

① function  $x = f(n)$

$x = 1;$

for  $i = 1:n$

for  $j = 1:n$

$x = x + 1;$

\* The line  $x = x + 1;$  runs for

$$\sum_{i=1}^n \sum_{j=1}^{n+1} 1$$

\* The line for  $j = 1:n$  runs for

$$\sum_{i=1}^n \sum_{j=1}^{n+1} 1$$

Time Complexity  $T(n) = n^2 + n + n^2 + 1 + n + 1$

$$\Rightarrow 3n^2 + 3n + 2$$

where The highest degree polynomial is

$(n^2)$  so runtime is  $O(n^2)$

③ The find polynomials that are upper bound, lower bound & specify big-O, big-omega & big-theta.

①  $\rightarrow$  Big-O (upper bound)

$\Rightarrow O(n^2)$  This function doesn't grow even faster than the Asymptotic function

② Big-omega  $\rightarrow$  (Lower bound)

$\rightarrow$  This function also doesn't grow slower than the Asymptotic function

$$\Omega(n^2)$$

③ Big-Theta: This is our function which grows Asymptotically as  $n^2$ ,



if the function was to be modified.

$x = f(n)$

$x = 1;$

$y = 1;$

for  $i = 1:n$

for  $j = 1:n$

$x = x + 1;$

$y = i + j;$

④

Will this increase the Runtime?

→ Yes, This will increase the Runtime of the New function compared to previous one. As  $y = i + j$  has a complexity of  $O(1)$ . This will attribute a small increased Runtime.

But the Time complexity is  $O(n^2)$ .

⑤

No, it won't effect our Results from #1

The effects won't be visible but in a significantly low Runtime.