

# Homework 4 Report

Heng Zhang  
0029109755  
zhan2614

## Introduction

In this homework we are using the MNIST dataset to evaluate the neural network we built for previous homework and the neural network class from torch. The dataset has 60000 pictures showing numbers from 0 to 9 and the task of both neural networks is to check if the neural network can correctly recognize those numbers.

## Setup

I use `my_img2num.py` and `nn_img2num.py` to denote the use of my own implementation of neural network and the neural network interface provided by torch. In both cases, the size of the neural network is  $784 * 512 * 256 * 64 * 10$ . The output has ten features indexed from 0 to 9 and final predicted number will be the index of the feature that has the largest value. Each neural network will have 30 epochs. In both implementations, I use the training batch size of 60 samples and testing batch size of 1000 samples.

## Evaluation

To compare both implementations of the neural network, Figure 1 shows the prediction accuracy of both networks. They roughly converge at similar speed and both networks achieve comparable accuracy in the end. Figure 2 shows the running time of each epoch for both implementations. `torch.nn` runs faster. My own implementation of the neural network runs roughly 10 seconds for each epoch while the `torch.nn` runs for about 6 seconds. Figure 3 shows the change of loss of my nn and `torch.nn`. At the initial phase, my nn has larger losses in testing and training but eventually both implementations achieve comparable losses.

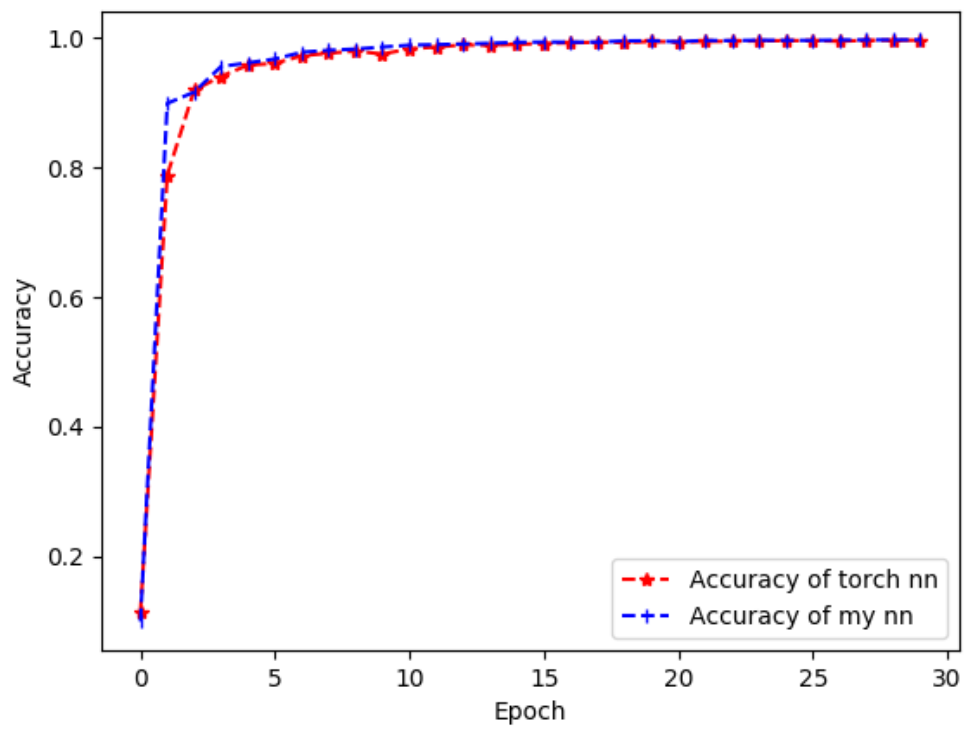


Figure 1 Accuracy in Both Implementations

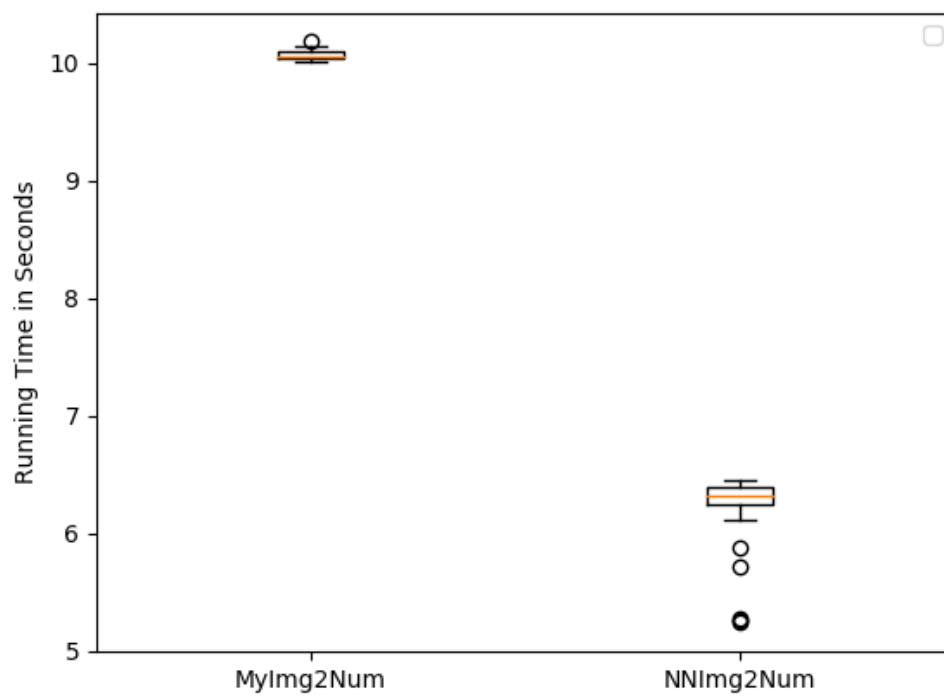


Figure 2 Running Time for Both Implementations

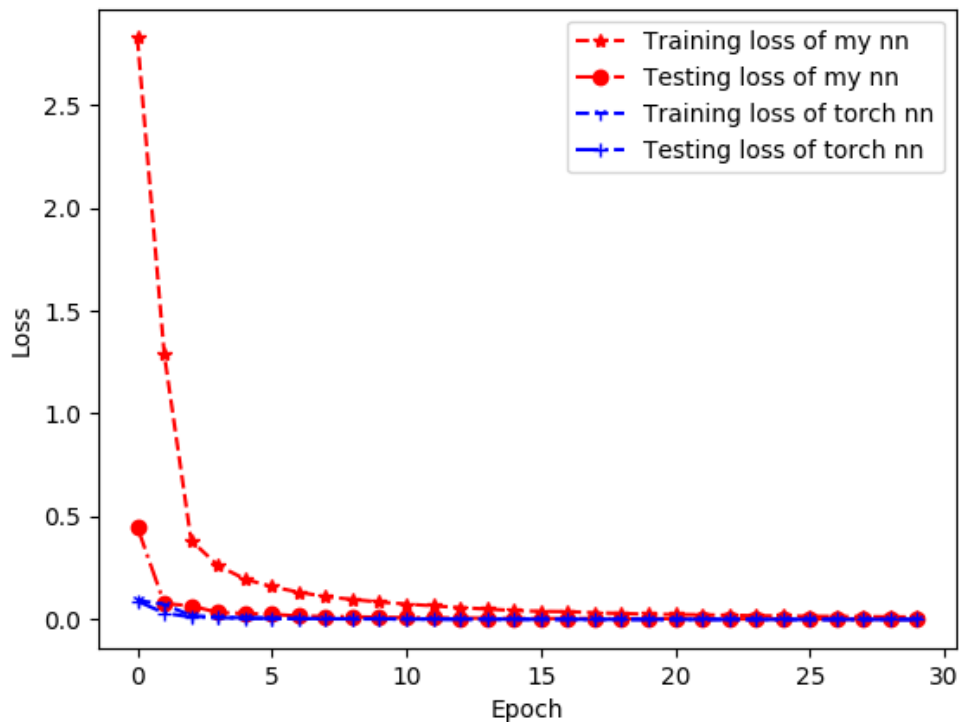


Figure 3 The change of Training and Testing Loss

## Appendix

my\_img2num.py

```

1. from pprint import pprint as pp
2. from neural_network import NeuralNetwork
3. import torch
4. from torchvision import datasets, transforms
5. from time import time
6. import matplotlib.pyplot as plt
7. plt.ioff()
8. class MyImg2Num:
9.     def __init__(self):
10.         self.train_batch_size = 60
11.         self.epoch = 30
12.         self.labels = 10
13.         self.rate = 0.1
14.         self.input_size = 28 * 28
15.         self.test_batch_size = 10 * self.train_batch_size
16.         self.test_loader = torch.utils.data.DataLoader(
17.             datasets.MNIST('./data',
18.                             train=True,
19.                             download=True,
```

```

20.         transform=transforms.Compose([transforms.ToTensor()))),
21.         batch_size=self.test_batch_size, shuffle=True)
22.
23.     self.train_loader = torch.utils.data.DataLoader(
24.         datasets.MNIST('./data',
25.             train=True,
26.             download=True,
27.             transform=transforms.Compose([transforms.ToTensor()))),
28.         batch_size=self.train_batch_size, shuffle=True)
29.
30.     # input image is 28 * 28 so convert to 1D matrix
31.     # output labels are 10 [0 - 9]
32.     self.nn = NeuralNetwork([self.input_size, 512, 256, 64, self.labels]
33. )
34.     def train(self, plot=False):
35.         print('training')
36.         def onehot_training(target, batch_size):
37.             output = torch.zeros(batch_size, self.labels)
38.             for i in range(batch_size):
39.                 output[i][int(target[i])] = 1.0
40.             return output
41.
42.         def training():
43.             loss = 0
44.             for batch_id, (data, target) in enumerate(self.train_loader):
45.                 # data.view change the dimension of input to use forward function
46.                 forward_pass_output = self.nn.forward(data.view(self.train_batch_size, self.input_size).type(torch.DoubleTensor))
47.                 onehot_target = onehot_training(target, self.train_batch_size).type(torch.DoubleTensor)
48.                 #print(onehot_target.type())
49.                 self.nn.backward(onehot_target)
50.                 loss += self.nn.total_loss
51.                 self.nn.updateParams(self.rate)
52.                 # loss / number of batches
53.                 avg_loss = loss / (len(self.train_loader.dataset) / self.train_batch_size)
54.                 return avg_loss
55.
56.         def testing():
57.             loss = 0
58.             correct = 0

```

```

59.         for batch_id, (data, target) in enumerate(self.test_loader):
60.             # data.view change the dimension of input to use forward function
61.             forward_pass_output = self.nn.forward(data.view(self.test_batch_size, self.input_size).type(torch.DoubleTensor))
62.             onehot_target = onehot_training(target, self.test_batch_size).type(torch.DoubleTensor)
63.             loss += (onehot_target - forward_pass_output).pow(2).sum() / 2
64.             #print(forward_pass_output.size())
65.             #print(onehot_target.size())
66.             for i in range(self.test_batch_size):
67.                 val, position = torch.max(forward_pass_output[i], 0)
68.                 # print('prediction = {}, actual = {}'.format(int(position), target[i]))
69.                 if position == target[i]:
70.                     correct += 1
71.             # loss / number of batches
72.             avg_loss = loss / len(self.test_loader.dataset)
73.             accuracy = correct / len(self.test_loader.dataset)
74.             return avg_loss, accuracy
75.         acc_list = []
76.         train_loss_list = []
77.         test_loss_list = []
78.         speed = []
79.
80.         for i in range(self.epoch):
81.             s = time()
82.             train_loss = training()
83.             e = time()
84.             test_loss, accuracy = testing()
85.             print('Epoch {}, training_loss = {}, testing_loss = {}, accuracy = {}, time = {}'.format(i, train_loss, test_loss, accuracy, e - s))
86.             acc_list.append(accuracy)
87.             train_loss_list.append(train_loss)
88.             test_loss_list.append(test_loss)
89.             speed.append(e-s)
90.         if plot:
91.             return speed, train_loss_list, test_loss_list, acc_list
92.
93.
94.         def forward(self, img):
95.
96.             output = self.nn.forward(img.view(1, self.input_size))

```

```

97.         _, result = torch.max(output, 1)
98.         return result
99.         ....
100.         plt.plot(range(self.epoch), acc_list, 'r|--', label='Accuracy')
101.         plt.plot(range(self.epoch), train_loss_list, 'b*--
            ', label='Training Loss')
102.         plt.plot(range(self.epoch), test_loss_list, 'yo--
            ', label='Test Loss')
103.         plt.xlabel('Epoch')
104.         plt.legend()
105.         plt.title('My Neural Network Evaluation')
106.         plt.savefig('my_compare.png')
107.         plt.clf()
108.         ...
109.

```

## neural\_network.py

```

1. import torch
2. from math import sqrt, exp
3.
4. class NeuralNetwork:
5.     def __init__(self, layers):
6.         # layers is a list of layer sizes
7.         if type(layers) != list:
8.             raise TypeError('Input is not a list')
9.
10.        self.layers = layers
11.        self.theta = {}
12.        self.dE_dTheta = {}
13.        self.a = {} # the result after applying the sigmoid functino
14.        self.z = {} # result after weight matrix multiplies the activation
15.        # self.L is the index of the output layer
16.        self.L = len(layers) - 1
17.
18.        # n layers neural network has n-1 weight matrices
19.        for i in range(len(self.layers) - 1):
20.            # the diemension includes one position for biasi
21.            size = (self.layers[i] + 1, self.layers[i+1])
22.            self.theta[i] = torch.normal(
23.                torch.zeros(size[0], size[1]),
24.                1/sqrt(self.layers[i])
25.            ).type(torch.DoubleTensor)
26.        self.total_loss = 1
27.

```

```

28.     def getTheta(self):
29.         return self.theta
30.
31.     def getLayer(self, layer):
32.
33.         if layer not in self.theta.keys():
34.             raise ValueError('Layer index not exists')
35.         # layer is an integer for the layer index
36.         # return the corresponding theta matrix from that layer to layer + 1
37.
38.         return self.theta[layer]
39.
40.     def forward(self, nn_input):
41.         # nn_input is mXn where m is the number of samples
42.         # n is the number of neurons in each sample
43.         #print('original input', nn_input)
44.         # the one iteration forward function
45.         def sigmoid(i):
46.             if str(i.type()) != 'torch.DoubleTensor':
47.                 raise TypeError('Input of sigmoid is not DoubleTensor')
48.             return 1 / (1 + torch.pow(exp(1), -i))
49.
50.         if str(nn_input.type()) != 'torch.DoubleTensor':
51.             raise TypeError('Input of forward is not DoubleTensor')
52.         si = [1, nn_input.size()[0]]
53.         #print('si', si)
54.
55.         bias = torch.ones(si, dtype=torch.double)
56.         #print('bias', bias)
57.         operation_input = nn_input.t()
58.         # operation_input has nxm dim
59.         self.a[0] = nn_input.t()
60.         #print('a[0]', self.a[0])
61.
62.         for i in self.theta.keys():
63.             # print('i=',i)
64.             # print('a[{}]={}'.format(i, self.a[i]))
65.             # print('bias=',bias)
66.             self.a[i] = torch.cat((self.a[i], bias), 0)
67.             # print('cat input', self.a[i])
68.             theta = torch.t(self.theta[i])
69.             # print('theta', theta)
70.             self.z[i + 1] = torch.mm(theta, self.a[i])

```

```

71.         # print('z', self.z[i+1])
72.         self.a[i + 1] = sigmoid(self.z[i + 1])
73.         # print('a', self.a[i+1])
74.         bias = torch.ones([1, self.a[i].t().size()[0]], dtype=torch.double)
75.         # print('end bias', bias)
76.         #print('return from forward', self.a[self.L].t())
77.         return self.a[self.L].t()
78.
79.
80.     def backward(self, target, loss='MSE'):
81.         target = target.t()
82.         #print('target size', target.size())
83.         if loss == 'MSE':
84.             # step 1 calculate the loss function
85.             self.total_loss = (self.a[self.L] - target).pow(2).sum() / 2 / len(target)
86.             # print('output activation:', self.a[self.L])
87.             # print('total loss', self.total_loss)
88.             delta = torch.mul((self.a[self.L] - target), torch.mul(self.a[self.L], (1 - self.a[self.L])))
89.             #print('delta', delta)
90.             #print(delta.size())
91.
92.             for i in range(self.L - 1, -1, -1):
93.                 if i != self.L - 1:
94.                     #indices = torch.LongTensor(list(range(self.a[i].size()[0] - 1)))
95.                     #print(indices)
96.                     #indices = torch.LongTensor([0,1])
97.                     #delta = torch.index_select(delta, 0, indices)
98.                     delta = delta.narrow(0, 0, delta.size(0) - 1)
99.                     # from the layer before the output
100.                    self.dE_dTheta[i] = torch.mm(self.a[i], delta.t())
101.                    delta = torch.mul(torch.mm(self.theta[i], delta), torch.mul(self.a[i], (1 - self.a[i])))
102.                    # print('dE_dTheta', self.dE_dTheta[i])
103.                    # print('theta', self.theta[i])
104.                    # print('delta', delta)
105.                    # print('diff_a', torch.mul(self.a[i], (1 - self.a[i])))
106.                elif loss == 'CE':
107.                    pass
108.
109.            else:

```



```

110.         print('unrecognized error functino')
111.
112.     def updateParams(self, rate):
113.         for i in range(len(self.theta)):
114.             # print('before update', self.theta[i])
115.             self.theta[i] = self.theta[i] - torch.mul(self.dE_dTheta[i], ra
te)
116.             # print('after update', self.theta[i])

```

## nn\_img2num.py

```

1. from pprint import pprint as pp
2. from neural_network import NeuralNetwork
3. import torch
4. import torch.nn as nn
5. from torchvision import datasets, transforms
6. from time import time
7. from torch.autograd import Variable
8. import matplotlib.pyplot as plt
9. plt.ioff()
10. class NNImp2Num:
11.
12.     def __init__(self):
13.         self.train_batch_size = 60
14.         self.epoch = 30
15.         self.labels = 10
16.         self.rate = 30
17.         self.input_size = 28 * 28
18.         self.test_batch_size = 10 * self.train_batch_size
19.         self.test_loader = torch.utils.data.DataLoader(
20.             datasets.MNIST('./data',
21.                             train=True,
22.                             download=True,
23.                             transform=transforms.Compose([transforms.ToTensor()])),
24.             batch_size=self.test_batch_size, shuffle=True)
25.
26.         self.train_loader = torch.utils.data.DataLoader(
27.             datasets.MNIST('./data',
28.                             train=True,
29.                             download=True,
30.                             transform=transforms.Compose([transforms.ToTensor()])),
31.             batch_size=self.train_batch_size, shuffle=True)
32.
33.         # input image is 28 * 28 so convert to 1D matrix

```

```

34.         # output labels are 10 [0 - 9]
35.         self.model = nn.Sequential(
36.             nn.Linear(self.input_size, 512), nn.Sigmoid(),
37.             nn.Linear(512, 256), nn.Sigmoid(),
38.             nn.Linear(256, 64), nn.Sigmoid(),
39.             nn.Linear(64, self.labels), nn.Sigmoid(),
40.         )
41.
42.         self.optimizer = torch.optim.SGD(self.model.parameters(), lr=self.ra
te)
43.         self.loss_function = nn.MSELoss()
44.
45.     def forward(self, img):
46.
47.         output = self.model.forward(img.view(1, self.input_size))
48.         _, result = torch.max(output, 1)
49.         return result
50.
51.     def train(self, plot=False):
52.         print('training')
53.         def onehot_training(target, batch_size):
54.             output = torch.zeros(batch_size, self.labels)
55.             for i in range(batch_size):
56.                 output[i][int(target[i])] = 1.0
57.             return output
58.
59.         def training():
60.             loss = 0
61.             self.model.train() # set to training mode
62.             for batch_id, (data, target) in enumerate(self.train_loader):
63.                 # data.view change the dimension of input to use forward fun
ction
64.                 self.optimizer.zero_grad()
65.                 forward_pass_output = self.model(data.view(self.train_batch_
size, self.input_size))
66.                 onehot_target = onehot_training(target, self.train_batch_siz
e)
67.                 #print(onehot_target.type())
68.                 cur_loss = self.loss_function(forward_pass_output, onehot_ta
rget)
69.                 loss += cur_loss.data
70.                 cur_loss.backward()
71.                 self.optimizer.step()
72.                 # loss / number of batches

```

```

73.         avg_loss = loss / (len(self.train_loader.dataset) / self.train_b
atch_size)
74.         return avg_loss
75.
76.     def testing():
77.         self.model.eval()
78.         loss = 0
79.         correct = 0
80.         for batch_id, (data, target) in enumerate(self.test_loader):
81.             # data.view change the dimension of input to use forward fun
ction
82.             forward_pass_output = self.model(data.view(self.test_batch_s
ize, self.input_size))
83.             onehot_target = onehot_training(target, self.test_batch_size
)
84.             cur_loss = self.loss_function(forward_pass_output, onehot_ta
rget)
85.             loss += cur_loss.data
86.             #print(forward_pass_output.size())
87.             #print(onehot_target.size())
88.             for i in range(self.test_batch_size):
89.                 val, position = torch.max(forward_pass_output.data[i], 0
)
90.                 # print('prediction = {}, actual = {}'.format(int(positio
n), target[i]))
91.                 if position == target[i]:
92.                     correct += 1
93.             # loss / number of batches
94.             avg_loss = loss / (len(self.test_loader.dataset) / self.test_bat
ch_size)
95.             accuracy = correct / len(self.test_loader.dataset)
96.             return avg_loss, accuracy
97.         acc_list = []
98.         train_loss_list = []
99.         test_loss_list = []
100.        speed = []
101.        for i in range(self.epoch):
102.            s = time()
103.            train_loss = training()
104.            e = time()
105.            test_loss, accuracy = testing()
106.            print('Epoch {}, training_loss = {}, testing_loss = {}, accurac
y = {}, time = {}'.format(i, train_loss, test_loss, accuracy, e - s))
107.            acc_list.append(accuracy)

```

```

108.         train_loss_list.append(train_loss)
109.         test_loss_list.append(test_loss)
110.         speed.append(e-s)
111.         if plot == True:
112.             return speed, train_loss_list, test_loss_list, acc_list
113.
114.     '''
115.     plt.plot(range(self.epoch), acc_list, 'r|--', label='Accuracy')
116.     plt.plot(range(self.epoch), train_loss_list, 'b*--',
117.              label='Training Loss')
117.     plt.plot(range(self.epoch), test_loss_list, 'yo--',
118.              label='Test Loss')
118.     plt.xlabel('Epoch')
119.     plt.legend()
120.     plt.title('Library Neural Network Evaluation')
121.     plt.savefig('nn_compare.png')
122.     plt.clf()
123.     '''
124.

```

## test.py

```

1.  from my_img2num import MyImg2Num
2.  import matplotlib.pyplot as plt
3.  from nn_img2num import NNImg2Num
4.  plt.ioff()
5.  print('running self nn')
6.  my_img_2num = MyImg2Num()
7.  my_time, my_train_loss, my_test_loss, my_accuracy = my_img_2num.train(True)
8.  print(my_time)
9.  print('running library nn')
10. nn_img = NNImg2Num()
11. nn_time, nn_train_loss, nn_test_loss, nn_accuracy = nn_img.train(True)
12. print(nn_time)
13. data = [my_time, nn_time]
14. plt.boxplot(data)
15. plt.xticks(range(1, 3), ['MyImg2Num', 'NNImg2Num'])
16. plt.ylabel('Running Time in Seconds')
17. plt.savefig('efficiency.png')
18. plt.clf()
19.
20. plt.plot(range(30), nn_accuracy, 'r*--', label='Accuracy of torch nn')
21. plt.plot(range(30), my_accuracy, 'b|--', label='Accuracy of my nn')
22. plt.xlabel('Epoch')

```

```
23. plt.ylabel('Accuracy')
24. plt.savefig('accuracy.png')
25. plt.clf()
26.
27. plt.plot(range(30), my_train_loss, 'r*--', label='Training loss of my nn')
28. plt.plot(range(30), nn_train_loss, 'b|--', label='Training loss of torch nn')
29.
30. plt.plot(range(30), my_test_loss, 'ro-.', label='Testing loss of my nn')
31. plt.plot(range(30), nn_test_loss, 'n+-.', label='Testing loss of torch nn')

32. plt.xlabel('Epoch')
33. plt.ylabel('Loss')
34. plt.savefig('loss.png')
35. plt.clf()
```