

*Introduction to Bayesian statistics*¹

Part 1 — Concepts

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🔗 <https://github.com/jorgetendeiro/GSMS-2020>

¹The template from these slides is inspired in that from [Mark Andrews](#)

Bayes rule

- ▶ \mathcal{D} = data
- ▶ θ = unknown parameter

$$p(\theta|\mathcal{D}) = \frac{p(\theta)p(\mathcal{D}|\theta)}{p(\mathcal{D})}$$

In words,

$$\text{posterior} = \frac{\text{prior} \times \text{likelihood}}{\text{evidence}}$$

The *evidence* does not depend on θ ; let's hide it:

$$\text{posterior} \propto \text{prior} \times \text{likelihood}$$

The symbol \propto means “proportional to”.

Bayes rule

$$\text{posterior} \propto \text{prior} \times \text{likelihood}$$

- ▶ *Prior*: Belief about the 'true' value of θ , *before looking at the data*.
- ▶ *Likelihood*: The statistical model, linking θ to data.
- ▶ *Posterior*: Updated knowledge about θ , in light of the observed data.

Bayes rule – Example

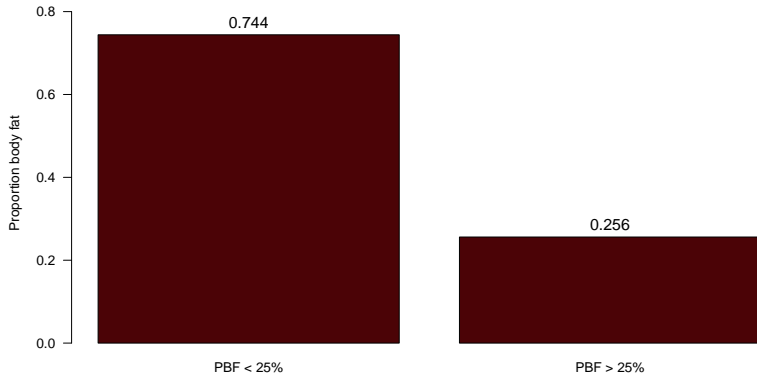
Data here:

<https://dasl.datadescription.com/datafile/bodyfat/>.

- ▶ Various measurements of 250 men.
- ▶ Keep it simple: Let's dichotomize the percentage of body fat (0 = PBF lower than 25%; 1 = PBF larger than 25%).
- ▶ *Goal*: Infer the proportion of obese men in the population.

```
url.data <- "https://dasl.datadescription.com/download/  
data/3079"  
PBF.data <- read.csv(url(url.data), header = TRUE, sep = "\t")  
PBF      <- ifelse(PBF.data$Pct.BF > 25, 1, 0)  
prop.table(table(PBF))
```

Bayes rule – Example



The rest

Therefore, the posterior distribution is basically a (rational, logically correct) means of merging together both our prior knowledge about some phenomenon with the information about the phenomenon that our data has to offer.

A small example

Let's make things concrete. I downloaded data from <https://dasl.datadescription.com/datafile/bodyfat/>, containing various measurements of 250 men. I focus on variable 'Pct.BF' (percentage of body fat) and dichotomize it (0 = PBF lower than 25%; 1 = PBF larger than 25%). I want to infer the proportion of obese men in the population.

```
PBF.data <- read.csv(url("https://dasl.datadescription.com/download/  
                        header = TRUE, sep = "\t"))
```

```
PBF      <- ifelse(PBF.data$Pct.BF > 25, 1, 0)  
head(PBF)
```

```
## [1] 0 0 1 0 1 0
```

```
length(PBF)
```

```
## [1] 250
```

References

Forder, L., & Lupyan, G. (2019). Hearing words changes color perception: Facilitation of color discrimination by verbal and visual cues. *Journal of Experimental Psychology: General*, 148(7), 1105. doi: [10.1037/xge0000560](https://doi.org/10.1037/xge0000560)