



LORDS INSTITUTE OF ENGINEERING AND TECHNOLOGY

(UGC AUTONOMOUS)

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B.E, I- PRE-FINAL EXAM

MATHEMATICS-I

(Common for CSE/CSD/CIVIL/MECH)

Course

Code:

U23MA101

Time: 3 Hours

Max. Marks: 60

Instructions to the Students:

- Question No. 1 is compulsory

- Answer any 4 questions from Q.No.2 -Q. No7

1. a. Show that the Series $1 - \frac{1}{2^2} + \frac{1}{3^2} - \frac{1}{4^2} + \dots$ is absolutely convergent. [2] CO1 BTL2
- b. Write the Taylors series expansion of $f(x) = e^x$ about $x=1$. [2] CO3 BTL1
- c. Find $\frac{dw}{dt}$ if $w = x^2 + y^2, x = \cos^2 t, y = \sin^2 t$ at $t = \frac{\pi}{4}$ [2] CO4 BTL4
- d. Evaluate $\int_0^1 \int_x^{\sqrt{x}} (x^2 + y^2) dy dx$ [2] CO5 BTL5
- e. State Green's theorem on a plane. [2] CO6 BTL1
- f. Test the Convergence of the Series $\sum_{n=1}^{\infty} \frac{\sqrt{n}}{n^2 + 1}$ [2] CO1 BTL2
2. a. State Logarithmic Test [12] CO1 BTL1
- b. Test the Convergence of the Series, $\frac{1}{2} + \left[\frac{2}{3}\right]x + \left[\frac{3}{4}\right]x^2 + \left[\frac{4}{5}\right]x^3 + \dots, x > 0$. CO2 BTL4
3. a. Prove using Mean value theorem $|\sin u - \sin v| \leq |u - v|$ [12] CC3 BTL4
- b. Show that the evolute of the cycloid $x=a(1-\sin\theta), y=a(1-\cos\theta)$ is another cycloid CO3 BTL4
- a. Examine for maximum and minimum values of the function $f(x, y) = x^2 - 3xy + y^2 + 2x$ [12] CO4 BTL4
- b. Find the minimum value of $x^2 + y^2 + z^2$ with the constraint $x + y + z = 3a$. CO4 BTL5
5. a. Evaluate $\int \int e^{2x+3y} dx dy$ over the triangle bounded by $x=0, y=0, x+y=1$. [12] CO4 BTL5
- b. Evaluate $\int_0^{4a} \int_{\frac{x^2}{4a}}^{2\sqrt{ax}} dy dx$ by changing the order of integration. CO4 BTL5
6. a. Evaluate $\oint_C x dy - y dx$ where C is the triangle with vertices $(0,0), (2,0)$ and $(0,1)$ using Greens theorem. [12] CO3 BTL4
- b. Find the Directional Derivative of $f(x, y, z) = x^2 - y^2 + 2z^2$ at the point $P(1,2,3)$ in the direction of the line PQ where Q is the point $(5,0,4)$. CO3 BTL5
- Verify Gauss divergence theorem for $F = (x^3 - yz) i - 2x^2 y j + z k$ taken over the surface of the cube bounded by the planes $x=y=z=a$ and coordinate planes. [12] CO6 BTL4