

章 全 2 章 2 5 中 国 自动化大会

论文编号: 120698

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# LLM-DiSC: LLM-enabled Distributed and Safe Coordination of **Multi-Robot Systems using Control Barrier Functions**

Qingqing Yang<sup>1</sup>, Guoxiang Zhao<sup>1,\*</sup>, Xiaoqiang Ren<sup>1</sup>, Xiaofan Wang<sup>2</sup>

<sup>1</sup>Shanghai University

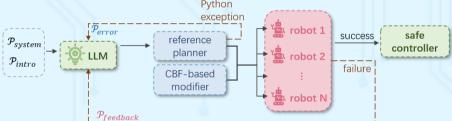
<sup>2</sup>Shanghai Institute of Technology

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## **Abstract**

Multi-robot systems (MRS) are widely used but often face motion conflicts during coordination. While large language models (LLM) show promise in complex planning tasks, their application to MRS remains limited by hallucinations and insufficient domain knowledge. To address this, we propose LLM-DiSC, a distributed and safe coordination framework that integrates LLM-generated planners with control barrier functions (CBF). It employs centralized training with feedback from simulation and CBF-based risk evaluation to refine planning, and distributed execution for scalability. Experiments demonstrate LLM-DiSC's safety, scalability, and near-optimal performance.

#### Method Python



#### Reference planner:

LLM generates the reference planner in Python, with automatic semantic correction through error feedback to the LLM.

### **CBF-based modifier:**

Unsafe reference signals are corrected by the CBF-based modifier to ensure safety.

Define the safe state set S using a continuously differentiable function h(x),  $S = \{x \in \mathbb{R}^n : h(x) \ge 0\}$ . Given the system's dynamics and the safe state set, h is a CBF if there exists a class  ${\mathcal K}$  function  ${\alpha}$ , such that  $\forall x_i \in S$ :

$$\sup_{\mathbf{u}_i \in U} \left[ L_f h_i(\mathbf{x}_i) + L_g h_i(\mathbf{x}_i) \mathbf{u}_i + \alpha \left( h_i(\mathbf{x}_i) \right) \right] \ge 0.$$

Solve a Quadratic Program to find safe control input u close to LLM's reference output:

$$\min_{\boldsymbol{u}_{i}^{t}} \frac{1}{2} \|\boldsymbol{u}_{i}^{t} - \boldsymbol{u}_{ref}^{t}\|^{2}$$

s.t. 
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$$L_f h_{i,k}^o(\boldsymbol{x}_i^t) + L_g h_{i,k}^o(\boldsymbol{x}_i^t) \boldsymbol{u}_i^t + \alpha \left( h_{i,k}^o(\boldsymbol{x}_i^t) \right) \ge 0, \forall k \in \mathcal{O}$$

#### Planner optimization:

Planner optimization iteratively refines the LLM-generated planner using simulation feedback when robots fail to reach their targets.

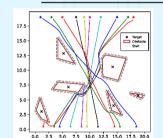
## **Experiments**

Experiments were conducted in environments with polygonal obstacles and multiple robots, where the reference planner was generated using OpenAI o1-preview. Performance of the LLM-DiSC was compared against a conventional distributed planner combining A\*, Pure Pursuit, and a CBF coordinator.

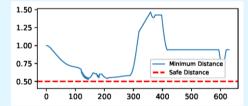
#### Safety and Scalability

TABLE I: Different robot models and group sizes

Model	Size	Pass@k			Iterations
Wodei	3126	k=1	k=5	k=10	iterations
Cinale Integrator	5	100%	100%	100%	1
Single Integrator	10	75%	100%	100%	1.37
Unicod	5	70%	100%	100%	1.67
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## Conclusions

By integrating LLM reasoning with CBF safety guarantees, our approach enables collision-free navigation and efficient task execution without relying on extensive training data or expert-designed models. The experimental results validate the superior performance of LLM-DiSC across different dynamic models and group sizes. This accessible solution significantly lowers technical barriers and computational demands for multi-robot motion planning.





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https://github.com/Yangniq/LLM-DiSC

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Multi-robot systems (MRS) are widely used but often face motion conflicts during coordination. While large language models (LLM) show promise in complex planning tasks, their application to MRS remains limited by hallucinations and insufficient domain knowledge. To address this, we propose LLM-DiSC, a distributed and safe coordination framework that integrates LLM-generated planners with control barrier functions (CBF). It employs centralized training with feedback from simulation and CBF-based risk evaluation to refine planning, and distributed execution for scalability. Experiments demonstrate LLM-DiSC's safety, scalability, and near-optimal performance.

#### Method Python exception robot 1 reference controller LLM failure CBF-based modifier robot N

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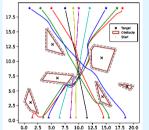
## **Experiments**

Experiments were conducted in environments with polygonal obstacles and multiple robots, where the reference planner was generated using OpenAI o1-preview. Performance of the LLM-DiSC was compared against a conventional distributed planner combining A\*, Pure Pursuit, and a CBF coordinator.

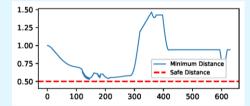
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The experimental environment consists of static polygonal obstacles and multiple robots. We use OpenAl o1-preview as the LLM to generate the reference planner. Performance of the proposed LLM-DiSC framework was compared against a conventional distributed motion planner consisting of an A\* target navigator combined with a Pure Pursuit tracker and the same parameterized CBF-based coordinator adopted by LLM-DiSC.

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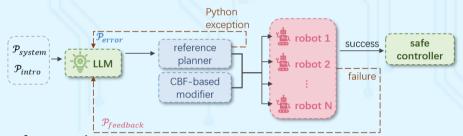
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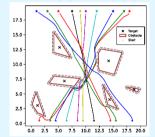
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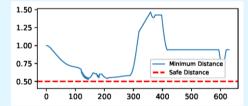
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