



# Reduce

An introduction to Reduce

Duration: 30 minutes

Q&A: 5 minutes by the end of the lecture

# Reduce: The Accumulator Pattern

**Reduce** is an abstraction for dealing with the *accumulator pattern*:

```
function something(array, ...) {  
  var acc = <starting value>;  
  each(array, function(element) {  
    // update acc using element  
  });  
  return acc;  
}
```

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Reduce

```
function sum(nums) {
```

```
}
```

Let's start by looking at a familiar example of **accumulation**: computing the sum of an array of numbers. We can begin by declaring a function called `sum`.

**Reduce**

```
function sum(nums) {  
  var total = 0;
```

```
  
  return total;  
}
```

We know that we'll need to keep track of a running total...



Reduce

```
function sum(nums) {  
  var total = 0;  
  each      (nums, function(      num) {  
    total = total + num;  
  });  
  return total;  
}
```

...and we can finish our sum function by iterating over the nums array and adding each number into our total.

```
function sum(nums) {  
  var total = 0;  
  each      (nums, function(      num) {  
    total = total + num;  
  });  
  return total;  
}
```

What makes this an example of accumulation? Why do we call it *accumulation*?



We can call this the **accumulator**.

Reduce

```
function sum(nums) {  
  var total = 0;  
  each (nums, function(      num) {  
    total = total + num;  
  });  
  return total;  
}
```

We use the **total** variable to store our accumulation, which starts at 0...



## Reduce

```
function sum(nums) {  
  var total = 0;  
  each      (nums, function(      num) {  
    total = total + num;  
  });  
  return total;  
}
```

...we **iterate** over an array...





## Reduce

```
function sum(nums) {  
  var total = 0;  
  each      (nums, function(  
    total = total + num;  
  ));  
  return total;  
}
```

...**combine** the accumulator with the next value (num in this case)...



## Reduce

```
function sum(nums) {  
  var total = 0;  
  each      (nums, function(      num) {  
    total = total + num;  
  });  
  return total;  
}
```

...update the accumulator...

```
function sum(nums) {  
  var total = 0;  
  each (nums, function(      num) {  
    total = total + num;  
  });  
  return total;  
}
```

...and finally **return** the accumulator when we are done iterating. This is what is meant by the *accumulator pattern*. How about another example?

```
function sum(nums) {  
  var total = 0;  
  each      (nums, function(      num) {  
    total = total + num;  
  });  
  return total;  
}
```

```
function everyNumberEven(nums) {
```

```
}
```

We are going to write a function that determines if every number in an array of numbers is even.



Reduce

```
function sum(nums) {  
  var total = 0;  
  each      (nums, function(      num) {  
    total = total + num;  
  });  
  return total;  
}
```

```
function everyNumberEven(nums) {
```

```
}
```

```
everyNumberEven([2, 4, 6, 8]);  
// => true
```

For instance, if we invoke this function on **[2, 4, 6, 8]**, we should get **true**, because all of those numbers are even.



Reduce

```
function sum(nums) {  
  var total = 0;  
  each      (nums, function(      num) {  
    total = total + num;  
  });  
  return total;  
}
```

```
function everyNumberEven(nums) {  
  
}
```

```
everyNumberEven([2, 4, 6, 8]);  
// => true
```

```
everyNumberEven([2, 4, 5, 8]);  
// => false
```

However, if we invoke this function on **[2, 4, 5, 8]**, we should get **false**, because the number **5** is odd.



Reduce

```
function sum(nums) {  
  var total = 0;  
  each      (nums, function(      num) {  
    total = total + num;  
  });  
  return total;  
}
```

```
function everyNumberEven(nums) {  
  
  each      (nums, function(      num) {  
  
  });  
  
}
```

```
everyNumberEven([2, 4, 6, 8]);  
// => true  
  
everyNumberEven([2, 4, 5, 8]);  
// => false
```

Our strategy will involve iterating over all of the numbers, but we need a way to keep track of whether or not each number we see is even or odd -- how can we do this?



Reduce

```
function sum(nums) {  
  var total = 0;  
  each (nums, function(num) {  
    total = total + num;  
  });  
  return total;  
}
```

```
function everyNumberEven(nums) {  
  var result ;  
  each (nums, function(num) {  
  
  });  
}
```

```
everyNumberEven([2, 4, 6, 8]);  
// => true  
  
everyNumberEven([2, 4, 5, 8]);  
// => false
```

Let's introduce an **accumulator** to keep track of whether or not the numbers so far are all even.



```
function sum(nums) {  
  var total = 0;  
  each (nums, function(num) {  
    total = total + num;  
  });  
  return total;  
}  
  
function everyNumberEven(nums) {  
  var result;  
  each (nums, function(num) {  
    num % 2 === 0;  
  });  
}
```

```
everyNumberEven([2, 4, 6, 8]);  
// => true  
  
everyNumberEven([2, 4, 5, 8]);  
// => false
```

We know that if `num % 2 === 0`, the number is even, and since *every number even* can be rephrased as the *first number is even* **and** the *second number is even* **and** the *third number is even*, etc...

```
function sum(nums) {  
  var total = 0;  
  each (nums, function(num) {  
    total = total + num;  
  });  
  return total;  
}  
  
function everyNumberEven(nums) {  
  var result ;  
  each (nums, function(num) {  
    result = result && num % 2 === 0;  
  });  
}
```

```
everyNumberEven([2, 4, 6, 8]);  
// => true  
  
everyNumberEven([2, 4, 5, 8]);  
// => false
```

We can use the logical **and** (&&) operator to express that `result` should be true if every number is even, and false if even *one* of them is odd.



Reduce

```
function sum(nums) {  
  var total = 0;  
  each (nums, function(num) {  
    total = total + num;  
  });  
  return total;  
}
```

```
function everyNumberEven(nums) {  
  var result ;  
  each (nums, function(num) {  
    result = result && num % 2 === 0;  
  });  
  return result;  
}
```

```
everyNumberEven([2, 4, 6, 8]);  
// => true  
  
everyNumberEven([2, 4, 5, 8]);  
// => false
```

We know that `result` should be what is returned by `everyNumberEven...`



Reduce

```
function sum(nums) {  
  var total = 0;  
  each      (nums, function(      num) {  
    total = total + num;  
  });  
  return total;  
}
```

```
function everyNumberEven(nums) {  
  var result = ???;  
  each      (nums, function(      num) {  
    result = result && num % 2 === 0;  
  });  
  return result;  
}
```

```
everyNumberEven([2, 4, 6, 8]);  
// => true  
  
everyNumberEven([2, 4, 5, 8]);  
// => false
```

But what should the first value of `result` be?



Reduce

```
function sum(nums) {  
  var total = 0;  
  each (nums, function(num) {  
    total = total + num;  
  });  
  return total;  
}
```

```
function everyNumberEven(nums) {  
  var result = true;  
  each (nums, function(num) {  
    result = result && num % 2 === 0;  
  });  
  return result;  
}
```

```
everyNumberEven([2, 4, 6, 8]);  
// => true  
  
everyNumberEven([2, 4, 5, 8]);  
// => false
```

Since a single false will make the entire result false (due to the nature of &&), and undefined will be treated like false, we need to start with true. Now it works!



Reduce

```
function sum(nums) {  
  var total = 0;  
  each (nums, function(num) {  
    total = total + num;  
  });  
  return total;  
}
```

```
function everyNumberEven(nums) {  
  var result = true;  
  each (nums, function(num) {  
    result = result && num % 2 === 0;  
  });  
  return result;  
}
```

```
everyNumberEven([2, 4, 6, 8]);  
// => true  
  
everyNumberEven([2, 4, 5, 8]);  
// => false
```

Let's take a moment to analyze the similarities and differences between these two completely unrelated functions. What is the same in both? What is different?

```
function sum(nums) {  
  var total = 0;  
  each      (nums, function(      num) {  
    total = total + num;  
  });  
  return total;  
}
```

```
function everyNumberEven(nums) {  
  var result = true;  
  each      (nums, function(      num) {  
    result = result && num % 2 === 0;  
  });  
  return result;  
}
```

```
everyNumberEven([2, 4, 6, 8]);  
// => true  
  
everyNumberEven([2, 4, 5, 8]);  
// => false
```

```
function reduce(      ) {  
  
  
}
```

Let's start a function called **reduce** that we'll use to abstract the pattern.

```
function sum(nums) {  
  var total = 0;  
  each (nums, function(num) {  
    total = total + num;  
  });  
  return total;  
}
```

```
function everyNumberEven(nums) {  
  var result = true;  
  each (nums, function(num) {  
    result = result && num % 2 === 0;  
  });  
  return result;  
}
```

```
everyNumberEven([2, 4, 6, 8]);  
// => true  
  
everyNumberEven([2, 4, 5, 8]);  
// => false
```

```
function reduce(          ) {  
  var acc  
  
  return acc;  
}
```

First, the similarities. Both have **accumulator** variables that are returned at the end of the function.



```
function sum(nums) {  
  var total = 0;  
  each (nums, function(num) {  
    total = total + num;  
  });  
  return total;  
}
```

```
function everyNumberEven(nums) {  
  var result = true;  
  each (nums, function(num) {  
    result = result && num % 2 === 0;  
  });  
  return result;  
}
```

```
everyNumberEven([2, 4, 6, 8]);  
// => true
```

```
everyNumberEven([2, 4, 5, 8]);  
// => false
```

```
function reduce(  
  var acc  
  each(  
    , function(element) {  
      });  
  return acc;  
}
```

Both utilize iteration...

```
function sum(nums) {
  var total = 0;
  each      (nums, function(      num) {
    total = total + num;
  });
  return total;
}
```

```
function everyNumberEven(nums) {
  var result = true;
  each      (nums, function(      num) {
    result = result && num % 2 === 0;
  });
  return result;
}
```

```
everyNumberEven([2, 4, 6, 8]);
// => true
```

```
everyNumberEven([2, 4, 5, 8]);
// => false
```

```
function reduce(      ) {
  var acc
  each(      , function(element) {
    acc =
  });
  return acc;
}
```

...and we always update the accumulator while iterating. Now, let's turn the differences into parameters.

```
function sum(nums) {
  var total = 0;
  each      (nums, function(      num) {
    total = total + num;
  });
  return total;
}
```

```
function everyNumberEven(nums) {
  var result = true;
  each      (nums, function(      num) {
    result = result && num % 2 === 0;
  });
  return result;
}
```

```
everyNumberEven([2, 4, 6, 8]);
// => true
```

```
everyNumberEven([2, 4, 5, 8]);
// => false
```

```
function reduce(array      ) {
  var acc
  each(array, function(element) {
    acc =
  });
  return acc;
}
```

We will definitely need an array to iterate over...

```
function sum(nums) {
  var total = 0;
  each      (nums, function(      num) {
    total = total + num;
  });
  return total;
}
```

```
function everyNumberEven(nums) {
  var result = true;
  each      (nums, function(      num) {
    result = result && num % 2 === 0;
  });
  return result;
}
```

```
everyNumberEven([2, 4, 6, 8]);
// => true
```

```
everyNumberEven([2, 4, 5, 8]);
// => false
```

```
function reduce(array      , start) {
  var acc = start;
  each(array, function(element) {
    acc =
  });
  return acc;
}
```

...and we also need to know what value to start the accumulator at.

```
function sum(nums) {
  var total = 0;
  each      (nums, function(      num) {
    total = total + num;
  });
  return total;
}
```

```
function everyNumberEven(nums) {
  var result = true;
  each      (nums, function(      num) {
    result = result && num % 2 === 0;
  });
  return result;
}
```

```
everyNumberEven([2, 4, 6, 8]);
// => true
```

```
everyNumberEven([2, 4, 5, 8]);
// => false
```

```
function reduce(array      , start) {
  var acc = start;
  each(array, function(element) {
    acc = ???
  });
  return acc;
}
```

The last thing that we need is a way to compute the **next** accumulator, given the **current** accumulator and an **element** in the array. What can we use to express this?

```
function sum(nums) {  
  var total = 0;  
  each      (nums, function(      num) {  
    total = total + num;  
  });  
  return total;  
}
```

```
function everyNumberEven(nums) {  
  var result = true;  
  each      (nums, function(      num) {  
    result = result && num % 2 === 0;  
  });  
  return result;  
}
```

```
everyNumberEven([2, 4, 6, 8]);  
// => true
```

```
everyNumberEven([2, 4, 5, 8]);  
// => false
```

```
function reduce(array, f, start) {  
  var acc = start;  
  each(array, function(element) {  
    acc = f(acc, element);  
  });  
  return acc;  
}
```

How about a function? Our function will be given the **current accumulator** and an **element** in the array as arguments, and should return a **new accumulator**. Let's start refactoring!

```
function sum(nums) {  
  var total = 0;  
  reduce(nums, function(  
    total = total + num;  
  ));  
  return total;  
}
```

```
function everyNumberEven(nums) {  
  var result = true;  
  reduce(nums, function(  
    result = result && num % 2 === 0;  
  ));  
  return result;  
}
```

```
everyNumberEven([2, 4, 6, 8]);  
// => true
```

```
everyNumberEven([2, 4, 5, 8]);  
// => false
```

```
function reduce(array, f, start) {  
  var acc = start;  
  each(array, function(element) {  
    acc = f(acc, element);  
  });  
  return acc;  
}
```

First, since reduce does iteration for us, let's replace each with reduce.

```
function sum(nums) {
  var total = 0;
  reduce(nums, function(      num) {
    return total + num;
  });
  return total;
}
```

```
function everyNumberEven(nums) {
  var result = true;
  reduce(nums, function(      num) {
    return result && num % 2 === 0;
  });
  return result;
}
```

```
everyNumberEven([2, 4, 6, 8]);
// => true
```

```
everyNumberEven([2, 4, 5, 8]);
// => false
```

```
function reduce(array, f, start) {
  var acc = start;
  each(array, function(element) {
    acc = f(acc, element);
  });
  return acc;
}
```

The function provided to reduce should **return** the next accumulator instead of doing assignment directly, so let's make that change.



```
function sum(nums) {  
  var total = 0;  
  reduce(nums, function(      num) {  
    return total + num;  
  });  
  return total;  
}
```

```
function everyNumberEven(nums) {  
  var result = true;  
  reduce(nums, function(      num) {  
    return result && num % 2 === 0;  
  });  
  return result;  
}
```

```
everyNumberEven([2, 4, 6, 8]);  
// => true
```

```
everyNumberEven([2, 4, 5, 8]);  
// => false
```

```
function reduce(array, f, start) {  
  var acc = start;  
  each(array, function(element) {  
    acc = f(acc, element);  
  });  
  return acc;  
}
```

reduce accomplishes the accumulation step by providing the accumulator as the first parameter to its function argument...

```
function sum(nums) {
    0;
    reduce(nums, function(total, num) {
        return total + num;
    });
    return
}
```

```
function everyNumberEven(nums) {
    true;
    reduce(nums, function(result, num) {
        return result && num % 2 === 0;
    });
    return
}
```

```
everyNumberEven([2, 4, 6, 8]);
// => true
```

```
everyNumberEven([2, 4, 5, 8]);
// => false
```

```
function reduce(array, f, start) {
    var acc = start;
    each(array, function(element) {
        acc = f(acc, element);
    });
    return acc;
}
```

...so we'll declare it as a parameter to the function and remove the variable that we used before. Only two steps remain:

```
function sum(nums) {  
    0;  
    reduce(nums, function(total, num) {  
        return total + num;  
    });  
    return  
}
```

```
function everyNumberEven(nums) {  
    true;  
    reduce(nums, function(result, num) {  
        return result && num % 2 === 0;  
    });  
    return  
}
```

```
everyNumberEven([2, 4, 6, 8]);  
// => true
```

```
everyNumberEven([2, 4, 5, 8]);  
// => false
```

```
function reduce(array, f, start) {  
    var acc = start;  
    each(array, function(element) {  
        acc = f(acc, element);  
    });  
    return acc;  
}
```

First, we need to take care of the **starting value** of the accumulator. How do we tell reduce what it should start the accumulator with?

```
function sum(nums) {
    reduce(nums, function(total, num) {
        return total + num;
    }, 0);
    return
}

function everyNumberEven(nums) {
    reduce(nums, function(result, num) {
        return result && num % 2 === 0;
    }, true);
    return
}
```

```
everyNumberEven([2, 4, 6, 8]);
// => true
```

```
everyNumberEven([2, 4, 5, 8]);
// => false
```

```
function reduce(array, f, start) {
    var acc = start;
    each(array, function(element) {
        acc = f(acc, element);
    });
    return acc;
}
```

We provide it as the third argument to reduce! What is the last change that we need to make?

```
function sum(nums) {  
  
  return reduce(nums, function(total, num) {  
    return total + num;  
  }, 0);  
  
}  
  
function everyNumberEven(nums) {  
  
  return reduce(nums, function(result, num) {  
    return result && num % 2 === 0;  
  }, true);  
  
}
```

```
everyNumberEven([2, 4, 6, 8]);  
// => true
```

```
everyNumberEven([2, 4, 5, 8]);  
// => false
```

```
function reduce(array, f, start) {  
  var acc = start;  
  each(array, function(element) {  
    acc = f(acc, element);  
  });  
  return acc;  
}
```

Because reduce results in its accumulator, the result of invoking reduce is what we want to return.



## Reduce

```
function sum(nums) {  
  return reduce(nums, function(total, num) {  
    return total + num;  
  }, 0);  
}  
  
function everyNumberEven(nums) {  
  return reduce(nums, function(result, num) {  
    return result && num % 2 === 0;  
  }, true);  
}
```

```
everyNumberEven([2, 4, 6, 8]);  
// => true
```

```
everyNumberEven([2, 4, 5, 8]);  
// => false
```

```
function reduce(array, f, start) {  
  var acc = start;  
  each(array, function(element) {  
    acc = f(acc, element);  
  });  
  return acc;  
}
```

And that's it!



# That's it

For Reduce