Ducrozet et al. (2012)). HOS solves nonlinear wave propagation in open-sea (HOS-Ocean) and also in numerical wave tank (HOS-NWT) with low computation time comparing with other nonlinear wave solvers because the theory is based on pseudo-spectral method (HOS (b) and HOS (a)). Those HOS wave solvers are released as open-source codes, which anyone can develop, use and distribute under the terms of GNU General Public Licence (GPLv3).

Nonlinear irregular wave generation in computational fluids dynamic (CFD) solvers becomes important recently in naval fields to better estimate the loads on offshore structure. The conventional linear superposition methods imply a long computational time for wave generation and the simulation is made almost impossible without having enough computational power. And if the method is based on linear wave theory, there is also question on occurrence of nonlinear phenomenon and the interaction between waves as the simulation goes. Therefore dedicated nonlinear wave solvers with high computational speed are needed.

Grid2Grid is developed as a wrapper program of HOS to generate wave fields from the results of HOS computation. Grid2Grid reconstructs wave fields of HOS with inverse fast Fourier transforms (FFTs) and uses a quick spline module, the nonlinear wave fields can be fastly reconstructed for arbitrary simulation time and space. The nonlinear wave simulation is then possible for a particular position and time where specific non linear phenomenon occur.

Grid2Grid compiles a shared library (libGrid2Grid.so) which can be used for communication with other programming language using the ISO_C_BINDING rule. It compiles also a post processing program of HOS.

2 Program Structure

The file structure of Grid2Grid is shown in Fig. 2.1. The directory config contains the compiling rule for makefile not cmake. The directory doc constains Grid2Grid manual files. The directory example contains the examples for interface between other languages and Grid2Grid. The directory src includes the libraries and source file directory. The library used Grid2Grid are libbspline and libFyMc. The libspline is b-spline interpolation library and libFyMc is a general Fortran library. The libGrid2Grid is the source code directory of Grid2Grid and it is composed of each modules which are sepated in a module directory with its sub-class(type) directories.

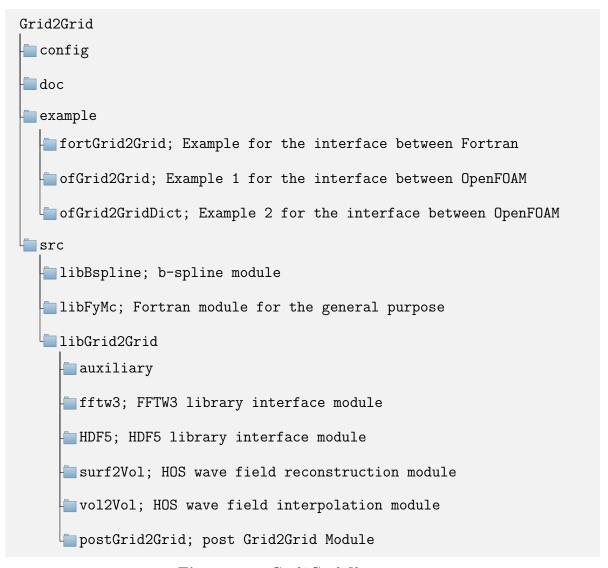


Figure 2.1. Grid2Grid file structure

The program structure of Grid2Grid is depicted in Fig. 2.2. The program is composed of several modules (.f90) with a suffix mod. HOS wave fields are generated by modSurf2Vol from the HOS result file (modes_HOS_SWENSE.dat or modes_HOS_SWENSE.hdf5). Since the results files only contains modes information, the volumic wave fields is reconstructed on the HOS grid by inverse FFTs (denoted as H_2 Operator). The volumic wave field in Grid2Grid at the certain time step is called as a snapshot of wave field. modVol2Vol constructs an interpolation data structure from several snapshots of wave field by using multidimensional spline module (Williams (2015)). modVol2Vol can directly compiled with other fortran program if the same Fortran compiler is used (gfortran;4.9.2). modGrid2Grid generates shared library named as libGrid2Grid.so to communicate with other languages. Standard program language rule ISO_C_BINDING is required to communicate with the library Grid2Grid. The examples are given in directory example. modPostGrid2Grid is a post processing module of Grid2Grid generating the HOS wave fields for the 3D visualization(VTK format) and the wave elevation time series.

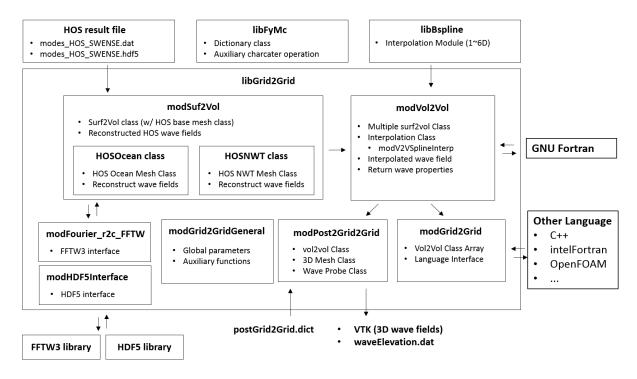


Figure 2.2. Program Structure of Grid2Grid

The main feature of each module is following.

- modSurf2Vol: HOS-Ocean and NWT classes and reconstructed HOS wave fields
- modVol2Vol: Interpolate reconstructed HOS wave fields
- modGrid2Grid: Communication with other language with ISO_C_BINDING
- modPostGrid2Grid: Post processing of HOS (wave fields and elevation)
- modFourier_r2c_FFTW : Interface module of FFTW open library
- modHDF5Interface : Interface module of HDF5 open library
- modGrid2GridGeneral : Grid2Grid global variables and auxiliary functions
- libBspline : Multidimensional b-spline module written in Fortran.
- libFyMc : Auxiliary fortran functions (Dictionary, Character operation, ...)

2.1 typSurf2Vol

2.1.1 Description

Surf2Vol is a wrapper class to access HOS Ocean and NWT class. HOS-Ocean and NWT classes have the similar class structures but only reconstruction schemes and definition of meshes are slightly different. The reconstructed wave fields by two HOS classes are saved in each HOS mesh class which is derived class from base HOS mesh class. By using this mesh pointer, Surf2Vol class can access both HOS reconstructed wave fields. It is reminded that the direct access to the HOS wave fields is possible on HOS simulation time and grid by only HOS mesh pointer to prevent misuse of HOS wave data.

Surf2Vol class structure is depicted in Fig. 2.3. Surf2Vol class contains HOSOceanSurf2Vol and HOSNWTSurf2Vol classes. When the function is called, it calls the sub-class function distiguished by HOS type.

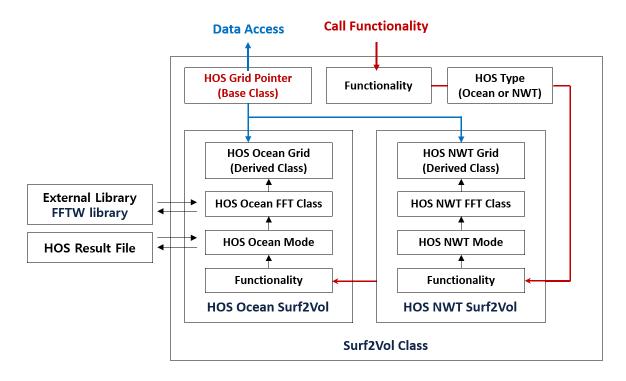


Figure 2.3. Surf2Vol class structure

hosNWTSurf2Vol and hosOceanSurf2Vol classes reconstruct the HOS wave fields from the result file of HOS by using the H_2 operator (inverse FFTs). Wave reconstruction and HOS wave theory is well explained in Ducrozet et al. (2007) and Ducrozet et al. (2012). Each class reconstruct the wave fields on the derived HOS mesh class.

HOS wave theory is based on the superposition of modes satisfying the Laplace equation, sea bottom and free surface boundary condition basically. The vertical profile of the mode function is usually given as the exponential or hyperbolic functions. The vertical profile could magnify the local properties when the number of modes is increased and the wave steepness is signigicantly high. Those behaviors usually happens above the z=0. It is resulted from the amplitudes reduction is not as much decreasing with the number of modes. Therefore those mathematical formulation gives the unnatural values. To prevent those things, the criterion to cut the local mode contribution above the z=0 is introduced as (2.1).

$$f_{mn}(z) = \begin{cases} \frac{\cosh k_{mn}(z+H)}{\cosh k_{mn}H} & \text{if } f_{mn}(z) < C_{f(z)} \\ C_{f(z)} & \text{if } f_{mn}(z) \ge C_{f(z)} \end{cases}$$
(2.1)

where

 k_{mn} : HOS mode wave number z: HOS z-coordinates H: water depth

 $C_{f(z)}: f_{mn}(z)$ function criterion value (default = 10)

The parameter $C_{f(z)}$ is set to be 10 in Grid2Grid as a defualt value. If the local wave velocities generated by Grid2Grid are not sufficient, the parameter can be changed. The parameter is defined in modGrid2GridGeneral.f90 as a FNZ_VALUE.

HOS result file only contains the mode amplitudes computed at each HOS simulation time. The volumic grid should be generated and the wave fields are reconstructed on this grid. The generated volumic grid is used as a background grid for the interpolation. To constuct the HOS grid, following information should be given when surf2vol class is initialised.

- o zMin, zMax
- o nZMin, nZMax
- o nZMinRatio, nZMaxRatio [Optional]

where zMin and zMax is used to set z-directional domain length and it should have the negative and positive value. nZMin and nZMax are the number of z-directional grid. It is recommended to have at least 50-100 for the sufficient interpolation. If the number of grid points is not sufficient, the interpolated values could be strange due to the vertical profile of $f_{mn}(z)$. nZMinRatio and nZMaxRatio are the ratio of maximum and minumum height of grid $(\Delta z_{max}/\Delta z_{min})$. Minimum grid is located at z=0. Those are optional values set to be 3 as default. The generated HOS grid is automatically saved whe surf2vol class is initialised. And it is visualized by using ParaView. The VTK file is located at VTK/Grid2Grid/surf2volMesh.vtk.

2.1.2 Class (Type)

Class: Surf2Vol

- Data:
 - o hosNWTSurf2Vol_: HOS-NWT Surf2Vol Class
 - o hosOceanSurf2Vol_: HOS-Ocean Surf2Vol Class
 - optrHOSMesh_: HOS Mesh Pointer
- Functionality:
 - o initialize : Initialise HOS Surf2Vol class
 - o correct : Update HOS wave fields
 - o destroy: Class desroyer

Class: HOSOcean and HOSNWT

- Data:
 - HOSfile: HOS result file (modes_HOS_SWENSE.dat) or modes_HOS_SWENSE.hdf5
 - o HOSmode: HOS Ocean or NWT modes
 - o HOSmesh: HOS Ocean or NWT mesh
 - \circ HOSfftw: HOS FFT class for H_2 operator
- Public Functionality:
 - o initialize : Initialise HOS Ocean or NWT Surf2Vol
 - o correct: Update HOS Ocean or NWT wave fields
 - o destroy: Class desroyer
- Private Functionality:
 - o init_read_mod: Read HOS number of modes and allocate dynamic array
 - o read_mod: Read HOS modes at given HOS time index
 - o buildGlobalMesh: Build HOS mesh with the given HOS construction parameter
 - \circ reconstructionFFTs: Reconstruct the wave fields by H_2 operator

2.1.3 How to use

- Initialise Surf2Vol

```
Call hosS2V%initialize(hosType, filePath, zMin, zMax, nZmin, nZmax,
   zMinRatio, zMaxRatio)
              : Surf2vol Class (Type)
! hosS2V
              : HOS Type (Ocean or NWT)
! hosType
! filePath
              : HOS result file path (modes_HOS_SWENS.dat)
! zMin, zMax : HOS grid z-minimum and z-maximul (vertical domain)
! nZmin, nZmax : Number of z-directional Grid
! zMinRatio, zMaxRatio (Optional)
! : Ratio of maximum and minimum height of grid (default=3)
! or
Call hosS2V%initialize(dict)
! hosS2V
             : Surf2vol Class (Type)
! dict
          : HOS dictionary to initialize HOS surf2vol (Type)
```

- Correct Surf2Vol

```
Call hosS2V%correct(hosIndex)
! hosS2V : Surf2vol Class (Type)
! hosIndex : HOS time index
```

- Data access on wave field of Surf2Vol
 - Wave elevation

 \circ Wave velocity

```
u = hosS2V%ptrHOSMesh_%eta(ix, iy, iz)
v = hosS2V%ptrHOSMesh_%eta(ix, iy, iz)
w = hosS2V%ptrHOSMesh_%eta(ix, iy, iz)
```

```
! hosS2V : Surf2vol class (Type)
! ix, iy, iz : HOS grid index (x, y, z)
! u, v, w : Wave velocity (x, y, z)
```

 \circ Dynamic pressure $(p_d = p - \rho gz)$

```
pd = hosS2V%ptrHOSMesh_%pd(ix, iy, iz)
! hosS2V : Surf2Vol class (Type)
! ix, iy, iz : HOS grid index (x, y, z)
! pd : Dynamic pressure
```

- Destruct of Surf2Vol

```
Call hosS2V%destroy()
! hosS2V : Surf2Vol class (Type)
```

2.2 typVol2Vol

2.2.1 Description

Vol2Vol interpolates the wave fields and return wave properties at given time and position. It has the multiple Surf2Vol classes and interpolation class. The Vol2Vol class structure is described in Fig 2.4. The reconstructed HOS wave fields (snapshot of wave field) retrived from Surf2Vol are used to construct interpolation data.

The HOS result file contains the whole simulation time information. If the HOS wave fields and interpolation is applied for the whole HOS simulatio time, the pre-computation time becomes too long and it needs hugh computation memory. Grid2Grid is designed for the efficient wave-field reconstruction demanded by CFD solvers for a relatively short period and small domain. Therefore it is not necessary to reconstruct whole HOS wave fields. For the efficient memory control, the revolving algorithm is introduced to holds multiple HOS wave fields and to update HOS wave field if it is demanded.

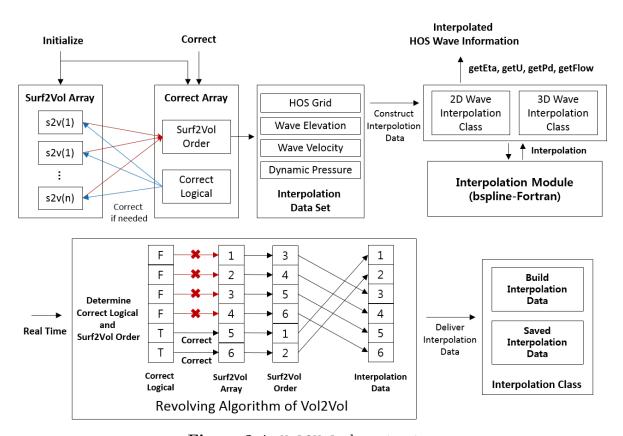


Figure 2.4. Vol2Vol class structure

When Vol2Vol initialised, the Surf2Vol class array is allocated and initialise multiple Surf2Vol and connect those Surf2Vol class array with the revolving algorithm. The revolving algorithm determine which Surf2Vol should be updated and the order of Surf2Vol array for the efficient generation of interpolation data.

The subroutine correct with an input t first determine HOS Surf2Vol correction indexand Surf2Vol order by revolving algorithm. Only necessary HOS Surf2Vol is updated and re-ordered to constructed for interpolation data. The interpolation data is constructed from the multiple wave field snapshot. The interpolation class holds the interpolation classes specific to HOS and it communicates with the bspline-Fortran module.

The subroutine getEta, getU, getPd and getFlow return the interpolated wave properties for the given time and space.

2.2.2 Class (Type)

```
Class: Vol2Vol

- Data:

onInterp_: Interpolation order (2: Linear, 3: Quadratic, 4: Cubic, ...)

onSaveT_: Number of Surf2Vol wave fields (nSaveT_> nInterp_)

oHOSs2v_(:): Array of Surf2Vol class

oitp2D_: Interpolation class for 2D waves

oitp3D_: Interpolation class for 3D waves

- Functionality:

oinitialize: Initialise HOS Vol2Vol class with HOS type, result file path, ...

ocorrect: Update HOS wave fields with real-time

ogetEta: Get interpolated wave elevation

ogetU: Get interpolated wave velocity

ogetPlow: Get flow information

odestroy: Class destroyer
```

2.2.3 How to use

- Initialise Vol2Vol

```
Call hosV2V%initialize(hosType, filePath, zMin, zMax, nZmin, nZmax,
zMinRatio, zMaxRatio, iflag)
! hosV2V
              : Vol2vol Class (Type)
              : HOS Type (Ocean or NWT)
! hosType
! filePath
              : HOS result file path (modes_HOS_SWENS.dat)
              : HOS grid z-minimum and z-maximul (vertical domain)
! zMin, zMax
! nZmin, nZmax : Number of z-directional Grid
! zMinRatio, zMaxRatio (Optional)
! : Ratio of maximum and minimum height of grid (default=3)
! iflag : Wriging option (iflag = 1, write Grid2Grid information)
! or
Call hosV2V%initialize(dict)
! hosV2V : Vol2vol Class (Type)
            : HOS dictionary to initialize HOS vol2vol (Type)
```

- Correct Vol2Vol

```
Call hosV2V%correct(simulTime)
! hosV2V : Vol2vol Class (Type)
! simulTime : Simulation time (real time value)
```

- Get wave elevation from Vol2Vol

- Get wave velocity from Vol2Vol

- Get dynamic pressure from Vol2Vol

- Get flow information from Vol2Vol

- Destroy Vol2Vol

```
Call hosV2V%destroy()
```

2.3 modGrid2Grid

2.3.1 Description

modGrid2Grid is not a class but the module which is desinged for the communication between other programming languages. The module structure is depicted in Fig. 2.5. It has a data base (DB) which has the input data information and Vol2Vol. The input data is saved in data base and dertermines whether new Vol2Vol is initialized. When the ohter program first initialise Grid2Grid, modGrid2Grid firstly checks the input variables. If the same input is previously given, it return previous Vol2Vol index. But it does not exist, it allocates new Vol2Vol and issues Vol2Vol index. Other programming language distingush the different HOS wave theory in a same simulation by HOSIndex (pointer in ISO_C_BINDING is complicate). Therefore the subroutines correct and get* should be called with HOSIndex, position and time.

The array size of modGrid2Grid is set to be 100 as a default (100 different HOS waves) but it does not consume much of memory because the classes of Grid2Grid are programmed with the dynamic arrays and consequently only a few static data are used. The variable nMaxVol2Vol in src/libGrid2Grid/modGrid2Grid.f90 can be changed.

The functionalities of modGrid2Grid are similar with Vol2Vol.

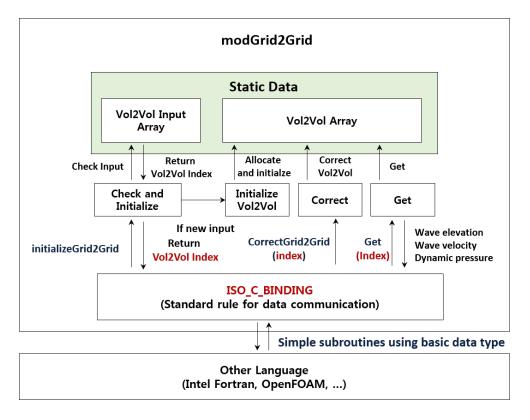


Figure 2.5. Grid2Grid Module structure

2.3.2 Subroutines

The interface between other languages with modGrid2Grid will be described in Chap. 4.

Subroutines:

- Initialise Grid2Grid
 - $\circ \ _modgrid2grid_MOD_initializegrid2grid\\$
 - ${\tt o_modgrid2grid_MOD_initializegrid2griddict}$
- Correct Grid2Grid
 - o __modgrid2grid_MOD_correctgrid2grid
- Get wave elevation
 - o __modgrid2grid_MOD_gethoseta
- Get wave velocity
 - $\circ \ _{\tt modgrid2grid_MOD_gethosu}$
- Get dynamic pressure
 - \circ _modgrid2grid_MOD_gethospd
- Get flow information
 - o __modgrid2grid_MOD_gethosflow
- Get HOS simulation end time
 - $\circ \ _{\tt modgrid2grid_MOD_gethosendtime}$
- Get HOS water depth
 - ${\tt o_modgrid2grid_MOD_gethoswaterdepth}$
- Get logical data indicating HOS wave theory is initialized
 - ${\tt o_modgrid2grid_MOD_isgrid2gridinitialized}$

2.4 PostGrid2Grid

2.4.1 Description

PostGrid2Grid is a HOS post-processing class. It generates 3D VTK files of wave fields for the visualization and wave elevation time series computed from Vol2Vol class. PostGrid2Grid algorithm is depicted in Fig. 2.6. PostGrid2Grid is initialised with the input file. The input file (postGrid2Grid.dict) contains the parameters needed for the post processing and HOS-reconstruction. It is composed with many dictionary input (HOS, simulation, vtkMesh and waveProbe dictionaries). PostGrid2Grid reads and checks the input file and then build 3D visualization grid and wave probes with given dictionaries. Vol2Vol class is also initialised with HOS dictionary. The subroutine doPostProcessing run a time simulation of reconstruction. The subroutine correct updates the Vol2Vol class and gets the wave fields. If the grid option airMesh is equal to false, 3D grid is fitted to the wave elevation.

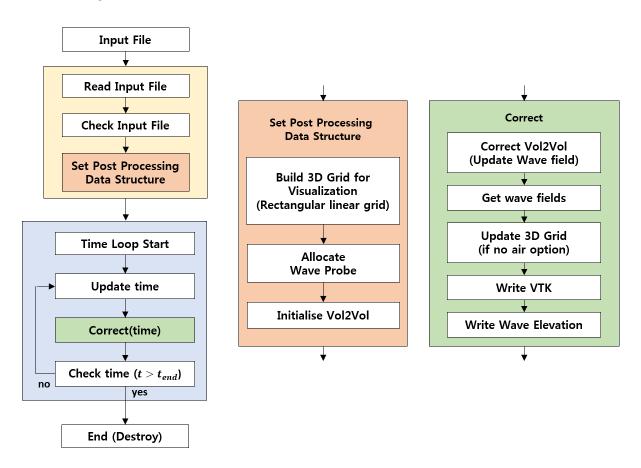


Figure 2.6. PostGrid2Grid Algorithm

2.4.2 Class(Type)

```
{\bf Class}: {\tt PostGrid2Grid}
```

- Data:
 - o hosVol2Vol_: Vol2Vol class
 - o rectLGrid_: Rectangular linear grid for 3D wave fields (VTK output)
 - ∘ waveProbe_(:) : Wave probe
- Functionality (Public):
 - o initialize : Initialise PostGrid2Grid class
 - o correct: Correct Vol2Vol, rectLGrid_ and waveProbe_ and write output
 - o writeVTK: Write 3D wave fields in VTK format
 - o doPostProcessing : Do post processing
 - o destroy: Destuctor of PostGrid2Grid class
- Functionality (Private):
 - o readPostG2GInputFileDict : Read PostGrid2Grid input file
 - o checkPostG2GParameter : Check PostGrid2Grid input file
 - writeVTKtotalASCII: Write wave fields (Including air domain)
 - o writeVTKnoAirASCII: Write wave fields (Grid is fitted to wave elevation)
 - o writeWaveProbe : Write wave elevation time series

2.4.3 Input File of PostGrid2Grid

PostGrid2Grid needs the input file. The input file name is postGrid2Grid.dict. The input is recognized by dictionary(keyword + value with sub-dictionary). The special characters are treated as a comment (!, # and \\) and C++ style comment block is also allowed.

- PostGrid2Grid variables

- HOS dictionary

```
### HOS dictionary -----
HOSDict
               # HOS solver type; NWT or Ocean
  type Ocean;
  filePath example/modes_HOS_SWENSE.dat; # HOS file path
  fileType ASCII; # Option; HOS result file type, ASCII or HDF5
  interpolationOrder 3; # Option; 3:Cubic spline [Default]
          -0.6; # HOS domain zMin
  zMin
  zMax
          0.6;
                # HOS domain zMax
         50; # HOS domain nZMin
  nZMin
  nZMax
         50;
              # HOS domain nZMax
  zMeshType meshRatio;  # Mesh type (uniform, sine, meshRatio)
  zMinRatio 3.0; # Option, z<=0 meshing ratio (meshRatio)</pre>
  zMaxRatio 3.0; # Option, z<=0 meshing ratio (meshRatio)</pre>
             true; # Option; write log option
  writeLog
}
```

- Simulation Dictionary

```
### Simulation dictionary -----
#

simulation
{
   startTime 2712.0;
   endTime 2812.0;

   dt 0.1;
}
```

- 3D visualization dictionary

```
### VTK mesh dictionary -----
vtkMesh
 airMesh false;
                    # Air meshing option
                   # VTK mesh xMin
 xMin
          0.0;
 xMax
         100.0;
                   # VTK mesh xMax
                   # VTK mesh yMin
 yMin
          0.0;
 yMax
         100.0;
                   # VTK mesh yMax
 nX
          50;
                   # VTK mesh nX
                    # VTK mesh nX
 nΥ
          50;
         -0.6; # VTK mesh zMin 0.6; # VTK mesh zMax
 zMin
 zMax
 nZMin 50;
                   # VTK mesh nZMin
                   # VTK mesh nZMax
 nZMax 50;
 zMeshType meshRatio;  # Mesh type (uniform, sine, meshRatio)
 zMinRatio 3.0; # Option, z<=0 meshing ratio (meshRatio)</pre>
 zMaxRatio 3.0; # Option, z<=0 meshing ratio (meshRatio)</pre>
}
```

- Wave probe dictionary

2.4.4 How to use

```
!! Subroutine to run PostGrid2Grid -----
Subroutine runPostGrid2Grid(inputFileName)
!! -----
               !! Use PostGrid2Grid Module
Use modPostGrid2Grid
!! -----
Implicit none
Character(Len = * ),intent(in) :: inputFileName !! postGrid2Grid.inp
Type(typPostGrid2Grid) :: postG2G !! postGrid2Grid Class
!! Initialize PostGrid2Grid with Input File
Call postG2G%initialize(inputFileName)
!! Do Post Processing
Call postG2G%doPostProcessing()
!! Destroy
Call postG2G%destroy
!! -----
End Subroutine
```

3 Installation

3.1 Pre-Install

3.1.1 FFTW Install

Grid2Grid needs a fast Fourier transform (FFT) library. FFTW is GNU licenced FFT library. The installation order is the following:

1. Download FFTW library

At the FFTW website (http://www.fftw.org/download.html), the latest version of FFTW is available. Download FFTW library.

Downloading FFTW

Mailing list / Announcements

Subscribe to the fftw-announce mailing list on Google Groups to receive an email when FFTW is upda

You can contact the FFTW authors at fftw@fftw.org.

FFTW 3.3.7

Version 3.3.7 is the latest stable release of FFTW, and full source code is found here:

- http: fftw-3.3.7.tar.gz (ftp: fftw-3.3.7.tar.gz) (md5sum) (4.1MB)
- you can also <u>browse</u> the ftp site
- Go <u>here for Windows</u>.
- · See below for other platform-specific notes/binaries and other stuff.

See the release notes to find out what's new.

Be sure to look at the installation section of the manual.

FFTW is distributed under the GNU GPL; see the License and Copyright section of the FFTW manual

Figure 3.1. Download FFTW library

2. Extract FFTW library

```
$ tar -xvzf fftw-3.3.7.tar.gz
```

3. Compile FFTW library

```
$ cd fftw-3.3.7/
$
$ export FFTW_PATH=$PWD
$
$ ./configure --prefix=$FFTW_PATH
$
$ make CFLAGS='-fPIC'
$
$ make install
```

4. Make soft link of FFTW library

If user has a super user authority

```
$ sudo ln -s $FFTW_PATH/lib/libfftw3.a /usr/local/lib/libfftw3.a
```

If user has no super user authority, FFTW library path should be changed manually. If FFTW library (libfftw3.a) locates at /home/user/lib/libfftw3.a, the FFTW3 library path should be changed as following:

- Compile with makefile

Change the library path in config/config.mk

```
FFTW_LIB=/home/user/lib/
```

- Compile with cmake

Change the library path in ${\tt CMakeLists.txt}$

```
set(FFTW3_LIB_PATH /home/user/lib)
```

3.1.2 HDF5 Install

In version 2.0, Grid2Grid needs a HDF5 library. The installation order is the following:

1. Download HDF5 library

At the HDF5 website (https://support.hdfgroup.org/HDF5/release/cmakebuild518.html), the source code of HDF5 with cmake is available (26 March 2018)

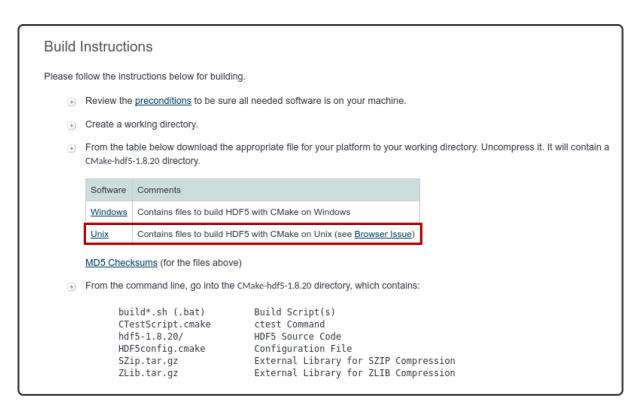


Figure 3.2. Download HDF5 source code with Cmake

2. Unzip the compressed folder

```
$ tar -xvzf CMake-hdf5-1.10.1.tar.gz
```

3. Add compiling rules in HDF5options.cmake

Open the file HDF5options.cmake inside of extracted folder and add compiling rules as following:

```
### disable packaging

#set(ADD_BUILD_OPTIONS "${ADD_BUILD_OPTIONS} -DHDF5_NO_PACKAGES:BOOL=ON
    ")

### Create install package with external libraries (szip, zlib)

set(ADD_BUILD_OPTIONS "${ADD_BUILD_OPTIONS} -DHDF5_PACKAGE_EXTLIBS:BOOL=ON")

set(ADD_BUILD_OPTIONS "${ADD_BUILD_OPTIONS} -DHDF5_BUILD_FORTRAN:BOOL=ON
    ")

set(ADD_BUILD_OPTIONS "${ADD_BUILD_OPTIONS} -DBUILD_SHARED_LIBS:BOOL=ON"
    )

set(ADD_BUILD_OPTIONS "${ADD_BUILD_OPTIONS} -DHDF5_BUILD_CPP_LIB:BOOL=ON"
    ")

#set(ADD_BUILD_OPTIONS "${ADD_BUILD_OPTIONS} -DHDF5_ENABLE_THREADSAFE:
BOOL=ON")

#set(ADD_BUILD_OPTIONS "${ADD_BUILD_OPTIONS} -DHDF5_BUILD_JAVA:BOOL=ON")

#set(ADD_BUILD_OPTIONS "${ADD_BUILD_OPTIONS} -DHDF5_BUILD_JAVA:BOOL=ON")
```

4. Compile the source code with Cmake

```
$ ctest -S HDF5config.cmake,BUILD_GENERATOR=Unix -C Release -V -O
hdf5.log
```

5. Check the compiled libraries exist in sub-directory build/bin

```
$ ls build/bin/libhdf5.a build/bin/libhdf5_fortran.a build/bin/
libszip.a build/bin/libz.a
```

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6. Make soft link of HDF5 or connect HDF5 library with Grid2Grid

If the user has a super user authority, and want to add HDF5 library on user library path :

```
export HDF5_PATH=/home/CMake-hdf5-x
$ ln -s $HDF5_PATH /usr/local/lib/hdf5
```

If the user have no super user authority, or do not want to add HDF5 library on user library path :

- Compile with makefile

Change the library path in config/config.mk

```
HDF5_LIB=/home/CMake-hdf5-x/build/bin
```

- Compile with cmake

Change the library path in CMakeLists.txt

```
set(HDF5_LIB_PATH /home/CMake-hdf5-x/build/bin)
```

3.1.3 HOS Ocean and NWT (Optional)

Grid2Grid needs the result file of HOS solver. Installation of HOS is the following:

1. Install FFTW and HDF5

See Chapters 3.1.1 and 3.1.2

2. Install makedepf90

```
$ sudo apt-get install makedepf90
```

3. Install LAPACK

```
$ sudo apt-get install liblapack-dev liblapack-doc-man liblapack-doc
liblapack-pic liblapack3 liblapack-test liblapack3gf liblapacke
liblapacke-dev
```

4. Download HOS Ocean and NWT

```
$ # Path to desired installation path
$
$ cd $HOS_INSTALLATION_PATH
$
$ git clone https://github.com/LHEEA/HOS-ocean.git
$
$ git clone https://github.com/LHEEA/HOS-NWT.git
```

5. Change the library path defined in makefile

Open makefile of HOS Ocean and NWT and change as following:

```
HDF5_INCLUDE=/usr/local/lib/hdf5/build/bin/static/
HDF5_LIB=/usr/local/lib/hdf5/build/bin/

#LINKLIB = $(LIBDIR)libfftw3.a $(LIBDIR)liblapack.a $(LIBDIR)
librefblas.a

LINKLIB = $(LIBDIR)libfftw3.a -llapack
```

```
LINKLIB+= $(HDF5_LIB)libhdf5_fortran.a $(HDF5_LIB)libhdf5_f90cstub.a $(HDF5_LIB)libhdf5.a $(HDF5_LIB)libszip.a $(HDF5_LIB)libz.a -ldl - pthread
```

The setting of FFTW3 and HDF5 library is depicted in the previous chapters

6. Comple HOS NWT and HOS Ocean

```
$ cd HOS-ocean/
$ make
$ cd ../HOS-NWT/
$ make
$ cd ..
```

7. Check executable is generated

```
$ # Check HOS NWT
$ ls HOS-NWT/bin/HOS-NWT
$
$ # Check HOS Ocean
$ ls HOS-ocean/bin/HOS-ocean
```

8. Make soft link (optional)

```
$ # Make Soft Link (Optional)
$
$ export HOS_PATH=$PWD
$
$ sudo ln -s $HOS_PATH/bin/HOS-NWT /usr/bin/HOS-NWT
$
$ sudo ln -s $HOS_PATH/bin/HOS-ocean /usr/bin/HOS-ocean
```

3.2 Grid2Grid Installation

3.2.1 Download Grid2Grid

Download Grid2Grid

```
$ # Path to desired installation path
$
$ cd $HOS_INSTALLATION_PATH
$
$ git clone https://github.com/LHEEA/Grid2Grid.git
```

Set FFTW and HDF5 library path

See chapters 3.1.1 and 3.1.2

3.2.2 Compile PostGrid2Grid with makefile

- Compile with makefile

```
$ cd Grid2Grid
$
$ make create
```

3.2.3 Compile Grid2Grid Shared Library

- Compile libGrid2Grid.so in Grid2Grid/lib/

```
$ make createlib
```

- Compile libGrid2Grid.so in \$FOAM_USER_LIBBIN

If OpenFOAM is installed, libGrid2Grid.so can be compiled at \$FOAM_USER_LIBBIN. If OpenFOAM environment is called, following make rule can be used directly.

```
$ make createOFlib
```

3.2.4 Compile with cmake

- Compile libGrid2Grid.so in lib/ and postG2G in Grid2Grid

```
$ cd Grid2Grid
$
$ cmake -H. -Bbuild
$
$ cmake --build build
```

- Compile libGrid2Grid.so in \$FOAM_USER_LIBBIN and postG2G in Grid2Grid If OpenFOAM is installed, libGrid2Grid.so can be compiled at \$FOAM_USER_LIBBIN.

```
$ cd Grid2Grid
$
$ cmake -H. -BbuildOF -DBUILD_OF_LIB=ON
$
$ cmake --build buildOF
```

4 Interface

4.1 GNU and Intel Fortran

An interface example fortran program is included in interface/fortGrid2Grid. To communicate with Grid2Grid, the fortran script modCommG2G.f90 in interface/fortGrid2Grid is needed. It is a communication module with libGrid2Grid.so. The fortran interface example program is following:

```
!! Program Start ------
Program Main
use modCommG2G    !! Use Communication Module
             ______
Implicit None
!! Variables ------
Integer,Parameter :: nChar = 300 !! Default Character Length
Character(len = nChar) :: grid2gridPath !! libGrid2Grid.so Path
Double precision :: t, dt !! Simulation Time, dt
Double precision :: x, y, z !! Computation Point
Double precision :: eta, u, v, w, pd !! HOS Wave Information
!! Dummy variables -----
integer :: it !! Dummy time loop integer
!! Program Body ---------
!!!... Write Program Start
write(*,*) "Test program (Connect to Fortran) to use Grid2Grid shared
library"
!!!... Set libGrid2Grid.so path.
!!! It is recommended to use absolute path
! grid2gridPath = "/usr/lib/libGrid2Grid.so" (if soft link is made)
grid2gridPath = "../../obj/libGrid2Grid.so"
!!!... Load libGrid2Grid.so and connect subroutines
Call callGrid2Grid(grid2gridPath)
!!!... Declare HOS Index
hosIndex = -1
```

```
!!!... Set HOS Type (Ocean or NWT)
hosSolver = "NWT"
!!!... Set HOS Result file Path
hosFileName = "modes_HOS_SWENSE.dat"
!!!... Set HOS Surf2Vol Domain and Vertical Grid
zMin = -0.6d0; zMax = 0.6d0
nZmin = 50;
                    nZmax = 50
zMinRatio = 3.d0;
                    zMaxRatio = 3.d0
!!... Initialize Grid2Grid and Get HOS Index
Call initializeGrid2Grid(hosSolver, hosFileName, zMin, zMax, nZmin,
nZmax, zMinRatio, zMaxRatio, hosIndex)
!! Time Information
t = 0.0d0; dt = 0.1d0
!! Given Point
            y = 0.5d0; z = -0.5d0
x = 0.5d0;
!! Time Loop
do it = 1,10
  !! Correct HOS Vol2VOl for given time
  Call correctGrid2Grid(hosIndex, t)
  !! Get Wave Elevation
  Call getHOSeta(hosIndex, x, y , t, eta)
 !! Get Flow Velocity
  Call getHOSU(hosIndex, x, y, z, t, u, v ,w)
 !! Get Dynamic Pressure
  Call getHOSPd(hosIndex, x, y, z, t, pd)
  !! Write Flow Information
  write(*,*) t, eta, u, v, w, pd
 !! Time Update
  t = t + dt
enddo
!! Write End of Program
write(*,*) "Test program (Connect to Fortran) is done ..."
!! -----
End Program
```

4.2 OpenFOAM

An interface example OpenFOAM program is included in interface/ofGrid2Grid. The shared library libGrid2Grid.so should be compiled at \$FOAM_USER_LIBBIN. To check libGrid2Grid.so exists at \$FOAM_USER_LIBBIN, use following shell command:

```
$ ls $FOAM_USER_LIBBIN/libGrid2Grid.so
```

If libGrid2Grid.so not exists, refer to Chapter 3.2.

To call shared library libGrid2Grid.so in \$FOAM_USER_LIBBIN, OpenFOAM compiling option is added at Make/option. Open Make/option and add following compiling option.

```
EXE_LIBS = \
...
-lgfortran \
-L$(FOAM_USER_LIBBIN) \
-lGrid2Grid
```

OpenFOAM interface example program is given next page.

```
#include "fvCFD.H"
namespace Foam
  //- Grid2Grid Initial Character Length
 const int nCharGridGrid(300);
  //- Initialize Grid2Grid Class in Fortran
  //
 11
      __modgrid2grid_MOD_initializegrid2grid
  // (
  //
         hosSolver,
  //
         hosFileName,
  //
        zMin,
  //
        zMax,
  //
        nZmin,
 //
        nZmax,
 //
        zMinRatio,
  11
        zMaxRatio,
  11
        hosIndex
  // )
  //
  //
      Input
  //
       hosSolver
                             : "NWT" or "Ocean"
 //
        hosFileName
                             : filePath of HOS mode result file
  //
                             : HOS grid zMin and zMax
        zMin, zMax
                           : HOS number of z grid
  //
        nZmin, nZmax
  //
        zMinRatio, zMaxRatio : HOS z grid max/min ratio
  //
  //
      Output
  //
                             : HOS Vol2Vol Index
        hosIndex
  //
  extern "C" void __modgrid2grid_MOD_initializegrid2grid
  const char[nCharGridGrid],
  const char[nCharGridGrid],
  const double*,
  const double*,
  const int*,
  const int*,
  const double*,
  const double*,
  int*
  );
  //- Correct Grid2Grid for given simulation Time
  //
  //
     __modgrid2grid_MOD_correctgrid2grid(hosIndex, simulTime)
  11
 // Input
```

```
// hosIndex : HOS Vol2Vol Index
//
        simulTime : Simulation Time
11
extern "C" void __modgrid2grid_MOD_correctgrid2grid
const int *,
const double *
);
//- Get HOS Wave Elevation
//
//
    __modgrid2grid_MOD_gethoseta(hosIndex, x, y, t, eta)
//
//
      Input
//
       hosIndex : HOS Vol2Vol Index
//
       x, y, t : (x and y) position and simulation Time (t)
//
//
     Output
11
        eta
                 : wave elevation
11
extern "C" void __modgrid2grid_MOD_gethoseta
const int *,
const double *,
const double *,
const double *,
double *
);
//- Get HOS Flow Velocity
//
// __modgrid2grid_MOD_gethosu(hosIndex, x, y, z, t, u, v, w)
//
//
      Input
11
       hosIndex : HOS Vol2Vol Index
11
        x, y, z, t : (x, y, z) position and simulation Time (t)
11
//
      Output
//
       u, v, w : (x, y, z) - directional flow velocity
//
extern "C" void __modgrid2grid_MOD_gethosu
const int *,
const double *,
const double *,
const double *,
const double *,
double *,
double *,
double *
);
```

```
//- Get HOS Dynamic Pressure
 //
      __modgrid2grid_MOD_gethospd(hosIndex, x, y, z, t, pd)
 11
  11
  11
       Input
         hosIndex : HOS Vol2Vol Index
  11
  //
         x, y, z, t : (x, y, z) position and simulation Time (t)
  11
  //
        Output
                 : Dynamic Pressure p = -rho*d(phi)/dt-0.5*rho*|U*U|
 //
         pd
  //
  extern "C" void __modgrid2grid_MOD_gethospd
  const int *,
  const double *,
  const double *,
  const double * ,
  const double *,
  double *
  );
  //- Get HOS Wave Elevation, Flow Velocity and Dynamic Pressure
  11
  //
      __modgrid2grid_MOD_gethosflow(hosIndex, x, y, z, t, eta, u, v, w,
  pd)
  //
  11
       Input
  //
         hosIndex : HOS Vol2Vol Index
  //
         x, y, z, t : (x, y, z) position and simulation Time (t)
  //
  //
      Output
  //
                     : wave elevation
         eta
  //
                    : (x, y, z) - directional flow velocity
         u, v, w
  //
                      : Dynamic Pressure p = -rho * d(phi)/dt - 0.5 *
         pd
  rho * |U * U|
  //
  extern "C" void __modgrid2grid_MOD_gethosflow
  const int *,
  const double *,
  const double *,
  const double * ,
  const double *,
  double *,
  double *,
  double * ,
  double *,
  double *
  );
}
```

```
// Main OpenFOAM Program Start
int main(int argc, char *argv[])
  // Write Program Start
  Info << "OpenFOAM Program Example to Call Grid2Grid (HOS Wrapper) in
   OpenFOAM" << endl;</pre>
  // Set HOS Solver Type
  const word HOSsolver_("NWT");
  const word HOSFileName_("./modes_HOS_SWENSE.dat");
  // Set File Name
  string strHOSSolver = string(HOSsolver_);
  string strHOSFileName = string(HOSFileName_);
  // Set HOS Solver Type
  const char *HOSsolver = strHOSSolver.c_str();
  // Set HOS Mode Result File Path
  const char *HOSfileName = strHOSFileName.c_str();
  // Set HOS Z Grid Information
  int indexHOS(-1);
  double zMin(-0.6), zMax(0.6);
  int nZmin(50), nZMax(50);
  double zMinRatio(3.0), zMaxRatio(3.0);
  // Initialize Grid2Grid
  __modgrid2grid_MOD_initializegrid2grid(HOSsolver, HOSfileName,
  &zMin, &zMax,
  &nZmin, &nZMax,
  &zMinRatio, &zMaxRatio, &indexHOS);
  Info << "HOS Label : " << indexHOS << endl;</pre>
  // Set Position
  double x(0.5), y(0.0), z(-0.5);
  // Define Flow Quantities
  double eta, u, v, w, pd;
  // Set Simulation Time and Time Difference
  double simulTime(0.0);
  double dt(0.1);
```

```
// Time Loop
for (int it = 0; it < 11; it++)</pre>
  // Correct Grid2Grid
  __modgrid2grid_MOD_correctgrid2grid(&indexHOS, &simulTime);
  // Get Wave Eta
  __modgrid2grid_MOD_gethoseta(&indexHOS, &x, &y, &simulTime, &eta);
  // Get Flow Velocity
  __modgrid2grid_MOD_gethosu(&indexHOS, &x, &y, &z, &simulTime, &u, &v
  , &w);
  // Get Dynamic Pressure
  __modgrid2grid_MOD_gethospd(&indexHOS, &x, &y, &z, &simulTime, &pd);
  Info << " sumulTime : " << simulTime << endl;</pre>
  Info << " eta : " << eta << endl;</pre>
  Info << " u, v, w : " << u << " " << v << " " << w << endl;
  Info << " pd
                  : " << pd << nl << endl;
  // Get whole Information
  __modgrid2grid_MOD_gethosflow(&indexHOS, &x, &y, &z, &simulTime, &
  eta, &u, &v, &w, &pd);
  Info << " eta : " << eta << endl;</pre>
  Info << " u, v, w : " << u << " " << v << " " << w << endl;
  Info << " pd
                     : " << pd << nl << endl;
  // Time Update
  simulTime+=dt;
return 0;
```

5 Validation

foamStar is used to validate Grid2Grid. foamStar is developed by Bureau Veritas and shared with Ecole Centrale de Nantes and it can simulate nonlinear waves, seakeeping problem and also hydro-elasticity problem. It solves multiphase problem with Reynolds Averaged Navier-Stokes equations (RANS) with Volume of fraction (VOF). It is based on standard multiphase solver in OpenFOAM (interDymFoam). To generate waves, foamStar uses explicit blending scheme which blends computed flow values to target values with weight function. The blending function is given as equation (5.1). Some details of foamStar are explained in Seng (2012) and Monroy et al. (2017).

$$U = (1 - w)U + wU^{target}$$
(5.1a)

$$\alpha = (1 - w)\alpha + w\alpha^{target} \tag{5.1b}$$

where

$$w = 1 - (1 - w_{base})^{\chi} \qquad \chi = \frac{\Delta U \Delta t}{\Delta x} \qquad w_{base} = -2\xi^3 + 3\xi^2$$

By using Grid2Grid, the target values at blending zone can be replaced by the wave components computed from HOS wave theory. For the validation, considered HOS simulation condition is given in Table 5.1.

Table 5.1. HOS Wave condition for validation

Wave Type	Value	HOS-Ocean		HOS-NWT	
		2D	3D	2D	3D
Regular Wave	T[s]	-	-	0.702	0.702
	H [m]	-	-	0.0431	0.0288
	T_p [s]	0.702	1.0	1.0	0.702
Irregular Waves	$H_s[\mathrm{m}]$	0.0288	0.10	0.05	0.0384
	γ [-]	3.3	3.3	3.3	3.3
Extreme Waves	T_p [s]	-	-	17.5	-
	$H_s[\mathrm{m}]$	-	-	15.5	-
	γ [-]	-	-	3.3	-

5.1 Simulation results

The wave elevation computed by using foamStar and HOS-Ocean are compared in Fig. 5.1. Small differences are observed but it is assumed to be caused by the resolution of the finite volume mesh which is not sufficient near the free surface. The VOF solver gives then those differences. Snapshots of HOS-Ocean wave fields are shown in Fig. 5.1.

The results of HOS-NWT for a two dimensional case is shown in Fig. 5.3. And a simulation snapshot is shown in Fig. 5.4. Three dimensional waves with HOS-NWT are also given in Figs. 5.5 and 5.6.

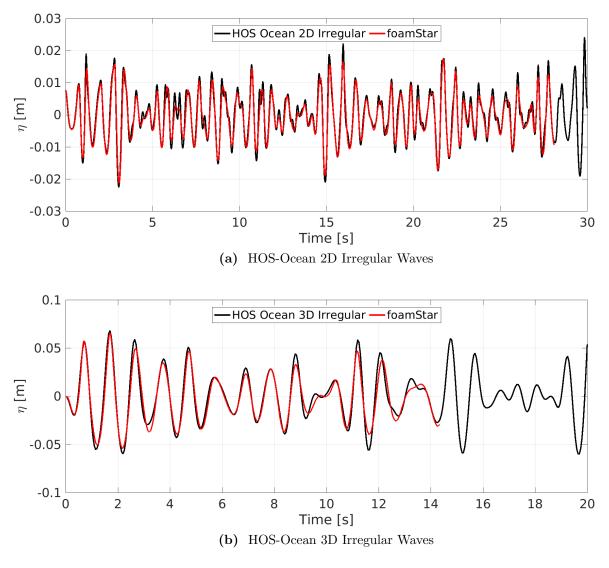
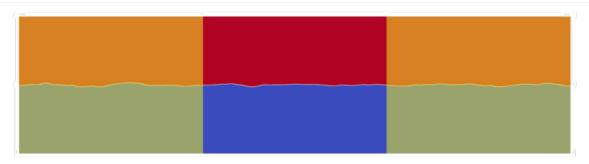


Figure 5.1. Comparison of HOS-Ocean wave elevation



(a) HOS-Ocean 2D Irregular Waves

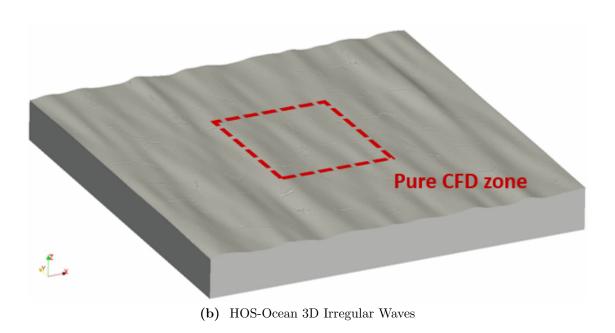


Figure 5.2. Snapshot of HOS-Ocean wave fields by foamStar

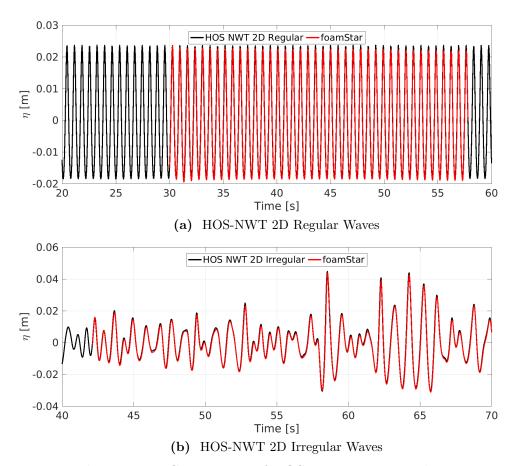


Figure 5.3. Comparison of HOS-NWT 2D wave elevation

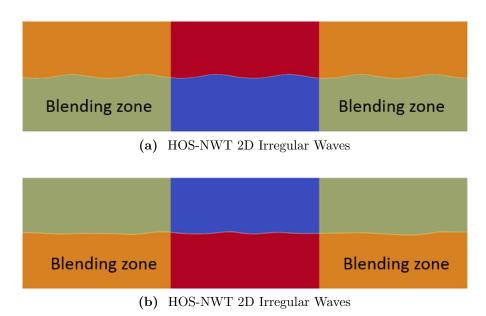


Figure 5.4. Snapshot of HOS-NWT 2D wave fields by foamStar

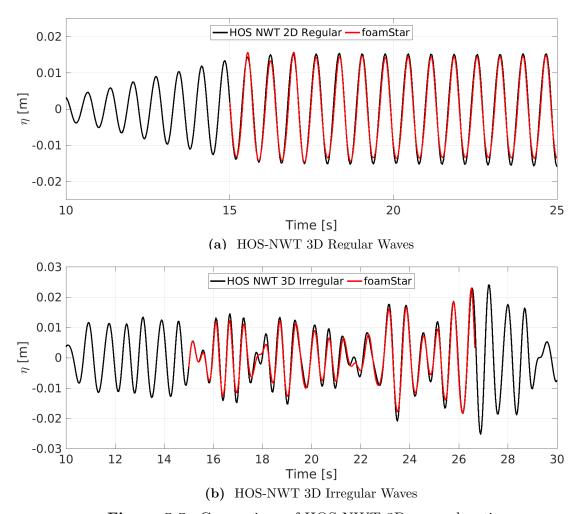


Figure 5.5. Comparison of HOS-NWT 3D wave elevation

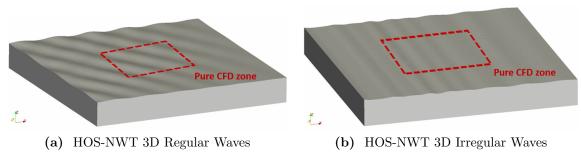


Figure 5.6. Snapshot of HOS-NWT 3D wave fields by foamStar

Simulation of extreme waves (1000 year return period waves in Gulf of Mexico(GOM) (Condition: $H_s = 17.5m, T_p = 15.5s, \gamma = 3.3$) is simulated with HOS-NWT for 2D cases and used to generate waves in foamStar. The waves are compared with experiments performed in the wave basin of Ecole Centrale de Nantes (ECN). To simulate nonlinear breaking waves, the wave breaking model in HOS is utilized and allows also to capture when wave breaking occur. The expected wave breaking events are shown in Fig. 5.7. In the experiments, wave breaking is observed at the expected position and time by HOS wave theory. The breaking moment in the experiment is shown in Fig. 5.8. The time series of wave elevation measured in the experiments are compared with the results of simulation using Grid2Grid in Fig 5.9. The simulation snapshot when wave breaking occur is shown in Fig. 5.10. The small disturbance at the wave front is observed.

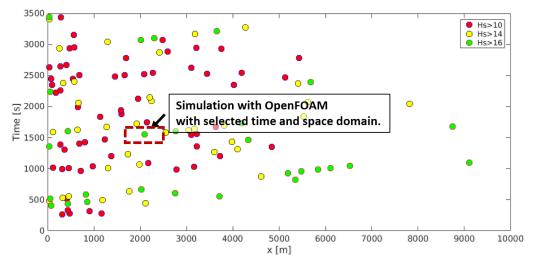


Figure 5.7. Expected wave breaking by HOS

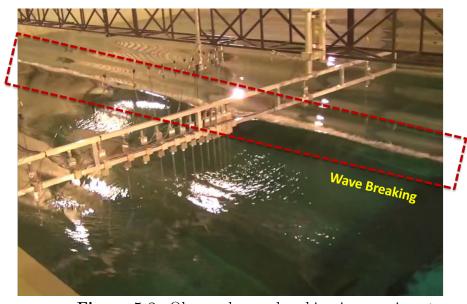
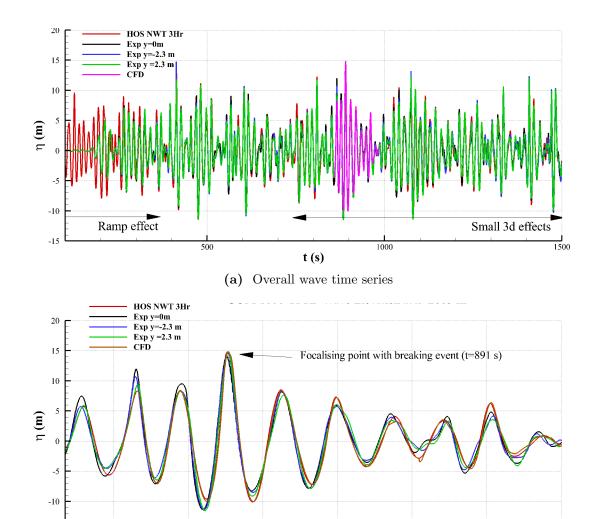


Figure 5.8. Observed wave breaking in experiment



(b) Wave elevation at the wave breaking moment

t (s) 920

940

960

Figure 5.9. Snapshot of HOS-NWT 3D wave fields by foamStar

900

-15

860

880

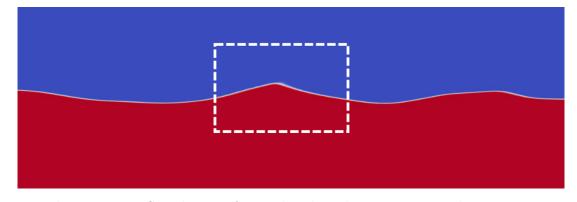


Figure 5.10. Simulation of wave breaking by foamStar and Grid2Grid

6 Summary

HOS wrapper program called **Grid2Grid** is developed for the nonlinear wave simulation of numerical solvers. Most of data and functionality is encapsuled as a class to be easily used and maintained. **Grid2Grid** generates dynamic linked library as an independent package to be called and easily used in other languages.

The post processing of HOS is also possible by using Grid2Grid. Included post processing program is called postGrid2Grid. The usage is explained in Chapter 2.4.

Grid2Grid is validated by using the code foamStar based on standard multiphase solver of OpenFOAM and also with an experiment. In the experiment, waves corresponding to 1000 year return period in Gulf of Mexico are generated. The wave elevation is measured at the wave breaking position expected by HOS wave theory and compared with the results of the simulation. Good agreement is shown between the measurement and the numerical solutions and the nonlinear wave phenomenon is observed both in experiment and in simulation.

In this document, the <code>Grid2Grid</code> program architecture, class and module structure, principle class data and functionality are explained to understand the feature of <code>Grid2Grid</code> and to be easily applied to numerical solvers. The interface examples with other programming languages are given as a source code and also in <code>Grid2Grid</code> package.

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