Prove that  $(A - B) \subseteq B \iff (A - B) = \emptyset$ .

First we consider the forward direction:

By definition 2.1.4,  $(A-B)=\{x\in A\mid x\not\in B\}$ , which means (A-B) consists of elements in A but not in B.

Since  $(A-B) \subseteq B$ , every element  $x \in (A-B)$  must also belong to B. This leads to a contradiction.

Thus, there can't be any element in (A-B), which implies that  $(A-B)=\emptyset$ . Then we consider the reverse direction:

Since  $(A - B) = \emptyset$ , there can't be any element in (A - B). By definition, an empty set is a subset of any set.

Therefore,  $(A - B) \subseteq B$ .

We conclude that:

$$(A-B) \subseteq B \iff (A-B) = \emptyset$$