

## Structural and vibrational studies of $\text{NaZr}_2(\text{AsO}_4)_3$

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### Abstract

The structure of  $\text{NaZr}_2(\text{AsO}_4)_3$ , which belongs to the Nasicon-type family, was solved by the Rietveld method in the  $R\bar{3}c$  space group, from X-ray powder diffraction data. The hexagonal unit cell parameters are  $a_h = 9.1518(2)$  Å and  $c_h = 23.1097(4)$  Å. The structure is formed by a three-dimensional network of  $\text{AsO}_4$  tetrahedra and  $\text{ZrO}_6$  octahedra sharing corners. Na atoms occupy totally the M1 site. Raman and infrared spectra were recorded and assignments of the As–O stretching and bending modes were made.

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### 1. Introduction

Nasicon-type materials have been extensively studied in context of various fields of solid state chemistry: solid electrolytes, electrode materials, low thermal expansion ceramics, etc. [1–9]. Their structure was initially described for  $\text{NaA}_2(\text{PO}_4)_3$  ( $A = \text{Ti, Zr, Ge}$ ) [1]. It consists of a three-dimensional (3D) network built up of  $\text{PO}_4$  tetrahedra sharing corners with  $\text{AO}_6$  octahedra. Within the 3D-framework, two sites, usually labelled M1 and M2, are available for the alkali metal cations. The M1 site is an antiprism formed by the triangular faces of two  $\text{AO}_6$  octahedra along  $c$ -axis of the hexagonal cell. Thus, the network of  $\text{NaA}_2(\text{PO}_4)_3$  can be considered as made up of infinite ribbons of composition  $(\text{O}_3\text{AO}_3\text{M1}(\text{Na})\text{O}_3\text{AO}_3)_\infty$  connected by  $\text{PO}_4$  tetrahedra. The M2 sites are located between these ribbons in large cavities with a eight-fold coordination. The M1 and M2 sites may be completely empty as in  $\text{NbTi}(\text{PO}_4)_3$  [10], partially occupied as in  $\text{NaZr}_2(\text{PO}_4)_3$  [1] and  $\text{Na}_3\text{CaTi}(\text{PO}_4)_3$  [11], or fully occupied as in  $\text{Na}_5\text{Ti}(\text{PO}_4)_3$  [12]. In contrast to the extensive studies of the Nasicon-type phosphates and silicates, only a few investigations have been reported for the arsenates analogues. To our knowledge only X-ray

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Table 1

Crystallographic data for  $\text{NaZr}_2(\text{AsO}_4)_3$ 

Wavelength (Å)	$\lambda_{\text{K}\alpha 1} = 1.5406$ ; $\lambda_{\text{K}\alpha 2} = 1.5444$
Step width (°); counting time (s)	0.02; 30
Angular range (°)	10–100
Pseudo-Voigt function	$\text{PV} = \eta\text{L} + (1-\eta)\text{G}$ ; $\eta = 0.71(2)$ ;
Caglioti law parameters	$U = 0.062(2)$ ; $V = -0.003(1)$ ; $W = 0.013(1)$
Number of reflections	401
Number of refined parameters	33
System; space group	Hexagonal; $R\bar{3}c$
$a$ (Å); $c$ (Å); $V$ (Å <sup>3</sup> ); $Z$	9.1518(2); 23.1097(4); 1676.26(1); 6
$R_F$ ; $R_B$ ; $R_P$ ; $R_{WP}$ ; $\chi^2$	0.02; 0.03; 0.08; 0.11; 1.97

powder diffraction patterns have been reported for  $\text{MTi}_2(\text{AsO}_4)_3$  ( $M = \text{Li, Na, Ag, K}$ ),  $\text{M}_{0.5}\text{Ti}_2(\text{AsO}_4)_3$  ( $M = \text{Mg, Ca, Sr}$ ) [13] and  $\text{MeZr}_2(\text{As}_{1-x}\text{P}_x\text{O}_4)_3$  ( $\text{Me} = \text{Na, K}$ ) [14]. The structures of  $\text{KZr}_2(\text{AsO}_4)_3$  [15] and  $\text{Na}_3\text{Sc}_2(\text{AsO}_4)_3$  [16] have been determined from single crystal X-ray diffraction data. Structural [17,18], electrochemical [19] and vibrational [20,21] studies of  $\text{A}_3\text{M}_2(\text{AsO}_4)_3$  ( $A = \text{Li, Na}$ ;  $M = \text{Al, Fe, In}$ ) have been reported. Recently we initiated a program on arsenate compounds in order to compare their properties to those of the phosphates. The present paper reports on the crystal structure and vibrational spectra of  $\text{NaZr}_2(\text{AsO}_4)_3$ .

## 2. Experimental

$\text{NaZr}_2(\text{AsO}_4)_3$  arsenate powder was prepared from  $\text{Na}_2\text{CO}_3$  dissolved in dilute nitric acid solution (I) and aqueous solutions of  $\text{ZrOCl}_2 \cdot 8\text{H}_2\text{O}$  (II) and  $(\text{NH}_4)_2\text{H}_2\text{AsO}_4$  (III) in stoichiometric proportions. After addition of (III) in (I + II) mixture at room temperature and slow evaporation at about 60 °C, the resulting powder was heated progressively at different temperatures, between 200 and 800 °C, with intermitting regrinding. The powder of  $\text{NaZr}_2(\text{AsO}_4)_3$  is white.

Powder X-ray diffraction data were collected at room temperature on a Philips PW 3040 ( $\theta$ – $\theta$ ) diffractometer (40 kV, 40 mA). The structure of  $\text{NaZr}_2(\text{AsO}_4)_3$  was refined with the Rietveld method using the program Fullprof [22]. The experimental conditions are given in Table 1.

Raman spectra were recorded using a Dilor XY Raman microprobe. The crystalline samples were excited with the 514.5 nm line of an Argon ion laser (Coherent model Innova 300). The spectral resolution was 3  $\text{cm}^{-1}$ , the laser output power was 110 mW and the integration time 60 s. Infrared spectra were recorded on a Bruker IFS 113 v FTIR spectrometer as KBr pellets.

## 3. Results and discussion

### 3.1. Structural determination

X-ray powder diffraction pattern of  $\text{NaZr}_2(\text{AsO}_4)_3$  is similar to that of  $\text{NaZr}_2(\text{PO}_4)_3$  with a shift of the peaks toward lower values of  $2\theta$  Bragg's angles (Fig. 1). It was indexed assuming a hexagonal cell:  $a_h = 9.1518(2)$  Å and  $c_h = 23.1097(4)$  Å. All of the observed reflections are compatible with the  $R\bar{3}c$

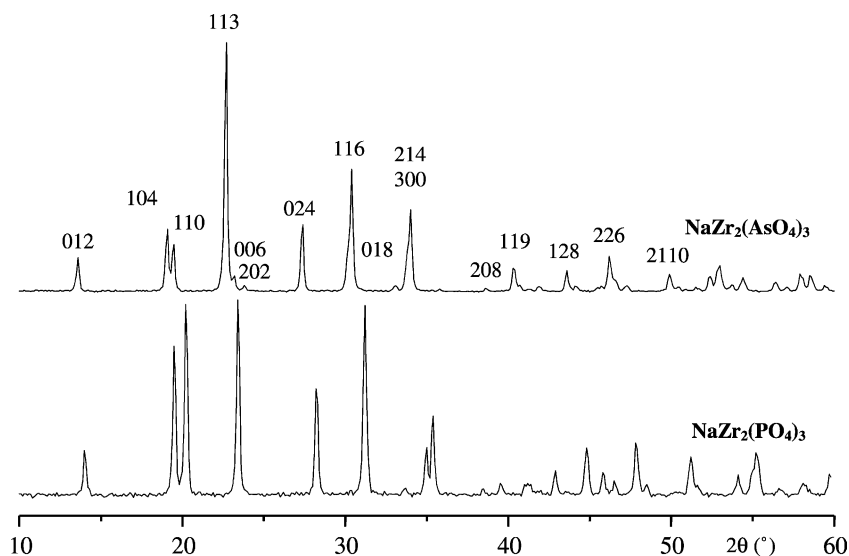


Fig. 1. X-ray powder patterns of  $\text{NaZr}_2(\text{AsO}_4)_3$  and  $\text{NaZr}_2(\text{PO}_4)_3$ .

space group. The initial atomic coordinates used for the refinement of the structure of  $\text{NaZr}_2(\text{AsO}_4)_3$  were those of the isostructural compound  $\text{NaZr}_2(\text{PO}_4)_3$ . After the refinement of 33 parameters (fractional atomic coordinates, temperature factors, scale factor, zero point, unit cell parameters, six background terms, profile parameters), the conventional reliability factors were:  $R_p = 0.08$ ,  $R_{wp} = 0.11$ ,  $R_F = 0.02$  and  $R_B = 0.03$ . The results of the refinement as well as different structural parameters are given in Tables 1 and 2. Fig. 2 shows good agreement between the observed and calculated patterns.

The structure of  $\text{NaZr}_2(\text{AsO}_4)_3$  (Fig. 3) is similar to that of  $\text{NaZr}_2(\text{PO}_4)_3$  [1]. The Zr–O (2.08 Å) and As–O (1.67 Å) distances of the covalent anionic framework  $[\text{Zr}_2(\text{AsO}_4)_3]$  are slightly smaller than those calculated from the ionic radii (Zr–O: 2.12 Å, As–O: 1.73 Å) [23]. Consequently the Na–O bond length

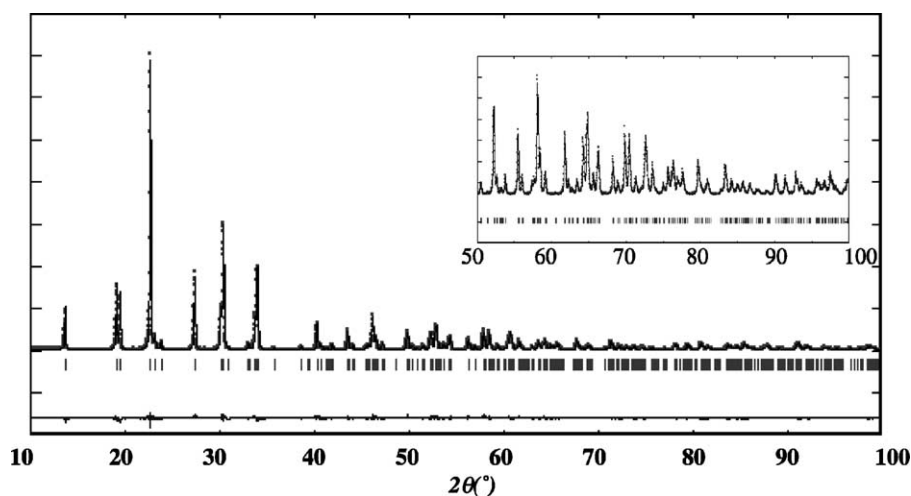
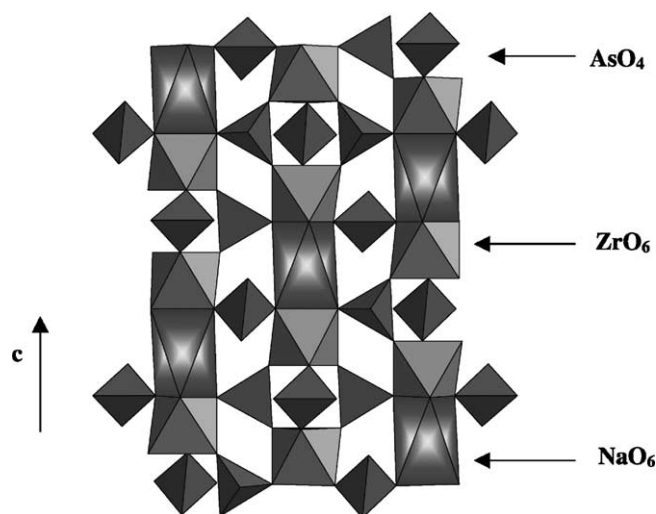


Fig. 2. Final observed (.), calculated (—) and difference X-ray profiles for  $\text{NaZr}_2(\text{AsO}_4)_3$ .

Fig. 3. Structure of  $\text{NaZr}_2(\text{AsO}_4)_3$ .

(2.50 Å) is larger than that obtained from the ionic radii sum of  $\text{Na}^+$  and  $\text{O}^{2-}$  (2.42 Å) reflecting a higher degree of ionicity. Valence bond sums,  $\sigma_i = \sum \exp[(R_{ij} - d_{ij})/b]$  with  $b = 0.37$  Å [24], based on bond-strength analysis (Na: 0.90; Zr: 4.054; As: 5.24;  $\text{O}_1$ : 2.07;  $\text{O}_2$ : 2.05), are in good agreement with the expected formal oxidation state of  $\text{Na}^+$ ,  $\text{Zr}^{4+}$ ,  $\text{As}^{5+}$  and  $\text{O}^{2-}$  ions.

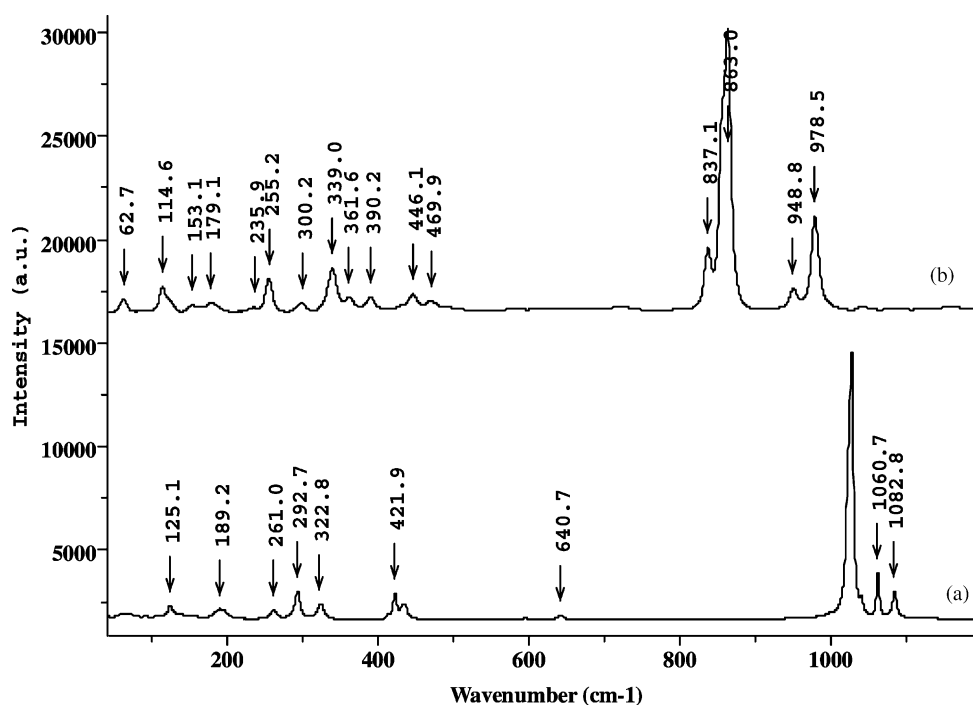
Fig. 4. Raman spectra of  $\text{NaZr}_2(\text{PO}_4)_3$  (a) and  $\text{NaZr}_2(\text{AsO}_4)_3$  (b).

Table 2

Atomic coordinates and isotropic temperatures factors

Atom	Wyckof site	<i>x</i>	<i>y</i>	<i>z</i>	<i>B</i> <sub>iso.</sub> (Å <sup>2</sup> )	Occ.
Na	6b	0.00	0.00	0.00	3.73	1
Zr	12c	0.00	0.00	0.1436	0.09	1
As	18e	0.2903	0.00	0.2500	0.42	1
O(1)	36f	0.1811	−0.0171	0.1902	0.35	1
O(2)	36f	0.1855	0.1611	0.0833	0.45	1

Table 3 compares the cell parameters of NaZr<sub>2</sub>(AsO<sub>4</sub>)<sub>3</sub>, NaZr<sub>2</sub>(PO<sub>4</sub>)<sub>3</sub> [1] and KZr<sub>2</sub>(AsO<sub>4</sub>)<sub>3</sub> [15]. The observed variations can be explained in the context of the Nasicon-type structure which can be considered as built of (O<sub>3</sub>ZrO<sub>3</sub>M1O<sub>3</sub>ZrO<sub>3</sub>) units connected by XO<sub>4</sub> tetrahedra (X = As, P) in three dimensions. When X is As, the lengths of the O–O tetrahedron edges increase, consequently the cell parameters of NaZr<sub>2</sub>(AsO<sub>4</sub>)<sub>3</sub> are superior to those of NaZr<sub>2</sub>(PO<sub>4</sub>)<sub>3</sub>. For AZr<sub>2</sub>(AsO<sub>4</sub>)<sub>3</sub> (A = Na, K), the increase of *c*<sub>h</sub> when sodium is replaced by potassium in M1 sites, located in the ribbons along this axis, is due to the size of K<sup>+</sup> (*r* = 1.16 Å) which is larger than that of Na<sup>+</sup> (*r* = 1.00 Å). The decrease of *a*<sub>h</sub> is due to the elasticity of the network formed by polyhedra linked together only by corners. Therefore, an elongation in one direction (*c*<sub>h</sub>) induces compression in the perpendicular direction (*a*<sub>h</sub>).

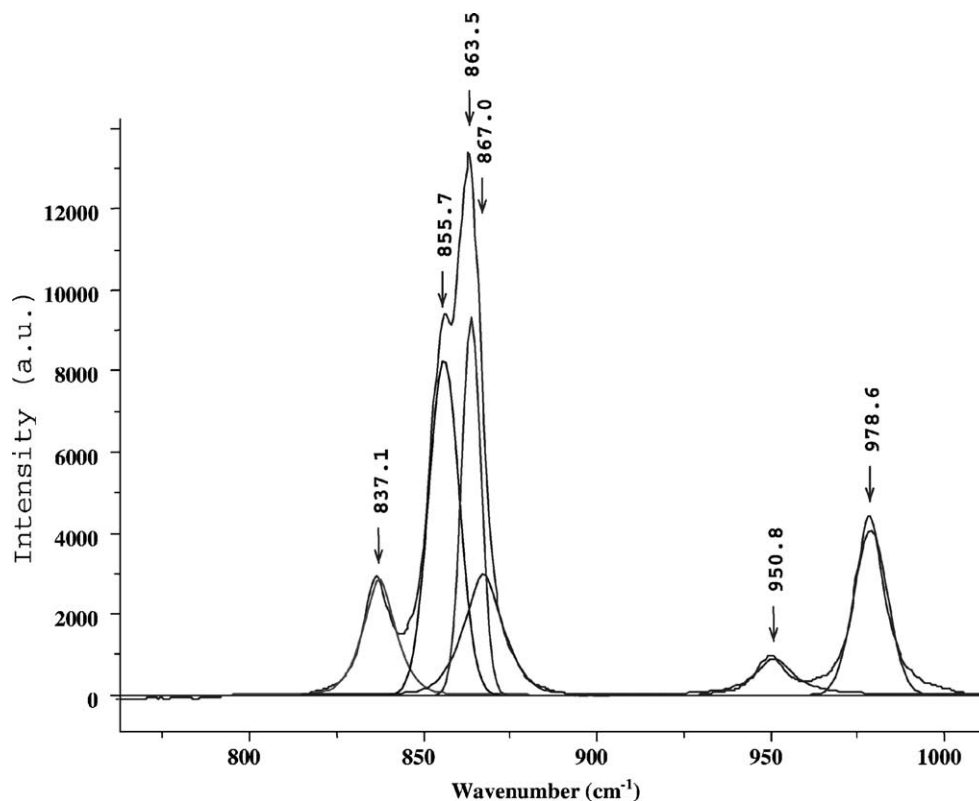
Fig. 5. Deconvoluted Raman spectrum of NaZr<sub>2</sub>(AsO<sub>4</sub>)<sub>3</sub> in the range of 750–1000 cm<sup>−1</sup>.

Table 3

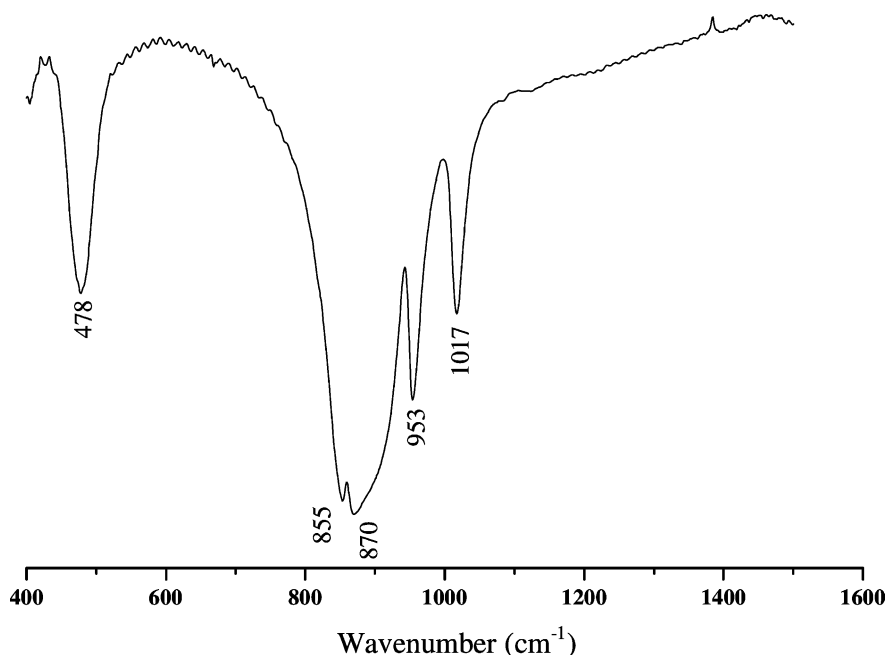
Lattice parameters of  $\text{NaZr}_2(\text{PO}_4)_3$ ,  $\text{NaZr}_2(\text{AsO}_4)_3$  and  $\text{KZr}_2(\text{AsO}_4)_3$ 

$\text{MZr}_2(\text{XO}_4)_3$	$r(\text{X}^{5+})$ (Å)	$R(\text{M}^{+})$ (Å)	$a_h$ (Å)	$c_h$ (Å)	$V$ (Å <sup>3</sup> )
$\text{NaZr}_2(\text{PO}_4)_3$ [1]	0.170	1.02	8.80	22.75	1526
$\text{NaZr}_2(\text{AsO}_4)_3$	0.335	1.02	9.15	23.11	1677
$\text{KZr}_2(\text{AsO}_4)_3$ [15]	0.335	1.38	9.03	24.40	1722

### 3.2. Vibrational spectroscopy

Vibrational analysis for an isolated  $\text{AsO}_4^{3-}$  anion with point group Td leads to four modes:  $A_1[(v_1:v_s(\text{AsO}_4))]$ ,  $E[(v_2:\delta_s(\text{AsO}_4))]$ ,  $2F_2[v_3:v_{as}(\text{AsO}_4)]$  and  $[v_4:\delta_{as}(\text{AsO}_4)]$ . All of them are Raman active whereas only  $v_3$  and  $v_4$  are infrared active. In  $\text{NaZr}_2(\text{AsO}_4)_3$  ( $R\bar{3}c$  space group) the arsenic site has a  $C_2$  symmetry; therefore, we expect six Raman-active modes for the stretching vibrations;  $2v_1(A_{1g}, E_g) + 4v_3(A_{1g}, E_g)$  and six IR-active modes;  $v_1(E_u) + 5v_3(A_{2u}, E_u)$ . For the bending vibrations we achieved eight Raman-active modes;  $4v_2(A_{1g}, E_g) + 4v_4(A_{1g}, E_g)$  and seven IR-active modes;  $2v_2(E_u) + 5v_4(A_{2u}, E_u)$ . The external modes consist of the translational vibrations of the  $\text{Na}^+$ ,  $\text{Zr}^{4+}$  and  $\text{AsO}_4^{3-}$  ions.

Fig. 4 compares Raman spectra of  $\text{NaZr}_2(\text{PO}_4)_3$  and  $\text{NaZr}_2(\text{AsO}_4)_3$ . The shift of the peaks, toward the lower energy in the arsenate, is due to longer As–O bonds compared to P–O bonds. The high frequency part (800–1050  $\text{cm}^{-1}$ ) of the Raman spectrum of  $\text{NaZr}_2(\text{AsO}_4)_3$  (Fig. 5) corresponds to the stretching vibrations of the  $\text{AsO}_4$  tetrahedra and exhibits six peaks at 979, 951, 867, 863, 856 and 837  $\text{cm}^{-1}$ , in good agreement with results of the factor group analysis. For the infrared spectrum (Fig. 6), four peaks (1017, 953, 870 and 855  $\text{cm}^{-1}$ ) and a shoulder (906  $\text{cm}^{-1}$ ) are observed in this region. The six Raman peaks

Fig. 6. Infrared spectrum of  $\text{NaZr}_2(\text{AsO}_4)_3$ .

observed at 470, 446, 390, 362, 339 and 300  $\text{cm}^{-1}$  are assigned to the As–O bending vibrations, the predicted ones are eight. The peaks situated below 300  $\text{cm}^{-1}$  are attributed to the external modes; seven Raman peaks (255, 236, 179, 153, 124, 115 and 63  $\text{cm}^{-1}$ ) are observed between 250 and 50  $\text{cm}^{-1}$ .

#### 4. Conclusion

The arsenate  $\text{NaZr}_2(\text{AsO}_4)_3$  has been synthesised and characterized by mean of X-ray diffraction and vibrational spectroscopy. Its structure has been solved in  $R\bar{3}c$  space group. It is formed by a 3D network of  $\text{ZrO}_6$  octahedra and  $\text{AsO}_4$  tetrahedra linked by corners. The sodium is at the centre of the antiprism located between two  $\text{ZrO}_6$  octahedra. Assignments of internal modes of the  $\text{AsO}_4$  tetrahedra have been made. The number of the peaks observed, in Raman and infrared spectra, is in good agreement with that predicted by the factor group analysis of the  $R\bar{3}c$  space group.

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