CS 188 Introduction to Spring 2019 Artificial Intelligence

Written HW 7

Due: Monday 4/1/2019 at 11:59pm (submit via Gradescope).

Leave self assessment boxes blank for this due date.

Self assessment due: Monday 4/8/2019 at 11:59pm (submit via Gradescope)

For the self assessment, fill in the self assessment boxes in your original submission (you can download a PDF copy of your submission from Gradescope – be sure to delete any extra title pages that Gradescope attaches). For each subpart where your original answer was correct, write "correct." Otherwise, write and explain the correct answer. Do not leave any boxes empty.

If you did not submit the homework (or skipped some questions) but wish to receive credit for the self-assessment, we ask that you first complete the homework without looking at the solutions, and then perform the self assessment afterwards.

Policy: Can be solved in groups (acknowledge collaborators) but must be written up individually

Submission: Your submission should be a PDF that matches this template. Each page of the PDF should align with the corresponding page of the template (page 1 has name/collaborators, question 1 begins on page 2, etc.). **Do not reorder, split, combine, or add extra pages.** The intention is that you print out the template, write on the page in pen/pencil, and then scan or take pictures of the pages to make your submission. You may also fill out this template digitally (e.g. using a tablet.)

First name	
Last name	
SID	
Collaborators	

Q1. Probability

- (a) For the following questions, you will be given a set of probability tables and a set of conditional independence assumptions. Given these tables and independence assumptions, write an expression for the requested probability tables. Keep in mind that your expressions cannot contain any probabilities other than the given probability tables. If it is not possible, mark "Not possible."
 - (i) Using probability tables P(A), $P(A \mid C)$, $P(B \mid C)$, $P(C \mid A, B)$ and no conditional independence assumptions, write an expression to calculate the table $P(A, B \mid C)$.

tions, write an expression to calculate the table I (A, B)	C).
$\mathbf{P}(\mathbf{A}, \mathbf{B} \mid \mathbf{C}) =$	Not possible.
(ii) Using probability tables $P(A)$, $P(A \mid C)$, $P(B \mid A)$, $P(C \mid tions)$, write an expression to calculate the table $P(B \mid A)$,	
$\mathbf{P}(\mathbf{B} \mid \mathbf{A}, \mathbf{C}) =$	Not possible.
(iii) Using probability tables $P(A \mid B), P(B), P(B \mid A, C), P$ tion $A \perp\!\!\!\perp B$, write an expression to calculate the table P	
$\mathbf{P}(\mathbf{C}) =$	Not possible.
(iv) Using probability tables $P(A \mid B, C), P(B), P(B \mid A, C)$, sumption $A \perp \!\!\!\perp B \mid C$, write an expression for $P(A, B, C)$	
P(A, B, C) =	
Self assessment If correct, write "correct" in the box. Otherwise	, write and explain the correct answer.

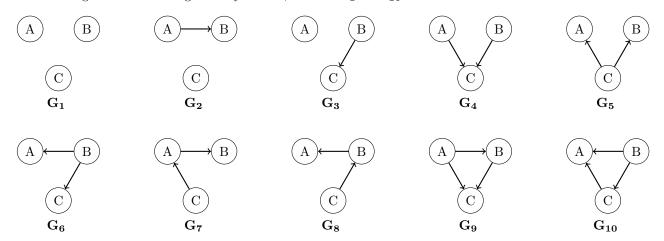
- (b) For each of the following equations, select the *minimal set* of conditional independence assumptions necessary for the equation to be true.
 - (i) $P(A, C) = P(A \mid B) P(C)$ $\square A \perp \!\!\!\perp B$ $\square A \perp \!\!\!\perp B \mid C$ $\square A \perp \!\!\!\perp C$ $\square A \perp \!\!\!\perp C \mid B$

 $\begin{array}{ccc} \square & A \perp \!\!\! \perp C \\ \square & A \perp \!\!\! \perp C \mid B \end{array}$

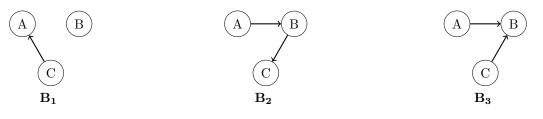
	(iii) P ($(\mathbf{A}, \mathbf{B}) = \sum_{\mathbf{c}} \mathbf{P}(\mathbf{A} \mid \mathbf{B}, \mathbf{c}) \ \mathbf{P}(\mathbf{B} \mid \mathbf{c}) \ \mathbf{P}(\mathbf{c})$		
		$\begin{array}{c} A \perp\!\!\!\perp B \\ A \perp\!\!\!\perp B \mid C \\ A \perp\!\!\!\perp C \\ A \perp\!\!\!\perp C \mid B \end{array}$		$B \perp \!\!\! \perp C$ $B \perp \!\!\! \perp C \mid A$ No independence assumptions needed.
	(iv) P ($(\mathbf{A}, \mathbf{B} \mid \mathbf{C}, \mathbf{D}) = \mathbf{P}(\mathbf{A} \mid \mathbf{C}, \mathbf{D}) \ \mathbf{P}(\mathbf{B} \mid \mathbf{A}, \mathbf{C}, \mathbf{D})$		
		$\begin{array}{c} A \perp\!\!\!\perp B \\ A \perp\!\!\!\perp B \mid C \\ A \perp\!\!\!\perp B \mid D \\ C \perp\!\!\!\perp D \end{array}$		$C \perp\!\!\!\perp D \mid A$ $C \perp\!\!\!\!\perp D \mid B$ No independence assumptions needed.
	Self as	sessment If correct, write "correct" in the box. Oth	erwise	e, write and explain the correct answer.
(c)	(i) Mai	rk all expressions that are equal to $P(A \mid B)$, gi	ven :	no independence assumptions.
		$\sum_{c} P(A \mid B, c)$		$\frac{P(A,C B)}{P(C B)}$
		$\sum_{c} P(A, c \mid B)$		$\frac{P(A C,B) \ P(C A,B)}{P(C B)}$
		$\frac{P(B A) \ P(A C)}{\sum_{c} P(B,c)}$		None of the provided options.
		$\frac{\sum_{c} P(A,B,c)}{\sum_{c} P(B,c)}$		
	(ii) Mai	rk all expressions that are equal to $\mathbf{P}(\mathbf{A}, \mathbf{B}, \mathbf{C})$, a	given	that $\mathbf{A} \perp \!\!\! \perp \mathbf{B}$.
		$P(A \mid C) P(C \mid B) P(B)$		$P(A) P(B \mid A) P(C \mid A, B)$
		$P(A) P(B) P(C \mid A, B)$		$P(A,C) \ P(B \mid A,C)$
		$P(C) P(A \mid C) P(B \mid C)$		None of the provided options.
		$P(A) \ P(C \mid A) \ P(B \mid C)$		
	(iii) Ma	rk all expressions that are equal to $P(A, B \mid C)$,	give	n that $\mathbf{A} \perp \!\!\! \perp \mathbf{B} \mid \mathbf{C}$.
		$P(A \mid C) \ P(B \mid C)$		$\frac{\sum_{c} P(A, B, c)}{P(C)}$
		$\frac{P(A) \ P(B A) \ P(C A,B)}{\sum_{c} P(A,B,c)}$		$\frac{P(C,A B)\ P(B)}{P(C)}$
		$P(A \mid B) \ P(B \mid C)$		None of the provided options.
		$\frac{P(C) \ P(B C) \ P(A C)}{P(C A,B)}$		
	Self as	sessment If correct, write "correct" in the box. Oth	erwise	e, write and explain the correct answer.

Q2. Bayes' Nets: Representation

Assume we are given the following ten Bayes' nets, labeled $\mathbf{G_1}$ to $\mathbf{G_{10}}$:



Assume we are also given the following three Bayes' nets, labeled ${\bf B_1}$ to ${\bf B_3}:$



(continued on next page)

the following Bayes' nets that are guaranteed to be able to represent d_1 . $\begin{array}{c c c c c c c c c c c c c c c c c c c $
(b) Assume we know that a joint distribution $\mathbf{d_2}$ (over $\mathbf{A}, \mathbf{B}, \mathbf{C}$) can be represented by Bayes' net $\mathbf{B_2}$. Mark the following Bayes' nets that are guaranteed to be able to represent $\mathbf{d_2}$. \square $\mathbf{G_1}$ \square $\mathbf{G_2}$ \square $\mathbf{G_3}$ \square $\mathbf{G_4}$ \square $\mathbf{G_5}$ \square $\mathbf{G_6}$ \square $\mathbf{G_7}$ \square $\mathbf{G_8}$ \square $\mathbf{G_9}$ \square $\mathbf{G_{10}}$ \square None of the above.
(b) Assume we know that a joint distribution $\mathbf{d_2}$ (over $\mathbf{A}, \mathbf{B}, \mathbf{C}$) can be represented by Bayes' net $\mathbf{B_2}$. Mark the following Bayes' nets that are guaranteed to be able to represent $\mathbf{d_2}$. \square $\mathbf{G_1}$ \square $\mathbf{G_2}$ \square $\mathbf{G_3}$ \square $\mathbf{G_4}$ \square $\mathbf{G_5}$ \square $\mathbf{G_6}$ \square $\mathbf{G_7}$ \square $\mathbf{G_8}$ \square $\mathbf{G_9}$ \square $\mathbf{G_{10}}$ \square None of the above.
the following Bayes' nets that are guaranteed to be able to represent d_2 . \square G_1 \square G_2 \square G_3 \square G_4 \square G_5 \square G_6 \square G_7 \square G_8 \square G_9 \square G_{10} \square None of the above.
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$\begin{array}{c ccccccccccccccccccccccccccccccccccc$
\square G_6 \square G_7 \square G_8 \square G_9 \square G_{10} \square None of the above.
☐ None of the above.
Son assessment in correct, write correct in the box. Otherwise, write and explain the correct answer.
(c) Assume we know that a joint distribution d ₃ (over A, B, C) cannot be represented by Bayes' net B ₃ . If all of the following Bayes' nets that are guaranteed to be able to represent d ₃ .
\square G_1 \square G_2 \square G_3 \square G_4 \square G_5
\square G_6 \square G_7 \square G_8 \square G_9 \square G_{10}
\square None of the above.
Self assessment If correct, write "correct" in the box. Otherwise, write and explain the correct answer.
(d) Assume we know that a joint distribution d_4 (over A, B, C) can be represented by Bayes' nets B_1 , B_2 B_3 . Mark all of the following Bayes' nets that are guaranteed to be able to represent d_4 .
\square
$\square \ \ G_6 \qquad \square \ \ G_7 \qquad \square \ \ G_8 \qquad \square \ \ G_9 \qquad \square \ \ G_{10}$
□ None of the above.
Self assessment If correct, write "correct" in the box. Otherwise, write and explain the correct answer.
To an abboth in correct, write correct in the box. Otherwise, write and explain the correct answer.