

## DSnP HW5

### Implementation of some ADT

- **Dynamic Array**  
Just an normal STL-vector-like container.  
Uses `<algorithm>::sort()`.  
Time complexities:  
**Insert random place:**  $O(n)$ , since we may need to move all our data to other place.  
**Delete random place:**  $O(1)$ , since we just swap it with `back()`, and then `pop_back()`.  
**Sort:**  $O(\ln(n))$ , since we use STL sort, and didn't utilize the mutable variable `is_sorted`.  
(which shall not be used, since we have functions that return non-const iterators, and thus our data could be modified even when there's no element deleted/inserted – they are modified through these iterators.)  
**Size:**  $O(1)$ , since dynamic arrays itself have to maintain its size and capacity, and we could just return them.
- **Doubly Linked List**  
Basically it's a ring. Contains a dummy node.  
Uses merge-sort variant for linked lists.  
**Push Back:**  $O(1)$ , since we just need to modify fixed amount of pointers.  
**Delete random place:**  $O(n)$ , since we have to find where to delete. After the item was found, it's constant time operation.  
**Sort:**  $O(\ln(n))$ , since we used merge sort. BTW we just modify the pointers to sort the list, so there's no copy or move (c++11 or later) constructor used when sort. Which I think is handy.  
**Size:**  $O(n)$ , since I didn't maintain the size, I have to traverse the whole list.
- **Binary Search Tree**  
A Red-Black tree variant. Uses `nullptr` instead of `NIL`, that is, there's no dummy tree node.  
Shall not be very stable actually, but at least it passed do1 to do4.  
**Insert:**  $O(\ln(n))$ , since R-B tree is balanced, so insert time complexity for trees  $O(\text{height})$  is just  $O(\ln(n))$ .  
**Delete random index:**  $O(n)$ , since I used in-order traversal.  
**Delete random key:**  $O(\ln(n))$ , since R-B tree is balanced, so delete time complexity for trees  $O(\text{height})$  degenerates to  $O(\ln(n))$ .  
**Sort:**  $O(1)$ , since R-B tree itself is a binary search tree, which is sorted.  
**Size:**  $O(1)$ , since I have an size data field for the whole tree.
- **Some Experiments: (uses g++ -g -O2)**
  - Doubly linked list, random add, sort, quit. String length is 6.

Item #	1000000	2000000	3000000	4000000
Period Time (ms)	1320	2780	4410	5900

- Binary Search tree, random add. String length is 6.

Item #	100w	200w	300w	400w
Period Time (ms)	1690	3770	6130	8660