

$$\boxed{|\tau| = T}$$

$$\begin{aligned} |\alpha| &= \alpha \\ |\{\}| &= () \\ |\tau_1| \rightarrow |\tau_2| &= |\tau_1| \rightarrow |\tau_2| \\ |\forall \alpha. \tau| &= \forall \alpha. |\tau| \\ |\tau_1 \& \tau_2| &= (|\tau_1|, |\tau_2|) \\ |[l:\tau]| &= |\tau| \end{aligned}$$

Figure 1: Type translation.

$$\begin{aligned} &\boxed{\tau <: \tau \hookrightarrow C} \quad \frac{}{\alpha <: \alpha \hookrightarrow \lambda(x:|\alpha|).x} \text{subvar} \quad \frac{}{\tau <: \{\} \hookrightarrow \lambda(x:|\tau|).()} \text{subtop} \\ &\frac{\tau_3 <: \tau_1 \hookrightarrow C_1 \quad \tau_2 <: \tau_4 \hookrightarrow C_2}{\tau_1 \rightarrow \tau_2 <: \tau_3 \rightarrow \tau_4 \hookrightarrow \lambda(f:|\tau_1 \rightarrow \tau_2|). \lambda(x:|\tau_3|). C_2 (f (C_1 x)))} \text{subfun} \\ &\frac{\tau_1 <: [\alpha_1/\alpha_2]\tau_2 \hookrightarrow C}{\forall \alpha_1. \tau_1 <: \forall \alpha_2. \tau_2 \hookrightarrow \lambda(f:|\forall \alpha. \tau_1|). \Lambda \alpha. C (f \alpha)} \text{subforall} \\ &\frac{\tau_1 <: \tau_2 \hookrightarrow C_1 \quad \tau_1 <: \tau_3 \hookrightarrow C_2}{\tau_1 <: \tau_2 \& \tau_3 \hookrightarrow \lambda(x:|\tau_1|). (C_1 x, C_2 x)} \text{suband} \\ &\frac{\tau_1 <: \tau_3 \hookrightarrow C}{\tau_1 \& \tau_2 <: \tau_3 \hookrightarrow \lambda(x:|\tau_1 \& \tau_2|). C (\text{proj}_1 x)} \text{suband}_1 \\ &\frac{\tau_2 <: \tau_3 \hookrightarrow C}{\tau_1 \& \tau_2 <: \tau_3 \hookrightarrow \lambda(x:|\tau_1 \& \tau_2|). C (\text{proj}_2 x)} \text{suband}_2 \\ &\frac{\tau_1 <: \tau_2 \hookrightarrow C}{\{l:\tau_1\} <: \{l:\tau_2\} \hookrightarrow \lambda(x:|\{l:\tau_1\}|). C x} \text{subrec} \end{aligned}$$

Figure 2: Elaboration subtyping.

$$\begin{array}{c}
\boxed{\gamma \vdash e : \tau \hookrightarrow E} \quad \frac{(x, \tau) \in \gamma}{\gamma \vdash x : \tau \hookrightarrow x} \text{Evar} \quad \frac{}{\gamma \vdash \{\} : \{\} \hookrightarrow ()} \text{Etop} \\
\\
\frac{\gamma, x : \tau \vdash e : \tau_1 \hookrightarrow E \quad \gamma \vdash \tau}{\gamma \vdash \lambda(x : \tau). e : \tau \rightarrow \tau_1 \hookrightarrow \lambda(x : |\tau|). E} \text{Elam} \\
\\
\frac{\gamma \vdash e_1 : \tau_1 \rightarrow \tau_2 \hookrightarrow E_1 \quad \gamma \vdash e_2 : \tau_3 \hookrightarrow E_2 \quad \tau_3 <: \tau_1 \hookrightarrow C}{\gamma \vdash e_1 \ e_2 : \tau_2 \hookrightarrow E_1 \ (C \ E_2)} \text{Eapp} \\
\\
\frac{\gamma, \alpha \vdash e : \tau \hookrightarrow E}{\gamma \vdash \Lambda \alpha. e : \forall \alpha. \tau \hookrightarrow \Lambda \alpha. E} \text{Eblam} \quad \frac{\gamma \vdash e : \forall \alpha. \tau_1 \hookrightarrow E \quad \gamma \vdash \tau}{\gamma \vdash e \ \tau : [\tau/\alpha] \tau_1 \hookrightarrow E \ |\tau|} \text{Etapp} \\
\\
\frac{\gamma \vdash e_1 : \tau_1 \hookrightarrow E_1 \quad \gamma \vdash e_2 : \tau_2 \hookrightarrow E_2}{\gamma \vdash e_1, e_2 : \tau_1 \ \& \ \tau_2 \hookrightarrow (E_1, E_2)} \text{Emerge} \\
\\
\frac{\gamma \vdash e : \tau \hookrightarrow E}{\gamma \vdash \{l = e\} : \{l : \tau\} \hookrightarrow E} \text{Erec-construct} \\
\\
\frac{\gamma \vdash e : \tau \hookrightarrow E \quad \tau \bullet l = \tau_1 \hookrightarrow C}{\gamma \vdash e.l : \tau_1 \hookrightarrow C \ E} \text{Erec-select} \\
\\
\frac{\gamma \vdash e : \tau \hookrightarrow E \quad \tau - l = \tau_1 \hookrightarrow C}{\gamma \vdash e - l : \tau_1 \hookrightarrow C \ E} \text{Erec-restrict} \\
\\
\\
\boxed{\tau_1 \bullet l = \tau_2 \hookrightarrow C} \quad \frac{}{\{l : \tau\} \bullet l = \tau \hookrightarrow \lambda(x : \{l : \tau\}). x} \text{select} \\
\\
\frac{\tau_1 \bullet l = \tau \hookrightarrow C}{\tau_1 \ \& \ \tau_2 \bullet l = \tau \hookrightarrow \lambda(x : |\tau_1 \ \& \ \tau_2|). C \ (\text{proj}_1 x)} \text{select}_1 \\
\\
\frac{\tau_2 \bullet l = \tau \hookrightarrow C}{\tau_1 \ \& \ \tau_2 \bullet l = \tau \hookrightarrow \lambda(x : |\tau_1 \ \& \ \tau_2|). C \ (\text{proj}_2 x)} \text{select}_2 \\
\\
\\
\boxed{\tau_1 - l = \tau_2 \hookrightarrow C} \quad \frac{}{\{l : \tau\} - l = \{\} \hookrightarrow \lambda(x : \{l : \tau\}). ()} \text{restrict} \\
\\
\frac{\tau_1 - l = \tau \hookrightarrow C}{\tau_1 \ \& \ \tau_2 - l = \tau \ \& \ \tau_2 \hookrightarrow \lambda(x : |\tau_1 \ \& \ \tau_2|). (C \ (\text{proj}_1 x), \text{proj}_2 x)} \text{restrict}_1 \\
\\
\frac{\tau_2 - l = \tau \hookrightarrow C}{\tau_1 \ \& \ \tau_2 - l = \tau_1 \ \& \ \tau \hookrightarrow \lambda(x : |\tau_1 \ \& \ \tau_2|). (\text{proj}_1 x, C \ (\text{proj}_2 x))} \text{restrict}_2
\end{array}$$

Figure 3: Elaboration typing.