

1 Data-Structure

1.1 Treap

```

1 template<class S,
2     S (*node_pull)(S, S),
3     S (*node_init)(S),
4     class T,
5     S (*mapping)(S, T),
6     T (*tag_pull)(T, T),
7     T (*tag_init)()>
8 struct Treap{
9     struct node{
10         node *l = NULL,*r = NULL,*p = NULL;
11         const int pri = rand();
12         int sz = 1;
13         S info;
14         T tag = tag_init();
15         bool rev;
16         node(S k) : info(k){}
17         ~node(){
18             for(auto &i:{l,r})
19                 delete i;
20         }
21         void all_apply(T t,bool is_rev){
22             if(is_rev){
23                 swap(l,r);
24                 rev^=1;
25             }
26             info = mapping(info, t);
27             tag = tag_pull(tag, t);
28         }
29         void push(){
30             for(auto &i:{l,r})
31                 if(i)i->all_apply(tag, rev);
32             tag = tag_init();
33             rev = 0;
34         }
35         void pull(){
36             sz = 1,info = node_init(info);
37             for(auto &i:{l,r}){
38                 if(i){
39                     sz+=i->sz,i->p = this;
40                     info = node_pull(info,i->info);
41                 }
42             }
43         }
44     };
45     node *root = NULL;
46     int size(node *a){
47         return a?a->sz:0;
48     }
49     int size(){
50         return size(root);
51     }
52     node *merge(node *a,node *b){
53         if(!a or !b)return a?:b;
54         if(a->pri>b->pri){
55             a->push();
56             a->r = merge(a->r,b);
57             a->r->p = a;
58             a->pull();
59             return a;
60         }
61         else{
62             b->push();
63             b->l = merge(a,b->l);
64             b->l->p = b;
65             b->pull();
66             return b;
67         }
68     }
69     void split(node *t, long long k, node *&a, node *&b, const
70         bool &bst){
71         if(!t){a = b = NULL;return;}
72         t->push();
73         if((bst==0 and size(t->l)+1<=k) or (bst==1 and t->info.key
74             <=k)){
75             a = t;
76             split(t->r, (bst ? k : k - size(t->l) - 1), a->r, b,
77                 bst);
78             if(b)b->p = NULL;
79             a->pull();
80         }
81         else{
82             b = t;
83             split(t->l, k, a, b->l, bst);
84             if(a)a->p = NULL;
85             b->pull();
86         }
87     }
88     void *insert(long long idx, S x,bool bst = 0){
89         node *a,*b;
90         split(root, idx, a, b, bst);

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88     node *tmp = new node(x);
89     root = merge(a, merge(tmp, b));
90     return tmp;
91 }
92 void erase(long long l,long long r,bool bst = 0){
93     node *a,*b,*c;
94     split(root, (bst? l-1 : l), a, b, bst);
95     split(b, (bst? r : r - l + 1), b, c, bst);
96     delete b;
97     root = merge(a,c);
98 }
99 S operator [](int x){
100     node *a, *b, *c;
101     split(root, x, a, b, 0);
102     split(b, 1, b, c, 0);
103     assert(b!=NULL);
104     S ans = b->info;
105     root = merge(a, merge(b, c));
106     return ans;
107 }
108 int rank(long long k){
109     node *a, *b;
110     split(root, k - 1, a, b, 1);
111     int ans = size(a);
112     root = merge(a, b);
113     return ans;
114 }
115 S* find_next(long long k){
116     node *a, *b, *c;
117     split(root, k - 1, a, b, 1);
118     split(b, 1, b, c, 0);
119     S* ans = NULL;
120     if(b)ans = &b->info;
121     root = merge(a, merge(b, c));
122     return ans;
123 }
124 S* find_prev(long long k){
125     node *a, *b, *c;
126     split(root, k, a, b, 1);
127     split(a, size(a) - 1, a, c, 0);
128     S* ans = NULL;
129     if(c)ans = &c->info;
130     root = merge(merge(a, c), b);
131     return ans;
132 }
133 void update(long long l,long long r,T t,bool bst = 0){
134     node *a, *b, *c;
135     split(root, (bst? l - 1 : l), a, b, bst);
136     split(b, (bst? r : r - l + 1), b, c, bst);
137     if(b)b->all_apply(t, 0);
138     root = merge(a, merge(b, c));
139 }
140 void reverse(long long l,long long r,bool bst = 0){
141     node *a, *b, *c;
142     split(root, (bst? l - 1 : l), a, b, bst);
143     split(b, (bst? r : r - l + 1), b, c, bst);
144     if(b)b->all_apply(tag_init(), 1);
145     root = merge(a, merge(b, c));
146 }
147 S query(long long l,long long r,bool bst = 0){
148     node *a, *b, *c;
149     split(root, (bst? l - 1 : l), a, b, bst);
150     split(b, (bst? r : r - l + 1), b, c, bst);
151     S ans;
152     if(b)ans = b->info;
153     root = merge(a, merge(b, c));
154     return ans;
155 }
156 };

```

1.2 Segtree

```

1 template<class S,
2     S (*node_pull)(S, S),
3     S (*node_init)(),
4     class T,
5     S (*mapping)(S, T),
6     T (*tag_pull)(T, T),
7     T (*tag_init)()>
8 struct segment_tree{
9     struct node{
10         S seg;
11         T tag = tag_init();
12         int l,r;
13         node(S _seg = node_init(),int _l = -1,int _r = -1) : seg(
14             _seg), l(_l), r(_r){}
15         friend node operator +(const node &lhs,const node &rhs){
16             if(lhs.l==-1)return rhs;
17             if(rhs.l==-1)return lhs;
18             return node(node_pull(lhs.seg,rhs.seg),lhs.l,rhs.r);
19         };
20     };
21     vector<node>arr;
22     void all_apply(int idx,T t){

```

```

22     arr[idx].seg = mapping(arr[idx].seg, t);
23     arr[idx].tag = tag_pull(arr[idx].tag, t);
24 }
25 void push(int idx){
26     all_apply(idx<<1, arr[idx].tag);
27     all_apply(idx<<1|1, arr[idx].tag);
28     arr[idx].tag = tag_init();
29 }
30 inline void build(const vector<S> &v, const int &l, const int &
    r, int idx = 1){
31     if(idx==1)arr.resize((r-1+1)<<2);
32     if(l==r){
33         arr[idx].seg = v[l];
34         arr[idx].tag = tag_init();
35         arr[idx].l = arr[idx].r = l;
36         return;
37     }
38     int m = (l+r)>>1;
39     build(v, l, m, idx<<1);
40     build(v, m+1, r, idx<<1|1);
41     arr[idx] = arr[idx<<1]+arr[idx<<1|1];
42 }
43 inline void update(const int &q1, const int &qr, T t, int idx =
    1){
44     assert(q1<=qr);
45     if(q1==arr[idx].l and arr[idx].r==qr){
46         all_apply(idx, t);
47         return;
48     }
49     push(idx);
50     int m = (arr[idx].l+arr[idx].r)>>1;
51     if(q1<=m)update(q1, qr, t, idx<<1);
52     if(qr>m)update(q1, qr, t, idx<<1|1);
53     arr[idx] = arr[idx<<1]+arr[idx<<1|1];
54 }
55 inline S query(const int &q1, const int &qr, int idx = 1){
56     assert(q1<=qr);
57     if(q1==arr[idx].l and arr[idx].r==qr){
58         return arr[idx].seg;
59     }
60     push(idx);
61     int m = (arr[idx].l+arr[idx].r)>>1;
62     S ans = node_init(), lhs = node_init(), rhs = node_init();
63     if(q1<=m)lhs = query(q1, qr, idx<<1);
64     if(qr>m)rhs = query(q1, qr, idx<<1|1);
65     ans = node_pull(lhs, rhs);
66     return ans;
67 }
68 };

```

1.3 DsuUndo

```

1 struct dsu_undo{
2     vector<int>sz, p;
3     int comps;
4     dsu_undo(int n){
5         sz.assign(n+5, 1);
6         p.resize(n+5);
7         for(int i = 1; i<=n; ++i)p[i] = i;
8         comps = n;
9     }
10    vector<pair<int, int>>opt;
11    int Find(int x){
12        return x==p[x]?x:Find(p[x]);
13    }
14    bool Union(int a, int b){
15        int pa = Find(a), pb = Find(b);
16        if(pa==pb)return 0;
17        if(sz[pa]<sz[pb])swap(pa, pb);
18        sz[pa]+=sz[pb];
19        p[pb] = pa;
20        opt.push_back({pa, pb});
21        comps--;
22        return 1;
23    }
24    void undo(){
25        auto [pa, pb] = opt.back();
26        opt.pop_back();
27        p[pb] = pb;
28        sz[pa]-=sz[pb];
29        comps++;
30    }
31 };

```

1.4 DSU

```

1 struct DSU{
2     vector<int>sz;
3     int n;
4     DSU(int _n):n(_n){
5         sz.assign(n+1, -1);

```

```

6     }
7     int Find(int x){
8         return sz[x]<0?x:sz[x] = Find(sz[x]);
9     }
10    bool Union(int a, int b){
11        int pa = Find(a), pb = Find(b);
12        if(pa==pb)return 0;
13        if((-sz[pa])<(-sz[pb]))swap(pa, pb);
14        sz[pa]+=sz[pb];
15        sz[pb] = pa;
16        return 1;
17    }
18 };

```

1.5 Fenwick

```

1 template<class T>struct fenwick_tree{
2     int n;
3     vector<T>arr;
4     inline int lowbit(int x){
5         return x&(-x);
6     }
7     fenwick_tree(int _n) : n(_n){
8         arr.assign(n+5, 0);
9     }
10    T query(int x){
11        T ans = 0;
12        for(int i = x; i>0; i-=lowbit(i)){
13            ans+=arr[i];
14        }
15        return ans;
16    }
17    void update(int x, T y){
18        for(int i = x; i<=n; i+=lowbit(i)){
19            arr[i]+=y;
20        }
21    }
22 };

```

1.6 Persistent DSU

```

1 int rk[200001] = {};
2 struct Persistent_DSU{
3     rope<int>*p;
4     int n;
5     Persistent_DSU(int _n = 0):n(_n){
6         if(n==0)return;
7         p = new rope<int>;
8         int tmp[n+1] = {};
9         for(int i = 1; i<=n; ++i)tmp[i] = i;
10        p->append(tmp, n+1);
11    }
12    Persistent_DSU(const Persistent_DSU &tmp){
13        p = new rope<int>(*tmp.p);
14        n = tmp.n;
15    }
16    int Find(int x){
17        int px = p->at(x);
18        return px==x?x:Find(px);
19    }
20    bool Union(int a, int b){
21        int pa = Find(a), pb = Find(b);
22        if(pa==pb)return 0;
23        if(rk[pa]<rk[pb])swap(pa, pb);
24        p->replace(pb, pa);
25        if(rk[pa]==rk[pb])rk[pa]++;
26        return 1;
27    }
28 };

```

1.7 TimingSegtree

```

1 template<class T, class D>struct timing_segment_tree{
2     struct node{
3         int l, r;
4         vector<T>opt;
5     };
6     vector<node>arr;
7     void build(int l, int r, int idx = 1){
8         if(idx==1)arr.resize((r-1+1)<<2);
9         if(l==r){
10            arr[idx].l = arr[idx].r = l;
11            arr[idx].opt.clear();
12            return;
13        }
14        int m = (l+r)>>1;
15        build(l, m, idx<<1);
16        build(m+1, r, idx<<1|1);
17        arr[idx].l = l, arr[idx].r = r;

```

```

18     arr[idx].opt.clear();
19 }
20 void update(int ql,int qr,T k,int idx = 1){
21     if(ql<=arr[idx].l and arr[idx].r<=qr){
22         arr[idx].opt.push_back(k);
23         return;
24     }
25     int m = (arr[idx].l+arr[idx].r)>>1;
26     if(ql<=m)update(ql,qr,k,idx<<1);
27     if(qr>m)update(ql,qr,k,idx<<1|1);
28 }
29 void dfs(D &d,vector<int>&ans,int idx = 1){
30     int cnt = 0;
31     for(auto [a,b]:arr[idx].opt){
32         if(d.Union(a,b))cnt++;
33     }
34     if(arr[idx].l==arr[idx].r)ans[arr[idx].l] = d.comps;
35     else{
36         dfs(d,ans,idx<<1);
37         dfs(d,ans,idx<<1|1);
38     }
39     while(cnt-->0)d.undo();
40 }
41 };

```

1.8 AreaOfRectangles

```

1 long long AreaOfRectangles(vector<tuple<int,int,int,int>>>v){
2     vector<tuple<int,int,int,int>>tmp;
3     int L = INT_MAX,R = INT_MIN;
4     for(auto [x1,y1,x2,y2]:v){
5         tmp.push_back({x1,y1+1,y2,1});
6         tmp.push_back({x2,y1+1,y2,-1});
7         R = max(R,y2);
8         L = min(L,y1);
9     }
10    vector<long long>seg((R-L+1)<<2),tag((R-L+1)<<2);
11    sort(tmp.begin(),tmp.end());
12    function<void(int,int,int,int,int,int)>update = [&](int ql,
13        int qr,int val,int l,int r,int idx){
14        if(ql<=l and r<=qr){
15            tag[idx]+=val;
16            if(tag[idx])seg[idx] = r-l+1;
17            else if(l==r)seg[idx] = 0;
18            else seg[idx] = seg[idx<<1]+seg[idx<<1|1];
19            return;
20        }
21        int m = (l+r)>>1;
22        if(ql<=m)update(ql,qr,val,l,m,idx<<1);
23        if(qr>m)update(ql,qr,val,m+1,r,idx<<1|1);
24        if(tag[idx])seg[idx] = r-l+1;
25        else seg[idx] = seg[idx<<1]+seg[idx<<1|1];
26    };
27    long long last_pos = 0,ans = 0;
28    for(auto [pos,l,r,val]:tmp){
29        ans+=(pos-last_pos)*seg[l];
30        update(l,r,val,L,R,1);
31        last_pos = pos;
32    }
33    return ans;
34 }

```

1.9 SparseTable

```

1 template<class T,T (*op)(T,T)>struct sparse_table{
2     int n;
3     vector<vector<T>>mat;
4     sparse_table(): n(0){}
5     sparse_table(const vector<T>&v){
6         n = (int)(v.size());
7         mat.resize(30);
8         mat[0] = v;
9         for(int i = 1;(1<<i)<=n;++i){
10             mat[i].resize(n-(1<<i)+1);
11             for(int j = 0;j<n-(1<<i)+1;++j){
12                 mat[i][j] = op(mat[i-1][j],mat[i-1][j+(1<<(i-1))]);
13             }
14         }
15     }
16     T query(int ql,int qr){
17         int k = __lg(qr-ql+1);
18         return op(mat[k][ql],mat[k][qr-(1<<k)+1]);
19     }
20 };

```

1.10 VEBTree

```

1 // Can correctly work with numbers in range [0; MAXN]
2 // Supports all std::set operations in O(1) on random queries /
3 // dense arrays, O(log64(N)) in worst case (sparse array).
4 // Count operation works in O(1) always.
5 template<unsigned int MAXN>
6 class fast_set {
7 private:
8     static const unsigned int PREF = (MAXN <= 64 ? 0 :
9         MAXN <= 4096 ? 1 :
10         MAXN <= 262144 ? 1 + 64 :
11         MAXN <= 16777216 ? 1 + 64 + 4096 :
12         MAXN <= 1073741824 ? 1 + 64 + 4096 + 262144 :
13         227) + 1;
14     static constexpr unsigned long long lowest_bits11[] = {0ULL,
15         1ULL, 3ULL, 7ULL, 15ULL, 31ULL, 63ULL, 127ULL, 255ULL,
16         511ULL, 1023ULL, 2047ULL, 4095ULL, 8191ULL, 16383ULL,
17         32767ULL, 65535ULL, 131071ULL, 262143ULL, 524287ULL,
18         1048575ULL, 2097151ULL, 4194303ULL, 8388607ULL, 16777215
19         ULL, 33554431ULL, 67108863ULL, 134217727ULL, 268435455ULL
20         , 536870911ULL, 1073741823ULL, 2147483647ULL, 4294967295
21         ULL, 8589934591ULL, 17179869183ULL, 34359738367ULL,
22         68719476735ULL, 137438953471ULL, 274877906943ULL,
23         549755813887ULL, 1099511627775ULL, 2199023255551ULL,
24         4398046511103ULL, 8796093022207ULL, 17592186044415ULL,
25         35184372088831ULL, 70368744177663ULL, 140737488355327ULL,
26         281474976710655ULL, 562949953421311ULL, 1125899906842623
27         ULL, 2251799813685247ULL, 4503599627370495ULL,
28         9007199254740991ULL, 18014398509481983ULL,
29         36028797018963967ULL, 72057594037927935ULL,
30         14411518807585871ULL, 288230376151711743ULL,
31         576460752303423487ULL, 1152921504606846975ULL,
32         2305843009213693951ULL, 4611686018427387903ULL,
33         9223372036854775807ULL, 18446744073709551615ULL};
34     static const unsigned int SZ = PREF + (MAXN + 63) / 64 + 1;
35     unsigned long long m[SZ] = {0};
36
37     inline unsigned int left(unsigned int v) const {
38         return (v - 62) * 64;
39     }
40
41     inline unsigned int parent(unsigned int v) const {
42         return v / 64 + 62;
43     }
44
45     inline void setbit(unsigned int v) {
46         m[v >> 6] |= 1ULL << (v & 63);
47     }
48
49     inline void resetbit(unsigned int v) {
50         m[v >> 6] &= ~(1ULL << (v & 63));
51     }
52
53     inline unsigned int getbit(unsigned int v) const {
54         return m[v >> 6] >> (v & 63) & 1;
55     }
56
57     inline unsigned long long childs_value(unsigned int v) const
58     {
59         return m[left(v) >> 6];
60     }
61
62     inline int left_go(unsigned int x, const unsigned int c)
63     const {
64         const unsigned long long rem = x & 63;
65         unsigned int bt = PREF * 64 + x;
66         unsigned long long num = m[bt >> 6] & lowest_bits11[rem + c
67             ];
68         if(num) {
69             return (x ^ rem) | __lg(num);
70         }
71         for(bt = parent(bt); bt > 62; bt = parent(bt)) {
72             const unsigned long long rem = bt & 63;
73             num = m[bt >> 6] & lowest_bits11[rem];
74             if(num) {
75                 bt = (bt ^ rem) | __lg(num);
76                 break;
77             }
78         }
79         if(bt == 62) {
80             return -1;
81         }
82         while(bt < PREF * 64) {
83             bt = left(bt) | __lg(m[bt - 62]);
84         }
85         return bt - PREF * 64;
86     }
87
88     inline int right_go(unsigned int x, const unsigned int c)
89     const {
90         const unsigned long long rem = x & 63;
91         unsigned int bt = PREF * 64 + x;
92         unsigned long long num = m[bt >> 6] & ~lowest_bits11[rem +
93             c];
94         if(num) {
95             return (x ^ rem) | __builtin_ctzll(num);
96         }
97         for(bt = parent(bt); bt > 62; bt = parent(bt)) {

```

```

22     const unsigned long long rem = bt & 63;
23     num = m[bt >> 6] & ~lowest_bitsll[rem + 1];
24     if(num) {
25         bt = (bt ^ rem) | __builtin_ctzll(num);
26         break;
27     }
28 }
29 if(bt == 62) {
30     return -1;
31 }
32 while(bt < PREF * 64) {
33     bt = left(bt) | __builtin_ctzll(m[bt - 62]);
34 }
35 return bt - PREF * 64;
36 }
37
38 public:
39 fast_set() {
40     assert(PREF != 228);
41     setbit(62);
42 }
43
44 bool empty() const {return getbit(63);}
45
46 void clear() {
47     fill(m, m + SZ, 0);
48     setbit(62);
49 }
50
51 bool count(unsigned int x) const {
52     return m[PREF + (x >> 6)] >> (x & 63) & 1;
53 }
54
55 void insert(unsigned int x) {
56     for(unsigned int v = PREF * 64 + x; !getbit(v); v = parent(
57         v)){
58         setbit(v);
59     }
60 }
61
62 void erase(unsigned int x) {
63     if(!getbit(PREF * 64 + x)) {
64         return;
65     }
66     resetbit(PREF * 64 + x);
67     for(unsigned int v = parent(PREF * 64 + x); v > 62 && !
68         childs_value(v); v = parent(v)) {
69         resetbit(v);
70     }
71 }
72
73 int find_next(unsigned int x) const {
74     return right_go(x, 0);
75 }
76
77 int find_prev(unsigned int x) const {
78     return left_go(x, 1);
79 }
80 };

```

1.11 DynamicSegtree

```

1
2 template<class T>struct dynamic_segment_tree{
3     struct node{
4         node *l = NULL,*r = NULL;
5         T sum;
6         node(T k = 0): sum(k){}
7         node(node *p){if(p)*this = *p;}
8         ~node(){
9             for(auto &i:{l,r})
10                 if(i)delete i;
11         }
12         void pull(){
13             sum = 0;
14             for(auto i:{l,r})
15                 if(i)sum+=i->sum;
16         }
17     }*root = NULL;
18     int n;
19     dynamic_segment_tree(){}
20     dynamic_segment_tree(const dynamic_segment_tree<T>&tmp){root
21         = new node(tmp.root);}
22     void update(node *&t,int pos,T k,int l,int r){
23         if(!t)t = new node();
24         if(l==r)return t = new node(k),void();
25         int m = (l+r)>>1;
26         t = new node(t);
27         if(pos<=m)update(t->l,pos,k,l,m);
28         else update(t->r,pos,k,m+1,r);
29         t->pull();
30     }void update(int pos,T k,int l = -1e9,int r = 1e9){update(
31         root,pos,k,l,r);}
32     T query(node *&t,int ql,int qr,int l,int r){

```

```

31     if(!t)return 0;
32     if(ql<=l and r<=qr)return t->sum;
33     int m = (l+r)>>1;
34     T ans = 0;
35     if(ql<=m)ans+=query(t->l,ql,qr,l,m);
36     if(qr>m)ans+=query(t->r,ql,qr,m+1,r);
37     return ans;
38 }T query(int ql,int qr,int l = -1e9,int r = 1e9){return query
39     (root,ql,qr,l,r);}
40 };

```

1.12 ZkwSegtree

```

1 template<class S,
2     S (*node_pull)(S, S),
3     S (*node_init)(),
4     class F,
5     S (*mapping)(S, F),
6     F (*tag_pull)(F, F),
7     F (*tag_init)()>
8 class segment_tree {
9 public:
10     segment_tree() : segment_tree(0) {}
11     explicit segment_tree(int _n) : segment_tree(vector<S>(_n,
12         node_init())) {}
13     explicit segment_tree(const vector<S>& v) : n((int) v.size())
14     {
15         log = std::__lg(2 * n - 1);
16         size = 1 << log;
17         d = vector<S>(size << 1, node_init());
18         lz = vector<F>(size, tag_init());
19         for(int i = 0; i < n; i++) {
20             d[size + i] = v[i];
21         }
22         for(int i = size - 1; i; --i) {
23             update(i);
24         }
25     }
26     void set(int p, S x) {
27         assert(0 <= p && p < n);
28         p += size;
29         for(int i = log; i; --i) {
30             push(p >> i);
31         }
32         d[p] = x;
33         for(int i = 1; i <= log; ++i) {
34             update(p >> i);
35         }
36     }
37     S get(int p) {
38         assert(0 <= p && p < n);
39         p += size;
40         for(int i = log; i; i--) {
41             push(p >> i);
42         }
43         return d[p];
44     }
45     S operator[](int p) {
46         return get(p);
47     }
48     S query(int l, int r) {
49         r++;
50         assert(l<=r);
51         l += size;
52         r += size;
53         for(int i = log; i; i--) {
54             if(((l >> i) << i) != 1) {
55                 push(l >> i);
56             }
57             if(((r >> i) << i) != r) {
58                 push(r >> i);
59             }
60         }
61         S sml = node_init(), smr = node_init();
62         while(l < r) {
63             if(l & 1) {
64                 sml = node_pull(sml, d[l++]);
65             }
66             if(r & 1) {
67                 smr = node_pull(d[--r], smr);
68             }
69             l >>= 1;
70             r >>= 1;
71         }
72         return node_pull(sml, smr);
73     }
74     void apply(int p, F f) {
75         assert(0 <= p && p < n);
76         p += size;
77         for(int i = log; i; i--) {
78             push(p >> i);
79         }
80         d[p] = mapping(f, d[p]);
81         for(int i = 1; i <= log; i++) {

```

```

80     update(p >> i);
81 }
82 }
83 void update(int l, int r, F f) {
84     r++;
85     assert(l<=r);
86     l += size;
87     r += size;
88     for(int i = log; i; i--) {
89         if(((l >> i) << i) != 1) {
90             push(l >> i);
91         }
92         if(((r >> i) << i) != r) {
93             push((r - 1) >> i);
94         }
95     }
96     {
97         int l2 = l, r2 = r;
98         while(l < r) {
99             if(l & 1) {
100                 all_apply(l++, f);
101             }
102             if(r & 1) {
103                 all_apply(--r, f);
104             }
105             l >>= 1;
106             r >>= 1;
107         }
108         l = l2;
109         r = r2;
110     }
111     for(int i = 1; i <= log; i++) {
112         if(((l >> i) << i) != 1) {
113             update(l >> i);
114         }
115         if(((r >> i) << i) != r) {
116             update((r - 1) >> i);
117         }
118     }
119 }
120 private:
121 int n, size, log;
122 vector<S> d;
123 vector<F> lz;
124 inline void update(int k) { d[k] = node_pull(d[k << 1], d[k
    << 1 | 1]); }
125 void all_apply(int k, F f) {
126     d[k] = mapping(d[k], f);
127     if(k < size) {
128         lz[k] = tag_pull(lz[k], f);
129     }
130 }
131 void push(int k) {
132     all_apply(k << 1, lz[k]);
133     all_apply(k << 1 | 1, lz[k]);
134     lz[k] = tag_init();
135 }
136 };

```

1.13 MoAlgo

```

1 struct qry{
2     int ql,qr,id;
3 };
4 template<class T>struct Mo{
5     int n,m;
6     vector<pii>ans;
7     Mo(int _n,int _m): n(_n),m(_m){
8         ans.resize(m);
9     }
10    void solve(vector<T>&v,vector<qry>&q){
11        int l = 0,r = -1;
12        vector<int>cnt,cntcnt;
13        cnt.resize(n+5);
14        cntcnt.resize(n+5);
15        int mx = 0;
16        function<void(int)>add = [&](int pos){
17            cntcnt[cnt[v[pos]]]--;
18            cnt[v[pos]]++;
19            cntcnt[cnt[v[pos]]]++;
20            mx = max(mx,cnt[v[pos]]);
21        };
22        function<void(int)>sub = [&](int pos){
23            if(--cntcnt[cnt[v[pos]]] and cnt[v[pos]]==mx)mx--;
24            cnt[v[pos]]--;
25            cntcnt[cnt[v[pos]]]++;
26            mx = max(mx,cnt[v[pos]]);
27        };
28        sort(all(q),[&](qry a,qry b){
29            static int B = max((int)1,n/max((int)sqrt(m),(int)1));
30            if(a.ql/B!=b.ql/B)return a.ql<b.ql;
31            if((a.ql/B)&1)return a.qr>b.qr;
32            return a.qr<b.qr;
33        });

```

```

34    for(auto [ql,qr,id]:q){
35        while(l>ql)add(--l);
36        while(r<qr)add(++r);
37        while(l<ql)sub(l++);
38        while(r>qr)sub(r--);
39        ans[id] = {mx,cntcnt[mx]};
40    }
41 }
42 };

```

1.14 Hash

```

1 struct custom_hash {
2     static uint64_t splitmix64(uint64_t x) {
3         x += 0x9e3779b97f4a7c15;
4         x = (x ^ (x >> 30)) * 0xbf58476d1ce4e5b9;
5         x = (x ^ (x >> 27)) * 0x94d049bb133111eb;
6         return x ^ (x >> 31);
7     }
8     size_t operator()(uint64_t x) const {
9         static const uint64_t FIXED_RANDOM = chrono::steady_clock::
            now().time_since_epoch().count();
10        return splitmix64(x + FIXED_RANDOM);
11    }
12    size_t operator()(pair<uint64_t,uint64_t> x) const {
13        static const uint64_t FIXED_RANDOM = chrono::steady_clock::
            now().time_since_epoch().count();
14        return splitmix64(3*x.first + x.second + FIXED_RANDOM);
15    }
16 };
17 template<class T,class U>using hash_map = gp_hash_table<T,U,
    custom_hash>;

```

1.15 RedBlackTree

```

1 template<class T, typename cmp=less<>>struct _tree{//#include<
    bits/extc++.h>
2     tree<pair<T,int>,null_type,cmp,rb_tree_tag,
        tree_order_statistics_node_update>st;
3     int id = 0;
4     void insert(T x){st.insert({x,id++});}
5     void erase(T x){st.erase(st.lower_bound({x,0}));}
6     int order_of_key(T x){return st.order_of_key(*st.lower_bound
        ({x,0}));}
7     T find_by_order(int x){return st.find_by_order(x)->first;}
8     T lower_bound(T x){return st.lower_bound({x,0})->first;}
9     T upper_bound(T x){return st.upper_bound({x,(int)1e9+7})->
        first;}
10    T smaller_bound(T x){return (--st.lower_bound({x,0}))->first
        ;}
11 };

```

2 Geometry

2.1 Theorem

- Pick' s Theorem

$$A = I + \frac{B}{2} - 1$$

$$A := Area$$

$$i := PointsInside$$

$$B := PointsBoundary$$

2.2 PointInPolygon

```

1 template<class T>
2 int PointInPolygon(const vector<Point<T>> &Poly, const Point<T>
    p){
3     int ans = 0;
4     for(auto a = --Poly.end(),b = Poly.begin();b!=Poly.end();a =
        b++){
5         if(PointOnSegment(*a,*b,p)){
6             return -1;
7         }
8         if(seg_intersect(p,p+Point<T>(2e9+7,1),*a,*b)){
9             ans = !ans;
10        }
11    }
12    return ans;
13 }

```

2.3 PointInConvex

```

1 template<class T>
2 int PointInConvex(const vector<Point<T>>&C, const Point<T>&p){
3     if(btw(C[0], C[1], p) || btw(C[0], C.back(), p)) return -1;
4     int l = 0, r = (int)C.size() - 1;
5     while(l <= r){
6         int m = (l + r) >> 1;
7         auto a1 = (C[m] - C[0]) ^ (p - C[0]);
8         auto a2 = (C[(m+1)%C.size()] - C[0]) ^ (p - C[0]);
9         if(a1 >= 0 and a2 <= 0){
10             auto res = (C[(m+1)%C.size()] - C[m]) ^ (p - C[m]);
11             return res > 0 ? 1 : (res >= 0 ? -1 : 0);
12         }
13         if(a1 < 0) r = m - 1;
14         else l = m + 1;
15     }
16     return 0;
17 }

```

2.4 MaximumDistance

```

1 template<class T>
2 T MaximumDistance(vector<Point<T>>&p){
3     vector<Point<T>>C = ConvexHull(p, 0);
4     int n = C.size(), t = 2;
5     T ans = 0;
6     for(int i = 0; i < n; i++){
7         while(((C[i] - C[t]) ^ (C[(i+1)%n] - C[t])) < ((C[i] - C[(t+1)%n]) ^ (C[(i+1)%n] - C[(t+1)%n]))) t = (t + 1) % n;
8         ans = max({ans, abs2(C[i] - C[t]), abs2(C[(i+1)%n] - C[t])});
9     }
10    return ans;
11 }

```

2.5 PolarAngleSort

```

1 template<class T>
2 bool cmp(const Point<T> &a, const Point<T> &b){
3     int lhs = (a.y < 0 || a.y == 0 && a.x > 0) ? 0 : (1 + (a.x != 0 || a.y != 0));
4     int rhs = (b.y < 0 || b.y == 0 && b.x > 0) ? 0 : (1 + (b.x != 0 || b.y != 0));
5     if(lhs != rhs) {
6         return lhs < rhs;
7     }
8     long long area = (a ^ b);
9     return area ? area > 0 : abs(a.x) + abs(a.y) < abs(b.x) + abs(b.y);
10 }

```

2.6 MinimumDistance

```

1 template<class T>
2 T MinimumDistance(vector<Point<T>>&p, int l = -1, int r = -1){
3     if(l == -1 and r == -1){
4         sort(p.begin(), p.end(), [](Point<T> a, Point<T> b){
5             if(a.x != b.x) return a.x < b.x;
6             return a.y < b.y;
7         });
8         p.erase(unique(p.begin(), p.end()), p.end());
9         return MinimumDistance(p, 0, p.size() - 1);
10    }
11    if(l == r) return numeric_limits<T>::max();
12    int m = (l + r) >> 1, mid_pos = p[m].x;
13    T ans = min(MinimumDistance(p, l, m), MinimumDistance(p, m + 1, r));
14    vector<Point<T>>tmp((r - l + 1), Point<T>(0, 0));
15    merge(p.begin() + l, p.begin() + m + 1, p.begin() + m + 1, p.begin() + r + 1,
16          tmp.begin(), [](Point<T> a, Point<T> b){ return a.y < b.y; });
17    tmp.clear();
18    for(int i = l; i <= r; i++){
19        if((p[i].x - mid_pos) * (p[i].x - mid_pos) < ans){
20            tmp.push_back(p[i]);
21        }
22    }
23    int n = tmp.size();
24    for(int i = 0; i < n; i++){
25        for(int j = i + 1; j < n; j++){
26            ans = min(ans, abs2(tmp[i] - tmp[j]));
27            if(((tmp[i].y - tmp[j].y) * (tmp[i].y - tmp[j].y)) > ans){
28                break;
29            }
30        }
31    }
32 }

```

```

31 }
32 return ans;
33 }

```

2.7 ConvexHull

```

1 template<class T>
2 vector<Point<T>> ConvexHull(vector<Point<T>> v, bool Boundary = 1){
3     sort(begin(v), end(v), [](Point<T> &a, Point<T> &b){
4         if(a.x != b.x) return a.x < b.x;
5         return a.y < b.y;
6     });
7     vector<Point<T>>ans;
8     int t = 1;
9     auto add = [](Point<T> &p){
10         while(ans.size() > t and ((p - ans[ans.size() - 2]) ^ (ans.back() - ans[ans.size() - 2])) > (Boundary ? 0 : 0 - eps))
11             ans.pop_back();
12         ans.push_back(p);
13     };
14     for(int i = 0; i < v.size(); ++i) add(v[i]);
15     t = ans.size();
16     for(int i = (int)(v.size()) - 2; i >= 0; --i) add(v[i]);
17     if(v.size() > 1) ans.pop_back();
18     return ans;
19 }

```

2.8 Template

```

1 template<class T>
2 struct Point{
3     T x, y;
4     Point(T x = 0, T y = 0) : x(x), y(y) {}
5     Point operator + (const Point &b) const {
6         return Point(x + b.x, y + b.y);
7     }
8     Point operator - (const Point &b) const {
9         return Point(x - b.x, y - b.y);
10    }
11    Point operator * (T b) const {
12        return Point(x * b, y * b);
13    }
14    Point operator / (T b) const {
15        return Point(x / b, y / b);
16    }
17    T operator * (const Point &b) const {
18        return x * b.x + y * b.y;
19    }
20    T operator ^ (const Point &b) const {
21        return x * b.y - y * b.x;
22    }
23 };
24 int sign(double a){
25     return fabs(a) < eps ? 0 : a > 0 ? 1 : -1;
26 }
27 template<class T>
28 double abs(const Point<T>&p){
29     return sqrt(1 + p * p);
30 }
31 template<class T>
32 T abs2(const Point<T>&p){
33     return p * p;
34 }
35 template<class T>
36 int ori(Point<T> a, Point<T> b, Point<T> c){
37     return sign((b - a) ^ (c - a));
38 }
39 template<class T>
40 bool collinearity(Point<T> p1, Point<T> p2, Point<T> p3){
41     return sign((p1 - p3) ^ (p2 - p3)) == 0;
42 }
43 template<class T>
44 bool btw(Point<T> p1, Point<T> p2, Point<T> p3) {
45     if(!collinearity(p1, p2, p3)) return 0;
46     return sign((p1 - p3) * (p2 - p3)) <= 0;
47 }
48 template<class T>
49 bool PointOnSegment(const Point<T> &p1, const Point<T> &p2, const Point<T> &p3){
50     return collinearity(p1, p2, p3) && btw(p1, p2, p3);
51 }
52 template<class T>
53 bool seg_intersect(Point<T> p1, Point<T> p2, Point<T> p3, Point<T> p4) {
54     int a123 = ori(p1, p2, p3);
55     int a124 = ori(p1, p2, p4);
56     int a341 = ori(p3, p4, p1);
57     int a342 = ori(p3, p4, p2);
58     if(a123 == 0 && a124 == 0)

```



```

59     return btw(p1, p2, p3) || btw(p1, p2, p4) || btw(p3, p4, p1
60         ) || btw(p3, p4, p2);
61     return a123 * a124 <= 0 && a341 * a342 <= 0;
62 }
63 template<class T>
64 double area(vector<Point<T>> v){
65     if(v.size()<=2)return 0;
66     double ans = 0;
67     for(int i = 1;i<v.size()-1;++i){
68         ans+=((v[i]-v[0])^(v[i+1]-v[0]));
69     }
70     return abs(ans)/2.;
71 }

```

3 Graph

3.1 HLD

```

1 struct heavy_light_decomposition{
2     int n;
3     vector<int>dep,father,sz,mxson,topf,id;
4     vector<vector<int>>>g;
5     heavy_light_decomposition(int _n = 0) : n(_n) {
6         g.resize(n+5);
7         dep.resize(n+5);
8         father.resize(n+5);
9         sz.resize(n+5);
10        mxson.resize(n+5);
11        topf.resize(n+5);
12        id.resize(n+5);
13    }
14    void add_edge(int u, int v){
15        g[u].push_back(v);
16        g[v].push_back(u);
17    }
18    void dfs(int u,int p){
19        dep[u] = dep[p]+1;
20        father[u] = p;
21        sz[u] = 1;
22        mxson[u] = 0;
23        for(auto v:g[u]){
24            if(v==p)continue;
25            dfs(v,u);
26            sz[u]+=sz[v];
27            if(sz[v]>sz[mxson[u]])mxson[u] = v;
28        }
29    }
30    void dfs2(int u,int top){
31        static int idn = 0;
32        topf[u] = top;
33        id[u] = ++idn;
34        if(mxson[u])dfs2(mxson[u],top);
35        for(auto v:g[u]){
36            if(v!=father[u] and v!=mxson[u]){
37                dfs2(v,v);
38            }
39        }
40    }
41    void build(int root){
42        dfs(root,0);
43        dfs2(root,root);
44    }
45    vector<pair<int, int>> path(int u,int v){
46        vector<pair<int, int>>ans;
47        while(topf[u]!=topf[v]){
48            if(dep[topf[u]]<dep[topf[v]])swap(u,v);
49            ans.push_back({id[topf[u]], id[u]});
50            u = father[topf[u]];
51        }
52        if(id[u]>id[v])swap(u,v);
53        ans.push_back({id[u], id[v]});
54        return ans;
55    }
56 };

```

3.2 Bridges

```

1 vector<pii> findBridges(const vector<vector<int>>& g) {
2     int n = (int) g.size();
3     vector<int> id(n, -1), low(n);
4     vector<pii> bridges;
5     function<void(int, int)> dfs = [&](int u, int p) {
6         static int cnt = 0;
7         id[u] = low[u] = cnt++;
8         for(auto v : g[u]) {
9             if(v == p) continue;
10            if(id[v] != -1) low[u] = min(low[u], id[v]);
11            else {
12                dfs(v, u);

```

```

13                low[u] = min(low[u], low[v]);
14                if(low[v] > id[u]) bridges.EB(u, v);
15            }
16        }
17    };
18    for(int i = 0; i < n; ++i) {
19        if(id[i] == -1) dfs(i, -1);
20    }
21    return bridges;
22 }

```

3.3 TwoSat

```

1 struct two_sat{
2     SCC s;
3     vector<bool>ans;
4     int have_ans = 0;
5     int n;
6     two_sat(int _n) : n(_n) {
7         ans.resize(n+1);
8         s = SCC(2*n);
9     }
10    int inv(int x){
11        if(x>n)return x-n;
12        return x+n;
13    }
14    void add_or_clause(int u, bool x, int v, bool y){
15        if(!x)u = inv(u);
16        if(!y)v = inv(v);
17        s.add_edge(inv(u), v);
18        s.add_edge(inv(v), u);
19    }
20    void check(){
21        if(have_ans!=0)return;
22        s.build();
23        for(int i = 0;i<=n;++i){
24            if(s.scc[i]==s.scc[inv(i)]){
25                have_ans = -1;
26                return;
27            }
28            ans[i] = (s.scc[i]<s.scc[inv(i)]);
29        }
30        have_ans = 1;
31    }
32 };

```

3.4 MCMF

```

1 template<class Cap_t, class Cost_t>
2 class MCMF {
3 public:
4     struct Edge {
5         int from;
6         int to;
7         Cap_t cap;
8         Cost_t cost;
9         Edge(int u, int v, Cap_t _cap, Cost_t _cost) : from(u), to(
10            v), cap(_cap), cost(_cost) {}
11    };
12    static constexpr Cap_t EPS = static_cast<Cap_t>(1e-9);
13    int n;
14    vector<Edge> edges;
15    vector<vector<int>> g;
16    vector<Cost_t> d;
17    vector<bool> in_queue;
18    vector<int> previous_edge;
19
20    MCMF() {}
21    MCMF(int _n) : n(_n+1), g(_n+1), d(_n+1), in_queue(_n+1),
22        previous_edge(_n+1) {}
23
24    void add_edge(int u, int v, Cap_t cap, Cost_t cost) {
25        assert(0 <= u && u < n);
26        assert(0 <= v && v < n);
27        g[u].push_back(edges.size());
28        edges.emplace_back(u, v, cap, cost);
29        g[v].push_back(edges.size());
30        edges.emplace_back(v, u, 0, -cost);
31    }
32
33    bool spfa(int s, int t) {
34        bool found = false;
35        fill(d.begin(), d.end(), numeric_limits<Cost_t>::max());
36        d[s] = 0;
37        in_queue[s] = true;
38        queue<int> que;
39        que.push(s);
40        while(!que.empty()) {
41            int u = que.front();

```

```

42     que.pop();
43     if(u == t) {
44         found = true;
45     }
46     in_queue[u] = false;
47     for(auto& id : g[u]) {
48         const Edge& e = edges[id];
49         if(e.cap > EPS && d[u] + e.cost < d[e.to]) {
50             d[e.to] = d[u] + e.cost;
51             previous_edge[e.to] = id;
52             if(!in_queue[e.to]) {
53                 que.push(e.to);
54                 in_queue[e.to] = true;
55             }
56         }
57     }
58 }
59 return found;
60 }
61
62 pair<Cap_t, Cost_t> flow(int s, int t, Cap_t f =
    numeric_limits<Cap_t>::max()) {
63     assert(0 <= s && s < n);
64     assert(0 <= t && t < n);
65     Cap_t cap = 0;
66     Cost_t cost = 0;
67     while(f > 0 && spfa(s, t)) {
68         Cap_t send = f;
69         int u = t;
70         while(u != s) {
71             const Edge& e = edges[previous_edge[u]];
72             send = min(send, e.cap);
73             u = e.from;
74         }
75         u = t;
76         while(u != s) {
77             Edge& e = edges[previous_edge[u]];
78             e.cap -= send;
79             Edge& b = edges[previous_edge[u] ^ 1];
80             b.cap += send;
81             u = e.from;
82         }
83         cap += send;
84         f -= send;
85         cost += send * d[t];
86     }
87     return make_pair(cap, cost);
88 }
89 };

```

3.5 LCA

```

1 vector<vector<int>>>g,dp;
2 vector<int>deep;
3 void build(int root,int n){
4     dp.assign(25,vector<int>(n+5));
5     deep.assign(n+5,0);
6     function<void(int,int,int)>dfs = [&](int u,int p,int dis){
7         dp[0][u] = p;
8         deep[u] = dis;
9         for(auto v:g[u]){
10             if(v==p)continue;
11             dfs(v,u,dis+1);
12         }
13     };
14     dfs(root,0,1);
15     for(int i = 1;i<=20;++i){
16         for(int j = 1;j<=n;++j){
17             dp[i][j] = dp[i-1][dp[i-1][j]];
18         }
19     }
20 }
21 int LCA(int u,int v){
22     if(deep[u]<deep[v])swap(u,v);
23     for(int i = 20;i>=0;--i){
24         if(deep[dp[i][u]]>=deep[v])
25             u = dp[i][u];
26     }
27     if(u==v)return u;
28     for(int i = 20;i>=0;--i){
29         if(dp[i][u]!=dp[i][v])u = dp[i][u],v = dp[i][v];
30     }
31     return dp[0][u];
32 }

```

3.6 CentroidDecomposition

```

1 vector<vector<int>>>g;
2 vector<int>sz,tmp;
3 vector<bool>vis; //visit_centroid
4 int tree_centroid(int u,int n){

```

```

5     function<void(int,int)>dfs1 = [&](int u,int p){
6         sz[u] = 1;
7         for(auto v:g[u]){
8             if(v==p)continue;
9             if(vis[v])continue;
10            dfs1(v,u);
11            sz[u]+=sz[v];
12        }
13    };
14    function<int(int,int)>dfs2 = [&](int u,int p){
15        for(auto v:g[u]){
16            if(v==p)continue;
17            if(vis[v])continue;
18            if(sz[v]*2<n)continue;
19            return dfs2(v,u);
20        }
21        return u;
22    };
23    dfs1(u,-1);
24    return dfs2(u,-1);
25 }
26 int cal(int u,int p = -1,int deep = 1){
27     int ans = 0;
28     tmp.pb(deep);
29     sz[u] = 1;
30     for(auto v:g[u]){
31         if(v==p)continue;
32         if(vis[v])continue;
33         ans+=cal(v,u,deep+1);
34         sz[u]+=sz[v];
35     }
36     //calcuat the answer
37     return ans;
38 }
39 int centroid_decomposition(int u,int tree_size){
40     int center = tree_centroid(u,tree_size);
41     vis[center] = 1;
42     int ans = 0;
43     for(auto v:g[center]){
44         if(vis[v])continue;
45         ans+=cal(v);
46         for(int i = sz(tmp)-sz[v];i<sz(tmp);++i){
47             //update
48         }
49     }
50     while(!tmp.empty()){
51         //roll_back(tmp.back())
52         tmp.pop_back();
53     }
54     for(auto v:g[center]){
55         if(vis[v])continue;
56         ans+=centroid_decomposition(v,sz[v]);
57     }
58     return ans;
59 }

```

3.7 BCC AP

```

1 struct BCC_AP{
2     int dfn_cnt = 0,bcc_cnt = 0,n;
3     vector<int>dfn,low,ap,bcc_id;
4     stack<int>st;
5     vector<bool>vis,is_ap;
6     vector<vector<int>>>bcc;
7     BCC_AP(int _n):n(_n){
8         dfn.resize(n+5),low.resize(n+5),bcc.resize(n+5),vis.resize(
9             n+5),is_ap.resize(n+5),bcc_id.resize(n+5);
10    }
11    inline void build(const vector<vector<int>>>&g,int u,int p =
12        -1){
13        int child = 0;
14        dfn[u] = low[u] = ++dfn_cnt;
15        st.push(u);
16        vis[u] = 1;
17        if(g[u].empty() and p!=-1){
18            bcc_id[u] = ++bcc_cnt;
19            bcc[bcc_cnt].push_back(u);
20            return;
21        }
22        for(auto v:g[u]){
23            if(v==p)continue;
24            if(!dfn[v]){
25                build(g,v,u);
26                child++;
27                if(dfn[u]<=low[v]){
28                    is_ap[u] = 1;
29                    bcc_id[u] = ++bcc_cnt;
30                    bcc[bcc_cnt].push_back(u);
31                    while(vis[v]){
32                        bcc_id[st.top()] = bcc_cnt;
33                        bcc[bcc_cnt].push_back(st.top());
34                        vis[st.top()] = 0;
35                        st.pop();
36                    }
37                }
38            }
39        }
40    }

```



```

35     }
36     low[u] = min(low[u], low[v]);
37 }
38 low[u] = min(low[u], dfn[v]);
39 }
40 if(p == -1 and child < 2) is_ap[u] = 0;
41 if(is_ap[u]) ap.push_back(u);
42 }
43 };

```

3.8 SCC

```

1 struct SCC{
2     int n, cnt = 0, dfn_cnt = 0;
3     vector<vector<int>>>g;
4     vector<int>sz, scc, low, dfn;
5     stack<int>st;
6     vector<bool>vis;
7     SCC(int _n = 0) : n(_n){
8         sz.resize(n+5), scc.resize(n+5), low.resize(n+5), dfn.resize(n
9             +5), vis.resize(n+5);
10        g.resize(n+5);
11    }
12    inline void add_edge(int u, int v){
13        g[u].push_back(v);
14    }
15    inline void build(){
16        function<void(int, int)>dfs = [&](int u, int dis){
17            low[u] = dfn[u] = ++dfn_cnt, vis[u] = 1;
18            st.push(u);
19            for(auto v : g[u]){
20                if(!dfn[v]){
21                    dfs(v, dis+1);
22                    low[u] = min(low[u], low[v]);
23                }
24                else if(vis[v]){
25                    low[u] = min(low[u], dfn[v]);
26                }
27            }
28            if(low[u] == dfn[u]){
29                ++cnt;
30                while(vis[u]){
31                    auto v = st.top();
32                    st.pop();
33                    vis[v] = 0;
34                    scc[v] = cnt;
35                    sz[cnt]++;
36                }
37            }
38            for(int i = 0; i <= n; ++i){
39                if(!scc[i]){
40                    dfs(i, 1);
41                }
42            }
43        }
44        vector<vector<int>>> compress(){
45            vector<vector<int>>>ans(cnt+1);
46            for(int u = 0; u <= n; ++u){
47                for(auto v : g[u]){
48                    if(scc[u] == scc[v]){
49                        continue;
50                    }
51                    ans[scc[u]].push_back(scc[v]);
52                }
53            }
54            for(int i = 0; i <= cnt; ++i){
55                sort(ans[i].begin(), ans[i].end());
56                ans[i].erase(unique(ans[i].begin(), ans[i].end()), ans[i]
57                    .end());
58            }
59            return ans;
60        };

```

3.9 LineContainer

```

1 template<class T>
2 T floor_div(T a, T b) {
3     return a / b - ((a ^ b) < 0 && a % b != 0);
4 }
5
6 template<class T>
7 T ceil_div(T a, T b) {
8     return a / b + ((a ^ b) > 0 && a % b != 0);
9 }
10
11 namespace line_container_internal {
12
13 struct line_t {
14     mutable long long k, m, p;

```

```

15
16     inline bool operator<(const line_t& o) const { return k < o.k
17         ; }
18     inline bool operator<(long long x) const { return p < x; }
19 };
20 // LineContainer_internal
21
22 template<bool MAX>
23 struct line_container : std::multiset<line_container_internal::
24     line_t, std::less<>> {
25     static const long long INF = std::numeric_limits<long long>::
26         max();
27
28     bool isect(iterator x, iterator y) {
29         if(y == end()) {
30             x->p = INF;
31             return 0;
32         }
33         if(x->k == y->k) {
34             x->p = (x->m > y->m ? INF : -INF);
35         }
36         else {
37             x->p = floor_div(y->m - x->m, x->k - y->k);
38         }
39         return x->p >= y->p;
40     }
41
42     void add_line(long long k, long long m) {
43         if(!MAX) {
44             k = -k;
45             m = -m;
46         }
47         auto z = insert({k, m, 0}), y = z++, x = y;
48         while(isect(y, z)) {
49             z = erase(z);
50         }
51         if(x != begin() && isect(--x, y)) {
52             isect(x, y = erase(y));
53         }
54         while((y = x) != begin() && (--x)->p >= y->p) {
55             isect(x, erase(y));
56         }
57     }
58
59     long long get(long long x) {
60         assert(!empty());
61         auto l = *lower_bound(x);
62         return (1.l * x + 1.m) * (MAX ? +1 : -1);
63     }
64 };

```

3.10 Dinic

```

1 template<class T>
2 struct Dinic{
3     struct edge{
4         int from, to;
5         T cap;
6         edge(int _from, int _to, T _cap) : from(_from), to(_to),
7             cap(_cap) {}
8     };
9     int n;
10    vector<edge> edges;
11    vector<vector<int>>> g;
12    vector<int> cur, h;
13    Dinic(int _n) : n(_n+1), g(_n+1) {}
14    void add_edge(int u, int v, T cap){
15        g[u].push_back(edges.size());
16        edges.push_back(edge(u, v, cap));
17        g[v].push_back(edges.size());
18        edges.push_back(edge(v, u, 0));
19    }
20    bool bfs(int s, int t){
21        h.assign(n, -1);
22        h[s] = 0;
23        queue<int> que;
24        que.push(s);
25        while(!que.empty()) {
26            int u = que.front();
27            que.pop();
28            for(auto id : g[u]) {
29                const edge& e = edges[id];
30                int v = e.to;
31                if(e.cap > 0 && h[v] == -1) {
32                    h[v] = h[u] + 1;
33                    if(v == t) {
34                        return 1;
35                    }
36                    que.push(v);
37                }
38            }
39        }
40        return 0;

```

```

41 T dfs(int u, int t, T f) {
42     if(u == t) {
43         return f;
44     }
45     T r = f;
46     for(int& i = cur[u]; i < (int) g[u].size(); ++i) {
47         int id = g[u][i];
48         const edge& e = edges[id];
49         int v = e.to;
50         if(e.cap > 0 && h[v] == h[u] + 1) {
51             T send = dfs(v, t, min(r, e.cap));
52             edges[id].cap -= send;
53             edges[id ^ 1].cap += send;
54             r -= send;
55             if(r == 0) {
56                 return f;
57             }
58         }
59     }
60     return f - r;
61 }
62 T flow(int s, int t, T f = numeric_limits<T>::max()) {
63     T ans = 0;
64     while(f > 0 && bfs(s, t)) {
65         cur.assign(n, 0);
66         T send = dfs(s, t, f);
67         ans += send;
68         f -= send;
69     }
70     return ans;
71 }
72 vector<pair<int,int>> min_cut(int s) {
73     vector<bool> vis(n);
74     vis[s] = true;
75     queue<int> que;
76     que.push(s);
77     while(!que.empty()) {
78         int u = que.front();
79         que.pop();
80         for(auto id : g[u]) {
81             const auto& e = edges[id];
82             int v = e.to;
83             if(e.cap > 0 && !vis[v]) {
84                 vis[v] = true;
85                 que.push(v);
86             }
87         }
88     }
89     vector<pair<int,int>> cut;
90     for(int i = 0; i < (int) edges.size(); i += 2) {
91         const auto& e = edges[i];
92         if(vis[e.from] && !vis[e.to]) {
93             cut.push_back(make_pair(e.from, e.to));
94         }
95     }
96     return cut;
97 }
98 };

```

4 Math

4.1 Numbers

- Bernoulli numbers

$$B_0 = 1, B_1^\pm = \pm \frac{1}{2}, B_2 = \frac{1}{6}, B_3 = 0$$

$$\sum_{j=0}^m \binom{m+1}{j} B_j = 0, \text{EGF is } B(x) = \frac{x}{e^x - 1} = \sum_{n=0}^{\infty} B_n \frac{x^n}{n!}.$$

$$S_m(n) = \sum_{k=1}^n k^m = \frac{1}{m+1} \sum_{k=0}^m \binom{m+1}{k} B_k^+ n^{m+1-k}$$

- Stirling numbers of the second kind Partitions of n distinct elements into exactly k groups.

$$S(n, k) = S(n-1, k-1) + kS(n-1, k), S(n, 1) = S(n, n) = 1$$

$$S(n, k) = \frac{1}{k!} \sum_{i=0}^k (-1)^{k-i} \binom{k}{i} i^n$$

$$x^n = \sum_{i=0}^n S(n, i) (x)_i$$

- Pentagonal number theorem

$$\prod_{n=1}^{\infty} (1 - x^n) = 1 + \sum_{k=1}^{\infty} (-1)^k \left(x^{k(3k+1)/2} + x^{k(3k-1)/2} \right)$$

- Catalan numbers

$$C_n^{(k)} = \frac{1}{(k-1)n+1} \binom{kn}{n}$$

$$C^{(k)}(x) = 1 + x[C^{(k)}(x)]^k$$

- Eulerian numbers

Number of permutations $\pi \in S_n$ in which exactly k elements are greater than the previous element. k j:s s.t. $\pi(j) > \pi(j+1)$, $k+1$ j:s s.t. $\pi(j) \geq j$, k j:s s.t. $\pi(j) > j$.

$$E(n, k) = (n-k)E(n-1, k-1) + (k+1)E(n-1, k)$$

$$E(n, 0) = E(n, n-1) = 1$$

$$E(n, k) = \sum_{j=0}^k (-1)^j \binom{n+1}{j} (k+1-j)^n$$

4.2 ExtendGCD

```

1 // @return $x, $y s.t. $ax + by = \gcd(a, b)$
2 ll ext_gcd(ll a, ll b, ll& x, ll& y) {
3     if(b == 0) {
4         x = 1; y = 0;
5         return a;
6     }
7     ll x2, y2;
8     ll c = a % b;
9     if(c < 0) c += b;
10    ll g = ext_gcd(b, c, x2, y2);
11    x = y2;
12    y = x2 - (a / b) * y2;
13    return g;
14 }

```

4.3 BerlekampMassey

```

1 template <typename Tfield>
2 std::pair<int, std::vector<Tfield>> find_linear_recurrence(
3     const std::vector<Tfield> &S) {
4     int N = S.size();
5     using poly = std::vector<Tfield>;
6     poly C_reversed{1}, B{1};
7     int L = 0, m = 1;
8     Tfield b = 1;
9
10    // adjust: C(x) <- C(x) - (d / b) x^m B(x)
11    auto adjust = [](poly C, const poly &B, Tfield d, Tfield b,
12        int m) -> poly {
13        C.resize(std::max(C.size(), B.size() + m));
14        Tfield a = d / b;
15        for (unsigned i = 0; i < B.size(); i++) C[i + m] -= a * B[i];
16        return C;
17    };
18
19    for (int n = 0; n < N; n++) {
20        Tfield d = S[n];
21        for (int i = 1; i <= L; i++) d += C_reversed[i] * S[n - i];
22
23        if (d == 0) m++;
24        else if (2 * L <= n) {
25            poly T = C_reversed;
26            C_reversed = adjust(C_reversed, B, d, b, m);
27            L = n + 1 - L;
28            B = T;
29            b = d;
30            m = 1;
31        } else {
32            C_reversed = adjust(C_reversed, B, d, b, m++);
33        }
34    }
35
36    // Calculate $x^N \bmod f(x)$
37    // Known as `Kitamasa method`
38    // Input: f_reversed: monic, reversed (f_reversed[0] = 1)
39    // Complexity: $O(K^2 \log N)$ ($K$: deg. of $f$)
40    // Example: (4, [1, -1, -1]) -> [2, 3]
41    // (x^4 = (x^2 + x + 2)(x^2 - x - 1) + 3x + 2)
42    // Reference: http://misawa.github.io/others/fast_kitamasa_method.html
43    // http://sugarknri.hatenablog.com/entry/2017/11/18/233936
44    template <typename Tfield>
45    std::vector<Tfield> monomial_mod_polynomial(long long N, const
46        std::vector<Tfield> &f_reversed) {
47        assert(!f_reversed.empty() and f_reversed[0] == 1);
48        int K = f_reversed.size() - 1;
49        if (!K) return {};
50        int D = 64 - __builtin_clzll(N);
51        std::vector<Tfield> ret(K, 0);
52        ret[0] = 1;
53        auto self_conv = [](std::vector<Tfield> x) -> std::vector<
54            Tfield> {
55            int d = x.size();
56            std::vector<Tfield> ret(d * 2 - 1);

```

```

55     for (int i = 0; i < d; i++) {
56         ret[i * 2] += x[i] * x[i];
57         for (int j = 0; j < i; j++) ret[i + j] += x[i] * x[
            j] * 2;
58     }
59     return ret;
60 };
61 for (int d = D; d--;) {
62     ret = self_conv(ret);
63     for (int i = 2 * K - 2; i >= K; i--) {
64         for (int j = 1; j <= K; j++) ret[i - j] -= ret[i] *
            f_reversed[j];
65     }
66     ret.resize(K);
67     if ((N >> d) & 1) {
68         std::vector<Tfield> c(K);
69         c[0] = -ret[K - 1] * f_reversed[K];
70         for (int i = 1; i < K; i++) { c[i] = ret[i - 1] -
            ret[K - 1] * f_reversed[K - i]; }
71         ret = c;
72     }
73 }
74 return ret;
75 }
76
77 // Guess k-th element of the sequence, assuming linear
78 // recurrence
79 // initial_elements: 0-ORIGIN
80 // Verify: abc198f https://atcoder.jp/contests/abc198/
81 // submissions/21837815
82 template <typename Tfield>
83 Tfield guess_kth_term(const std::vector<Tfield> &
84     initial_elements, long long k) {
85     assert(k >= 0);
86     if (k < static_cast<long long>(initial_elements.size()))
87         return initial_elements[k];
88     const auto f = find_linear_recurrence<Tfield>(
89         initial_elements).second;
90     const auto g = monomial_mod_polynomial<Tfield>(k, f);
91     Tfield ret = 0;
92     for (unsigned i = 0; i < g.size(); i++) ret += g[i] *
93         initial_elements[i];
94     return ret;
95 }

```

4.4 InvGCD

```

1 pair<long long, long long> inv_gcd(long long a, long long b) {
2     a %= b;
3     if(a < 0) a += b;
4     if(a == 0) return {b, 0};
5     long long s = b, t = a;
6     long long m0 = 0, m1 = 1;
7     while(t) {
8         long long u = s / t;
9         s -= t * u;
10        m0 -= m1 * u;
11        swap(s, t);
12        swap(m0, m1);
13    }
14    if(m0 < 0) m0 += b / s;
15    return {s, m0};
16 }

```

4.5 Generating Functions

- Ordinary Generating Function $A(x) = \sum_{i \geq 0} a_i x^i$

$$\begin{aligned}
 & - A(rx) \Rightarrow r^n a_n \\
 & - A(x) + B(x) \Rightarrow a_n + b_n \\
 & - A(x)B(x) \Rightarrow \sum_{i=0}^n a_i b_{n-i} \\
 & - A(x)^k \Rightarrow \sum_{i_1+i_2+\dots+i_k=n} a_{i_1} a_{i_2} \dots a_{i_k} \\
 & - xA(x)' \Rightarrow na_n \\
 & - \frac{A(x)}{1-x} \Rightarrow \sum_{i=0}^n a_i
 \end{aligned}$$

- Exponential Generating Function $A(x) = \sum_{i \geq 0} \frac{a_i}{i!} x^i$

$$\begin{aligned}
 & - A(x) + B(x) \Rightarrow a_n + b_n \\
 & - A^{(k)}(x) \Rightarrow a_{n+k} \\
 & - A(x)B(x) \Rightarrow \sum_{i=0}^n \binom{n}{i} a_i b_{n-i} \\
 & - A(x)^k \Rightarrow \sum_{i_1+i_2+\dots+i_k=n} \binom{n}{i_1, i_2, \dots, i_k} a_{i_1} a_{i_2} \dots a_{i_k} \\
 & - xA(x) \Rightarrow na_n
 \end{aligned}$$

- Special Generating Function

$$\begin{aligned}
 & - (1+x)^n = \sum_{i \geq 0} \binom{n}{i} x^i \\
 & - \frac{1}{(1-x)^n} = \sum_{i \geq 0} \binom{n-1}{i} x^i
 \end{aligned}$$

4.6 Theorem

- Modular Arithmetic

$$(a + b) \bmod m = (a \bmod m + b \bmod m) \bmod m$$

$$(a - b) \bmod m = (a \bmod m - b \bmod m) \bmod m$$

$$(a \cdot b) \bmod m = ((a \bmod m) \cdot (b \bmod m)) \bmod m$$

$$a^b \bmod m = (a \bmod m)^{b \bmod m-1} \bmod m$$

- Cramer's rule

$$\begin{aligned}
 ax + by &= e & x &= \frac{ed - bf}{ad - bc} \\
 cx + dy &= f & y &= \frac{af - ec}{ad - bc}
 \end{aligned}$$

- Kirchhoff's Theorem

Denote L be a $n \times n$ matrix as the Laplacian matrix of graph G , where $L_{ii} = d(i)$, $L_{ij} = -c$ where c is the number of edge (i, j) in G .

- The number of undirected spanning in G is $|\det(\tilde{L}_{11})|$.
- The number of directed spanning tree rooted at r in G is $|\det(\tilde{L}_{rr})|$.

- Tutte's Matrix

Let D be a $n \times n$ matrix, where $d_{ij} = x_{ij}$ (x_{ij} is chosen uniformly at random) if $i < j$ and $(i, j) \in E$, otherwise $d_{ij} = -d_{ji}$. $\frac{\text{rank}(D)}{2}$ is the maximum matching on G .

- Cayley's Formula

- Given a degree sequence d_1, d_2, \dots, d_n for each labeled vertices, there are $\frac{(n-2)!}{(d_1-1)!(d_2-1)!\dots(d_n-1)!}$ spanning trees.
- Let $T_{n,k}$ be the number of labeled forests on n vertices with k components, such that vertex $1, 2, \dots, k$ belong to different components. Then $T_{n,k} = kn^{n-k-1}$.

- Erdős–Gallai theorem

A sequence of nonnegative integers $d_1 \geq \dots \geq d_n$ can be represented as the degree sequence of a finite simple graph on n vertices if and only if $d_1 + \dots + d_n$

is even and $\sum_{i=1}^k d_i \leq k(k-1) + \sum_{i=k+1}^n \min(d_i, k)$ holds for every $1 \leq k \leq n$.

- Gale–Ryser theorem

A pair of sequences of nonnegative integers $a_1 \geq \dots \geq a_n$ and b_1, \dots, b_n is bigraphic if and only if $\sum_{i=1}^n a_i = \sum_{i=1}^n b_i$ and $\sum_{i=1}^k a_i \leq \sum_{i=1}^n \min(b_i, k)$ holds for every $1 \leq k \leq n$.

- Fulkerson–Chen–Anstee theorem

A sequence $(a_1, b_1), \dots, (a_n, b_n)$ of nonnegative integer pairs with $a_1 \geq \dots \geq$

a_n is digraphic if and only if $\sum_{i=1}^n a_i = \sum_{i=1}^n b_i$ and $\sum_{i=1}^k a_i \leq \sum_{i=1}^k \min(b_i, k-1) + \sum_{i=k+1}^n \min(b_i, k)$ holds for every $1 \leq k \leq n$.

- Möbius inversion formula

$$\begin{aligned}
 & - f(n) = \sum_{d|n} g(d) \Leftrightarrow g(n) = \sum_{d|n} \mu(d) f\left(\frac{n}{d}\right) \\
 & - f(n) = \sum_{n|d} g(d) \Leftrightarrow g(n) = \sum_{n|d} \mu\left(\frac{d}{n}\right) f(d)
 \end{aligned}$$

- Spherical cap

- A portion of a sphere cut off by a plane.
- r : sphere radius, a : radius of the base of the cap, h : height of the cap, θ : $\arcsin(a/r)$.
- Volume $= \pi h^2 (3r - h) / 3 = \pi h (3a^2 + h^2) / 6 = \pi r^3 (2 + \cos \theta) (1 - \cos \theta)^2 / 3$.
- Area $= 2\pi r h = \pi (a^2 + h^2) = 2\pi r^2 (1 - \cos \theta)$.

4.7 FloorSum

```

1 // @param $n < 2^{32}$
2 // @param $1 \leq m < 2^{32}$
3 // @return $\sum_{i=0}^{n-1} \lfloor \frac{ai+b}{m} \rfloor \pmod{2^{64}}$
4 ull floor_sum_unsigned(ull n, ull m, ull a, ull b) {
5     ull ans = 0;
6     while(true) {
7         if(a >= m) {
8             ans += n * (n - 1) / 2 * (a / m);
9             a %= m;
10        }
11        if(b >= m) {
12            ans += n * (b / m);
13            b %= m;
14        }
15        ull y_max = a * n + b;
16        if(y_max < m) break;
17        n = (ull)(y_max / m);
18        b = (ull)(y_max % m);
19        swap(m, a);
20    }
21    return ans;
22 }
23
24 ll floor_sum(ll n, ll m, ll a, ll b) {
25     assert(0 <= n && n < (1LL << 32));
26     assert(1 <= m && m < (1LL << 32));
27     ull ans = 0;
28     if(a < 0) {
29         ull a2 = (a % m + m) % m;
30         ans -= 1ULL * n * (n - 1) / 2 * ((a2 - a) / m);
31         a = a2;
32     }
33     if(b < 0) {
34         ull b2 = (b % m + m) % m;
35         ans -= 1ULL * n * ((b2 - b) / m);
36         b = b2;
37     }
38     return ans + floor_sum_unsigned(n, m, a, b);
39 }

```

4.8 Factorizer

```

1 template<class T>
2 vector<pair<T, int>> MergeFactors(const vector<pair<T, int>>& a
3     , const vector<pair<T, int>>& b) {
4     vector<pair<T, int>> c;
5     int i = 0, j = 0;
6     while(i < SZ(a) || j < SZ(b)) {
7         if(i < SZ(a) && j < SZ(b) && a[i].F == b[j].F) {
8             c.EB(a[i].F, a[i].S + b[j].S);
9             ++i, ++j;
10            continue;
11        }
12        if(j == SZ(b) || (i < SZ(a) && a[i].F < b[j].F)) c.PB(a[i]
13            ++);
14        else c.PB(b[j++]);
15    }
16    return c;
17 }
18 template<class T>
19 vector<pair<T, int>> RhoC(const T& n, const T& c) {
20     if(n <= 1) return {};
21     if(n % 2 == 0) return MergeFactors({{2, 1}}, RhoC(n / 2, c));
22     if(is_prime_constexpr(n)) return {{n, 1}};
23     T x = 2, saved = 2, p = 1, lam = 1;
24     while(true) {
25         x = (x * x % n + c) % n;
26         T g = __gcd(((x - saved) + n) % n, n);
27         if(g != 1) return MergeFactors(RhoC(g, c + 1), RhoC(n / g,
28             c + 1));
29         if(p == lam) {
30             saved = x;
31             p <+= 1;
32             lam = 0;
33         }
34         lam += 1;
35     }
36     return {};
37 }
38 template<class T>
39 vector<pair<T, int>> Factorize(T n) {
40     if(n <= 1) return {};
41     return RhoC(n, T(1));
42 }
43 template<class T>
44 vector<T> BuildDivisorsFromFactors(const vector<pair<T, int>>&
45     factors) {
46     int total = 1;
47     for(int i = 0; i < SZ(factors); ++i) total *= factors[i].
48         second + 1;

```

```

44 vector<T> divisors;
45 divisors.reserve(total);
46 divisors.PB(1);
47 for(auto [p, cnt] : factors) {
48     int sz = SZ(divisors);
49     for(int i = 0; i < sz; ++i) {
50         T cur = divisors[i];
51         for(int j = 0; j < cnt; ++j) {
52             cur *= p;
53             divisors.PB(cur);
54         }
55     }
56 }
57 // sort(ALL(divisors));
58 return divisors;
59 }

```

4.9 PowMod

```

1 constexpr long long Pow(long long x, long long n, int m) {
2     if(m == 1) return 0;
3     unsigned int _m = (unsigned int)(m);
4     unsigned long long r = 1;
5     x %= m;
6     if(x < 0) x += m;
7     unsigned long long y = x;
8     while(n) {
9         if(n & 1) r = (r * y) % _m;
10        y = (y * y) % _m;
11        n >>= 1;
12    }
13    return r;
14 }

```

4.10 CRT

```

1 // @return
2 // $\text{remainder, modulo}$
3 // or
4 // $0, 0$ if do not exist
5 pair<long long, long long> crt(const vector<long long>& r,
6     const vector<long long>& m) {
7     assert(r.size() == m.size());
8     int n = r.size();
9     // Contracts: 0 <= r0 < m0
10    long long r0 = 0, m0 = 1;
11    for(int i = 0; i < n; ++i) {
12        assert(1 <= m[i]);
13        long long r1 = r[i] % m[i];
14        if(r1 < 0) r1 += m[i];
15        long long m1 = m[i];
16        if(m0 < m1) {
17            swap(r0, r1);
18            swap(m0, m1);
19        }
20        if(m0 % m1 == 0) {
21            if(r0 % m1 != r1) return {0, 0};
22            continue;
23        }
24        long long g, im;
25        tie(g, im) = inv_gcd(m0, m1);
26        long long u1 = (m1 / g);
27        if((r1 - r0) % g) return {0, 0};
28        long long x = (r1 - r0) / g % u1 * im % u1;
29        r0 += x * m0;
30        m0 *= u1;
31        if(r0 < 0) r0 += m0;
32    }
33    return {r0, m0};

```

4.11 DiscreteLog

```

1 int DiscreteLog(int s, int x, int y, int m) {
2     constexpr int K = 0;
3     hash_map<int, int> p;
4     int b = 1;
5     for(int i = 0; i < K; ++i) {
6         p[y] = i;
7         y = 1LL * y * x % m;
8         b = 1LL * b * x % m;
9     }
10    for(int i = 0; i < m + 10; i += K) {
11        s = 1LL * s * b % m;
12        if(p.find(s) != p.end()) return i + K - p[s];
13    }
14    return -1;
15 }
16 int DiscreteLog(int x, int y, int m) {

```

```

17 | if(m == 1) return 0;
18 | int s = 1;
19 | for(int i = 0; i < 100; ++i) {
20 |     if(s == y) return i;
21 |     s = 1LL * s * x % m;
22 | }
23 | if(s == y) return 100;
24 | int p = 100 + Discretelog(s, x, y, m);
25 | return (pow_mod(x, p, m) != y ? -1 : p);
26 | }

```

4.12 LinearSieve

```

1 | vector<bool> is_prime;
2 | vector<int> primes, phi, mobius, least;
3 | void linear_sieve(int n) {
4 |     n += 1;
5 |     is_prime.resize(n);
6 |     least.resize(n);
7 |     fill(2 + begin(is_prime), end(is_prime), true);
8 |     phi.resize(n); mobius.resize(n);
9 |     phi[1] = mobius[1] = 1;
10 |    least[0] = 0, least[1] = 1;
11 |    for(int i = 2; i < n; ++i) {
12 |        if(is_prime[i]) {
13 |            primes.push_back(i);
14 |            phi[i] = i - 1;
15 |            mobius[i] = -1;
16 |            least[i] = i;
17 |        }
18 |        for(auto j : primes) {
19 |            if(i * j >= n) break;
20 |            is_prime[i * j] = false;
21 |            least[i * j] = j;
22 |            if(i % j == 0) {
23 |                mobius[i * j] = 0;
24 |                phi[i * j] = phi[i] * j;
25 |                break;
26 |            } else {
27 |                mobius[i * j] = mobius[i] * mobius[j];
28 |                phi[i * j] = phi[i] * phi[j];
29 |            }
30 |        }
31 |    }
32 | }

```

5 Misc

5.1 FastIO

```

1 | inline char gc() {
2 |     static const int BUF_SIZE = 1 << 22;
3 |     static int Counts = 1 << 23;
4 |     static char Buffer[BUF_SIZE];
5 |     static char *Pointer = Buffer, *End = Buffer;
6 |     if(Pointer == End) {
7 |         if(Counts < BUF_SIZE) {
8 |             return EOF;
9 |         }
10 |        Counts = fread(Buffer, 1, BUF_SIZE, stdin);
11 |        Pointer = Buffer;
12 |        End = Buffer + Counts;
13 |    }
14 |    return *(Pointer++);
15 | }
16 |
17 | template<class T>
18 | inline void read(T& x) {
19 |     static char c;
20 |     do {
21 |         c = gc();
22 |     } while(c < '0' && c != '-');
23 |     bool neg = (c == '-');
24 |     if(!neg) {
25 |         x = c - '0';
26 |     } else x = 0;
27 |     while((c = gc()) >= '0') {
28 |         x = (x << 3) + (x << 1) + (c & 15);
29 |     }
30 |     if(neg) {
31 |         x = -x;
32 |     }
33 | }
34 |
35 | template<class T, class... U>
36 | inline void read(T& a, U&... b) {
37 |     read(a);
38 |     read(b...);
39 | }

```

```

40 |
41 | template<class T>
42 | inline void write(T temp, char end = '\n') {
43 |     static short digits[20], P;
44 |     if(temp == 0) {
45 |         putchar_unlocked('0');
46 |         putchar_unlocked(end);
47 |         return;
48 |     }
49 |     if(temp < 0) {
50 |         putchar_unlocked('-');
51 |         write(-temp, end);
52 |         return;
53 |     }
54 |     P = -1;
55 |     while(temp) {
56 |         digits[++P] = temp % 10;
57 |         temp /= 10;
58 |     }
59 |     while(P >= 0) {
60 |         putchar_unlocked(digits[P--] + '0');
61 |     }
62 |     putchar_unlocked(end);
63 |     return;
64 | }

```

5.2 Debug

```

1 | #ifdef LOCAL
2 | #define printf(...) { fprintf(stderr, __VA_ARGS__); fflush(
3 |     stderr); }
4 | #else
5 | #define printf(...) 42
6 | #endif

```

5.3 Discrete

```

1 | template<class T>
2 | vector<int> Discrete(const vector<T>&v){
3 |     vector<int>ans;
4 |     vector<T>tmp(v);
5 |     sort(begin(tmp), end(tmp));
6 |     tmp.erase(unique(begin(tmp), end(tmp)), end(tmp));
7 |     for(auto i:v)ans.push_back(lower_bound(begin(tmp), end(tmp), i)
8 |         -tmp.begin()+1);
9 |     return ans;
10 | }

```

5.4 DuiPai

```

1 | #include<bits/stdc++.h>
2 | using namespace std;
3 | int main(){
4 |     string sol,bf,make;
5 |     cout<<"Your solution file name :";
6 |     cin>>sol;
7 |     cout<<"Brute force file name :";
8 |     cin>>bf;
9 |     cout<<"Make data file name :";
10 |    cin>>make;
11 |    system(("g++ "+sol+" -o sol").c_str());
12 |    system(("g++ "+bf+" -o bf").c_str());
13 |    system(("g++ "+make+" -o make").c_str());
14 |    for(int t = 0; t<10000; ++t){
15 |        system("./make > ./1.in");
16 |        double st = clock();
17 |        system("./sol < ./1.in > ./1.ans");
18 |        double et = clock();
19 |        system("./bf < ./1.in > ./1.out");
20 |        if(system("diff ./1.out ./1.ans")) {
21 |            printf("\033[0;31mWrong Answer\033[0m on test #%d", t);
22 |            return 0;
23 |        }
24 |        else if(et-st>2000){
25 |            printf("\033[0;32mTime Limit exceeded\033[0m on test #%d,
26 |                Time %.0lfms\n", t, et-st);
27 |            return 0;
28 |        }
29 |        else {
30 |            printf("\033[0;32mAccepted\033[0m on test #%d, Time
31 |                %.0lfms\n", t, et - st);
32 |        }
33 |    }
34 | }

```

5.5 Timer

```
1 const clock_t startTime = clock();
2 inline double getCurrentTime() {
3     return (double) (clock() - startTime) / CLOCKS_PER_SEC;
4 }
```

5.6 TernarySearch

```
1 // return the maximum of $f(x)$ in $[L, r]$
2 double ternary_search(double l, double r) {
3     while(r - l > EPS) {
4         double m1 = l + (r - l) / 3;
5         double m2 = r - (r - l) / 3;
6         double f1 = f(m1), f2 = f(m2);
7         if(f1 < f2) l = m1;
8         else r = m2;
9     }
10    return f(l);
11 }
12
13 // return the maximum of $f(x)$ in $[L, r]$
14 int ternary_search(int l, int r) {
15     while(r - l > 1) {
16         int mid = (l + r) / 2;
17         if(f(m) > f(m + 1)) r = m;
18         else l = m;
19     }
20    return r;
21 }
```

6 Other

6.1 TouristIO

```
1 static struct FastInput {
2     static constexpr int BUF_SIZE = 1 << 20;
3     char buf[BUF_SIZE];
4     size_t chars_read = 0;
5     size_t buf_pos = 0;
6     FILE *in = stdin;
7     char cur = 0;
8
9     inline char get_char() {
10        if(buf_pos >= chars_read) {
11            chars_read = fread(buf, 1, BUF_SIZE, in);
12            buf_pos = 0;
13            buf[0] = (chars_read == 0 ? -1 : buf[0]);
14        }
15        return cur = buf[buf_pos++];
16        // return cur = getchar_unlocked();
17    }
18
19    inline void tie(int) {}
20
21    inline explicit operator bool() {
22        return cur != -1;
23    }
24
25    inline static bool is_blank(char c) {
26        return c <= ' ';
27    }
28
29    inline bool skip_blanks() {
30        while(is_blank(cur) && cur != -1) {
31            get_char();
32        }
33        return cur != -1;
34    }
35
36    inline FastInput& operator>>(char& c) {
37        skip_blanks();
38        c = cur;
39        return *this;
40    }
41
42    inline FastInput& operator>>(string& s) {
43        if(skip_blanks()) {
44            s.clear();
45            do {
46                s += cur;
47            } while(!is_blank(get_char()));
48        }
49        return *this;
50    }
51
52    template<class T>
53    inline FastInput& read_integer(T& n) {
```

```
54    // unsafe, doesn't check that characters are actually
55    // digits
56    n = 0;
57    if(skip_blanks()) {
58        int sign = +1;
59        if(cur == '-') {
60            sign = -1;
61            get_char();
62        }
63        do {
64            n += n << 3 + cur - '0';
65        } while(!is_blank(get_char()));
66        n *= sign;
67    }
68    return *this;
69 }
70
71 template<class T>
72 inline typename enable_if<is_integral<T>::value, FastInput
73     &>::type operator>>(T& n) {
74     return read_integer(n);
75 }
76
77 #if !defined(_WIN32) || defined(_WIN64)
78 inline FastInput& operator>>(__int128& n) {
79     return read_integer(n);
80 }
81 #endif
82
83 template<class T>
84 inline typename enable_if<is_floating_point<T>::value,
85     FastInput&>::type operator>>(T& n) {
86     // not sure if really fast, for compatibility only
87     n = 0;
88     if(skip_blanks()) {
89         string s;
90         (*this) >> s;
91         sscanf(s.c_str(), "%Lf", &n);
92     }
93     return *this;
94 }
95
96 } fast_input;
97
98 #define cin fast_input
99
100 static struct FastOutput {
101     static constexpr int BUF_SIZE = 1 << 20;
102     char buf[BUF_SIZE];
103     size_t buf_pos = 0;
104     static constexpr int TMP_SIZE = 1 << 20;
105     char tmp[TMP_SIZE];
106     FILE *out = stdout;
107
108     inline void put_char(char c) {
109         buf[buf_pos++] = c;
110         if(buf_pos == BUF_SIZE) {
111             fwrite(buf, 1, buf_pos, out);
112             buf_pos = 0;
113         }
114         // putchar_unlocked(c);
115     }
116
117     ~FastOutput() {
118         fwrite(buf, 1, buf_pos, out);
119     }
120
121     inline FastOutput& operator<<(char c) {
122         put_char(c);
123         return *this;
124     }
125
126     inline FastOutput& operator<<(const char* s) {
127         while(*s) {
128             put_char(*s++);
129         }
130         return *this;
131     }
132
133     inline FastOutput& operator<<(const string& s) {
134         for(int i = 0; i < (int) s.size(); i++) {
135             put_char(s[i]);
136         }
137         return *this;
138     }
139
140     template<class T>
141     inline char* integer_to_string(T n) {
142         // beware of TMP_SIZE
143         char* p = tmp + TMP_SIZE - 1;
144         if(n == 0) {
145             *--p = '0';
146         } else {
147             bool is_negative = false;
148             if(n < 0) {
149                 is_negative = true;
150                 n = -n;
151             }
```



```

148     while(n > 0) {
149         *--p = (char) ('0' + n % 10);
150         n /= 10;
151     }
152     if(is_negative) {
153         *--p = '-';
154     }
155 }
156 return p;
157 }
158
159 template<class T>
160 inline typename enable_if<is_integral<T>::value, char*>::type
161     stringify(T n) {
162     return integer_to_string(n);
163 }
164
165 #ifndef _WIN32 || defined(_WIN64)
166 inline char* stringify(__int128 n) {
167     return integer_to_string(n);
168 }
169 #endif
170
171 template<class T>
172 inline typename enable_if<is_floating_point<T>::value, char
173     *>::type stringify(T n) {
174     sprintf(tmp, "%.17f", n);
175     return tmp;
176 }
177
178 template<class T>
179 inline FastOutput& operator<<(const T& n) {
180     auto p = stringify(n);
181     for(; *p != 0; p++) {
182         put_char(*p);
183     }
184     return *this;
185 } fast_output;
186 #define cout fast_output

```

7 Setup

7.1 Template

```

1 #include <bits/extc++.h>
2 #include <bits/stdc++.h>
3 #pragma GCC optimize("O3,unroll-loops")
4 #pragma GCC target("avx2,bmi,bmi2,lzcnt,popcnt")
5 #define IOS ios::sync_with_stdio(0),cin.tie(0),cout.tie(0)
6 #define int long long
7 #define double long double
8 #define pb push_back
9 #define sz(x) (int)(x).size()
10 #define all(v) begin(v),end(v)
11 #define debug(x) cerr<<#x<<" = "<<x<<'\n'
12 #define LINE cout<<"\n-----\n"
13 #define endl '\n'
14 #define VI vector<int>
15 #define F first
16 #define S second
17 #define MP(a,b) make_pair(a,b)
18 #define rep(i,m,n) for(int i = m;i<=n;++i)
19 #define res(i,m,n) for(int i = m;i>=n;--i)
20 #define gcd(a,b) __gcd(a,b)
21 #define lcm(a,b) a*b/gcd(a,b)
22 #define Case() int _;cin>>_;for(int Case = 1;Case<=;_;++Case)
23 #define pii pair<int,int>
24 using namespace __gnu_cxx;
25 using namespace __gnu_pbds;
26 using namespace std;
27 template <typename K, typename cmp = less<K>, typename T =
28     thin_heap_tag> using _heap = __gnu_pbds::priority_queue<K,
29     cmp, T>;
30 template <typename K, typename M = null_type> using _hash =
31     gp_hash_table<K, M>;
32 const int N = 1e6+5,L = 20,mod = 1e9+7;
33 const long long inf = 2e18+5;
34 const double eps = 1e-7,pi = acos(-1);
35 void solve(){
36 }
37 signed main(){
38     IOS;
39     solve();
40 }

```

8 String

8.1 DynamicKMP

```

1 template<int ALPHABET, int (*f)(char)>
2 class DynamicKMP {
3 public:
4     DynamicKMP() {}
5
6     DynamicKMP(const string& s) {
7         reserve(s.size());
8         for(const char& c : s) {
9             push(c);
10        }
11    }
12
13    void push(char c) {
14        int v = f(c);
15        dp.emplace_back();
16        dp.back()[v] = (int) dp.size();
17        if(p.empty()) {
18            p.push_back(0);
19            return;
20        }
21        int i = (int) p.size();
22        for(int j = 0; j < ALPHABET; ++j) {
23            if(j == v) {
24                p.push_back(dp[p[i - 1]][j]);
25            } else {
26                dp.back()[j] = dp[p[i - 1]][j];
27            }
28        }
29    }
30
31    void pop() {
32        p.pop_back();
33        dp.pop_back();
34    }
35
36    int query() const {
37        return p.back();
38    }
39
40    vector<int> query_all() const {
41        return p;
42    }
43
44    void reserve(int sz) {
45        p.reserve(sz);
46        dp.reserve(sz);
47    }
48
49 private:
50     vector<int> p;
51     vector<array<int, ALPHABET>> dp;
52 };

```

8.2 RollingHash

```

1 template<int HASH_COUNT, bool PRECOMPUTE_POWERS = false>
2 class Hash {
3 public:
4     static constexpr int MAX_HASH_PAIRS = 10;
5
6     // {mul, mod}
7     static constexpr const pair<int, int> HASH_PAIRS[] =
8         {{827167801, 999999937}, {998244353, 999999929},
9          {146672737, 922722049}, {204924373, 952311013},
10          {585761567, 955873937}, {484547929, 901981687},
11          {856009481, 987877511}, {852853249, 996724213},
12          {937381759, 994523539}, {116508269, 993179543}};
13
14     Hash() : Hash("") {}
15
16     Hash(const string& s) : n(s.size()) {
17         static_assert(HASH_COUNT > 0 && HASH_COUNT <=
18             MAX_HASH_PAIRS);
19         for(int i = 0; i < HASH_COUNT; ++i) {
20             const auto& p = HASH_PAIRS[i];
21             pref[i].resize(n);
22             pref[i][0] = s[0];
23             for(int j = 1; j < n; ++j) {
24                 pref[i][j] = (1LL * pref[i][j - 1] * p.first + s[j]) %
25                     p.second;
26             }
27         }
28         if(PRECOMPUTE_POWERS) {
29             build_powers(n);
30         }
31     }
32 }
33
34 }
35
36 }
37
38 }
39
40 }

```

```

26 void add_char(char c) {
27     for(int i = 0; i < HASH_COUNT; ++i) {
28         const auto& p = HASH_PAIRS[i];
29         pref[i].push_back((1LL * (n == 0 ? 0 : pref[i].back()) *
30             p.first + c) % p.second);
31     }
32     n += 1;
33     if(PRECOMPUTE_POWERS) {
34         build_powers(n);
35     }
36 }
37 // Return hash values for [l, r)
38 array<int, HASH_COUNT> substr(int l, int r) {
39     array<int, HASH_COUNT> res{};
40     for(int i = 0; i < HASH_COUNT; ++i) {
41         res[i] = substr(i, l, r);
42     }
43     return res;
44 }
45
46 array<int, HASH_COUNT> merge(const vector<pair<int, int>>&
47     seg) {
48     array<int, HASH_COUNT> res{};
49     for(int i = 0; i < HASH_COUNT; ++i) {
50         const auto& p = HASH_PAIRS[i];
51         for(auto [l, r] : seg) {
52             res[i] = (1LL * res[i] * get_power(i, r - 1) + substr(i
53                 , l, r)) % p.second;
54         }
55     }
56     return res;
57 }
58 // build powers up to x^k
59 void build_powers(int k) {
60     for(int i = 0; i < HASH_COUNT; ++i) {
61         const auto& p = HASH_PAIRS[i];
62         int sz = (int) POW[i].size();
63         if(sz > k) {
64             continue;
65         }
66         if(sz == 0) {
67             POW[i].push_back(1);
68             sz = 1;
69         }
70         while(sz <= k) {
71             POW[i].push_back(1LL * POW[i].back() * p.first % p.
72                 second);
73             sz += 1;
74         }
75     }
76 }
77 inline int size() const {
78     return n;
79 }
80 private:
81 int n;
82 static vector<int> POW[MAX_HASH_PAIRS];
83 array<vector<int>, HASH_COUNT> pref;
84
85 int substr(int k, int l, int r) {
86     assert(0 <= k && k < HASH_COUNT);
87     assert(0 <= l && l <= r && r <= n);
88     const auto& p = HASH_PAIRS[k];
89     if(l == r) {
90         return 0;
91     }
92     int res = pref[k][r - 1];
93     if(l > 0) {
94         res -= 1LL * pref[k][l - 1] * get_power(k, r - 1) % p.
95             second;
96     }
97     if(res < 0) {
98         res += p.second;
99     }
100     return res;
101 }
102 int get_power(int a, int b) {
103     if(PRECOMPUTE_POWERS) {
104         build_powers(b);
105         return POW[a][b];
106     }
107     const auto& p = HASH_PAIRS[a];
108     return power(p.first, b, p.second);
109 }
110 };
111 template<int A, bool B> vector<int> Hash<A, B>::POW[Hash::
    MAX_HASH_PAIRS];

```

8.3 SuffixArray

```

1 struct suffix_array{
2     int n;
3     vector<int>SA, Rank, LCP;
4     void counting_sort(vector<int>&v, auto getkey){
5         int n = 0;
6         for(auto i:v)n = max(n, getkey(i)+1);
7         vector<int>bucket(n, ans(v.size()));
8         for(auto i:v)++bucket[getkey(i)];
9         partial_sum(begin(bucket), end(bucket), begin(bucket));
10        for(auto ite = v.rbegin(); ite!=v.rend(); ++ite)ans[--bucket[
11            getkey(*ite)]] = move(*ite);
12        v.swap(ans);
13        return;
14    }
15    suffix_array(string s):n(s.size()){
16        SA.resize(n), Rank.resize(n), LCP.resize(n);
17        for(int i = 0; i<n; ++i)SA[i] = i;
18        sort(SA.begin(), SA.end(), [&](int a, int b){
19            return s[a]<s[b];
20        });
21        for(int i = 0; i<n; ++i){
22            Rank[SA[i]] = (i?Rank[SA[i-1]]+(s[SA[i]]!=s[SA[i-1]]):SA
23                [0]);
24        }
25        for(int k = 0; (1<<k)<=n; ++k){
26            vector<int>idx;
27            for(int i = n-(1<<k); i<n; ++i)idx.push_back(i);
28            for(auto i:SA)if(i>=(1<<k))idx.push_back(i-(1<<k));
29            counting_sort(idx, [&](int a){return Rank[a];});
30            SA.swap(idx);
31            vector<int>new_rank(n);
32            new_rank[SA[0]] = 0;
33            for(int i = 1; i<n; ++i){
34                auto cmp = [&](int a, int b){
35                    return Rank[a]!=Rank[b] or a+(1<<k)>=n or Rank[a+(1<<
36                        k)]!=Rank[b+(1<<k)];
37                };
38                new_rank[SA[i]] = new_rank[SA[i-1]]+cmp(SA[i-1], SA[i]);
39            }
40            Rank.swap(new_rank);
41        }
42        for(int i = 0, k = 0; i<n; ++i){
43            if(Rank[i]==0)continue;
44            if(k)--k;
45            while(i+k<n and SA[Rank[i]-1]+k<n and s[i+k]==s[SA[Rank[i]
46                ]-1+k]))++k;
47            LCP[Rank[i]] = k;
48        }
49    }
50 };

```

8.4 Trie

```

1 template<int ALPHABET = 26, char MIN_CHAR = 'a'>
2 class trie {
3 public:
4     struct Node {
5         int go[ALPHABET];
6         Node() {
7             memset(go, -1, sizeof(go));
8         }
9     };
10
11     trie() {
12         newNode();
13     }
14
15     inline int next(int p, int v) {
16         return nodes[p].go[v] != -1 ? nodes[p].go[v] : nodes[p].go[
17             v] = newNode();
18     }
19
20     inline void insert(const vector<int>& a, int p = 0) {
21         for(int v : a) {
22             p = next(p, v);
23         }
24     }
25
26     inline void clear() {
27         nodes.clear();
28         newNode();
29     }
30
31     inline int longest_common_prefix(const vector<int>& a, int p
32         = 0) const {
33         int ans = 0;
34         for(int v : a) {
35             if(nodes[p].go[v] != -1) {
36                 ans += 1;
37                 p = nodes[p].go[v];
38             } else {

```

```
37         break;
38     }
39 }
40 return ans;
41 }
42
43 private:
44     vector<Node> nodes;
45
46     inline int newNode() {
47         nodes.emplace_back();
48         return (int) nodes.size() - 1;
49     }
50 };
```

ACM ICPC Team

Reference -

LeeJiaHuaPlayMinecraft

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ACM ICPC Judge Test - LeeJiaHuaPlayMinecraft

C++ Resource Test

```
1 #include <bits/stdc++.h>
2 using namespace std;
3
4 namespace system_test {
5
6     const size_t KB = 1024;
7     const size_t MB = KB * 1024;
8     const size_t GB = MB * 1024;
9
10    size_t block_size, bound;
11    void stack_size_dfs(size_t depth = 1) {
12        if (depth >= bound)
13            return;
14        int8_t ptr[block_size]; // 若無法編譯將 block_size 改成常數
15        memset(ptr, 'a', block_size);
16        cout << depth << endl;
17        stack_size_dfs(depth + 1);
18    }
19
20    void stack_size_and_runtime_error(size_t block_size, size_t
        bound = 1024) {
21        system_test::block_size = block_size;
22        system_test::bound = bound;
23        stack_size_dfs();
24    }
25
26    double speed(int iter_num) {
27        const int block_size = 1024;
28        volatile int A[block_size];
29        auto begin = chrono::high_resolution_clock::now();
30        while (iter_num--)
31            for (int j = 0; j < block_size; ++j)
32                A[j] += j;
33        auto end = chrono::high_resolution_clock::now();
34        chrono::duration<double> diff = end - begin;
35        return diff.count();
```

```
36    }
37
38    void runtime_error_1() {
39        // Segmentation fault
40        int *ptr = nullptr;
41        *(ptr + 7122) = 7122;
42    }
43
44    void runtime_error_2() {
45        // Segmentation fault
46        int *ptr = (int *)memset;
47        *ptr = 7122;
48    }
49
50    void runtime_error_3() {
51        // munmap_chunk(): invalid pointer
52        int *ptr = (int *)memset;
53        delete ptr;
54    }
55
56    void runtime_error_4() {
57        // free(): invalid pointer
58        int *ptr = new int[7122];
59        ptr += 1;
60        delete[] ptr;
61    }
62
63    void runtime_error_5() {
64        // maybe illegal instruction
65        int a = 7122, b = 0;
66        cout << (a / b) << endl;
67    }
68
69    void runtime_error_6() {
70        // floating point exception
71        volatile int a = 7122, b = 0;
72        cout << (a / b) << endl;
73    }
74
75    void runtime_error_7() {
76        // call to abort.
77        assert(false);
78    }
79
80    } // namespace system_test
81
82    #include <sys/resource.h>
83    void print_stack_limit() { // only work in Linux
84        struct rlimit l;
85        getrlimit(RLIMIT_STACK, &l);
86        cout << "stack_size = " << l.rlim_cur << " byte" << endl;
87    }
```