

Gravitational Potential potential

$$\text{U} \propto -\frac{m}{r^2}$$

m/r^2

The Gravity Method

Lu Li & Mareen Lösing

CAGE September 2024

Introduction

Lu Li



Mareen Lösing



- Post-doctoral researchers at University of Western Australia
 - Recently been to Antarctica (with a gravimeter)

Introduction



Overview

Goals:

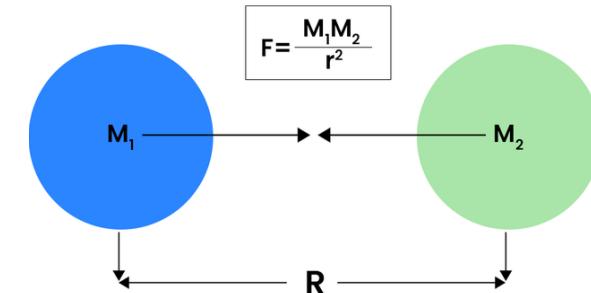
1. Understand basics of Gravity
2. Understand related geological properties
3. Gravimeter Introduction
4. Removing unwanted signal / corrections
5. Introduction to the Workflow & Code



Overview

Fundamentals:

- Force that attracts two bodies toward each other, proportional to their masses and inversely proportional to the square of the distance between them
- Gravitational acceleration ($g \approx 9.81 \text{ m/s}^2$) varies slightly depending on location (e.g., altitude, latitude)
- Units of gravity measurements:
 - Galileo or Gal; 1 Gal = 1 cm/s²
 - Used in milligals (1 mGal = 10⁻⁵ m/s²) in geological exploration



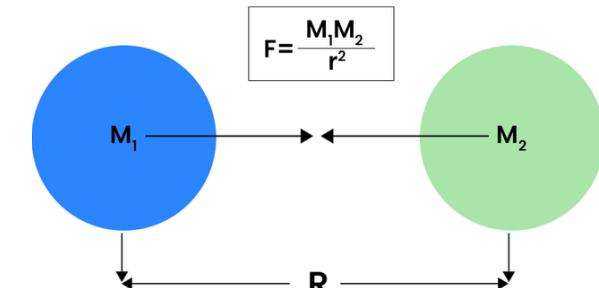
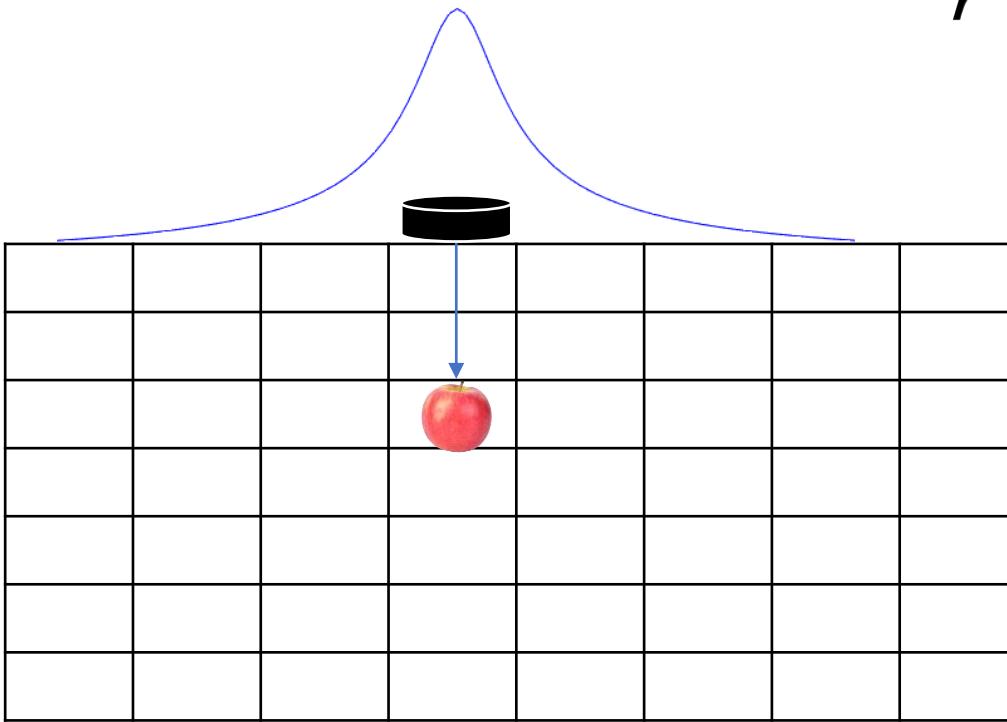
Gravitational constant
($6.674 * 10^{-11} \text{ Nm}^2/\text{kg}^2$)

$$g = \frac{GM}{r^2}$$

Earth's mass Distance from Earth's center

A point source

$$g = \frac{GM}{r^2} = \frac{G\rho V}{r^2}$$



Gravitational constant
 $(6.674 * 10^{-11} \text{ Nm}^2/\text{kg}^2)$

$$g = \frac{GM}{r^2}$$

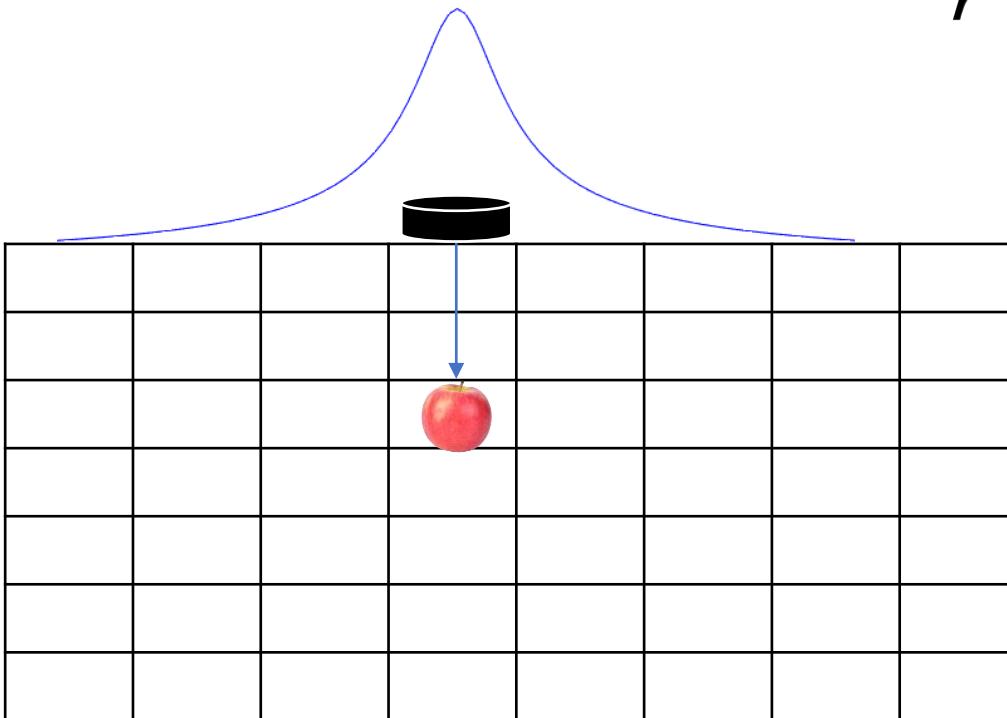
Diagram labels:

- GM : Earth's mass (points to the GM term)
- r^2 : Distance from Earth's center (points to the r^2 term)

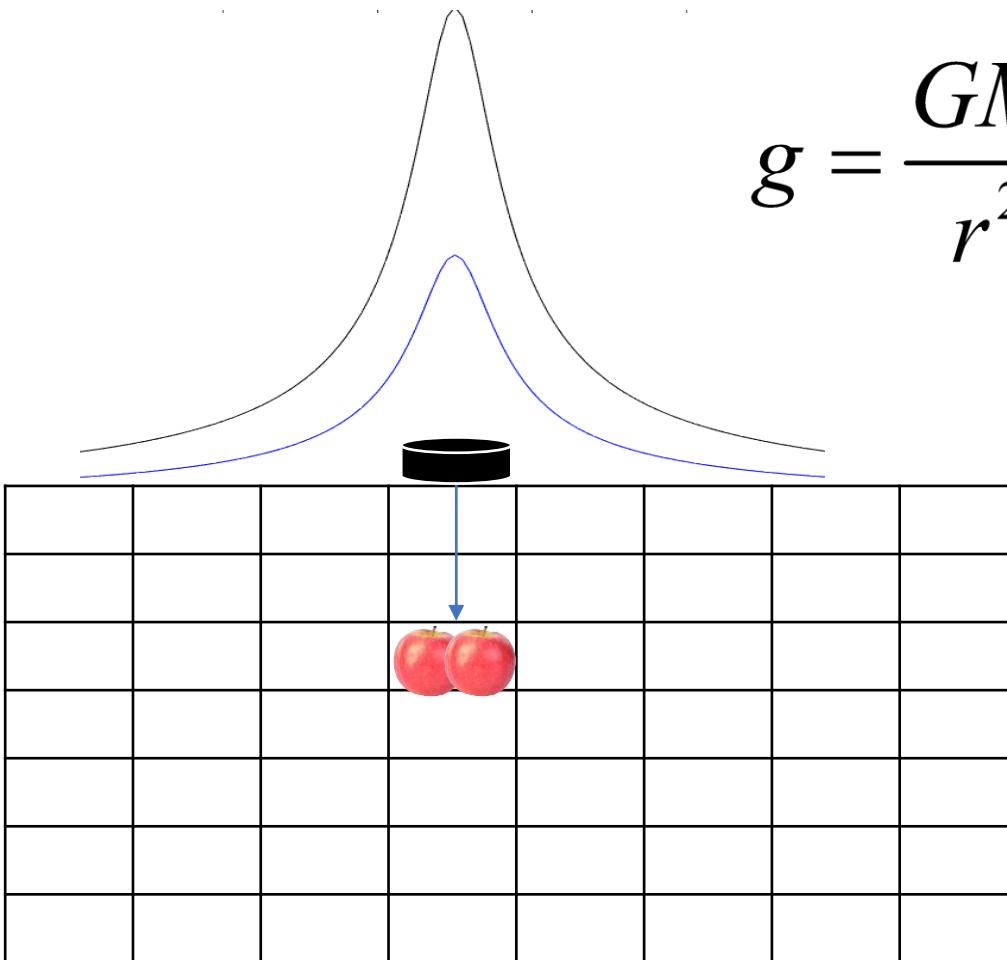
A point source

$$g = \frac{GM}{r^2} = \frac{G\rho V}{r^2}$$

Density Distance



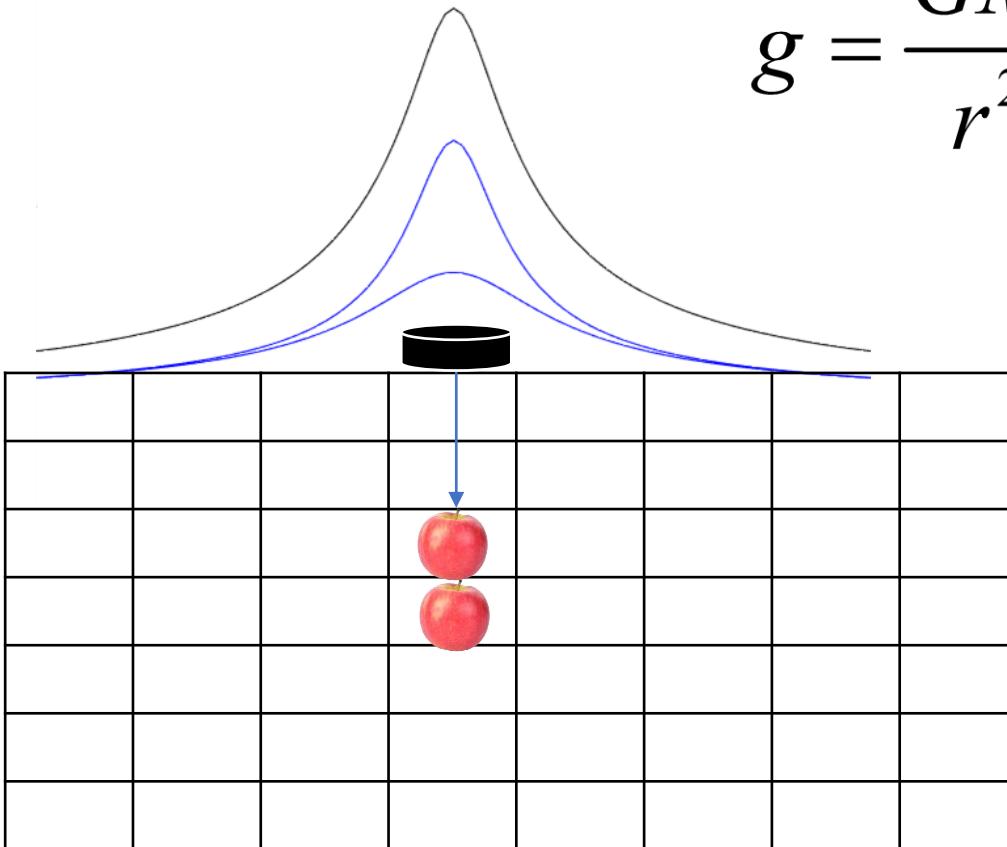
A point source



$$g = \frac{GM}{r^2} = \frac{G\rho V}{r^2}$$

If we double the density, then we double the gravity effect

A point source



$$g = \frac{GM}{r^2} = \frac{G\rho V}{r^2}$$

Density

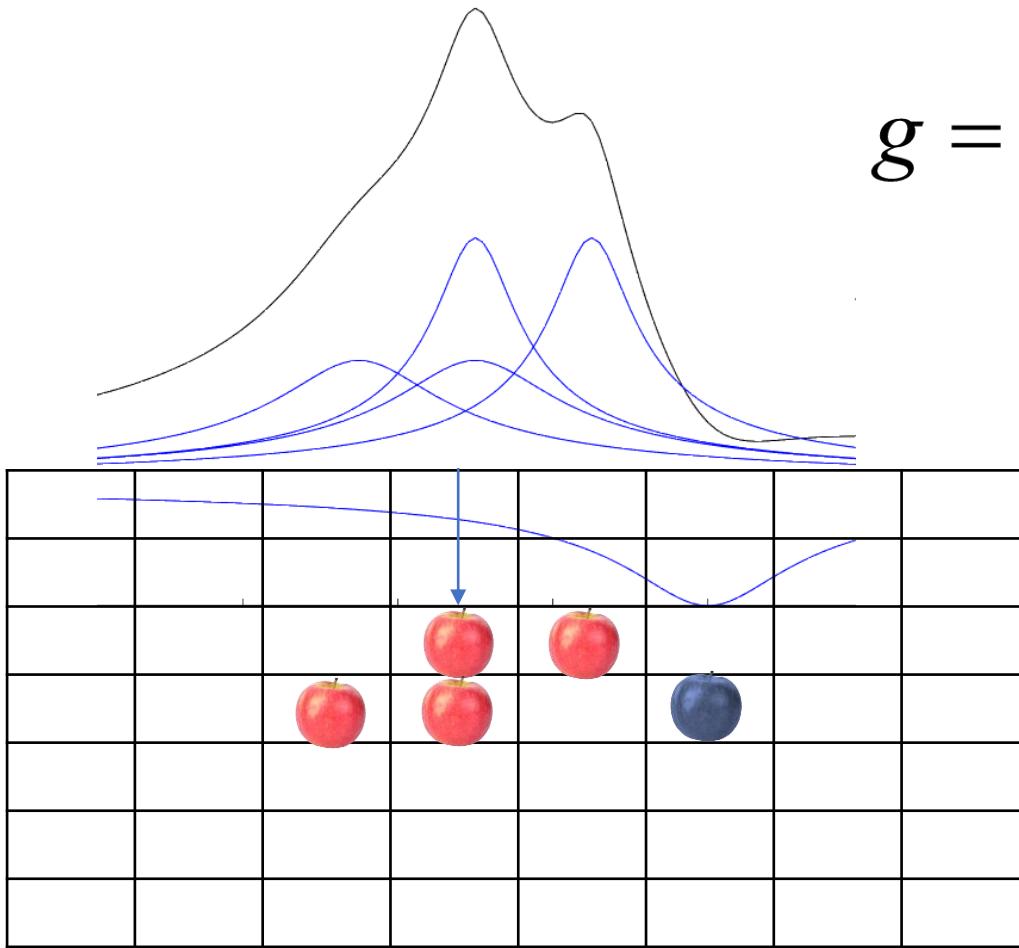
Distance

If we increase the distance between observation point and source, we will see a broader but smaller anomaly.

Increase the distance between observation point and source:

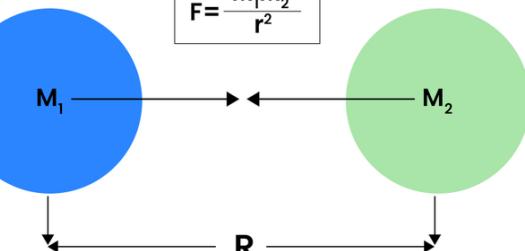
1. Source getting deeper
2. Observational surface getting higher

A lot of point sources



$$g = \frac{GM}{r^2} = \sum \frac{G\rho V}{r^2}$$

$$F = \frac{M_1 M_2}{r^2}$$



Gravitational constant
 $(6.674 * 10^{-11} \text{ Nm}^2/\text{kg}^2)$

$$g = \frac{GM}{r^2}$$

GM → Earth's mass
 r → Distance from Earth's center



Overview

Earth's gravity field

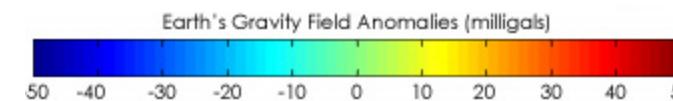
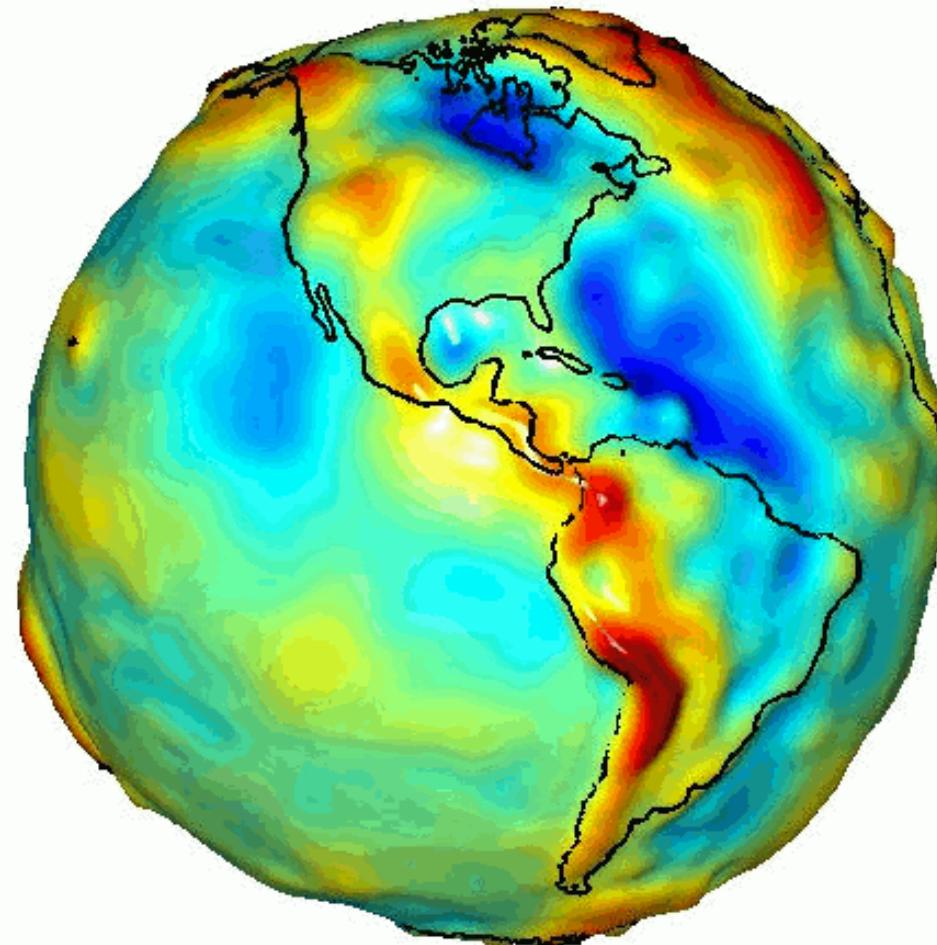


Image: NASA

Types of Gravity Surveys

Satellite

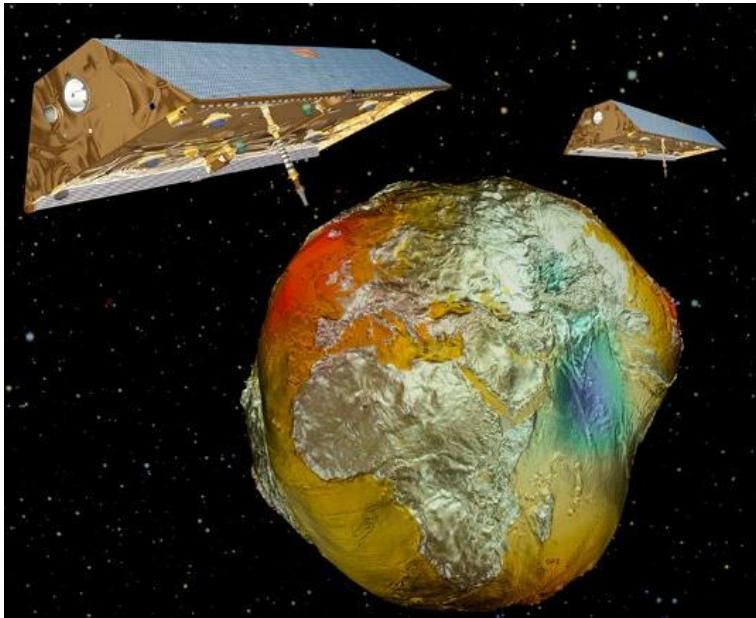


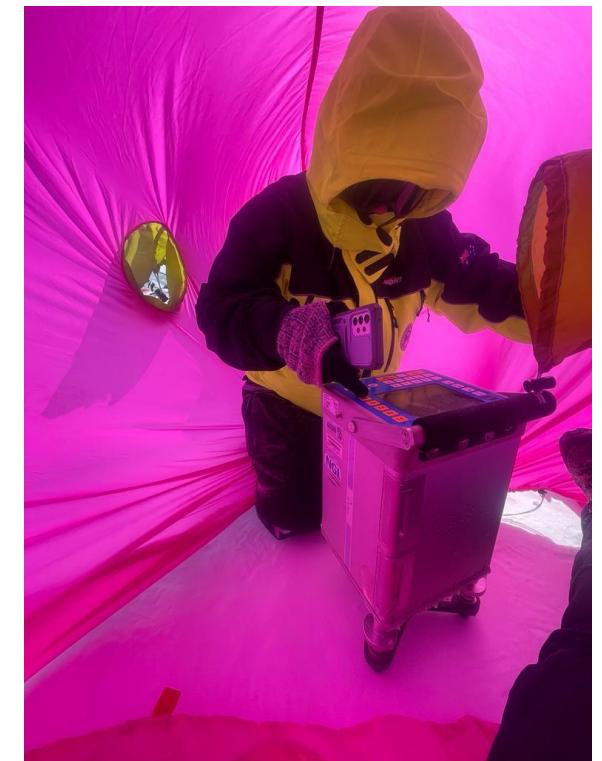
Image: GFZ

Airborne



Image: British Antarctic Survey

Ground-based



What can gravity data tell us?

- Time variable gravity field,
➤ Monitor ice, water change

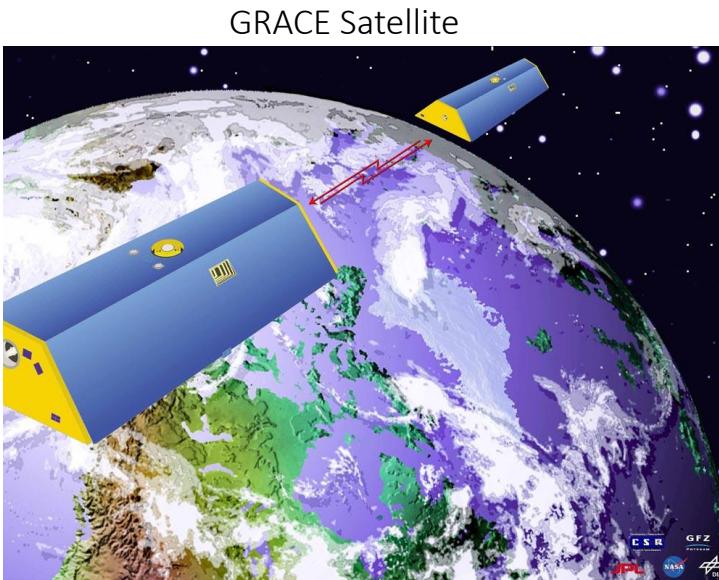
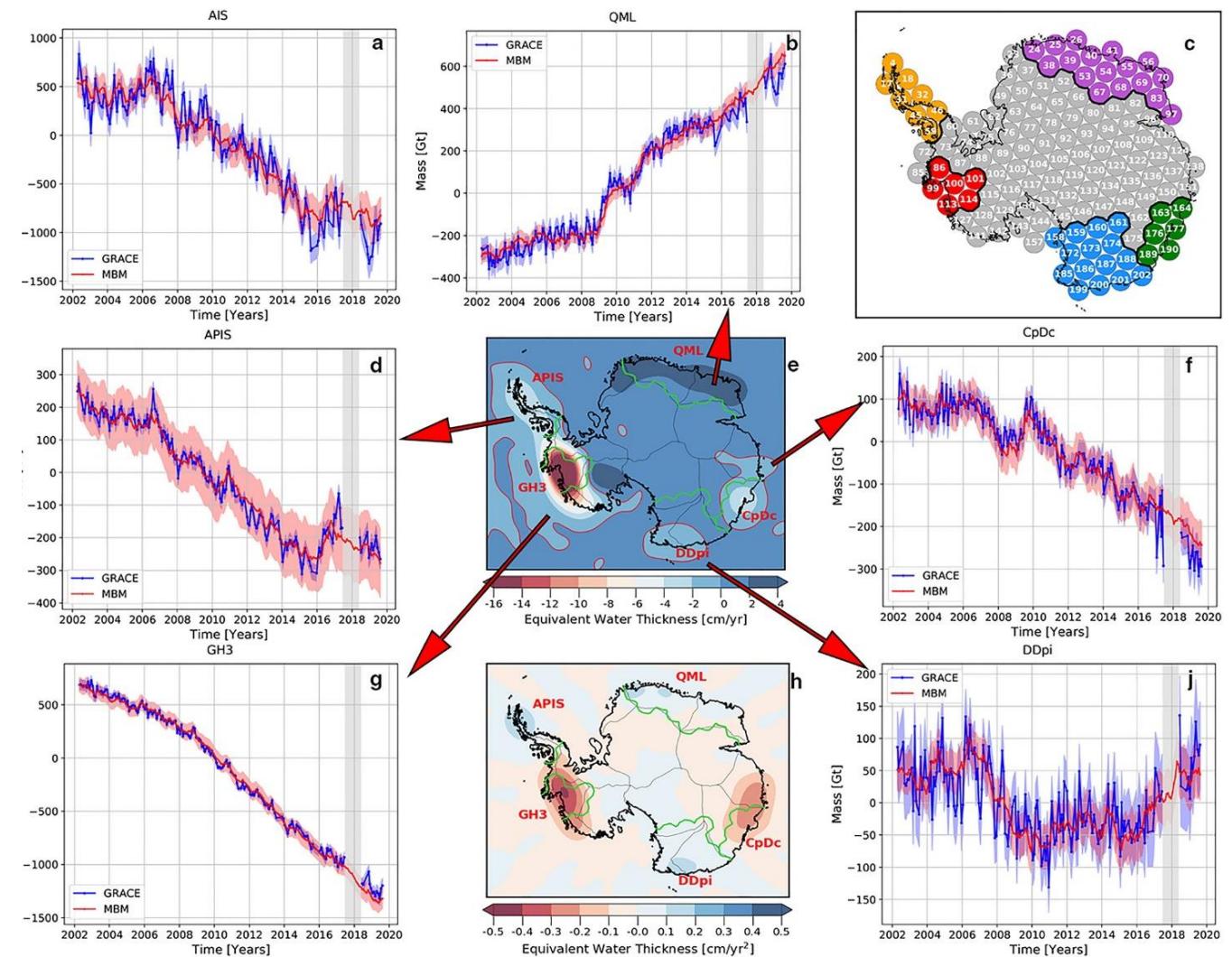


Image: <https://www.jpl.nasa.gov/missions/gravity-recovery-and-climate-experiment-grace>



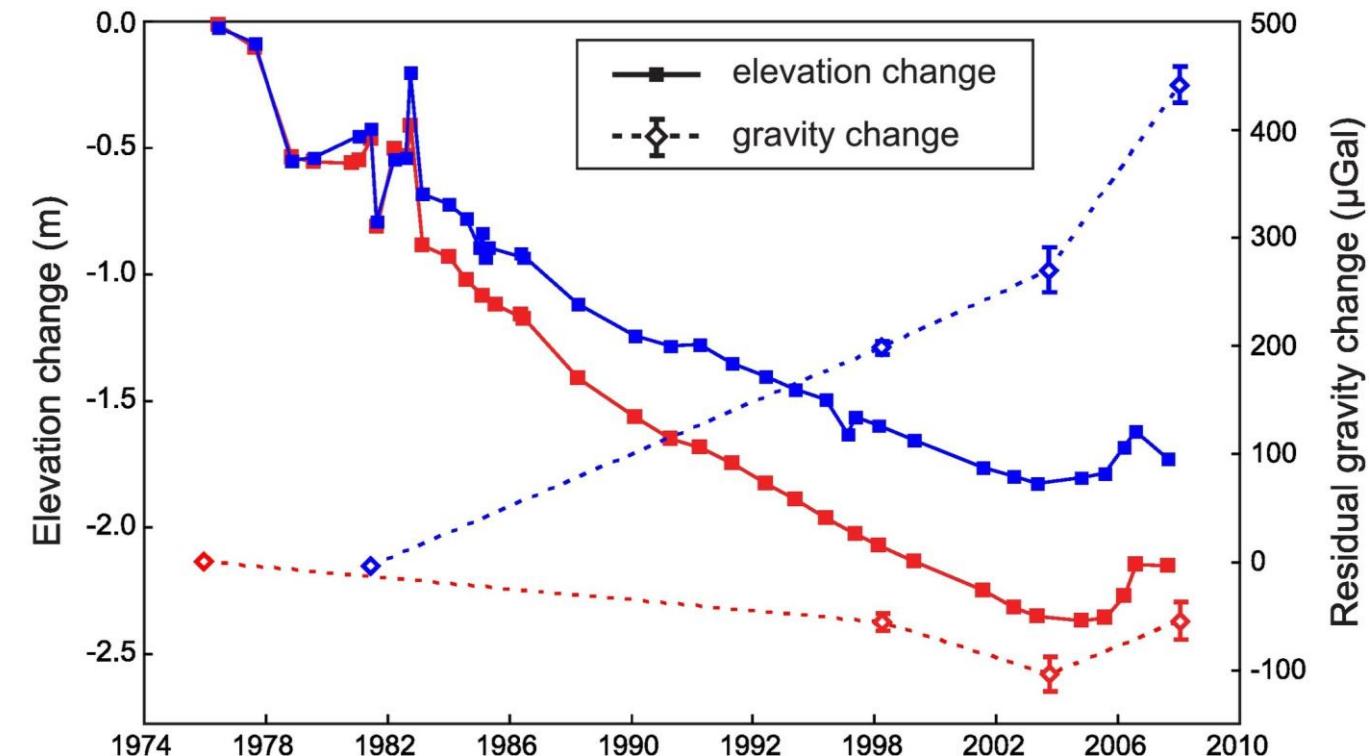
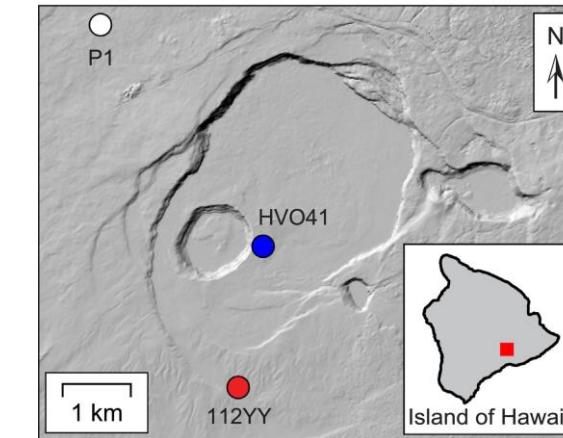
What can gravity data tell us?

- High resolution time variable gravity field,
 ➤ Monitor volcano



USGS

<https://www.usgs.gov/news/volcano-watch-how-measuring-gravity-mauna-kea-helps-us-monitor-mauna-loa>

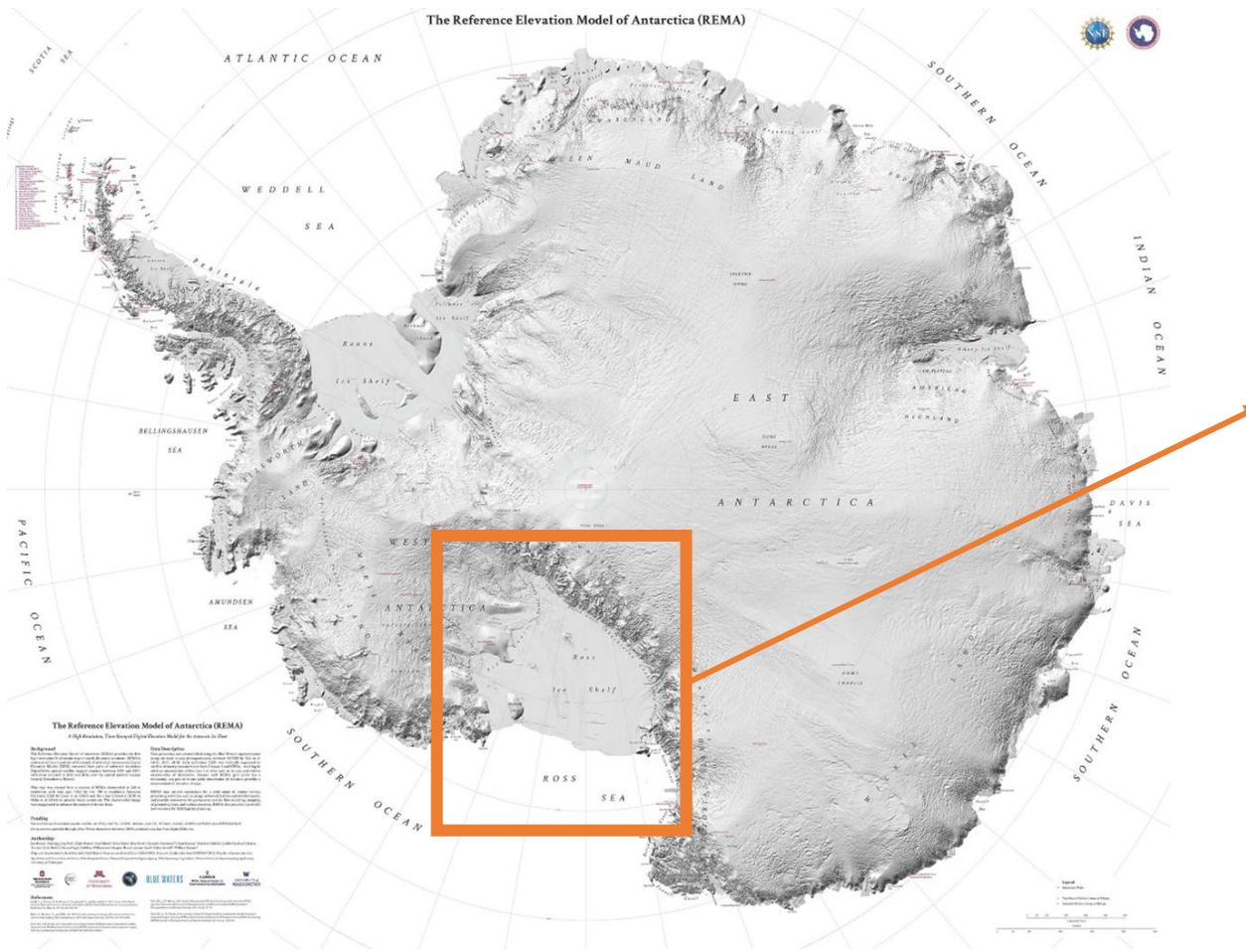


de Zeeuw-van Dalfsen & Poland., 2023

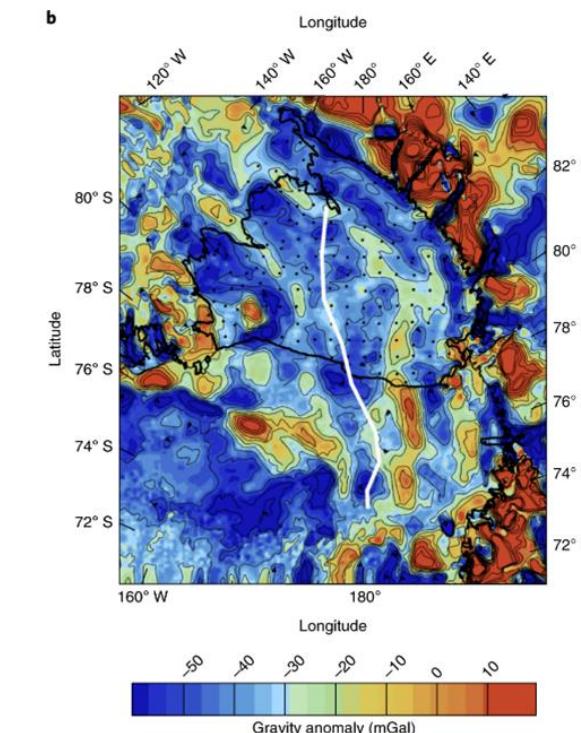
$$1\mu\text{Gal} = 1\text{e-}3 \text{ mGal} = 1\text{e-}8 \text{ m/s}^2$$

What can gravity data tell us?

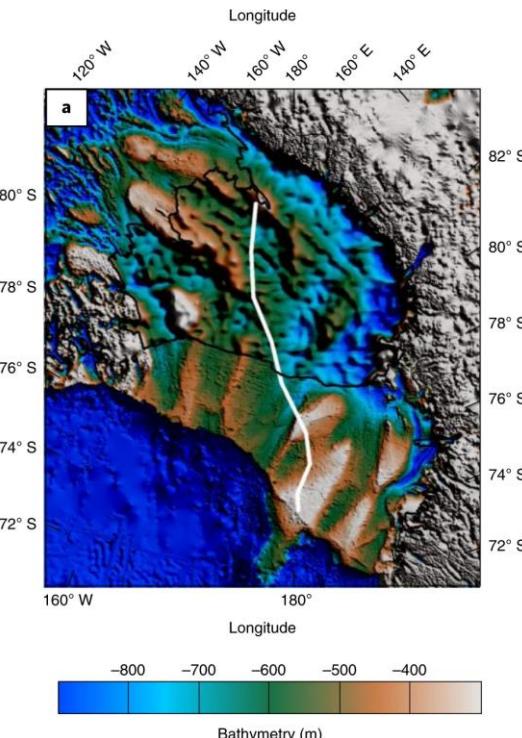
- sub-ice shelf bathymetry



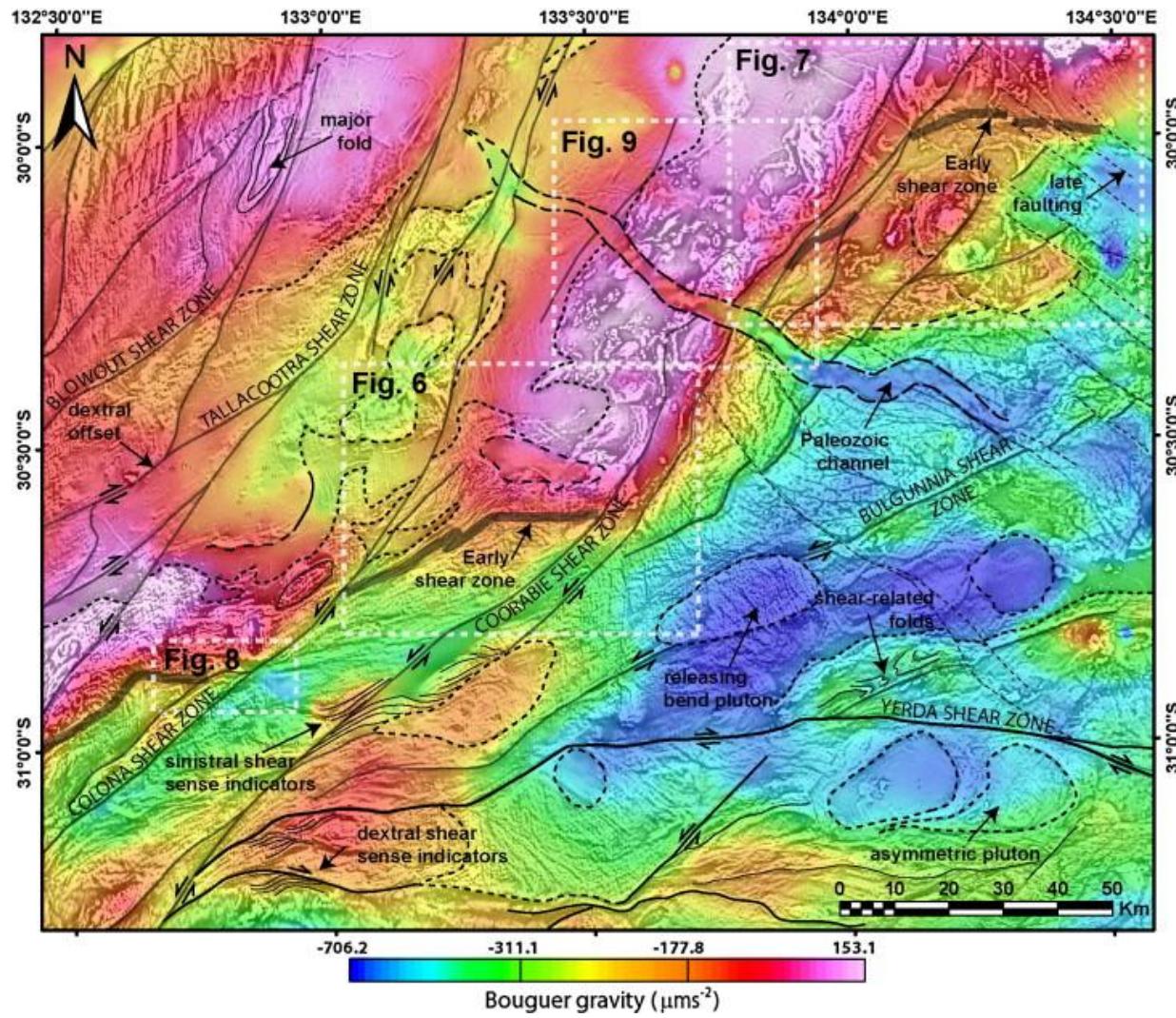
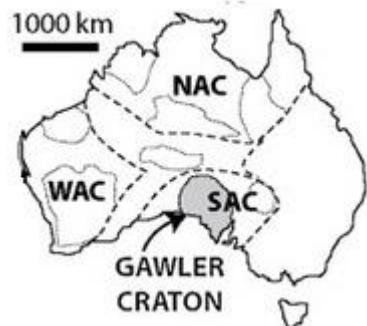
Howat et al., 2019



Tinto et al., 2019



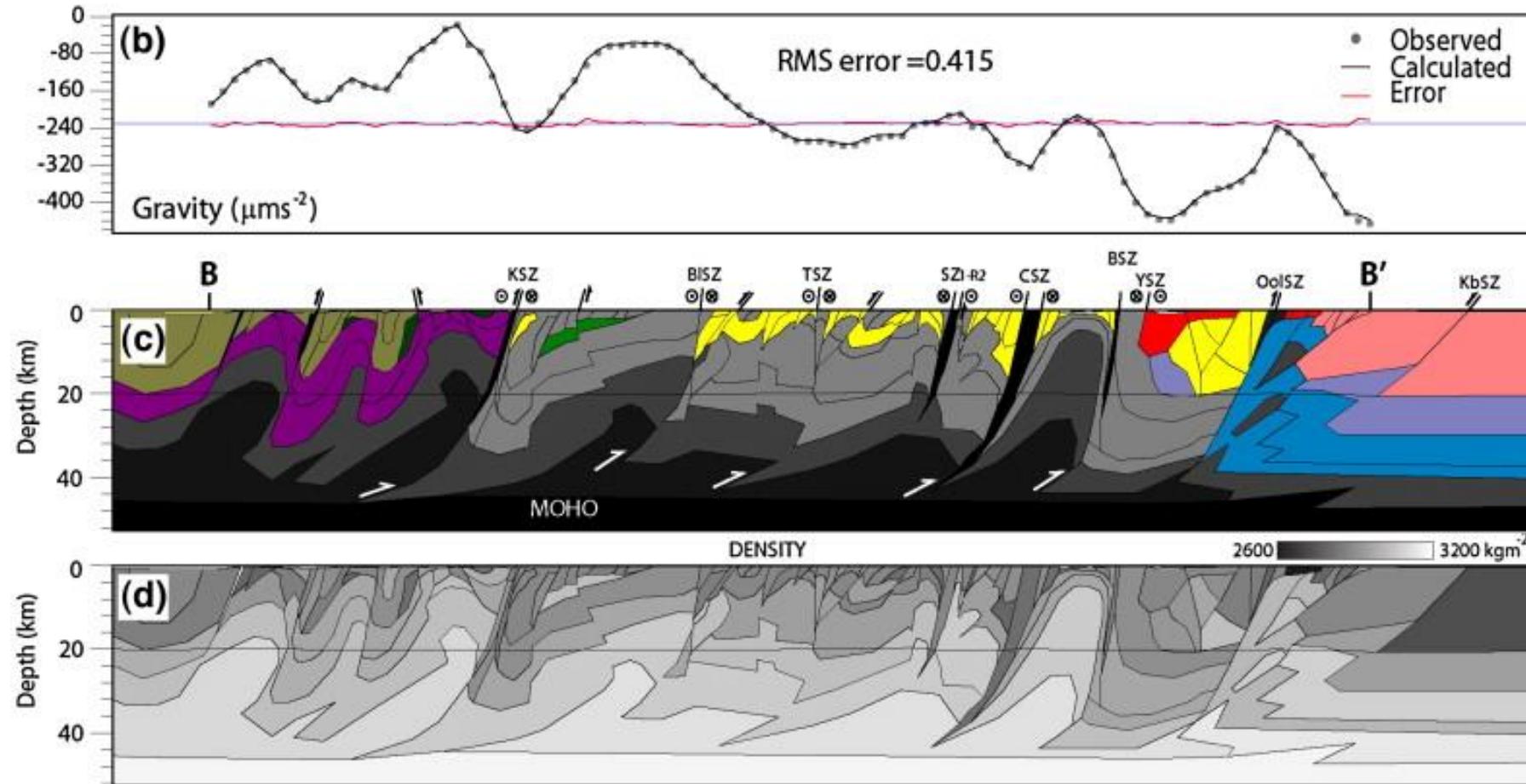
What can gravity data tell us?



- Mapping geological units: fold, shear zone, fault, dike

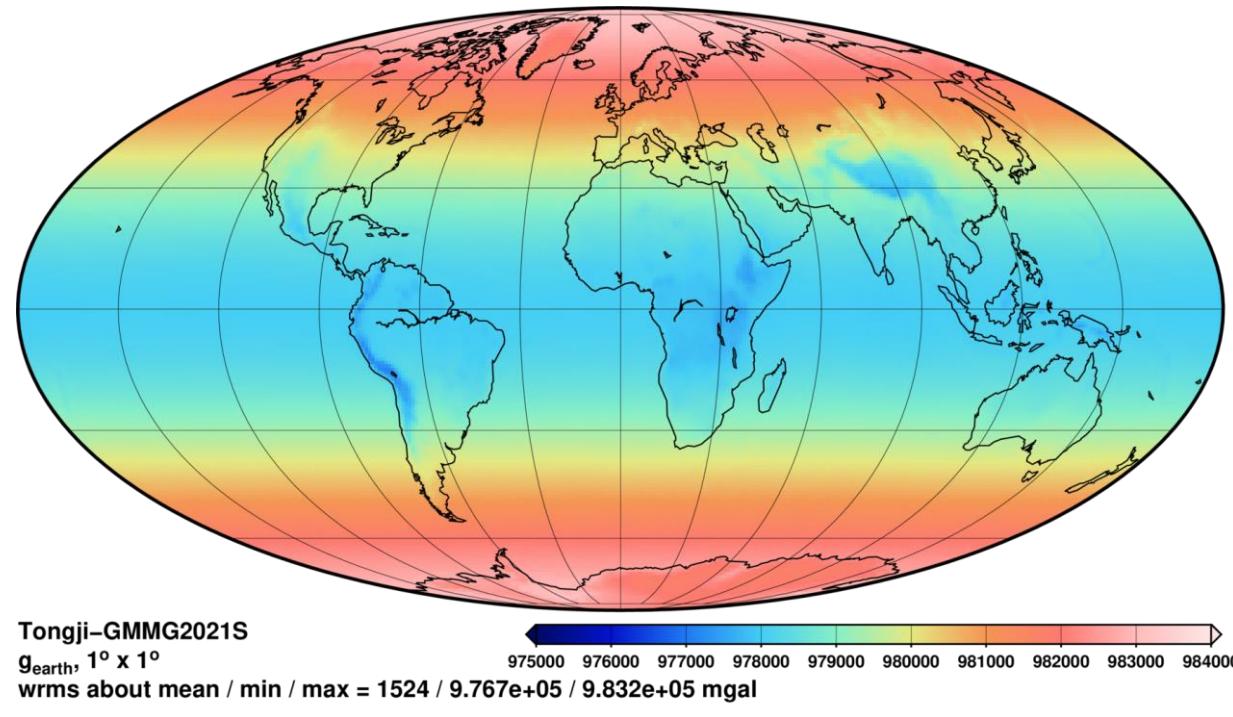
What can gravity data tell us?

- process-oriented geological modelling

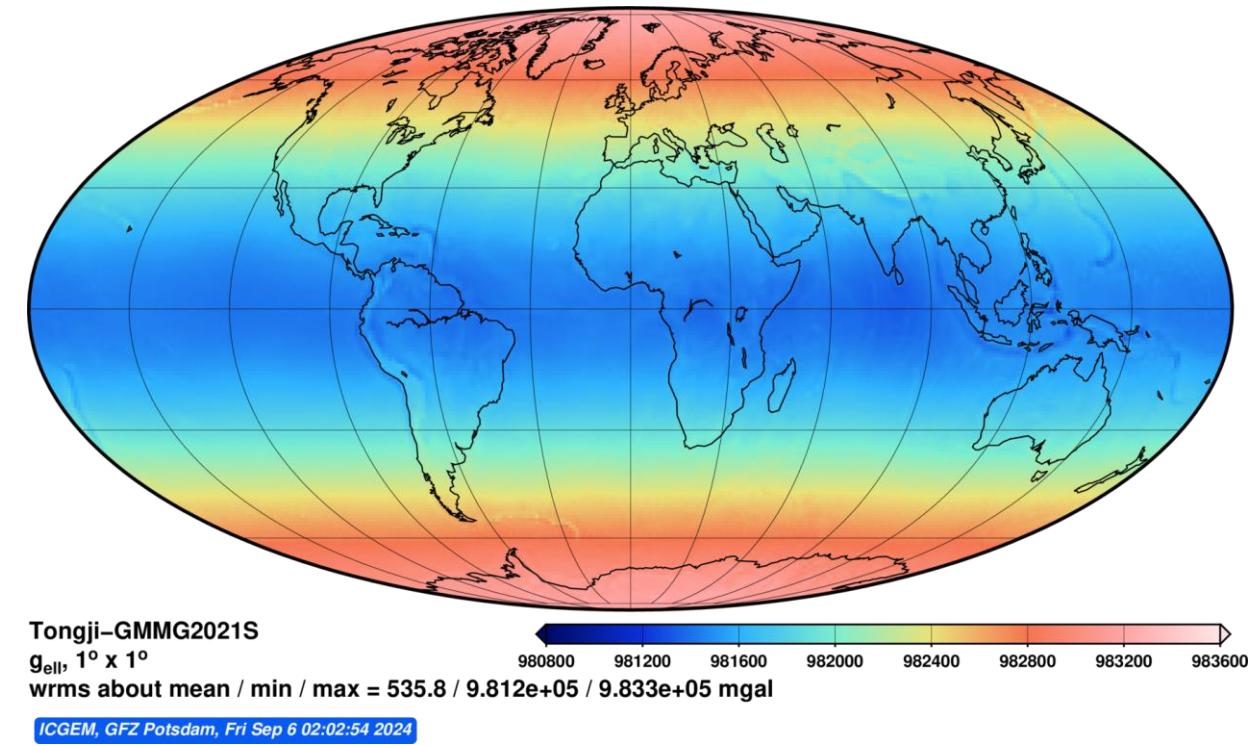


Earth Gravity field

- The solid-earth is not homogenous



Earth Gravity at surface topography

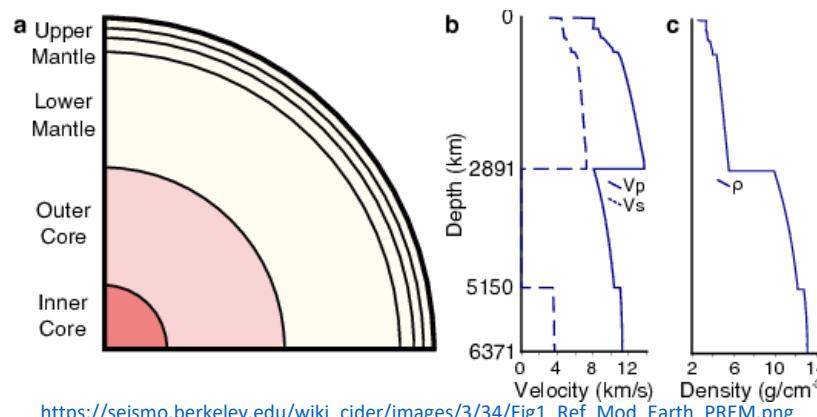
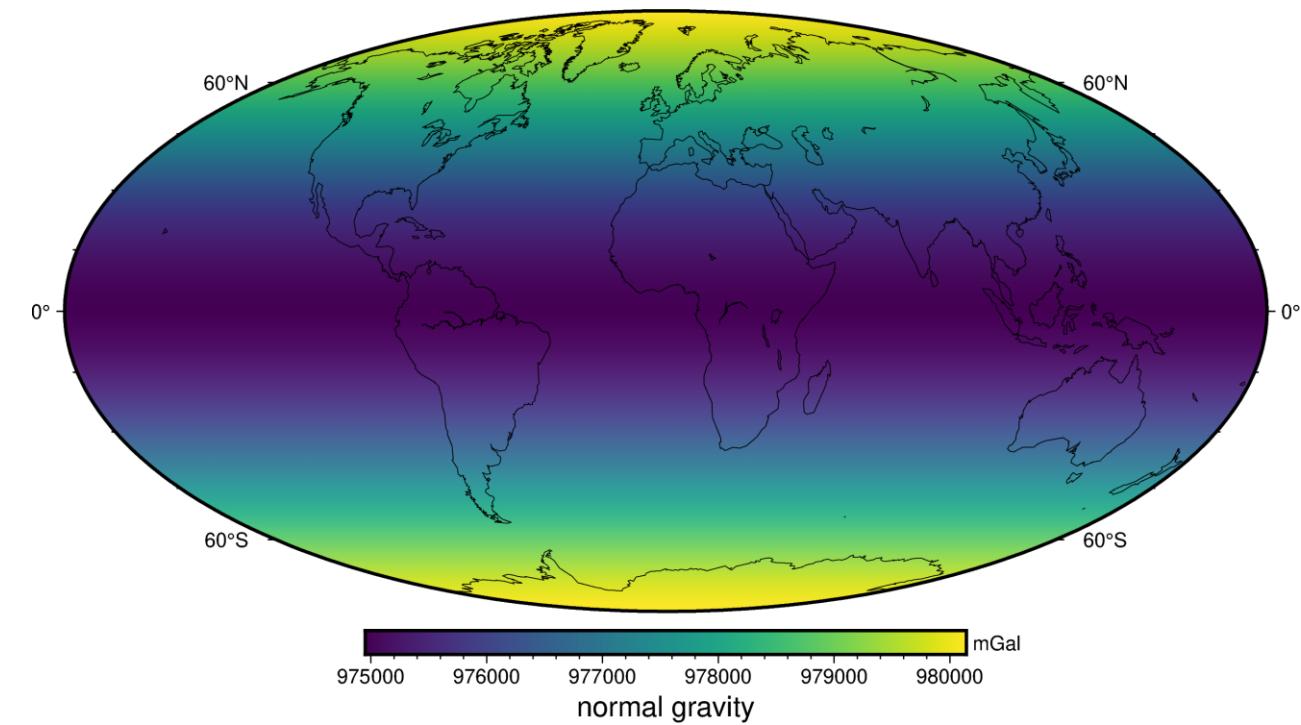
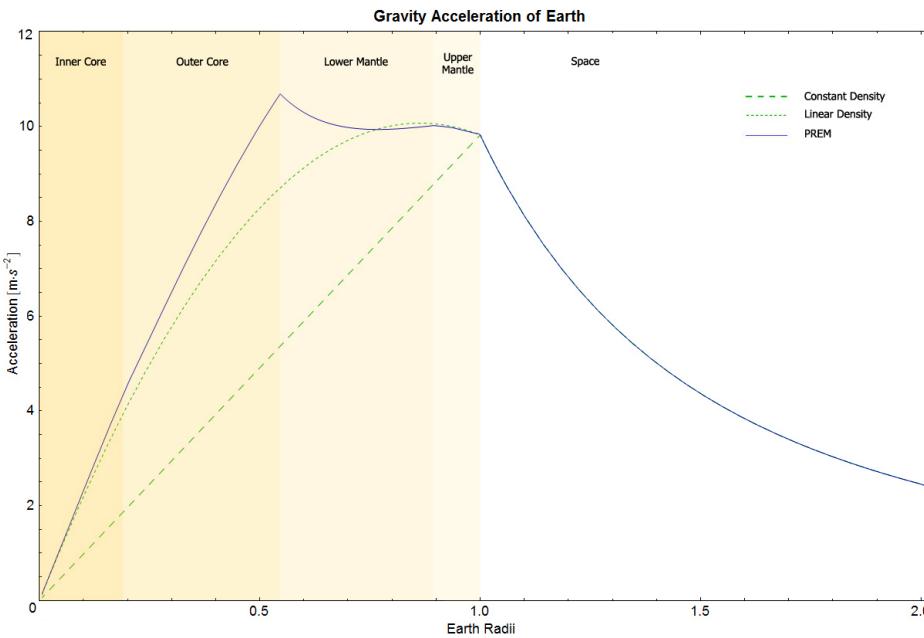


Earth Gravity at ellipsoid

- Do you notice the difference between these two maps?
- What controls the gravity we see?

Reference Earth Model

- 1 D reference earth model and normal gravity

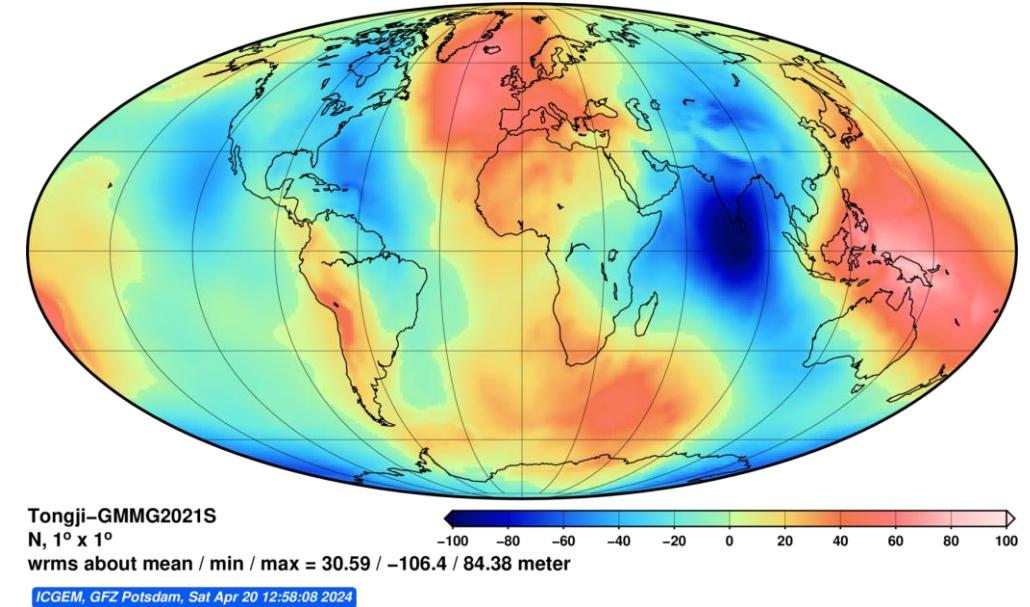
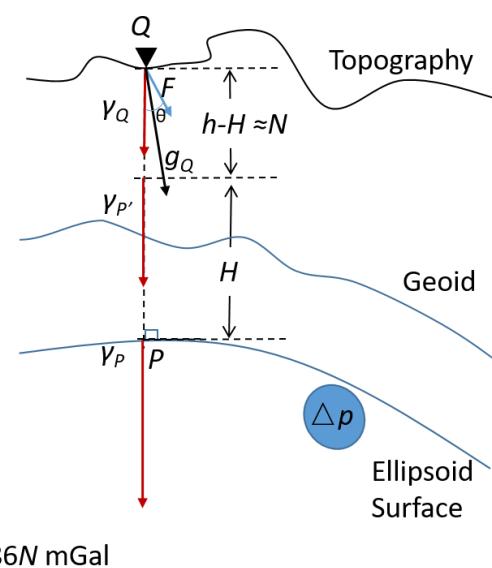
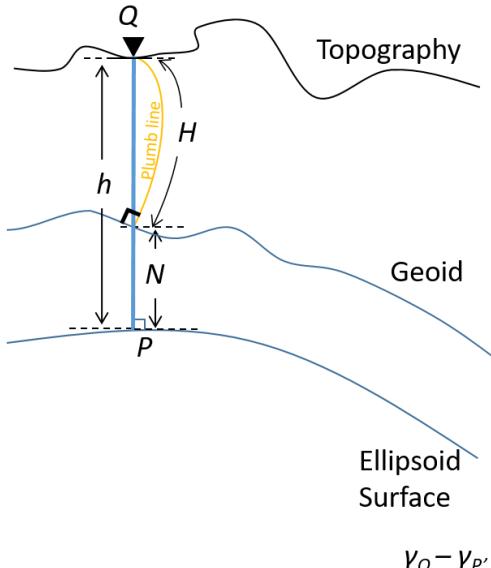


WGS84 normal gravity at ellipsoid

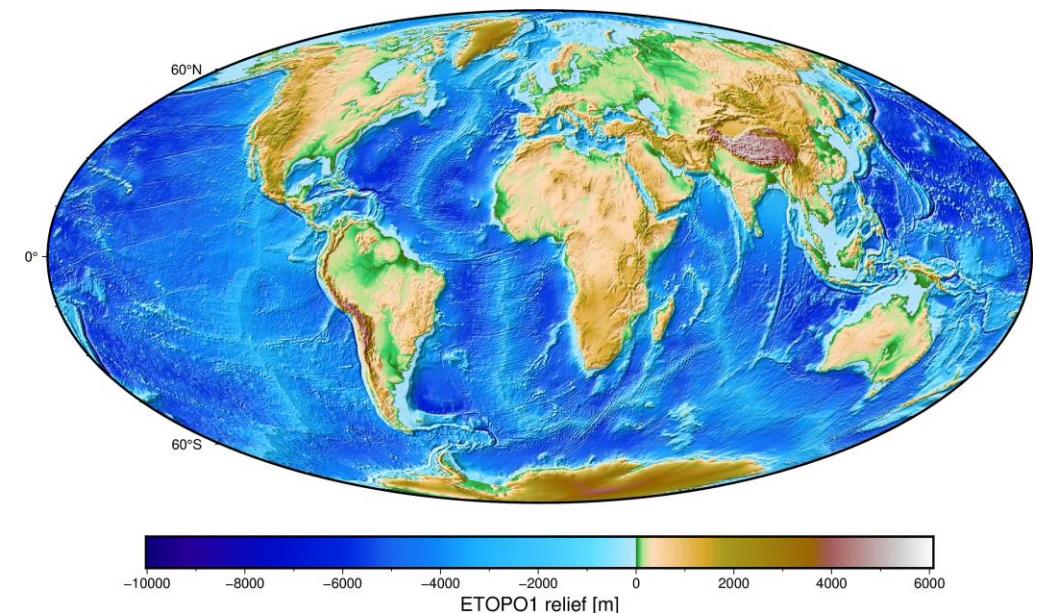
Reference Earth Model

- Geoid and Ellipsoid

Geoids represent a hypothetical global sea level as it would be shaped by gravity if oceans could flow unobstructed through land.
 AKA: mean sea-level

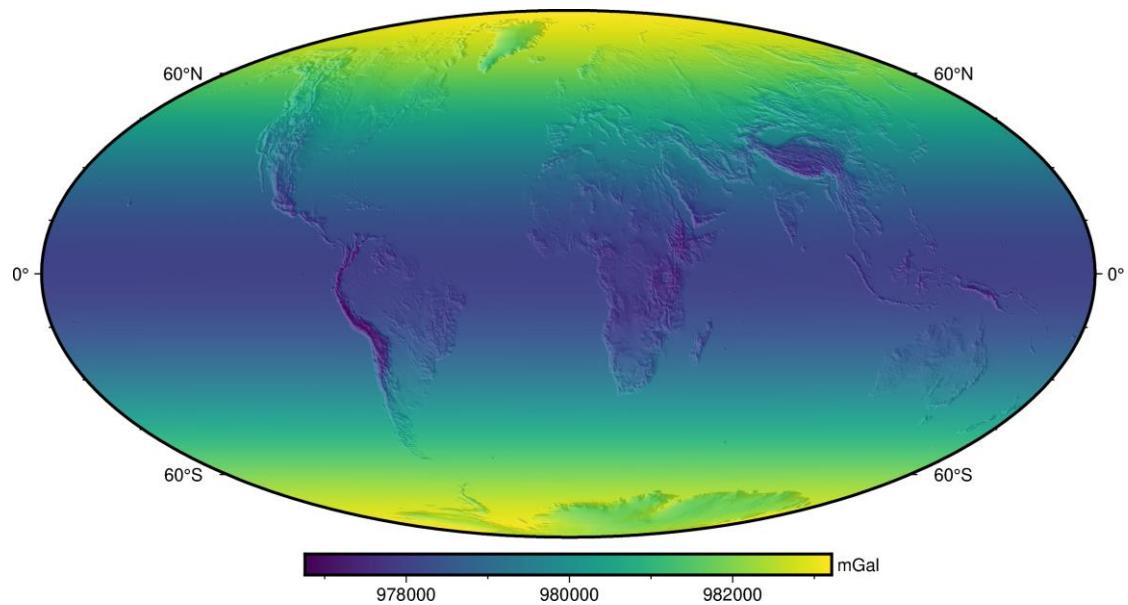
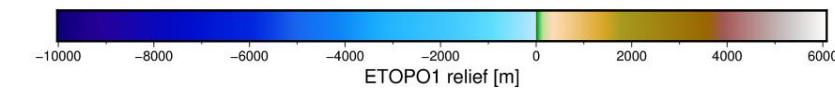
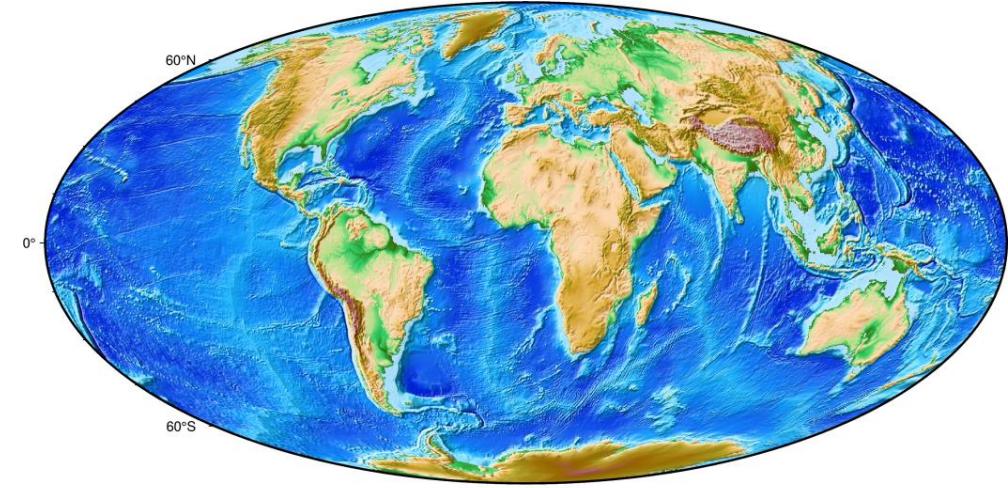


Geoid (relative to ellipsoid, WGS84)

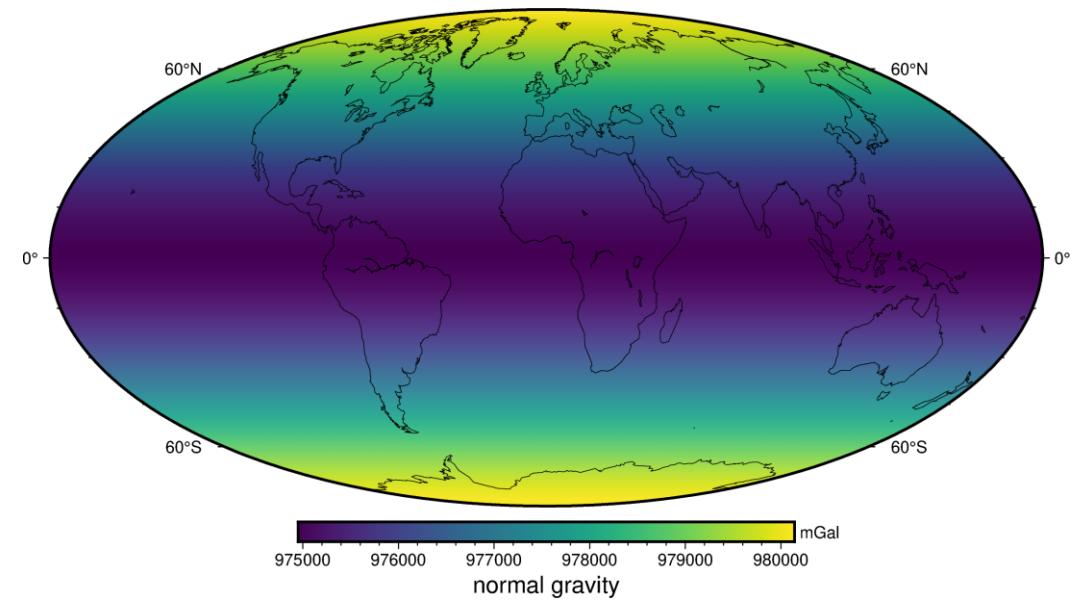


Reference Earth Model

- The impact of observational height

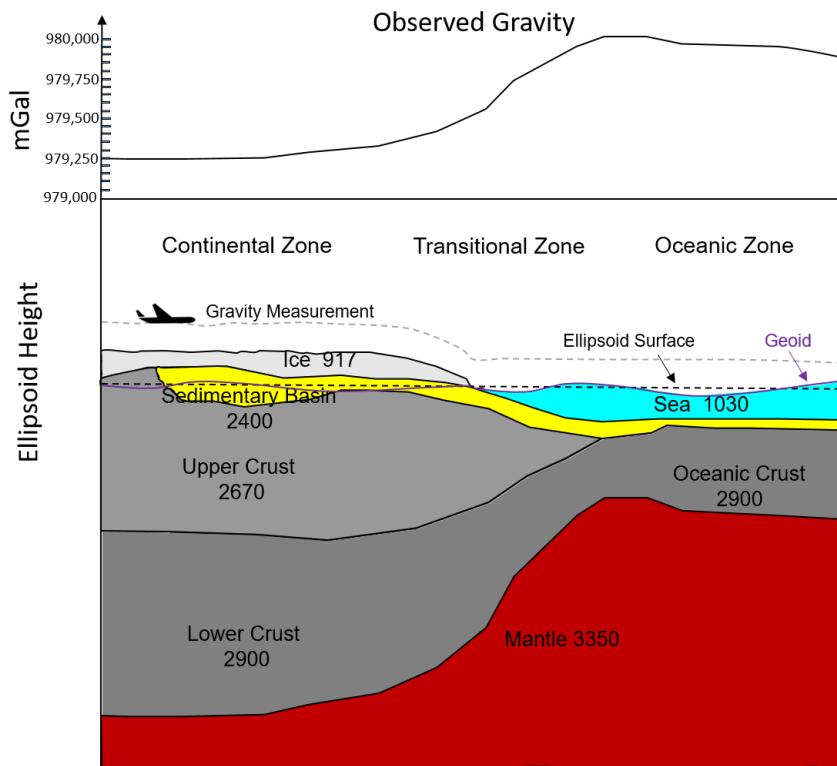


WGS84 normal gravity at earth surface



WGS84 normal gravity at ellipsoid

- The solid-earth is not homogenous



Sedimentary Rocks

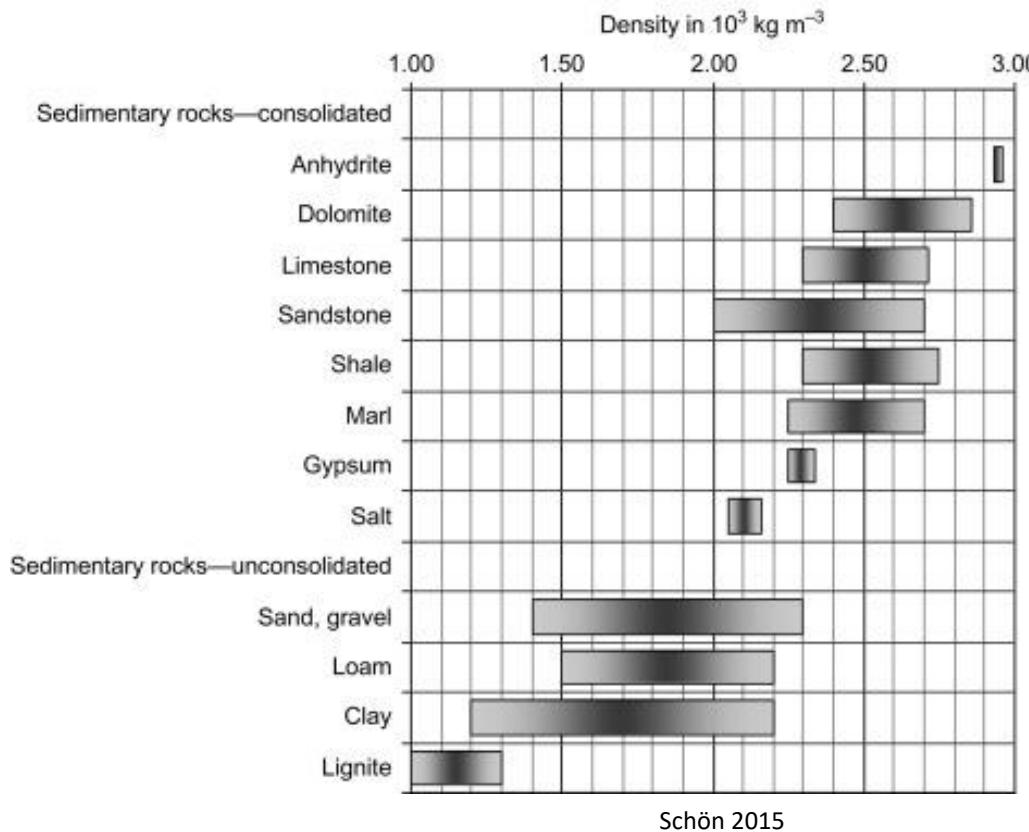
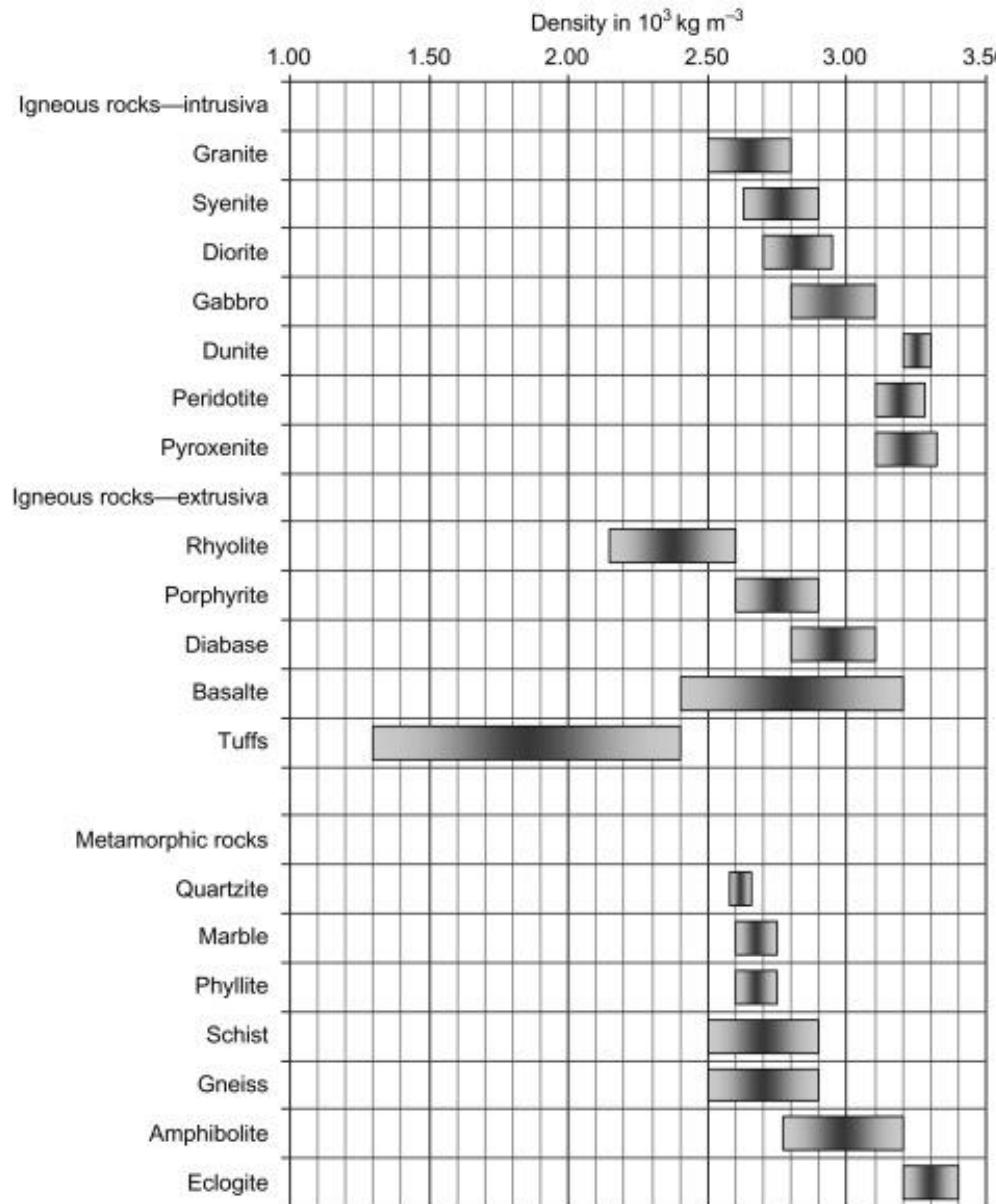
- Compaction – increases density by reducing pore-spaces
- Cementation – increase density by infilling pore-spaces
- Fluid-flux – replacing fluid with a different density can track fluid flux (e.g. injecting CO₂ into a brine aquifer)
- Changes in depositional environment – e.g. shale vs sandstone
- Metamorphism

Crust – Bulk chemistry

- Bulk chemistry (mafic vs intermediate vs felsic)
- Alteration
- Temperature

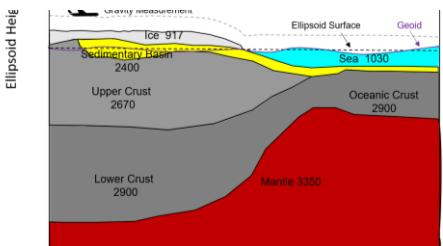
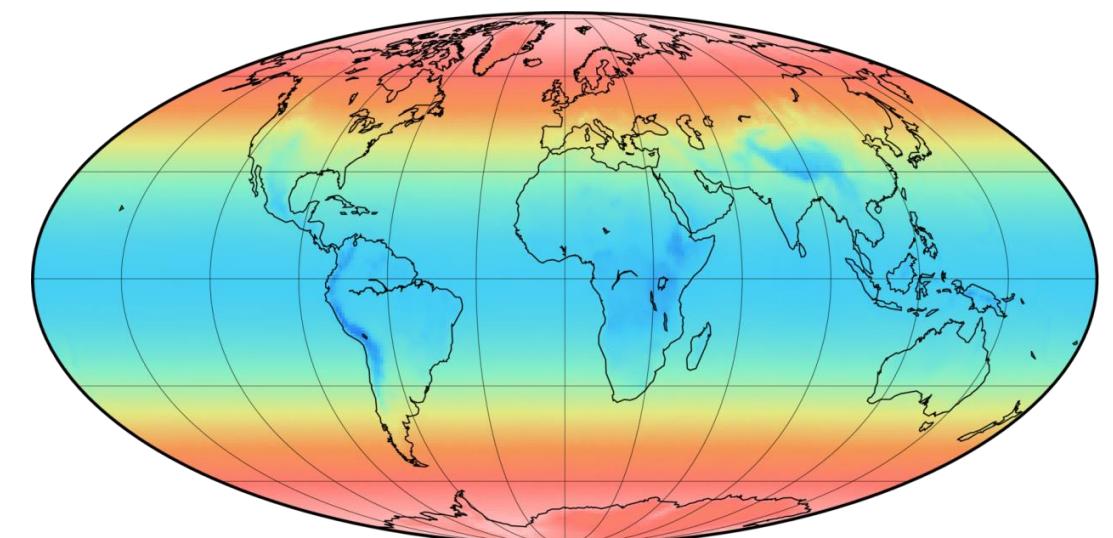
Mantle thermal expansion and Bulk chemistry

- What controls the density?

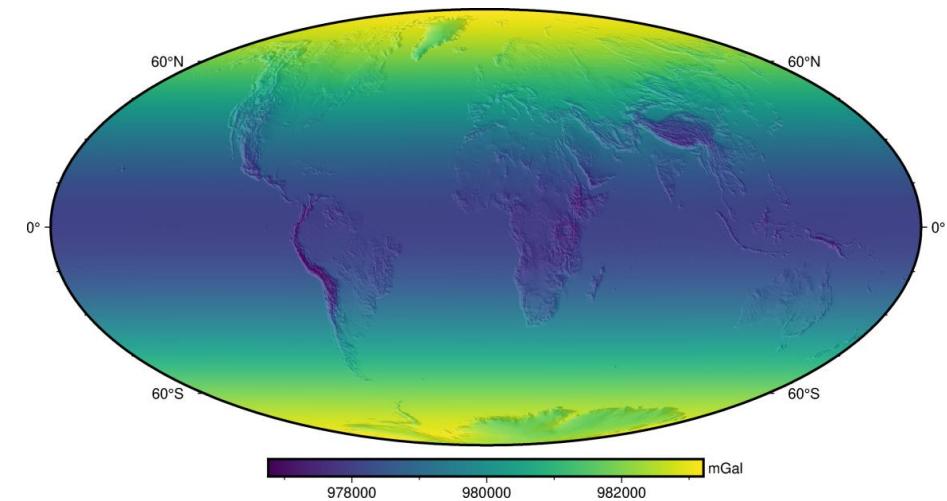


Schön 2015

- Earth Gravity field

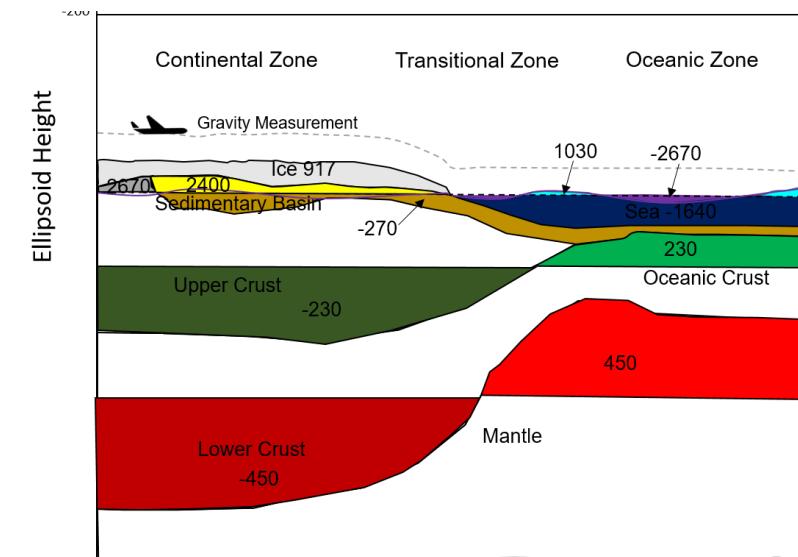


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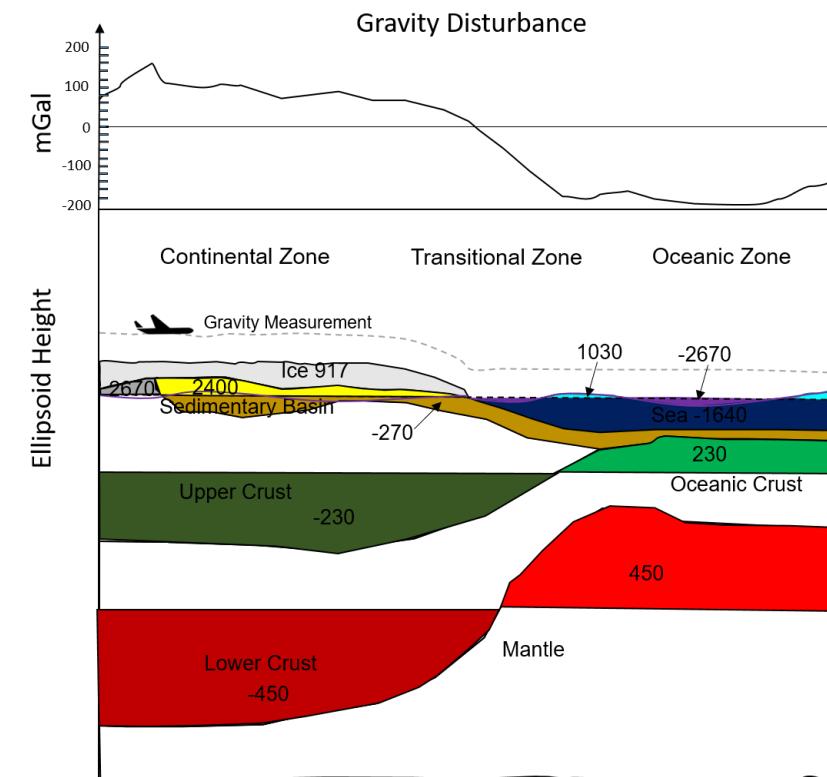
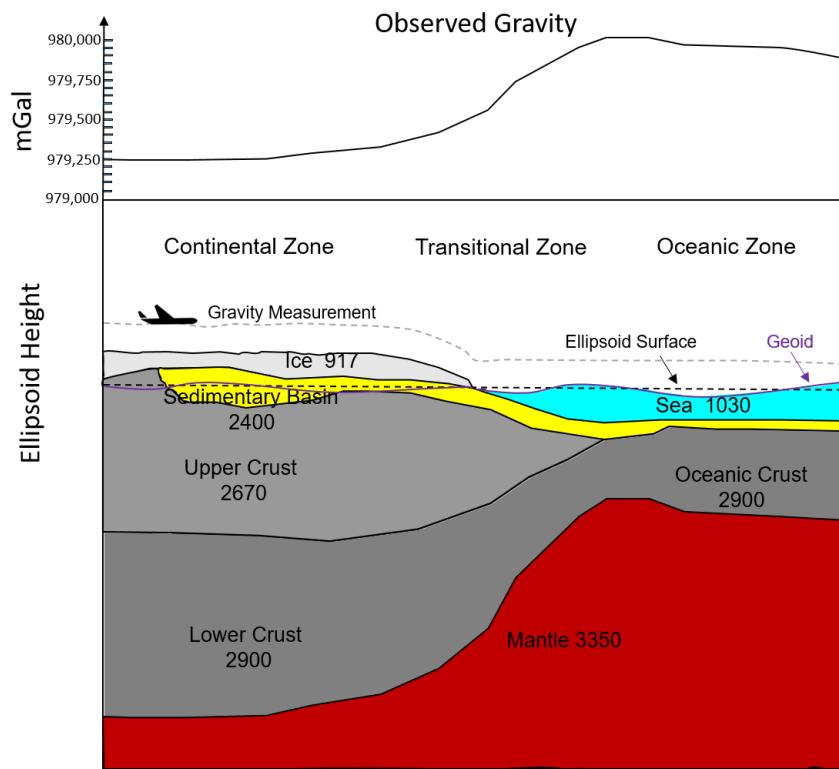
Normal gravity (latitude variation + height variation)

+



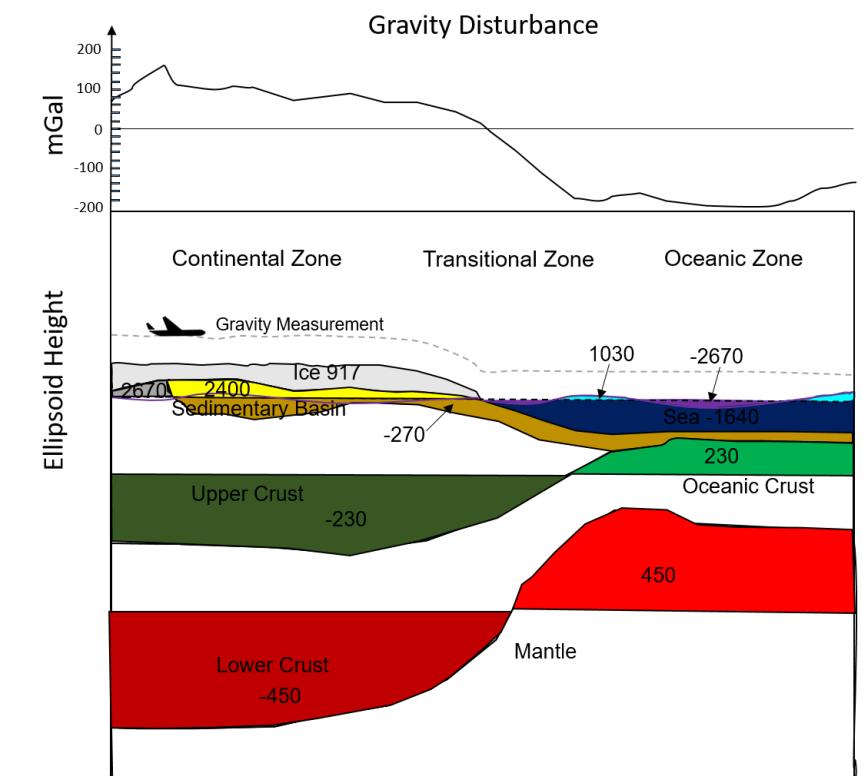
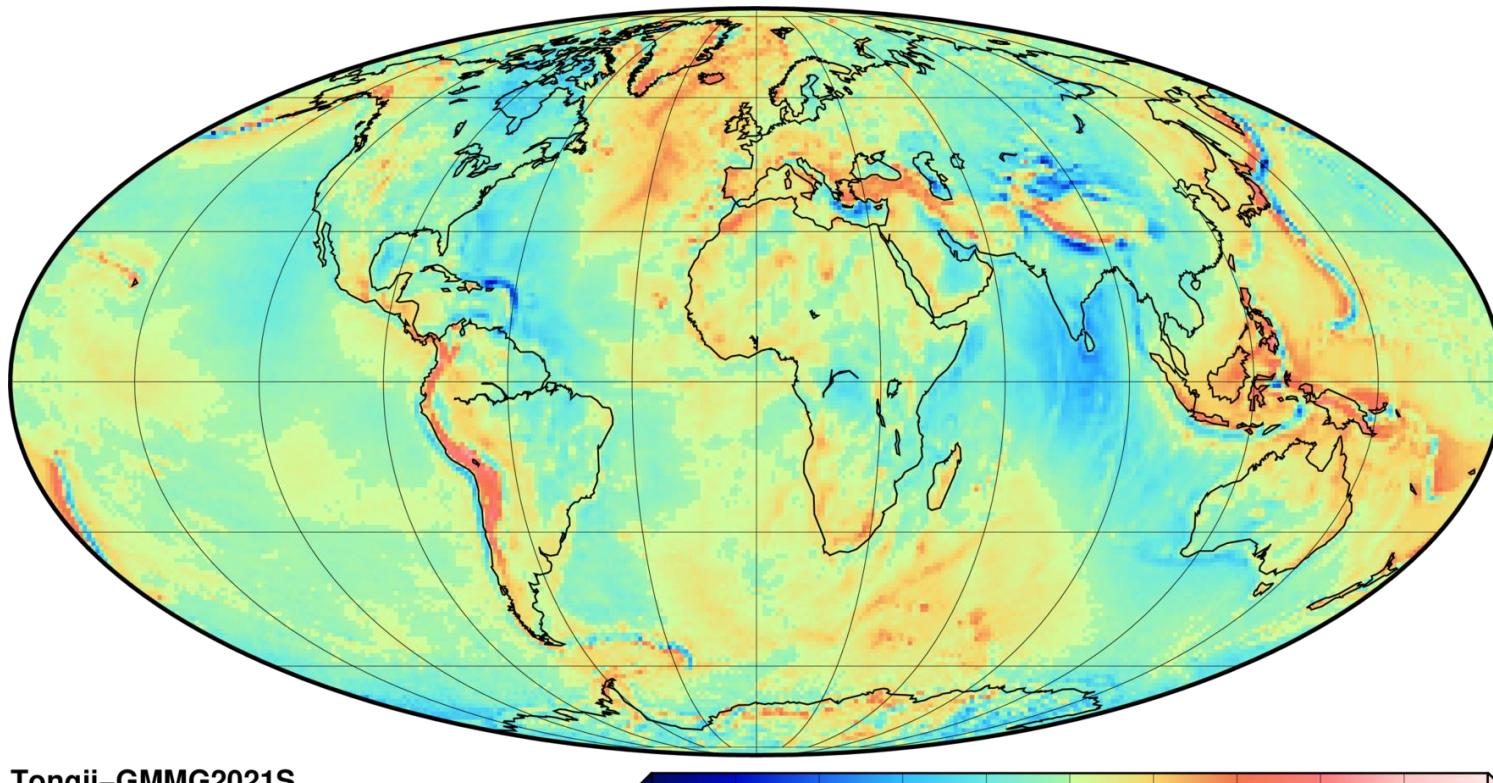
Density variation due to geology

- Free-Air Disturbance

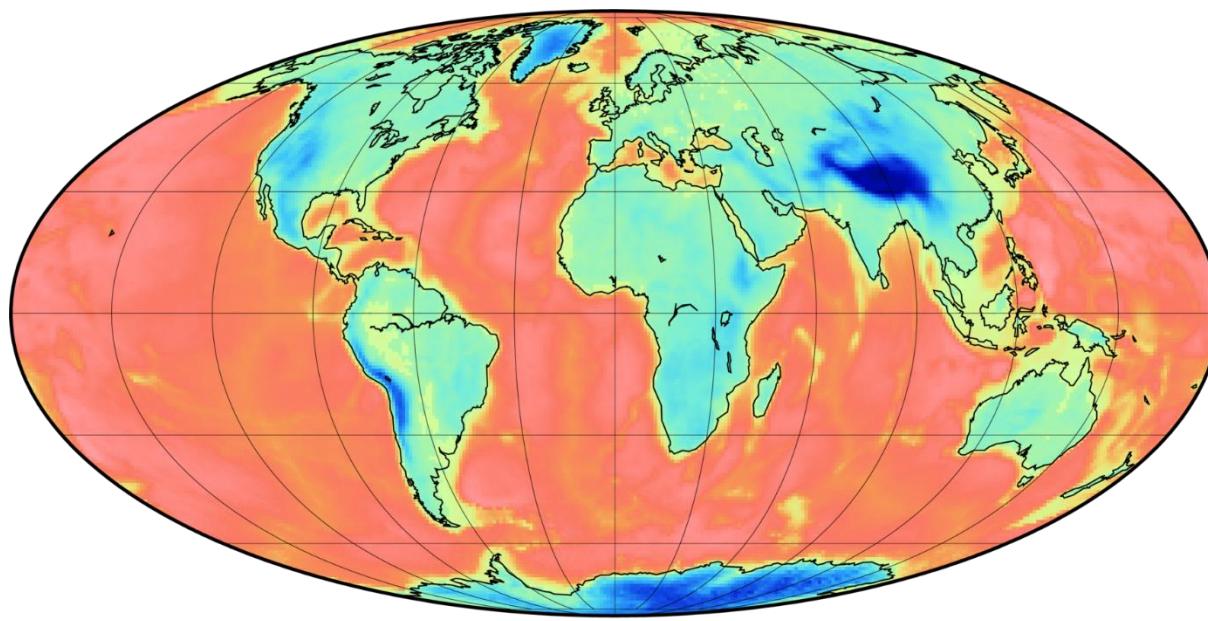


What controls the density?

- Free-Air Disturbance

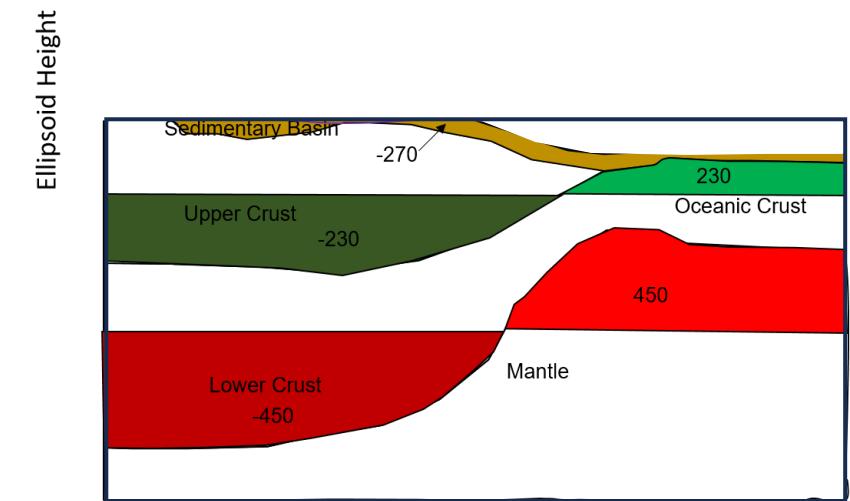


- Bouguer Gravity

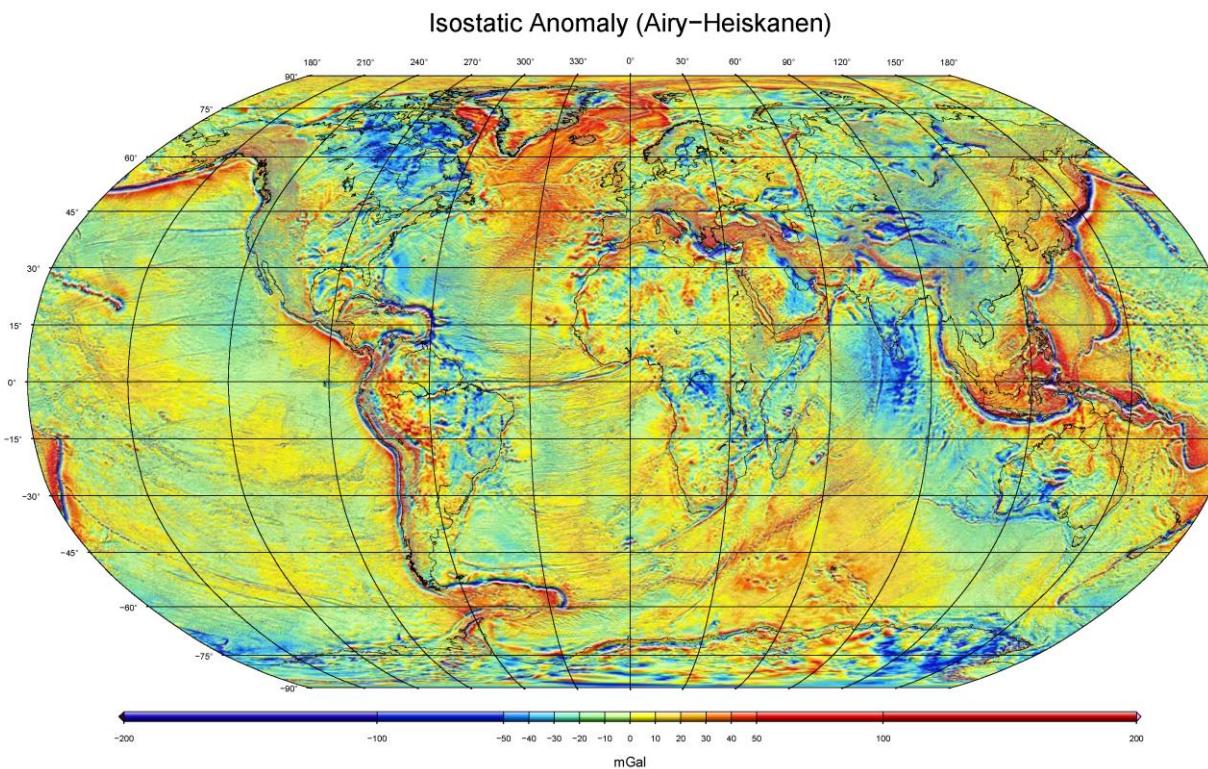


Tongji–GMMG2021S
 Δg_B , $1^\circ \times 1^\circ$
wrms about mean / min / max = 185.3 / -586.5 / 454.2 mgal

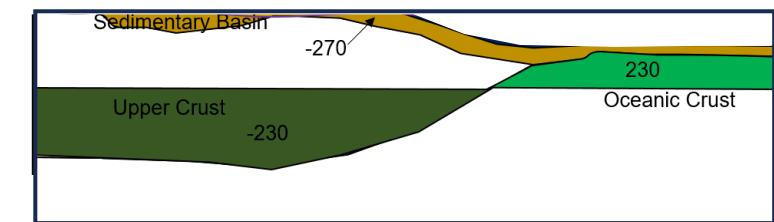
ICGEM, GFZ Potsdam, Wed Nov 30 13:08:30 2022



- Residual Gravity

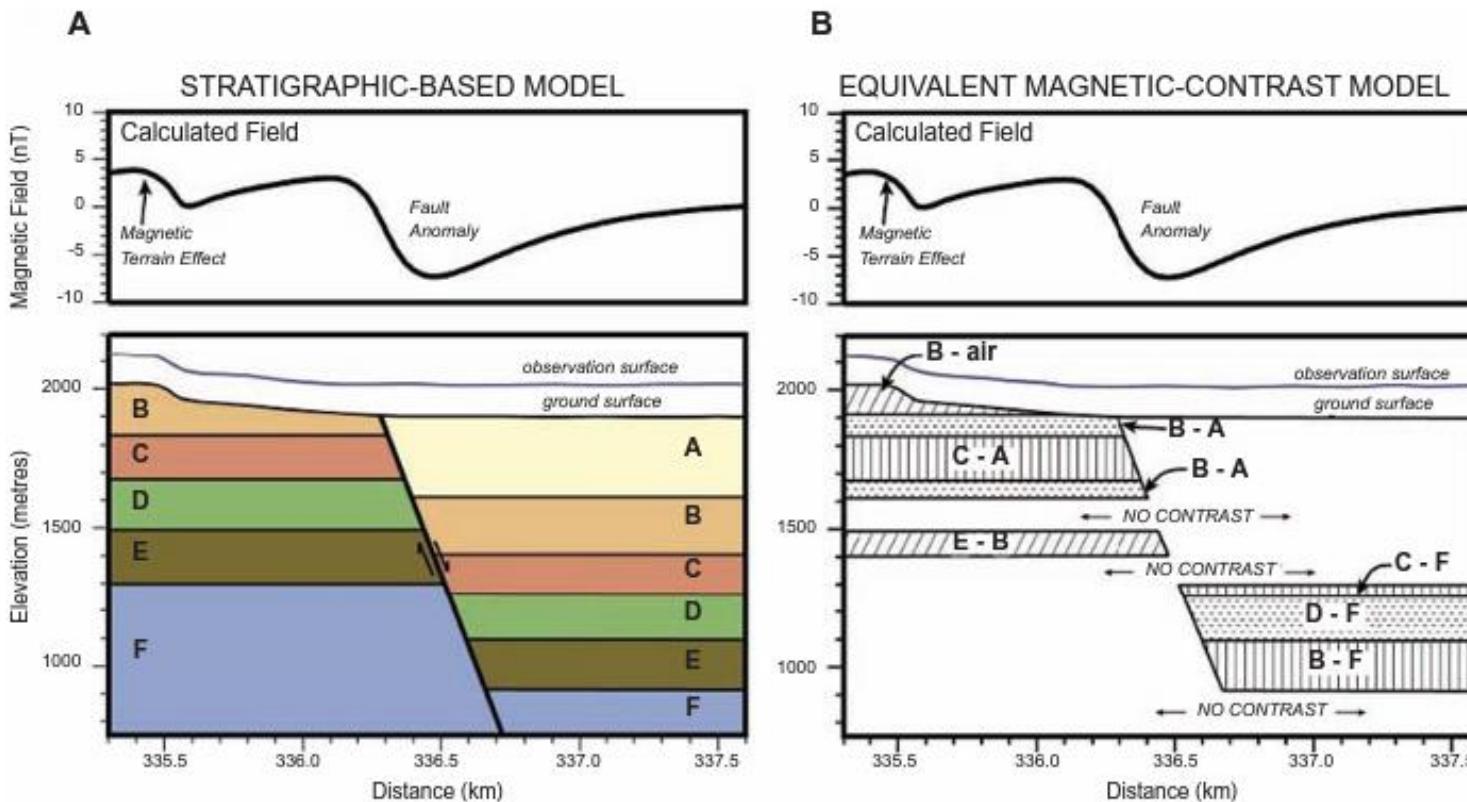


Ellipsoid Height



Bonvalot, S., Briais, A., Kuhn, M., Peyrefitte, A., Vales, N., Biancale, R., Gabalda, G., Moreaux, G., Reinquin, F. & Sarrailh, M. (2012). Global grids : World Gravity Map (WGM2012). Bureau Gravimetrique International. <https://doi.org/10.18168/bgi.23>

- We detect contrasts

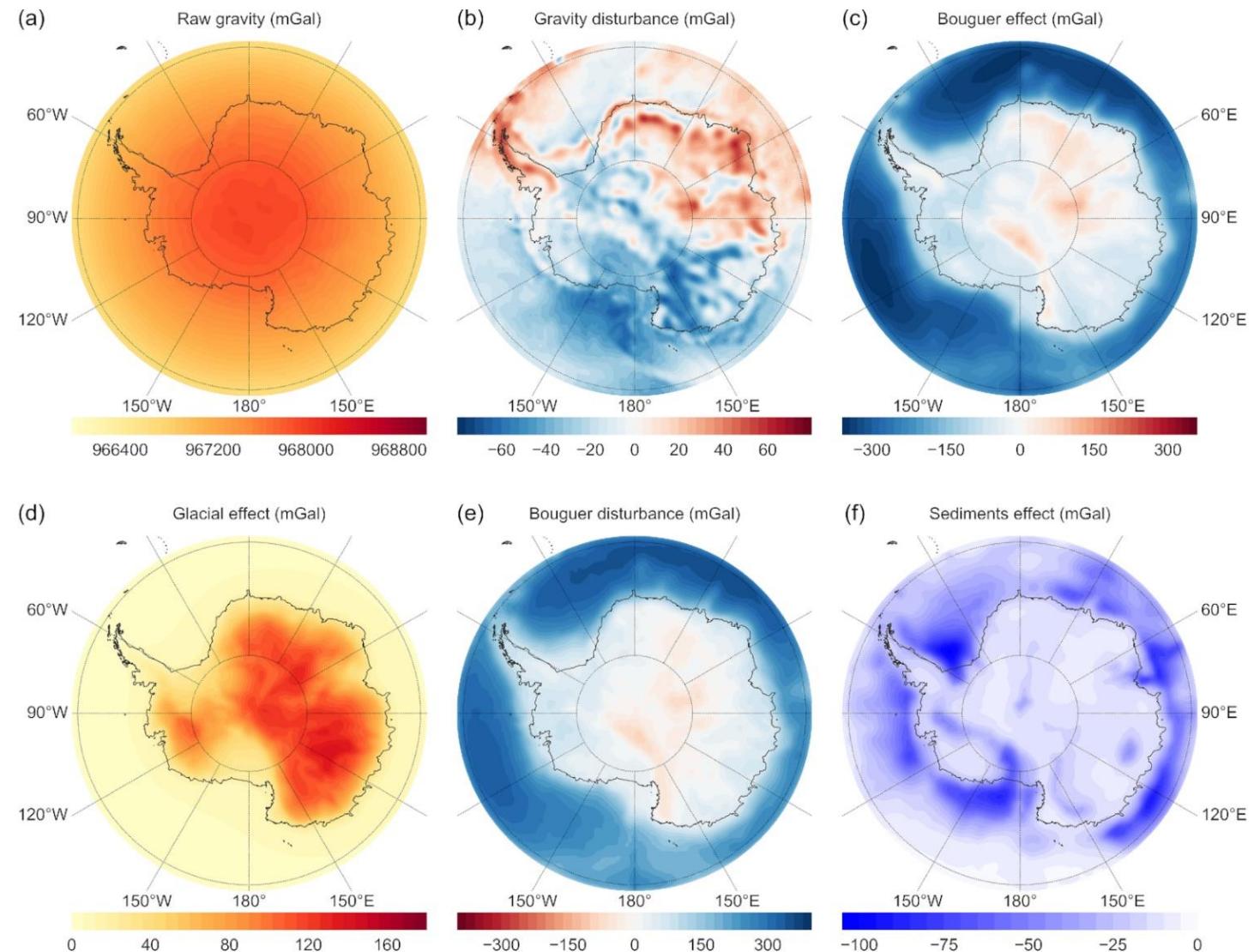
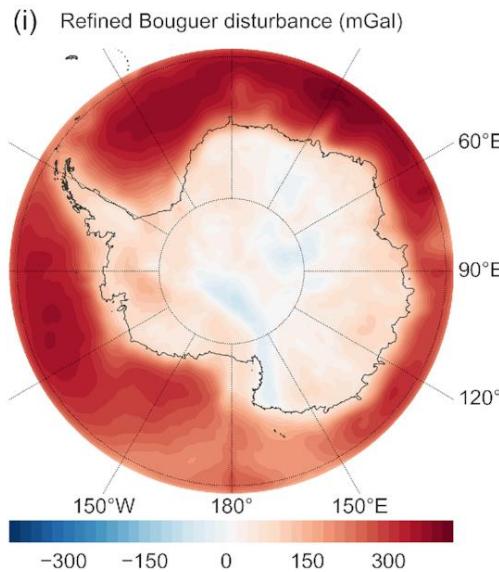


Isles & Rankin 2013

<https://www.aseg.org.au/sites/default/files/ebook-ASEG-eBook-Geo-Interpretation-of-Aeromagnetic-Data-Opt-for-user-1621.pdf>

Gravity anomalies

- Gravity effect of earth layers

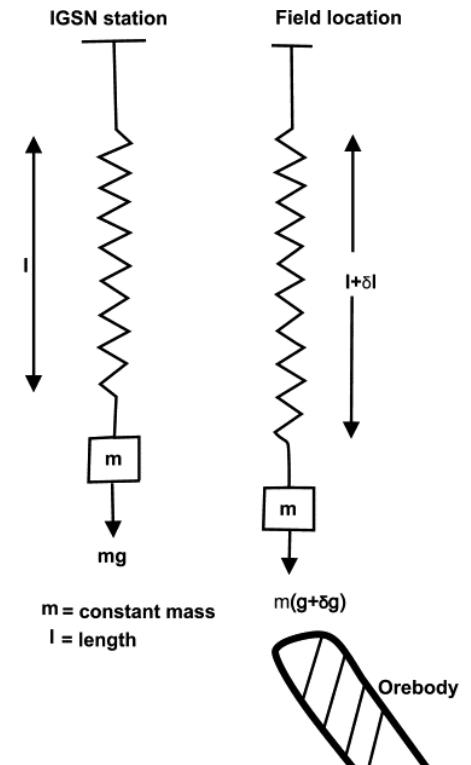


The gravimeter

CG6

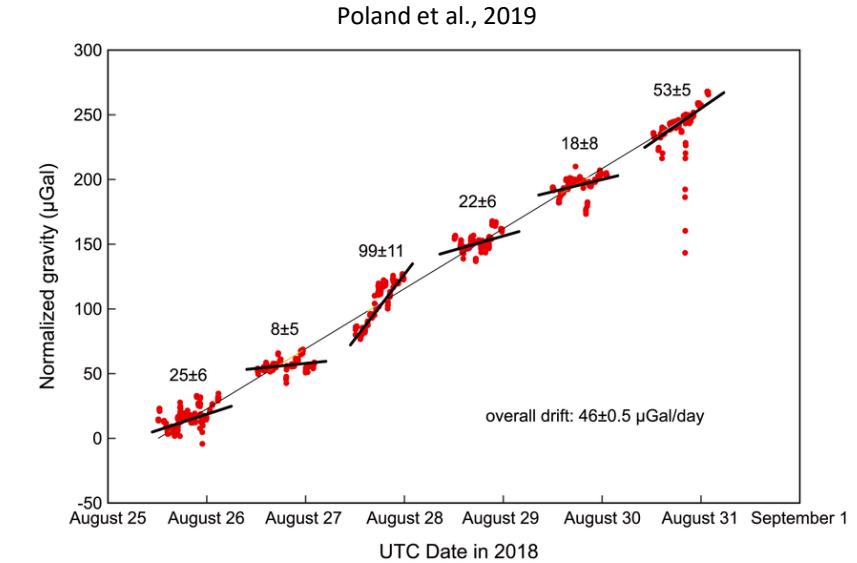


- Spring-based relative gravimeter
 - measures gravitational acceleration by detecting the displacement of a mass suspended on a spring
 - The displacement is proportional to the change in gravitational force
 - equipped with stabilizing system to reduce the effects of temperature changes and vibrations
 - Precision: ~0.1 microGal ($0.1 \mu\text{Gal} = 0.000001 \text{ m/s}^2$)



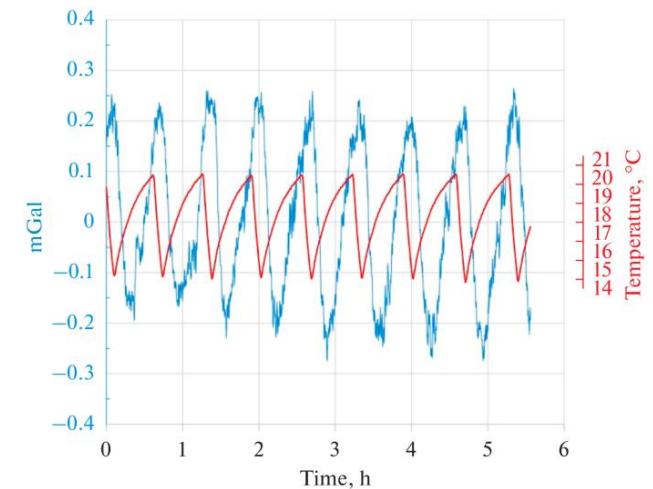
Instrument Drift:

- Gradual changes in the instrument's readings over time due to factors like mechanical wear or temperature variations.
- Can affect accuracy and consistency of measurements.
- Regular calibration and monitoring to detect and correct drift. Use of stable reference points for comparison.



Environmental Factors:

- Temperature and humidity fluctuations can impact the sensitivity and stability of the gravimeter's components.
- External vibrations from machinery or natural sources can interfere with measurements.

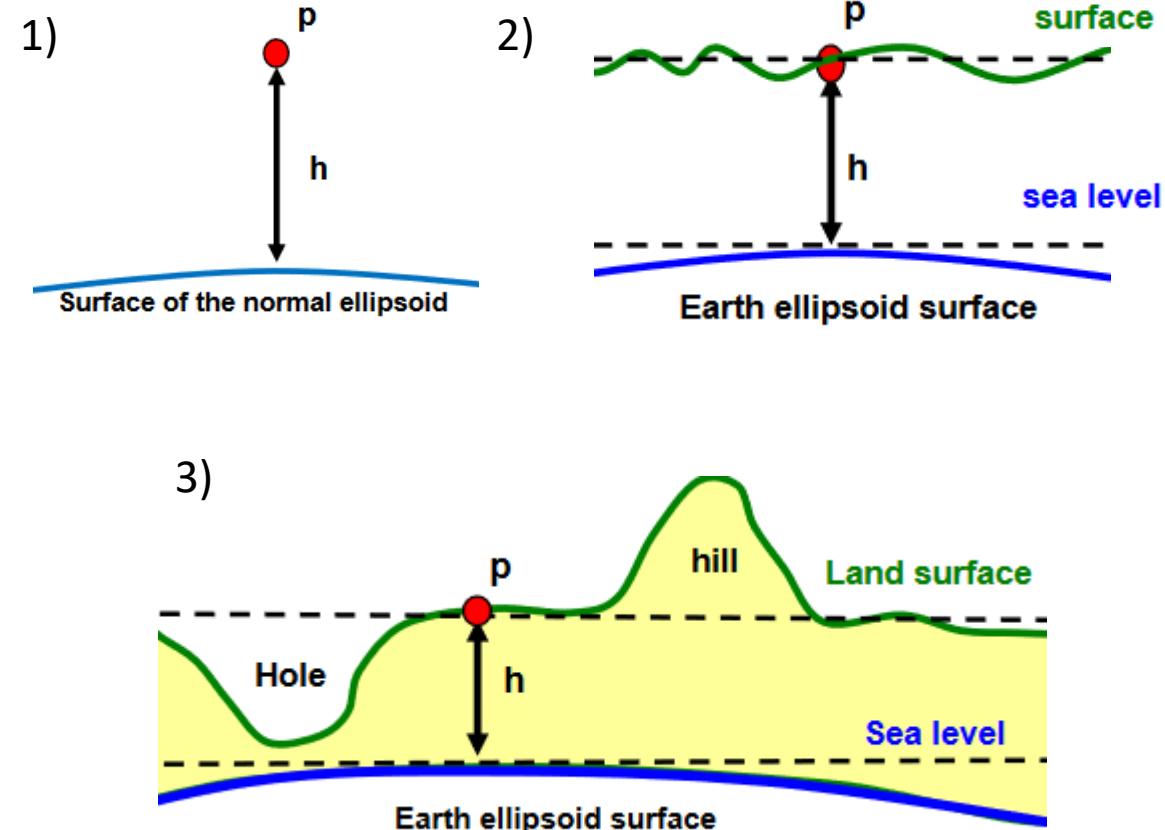


Zheleznyak et al., 2022

Gravity anomalies

- Types of Gravity Anomalies:

1. **Free-Air Anomaly/Disturbance:** Corrects for elevation but not for the mass of terrain.
2. **Bouguer Anomaly:** Corrects for the gravitational effect of topography and provides insight into subsurface density variations.
3. **Terrain Corrections:** Adjust for local topography to refine Bouguer anomalies.



Images: Introduction to Gravity Exploration method, Alsadi & Baban (2014)

- Variations in the Earth's gravitational field caused by differences in subsurface density

Gravity anomalies

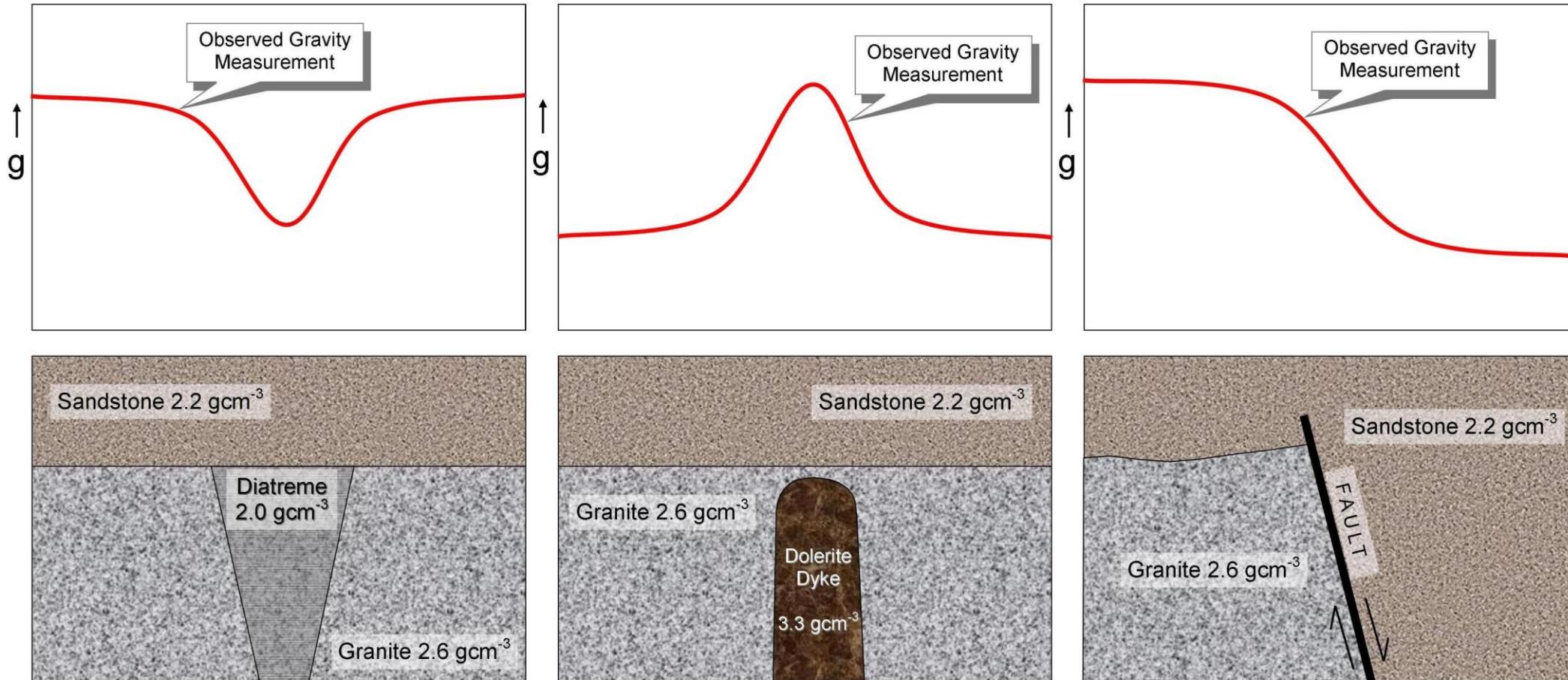
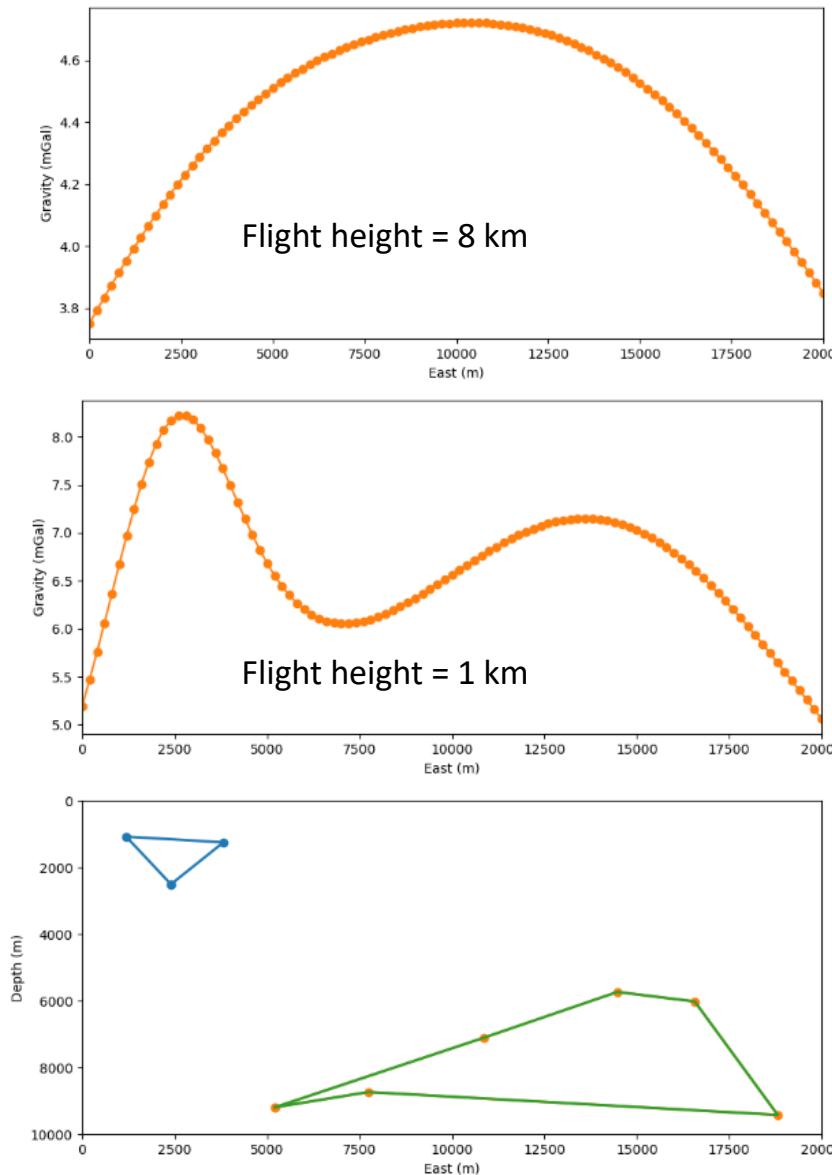
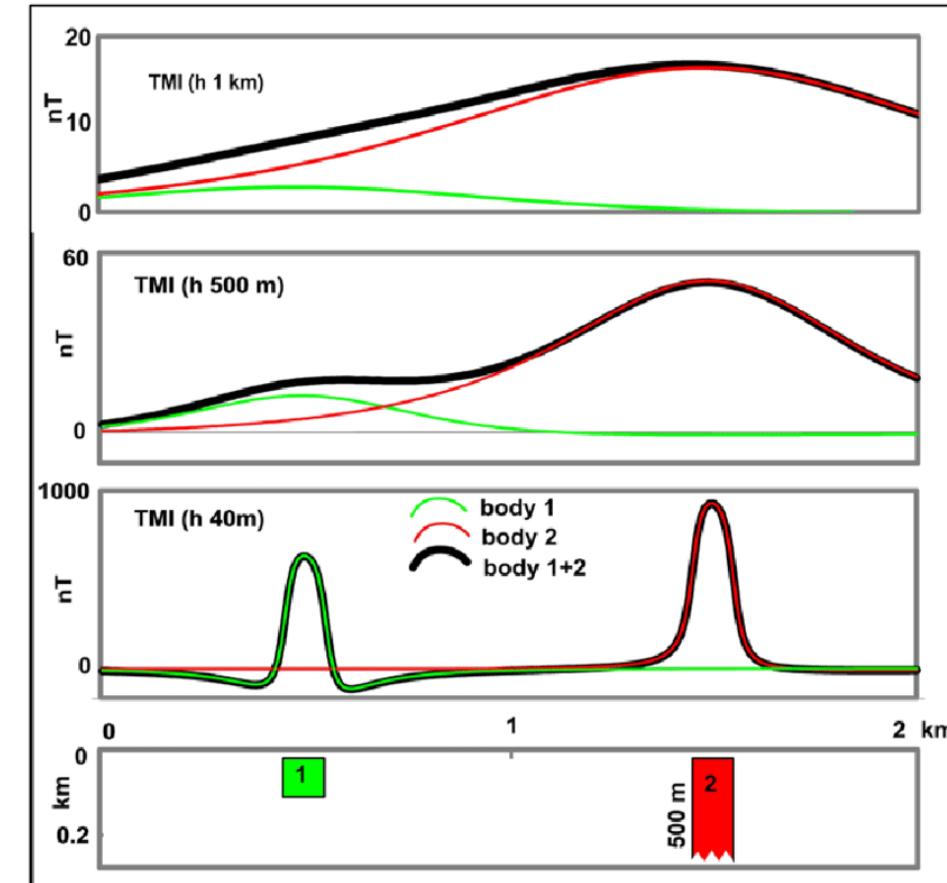


Image: Geology for Investors, David Tilley

Gravity anomalies



- Anomalies change with changing observation height



Isles & Rankin 2013

<https://www.aseg.org.au/sites/default/files/ebook-ASEG-eBook-Geo-Interpretation-of-Aeromagnetic-Data-Opt-for-user-1621.pdf>

Non-Uniqueness

- **Multi-Method Approach:** Integrating gravity data with other geophysical methods like magnetics, seismic, and electromagnetic surveys is important to get a comprehensive understanding of the subsurface.
- **Reducing Ambiguities:** Combining different types of geophysical data helps reduce ambiguities in interpreting subsurface structures.

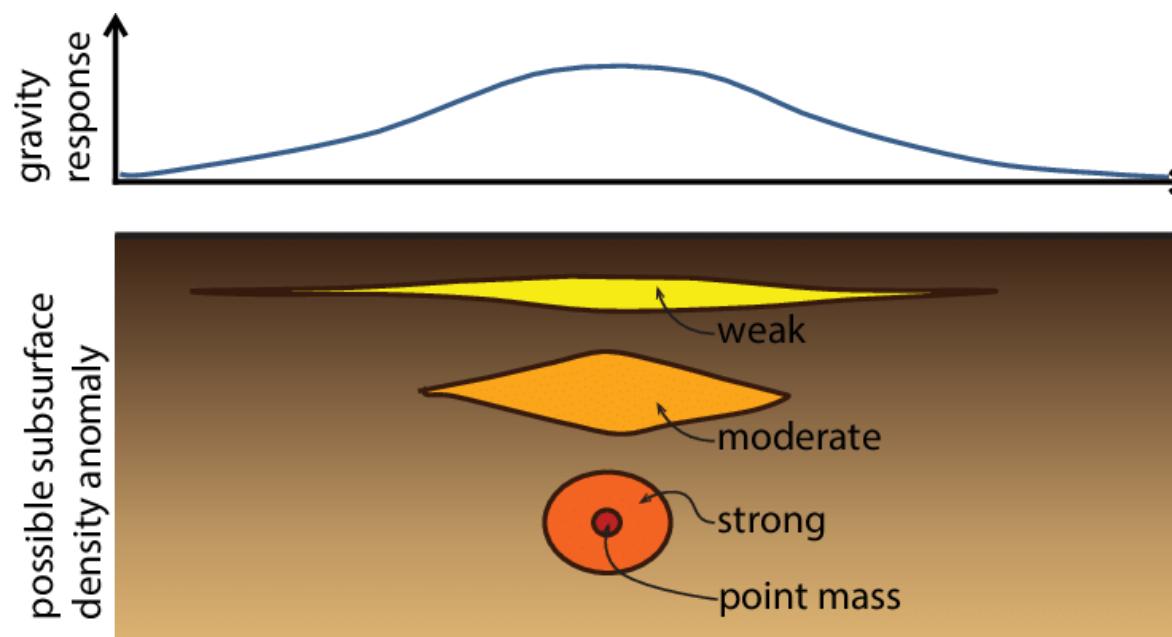


Image: UU Dept. of Earth Sciences



"Gravity" – movie poster, 2013

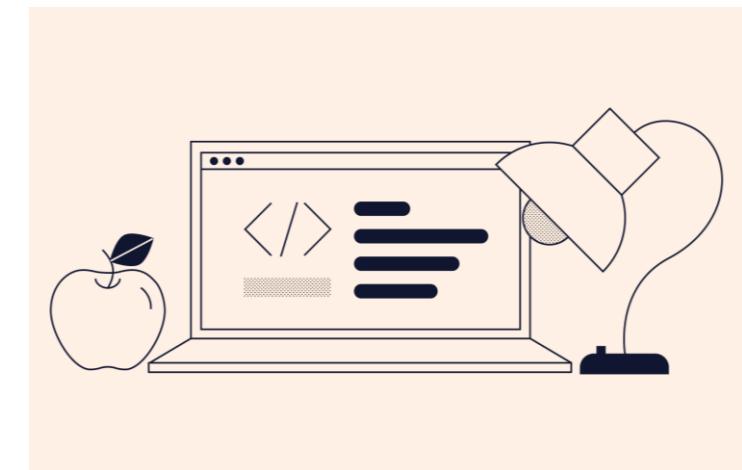
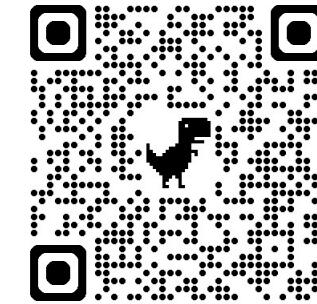
Check out the Online Jupyter Notebooks:

<https://github.com/LL-Geo/CAGE2024>

<https://mybinder.org/v2/gh/LL-Geo/CAGE2024/HEAD>

Tutorial series from raw data to inversion

1. Raw_gravity_with_drift_correction
2. Normal_Gravity_correction
3. Topography_Correction
4. Data_Processing
5. Gravity inversion



Example series

example_point_source: Interactive notebook to See how gravity change with point source

example_2d_simpeg: run inversion for a 2d profile

example_sea_ice: real world example to get free air gravity in Antarctica