

```

1- a) void imprime (int *v, int n) {
    if (n != 0)
        cout << v[n-1] << " ";
    imprime(v, n-1);
}

```

Relação de
recorrência

$$\Rightarrow T(n) = T(n-1) + 2$$

Resolução por interação

$$T(n) = T(n-1) + 2$$

$$T(n-1) = T(n-2) + 2 + 2$$

$$T(n-2) = T(n-3) + 2 + 2 + 2$$

⋮

$$T(n) = T(n-h) + h \cdot 2$$

$$\rightarrow T(1) = T(n-h)$$

$$h = n-1$$

$$T(n-(n-1)) + (n-1) \cdot 2 =$$

$$T(1) + 2n-2 =$$

$$2 + 2n-2 =$$

$$2n \text{ ou } n.c$$

$$\text{Logo, } T(n) \in \Theta(n)$$

2- a) $T(n) = 3T(n/3) + n$

$h=0$	$T(n)$	$\rightarrow n = n \leftarrow 0$
$h=1$	$T(n/3) \quad T(n/3) \quad T(n/3)$	$\rightarrow 3(n/3) = n \leftarrow 1$
$h=2$	$T(n/3^2) \dots$	$\rightarrow 9(n/9) = n \leftarrow 2$
\vdots		
$h=n$	$T(n/3^n)$	$\rightarrow 3^h(n/3^h) = n \leftarrow h$

$T(n/3^h) = T(1)$
 $n = 3^h$
 $\log_3 n = h$

$h \cdot n = n \cdot \log_3 n$
 $= n \cdot \log n$

$\log_3 T(n) \in \Theta(n \log n)$

b) $T(n) = 3T(n/3) + 1$

$T(n) = 3^1 T(n/3^1) + 3^1 \cdot 1$
 $3^2 T(n/3^2) + 3^2 \cdot 1$
 $3^3 T(n/3^3) + 3^3 \cdot 1$
 \vdots
 $3^k T(n/3^k) + 3^k$

$\rightarrow T(n/3^k) = T(1)$
 $n = 3^k$
 $\log_3 n = k$

Assum

$$3^k (n/3^k) + \sum_{i=0}^k 3^i \rightarrow 3^{\log_3 n} (n/3^{\log_3 n}) + \frac{1(3^{\log_3 n} - 1)}{3-1}$$

$= n + \frac{n-1}{2} = \frac{3n-1}{2}$
 $\log_3 T(n) \in \Theta(n)$

3. insert N \rightarrow hash = 1

insert I \rightarrow hash = 4

insert O \rightarrow hash = 2

insert V \rightarrow hash = 9

insert Z \rightarrow hash = 0

insert A \rightarrow hash = 12

insert P \rightarrow hash = 3

insert K \rightarrow hash = 2

insert R \rightarrow hash = 5

insert Q \rightarrow hash = 4

insert S \rightarrow hash = 6

