

1. (5 points) Consider the following recursive function:

```
def mystery(x, y):  
    if y > x:  
        return y - 1  
    print(x, y)  
    return 3 + mystery(x // 2, y + 1)
```

a. What output will be produced by the call `mystery(16, 0)`?

16 0  
8 1  
4 2

b. What is the result (return value) produced by the call `mystery(16, 0)`?

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2. (5 points) Write a recursive function `sum_odds(lst)` that takes a list of integers `lst` and returns the sum of the odd integers in `lst`.

For example, `sum_odds([1, 4, 8, 5])` should return 6, because 1 and 5 are the only odd values in `[1, 4, 8, 5]`, and their sum is 6.

*Hint:* You will need the `%` operator.

```
def sum_odds(lst):  
    """ takes a list of integers lst  
    and returns the sum of the odd int  
    in lst  
    """  
    if lst == []:  
        return 0  
    else:  
        rest = sum_odds(lst[1:])  
        if lst[0] % 2 == 1:  
            return rest + lst[0]  
        else:  
            return rest
```

3. (5 points) Write a recursive function named `double_vowels(s)` that takes a string `s` and returns a string in which all of the vowels (a, e, i, o, u) in `s` are "doubled" (i.e., replaced by two occurrences of themselves), and all non-vowels are left alone. For example:

`double_vowels('about')` should return the string `'aaboouut'`

`double_vowels('time')` should return the string `'tiimee'`

You may assume that the input contains only lowercase letters and no spaces.

`def double_vowels(s):`  
 """ takes a string s and double  
 the vowels in string and return  
 """

if `s == ''`:  
 return ''

else:

rest = `double_vowels(s[1:])`

if `s[0] in ['a', 'e', 'i', 'o', 'u']`:  
 return `s[0]*2 + rest`

else:

return `s[0] + rest`

4. (5 points) Binary numbers:

- a. Convert this 8-bit binary number to decimal, showing your work: 10101100

$$10101100 = 2^2 + 2^3 + 2^5 + 2^7$$

$$= 4 + 8 + 32 + 128$$

$$= 172$$

- b. Add these 4-bit binary numbers, without converting to decimal: 1010 + 0111  
Show all of your work

$$\begin{array}{r} 11 \\ 1010 \\ + 0111 \\ \hline 10001 \end{array}$$