

1. Given amount function,  $A(t) = 4t^2 + 8t + 4$ . What is the interest earned in the second year

0.8  
 36

9  
 20

ignore, same like practice 1

$$A(2) = 4(2)^2 + 8(2) + 4 = 36.$$

$$A(1) = 4(1)^2 + 8(1) + 4 = 16.$$

$$\text{Interest} = A(2) - A(1) = 20.$$

2. An investor puts 100 into Fund X and 100 into Fund Y. Fund Y earns compound interest at the annual rate of  $j > 0$ , and Fund X earns simple interest at the annual rate of  $1.05j$ . At the end of 2 years, the amount in Fund Y is equal to the amount in Fund X. Calculate the amount in Fund Y at the end of 5 years.

153  
 161

AV using simple vs compound interest

At the end of 2 years.

$$\text{Fund X} = [1 + 1.05j \cdot 12] \cdot 100$$

$$\text{Fund Y} = (1 + j)^2 \cdot 100.$$

$$\text{So } 1 + 2.1j = (1 + j)^2 \Rightarrow j = 0.1$$

At the end of 5 years.

$$\text{Fund Y} = 100(1+j)^5 = 161.$$

3. Smith lends Jones \$900. After 6 months, Jones settle the debt for \$960. Calculate the annual effective rate of discount.

2/17  
 31/16<sup>2</sup>

ignore, same like practice 1

$$d_1 = \frac{960 - 900}{960} = \frac{1}{16}. \quad \text{It is the semi-annual effective discount rate.}$$

$$\text{Then, } 1 - d_2 = (1 - d_1)^2. \Rightarrow d_2 = 1 - (1 - d_1)^2 = \frac{31}{16^2}$$

$$\text{Method: } 900(1-d)^{-0.5} = 960. \quad d = \frac{31}{16^2}.$$

Definition: the ratio of the amount of interest (amount of discount) earned during the period to the amount invested at the end of the period.

$$d = \frac{AV_{t+1} - AV_t}{AV_{t+1}}.$$

4. PV of \$750 due 7 years from now, at a nominal annual rate of interest of 6% compounded monthly.

493.30  
 706.43

492.27  
 498.79

find PV using nominal interest rate

$$PV = 750 \left(1 + \frac{6\%}{12}\right)^{-12 \times 7} = 493.30 .$$

5. Emma deposits 1000 into a fund that credits interest at a nominal discount rate of 6% compounded once every 2 years. What is the value of the fund 7 years from now?

1500  
 2556.93

1564.27  
 2210

find AV using nominal discount rate

$$AV = 1000 \left(1 - \frac{d^{(\frac{1}{2})}}{2}\right)^{-3.5} = 1564.27 .$$

6. \$1,000 is deposited into a savings account at time  $t = 0$ . No other amounts are deposited. The accumulated amount in the account at any time,  $t$ , is given by

$$A(t) = \$1,000 \cdot (1 + 2t/35)^2$$

At time  $t_1$  the force of interest equals .04. What is  $t_1$  ?

32.5  
 35.5

29.5  
 41.5

find force of interest

$$\delta(t) = \frac{A'(t)}{A(t)} \Rightarrow \delta(t) = \frac{d}{dt} \ln A(t)$$

$$A(t) = 1000 \left(1 + \frac{2t}{35}\right)^2 \quad \ln A(t) = \ln [1000 \cdot \left(1 + \frac{2t}{35}\right)^2] = \ln 1000 + 2 \ln \left(1 + \frac{2t}{35}\right) .$$

$$\delta(t) = \frac{d}{dt} \ln A(t) = 2 \cdot \frac{\frac{2}{35}}{1 + \frac{2t}{35}} = 0.04 .$$

$$t = \frac{35}{2} \left[ \left( \frac{4}{35} / 0.04 \right) - 1 \right] = 32.5$$

7. At time 2, 100 is deposited into Fund X. Fund X accumulates at a force of interest

$$\delta_t = 0.5(1 + t)^{-2}$$

Find the accumulated value of Fund X at time 9.

112.37  
 9002

156.83  
 105.71

find AV using varuing delta

$$A(t_1, t_2) = C \cdot \exp \left( \int_{t_1}^{t_2} \delta_r dr \right) .$$

$$\begin{aligned}
 &= 100 \cdot \exp\left(\int_2^7 0.5(1+t)^{-2} dt\right) \quad \text{0.5} \int_2^7 (1+t)^{-2} dt = -0.5 \frac{1}{1+t} \Big|_2^7 \\
 &= 100 \cdot e^{0.1042} = 110.98 \quad = -0.5 \left(\frac{1}{8} - \frac{1}{3}\right) \\
 &= 0.1042 .
 \end{aligned}$$

8. John is 35 years old. What is the present value of a perpetuity paying 3000 at the end of each month forever. The first payment is a month after his 60th birthday and the effective interest rate is 5%.

736,354

217,448

monthly perpetuity

17,718

60,000

Method 1:



$$PV|_{t=0} = v^{300} \cdot \frac{1}{i} \cdot 300 = \text{where } i \text{ is the effective interest rate of month.}$$

$$(1+i)^{12} = 1.05 \quad i = 0.0041 .$$

$$PV|_{t=0} = (1.0041)^{-300} \cdot \frac{300}{0.0041} = 214411.1049 .$$

$$\begin{aligned}
 \text{Method 2: } PV|_{t=0} &= v^{25} \cdot 3000 \cdot a_{\overline{30}5\%}^{(12)} \cdot 12 = (1.05)^{-25} \cdot 3000 \cdot 12 \cdot \frac{1}{0.0492} = 216075.1988 \\
 (1 + \frac{i^{(m)}}{12})^{12} &= 1.05 \quad i^{(m)} = 0.0041 \times 12 = 0.0492 .
 \end{aligned}$$

9.

Annuities X and Y provide the payments as per table on the left.  
Annuities X and Y have equal present values at an effective annual interest rate  $i$  such that  $v^{10} = 1/2$ .

Determine K

5/3

9/5

4/3

7/4

$$X: PV|_{t=0} = a_{\overline{10}} + a_{\overline{20}} - a_{\overline{30}}$$

$$Y: PV|_{t=0} = k \cdot a_{\overline{30}} - k \cdot a_{\overline{20}} + k \cdot a_{\overline{10}}$$

$$PV|_{t=0}^X = PV|_{t=0}^Y \quad v^{10} = \frac{1}{2} \quad k = \frac{9}{5} .$$

10. A loan is to be repaid by annual payments continuing forever, the first one due one year after the loan is made.

Find the amount of the loan if the payments are 1, 2, 3, 1, 2, 3, ... assuming an annual effective interest rate of 10%.

at least 22

at least 19, but less than 20

interesting  
annuity

less than 19

at least 20, but less than 21



Method: Let  $X, Y, Z$  be the payment of 1, 2, 3 respectively.

$d_j$  is the effective discount rate of 3 years.

$$d_j = \frac{j}{1+j} . j \text{ is the effective interest rate of 3 years}$$

$$(1+j)^3 = 1+i . j = 0.331$$

$$X: PV|_{t=0} = 1 \cdot \ddot{a}_{\overline{3}|j} \cdot (1+i)^{-1} = \frac{1+j}{j} \cdot (1.1)^{-1} = (4.0211) \cdot (1.1)^{-1} = 3.6555 .$$

$$Y: PV|_{t=0} = 2 \cdot \ddot{a}_{\overline{3}|j} \cdot (1+i)^{-2} = 2 \cdot (4.0211) \cdot (1.1)^{-2} = 6.6464 .$$

$$Z: PV|_{t=0} = 3 \cdot \ddot{a}_{\overline{3}|j} \cdot (1+i)^{-3} = 9.0633 .$$

$$PV|_{t=0} = (PV|_{t=0})_{x+y+z} = 19.3652 .$$

Method 2: Using  $\ddot{a}_{\overline{3}|j}$ .  $j$  is 0.331 for the effective interest rate of 3 years.

$$X: PV|_{t=0} = 1 \cdot \ddot{a}_{\overline{3}|j} \cdot (1+i)^2 = 3.6555 .$$

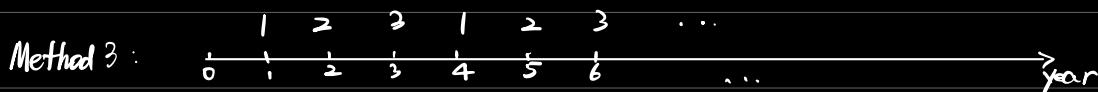
$$Y: PV|_{t=0} = 2 \cdot \ddot{a}_{\overline{3}|j} \cdot (1+i) = 6.6464 .$$

$$Z: PV|_{t=0} = 3 \cdot \ddot{a}_{\overline{3}|j} = 9.0634 .$$

$$PV|_{t=0} = (PV|_{t=0})_{x+y+z} = 19.3653 .$$

Notice that the difference from  $\ddot{a}_{\overline{3}|}$  and  $\ddot{a}_{\overline{3}|j}$  with  $j$ .

(since the evaluation time is different from  $\ddot{a}_{\overline{3}|}$  and  $\ddot{a}_{\overline{3}|j}$ ).



Let the first payment be 1, 2, 3 for a cycle.

$$X = 1 \cdot v + 2 \cdot v^2 + 3v^3 = 4.8159 .$$

That is, the annuity payments are

$$1+j = (1+i)^3 . j = 0.331 . d_j = \frac{j}{1+j} = \frac{0.331}{1.331}$$

$$PV|_{t=0} = X \cdot \ddot{a}_{\overline{3}|j} = \frac{4.8159}{d_j} = 19.3655 .$$

11. A man turns 40 today and wishes to purchase perpetuity at age 65 with a price of RM300,000 that will give him some retirement income.

Starting today, he makes monthly contributions of  $X$  to a fund for 25 years. The fund earns a nominal rate of 9% compounded monthly. Find  $X$ .

267.59

2,517.59

similar with tuto

2498.85

265.60

$$\begin{array}{cccc} x & x & x & \dots \\ \hline 1 & 2 & \dots \end{array}$$

(40)

$$\begin{array}{c} x \\ \hline 299 & 300 \end{array} \rightarrow \text{month}$$

1.65)

$\uparrow$  RM 300,000.

$x \cdot \bar{s}_{300|j} = 300000$ .  $j$  is effective interest rate of monthly.

$$j = \frac{9\%}{12} = 0.0075$$

$$x \cdot \frac{(1.0075)^{300} - 1}{0.0075} \cdot (1.0075) = 300000$$

$$x = 265.5971$$

12. The present value of a 5-year annuity immediate, with payments of \$1,000 each 6 times per year, is \$20,930. Determine the force of interest.

need to solve with calculator

- |                          |                                      |                          |                                       |
|--------------------------|--------------------------------------|--------------------------|---------------------------------------|
| <input type="checkbox"/> | t least 14.75%, but less than 14.85% | <input type="checkbox"/> | at least 14.65%, but less than 14.75% |
| <input type="checkbox"/> | at least 14.85%                      | <input type="checkbox"/> | Less than 14.65%                      |

$$PV|_{t=0} = 1000 \cdot a_{30|j} \quad j \text{ is the effective interest rate for 2 months.}$$

$$j = 2.5001\% \quad (1+j)^6 = 1+i \quad i = 15.97\%$$

$$\delta = \ln(1+i) = 14.82\%$$

13. If  $i = 3.25\%$ , what is the PV of the annual perpetuity immediate payments as follows: 1, 2, 3, ..., 10, 11, 11, 11, ...

- |                          |        |                          |        |                                       |
|--------------------------|--------|--------------------------|--------|---------------------------------------|
| <input type="checkbox"/> | 280.79 | <input type="checkbox"/> | 390.30 | increasing annuity then<br>perpetuity |
| <input type="checkbox"/> | 289.92 | <input type="checkbox"/> | 338.46 |                                       |

$$\text{Method 1: } PV|_{t=0} = (Ia)_{\overline{n}|i} + v^{10} \cdot 11 \cdot a_{\overline{\infty}|i}$$

$$= \frac{a_{\overline{n}|i} - 10v^{10}}{i} + v^{10} \cdot 11 \cdot \frac{1}{i}$$

$$\begin{aligned} \text{Method 2: } PV|_{t=0} &= 11 \cdot a_{\overline{\infty}|i} - a_{\overline{10}} - a_{\overline{9}} - \dots - a_{\overline{1}} \\ &= 11 \cdot a_{\overline{\infty}|i} - (a_{\overline{10}} + a_{\overline{9}} + \dots + a_{\overline{1}}) \\ &= 11 \cdot a_{\overline{\infty}|i} - (Dd)_{\overline{10}} \end{aligned}$$

14. Barbara purchases an increasing perpetuity with payments occurring at the end of every 2 years. The first payment is 3, the second one is 4, the third one is 5, etc. The price of the perpetuity is 110. Calculate the annual effective interest rate.

- |                          |       |                          |       |                         |
|--------------------------|-------|--------------------------|-------|-------------------------|
| <input type="checkbox"/> | 4.88% | <input type="checkbox"/> | 5.35% | non standard perpetuity |
| <input type="checkbox"/> | 10%   | <input type="checkbox"/> | 11%   |                         |

$$P = 3, Q = 1$$

$$PV|_{t=0} = 3 \cdot a_{\overline{2}|j} + 1 \cdot \frac{a_{\overline{2}|j}}{j} = \frac{3}{j} + \frac{1}{j^2} = 110 \quad ; \quad j \text{ is the effective interest rate of 2 years.}$$

$$(1+i) = (1+i)^{\frac{1}{v}} . \quad v = \underline{\hspace{2cm}}$$

$$\lim_{n \rightarrow \infty} (P\bar{a}_m + Q \frac{\bar{a}_{m-n} v^n}{v}) = P \cdot \frac{1}{v} + Q \frac{1}{v} = \frac{P}{v} + \frac{Q}{v^2} .$$

15. You are given  $\delta_t = \frac{1}{(1+t)}$  for  $0 \leq t \leq 5$ . Calculate "s angle 5"

8.7

13.7

ignore this, same like practice 2

7.5

10.5

$$a(t) = \exp\left(\int_0^t \frac{1}{1+r} dr\right) = \exp(\ln(1+r)|_0^t) = 1+t .$$



$$\begin{aligned} S_{\bar{5}|} &= a(5) \left[ \frac{1}{a(1)} + \frac{1}{a(2)} + \frac{1}{a(3)} + \frac{1}{a(4)} + \frac{1}{a(5)} \right] \\ &= 6 \left( \frac{1}{2} + \frac{1}{3} + \frac{1}{4} + \frac{1}{5} + \frac{1}{6} \right) = 8.7 . \end{aligned}$$

$$a_m = \frac{1}{a(1)} + \frac{1}{a(2)} + \dots + \frac{1}{a(m)} . \quad S_m = a(m) \cdot a_{\bar{m}}$$

(Continuous Force of Interest, but Discrete Payments).

16.  $\int_0^n \bar{a}_{\bar{t}} dt = 100$  You are given the equation on the left. Calculate "a angle n bar"

$n\delta$

$100n\delta$

tricky, need to recognize this is  
D-bar a-bar angle n  
Remember a relationship in  
chapter 3 slide 10.

$100 - n\delta$

$n - 100\delta$

This is decreasing continuous annuities.

Assuming  $f(t) = n-t$ . and  $\delta$  denotes the constant force of interest.

The PV is denoted by  $(\bar{D}\bar{a})_{\bar{n}}$ .

$$(\bar{D}\bar{a})_{\bar{n}} = \int_0^n (n-t) \cdot v^t dt = \frac{n - \bar{a}_{\bar{n}}}{\delta} = 100 . \quad \bar{a}_{\bar{n}} = n - 100\delta .$$

$$\text{Note: } (Ia)_{\bar{n}} = \sum_{t=0}^{n-1} v^t \cdot a_{\bar{n}-t}$$

$$(Da)_{\bar{n}} = \sum_{t=1}^n a_{\bar{n}} .$$

$$(12) . \quad PV = \int_0^n f(t) \exp(-\int_0^t \delta_r dr) dt = \int_0^n f(t) \cdot v^t dt$$

$$(\bar{I}\bar{a})_{\bar{n}} = \int_0^n t \cdot v^t dt$$

$$(\bar{D}\bar{a})_{\bar{n}} = \int_0^n (n-t) \cdot v^t dt = n \cdot \bar{a}_{\bar{n}} - (\bar{I}\bar{a})_{\bar{n}} = \int_0^n \bar{a}_{\bar{t}} dt .$$

17. For a given interest rate  $i > 0$ , the present value of a 20-year continuous annuity of one dollar per year is equal to 1.5 times the present value of a 10-year continuous annuity of one dollar per year.

Calculate the accumulated value of a 7-year continuous annuity of one dollar per year.

5.36

5.55

8.70

9.01

relationship between  $n$  and  $2n$  annuity

$$PV|_{t=0} = \bar{a}_{\overline{n}i} = 1.5 \bar{a}_{\overline{n}i}$$

$$\frac{\bar{a}_{\overline{n}i}}{\bar{a}_{\overline{n}i}} = 1 + v^{10} = 1.5 . \quad s = 0.0693 . \quad i = e^s - 1 = 0.0718 .$$

$$AV|_{t=0} = \bar{s}_{\overline{7}i} = \frac{(1+i)^7 - 1}{s} = 9.0157 .$$

18. Joan has won a lottery that pays 1,000 per month in the first year, 1,100 per month in the second year, 1,200 per month in the third year, etc. Payments are made at the end of each month for 10 years. Using an effective interest rate of 3% per annum, calculate the present value of this prize.

123,000

114,000

non standard

107,000

148,000

Method:

$$P = 1000 . \quad Q = 100 . \quad n = 120 . \quad 1 + j = (1 + i)^{12} . \quad i = (1.03)^{\frac{1}{12}} - 1 = 0.00247 .$$

$$PV|_{t=0} = 1000 \cdot \bar{a}_{\overline{120}i} + 100 \cdot \frac{\bar{a}_{\overline{120}i} - 120v_i^{120}}{i}$$

Method 2: The first year:  $X = 1000 \cdot \bar{s}_{\overline{12}i}$

The Second year:  $Y = 1100 \bar{s}_{\overline{12}i}$

$$So \quad P = 1000 \cdot \bar{s}_{\overline{12}i} . \quad Q = 100 \bar{s}_{\overline{12}i} .$$

$$PV|_{t=0} = 1000 \cdot \bar{s}_{\overline{12}i} \cdot \bar{a}_{\overline{10}j} + \frac{\bar{a}_{\overline{10}j} - 10v_i^{10}}{j} \cdot 100 \cdot \bar{s}_{\overline{12}i} .$$

19.

$$(I^{(2)} a)^{(2)}_{\overline{3}}$$

The present value of a series of payments is represented by the expression.

Find the sum of the series of payments (ignore discounting)

2.625

7.875

10.50

recognizing double m notation

For this expression.  $m=2$ . the first payment is  $\frac{1}{m^2} = \frac{1}{4}$ .

and with each subsequent payment increasing by  $\frac{1}{4}$ .

$$\frac{1}{4} + \frac{1}{4} \times 2 + \frac{1}{4} \times 3 + \dots + \frac{1}{4} \times 6 = \frac{1}{4} (1+2+\dots+6) = 5.25 .$$

20. You are given an annuity-immediate paying 10 for 10 years, then decreasing by one per year for nine years and paying one per year thereafter, forever. The annual effective rate of interest is 4%. Calculate the present value of this annuity.

123

121

119

125

decreasing then level



$$\text{Method 1: } PV|_{t=0} = \frac{1}{i} + a_{\overline{8}|} + a_{\overline{9}|} + \dots + a_{\overline{19}|} + a_{\overline{\infty}|}$$

$$= \frac{1}{i} + \sum_{t=1}^{18} a_{\overline{t}|} - \sum_{t=1}^9 a_{\overline{t}|}.$$

$$= \frac{1}{i} + (Da)_{\overline{8}|} - (Da)_{\overline{9}|}$$

$$= \frac{1}{i} + \frac{18 - a_{\overline{8}|}}{i} - \frac{9 - a_{\overline{9}|}}{i}$$

$$\frac{a_{\overline{8}|}}{a_{\overline{9}|}} = 1 + v^9$$

$$i = 0.04, \quad a_{\overline{8}|} = 12.6593, \quad a_{\overline{9}|} = \frac{a_{\overline{8}|}}{1+v^9} = 7.4353.$$

$$PV|_{t=0} = 119.4.$$

$$\text{Method 2: } PV|_{t=0} = 10 \cdot a_{\overline{9}|} + (Da)_{\overline{10}|} \cdot v^9 + \frac{1}{i} \cdot v^{19}.$$

21. fission method on perpetuity: Perpetuity Y has annual payments of  $q, q, 2q, 2q, 3q, 3q, \dots$  at the end of each year. The present value of perpetuity Y is equal to 110, at an annual effective interest rate of 10%. Calculate  $q$ .

1.9

0.488

0.59

1.7



the first 2 payments of  $q$  in perpetuity Y is equivalent to the payment of  $p$  at time 2 in perpetuity X.

$$P_1 = S_{2|i} \cdot q, \quad \text{where } S_{2|i} = \frac{(1+i)^2 - 1}{0.1} = 2.1$$

the second 2 payments of  $q \dots$

$$P_2 = S_{2|i} \cdot 2q.$$

So the perpetuity X has payments of  $q \cdot S_{2|i}, 2q \cdot S_{2|i}, \dots$  at the end of 2 years.

Using P-Q formula,

$$PV|_{t=0} = q \cdot S_{2|i} \cdot a_{\overline{\infty}|j} + q \cdot S_{2|i} \cdot \frac{a_{\infty|j}}{j}, \quad j \text{ is the effective interest rate of 2 years.}$$

$$= q \cdot S_{2|i} \cdot \frac{1}{j} + q \cdot S_{2|i} \cdot \frac{1}{j^2}$$

$$(1+j) = (1+i)^2$$

$$j = 0.21.$$

$$= q \cdot (2.1) \cdot \left( \frac{1}{0.21} + \frac{1}{(0.21)^2} \right) = 110.$$

$$f = 1.9091.$$

22. geometric annuity: An annuity provides for 12 annual payments. The first payment is \$100, paid at the end of the first year, and each subsequent payment is 5.0% more than the one preceding it. Calculate the present value of this annuity if  $i = 0.07$ .

- At least \$1000, but less than \$1,100       At least \$11,000  
 At least \$990, but less than \$1,000       Less than \$990



$$PV|_{t=0} = 100 \cdot \frac{1}{1.05} + 100(1.05) \cdot \frac{1}{1.05^2} + \dots + 100(1.05)^{11} \cdot \frac{1}{1.05^{12}}.$$

23. Mary is to receive an annuity with 30 annual payments. The first payment of \$1,000 is due immediately and each successive payment is 5% less than the payment for the preceding year. Interest is 12% compounded annually. Determine the present value of the annuity.

- At least \$6,600       At least \$6,400 but less than \$6,500  
 Less than \$6,400       At least \$6,500 but less than \$6,600



$$PV|_{t=0} = P_1 + \frac{P_2}{1+i} + \dots + \frac{P_{30}}{(1+i)^{29}}.$$

$P_1$  — the first payment.  $P_2 = P_1(1-d)$ . ...  $P_{30} = P_1(1-d)^{29}$ .

$$\begin{aligned} PV|_{t=0} &= P_1 \sum_{k=0}^{29} \frac{(1-d)^k}{(1+i)^k} & d = 0.05, i = 0.12 \\ &= P_1 \sum_{k=0}^{29} \left(\frac{1-d}{1+i}\right)^k = P_1 \cdot \frac{1 - \left(\frac{1-d}{1+i}\right)^{29}}{1 - \left(\frac{1-d}{1+i}\right)} = 6541.04. \end{aligned}$$

24. A continuously increasing annuity with a term of  $n$  years has payments payable at an annual rate  $t$  at time  $t$ .

The force of interest is equal to  $1/n$ . Calculate the present value of this annuity.

- $n^2 \left(1 - 2e^{-\frac{1}{n}}\right)$         $n^2 \left(1 - e^{-1}\right)$   
  $n^2 \left(1 - e^{-\frac{1}{n}}\right)$         $n^2 \left(1 - 2e^{-1}\right)$

$$PV|_{t=0} = \int_0^n t e^{-st} dt = \int_0^n t e^{-\frac{t}{n}} dt$$

$$\text{Let } u = t. \quad e^{-\frac{t}{n}} dt = du. \quad u = -n e^{-\frac{t}{n}}.$$

$$PV|_{t=0} = -n t e^{-\frac{t}{n}} \Big|_0^n + \int_0^n n e^{-\frac{t}{n}} dt = n^2 (1 - 2e^{-1})$$

25. Bill purchases an annuity at a price of 10,000. The annuity makes payments of 500 at the end of every 6 months for 20 years. The payments are reinvested in a fund, which earns interest at an annual effective rate  $j$ . Bill realizes an overall effective annual yield of 7% on his original investment over the 20-year period. Calculate  $j$

6.1%

6.7%

this is chapter 5,

6.5%

6.3%

Yield 2  
calculation



Interest:  $500i \ 1000i \ \dots \ 19500i$

$i$  is the effective interest rate of semi-annual.

$$\begin{aligned} 10000(1.07)^{20} &= 500 \cdot (40) + 500i \cdot (S_{40|i})_{\overline{40}|i} \\ &= 20000 + 500i \cdot \frac{S_{40|1} - 40}{i} \end{aligned}$$

$$\Rightarrow 10000(1.07)^{20} = 500 \cdot S_{40|i}. \quad i = 3.1148\%.$$

$$(1+i)^2 = 1+j. \quad j = 0.0632\%.$$

Understanding here  $10000(1.07)^{20} = 500 S_{40|i}$ .

26. Susan invests 100 at the end of each year for seven years at an annual effective interest rate of 5%. The interest credited is reinvested at an annual effective rate of 6%. The accumulated value at the end of seven years is X. Calculate X.

878

898

you can do this one. concept of growing money in 2 funds.

828

858



Interests  $100i \ 200i \ 300i \ 400i \ 500i \ 600i \ 700i$

$$X = AV|_{t=7} = 700 + 100i \cdot (I_s)_{\overline{7}|j} = 700 + 100 \cdot 5\% \cdot \frac{S_{7|1} - 7}{6\%} = 858.122\%.$$

27.

Table show info for an investment account. Calculate the absolute difference in the yield rates by dollar-weighted and time-weighted methods

12.3%

6.4%

2.3%

9.8%

last part of chapter 5, belum belajar

$$DWRR. \quad 50000(1+i) + 15000(1+\frac{2}{3}i) - 25000(1+\frac{1}{3}i) = 67000. \quad i = 52.2581\%.$$

$$TWRR. \quad 1+i = \frac{75000}{50000} \cdot \frac{90000}{175000+15000} \cdot \frac{67000}{(90000-25000)} \Rightarrow i = 54.6154\%$$