# Robustness against rendezvous

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CCS Concepts: • Software and its engineering → General programming languages;

Additional Key Words and Phrases: Concurrency, Serializability

#### **ACM Reference format:**

Anonymous Author(s). 2017. Robustness against rendezvous. *Proc. ACM Program. Lang.* 1, 1, Article 1 (January 2017), 5 pages.

https://doi.org/10.1145/nnnnnnnnnnnnn

#### 1 INTRODUCTION

#### 2 OVERVIEW

#### 3 MESSAGE PASSING SYSTEMS

We fix arbitrary sets  $\mathbb{P}$  and  $\mathbb{V}$  of process ids and message payloads. For given sets  $\mathbb{P}$  and  $\mathbb{V}$ , we fix the sets

$$S = \{ \operatorname{send}(p, q, v) : p, q \in \mathbb{P}, v \in \mathbb{V} \}, \text{ and } R = \{ \operatorname{rec}(q, v) : q \in \mathbb{P}, v \in \mathbb{V} \}$$

of *send actions* and *receive actions*. Each send action  $\operatorname{send}(p,q,v)$  combines two process ids  $p,q\in\mathbb{P}$  denoting the sender and the receiver of the message, respectively, and a message payload  $v\in\mathbb{V}$ . Receive actions specify the process  $q\in\mathbb{P}$  receiving the message, and the message payload  $v\in\mathbb{V}$ . We write  $\operatorname{send}(p,q,\_)$  and  $\operatorname{rec}(q,\_)$  when the message payload is unconstrained. We denote the process executing a  $\operatorname{send}/\operatorname{receive}$  action  $a\in S\cup R$  by  $\operatorname{proc}(a)$ , i.e.,  $\operatorname{proc}(a)=p$  for every  $a=\operatorname{send}(p,q,v)$ , and  $\operatorname{proc}(a)=q$  for every  $a=\operatorname{rec}(q,v)$ , and the destination of a  $\operatorname{send}$  action  $s\in S$  by  $\operatorname{dest}(s)$ , i.e.,  $\operatorname{dest}(\operatorname{send}(p,q,v))=q$ .

A message passing system consists of a finite set of processes that communicate via messages. Each process is described as a state machine that evolves by executing send or receive actions, or local actions (specified as  $\epsilon$  transitions) and it is equipped with an instance of some fixed collection data type, e.g., FIFO queue, that acts as a message buffer (storing incoming messages before being received).

Formally, a *message passing system* is a tuple  $A = (L, \delta, l_0, \mathbb{T})$  where L is a set of local process states,  $\delta \subseteq L \times (S \cup R \cup \{\epsilon\}) \times L$  is a transition relation describing the evolution of all processes,  $l_0$  is the initial state of every process, and  $\mathbb{T}$  is a collection data type with interface add(m) for adding an element m to the collection and rem() that removes and returns an element from the collection (this method returns only when the collection is non-empty, otherwise it blocks).

A configuration  $c = \langle \vec{l}, \vec{b} \rangle$  is a vector of local states  $\vec{l}$  together with a vector of message buffers  $\vec{b}$  that are instances of the collection data type  $\mathbb{T}$ . These two vectors are indexed by elements of  $\mathbb{P}$ . For a vector  $\vec{x}$ , let  $\vec{x}_p$  denote the element of  $\vec{x}$  of index p. The state of the process p is defined by the local state  $\vec{l}_p$  and the message buffer  $\vec{b}_p$ .

We fix an arbitrary set M of message identifiers, and the sets

$$S_{id} = \{s_i : s \in S, i \in M\} \text{ and } R_{id} = \{r_i : r \in R, i \in M\}$$

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Fig. 1. The asynchronous semantics of a message passing system A. Above,  $\vec{l}[\vec{l}_p \leftarrow l]$  denotes an update of  $\vec{l}$  where the element of index p is replaced by l. Also,  $\vec{b}[\vec{b}_q]$ . add(m) denotes the vector of message buffers obtained from  $\vec{b}$  by calling the method add(m) of the element of index q.

of indexed actions; an indexed action combines a send/receive action with a message identifier  $i \in \mathbb{M}$ . Message identifiers are used to pair send and receive actions. We denote the message id of an indexed send/receive action a by  $\mathsf{msg}(a)$ . Indexed send and receive actions  $s \in S_{id}$  and  $r \in R_{id}$  are  $\mathsf{matching}$ , written  $s \vdash r$ , when  $\mathsf{msg}(s) = \mathsf{msg}(r)$ . For notational convenience, we often associate  $\mathbb{M}$  with  $\mathbb{N}$ , e.g., writing  $\mathsf{send}_1(p,q,v)$  and  $\mathsf{rec}_2(q',v')$  in place of  $\mathsf{send}_{i_1}(p,q,v)$  and  $\mathsf{rec}_{i_2}(q',v')$ .

The transition relation  $\rightarrow$  in Figure 1 is determined by a message passing system A, and maps a configuration  $c_1$  to another configuration  $c_2$  and indexed action  $a \in S_{id} \cup R_{id}$  or  $\epsilon$ . Send transitions ... RECEIVE transitions ... LOCAL transitions TODO FILL IN

An *execution* of a system A under the asynchronous semantics to configuration  $c_n$  is a configuration sequence  $c_0c_1\ldots c_n$  such that  $c_m\xrightarrow{a_{m+1}}c_{m+1}$  for  $0\leq m< n$ . We call the sequence  $a_1\ldots a_n$  the *trace* of  $c_0c_1\ldots c_n$  and we say that  $c_n$  is reachable in A under the asynchronous semantics, with trace  $a_1\ldots a_n$ . The *reachable local state vectors* of A, denoted Asynch-States(A), is the set of local state vectors in reachable configurations. The set of traces of A under the asynchronous semantics is denoted by AsynchTr(A).

Given a trace t, a send action s in t is called an *unmatched send* when t contains no receive action r with  $s \mapsto r$ . A trace t is called *matched* when it contains no unmatched send.

### **4 SYNCHRONIZABILITY**

 We define a notion of robustness, called *synchronizability*, which ensures that even if the system uses buffers to store messages it provides the illusion that messages are received instantaneously, as in a synchronous (rendez-vous) semantics. This is analogous to the atomicity criterion for concurrent shared-memory systems, where even though transactions can interleave, every execution is "equivalent" to an execution where transactions happen atomically without interference.

We define a conflict relation  $\prec$  on actions in  $S_{id} \cup R_{id}$  that relates every two actions of the same process and every send with the matching receive. Formally,

$$a < a'$$
 iff  $proc(a) = proc(a')$  or  $a \mapsto a'$ 

A permutation t' of a trace t is *conflict-preserving* when every pair a and a' of actions of t appear in the same order in t' whenever a < a'. From now on, whenever we use the term permutation we mean conflict-preserving permutation. Intuitively, a message passing system can not distinguish between two traces, one being a conflict-preserving permutation of the other.

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$$\begin{split} & \underbrace{l \in \delta(\vec{l}_p, \operatorname{send}(p, q, \upsilon)) \neq \emptyset}_{\substack{\vec{l}, \vec{b} \xrightarrow{\operatorname{send}(p, q, \upsilon)}} \stackrel{\text{EDCAL}}{\vec{l} \in \delta(\vec{l}_p, \operatorname{send}(v))} \underbrace{l \in \delta(\vec{l}_p, \varepsilon) \neq \emptyset}_{\substack{\vec{l}, \vec{b} \xrightarrow{\epsilon} \vec{l} [\vec{l}_p \leftarrow l], \vec{b} \in \mathcal{I}, \vec{b} \xrightarrow{\epsilon} \vec{l} [\vec{l}_p \leftarrow l], \vec{b}}_{\substack{\vec{l}, \vec{b} \xrightarrow{\epsilon} \vec{l} \in \mathcal{I}, \vec{b} \xrightarrow{\epsilon} \vec{l} = 0}} \underbrace{l \in \delta(\vec{l}_p, \varepsilon) \neq \emptyset}_{\substack{\vec{l}, \vec{b} \xrightarrow{\epsilon} \vec{l} \in \mathcal{I}, \vec{b} \xrightarrow{\epsilon} \vec{l} = 0}} \underbrace{l \in \delta(\vec{l}_p, \varepsilon) \neq \emptyset}_{\substack{\vec{l}, \vec{b} \xrightarrow{\epsilon} \vec{l} \in \mathcal{I}, \vec{b} \xrightarrow{\epsilon} \vec{l} = 0}} \underbrace{l \in \delta(\vec{l}_p, \varepsilon) \neq \emptyset}_{\substack{\vec{l}, \vec{b} \xrightarrow{\epsilon} \vec{l} \in \mathcal{I}, \vec{b} \xrightarrow{\epsilon} \vec{l} = 0}} \underbrace{l \in \delta(\vec{l}_p, \varepsilon) \neq \emptyset}_{\substack{\vec{l}, \vec{b} \xrightarrow{\epsilon} \vec{l} \in \mathcal{I}, \vec{b} \xrightarrow{\epsilon} \vec{l} = 0}} \underbrace{l \in \delta(\vec{l}_p, \varepsilon) \neq \emptyset}_{\substack{\vec{l}, \vec{b} \xrightarrow{\epsilon} \vec{l} \in \mathcal{I}, \vec{b} \xrightarrow{\epsilon} \vec{l} = 0}} \underbrace{l \in \delta(\vec{l}_p, \varepsilon) \neq \emptyset}_{\substack{\vec{l}, \vec{b} \xrightarrow{\epsilon} \vec{l} \in \mathcal{I}, \vec{b} \xrightarrow{\epsilon} \vec{l} = 0}} \underbrace{l \in \delta(\vec{l}_p, \varepsilon) \neq \emptyset}_{\substack{\vec{l}, \vec{b} \xrightarrow{\epsilon} \vec{l} \in \mathcal{I}, \vec{b} \xrightarrow{\epsilon} \vec{l} = 0}} \underbrace{l \in \delta(\vec{l}_p, \varepsilon) \neq \emptyset}_{\substack{\vec{l}, \vec{b} \xrightarrow{\epsilon} \vec{l} \in \mathcal{I}, \vec{b} \xrightarrow{\epsilon} \vec{l} = 0}} \underbrace{l \in \delta(\vec{l}_p, \varepsilon) \neq \emptyset}_{\substack{\vec{l}, \vec{b} \xrightarrow{\epsilon} \vec{l} \in \mathcal{I}, \vec{b} \xrightarrow{\epsilon} \vec{l} = 0}} \underbrace{l \in \delta(\vec{l}_p, \varepsilon) \neq \emptyset}_{\substack{\vec{l}, \vec{b} \xrightarrow{\epsilon} \vec{l} \in \mathcal{I}, \vec{b} \xrightarrow{\epsilon} \vec{l} = 0}} \underbrace{l \in \delta(\vec{l}_p, \varepsilon) \neq \emptyset}_{\substack{\vec{l}, \vec{b} \xrightarrow{\epsilon} \vec{l} = 0}} \underbrace{l \in \delta(\vec{l}_p, \varepsilon) \neq \emptyset}_{\substack{\vec{l}, \vec{b} \xrightarrow{\epsilon} \vec{l} = 0}} \underbrace{l \in \delta(\vec{l}_p, \varepsilon) \neq \emptyset}_{\substack{\vec{l}, \vec{b} \xrightarrow{\epsilon} \vec{l} = 0}} \underbrace{l \in \delta(\vec{l}_p, \varepsilon) \neq \emptyset}_{\substack{\vec{l}, \vec{b} \xrightarrow{\epsilon} \vec{l} = 0}} \underbrace{l \in \delta(\vec{l}_p, \varepsilon) \neq \emptyset}_{\substack{\vec{l}, \vec{b} \xrightarrow{\epsilon} \vec{l} = 0}} \underbrace{l \in \delta(\vec{l}_p, \varepsilon) \neq \emptyset}_{\substack{\vec{l}, \vec{b} \xrightarrow{\epsilon} \vec{l} = 0}} \underbrace{l \in \delta(\vec{l}_p, \varepsilon) \neq \emptyset}_{\substack{\vec{l}, \vec{b} \xrightarrow{\epsilon} \vec{l} = 0}} \underbrace{l \in \delta(\vec{l}_p, \varepsilon) \neq \emptyset}_{\substack{\vec{l}, \vec{b} \xrightarrow{\epsilon} \vec{l} = 0}} \underbrace{l \in \delta(\vec{l}_p, \varepsilon) \neq \emptyset}_{\substack{\vec{l}, \vec{b} \xrightarrow{\epsilon} \vec{l} = 0}} \underbrace{l \in \delta(\vec{l}_p, \varepsilon) \neq \emptyset}_{\substack{\vec{l}, \vec{b} \xrightarrow{\epsilon} \vec{l} = 0}} \underbrace{l \in \delta(\vec{l}_p, \varepsilon) \neq \emptyset}_{\substack{\vec{l}, \vec{b} \xrightarrow{\epsilon} \vec{l} = 0}} \underbrace{l \in \delta(\vec{l}_p, \varepsilon) \neq \emptyset}_{\substack{\vec{l}, \vec{b} \xrightarrow{\epsilon} \vec{l} = 0}} \underbrace{l \in \delta(\vec{l}_p, \varepsilon) \neq \emptyset}_{\substack{\vec{l}, \vec{b} \xrightarrow{\epsilon} \vec{l} = 0}} \underbrace{l \in \delta(\vec{l}_p, \varepsilon) \neq \emptyset}_{\substack{\vec{l}, \vec{b} \xrightarrow{\epsilon} \vec{l} = 0}} \underbrace{l \in \delta(\vec{l}_p, \varepsilon) \neq \emptyset}_{\substack{\vec{l}, \vec{b} \xrightarrow{\epsilon} \vec{l} = 0}} \underbrace{l \in \delta(\vec{l}_p, \varepsilon) \neq \emptyset}_{\substack{\vec{l}, \vec{b} \xrightarrow{\epsilon} \vec{l} = 0}} \underbrace{l \in \delta(\vec{l}_p, \varepsilon) \neq \emptyset}_{\substack{\vec{l}, \vec{b} \xrightarrow{\epsilon} \vec{l} = 0}} \underbrace{l \in \delta(\vec{l}_p, \varepsilon) \neq \emptyset}_{\substack{\vec{l}, \vec{b} \xrightarrow{\epsilon} \vec{l} = 0}} \underbrace{l \in \delta(\vec{l}_p, \varepsilon)}$$

Fig. 2. The synchronous semantics of a message passing system A. The predicate empty( $\vec{b}_j$ ) denotes the fact that the buffer  $\vec{b}_i$  is empty, i.e,  $\vec{b}_i$ . rem() is not enabled.

## Example 4.1. The following traces

$$\operatorname{send}_1(p_1, q, \_) \operatorname{send}_2(p_2, q, \_) \operatorname{rec}_1(q, \_) \operatorname{rec}_2(q, \_)$$
  
 $\operatorname{send}_1(p_1, q_1, \_) \operatorname{send}_2(p_2, q_2, \_) \operatorname{rec}_2(q_2, \_) \operatorname{rec}_1(q_1, \_)$ 

have the following conflict-preserving permutations, respectively:

$$\operatorname{send}_1(p_1, q_1, \_) \operatorname{rec}_1(q, \_) \operatorname{send}_2(p_2, q, \_) \operatorname{rec}_2(q, \_)$$
  
 $\operatorname{send}_1(p_1, q_1, \_) \operatorname{rec}_1(q_1, \_) \operatorname{send}_2(p_2, q_2, \_) \operatorname{rec}_2(q_2, \_)$ 

LEMMA 4.2. For a given trace t, AsynchTr(A) contains every conflict-preserving permutation t' of t when  $t \in Asynch<math>Tr(A)$ .

A trace t is called *synchronous* when every send  $s \in S_{id}$  is immediately followed by the matching receive. Formally, for every  $0 \le k < |t| - 1$ , if  $t_k \in S_{id}$  then  $t_{k+1} \in R_{id}$  and  $t_k \mapsto t_{k+1}$ .

Informally, a trace t is called *synchronizable* when there exists a conflict-preserving permutation of t which is synchronous. The presence of unmatched send actions introduces a subtlety: a trace is considered synchronizable by supposing that every message is eventually received. To account for this, we define a *completion* of a trace t to be any sequence  $t \cdot t'$  where t' contains only receive actions that match one of the unmatched send actions in t.

Definition 4.3. A trace t is called *synchronizable* when there exists a synchronous conflict-preserving permutation of a completion of t.

Example 4.4. The traces in Example 4.1 are synchronizable while the following are not:

$$\begin{split} \operatorname{send}_1(p,q,\_) & \operatorname{send}_2(p,q,\_) \operatorname{rec}_2(q,\_) \operatorname{rec}_1(q,\_) \\ \operatorname{send}_1(p,q,\_) & \operatorname{send}_2(q,p,\_) \operatorname{rec}_2(p,\_) \operatorname{rec}_1(q,\_) \\ \operatorname{send}_1(p,q,\_) & \operatorname{send}_2(q,p,\_) \end{split}$$

The latter trace demonstrates the use of completions in defining synchronizability: none of its completions, i.e., one of the first two traces, cannot be permuted to a synchronous trace.

A message passing system A is synchronizable when every trace  $t \in A$ synchTr(A) is synchronizable.

The transition relation  $\Rightarrow$  in Figure 1 defines a new semantics for a message passing system A where a receive action of a process q is enabled only if the buffers of all the other processes are empty and the buffer of process q contains exactly one message. Executions and reachable local state vectors under the new semantics, denoted by Synch-States(A), are defined as in Section 3. The set of traces of A under the new semantics is denoted by Synch-Tr(A).

TODO DESCRIBE TRANSITIONS

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Lemma 4.5. The synchronous semantics of a message passing system A admits every synchronous trace of A under the asynchronous semantics.

TODO DEFINE THE CONDITION XXX THAT EVERY MESSAGE IS EVENTUALLY RECEIVED

LEMMA 4.6. For a given synchronizable XXX message passing system A, Asynch-States(A) = Synch-States(A).

Proof. TODO

#### 5 MONITORING SYNCHRONIZABILITY

 Checking that a given trace is synchronizable can be done by tracking a "conflict-graph" like in conflict serializability [] to show that every pair of matching send and receive actions can be executed atomically. Roughly, the nodes of this graph correspond to such pairs of matching actions, and the edges to conflicts between actions from one pair and another. Then, a trace is synchronizable iff the conflict-graph is acyclic. Dealing with unmatched sends and completions poses a technical difficulty since the conflict-graph should contain enough additional edges to anticipate for the possible completions.

Before defining conflict-graphs, we define a notion of action-graph that represents the order between all conflicting actions in some given trace.

Definition 5.1 (Action-Graph). The action-graph of a trace t is the directed graph  $G_t = \langle V, E \rangle$  where there is a node in V for each action in t, and E contains an edge from u to v iff act(u) < act(v) and act(u) occurs before act(v) in t (where act(v) is the action of trace t corresponding to the graph node v).

For two actions a and a' in a trace t,  $a \rightsquigarrow a'$  denotes the fact that  $G_t$  contains a path from the node representing a to that representing a'.

LEMMA 5.2. The action-graph of a trace is acyclic.

Definition 5.3 (Conflict-Graph). The conflict-graph of a trace t is the directed graph  $CG_t = \langle V', E' \rangle$  where V' includes one node for each pair of matching send and receive actions, and each unmatched send action in t, and we have  $(v, v') \in E'$  iff one of the following holds

- (1) there exist actions  $a \in \operatorname{act}(v)$  and  $a' \in \operatorname{act}(v')$  such that  $(a, a') \in E$  where  $G_t = (V, E)$  is the action-graph of t (and  $\operatorname{act}(v)$  is the set of actions of trace t corresponding to the graph node v), or
- (2) act(v) contains a send action  $s_1$  and act(v') contains an unmatched send action  $s_2$  such that  $dest(s_1) = dest(s_2)$ ,
- (3) act(v) contains an action a and act(v') contains an unmatched send action  $s_1$  with  $proc(a) = dest(s_1)$ .

The second and the third item above apply to unmatched traces and they represent conflicts occurring in specific completions. TODO GIVE A HINT. Before discussing these completions, a direct consequence of previous results on conflict serializability [] is that a matched trace is synchronizable whenever its conflict-graph is acyclic.

LEMMA 5.4. A matched trace is synchronizable iff its conflict-graph is acyclic.

We consider a notion of *canonical* completion where intuitively, the order between the receive actions added by the completion is consistent with the order of the send actions in t. Formally, a *completion*  $t \cdot t'$  of a trace t is called canonical when for every two unmatched send actions  $\operatorname{send}_1(p_1,q_1,\_)$  and  $\operatorname{send}_2(p_2,q_2,\_)$  occurring in this order in t, the suffix t' contains  $\operatorname{rec}_1(q_1,\_)$  before  $\operatorname{rec}_2(q_2,\_)$ .

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LEMMA 5.5. A trace t is synchronizable iff the canonical completion of t is synchronizable.

PROOF. The "if" direction is trivial. For the reverse, let t be a synchronizable trace. Therefore, there exists a completion  $t \cdot t'$  which is synchronizable. If  $t \cdot t'$  is canonical, then the proof is finished. Otherwise, let  $\operatorname{send}_1(p_1,q_1,\_)$  and  $\operatorname{send}_2(p_2,q_2,\_)$  be two unmatched send actions occurring in this order in t such that  $\operatorname{rec}_2(q_2,\_)$  occurs before  $\operatorname{rec}_1(q_1,\_)$  in t'. W.l.o.g., we assume that there is no other action of  $q_1$  or  $q_2$  in between  $\operatorname{rec}_2(q_2,\_)$  and  $\operatorname{rec}_1(q_1,\_)$ . Otherwise, for instance, if there is an action  $\operatorname{rec}_3(q_2,\_)$  in between  $\operatorname{rec}_2(q_2,\_)$  and  $\operatorname{rec}_1(q_1,\_)$ , then either  $\operatorname{send}_2(p_2,q_2,\_)$  occurs before  $\operatorname{send}_3(p_3,q_2,\_)$  (for some  $p_3$ ) and we can choose  $\operatorname{send}_1(p_1,q_1,\_)$  and  $\operatorname{send}_3(p_3,q_2,\_)$  satisfying this property, or  $\operatorname{send}_3(p_3,q_2,\_)$  occurs before  $\operatorname{send}_2(p_2,q_2,\_)$  and we can choose  $\operatorname{send}_2(p_2,q_2,\_)$  and  $\operatorname{send}_3(p_3,q_2,\_)$  satisfying this property.

Note that, since  $\operatorname{send}_1(p_1, q_1, \_)$  occurs before  $\operatorname{send}_2(p_2, q_2, \_)$ , it is impossible that  $\operatorname{send}_2(p_2, q_2, \_) \sim \operatorname{send}_1(p_1, q_1, \_)$ . By Lemma 5.4, the conflict graph of  $t \cdot t'$  is acyclic. Let  $t \cdot t''$  be a permutation of  $t \cdot t'$  where  $\operatorname{rec}_2(q_2, \_)$  and  $\operatorname{rec}_1(q_1, \_)$  are swapped (i.e.,  $\operatorname{rec}_1(q_1, \_)$  occurs before  $\operatorname{rec}_2(q_2, \_)$ ). If  $q_1 \neq q_2$ , then this permutation is conflict-preserving and the conflict graph of  $t \cdot t''$  is the same as the one of  $t \cdot t'$ . Now, assume that  $q_1 = q_2$ . Then, the conflict-graph of  $t \cdot t''$  is the conflict-graph of  $t \cdot t'$  where the edge from the node u representing  $\{\operatorname{send}_2(p_2, q_2, \_), \operatorname{rec}_2(q_2, \_)\}$  to the node v representing  $\{\operatorname{send}_1(p_1, q_1, \_), \operatorname{rec}_1(q_1, \_)\}$  is replaced with an edge from v to u. Since the conflict-graph of  $t \cdot t'$  is acyclic, the action graph of  $t \cdot t'$  contains no path from  $\operatorname{send}_1(p_1, q_1, \_)$  to  $\operatorname{send}_2(p_2, q_2, \_)$  (otherwise, this path together with the edge from  $\operatorname{rec}_2(q_2, \_)$  to  $\operatorname{rec}_1(q_1, \_)$  will induce a conflict-graph cycle). Therefore, the only path in  $CG_{t \cdot t'}$  between u and v is the single-edge path from v to v, and changing the direction of this edge will result in a graph that remains acyclic. Consequently, the conflict-graph of  $t \cdot t''$  is acyclic. Applying this reasoning further for every pair of unmatched send operations in v shows that the canonical completion of v is synchronizable. v

The second and the third item in Definition 5.3 represent conflicts occurring in canonical completions of the trace t.

LEMMA 5.6. For every trace t,  $CG_t$  is isomorphic to  $CG_{t'}$  where t' is the canonical completion of t.

The following is a direct consequence of Lemmas 5.5 and 5.6.

Theorem 5.7. A trace t is synchronizable iff  $CG_t$  is acyclic.

Theorem 5.7 can be used to define a runtime monitor checking for synchronizability. The monitor maintains the conflict-graph of the trace produced by the message passing system and checks whether it contains some cycle. While this approach requires dealing with the complexity of the asynchronous semantics (the unbounded message buffers), the next section shows that this is not necessary. Synchronizability violations, if any, can be exposed by executing the system under the *synchronous* semantics.