

Lab wk1-3: Recursive generation of Combinatorial Objects

Generating the Power Set of a set recursively

The bitstring representation of sets. Given a set A containing n -elements. Associate each elements with a number from 1 to $n=|A|$, then any subset can be represented by a bitstring of length n . E.g. $A = \{a,b,c,d\}$ then the subset $\{a,c\}$ is represented by 1010 if we have associate a with position 1, b with position 2 etc. This is a bijection between $P(A)$ the set of all subsets of A with the set of all the bitstrings of length $|A|$. Subsets are examples of combinatorial objects. **You will use this representation later but not in this lab!**

The goal of this lab is to practice your recursive programming skills and prepare you for the next assignment.

Given a set A , the set of all its subsets is called its Power set, and is usually denoted $\mathcal{P}(A)$. The **number** of subsets of a finite set $= |P(A)| = 2^{|A|}$.

For example: if $A = \{a, b, c\}$ then $\mathcal{P}(A)$ has 8 elements (written $|\mathcal{P}(A)| = 8$) since $|A| = 3$ and the number of subsets is 2^3 . The subsets are: $\{\}, \{a\}, \{b\}, \{c\}, \{a,b\}, \{a,c\}, \{b,c\}, \{a,b,c\}$

Write a recursive Java method that will generate all the subsets of the letters in a string (which is passed as an explicit parameter) and return the subsets as an ArrayList of strings. You should follow the high-level pseudo-code given below. (Your program will not necessarily generate the subsets in the order shown above!)

```
subsetGen(setString : a string with the characters that make up the set)
    let A and temp be empty ArrayLists
    if len(setString)>0
        temp = subsetGen(set without last character)
        // now loop over temp and create the subsets with and without
        // the last character of the original string
        for (int i = 0; i < temp.size(); i++)
            A.add(temp.get(i)) // adds subsets without last character
            A.add(temp.get(i) + " " + setString(length-1) subsets with
        return A
    else
        A.add("") // array list with only the empty string
        return A
```

Before you implement this make sure you can draw the call tree if it is called on “abc” so you are sure you understand what is going on.

A template for your program is provided on PolyLearn.

Deliverable:

Source code for a single class, **SubsetGen.java** with the method described below. Submit on PolyLearn.

```
public class SubsetGen
contains the method
public ArrayList<String> getSubsets (String word) {}
```